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Rashba Spin-Orbit Anisotropy and the Electric Field Control of Magnetism

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The control of the magnetism of ultra-thin ferromagnetic layers using an electric field, rather than a current, has many potential technologically important applications. It is usually insisted that such control occurs via an electric field induced surface charge doping that modifies the magnetic anisotropy. However, it remains the case that a number of key experiments cannot be understood within such a scenario. Much studied is the spin-splitting of the conduction electrons of non-magnetic metals or semi-conductors due to the Rashba spin-orbit coupling. This reflects a large surface electric field. For a magnet, this same splitting is modified by the exchange field resulting in a large magnetic anisotropy energy via the Dzyaloshinskii-Moriya mechanism. This different, yet traditional, path to an electrically induced anisotropy energy can explain the electric field, thickness, and material dependence reported in many experiments.

The possibility of controlling the magnetic anisotropy of thin ferromagnetic films using a static electric field E is of great interest since it can potentially lead to magnetic random access memory (MRAM) devices which require less energy than spin-torque-transfer random access memory STT-MRAM¹⁻⁷. Thin magnetic films with a perpendicular magnetic anisotropy (PMA) are important for applications^{8,9}. That an interfacial *internal* electric field might be used to engineer such a PMA is also of great interest. Experiment^{10,11} has indeed shown that such a PMA might, in turn, be modified by an *externally applied* electric field, however the data is usually interpreted in terms of changes to the electronic contribution to magnetic anisotropy due to the surface doping induced by the applied electric field^{3,11,12}.

The theory of the field-induced changes of the magnetic anisotropy reflecting surface doping is invariably developed in terms of band theory^{13–17}. The results for both the bulk and thin films can be adequately understood in terms of second order perturbation theory¹⁸ in which the relevant matrix elements of the spin-orbit interaction are between full and empty states. Large contributions come from regions where different *d*-bands (almost) cross. That such crossings should be close to the Fermi surface leads to a strong doping dependence in such theories. Nakamura *et al.*¹⁹ pointed out that the strong negative applied field dependence of the PMA for an isolated monolayer (ML) of Fe(001) arises directly from band splitting rather than from doping. In this case, an *E* perpendicular to the film breaks reflection symmetry causing a large spin-orbit splitting of *d*-levels near the Fermi surface. As will be explain below, despite these important theoretical developments, a clear explanation of a number of key experiments is still lacking.

Here we develop a simple analytic theory for the existence and electrical control of the PMA based upon the Rashba spin-orbit interaction^{20–22} and the single band Stoner model of magnetism. We exhibit the somewhat delicate, but very interesting, competition between the Rashba spin-orbit fields and the exchange interaction, reflecting electron correlations. This theory can potentially lead to a very large magnetic anisotropy arising from the internal electric fields E_{int} which exist at, e.g., ferromagnetic/metal and ferromagnetic/oxide insulator interfaces but modified by the addition of an applied electric field E_{ext} . There is a Rashba splitting of the band structure leading to a quadratic, $(E_{int} + E_{ext})^2$, contribution to the magnetic anisotropy, contrasting with a linear in E_{ext} doping effect.

Results

Model. This comprises a band Stoner model with the Rashba interaction added²³:

$$H = \frac{p^2}{2m} - J_0 \mathbf{S} \cdot \boldsymbol{\sigma} + \frac{\alpha_R}{\hbar} \left(\sigma_x p_y - \sigma_y p_x \right). \tag{1}$$



Figure 1 (a) The electric field $E = E\hat{z}$ is perpendicular to the ferromagnet surface while the order parameter direction $\hat{\mathbf{m}}$, is defined by the angle θ relative to \hat{z} . Whatever the direction of k, the Rashba magnetic field B_R of direction $k \times E$ lies in the $\hat{\mathbf{x}} - \hat{\mathbf{y}}$ plane. (b) The Rashba split bands of a nonmagnetic metal. The two Fermi sheets emerge from a "Dirac point" near the bottom of the illustration. For the magnetic case the two Fermi sheets are disconnected. (c) For a perpendicular $\hat{\mathbf{m}}$ the electron spins make a constant angle δ to the vertical such that the projection is as in (b). The additional exchange splitting increases as E^2 . (d) Same but for $\hat{\mathbf{m}}$ parallel to the plane. With $\hat{\mathbf{m}}$ along the *y*-direction the majority and minority Fermi seas shift along the *x*-axis in opposite directions. The tilt of the spin relative to $\hat{\mathbf{m}}$ is no longer a constant being zero along the *x*-axis and a maximum along the *y*-axis.

where p is the electron momentum operator, S the order parameter, σ the Pauli matrices and $\alpha_R = e\eta_{so}E$ the Rashba parameter proportional to η_{so} , which characterises the spin-orbit coupling. The electric field $E = E\hat{z}$ is taken to be perpendicular to the plane of the system, and $\hat{\mathbf{m}} = S/S$ is perpendicular to $\hat{\mathbf{x}}$ and makes an angle θ to the \hat{z} -direction, as in Fig. 1(a).

Illustrative non-magnetic example. Consider the Rashba effect in non-magnetic two dimensional electron gases or surface states on noble metals, e.g., a surface state of Au. As shown in the **methods**, the single particle energy

$$\epsilon_{k\sigma} = \frac{\hbar^2}{2m} (k - \sigma k_0)^2 - E_R, \qquad (2)$$

as the spin quantum number $\sigma = \pm 1$. The momentum shift $k_0 = ma_R/\hbar^2$, and

$$E_R = \frac{m\alpha_R^2}{2\hbar^2} = \frac{1}{2} \left(\frac{e\eta_{so}}{\hbar}\right)^2 mE^2,$$
(3)

identified in the inset of Fig. 1(b), reflects the single particle energy gain relative to zero electric field, i.e., E = 0 and hence $\alpha_R = 0$. For the three dimensional problem $\epsilon_{k\sigma} = \frac{\hbar^2}{2m} \left[(k - \sigma k_0)^2 + k_z^2 \right] - E_R$ and there is no equivalent momentum shift in k_z . For the surface state of Au, $E_R \approx 3.5 \text{ meV}^{24,25}$ exemplifying the energy scale.

The study of such surface states, and differences in chemical potentials, also helps set the scale for *E*. Between a metal and the vacuum, or dielectric, the $E \sim 10$ V/nm near the Cu (100) surface²⁶,

There are many experiments^{24,25,29-31} which put in evidence the Rashba splitting in two dimensional electron gases, surface states of noble metals, bulk layered systems, and e.g., of a surface state of ferromagnetic Yb.

Magnetic case - origin of the magnetic anisotropy energy. In the methods it is shown the θ dependent single particle energy, i.e., the equivalent of Eq. (2) for the magnetic case is:

$$\epsilon_{k\sigma} = \frac{\hbar^2}{2m} \left[(k_x - \sigma k_0 \sin \theta)^2 + k_y^2 \right] - E_R \sin^2 \theta - \sigma \left[(J_0 S)^2 + \alpha_R^2 (k_x^2 \cos^2 \theta + k_y^2) \right]^{1/2}.$$
(4)

The direction of the now θ dependent momentum shift changes sign as the spin index $\sigma = \pm 1$. These shifts also change sign with $\hat{\mathbf{m}} \rightarrow -\hat{\mathbf{m}}$ for a given σ . This "magnetic Rashba splitting" with $\hat{\mathbf{m}} \rightarrow -\hat{\mathbf{m}}$ is observed for the surface state of Yb³¹.

Also in the **methods** the Dzyaloshinskii-Moriya (DM) and pseudo-dipolar (PD) contributions to the magnetic anisotropy are highlighted by contrasting the perpendicular and parallel orientations of order parameter $\hat{\mathbf{m}}$ to the plane.

Assuming $(J_0S)^2 > (\alpha_R k_x)^2$ and retaining the θ -dependent terms up to the order of E^2 in (4), we obtained our principal result:

$$E_{\rm an} = E_R \left[1 - \frac{2T}{J_0 S} \right] \cos^2 \theta, \tag{5}$$

for the magnetic anisotropy energy, with

$$T = \frac{\hbar^2}{2m} \left(\left\langle k_x^2 \right\rangle_{\uparrow} - \left\langle k_x^2 \right\rangle_{\downarrow} \right), \tag{6}$$

where $\langle \rangle$ denotes an average over the Fermi sea (see **methods**). The Rashba spin-orbit interaction produces a uni-axial anisotropy energy which, as in the Dzyaloshinskii-Moriya theory³²⁻³⁵, comprises a direct second order in *E* easy plane pseudo-dipolar interaction and an indirect contribution proportional to E^2/J_0S reflecting the competition between the first order in *E*, Rashba-Dzyaloshinskii-Moriya, and exchange fields.

Competition between the Dzyaloshinskii-Moriya and pseudodipolar contributions. Clearly Eq. (5) implies an E^2 dependent PMA results if $T > J_0 S/2$, i.e., when the DM is larger than the PD term. Taken literally, the Stoner model Eq. (1), with its quadratic dispersion, predicts the ratio of the DM and PD contributions to the PMA. The result, (see methods), depends upon the spatial dimension. In two dimensions the PD and DM terms cancel although higher order terms ($O(\alpha_R^4)$) lead to a PMA while in three dimensions the DM term is $-(4/5) E_R \cos^2 \theta$ and an in-plane magnetisation is favoured. Lastly, a two dimensional system with a highly anisotropic conductivity might be modelled as a series of parallel one dimensional chains. For chains the DM contribution $-(4/3) E_R \cos^2 \theta$ which dominates the PD energy $E_R \cos^2 \theta$, appropriate when $\hat{\mathbf{m}}$ is in-plane and perpendicular to the chains. Corresponding to the hardest axis, when $\hat{\mathbf{m}}$ in-plane but rather parallel to the chains, there is neither a DM or PD contribution to the magnetic anisotropy energy. There is thereby a predicted electric field dependence of the in-plane anisotropy as seen in early experiments³, given the large compressive strain that arises in these experiments.

However, for the real problem of 3*d* magnets, a quadratic dispersion is not at all realistic and the crystal potential $V(\mathbf{r})$ must be accounted for, see **methods**. For 3*d* elements the wavefunction ψ is well localised within the atomic sphere and the averages, e.g., $\hbar^2 \langle k_x^2 \rangle$, and hence *T*, are very much increased as compared to the above naïve estimates. In reality, the DM contribution will invariably lead to a PMA.

Discussion

The resulting anisotropy energy can be very large. The work already cited^{24–27} on conducting but non-magnetic materials helps set the scales. The value of the scaling prefactor E_R in Eq. (5) for the surface state of Au is ~ 3.5 meV or about 35 T in magnetic field units and very much larger than the typical ~ 1 T demagnetising field. If a Au film is polarised by contact with an ultra-thin ferromagnet, the second factor, $2T/J_0S$, in Eq. (5) for the field inside a Au surface layer can be quite large ~ 5 leading to a PMA and indeed ultra-thin Fe on Au does have such a PMA^{36,37}. Ultra-thin ferromagnetic films in contact with, e.g., Ru, Pd, Pt, and Ta, etc., also are found to have a PMA^{6,12,38,39}.

Schematically shown in Fig. 2(a) is the potential seen by electrons in a free standing ultrathin ferromagnetic film. At the surface, the potential reflects an electron's image charge but reaches the vacuum level within a few atomic spacing. As already discussed, this results in a finite large electric field $E \sim 10$ V/nm at each surface but in opposite senses. Assuming an appreciable spin-orbit coupling in the interface region, this results, in turn, in a Rashba field B_R which also changes sign between the two surfaces for a given momentum. Thus, for a perfectly symmetric film, the ferromagnetically polarised electrons see no average field B_R . This symmetry can be broken by the application of an external electric field as shown in Fig. 2(b). The electric field is increased at one surface and decreased at the other doubling the net effect. In contrast, for this same symmetric situation, the surface charges are opposite and doping effects must cancel. Experimentally applied fields of 1 V/nm are relatively easy to achieve implying a ~ 10% change in the surface anisotropy. Experiments⁴⁰ with a 1.5 nm Fe₈₀B₂₀ sandwiched between two MgO layers are perhaps closest to this situation although the thickness 1.5 nm and 2.5 nm of these layers are not equal. Roughly consistent with our estimate [see Fig. 2(c), case(i)], there is⁴⁰ an ~ 15% symmetric contribution to the magnetic anisotropy for an applied voltage of 2 V.

Clearly the intrinsic Rashba field B_R is modified when the materials adjacent to a 3d ferromagnet (F) are different. In a number of experiments an insulator I, often MgO, lies to one side and a normal metal (N), e.g., Au, Pt, Pd, Ta, or Ru, "cap" completes a tri-layer system. The potential, Figs. 2(d) and (e), will increase in passing from Fe to MgO but in passing from the F to N-layer the potential will either increase, Fig. 2(d), or decrease, Fig. 2(e). As discussed above, the relevant potential would be expected to increase, Fig. 2(d), in passing from a 3d element, e.g., Co, Fe, Ni, or Cu, to a 4d transition metal such as Ru, Pd, Ag but decrease, Fig. 2(e), for the 5d elements, e.g., Au, Pt, Ta. The latter case is particularly favourable since the intrinsic Rashba fields have the same sense and add. In addition, the 5*d* elements have a larger spin-orbit coupling, resulting in a larger α_R and hence are more likely to produce a sizeable PMA. If the electric field decreases at the FI interface, the average Rashba field increases in the first case [Fig. 2(f)] when the effects of the surfaces tend to cancel and, as illustrated in Fig. 2(g), decreases in the second case when the inverse is true [see Fig. 2c, case (ii) and (iii)]. Experiment¹² indeed shows an opposite field dependence for such systems with Pd(4d) and Pt(5d) N-layers. That the sign of the electric field contribution to the PMA reflects the N-layer whereas the field is applied to the opposite surface between F and I supports the current Rashba model. This is in stark contrast with the popular surface doping model^{3,12}, for which the effects of surface doping are limited by the



Figure 2 | (a) There is an electric field *E* in the surface region of a ferromagnet, however for a given wave vector \mathbf{k} , the Rashba field \mathbf{B}_{R} proportional to $\mathbf{k} \times \mathbf{E}$, has an opposite sign at the two surfaces and the average field is zero. (b) With a finite external field this symmetry is broken and there is a net Rashba field acting upon the electrons. (c) The gate voltage dependence of the anisotropy energy. The internal electric field causes the shift of the parabola in the lateral axis as indicated by V_0 for case i). For cases ii) and iii) the internal field shift is far beyond the external field range and nearly linear *E*-dependence arises. (d) The symmetry is also broken for a insulator-ferromagnet-metal sandwich. Also despite the electric field being smaller at the right surface, for a suitable metal, the spin-orbit coupling is larger and hence the metal interface can still dominate the net Rashba field. (e) Here the work function is larger for the metal than for the ferromagnet and the field for that surface is reversed. Now the Rashba fields at the two surfaces add. (f), (g) Applying positive gate voltages decreases the Rashba field at the insulating surface which, for this case, causes a net increase/decrease in the average Rashba field.

(possibly magnetically modified) Fermi-Thomas screening length. In reality¹², the screening length is estimated to be much less than 1 nm, and much too short for there to be an appreciable doping effect of the Pt or Pd layers that are typically distant by a few nanometers.

Simulating a large applied electric field *E*, the required asymmetry might be controlled in NFN tri-layers by varying in a systematic manner, at the mono-layer level, the thickness of one of the normal metal layers and by using metals with different spin-orbit couplings. In reality the effect of the substrate transmitted to, and through, the bottom normal metal will imply an asymmetry even for largish Nlayer thickness. Indeed the PMA surface term for Au/Fe(110)/ Au(111) structures does show an non-monotonic dependence on the top Au layer thickness³⁶. Experiments³⁷ for Fe layers on vicinal Ag(001) and Au(001) surfaces and which undergo a symmetry breaking (5 × 20) surface reconstruction manifest an in-plane surface term reflecting this broken symmetry and which is larger for Au, with its stronger spin-orbit coupling, than for Ag.

It is predicted that the surface coercivity field H_c is proportional to $(E_{\rm int} + E_{\rm ext})^2$ where $E_{\rm int}$ is the internal electric field corresponding to the zero-bias Rashba contribution to the anisotropy. Such a non-linear field dependence is observed, e.g., for the in-plane contribution for a (Ge,Mn)As/ZrO₂ surface³. In other experiments¹⁰ with CoFeB/MgO/CoFeB structures there is qualitative difference between the *E* dependence of the anisotropy field H_c of the, "top" and "bottom", CoFeB layers of this three layer structure, even when they have similar thicknesses. The bottom layer has a larger H_c and is roughly linear while H_c becomes highly non-linear as $H_c \rightarrow 0$ as would be expected as $E_{\rm ext} \rightarrow -E_{\rm int}$.

The most direct experimental test of the model is the observation of the band splittings for a model Rashba system with a variable contact with an itinerant ferromagnet. This can result in giant magnetic anisotropy (GMA) energies. For example an $E_R \sim 100 \text{ meV}$ (or \sim 1000 T) is reported in angle-resolved photoemission spectroscopy (ARPES) measurements⁴¹ on bulk BiTeI. For a thin film of this, or similar material, in contact with an itinerant ferromagnet such as Fe, a suitable exchange splitting J_0S , tuned to the order of E_R , might be induced and a GMA will result. ARPES performed as a function of the direction of the magnetisation m might determine both E_R and the momentum dependence of the exchange splitting leading to estimates of both the PM and DM contributions and which might be directly compared with magnetisation and magnetic resonance measurements. The electrical control of such a GMA has evident important application for non-volatile memory applications. There are clearly many more complicated embodiments of such a device.

In conclusion, it is suggested that the Rashba magnetic field due to the internal electric field in the surface region of an ultra-thin ferromagnet can make an important contribution to the perpendicular magnetic anisotropy. Such surface fields might be modified by application of an applied electric field. Since the internal fields at two surfaces tend to cancel, an asymmetry between the surfaces is important. Such an asymmetry is caused by different metal and insulator caping layers. These ideas are consistent with a large number of experiments.

Methods

The non-magnetic case. This corresponds to Eq. (1) with $J_0 = 0$. It is solved by taking the axis of quantisation $\hat{\mathbf{z}} \times \mathbf{k}$ to be perpendicular to the in-plane \mathbf{k} as in Fig. 1(b). The eigenstates are $e^{i\mathbf{k}\cdot\mathbf{r}}|s\rangle$ and $H = (\hbar^2/2m)k^2 - g\mu_B B_\mathbf{R} \cdot \sigma/2$, where the Rashba magnetic field in energy units is defined as $g\mu_B B_\mathbf{R} = 2\alpha_R (-k_y \hat{\mathbf{x}} + k_x \hat{\mathbf{y}})$, with μ_B the Bohr magneton and g the g-factor, leaving the spin state $|s\rangle$ to be determined. There are two concentric Fermi surfaces. The energy splitting $2\alpha_R k \equiv \Delta(k/k_F)$, where Δ is the value for $k_F \equiv (k_{F\uparrow} + k_{F\downarrow})/2$, with $k_{F\uparrow,\downarrow}$ the Fermi wave number for the spin up/down ($\sigma = \pm 1$) band. For the surface state of Au, $\Delta \approx 110$ meV while $E_F \approx 420$ meV giving the $E_R \approx 3.5$ meV cited in the text. The magnetic case. The full Eq. (1) is solved by defining axes such that $\hat{\mathbf{m}} = S/S$ lies in the y-z-plane and $S = S(\cos \theta \hat{\mathbf{c}} + \sin \theta \hat{\mathbf{y}})$. The total field, which defines the axis of quantisation, $g\mu_B B_T = 2[(J_0S + \alpha_R k_x \sin \theta)\hat{\mathbf{m}} - \alpha_R k_y \hat{\mathbf{x}} + \alpha_R k_x \cos \theta (\hat{\mathbf{m}} \times \hat{\mathbf{x}})]$. It is assumed that, for a 3d ferromagnet $J_0S \sim 0.5$ -1.0 eV and $g\mu_B B_R < J_0S$, i.e., the Rashba is smaller than the exchange splitting. To second

order in $g\mu_B B_R$, $g\mu_B B_T \approx 2(JS + \alpha_R k_x \sin \theta)\hat{\mathbf{m}}'$ where $JS = [(J_0S)^2 + \alpha_R^2(k_x^2 \cos^2 \theta + k_y^2)]^{1/2}$ and where $\hat{\mathbf{m}}'$ differs in direction from $\hat{\mathbf{m}}$ by a small angle δ where tan $\delta \approx \alpha_R(k_x^2 \cos^2 \theta + k_y^2)^{1/2}/J_0S$. The linear in k_x term, $\alpha_R k_x \sin \theta$, causes a shift in Fermi sea to give the the single particle energy Eq. (4).

With $\hat{\mathbf{m}}$ perpendicular to the plane, i.e., $\hat{\mathbf{m}} = \hat{\mathbf{z}} \ (\theta = 0)$, the exchange and Rashba fields are orthogonal and hence the net energy for a single electron Eq. (4) is

$$\epsilon_{k\sigma} = \frac{\hbar^2}{2m} k^2 - \sigma \left[(J_0 S)^2 + (\alpha_R k)^2 \right]^{1/2}.$$
 (7)

The axis of quantisation is tilted by $\delta(k) = \tan^{-1} \frac{\alpha_R k}{I_0 S}$ away from the *z*-axis as shown in Fig. 1(c). The $\sigma = \pm 1$ electrons gain/lose an energy that is even in *E*. This arises from the competition of the Rashba field, perpendicular to $\hat{\mathbf{m}}$, with the exchange field. Such a competition generates a second order in *E* contribution to the magnetic anisotropy and is identified with the Dzyaloshinskii-Moriya (DM) mechanism^{32–35}.

Now take $\hat{\mathbf{m}}$ parallel to the *y*-axis, i.e., $\hat{\mathbf{m}} = \hat{\mathbf{y}} \ (\theta = \pi/2)$. The *y*-component of \mathbf{B}_R is parallel to the exchange field and is combined with the kinetic energy. The Fermi sea is shifted along the *x*-axis and lowered by E_R as shown in Fig. 1(d). This energy gain corresponds to a pseudo-dipolar (PD) contribution to anisotropy energy³⁵ which favours an in-plane magnetisation. On the other hand, the *x*-component of \mathbf{B}_R , which is perpendicular to $J_0 \hat{\mathbf{Sm}}$, gives rise to a correction to the effective exchange field. The direction of the moment tilts away from the *y*-axis in the direction perpendicular to

the wave vector by $\delta(k_y) = \tan^{-1} \frac{\alpha_R k_y}{J_0 S}$ as shown in Fig. 1(d). The single particle energy, Eq. (4), is now,

$$\epsilon_{k\sigma} = \frac{\hbar^2}{2m} \left[(k_x - \sigma k_0)^2 + k_y^2 \right] - E_R - \sigma \left[(J_0 S)^2 + (\alpha_R k_y)^2 \right]^{1/2},$$
(8)

where the shift k_0 is the same as in Eq. (2) but only along the *x*-axis.

The effective exchange field in Eq. (8) is smaller than that in Eq. (7) due to the absence of a k_x^2 term. This indicates that the overall DM contribution favours a perpendicular $\hat{\mathbf{m}}$ while the PD term favours an in-plane $\hat{\mathbf{m}}$. This exchange field changes sign with $\sigma = \pm 1$.

Evaluation of the Dzyaloshinskii-Moriya and pseudo-dipolar contributions. Needed for *T* in Eq. (5) are the Fermi sea averages $\langle k_x^2 \rangle_{\uparrow,\downarrow} = k_{F\uparrow,\downarrow}^2/3$, $k_{F\uparrow,\downarrow}^2/4$, and $k_{F\uparrow,\downarrow}^2/5$, determined analytically, for quadratic dispersion, in one, two, and three dimensions respectively. For an isotropic system these averages are related to J_0S via

$$\frac{\hbar^2}{2m} \left(k_{F\uparrow}^2 - k_{F\downarrow}^2 \right) \simeq 2J_0 S. \tag{9}$$

which determines the ratio $2T/J_0S$ in the principal result, Eq. (5), given in the text.

Role of the crystal potential. The effects of the crystal potential $V(\vec{r})$ are exhibited by considering a wave function $\psi = \sum_{K} a_{K} e^{i(K+K)\cdot r}$ which is a linear combination of plane waves, where *K* are the reciprocal lattice vectors and the a_{K} are determined by *V* (*r*). While not convenient for 3*d* electrons, at least in principle, such an expansion in the true, rather than crystal, momentum states is always possible. The PD contribution, $E_{R} \cos^{2} \theta$ is independent of the momentum k + K. However $\hbar^{2} \langle k_{x}^{2} \rangle = \sum_{K} |a_{K}|^{2} \langle (p_{x} + \hbar K_{x})^{2} \rangle_{BZ}$, where $\langle \rangle_{BZ}$ is the average over the first Brillouin zone. For 3*d* electrons, the average $\hbar^{2} \langle k_{x}^{2} \rangle$, and hence *T*, are dominated by the a_{K} for largish *K*. It follows *T* is significantly increased with the consequences discussed in the text.

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Author contributions

S.E.B. identified the problem. S.E.B., J.I. and S.M. performed the analytical calculations, analysed the data, and wrote the manuscript. S.E.B. and J.I. devised and prepared the figures. All authors reviewed the manuscript.

Additional information

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