# COVIDOA: a novel evolutionary optimization algorithm based on coronavirus disease replication lifecycle 

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#### Abstract

This paper presents a novel bio-inspired optimization algorithm called Coronavirus Optimization Algorithm (COVIDOA). COVIDOA is an evolutionary search strategy that mimics the mechanism of coronavirus when hijacking human cells. COVIDOA is inspired by the frameshifting technique used by the coronavirus for replication. The proposed algorithm is tested using 20 standard benchmark optimization functions with different parameter values. Besides, we utilized five IEEE Congress of Evolutionary Computation (CEC) benchmark test functions (CECC06, 2019 Competition) and five CEC 2011 real-world problems to prove the proposed algorithm's efficiency. The proposed algorithm is compared to eight of the most popular and recent metaheuristic algorithms from the state-of-the-art in terms of best cost, average cost (AVG), corresponding standard deviation (STD), and convergence speed. The results demonstrate that COVIDOA is superior to most existing metaheuristics.


Keywords Coronavirus • Optimization • Frameshifting • Best cost • Convergence • Evolutionary algorithm

## 1 Introduction

Nature is full of principles and mechanisms that inspire scientists to develop complex computational problems [15]. Researchers developed various renature-inspired algorithms such as Genetic Algorithm (GA) [26] and Differential Evolution (DE) [63] over the years. These algorithms are based on the theory of natural evolution. Another group of Algorithms mimics the behavior of birds, animals, insects, plants, or fish, such as Particle Swarm Optimization (PSO) [44], Artificial Bee Colony (ABC)

[^0][41], Chicken Swarm Optimization (CSO) [48], Flower Pollination Algorithm (FPA) [75], Grey Wolf Optimization (GWO) [51], Whale Optimization Algorithm (WOA) [50], Cuckoo Search (CS) [76], Bird Mating Optimizer [6], Social Spider Optimization (SSO) [38], Krill Herd [25], and Seagull Optimization Algorithm (SOA) [19]. Other algorithms based on physical phenomena such as Water Cycle Algorithm (WCA) [22], Central Force Optimization (CFO) [24], Gravitational Search Algorithm (GSA) [60], Water Wave Optimization (WWO) [78], and Gradientbased Optimizer (GBO) (Ahmadianfar et al. 2020). Many other optimization algorithms are proposed by [5, 7, $10,11,13,17,28,42,47,53,55-57,61,62,64,66,69]$.

Generally speaking, optimization algorithms are classified into three categories: swarm-based, physics-based, and evolutionary algorithms. Swarm-based algorithms such as $\mathrm{ABC}, \mathrm{PSO}, \mathrm{CSO}$, and CS, mimic how a group of agents would behave with each other and their environment [1]. Based on Newton's gravitational law, physics-based algorithms are based on a mathematical idea or physical processes, such as CFO and GSA [3]. On the other hand, evolutionary algorithms are search methods inspired by biological evolution mechanisms, such as reproduction and mutation [77]. The most popular evolutionary algorithm is

Fig. 1 Most popular optimization algorithms


GA, inspired by Darwin's theory of biological evolution. As mentioned in [23], evolutionary algorithms have some advantages over other types of optimization algorithms, such as:
(2) In evolutionary algorithms, the individuals with the highest fitness are selected for reproduction, leading to new individuals' production closer to the optimum solution.
(3) Broad applicability: researchers can apply evolutionary algorithms to any problem formulated in the form of an optimization function. A list of the most popular nature-inspired algorithms is shown in Fig. 1.

Since 2020, the world has suffered from the pandemic of coronavirus disease 2019 (COVID-19). Researchers worldwide are doing their best to understand this novel virus's mechanism and find an effective therapy for this disease [40, 73]. More than one researcher discussed the mechanism of the novel Coronavirus from different perspectives in the optimization field. The authors in [47] proposed a bio-inspired metaheuristic algorithm based on the propagation model of coronavirus, and the experimental results showed quite remarkable performance of the algorithm. Al-Betal et al. [4] proposed an optimization algorithm based on herd immunity's effect in tackling the COVID pandemic. The comparative analysis showed that the proposed algorithm yields very competitive results compared to other well-established methods. Another algorithm [27] models the coronavirus distribution process as an optimization problem to minimize the number of COVID-19 infected countries and slow the epidemic.

Once the virus is inside the human body, the most severe problem is replication and transcription, in which new copies of the virus are created and target new healthy cells [49, 71]. This paper presents a novel evolutionary optimization algorithm named Coronavirus Disease Optimization Algorithm (COVIDOA).

COVIDOA mimics the attacking behavior of coronavirus inside human cells. It is worth mentioning that almost all kinds of viruses have the same general steps for replication: entry, uncoating, replication, assembly, and virion release. However, replication between viruses greatly varies depending on the genes involved [20].

In addition to the advantages of evolutionary algorithms, COVIDOA has several advantages when compared with other similar mechanisms:

1. Based on the virus's novelty and the lack of research on its various aspects, the reported numerical data about the coronavirus lifecycle may be inaccurate. Therefore, the proposed algorithm parameters, such as the number of virus particles in each generation and the number of viral proteins generated by each particle, haven't been set at fixed values. These reasons give the researchers' flexibility to use the extendable values for the controlling parameters that most fit according to their problem.
2. As mentioned in [8], the mutation rate of coronavirus is $1 \times 10^{-6}$, which is very low; however, the mutation rate in the proposed algorithm is set at a larger value in the range $[0.10 .001]$, which helps in exploring new promising regions and avoid getting stuck in a local minimum.
3. This study simulates a different virus replication technique known as the frameshifting technique [12, 43]. The virus uses frameshifting to create more copies of itself, leading to large-scale changes to polypeptide length and chemical composition. It is considered the most harmful to the molecular evolution of human cell proteins resulting in a non-functional protein that often disrupts the biochemical processes of a cell [59]. Applying the frameshifting technique in the proposed algorithm helps update solutions so that the solutions in each generation will not become too similar, which would allow the algorithm to converge to the global minimum.

The rest of the paper is structured as follows. Section 2 describes the inspiration and mathematical model of the proposed algorithm (COVIDOA). Experiments using test benchmark functions and the obtained results are discussed in Sect. 3. Finally, this study's conclusion and future work are presented in Sect. 4.

## 2 Proposed algorithm

In this section, the inspiration and mathematical model of COVIDOA are presented.

### 2.1 Inspiration

The new Coronavirus disease (COVID-19) is an infectious respiratory disease caused by Ssevere Aacute Respiratory Syndrome-CoronaVirus-2 (SARS-CoV-2). SARS-CoV-2 belongs to the coronaviruses family, named for crown-like spikes on their surface [34, 52], as shown in Fig. 2.

The coronavirus consists of a set of genetic instructions inside an oily membrane. These instructions are encoded in


Fig. 2 Structural proteins of COVID-19 (https://commons.wikimedia. org/wiki/File:3D_medical_animation_corona_virus.jpg) [30]

30,000 letters of Ribonucleic Acid (RNA)—a, $c, g$, and $u$-then read by the infected cell and translated into many types of virus proteins [8]. Like other Coronaviruses, SARS-CoV-2 (COID-19) has four structural proteins, including the spike $(S)$, envelope $(E)$, and membrane $(M)$ that constitute the viral coat, and the nucleocapsid $(\mathrm{N})$ protein, which encapsulates the viral RNA [12]. Human-to-human transmission of SARS-CoV-2 occurs primarily via respiratory droplets from coughs and sneezes. Complications may include acute respiratory distress syndrome (ARDS), multi-organ failure, septic shock, and death [43].

The most serious problem of the virus is rapid replication, where it creates millions of copies of itself and sends it out to damage as many as possible human healthy cells. The replication mechanism of coronavirus inspires the proposed algorithm. For the virus to replicate, it passes through several stages as follows:

### 2.1.1 Virus entry and uncoating

For replication, coronavirus needs to use the human cell's protein-making machinery. So, it first needs to gain entry into the cell. The virus contains a set of spike (S) proteins; it uses its spike proteins as a key to getting inside a human cell [9, 72]. One spike of the virus binds to a protein called angiotensin-converting enzyme 2 (ACE-2) [67] on the surface of some human cells, as shown in Fig. 3. Coronavirus has a sort of membrane that hides its genetic material from the outside world; human cells have the same membrane that hides their material from the outside world. So, when those two things come together, the virus must find a way to get inside the host cell [65]. Once inside, all structural proteins are removed, and the virus contents, the genomic RNA, will be released into the host cell cytoplasm. This process is called virus uncoating [74], as shown in Fig. 4.


Fig. 3 Virus attachment to human cell through spike protein (https:// time.com/5839932/how-remdesivir-works-coronavirus/) [31]


Fig. 4 Virus entry and uncoating


Fig. 5 Virus RNA converts to viral proteins

### 2.1.2 Virus replication

Suppose the virus is getting fused in the cell membrane. Its small genetic material must hijack big cellular machinery in the next step. It will be tedious if the virus has few proteins to hijack the cell. The virus genome starts to find something in the host cell called a ribosome [79], a ribosome turns the virus RNA into many virus proteins through the ribosomal frameshifting technique [36], as shown in Fig. 5.

### 2.1.2.1 Ribosomal frameshifting during genome transla-

 tion Ribosomal frameshifting is also known as translational frameshifting, a biological phenomenon that occurs during translation [36, 54]. This phenomenon creates multiple unique proteins from a single messenger RNA (mRNA) molecule [14]. The translation is when the mRNA (messenger Ribonucleic Acid) molecule provides information to ribosomes, leading to protein molecules' formation [36, 37]. At the same time, frameshifting is when a specific reading frame of RNA molecule shifts to another reading frame to provide a new protein sequence [67, 72, 74]. To understand this, we need to understand translation and frameshifting separately.Fig. 6 Generation of different protein sequences during frameshifting

Normal Translation

+1 Frameshifting Translation

-1 Frameshifting Translation
AC GCA CGC AUC AGC CAC GGA...



$\mathrm{M} \longrightarrow$ Protein sequence 3

(a)

(b)

Fig. 7 Different examples of frameshifting technique $\mathbf{a}-1$ frameshifting, $\mathbf{b}+1$ frameshifting, where $\mathrm{E}, \mathrm{P}$, and A , are the first, second, and third binding sites for RNA in the ribosome [14]

The frameshifting technique is presented in Fig. 6. As shown in the figure, in the replication process, the virus's mRNA is translated into viral proteins by reading tri-nucleotides (e.g., ACG). Each tri-nucleotide is translated into single amino acid [52]. Thus, shifting (backward or forward) the reading frame of the nucleotides sequence by any number (not divisible by 3 ) will create different sequences that will be translated into different viral proteins [68].

Each group of the newly created viral proteins is merged to form a new virion. According to this technique, the virus
can create millions of new particles than will damage millions of human cells.

In a translating ribosome, a frameshifting can result in either a nonsense mutation [68, 72] or a new protein after the frameshift. The most common types of frameshifting are -1 frameshifting and +1 frameshifting [58].
A. -1 Frameshifting

In -1 frameshifting, the ribosome slips back one


Fig. 8 Release of the new virion. (https://time.com/5839932/how-remdesivir-works-coronavirus/)
nucleotide (RNA letter) and continues translation in the -1 frame, as shown in Fig. 7a.
B. +1 Frameshifting

The ribosome starts translation from the +1 frame when 0 is the initial position, as shown in Fig. 7b. Because of shifting, the sequences are read differently and translated into different proteins.
2.1.2.2 Synthesis of both genomic and subgenomic RNA species The ribosomal frameshifting technique results in two types of RNAs, genomic RNA, and subgenomic

RNAs. Genomic RNA is produced through the replication process and becomes the genome of the new virus particle. At the same time, Subgenomic RNAs are translated into many structural proteins (S: spike protein, E: envelope protein, M : membrane protein, and N : nucleocapsid protein). The genomic RNA and subgenomic RNAs are combined to form a viral particle [45, 58]. Finally, the new virion is released, trying to hijack new healthy cells, Fig. 8.

### 2.1.3 Virus mutation

As coronaviruses spread from person to person, they randomly accumulate more mutations to escape from the immune system [45]. Mutations involve changing one or more letters that represent the virus genome. As mentioned in [8], coronavirus has lower mutation rates $\left(\approx 10^{-6}\right.$ per site per cycle) in comparison with influenza ( $\approx 3 \times 10^{-5}$ per site per cycle). The replication stages of coronavirus are summarized in Fig. 9.

### 2.2 Mathematical model of COVIDOA

In this section, the mathematical model of COVIDOA is provided. COVIDOA is summarized in the following steps:

1. Initialization population of solutions is randomly initialized, and the cost is evaluated for each solution. The solutions are then ordered ascendingly according


Fig. 9 Replication lifecycle of coronavirus
to the fitness function, and the first solution is considered the best solution.
2. Virus replication phase through frameshifting technique for each solution in the population, a parent is selected using roulette wheel selection [46] then,
a. The frameshifting technique is applied to produce several proteins from the selected parent as follows:
b. For each protein:
i. If the +1 frameshifting technique is used, the parent solution's values are shifted in the right direction by 1 , and the value in the first position is set at a random value in the range [minVal maxVal] as follows.
$S_{k}(1)=\operatorname{rand}(\operatorname{minVal}, \operatorname{maxVal})$,
$S_{k}(2: D)=P(1: D-1)$,
where minVal and maxVal are the minima and maximum values for the variables in each solution.
ii. If the -1 frameshifting technique is used, the parent solution values are shifted backward by 1 , and the value in the last position is to set a random value in the range [minVal, maxVal].

$$
\begin{align*}
& S_{k}(D)=\operatorname{rand}(\operatorname{minVal}, \operatorname{maxVal})  \tag{3}\\
& S_{k}(1: D-1)=P(2: D) \tag{4}
\end{align*}
$$

The symbol $S_{k}$ refers to the $k$ th generated protein, $P$ is the parent solution, and $D$ is the problem dimension (number of variables in each solution). The result of frameshifting represents a new protein sequence.
c. New virion formation a uniform crossover is applied to the generated sub-proteins to produce a new virion (new solution).
3. Mutation a mutation operator is applied to the solution created in the previous step to generate a new mutated solution as follows:

$$
Z(i)= \begin{cases}r & \text { if rand }(0,1)<\mathrm{MR}  \tag{5}\\ X(i) & \text { otherwise }\end{cases}
$$

$X$ is the solution before mutation. $Z$ is the mutated solution, $X(i)$ and $Z(i)$ are the $i$ th element in the old and new solutions, respectively, $i=1, \ldots, D$, and $r$ is a random value in the range [minVal, maxVal]. MR is the mutation rate.
4. The objective function is evaluated for the new solution, and the population is updated for the next generation (the solutions with the highest fitness remain, and the others are removed).
5. Repeat steps $(2-4)$ for the new population until termination criteria are achieved. For example, the maximum number of iterations is reached.
6. Output the best solution found so far.

The flowchart of the proposed algorithm is shown in Fig. 10.

### 2.3 Parameters of the proposed algorithm

The parameters of the proposed algorithm are suggested as follows:

- Max_Iter maximum number of iterations.
- PopNo number of solutions in the population.
- MinVal and MaxVal minimum and maximum value of variables in a solution.
- $D$ problem dimension (number of variables in each solution).
- CostFunction objective function;
- MR Mutation Rate, MR is set at a value in the range [0.1 0.001].

The pseudocode of the proposed algorithm is as follows:

```
Set the initial values of the population size PopNo, maximum number of iterations
Max_Iter, minimum and maximum values MinVal, MaxVal, problem dimension D, cost
function, mutation rate MR=0.001, frameshifting technique shifting = lor -1,
number of generated proteins numOfProtiens,
For (i= 1:i\leqn)do
    Generate initial random population }\mp@subsup{X}{i}{}(t)
    Evaluate the fitness function of each solution in the population.
End for
Order the solutions ascendingly according to the fitness function.
Set the first solution as the optimum solution Xi**(t).
Set t=1;
Repeat
    For (i=1:i\leqn)do
        Select a parent solution P,
        If (shiftingNo = 1) then
                                    For (k=1:k\leqnumOfProtiens) do
                                    Generate protein S Srom parent P using equations (1) and
    (2).
        End for
        Else
        For (k=1:k\leqnumOfProtiens) do
                        Generate protein S Srom parent P using equations (3) and
    (4).
                End for
        End if
        Apply uniform crossover between the set of generated proteins to
        produce new virion (new solution).
        If (rand (0,1)<MR) then
        Mutate the new solution using equation (5)
        End for
    End for
Until t > MaxIt
```

- Shifting a number that represents the type of frameshifting used. For example, shiftingNo $=1$ means that the +1 frameshifting technique is used. We noticed that the +1 frameshifting technique yields the best results.
- numOfProtiens number of proteins generated during virus replication in the proposed algorithm, numOfProteins is 2 .


## 3 Experimental results and discussion

### 3.1 Benchmark functions

To test the efficiency of the proposed COVIDOA, we utilized 30 benchmark functions. The first 20 are classical standard benchmark test functions (http://benchmarkfcns. xyz) [29]. We selected five functions from IEEE CEC 2019 Competition (https://www.mathworks.com/matlabcentral/
fileexchange/72123-cec-06-2019-matlabimplementation) [33], while the remaining five were selected from CEC 2011 Competition on Testing Evolutionary Algorithms on Real-World Optimization Problems [16] as follows:
I. Classical benchmark problems

Twenty standard optimization functions from the literature are discussed and used to test the proposed algorithm's efficiency. These functions are classified into four groups: unimodal, multimodal, fixed-dimension, and n-dimensional functions [35, 39]. In fixed-dimension problems, the number of design variables (problem dimension) is fixed, while the other n-dimension problems use any design variables. A multimodal function has multiple (at least locally optimum) solutions instead of a unimodal function with a single optimum solution [35]. As in "Table 11 in the Appendix", the chosen optimization functions are described in terms of the function name, formula, problem dimension (D), range of possible values, the global

Fig. 10 Flowchart of COVIDOA

optimum, and the group of benchmark functions to which it belongs.

## II. IEEE CEC 2019 benchmark problems

In addition to the classical benchmark functions, five CEC benchmark functions are utilized for evaluation. These are a group of modern test functions known as "The 100-Digit Challenge" intended to be used in single
objective numerical optimization IEEE competitions [2]. As shown in "Table 12 in the Appendix", these functions are described in terms of problem dimension, range of possible values, and the global optimum (https://www. mathworks.com/) [32].
III. CEC 2011 Real-World Problems
Table 1 Best Cost results of COVIDOA and the state-of-the-art algorithms

| Problem |  | Algorithm |  |  |  |  |  |  |  |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| No. | Name | GA [26] | DE [63] | PSO [44] | FPA [75] | GWO [51] | WOA [50] | CHIO [4] | SOA [19] | Proposed COVIDOA |
| 1 | Dixon-price function | 0.66667 | 0.40228 | 0.6667 | 4.9183 | 1 | 0.6667 | 1.694 | 0.6667 | 0.27378 |
| 2 | Happy Cat function | 0.1386 | 0.014702 | 0.24166 | 231.478 | 0.0122 | 1.4353 | 0.2691 | 0.005142 | 0.0023146 |
| 3 | Crosslegtable function | - 0.08493 | -0.084778 | - 0.07981 | -0.0006630 | - 3.869e-04 | - 0.0016362 | - 2.606e-04 | - $2.4310 \mathrm{e}-04$ | -1 |
| 4 | Eggholder function | - 4886.18 | - 7445.3819 | - 5858.46 | - 6292.2901 | - 6.006 e+03 | - 6319.4385 | - 6385 | - 5441.7 | - 7825.143 |
| 5 | stybtang function | - 566.287 | - 626.6587 | - 626.658 | - 530.9072 | - 626.086 | - 555.9751 | -619.1 | - 605.2622 | - 626.621 |
| 6 | Schwefel function | - 837.965 | - 837.9529 | - 837.965 | - 837.9657 | - 837.965 | - 837.9658 | -837.9548 | - 837.9658 | - 837.9658 |
| 7 | Keane function | - 0.67367 | - 0.67367 | - 0.67367 | - 0.67367 | -0.6736 | - 0.67367 | -0.6737 | - 0.67367 | - 0.67367 |
| 8 | Trid function | - 2 | - 2 | - 2 | -2 | - 2 | - 2 | - 2 | - 2 | -2 |
| 9 | Schaffern4fen function | 0.2926 | 0.29258 | 0.29258 | 0.29258 | 0.2926 | 0.29258 | 0.2926 | 0.29258 | 0.29258 |
| 10 | Branin function | 0.39789 | 0.39789 | 0.39789 | 0.39789 | 0.39789 | 0.39789 | 0.4071 | 0.39789 | 0.39789 |
| 11 | Wolfe function | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 |
| 12 | Zettl function | -0.0037 | -0.0037 | - 0.0037 | - 0.0037 | - 0.0038 | - 0.0038 | - 0.0037 | - 0.0038 | - 0.0038 |
| 13 | Alpine N. 2 function | - 14,320.0 | - 23,700.87 | - 14,320.08 | -8649.361 | - 2369 | - 23,700.7978 | - 1.7386 | - 14,277 | - 23,563.73 |
| 14 | Cross-in-Tray function | - 2.0626 | - 2.0626 | - 2.0626 | - 2.0626 | - 2.0626 | - 2.0626 | - 2.0626 | - 2.0626 | - 2.0626 |
| 15 | McCormick function | - 1.9105 | - 1.9105 | - 1.9105 | - 1.9105 | - 1.9105 | - 1.9105 | - 1.9105 | - 1.9105 | - 1.9105 |
| 16 | Gramacy and Lee function | - 2.8739 | - 2.8739 | - 2.8739 | - 2.8739 | - 2.8739 | - 2.8739 | - 2.8739 | - 2.8739 | - 2.8739 |
| 17 | Testubeholder function | - 10.8723 | - 10.8723 | - 10.8723 | - 10.8723 | - 10.8723 | - 10.8723 | - 10.8723 | - 10.8723 | - 10.8723 |
| 18 | Shubert function | - 186.7309 | - 186.7309 | - 186.7309 | - 186.7309 | - 186.7309 | - 186.7309 | - 186.7082 | - 186.7309 | - 186.7309 |
| 19 | price 2 function | 0.9 | 0.9 | 0.9 | 0.9004 | 0.9 | 0.9 | 0.9001 | 0.9 | 0.9 |
| 20 | Dejong5 | 0.998 | 0.998 | 0.998 | 0.998 | 0.998 | 0.998 | 0.9980 | 0.998 | 0.998 |

Table 2 Average Cost results of COVIDOA and the state-of-the-art algorithms

| Problem |  | Algorithm |  |  |  |  |  |  |  |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| No. | Name | GA [26] | DE [63] | PSO [44] | FPA [75] | GWO [51] | WOA [50] | CHIO [4] | SOA [19] | Proposed COVIDOA |
| 1 | Dixon-price function | 15.3545 | 126.5770 | 6.3509 | $1.0998 \mathrm{e}+03$ | 46.6686 | 30.0319 | $1.0734 \mathrm{e}+03$ | $9.897 \mathrm{e}+03$ | 5.23636 |
| 2 | Happy Cat function | 0.6517 | 0.0445 | 0.2636 | 371.4819 | 0.0802 | 20.4486 | 0.2930 | 0.0477 | 0.0137 |
| 3 | Crosslegtable function | -0.0683 | -0.0427 | - 0.0427 | - 0.7909 | - 5.1528e-04 | $-2.6865 \mathrm{e}-04$ | -2.182e-04 | - 0.0047 | - 0.8980 |
| 4 | Eggholder function | $-4.70 \mathrm{e}+03$ | $-6.75 \mathrm{e}+03$ | - $5.628 \mathrm{e}+03$ | $-5.681 \mathrm{e}+03$ | $-5.2816 \mathrm{e}+03$ | $-6.2799 \mathrm{e}+03$ | $-5.679 \mathrm{e}+03$ | $-4.262 \mathrm{e}+03$ | $-7.23 \mathrm{e}+03$ |
| 5 | Stybtang function | - 393.6128 | -619.9509 | - 619.2246 | - 475.8865 | - 577.2454 | - 552.6846 | - 572.8967 | - 594.1131 | -622.7337 |
| 6 | Schwefel function | - 835.3788 | -821.9348 | - 837.8732 | -837.5112 | -837.5351 | - 837.9275 | - 835.5825 | - 837.6662 | -837.9367 |
| 7 | Keane function | - 0.673659 | - 0.673667 | - 0.673667 | -0.67359 | -0.673661 | -0.673633 | - 0.6736 | - 0.673519 | - 0.673667 |
| 8 | Trid function | - 1.9999 | - 1.9999 | - 1.9999 | - 2 | - 1.9999 | - 1.9999 | - 1.9996 | - 1.9993 | - 2 |
| 9 | Schaffern4fcn function | 0.2928 | 0.2930 | 0.2926 | 0.2930 | 0.2927 | 0.2928 | 0.2961 | 0.2947 | 0.2926 |
| 10 | Branin function | 0.3980 | 0.3982 | 0.3979 | 0.3984 | 0.3987 | 0.3984 | 0.4673 | 0.4205 | 0.3981 |
| 11 | Wolfe function | 0.0144 | $1.7214 \mathrm{e}-04$ | $8.5733 \mathrm{e}-05$ | 0 | $3.3785 \mathrm{e}-04$ | $1.4367 \mathrm{e}-04$ | 0.0055 | 3.7236e-04 | 0 |
| 12 | Zettl function | - 0.0038 | - 0.0038 | - 0.0038 | - 0.0036 | - 0.0038 | - 0.0038 | - 0.0028 | - 0.0036 | - 0.0038 |
| 13 | Alpine N. 2 function | $-1.32 \mathrm{e}+04$ | $-2.114 \mathrm{e}+04$ | - $1.402 \mathrm{e}+04$ | $-5.826 \mathrm{e}+03$ | $-1.2565 \mathrm{e}+0$ | $-2.1515 \mathrm{e}+04$ | $-9.569 \mathrm{e}+03$ | $-2.014 \mathrm{e}+03$ | $-2.18 \mathrm{e}+04$ |
| 14 | Cross-in-Tray function | - 2.0626 | - 2.0626 | - 2.0626 | - 2.0626 | - 2.0626 | - 2.0626 | - 2.0626 | - 2.0626 | - 2.0626 |
| 15 | McCormick function | - 1.9105 | - 1.9105 | - 1.9105 | - 1.9105 | - 1.9105 | - 1.9105 | - 1.9103 | - 1.9105 | - 1.9105 |
| 16 | Gramacy and Lee function | - 2.87389 | - 2.87384 | - 2.87389 | - 2.87389 | - 2.87389 | - 2.87389 | - 2.8739 | - 2.87385 | - 2.87389 |
| 17 | Testtubeholder function | - 10.8718 | - 10.8720 | - 10.8721 | - 10.8718 | - 10.8721 | - 10.8717 | - 10.8697 | - 10.8638 | - 10.8721 |
| 18 | Shubert function | - 186.6132 | - 186.6495 | - 186.6853 | - 186.4929 | - 186.6285 | - 186.6954 | - 186.4249 | - 186.2621 | - 186.7009 |
| 19 | Price 2 function | 0.90037 | 0.900945 | 0.900233 | 0.902144 | 0.9006 | 0.90033 | 0.9031 | 0.91701 | 0.90004 |
| 20 | Dejong5 | 1.0115 | 1.0065 | 0.9987 | 1.0218 | 1.0122 | 1.0100 | 1.1783 | 1.2333 | 0.9980 |

Table 3 STD results of COVIDOA and the state-of-the-art algorithms

| Problem |  | Algorithm |  |  |  |  |  |  |  |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| No. | Name | GA [26] | DE [63] | PSO [44] | FPA [75] | GWO [51] | WOA [50] | CHIO [4] | SOA [19] | Proposed COVIDOA |
| 1 | Dixon-price function | 269.8620 | $1.1364 \mathrm{e}+03$ | 62.4047 | $3.545 \mathrm{e}+03$ | 894.3655 | 451.6185 | $4.0605 \mathrm{e}+03$ | $7.220 \mathrm{e}+03$ | 52.7791 |
| 2 | Happy Cat function | 0.1139 | 78.6462 | 46.1026 | 109.0887 | 0.0522 | 0.0406 | 0.0390 | 0.2955 | 0.0294 |
| 3 | crosslegtable function | 0.0321 | 0.0392 | 0.0357 | $1.557 \mathrm{e}-04$ | $4.8352 \mathrm{e}-05$ | $2.212 \mathrm{e}-04$ | $3.1194 \mathrm{e}-05$ | 2.6201e-05 | $2.8268 \mathrm{e}-05$ |
| 4 | Eggholder function | 380.0907 | 878.5967 | 426.2801 | 574.4192 | 450.2399 | 236.1962 | 701.8892 | 979.6934 | 425.3867 |
| 5 | Stybtang function | 36.0487 | 42.5232 | 13.4428 | 45.6925 | 26 | 21.2045 | 49.1493 | 50.9105 | 18.6986 |
| 6 | Schwef function | 3.5750 | 0.3603 | 0.2791 | 1.9761 | 0.6225 | 2.0103 | 3.2773 | 6.3983 | 0.1706 |
| 7 | Keane function | $9.276 \mathrm{e}-05$ | $4.1333 \mathrm{e}-06$ | 3.492e-06 | 0.0011 | $1.242 \mathrm{e}-04$ | $7.286 \mathrm{e}-04$ | 7.1552e-05 | 0.0033 | 6.6663e-08 |
| 8 | Trid function | 0.0015 | $9.1279 \mathrm{e}-04$ | $8.566 \mathrm{e}-05$ | $3.721 \mathrm{e}-04$ | $5.869 \mathrm{e}-04$ | 0.0023 | 7.1631e-04 | 0.0023 | 1.9900e-05 |
| 9 | Schaffern4fen function | $9.484 \mathrm{e}-04$ | 0.0033 | 0.0469 | 0.0016 | $6.954 \mathrm{e}-04$ | 0.0031 | 0.0050 | 0.0041 | 5.6588e-04 |
| 10 | Branin function | 0.0016 | 0.0013 | 3.902-04 | 0.0035 | 0.0063 | 0.0023 | 0.4256 | 0.0246 | 3.6041e-04 |
| 11 | Wolfe function | 0.0393 | 0.0027 | 0.0019 | 0 | 0.0076 | 0.0032 | 0.0303 | 0.0083 | 0 |
| 12 | Zettl function | $1.696 \mathrm{e}-04$ | $2.3912 \mathrm{e}-04$ | 6.959e-05 | 0.0011 | $8.467 \mathrm{e}-04$ | $1.704 \mathrm{e}-04$ | 0.0034 | 0.0015 | 1.1646e-04 |
| 13 | Alpine N. 2 function | $5.807 \mathrm{e}+03$ | $2.1124 \mathrm{e}+04$ | 1.247e+03 | $2.4308 \mathrm{e}+03$ | $6.94 \mathrm{e}+034$ | $3.901 \mathrm{e}+03$ | $5.3061 \mathrm{e}+03$ | $2.3812 \mathrm{e}+03$ | $1.7739 \mathrm{e}+03$ |
| 14 | Cross-in-Tray function | $3.718 \mathrm{e}-05$ | $2.8873 \mathrm{e}-05$ | $4.8930 \mathrm{e}-06$ | $3.0880 \mathrm{e}-04$ | $3.903 \mathrm{e}-05$ | $3.9988 \mathrm{e}-05$ | $1.4093 \mathrm{e}-04$ | 0.0012 | $4.5473 \mathrm{e}-06$ |
| 15 | McCormick function | $6.450 \mathrm{e}-05$ | $1.3749 \mathrm{e}-04$ | $1.361 \mathrm{e}-06$ | $8.3451 \mathrm{e}-05$ | 0.0013 | $7.382 \mathrm{e}-04$ | 0.0013 | 0.0041 | 2.6101e-07 |
| 16 | Gramacy and Lee function | $4.198 \mathrm{e}-04$ | 0.0010 | $1.856 \mathrm{e}-05$ | 7.1457e-06 | $4.162 \mathrm{e}-04$ | $6.207 \mathrm{e}-05$ | $4.8450 \mathrm{e}-05$ | 4.3901e-04 | 4.1554e-08 |
| 17 | Testtubeholder function | 0.0034 | 0.0018 | 0.0015 | 0.0065 | 0.0038 | 0.0058 | 0.0103 | 0.0207 | 0.0021 |
| 18 | shubert function | 0.6984 | 0.5832 | 0.4346 | 1.2720 | 1.2720 | 0.3873 | 0.7193 | 0.7625 | 0.2339 |
| 19 | Price 2 function | 0.0034 | 0.0068 | 0.0045 | 0.0063 | 0.0054 | 0.0050 | 0.0096 | 0.0375 | 1.4613e-04 |
| 20 | Dejong5 | 0.1339 | 0.1025 | $8.7297 \mathrm{e}-05$ | 0.1555 | 0.1185 | 0.1910 | 0.4304 | 0.7947 | 3.4653e-05 |

Table 4 Convergence speed of COVIDOA and the state-of-the-art algorithms

| Problem |  | Algorithms |  |  |  |  |  |  |  |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| No. | Name | GA [26] | DE [63] | PSO [44] | FPA [75] | $\begin{aligned} & \text { GWO } \\ & \text { [51] } \end{aligned}$ | WOA <br> [50] | CHIO [4] | $\begin{aligned} & \text { SOA } \\ & \text { [19] } \end{aligned}$ | Proposed <br> COVIDOA |
| 1 | Dixon-price function | Moderate | Moderate | Moderate | Slow | Moderate | Moderate | Moderate | Slow | Moderate |
| 2 | Happy Cat function | Moderate | Slow | Moderate | Slow | Slow | Slow | Slow | Slow | Moderate |
| 3 | Crosslegtable function | Moderate | Moderate | Moderate | Slow | Slow | Slow | Slow | Slow | Fast |
| 4 | Eggholder function | Slow | Slow | Slow | Slow | Slow | Slow | Slow | Slow | Moderate |
| 5 | Stybtang function | Slow | Slow | Slow | Slow | Slow | Fast | Fast | Slow | Fast |
| 6 | Schwef function | Fast | Fast | Fast | Fast | Fast | Fast | Moderate | Fast | Fast |
| 7 | Keane function | Fast | Fast | Fast | Fast | Fast | Fast | Fast | Fast | Fast |
| 8 | trid function | Fast | Fast | Fast | Fast | Fast | Fast | Fast | Slow | Fast |
| 9 | schaffern4fenfunction | Fast | Fast | Fast | Fast | Fast | Fast | Fast | Moderate | Fast |
| 13 | Alpine N. 2 function | Slow | Moderate | Slow | Slow | Moderate | Slow | Moderate | Slow | Moderate |
| 14 | Cross-in-Tray function | Fast | Fast | Fast | Fast | Fast | Fast | Fast | Slow | Fast |
| 15 | McCormick function | Fast | Fast | Fast | Fast | Fast | Fast | Fast | Fast | Fast |
| 18 | Shubert function | Fast | Fast | Fast | Fast | Fast | Fast | Fast | Fast | Fast |
| 19 | Price 2 function | Fast | Fast | Fast | Moderate | Fast | Fast | Fast | Fast | Fast |
| 20 | Dejong5 | Fast | Fast | Fast | Fast | Fast | Fast | Fast | Moderate | Fast |

For further evaluation, COVIDOA was applied to five real-world optimization problems. These are bound-constrained real-world optimization problems selected from the CEC 2011 Competition on Testing Evolutionary Algorithms on Real-World Optimization. These problems are as follows [16]:

1. Lennard-Jones Potential Problem.
2. Transmission Network Expansion Planning (TNEP) problem.
3. Tersoff Potential Function Minimization Problem for model $\mathrm{Si}(\mathrm{B})$.
4. Tersoff Potential Function Minimization Problem for model $\mathrm{Si}(\mathrm{C})$.
5. Spread spectrum radar polyphase problem.

A detailed description of these real-world problems is discussed in the 2011 IEEE-Congress on Evolutionary Computation (IEEE-CEC 2011) [16].

### 3.2 Experimental results

COVIDOA is utilized to solve the previously mentioned test problems. COVIDOA is implemented in MATLAB R2016a software. The results are compared with eight well-known and recent optimization algorithms: GA [26], DE [63], PSO [44], FPA [75], GWO [51], WOA [50], SOA [19], and CHIO [4]. We selected this group of algorithms for many reasons:
(1) Most of them are recent and published in reputable sources.
(2) All of them have high performance in singleobjective optimization on various benchmark functions.
(3) Their MATLAB implementations are publicly available on the MATLAB website (https://www.math works.com/) [32].
(4) Some of them are evolutionary algorithms, such as GA and DE, in the same category as COVIDOA. CHIO algorithm simulates coronavirus, as is COVIDOA, but each has its inspiration.

The obtained results change at each run in optimization algorithms due to the random process. The commonly used number of runs is 30 , which would give acceptable statistical precision. So, the proposed algorithm and the state-of-the-art algorithms are run 30 times.

The proposed and state-of-the-art algorithms use Max_Iter $=500$ and PopNo $=1000$ for the classical benchmark functions. The comparison is made regarding optimum cost, average cost, standard deviation (STD), and convergence speed. The authors downloaded the source code of the state-of-the-art optimization algorithms from the MATLAB website.

Tables 1, 2, 3 and 4 show the results of the best cost, average cost, standard deviation, and convergence speed, respectively, for the 20 classical benchmark functions. The best-obtained results in all the following tables are


4 Fig. 11 Comparison of convergence curves of COVIDOA and state-of-the-art algorithms for group 1 of the test problems
highlighted in bold. Table 1 shows that the proposed algorithm reaches the optimum global cost in 18 of 20 problems and gets very close to the global optimum in the two remaining problems. Table 2 proves the COVIDOA algorithm's efficiency in terms of the average cost. It reaches the minimum average cost in 17 from 20 problems and the second minimum average cost in three. The third criterion is STD, which shows how the cost values are far
from the average cost. Low STD values mean the cost values over the iterations are clustered closely around the average cost. Table 3 shows that the COVIDOA algorithm reaches the minimum STD values in 17 of 20 problems, the second minimum in two, and the third minimum in two, which means that the results of COVIDOA are more reliable than the other algorithms with higher STD values.

Compared with the recently proposed algorithm, CHIO, which simulates herd immunity's effect in tackling the COVID pandemic, COVIDOA is the best. As shown in Tables 1, 2, 3 and 4 and Figs. 11, 12, 13 and 14, CHIO reaches the minimum optimum cost in seven benchmark


Fig. 12 Comparison of convergence curves of COVIDOA and state-of-the-art algorithms for group 2 of the test problems


Fig. 13 Comparison of convergence curves of COVIDOA and state-of-the-art algorithms for CEC benchmark functions
functions only from 25; in contrast, COVIDOA reaches the minimum optimum cost in 21 from 25 test functions. This indicates that COVIDOA has robust exploration capabilities in comparison with CHIO.

Compared with PSO, GWO, and WOA, COVIDOA is superior according to most of the test problems' best cost, average cost, and STD values. It has a higher convergence speed as it reaches the global minimum after the first few iterations, as in functions (F3, F8, F7, F15, and F16).

The curves in Figs. 11 and 12 represent the relationship between the iterations and the corresponding best cost for the classical test functions. The obtained results using the
selected test problems are divided into two groups and displayed in Figs. 11 and 12. Figure 11 represents the test problems for which the COVIDOA algorithm outperforms the other algorithms. In contrast, Fig. 12 shows the results of test problems in which the COVIDOA algorithm has a performance very close to the others.

Additionally, to prove the results' statistical significance, the test results of the 20 classical benchmark functions are compared using Wilcoxon rank-sum test at the 5\% significance level [18]. A null hypothesis is a type of hypothesis used in statistics that assumes no significant difference between the two methods' average values.


Fig. 14 Comparison of convergence curves of COVIDOA and state-of-the-art algorithms for CEC 2011 real-world problems

A small $p$-value (typically $\leq 0.05$ ) indicates strong evidence against the null hypothesis [70].

Table 5 introduces the $p$ values computed by Wilcoxon rank-sum test that compares the COIDOA with eight wellknown metaheuristic algorithms for the 20 classical benchmark functions. We observed from Table 5 that all $p$ values are less than a $5 \%$ significance level for all comparative algorithms, strong evidence against the null hypothesis. Therefore, we conclude that the COVIDOA is better than all other comparative algorithms.

CEC benchmark functions, COVIDOA, and state-of-the-art algorithms search for the optimum cost for 250 iterations with 1000 solutions in each generation. The results of the best cost, average cost, and STD values are discussed in Table 6, and the convergence curves are shown in Fig. 13. COVIDOA is superior to the other algorithms in CEC01, CEC06, and CEC01. The CEC03 problem reaches the minimum best cost and the second minimum average cost ad STD value. In the case of CEC07, however, it is not the best; it achieves excellent results compared to GA, FPA, GWO, WOA, SOA, and CHIO algorithms.

All test results for the CEC benchmark functions were compared using the Wilcoxon rank-sum test to prove their statistical significance. Table 7 shows the $p$ values computed by Wilcoxon rank-sum test that compares the COIDOA with other well-known algorithms for CEC benchmark functions. It is evident from Table 7 that all $p$ values are less than $5 \%$ which proves the statistical significance of COVIDOA.

To test the impact of changing parameter values on the performance of OVIDOA, we used nine different scenarios by changing the values of the parameters MR (Mutation Rate) and numOfProtiens. We utilized the values of 0.1 , 0.01 , ad 0.001 for MR, 2, 4, and 6 for numOfProtiens which produces nine scenarios, as shown in Table 8. The results of each scenario on the selected five IEEE CEC benchmark problems are presented in Table 9. We noticed that scenario $1(\mathrm{MR}=0.1$ and numOfProtiens $=2)$ has better results, followed by scenario 4 . The common between these two scenarios is $\mathrm{MR}=0.1$ which represents a higher mutation rate. This comparison shows that higher MR values are better for improving the performance of the proposed algorithm.
Table 5 P values computed by Wilcoxon's rank-sum test compared the COVIDOA with other algorithms for 20 classical benchmark functions

| Problem |  | Algorithm |  |  |  |  |  |  |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| No. | Name | COVIDOA vs. GA | COVIDOA vs. DE | $\begin{aligned} & \text { COVIDOA vs. } \\ & \text { PSO } \end{aligned}$ | $\begin{aligned} & \text { COVIDOA vs. } \\ & \text { FPA } \end{aligned}$ | COVIDOA vs. GWO | COVIDOA vs. WOA | $\begin{aligned} & \text { COVIDOA vs. } \\ & \text { CHIO } \end{aligned}$ | $\begin{aligned} & \text { COVIDOA vs. } \\ & \text { SOA } \end{aligned}$ |
| 1 | Dixon-price function | $2.2242 \mathrm{e}-06$ | 8.0835e-24 | $1.3497 \mathrm{e}-09$ | 1.6207e-129 | 6.6181e-12 | $1.0616 \mathrm{e}-13$ | 4.0517e-134 | 2.2667e-102 |
| 2 | Happy Cat function | $2.3444 \mathrm{e}-41$ | $2.9609 \mathrm{e}-142$ | $4.6130 \mathrm{e}-59$ | 7.0570e-151 | $7.8828 \mathrm{e}-78$ | $6.2314 \mathrm{e}-153$ | $3.3083 \mathrm{e}-158$ | 2.3994e-168 |
| 3 | Crosslegtable function | 3.8478e-147 | 2.6216e-149 | $1.2983 \mathrm{e}-131$ | 5.9989e-71 | $8.8060 \mathrm{e}-112$ | 3.0525e-168 | 1.7277e-168 | 2.1944e-5 |
| 4 | Eggholder function | $1.5930 \mathrm{e}-08$ | $3.5431 \mathrm{e}-35$ | $4.7752 \mathrm{e}-101$ | 6.9415e-107 | 4.2077e-102 | $1.2085 \mathrm{e}-97$ | $7.0318 \mathrm{e}-99$ | 1.8854e-169 |
| 5 | stybtang function | $3.5988 \mathrm{e}-89$ | 3.8579e-92 | $9.8348 \mathrm{e}-156$ | $3.5551 \mathrm{e}-160$ | $1.3910 \mathrm{e}-150$ | $4.2362 \mathrm{e}-151$ | $4.8158 \mathrm{e}-148$ | 7.4638e-172 |
| 6 | Schwefel function | $1.3895 \mathrm{e}-123$ | $1.9569 \mathrm{e}-164$ | $4.7482 \mathrm{e}-132$ | $2.6478 \mathrm{e}-24$ | $2.7706 \mathrm{e}-42$ | $1.3129 \mathrm{e}-155$ | $1.9594 \mathrm{e}-121$ | 7.4398e-142 |
| 7 | Keane function | 2.1931e-145 | $4.5728 \mathrm{e}-141$ | $7.8435 \mathrm{e}-146$ | $7.4084 \mathrm{e}-141$ | 1.8957e-138 | $2.5242 \mathrm{e}-139$ | $4.3658 \mathrm{e}-155$ | 1.3654e-145 |
| 8 | Trid function | $2.3005 \mathrm{e}-04$ | $1.2665 \mathrm{e}-07$ | 5.4793e-15 | $3.9880 \mathrm{e}-12$ | 3.6942e-132 | 2.7804e-129 | $2.0510 \mathrm{e}-140$ | 7.0287e-143 |
| 9 | Schaffern4fen function | 8.6497e-151 | $1.4164 \mathrm{e}-133$ | 1.2696e-139 | $3.4423 \mathrm{e}-57$ | 8.8837e-158 | 1.5795e-160 | $5.5992 \mathrm{e}-53$ | 1.0205e-04 |
| 10 | Branin function | 1.4628e-170 | $1.5300 \mathrm{e}-166$ | $9.9148 \mathrm{e}-147$ | $3.9973 \mathrm{e}-56$ | $4.0798 \mathrm{e}-31$ | 1.5096e-163 | $3.7413 \mathrm{e}-04$ | 1.4814e-99 |
| 11 | Wolfe function | $8.6069 \mathrm{e}-11$ | $1.6745 \mathrm{e}-18$ | $1.3438 \mathrm{e}-25$ | $1.3438 \mathrm{e}-25$ | $8.1128 \mathrm{e}-25$ | 8.2198e-25 | $3.2408 \mathrm{e}-05$ | 8.2198e-25 |
| 12 | Zettl function | $2.4618 \mathrm{e}-47$ | $3.7395 \mathrm{e}-48$ | $7.9714 \mathrm{e}-46$ | $4.2188 \mathrm{e}-51$ | $8.4116 \mathrm{e}-43$ | $2.6398 \mathrm{e}-43$ | $6.3415 \mathrm{e}-64$ | 2.3241e-60 |
| 13 | Alpine N. 2 function | $1.1328 \mathrm{e}-63$ | $2.1170 \mathrm{e}-87$ | $4.9124 \mathrm{e}-160$ | $9.4075 \mathrm{e}-169$ | $2.3117 \mathrm{e}-98$ | $5.4748 \mathrm{e}-96$ | 5.4748e-96 | 3.0303e-170 |
| 14 | Cross-in-Tray function | 2.9415e-190 | $6.3621 \mathrm{e}-190$ | $9.4571 \mathrm{e}-165$ | 2.9144e-118 | 1.6057e-167 | $4.4898 \mathrm{e}-185$ | $8.7420 \mathrm{e}-20$ | 7.1009e-30 |
| 15 | McCormick function | 4.8145e-208 | $7.9734 \mathrm{e}-199$ | 2.4157e-205 | 2.7981e-185 | $1.7211 \mathrm{e}-193$ | 3.8569e-208 | $1.5483 \mathrm{e}-54$ | 1.6457e-188 |
| 16 | Gramacy and Lee function | 5.0302e-214 | $1.1779 \mathrm{e}-213$ | 1.7334e-200 | 2.6517e-189 | 2.1106e-212 | 1.5681e-192 | $2.3659 \mathrm{e}-191$ | 3.2889e-191 |
| 17 | Testtubeholder function | $1.3355 \mathrm{e}-161$ | 2.0663e-138 | $1.4054 \mathrm{e}-120$ | 6.2333e-26 | $2.0588 \mathrm{e}-151$ | 1.2910e-163 | $1.4419 \mathrm{e}-48$ | 9.7121e-15 |
| 18 | Shubert function | $7.8405 \mathrm{e}-182$ | 4.1448e-96 | 2.8226e-121 | 3.6690e-18 | 5.0688e-103 | 1.7861e-161 | 4.6324e-105 | 1.9701e-164 |
| 19 | price 2 function | $5.8287 \mathrm{e}-19$ | $2.4336 \mathrm{e}-06$ | $1.7689 \mathrm{e}-07$ | $2.1156 \mathrm{e}-119$ | $1.6710 \mathrm{e}-31$ | $1.1040 \mathrm{e}-24$ | $3.8123 \mathrm{e}-70$ | 3.1442e-18 |
| 20 | Dejong5 | $1.7349 \mathrm{e}-183$ | $6.1675 \mathrm{e}-188$ | $2.6969 \mathrm{e}-179$ | $7.4328 \mathrm{e}-178$ | $3.8529 \mathrm{e}-175$ | 5.8155e-177 | $4.8973 \mathrm{e}-178$ | 3.7030e-182 |

Table 6 Best, average, and STD results of COVIDOA and the state-of-the-art algorithms for CEC benchmark functions

| Problem | Metric | Algorithm |  |  |  |  |  |  |  |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
|  |  | GA [26] | DE [63] | PSO [44] | FPA [75] | GWO [51] | WOA [50] | CHIO [4] | SOA [19] | Proposed COVIDOA |
| CEC01 | Best | $4.79 \mathrm{e}+07$ | $8.067 \mathrm{e}+09$ | $2.130 \mathrm{e}+08$ | $2.525 \mathrm{e}+09$ | $6.58 \mathrm{e}+06$ | $4.585 \mathrm{e}+09$ | $7.011 \mathrm{e}+06$ | $7.35 \mathrm{e}+10$ | $1.25 \mathrm{e}+06$ |
|  | AVG | $7.767 \mathrm{e}+09$ | $3.648 \mathrm{e}+10$ | $4.108 \mathrm{e}+09$ | $3.4008 \mathrm{e}+10$ | $4.260 \mathrm{e}+09$ | $1.623 \mathrm{e}+10$ | $2.2465 \mathrm{e}+11$ | $1.294 \mathrm{e}+11$ | $1.044 \mathrm{e}+09$ |
|  | STD | $3.649 \mathrm{e}+10$ | $3.729 \mathrm{e}+10$ | $1.394 \mathrm{e}+10$ | $8.531 \mathrm{e}+10$ | $4.8333 \mathrm{e}+10$ | $5.6522 \mathrm{e}+10$ | $1.3991 \mathrm{e}+11$ | $1.755 \mathrm{e}+11$ | $6.249 \mathrm{e}+09$ |
| CEC03 | Best | 12.7024 | 12.7024 | 12.7024 | 12.7024 | 12.7024 | 12.7024 | 12.7024 | 12.7024 | 12.7024 |
|  | AVG | 12.7024 | 12.7025 | 12.7024 | 12.7026 | 12.7024 | 12.7024 | 12.7025 | 12.7028 | 12.7025 |
|  | STD | $1.8779 \mathrm{e}-04$ | $2.3779 \mathrm{e}-04$ | 4.8999e-05 | $3.7993 \mathrm{e}-04$ | 1.8226e-04 | $1.0041 \mathrm{e}-04$ | $2.5001 \mathrm{e}-04$ | 5.063e-04 | $9.8359 \mathrm{e}-05$ |
| CEC06 | Best | 10.0164 | 7.7598 | 8.5145 | 9.4978 | 9.2790 | 7.7528 | 9.3672 | 8.0529 | 7.6402 |
|  | AVG | 10.7198 | 8.7656 | 9.7656 | 9.7070 | 9.5928 | 8.6969 | 9.6018 | 9.2519 | 8.6512 |
|  | STD | 0.6542 | 8.6156 | 0.7421 | 0.5951 | 0.5048 | 1.2646 | 0.6372 | 0.8336 | 0.4291 |
| ECE07 | Best | 296.0888 | 165.6218 | 242.9147 | 176.8028 | 305.1 | 546.7268 | 277.5 | 317.7 | 276.0837 |
|  | AVG | 409.9065 | 265.9382 | 388.3867 | 334.7019 | 461.5165 | 570.3746 | 316.4750 | 566.4644 | 376.4779 |
|  | STD | 231.6249 | 186.9450 | 266.6071 | 159.2303 | 168.3036 | 176.3487 | 119.4227 | 170.8287 | 163.8042 |
| CEC10 | Best | 20.1179 | 20.0925 | 20.1074 | 20.3277 | 20.3589 | 20.0006 | 20.2471 | 20.1112 | 19.4927 |
|  | AVG | 20.4208 | 20.1859 | 20.2848 | 20.3669 | 20.3789 | 20.0226 | 20.3975 | 20.2414 | 19.4976 |
|  | STD | 0.0823 | 0.1245 | 0.1128 | 0.0686 | 0.0697 | 0.0863 | 0.0933 | 0.1412 | 0.0574 |

Table 7 P values computed by Wilcoxon's rank-sum test compared the COVIDOA with other algorithms for CEC benchmark functions

| Problem | Algorithm |  |  |  |  |  |  |  |
| :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- |
|  | COVIDOA | COVIDOA | COVIDOA | COVIDOA <br> vs. FPA | COVIDOA vs. <br> GWO | COVIDOA vs. <br> Gs. GA | vs. DE | vs. PSO |

Table 8 Scenarios of the tuning parameters

| Scenario | Parameters |  |
| :--- | :--- | :--- |
|  | MR | numOfProtiens |
| 1 | 0.1 | 2 |
| 2 | 0.01 | 2 |
| 3 | 0.001 | 2 |
| 4 | 0.1 | 4 |
| 5 | 0.01 | 4 |
| 6 | 0.001 | 4 |
| 7 | 0.1 | 6 |
| 8 | 0.01 | 6 |
| 9 | 0.001 | 6 |

For testing COVIDOA on CEC real-world problems, we obtain our results over 500 iterations. The proposed and state-of-the-art algorithms were run 25 independent times as suggested by IEEE-CEC 2011 Competition [16]. Table 10 and Fig. 14 show the results of the selected CEC real-world problems. The proposed algorithm achieves the optimum best cost, average cost, and STD values for all five selected problems.

Although the general steps of COVIDOA and other evolutionary algorithms, such as GA and DE, are very similar, COVIDOA is superior to them, as shown in Tables $1,2,3,4,5,6,7,8,9$ and 10 . This progress is caused by the additional step proposed in the replication phase of COVIDOA, the frameshifting technique. Adding frameshifting technique in the replication process helps

Table 9 The impact of COVIDOA parameters (MR, a numOfProtiens) on IEEE CEC problems

| Problem | Metric | Scenario 1 | Scenario 2 | Scenario 3 | Scenario 4 | Scenario 5 | Scenario 6 | Scenario 7 | Scenario 8 | Scenario 9 |
| :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- |
| CEC01 | Best | $8.41 \mathrm{e}+07$ | $1.93 \mathrm{e}+08$ | $4.84 \mathrm{e}+08$ | $\mathbf{7 . 2 2 e}+\mathbf{0 6}$ | $8.94 \mathrm{e}+08$ | $4.36 \mathrm{e}+08$ | $6.64 \mathrm{e}+08$ | $6.31 \mathrm{e}+08$ | $6.10 \mathrm{e}+08$ |
|  | AVG | $6.90 \mathrm{e}+09$ | $7.34 \mathrm{e}+09$ | $5.21 \mathrm{e}+09$ | $\mathbf{6 . 1 5 e}+\mathbf{0 8}$ | $4.82 \mathrm{e}+09$ | $4.47 \mathrm{e}+09$ | $1.03 \mathrm{e}+10$ | $9.49 \mathrm{e}+09$ | $6.44 \mathrm{e}+09$ |
|  | STD | $1.75 \mathrm{e}+10$ | $2.38 \mathrm{e}+10$ | $1.51 \mathrm{e}+10$ | $1.99 \mathrm{e}+10$ | $1.80 \mathrm{e}+10$ | $\mathbf{1 . 2 0 e}+\mathbf{1 0}$ | $3.22 \mathrm{e}+10$ | $4.06 \mathrm{e}+10$ | $1.79 \mathrm{e}+10$ |
| CEC03 | Best | $\mathbf{1 2 . 7 0 2 4}$ | $\mathbf{1 2 . 7 0 2 4}$ | $\mathbf{1 2 . 7 0 2 4}$ | 12.7025 | 12.7025 | 12.7025 | 12.7025 | 12.7025 | 12.7025 |
|  | AVG | $\mathbf{1 2 . 7 0 2 5}$ | $\mathbf{1 2 . 7 0 2 5}$ | $\mathbf{1 2 . 7 0 2 5}$ | $\mathbf{1 2 . 7 0 2 5}$ | 12.7026 | 12.7026 | $\mathbf{1 2 . 7 0 2 5}$ | 12.7026 | 12.7026 |
|  | STD | $2.08 \mathrm{e}-04$ | $\mathbf{8 . 3 4 e - 0 5}$ | $1.26 \mathrm{e}-04$ | $2.91 \mathrm{e}-04$ | $3.03 \mathrm{e}-04$ | $2.17 \mathrm{e}-04$ | $1.60 \mathrm{e}-04$ | $1.14 \mathrm{e}-04$ | $2.29 \mathrm{e}-04$ |
| CEC06 | Best | $\mathbf{7 . 6 4 0 2}$ | 9.0038 | 9.3928 | 9.0148 | 8.344 | 7.7169 | 8.8126 | 8.7189 | 9.1483 |
|  | AVG | $\mathbf{8 . 6 5 1 2}$ | 9.7509 | 9.9594 | 9.4252 | 8.9131 | 9.2187 | 8.8800 | 9.2262 | 9.6000 |
|  | STD | $\mathbf{0 . 4 2 9 1}$ | 1.0948 | 0.9469 | 0.5378 | 0.8895 | 1.2194 | 0.4741 | 0.7438 | 0.5159 |
| ECE07 | Best | 429.593 | 467.8152 | 525.5403 | $\mathbf{2 7 6 . 0 8 3 7}$ | 388.5537 | 508.3128 | 455.5922 | 560.6439 | 404.9701 |
|  | AVG | $\mathbf{4 7 8 . 6 8 1 2}$ | 600.8125 | 699.5776 | 493.5525 | 460.4821 | 640.0468 | 468.0766 | 719.8709 | 521.5527 |
|  | STD | 135.422 | 139.3537 | 101.7200 | 202.0033 | 137.9164 | 157.4621 | $\mathbf{8 7 . 5 6 6 0}$ | 145.9606 | 218.8682 |
| CEC10 | Best | $\mathbf{1 9 . 3 9 0 1}$ | 20.241 | 20.3035 | 20.301 | 20.104 | 20.2851 | 20.3317 | 20.2618 | 20.2906 |
|  | AVG | $\mathbf{2 0 . 1 4 9 1}$ | 20.3671 | 20.3797 | 20.3672 | 20.2833 | 20.3194 | 20.3450 | 20.3261 | 20.3269 |
|  | STD | 0.2631 | 0.0939 | 0.0591 | $\mathbf{0 . 0 4 7 8}$ | 0.1631 | 0.0615 | 0.0531 | 0.1012 | 0.0788 |

Table 10 The best, average, and STD results of COVIDOA and the state-of-the-art algorithms for CEC 2011 real-world problems

| Problem | Meric | Algorithms |  |  |  |  |  |  |  |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
|  |  | GA [26] | DE [63] | PSO [44] | FPA [75] | $\begin{aligned} & \text { GWO } \\ & \text { [51] } \end{aligned}$ | WOA [50] | CHIO [4] | SOA [19] | COVIDOA |
| Lennard-Jones Potential Problem | Best | -1 | - 1 | -1 | - 1 | - 1 | - 1 | - 1 | - 1 | -1 |
|  | AVG | -0.9984 | -0.9949 | -0.9999 | -0.9968 | -0.9967 | -0.9996 | $-0.9998$ | -0.9953 | -1 |
|  | STD | 0.0177 | 0.0461 | 0.0019 | 0.0409 | 0.0516 | 0.0087 | $5.7843 \mathrm{e}-04$ | 0.0549 | 4.8460-07 |
| Spread spectrum radar polyphase problem | Best | 0.5 | 0.5 | 0.5 | 0.5 | 0.5 | 0.5 | 0.5 | 0.5 | 0.5 |
|  | AVG | 0.5004 | 0.5 | 0.5 | 0.5014 | 0.5003 | 0.5007 | 0.5 | 0.5002 | 0.5 |
|  | STD | 0.0056 | 0 | 0 | 0.0096 | 0.0040 | 0.0094 | 0 | 0.0018 | 0 |
| Tersoff Potential function Minimization Problem for model $\mathrm{Si}(\mathrm{B})$ | Best | - 2.6237 | - 2.6237 | - 2.6237 | - 2.6237 | - 2.6237 | - 2.6237 | - 2.6237 | - 2.6237 | - 2.6237 |
|  | AVG | - 2.6237 | - 2.6237 | - 2.6237 | - 2.6235 | - 2.6236 | -2.6237 | - 2.6228 | - 2.6236 | - 2.6237 |
|  | STD | 1.3471e-05 | $1.5074 \mathrm{e}-04$ | $3.3914 \mathrm{e}-05$ | 0.0036 | 0.0016 | $2.5855 \mathrm{e}-04$ | 0.0145 | $2.3704 \mathrm{e}-04$ | 2.7394e-07 |
| Tersoff Potential function Minimization Problem for model $\mathrm{Si}(\mathrm{C})$ | Best | - 2.666 | - 2.666 | - 2.666 | - 2.666 | - 2.6660 | - 2.6660 | - 2.6660 | - 2.666 | - 2.666 |
|  | AVG | -2.6660 | -2.6660 | - 2.6660 | - 2.6660 | - 2.6656 | $-2.6660$ | - 2.6654 | - 2.6660 | $-2.6660$ |
|  | STD | 1.8503e-05 | 5.0644es- 04 | 6.2625e-06 | $2.8149 \mathrm{e}-05$ | 0.0068 | 7.0142e-05 | 0.0088 | $2.0518 \mathrm{e}-06$ | 5.8070--07 |
| Transmission Network Expansion Planning (TNEP) problem | Best | 435 | 435 | 435 | 435 | 435 | 442 | 442 | 442 | 435 |
|  | AVG | 435.0640 | 435.4125 | 435.0740 | 440.3519 | 441.4249 | 442.4413 | 478.2145 | 435.6794 | 435 |
|  | STD | 0.7134 | 2.5585 | 1.6547 | 32.7886 | 21.9935 | 9.8685 | 13.7593 | 3.7615 | 0 |

COVIDOA update solutions in each generation, helping to reach global optimum rapidly.

### 3.3 Explorations and exploitation capabilities of COVIDOA

It is essential to test the efficiency of the proposed algorithm. In other words, it is necessary to test its exploration and exploitation capabilities. In exploration, the algorithm searches for new solutions in new regions, while exploitation means using existing solutions and improving their fitness [21]. Mutation and crossover steps in COVIDOA are used to create new solutions, so they are methods to explore the problem space. On the other hand, selecting an existing parent virus and applying the frameshifting technique to produce new children represents the exploitation of the current solution features. Unimodal test functions F1, F7, F10, and F13 can evaluate the exploitation feature because they have only one global optimum solution. Multimodal functions F2, F3, F4, and F5 can help assess the exploration capability of COVIDOA because they have many optimum solutions.

### 3.4 Convergence of COVIDOA

In Table 4, the convergence speed of COVIDOA and the other algorithms for the classical benchmark functions are classified into three groups: Fast, Moderate, and Low, where algorithms that reach the minimum cost in the first 100 iterations are classified as fast convergence algorithms, those that get the minimum cost from iteration 100 to 300 are moderate convergence algorithms, and the others classified as slow convergence algorithms. As shown in Table 5 and Fig. 13, the proposed algorithm has fast convergence in the majority ( 16 from 20 ) of the test problems
and moderate in the others. In contrast, other state-of-theart algorithms may slow the test problems' convergence.

Overall results reveal that COVIDOA reaches the minimum best cost, average cost, and standard deviation in most test problems. It also has high exploration and exploitation capabilities and a high convergence speed during iterations.

## 4 Conclusion

A novel evolutionary optimization algorithm (COVIDOA) inspired by the replication lifecycle of SARS-CoV-2 is presented. The proposed COVIDOA was tested by solving 20 classical benchmark problems, five CEC benchmark test functions, and five CEC 2011 real-world problems. The proposed COVIDOA is compared with the state-of-the-art nature-inspired optimization algorithms in terms of best cost, average cost, standard deviation, and convergence speed. The proposed algorithm is implemented using MATLAB R2016a software, and the source code of the state-of-the-art algorithms and the benchmark problems are downloaded from the mathworks.com website. The experimental results proved that the proposed algorithm outperforms the state-of-the-art optimization algorithms in most test problems and has very close results to other algorithms in the rest of the test problems. COVIDOA has high exploitation and exploration capabilities and convergence speed compared to other metaheuristics.

Future work may include the implementation of COVIDOA in solving large-scale problems in different fields.

## Appendix

See Tables 11 and 12.
Table 11 Description of classical benchmark functions

| Function | Formula | Dimension (D) | Range | Global optimum cost | Properties |
| :---: | :---: | :---: | :---: | :---: | :---: |
| Dixon- price function | $F_{1}(x)=\left(x_{1}-1\right)^{2}+\sum_{i=2}^{d} i\left(2 x_{i}^{2}-x_{i-1}\right)^{2}$ | D | $\begin{aligned} & X_{i} \in \\ & {[-10,10],} \\ & \text { for all } \\ & i=1, \ldots, d \end{aligned}$ | 0 | Unimodal nD function |
| Happy Cat function | $\begin{aligned} F_{2}(x)= & {\left[\left(x^{2}-n\right)^{2}\right]^{\alpha} } \\ & +\frac{1}{n}\left(\frac{1}{2} x^{2}+\sum_{i=1}^{n} x_{i}\right)+\frac{1}{2} \end{aligned}$ <br> Where $\alpha=\frac{1}{8}$ | D | $\begin{aligned} & X_{i} \in \\ & {[-2,2],} \\ & \text { for all } \\ & i=1, \ldots, d \end{aligned}$ | 0 | Multimodal nD function |
| Cross-Leg Table function | $F_{3}(\mathrm{x})=\frac{1}{\left(\left.\left\|\sin \left(x_{1}\right) \sin \left(x_{2}\right)\right\| e^{\left\lvert\, \log \frac{\sqrt{x_{1}^{2}+x_{2}^{2}}}{\frac{1}{2}}\right.}\right\|_{+1}\right)^{0.1}}$ | 2 | $\begin{aligned} & X_{i} \in \\ & {[-10,10],} \\ & i=1,2 \end{aligned}$ | - 1 | Multimodal 2D function |
| Eggholder function | $F_{4}(x)=-\left(x_{2}+47\right) \sin \left(\sqrt{\left\|x_{2}+\frac{x_{1}}{2}+47\right\|}\right)-x_{1} \sin \left(\sqrt{\left\|x_{1}-x_{2}+47\right\|}\right)$ | 2 | $\begin{aligned} & X_{i} \in \\ & {[-5.12,5.12],} \\ & i=1,2 \end{aligned}$ | - 959.6407 | Multimodal 2D function |
| Alpine N. 2 function | $F_{5}(x) \prod_{i=1}^{n} \sqrt{x_{i}} \sin \left(x_{i}\right)$ | D | $\begin{aligned} & X_{i} \in \\ & {[0,10],} \\ & \text { for all } i=1, d \end{aligned}$ | $2.808^{\text {d }}$ | Multimodal nD function |
| Styblinski-tang function | $F_{6}(\mathrm{x})=\frac{1}{2} \sum_{i=1}^{d}\left(x_{i}^{4}-16 x_{i}^{2}+5 x_{i}\right)$ | D | $\begin{aligned} & X_{i} \in \\ & {[-5,5],} \\ & \text { for all } \\ & i=1, \ldots, d \end{aligned}$ | - 39,16599d | Multimodal nD function |
| Schwefel function | $F_{7}(x)=418.9829-\sum_{i=1}^{d} x_{i} \sin \left(\sqrt{\left\|x_{i}\right\|}\right)$ | D | $\begin{aligned} & x_{i} \in \\ & {[-500,500],} \\ & \text { for all } \\ & i=1, \ldots, d \end{aligned}$ | 0 | Unimodal nD function |
| Keane function | $F_{8}(x)=\frac{\sin ^{2}\left(x_{1}-x_{2}\right) \sin ^{2}\left(x_{1}+x_{2}\right)}{\sqrt{x_{1}^{2}+x_{2}^{2}}}$ | 2 | $\begin{aligned} & x_{i} \in \\ & {[0,10],} \\ & i=1,2 \end{aligned}$ | 0.6736675 | Multimodal 2D function |

Table 11 (continued)

| Function | Formula | Dimension (D) | Range | Global optimum cost | Properties |
| :---: | :---: | :---: | :---: | :---: | :---: |
| Trid function | $F_{9}(x)=\sum_{i=1}^{d}\left(x_{i}-1\right)^{2}-\sum_{i=2}^{d} x_{i} x_{i-1}$ | D | $\begin{aligned} & x_{i} \in \\ & {\left[-d^{2}, d^{2}\right],} \end{aligned}$ <br> for all $i=1, \ldots, d$ | $\frac{-d(d+4)(d-1)}{6}$ | Multimodal nD function |
| Schaffer function n. 4 | $F_{10}(x)=0.5+\frac{\cos ^{2}\left(\sin \left(\left\|x_{1}^{2}-x_{2}^{2}\right\|\right)\right)-0.5}{\left(1+0.001\left(x_{1}^{2}+x_{2}^{2}\right)\right)^{2}}$ | 2 | $\begin{aligned} & x_{i} \in \\ & {[-100,100],} \\ & i=1,2 \end{aligned}$ | 0.292579 | Unimodal 2D function |
| Branin function | $\begin{aligned} F_{11}(x)= & a\left(x_{2}-b x_{1}^{2}+c x_{1}-r\right)^{2} \\ & +\mathrm{s}(1-\mathrm{t}) \cos \left(\mathrm{x}_{1}\right)+\mathrm{s} \end{aligned}$ <br> The recommended values of $\mathrm{a}, \mathrm{b}, \mathrm{c}, \mathrm{r}, \mathrm{s}$ and t are: $\begin{aligned} & \mathrm{a}=1, \mathrm{~b}=5.1 /(4 \pi 2), \mathrm{c}=5 / \pi, \mathrm{r}=6, \mathrm{~s}=10 \\ & \text { and } \mathrm{t}=1 /(8 \pi) \end{aligned}$ | 2 | $\begin{aligned} & x_{1} \in \\ & {[-5,10],} \\ & x_{2} \in \\ & {[0,15]} \end{aligned}$ | 0.397887 | Multimodal 2D function |
| Wolfe function | $F_{12}(x, y, z)=\frac{4}{3}\left(x^{2}+y^{2}-x y\right)^{0.75}+z$ | 3 | $\begin{aligned} & x_{i} \in \\ & {[-65.536,} \\ & 65.536], \\ & i=1,2 \end{aligned}$ | 0.998 | Multimodal 2D function |
| Zettl function | $F_{13}(x)=\left(x_{0}^{2}+x_{1}^{2}-2 x_{0}\right)^{2}+0.25 x_{0}$ | 2 | $\begin{aligned} & x_{i} \in \\ & {[-5,5]} \\ & i=1,2 \end{aligned}$ | - 0.003791 | Unimodal 2D function |
| Cross-in-Tray function | $F_{14}(x)=0.0001\left(\left\|\sin \left(x_{1}\right) \sin \left(x_{2}\right) \exp \left(\left\|100-\frac{\sqrt{x_{1}^{2}+x_{2}^{2}}}{\pi}\right\|\right)\right\|+1\right)^{0.1}$ | 2 | $\begin{aligned} & x_{i} \in \\ & {[-10,10],} \\ & i=1,2 \end{aligned}$ | - 2.06261 | Multimodal 2D function |
| McCormick function | $\begin{aligned} F_{15}(x)= & \sin (x+y)+(x-y)^{2} \\ & -1.5 x+2.5 y+1 \end{aligned}$ | 2 | $\begin{aligned} & x_{1} \in \\ & {[-1.5,4],} \\ & \text { And } \\ & x_{2} \in \\ & {[-3,3]} \end{aligned}$ | - 1.9133 | Multimodal 2D function |

Table 11 (continued)

| Function | Formula | Dimension (D) | Range | Global optimum cost | Properties |
| :---: | :---: | :---: | :---: | :---: | :---: |
| Gramacy and Lee function | $F_{16}(x)=\sin \frac{10 \pi x}{2 x}+(x+1)^{4}$ | 1 | $\begin{aligned} & x \in \\ & {[-0.5,2.5]} \end{aligned}$ | -0.8690111349 | Multimodal 1D function |
| Test tube holder function | $F_{17}(x)=-4\left[\left(\sin (x 1) \cos (x 2) e^{\left\|\cos \left[\left(x_{1}^{2}+x_{2}^{2} / 200\right)\right]\right\|}\right)\right]$ | 2 | $\begin{aligned} & x_{i} \in \\ & {[-10,10],} \\ & i=1,2 \end{aligned}$ | - 10.872300 | Multimodal 2D function |
| Shubert function | $\begin{aligned} F_{18}(x) & =\left(\sum_{i=1}^{5} \alpha_{i} i \cos \left((i+1) x_{1}+i\right)\right) \\ & \left(\sum_{i=1}^{5} \alpha_{i} i \cos \left((i+1) x_{2}+i\right)\right) \end{aligned}$ | 2 | $\begin{aligned} & x_{i} \in \\ & {[-10,10],} \\ & i=1,2 \end{aligned}$ | - 186.7309 | Multimodal nD function |
| Price 2 function | $F_{19}(x)=1+\sin ^{2}\left(x_{1}\right)+\sin ^{2}\left(x_{2}\right)-0.1 e^{-x_{1}^{2}-x_{2}^{2}}$ | 2 | $\begin{aligned} & x_{i} \in \\ & {[-10,10],} \\ & i=1,2 \end{aligned}$ | 0.9 | Multimodal 2D function |
| De Jong function n. 5 | $\left.\begin{array}{l} F_{20}(x)=\left(0.002 \sum_{i=1}^{25} \frac{1}{i+\left(x_{1}+a_{i j}\right)^{\circ}+\left(x_{2}+a_{2 i}\right)^{6}}\right)^{-1}, \text { where } \\ a=\left(\begin{array}{cccccccc} -32 & -16 & 0 & 16 & 32 & -32 & 0 & 16 \\ -32 & -32 & -32 & -32 & -32 & -16 & 32 & 32 \end{array}\right. \\ 32 \end{array}\right) .$ | 2 | $\begin{aligned} & x_{i} \in \\ & {[-65.53665 .536],} \\ & i=1,2 \end{aligned}$ | 0 | Multimodal 2D function |

Table 12 Description of CEC benchmark functions

| No. | Function | Dimension | range | Global minimum |
| :--- | :--- | :--- | :--- | :--- |
| CEC01 | Storn's chebychev polynomial fitting problem | 9 | $[-8192,8192]$ | 1 |
| CEC03 | Lennard-Jones minimum energy cluster | 18 | $[-4,4]$ | 1 |
| CEC06 | Weierstrass function | 10 | $[-100,100]$ | 1 |
| CEC07 | Modified Shwefel function | 10 | $[-100,100]$ | 1 |
| CEC10 | Ackley function | 10 | $[-100,100]$ | 1 |

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Conflict of interest The authors declare that they have no conflict of interest.

Ethical approval This article does not contain any studies with human participants performed by any authors.

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