Evidence for Weak Selective Constraint on Human Gene Expression

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ABSTRACT Gene expression variation is a major contributor to phenotypic variation in human complex traits. Selection on complex traits may therefore be reflected in constraint on gene expression. Here, we explore the effects of stabilizing selection on *cis*-regulatory genetic variation in humans. We analyze patterns of expression variation at copy number variants and find evidence for selection against large increases in gene expression. Using allele-specific expression (ASE) data, we further show evidence of selection against smaller-effect variants. We estimate that, across all genes, singletons in a sample of 122 individuals have $\sim 2.2 \times$ greater effects on expression variation than the average variant across allele frequencies. Despite their increased effect size relative to common variants, we estimate that singletons in the sample studied explain, on average, only 5% of the heritability of gene expression from *cis*-regulatory variants. Finally, we show that genes depleted for loss-of-function variants are also depleted for *cis*-eQTLs and have low levels of allelic imbalance, confirming tighter constraint on the expression levels of these genes. We conclude that constraint on gene expression is present, but has relatively weak effects on most *cis*-regulatory variants, thus permitting high levels of gene-regulatory genetic variation.

KEYWORDS Gene expression; Allele-specific expression; Stabilizing selection; Heritability

ARIATION in human complex traits is connected to variation in gene expression (Nicolae *et al.* 2010; Giambartolomei *et al.* 2014; Gusev *et al.* 2014, 2016; Gamazon *et al.* 2015; Hormozdiari *et al.* 2016; Boyle *et al.* 2017). Selection on complex traits (*e.g.*, complex disease) may therefore be reflected in selection on gene expression levels.

Across species, gene expression has been shown to evolve more slowly than expected under a neutral model (Chan *et al.* 2009; Brawand *et al.* 2011; Khan *et al.* 2013; Chen *et al.* 2018). An analysis of mammalian gene duplications also showed that the total expression of gene pairs in species that experienced a duplication event is similar to the expression of the corresponding single gene copy in species without duplication (Lan and Pritchard 2016). As a duplication event would be expected to dramatically increase gene expression, this suggests that stabilizing selection on gene expression may act to return the total expression of duplicate gene pairs to an optimal expression level.

Constraint on gene expression has also been shown to influence patterns of genetic variation within humans. First, some genes are unusually depleted for loss-of-function and copy number variants (CNVs) (Lek *et al.* 2016; Ruderfer *et al.* 2016). These genes are thought to be particularly constrained with respect to their expression levels.

Further, individuals with extreme expression levels for a particular gene are more likely to have rare variants in *cis* than individuals with average expression (Li *et al.* 2014, 2017; Zeng *et al.* 2015; Zhao *et al.* 2016). This suggests that large expression changes are associated with rare genetic variation. As detailed below, this is consistent with stabilizing selection acting against large-effect regulatory variants.

Despite this evidence for constraint on expression, humans exhibit substantial variation in gene expression and possess many common gene regulatory variants (Gaffney *et al.* 2012;

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Battle *et al.* 2014; GTEx Consortium 2017). It is therefore of interest to characterize constraint on gene expression and its effects on regulatory variation across the human genome.

Under a model of stabilizing selection, the negative fitness effect of a *cis*-regulatory variant increases with its effect on expression. In other words, as large-effect variants move individuals further from an optimal gene expression value, selection acts against them, keeping them more rare than those with small effects or no effect on expression. This reduces the variance in gene expression and creates a global relationship between the allele frequencies and effect sizes of regulatory variants [Figure 1; see Simons *et al.* (2018) for a detailed model of stabilizing selection, genetic variation, and complex trait variance].

This model of stabilizing selection is consistent with observed patterns of gene-regulatory variation. Past studies have noted a relationship between the allele frequencies and effect sizes of expression quantitative trait loci (eQTLs) [Battle *et al.* 2014, but see Tung *et al.* (2015) for a nonselective explanation for this relationship]. More recently, polygenic models have shown a relationship between allele frequency and the variance in gene expression explained by trait-associated variants (Hernandez *et al.* 2017; Zeng *et al.* 2018). However, the strength and breadth of this selection across genes have yet to be quantified.

Here, we test whether patterns of regulatory variation are consistent with human gene expression evolving under stabilizing selection. We analyze gene expression and genetic variation related to CNVs, eQTLs, and allele-specifically expressed (ASE) transcripts. Together, these data show that, although constraint on expression affects variation in gene expression and in regulatory genetic variation, its effects are relatively weak.

Materials and Methods

Genotypes and relative expression of CNVs

We identified loci containing CNVs in healthy individuals, as well as the number of gene copies per locus per individual, by applying LUMPY (Layer *et al.* 2014) and Genome STRiP (Handsaker *et al.* 2011) to whole blood RNA sequencing data from version 4 of the Genotype Tissue Expression Project (GTEx) (GTEx Consortium 2017). Only CNVs containing an entire protein coding sequence were retained for downstream analysis. We obtained gene expression (RPKM) measurements for each CNV in each individual across 12 tissues.

eQTL mapping

We obtained genotype and RNA sequencing data from 922 European individuals included in the Depression Genes and Networks (DGN) dataset (Battle *et al.* 2014; Mostafavi *et al.* 2014). Genotypes were imputed to 1000 Genomes as described in Kukurba *et al.* (2016). We then polarized genotypes relative to the human ancestral allele.

A Effects of stabilizing selection



Figure 1 Expected signals of stabilizing selection on gene expression. (A) Effects of stabilizing selection. (B) Phenotypic variation. (C) Regulatory variation.

To determine the human ancestral allele, we compared the human major allele to the human-chimp ancestral allele. We obtained human major alleles from the 1000 Genomes dataset (1000 Genomes Project Consortium *et al.* 2015) and inferred the human-chimp ancestral allele from Ensembl multiple alignments using Ortheus (Paten *et al.* 2008).

At SNPs for which the human major allele and the humanchimp ancestral allele agree, we defined the human ancestral allele as the agreeing allele. At SNPs for which the human major allele and human-chimp ancestral allele disagree and the human minor allele is rare (<5% frequency), we defined the human ancestral allele as the human major allele. At SNPs for which the human major allele and human-chimp ancestral allele disagree and the human minor allele is common (>5% frequency), we defined the human ancestral allele as the human-chimp ancestral allele. At SNPs that lacked data regarding the human-chimp ancestral allele, we defined the human ancestral allele as the human major allele.

We considered SNPs with minor allele frequency >1% within a 100 kb window centered on the most upstream annotated transcription start site (TSS) to be candidate *cis*-eQTLs for the corresponding gene. TSSs, as annotated in Ensembl, were obtained using biomaRt (Kinsella *et al.* 2011).

To obtain comparable gene expression measurements across individuals, we normalized read counts at each gene by the total reads sampled per individual, and \log_2 transformed the resulting measurement.

To allow multiple independent eQTLs per gene, we mapped eQTLs using forward stepwise regression. For a detailed treatment of the challenges introduced by multiple regulatory variants per locus, see Zeng *et al.* (2017).

If any SNPs were significantly associated with gene expression ($\alpha = 0.05$ after Bonferroni correction for the original number of candidate eQTLs for the gene), the most significantly associated SNP was added to the model. All SNPs in linkage ($r^2 > 0.8$) with the newly called eQTL were excluded from the list of candidate eQTLs. This model selection procedure was repeated until no significantly associated SNPs remained.

Modeling the contribution of cis-regulatory variants to ASE

In general, ASE is measured by comparing reads expressed from each allele at a particular locus within an individual. This relies on a heterozygous site within a transcript that can be used to identify the allelic origin of each read.

We first sought to define a metric of ASE that is robust to variation in read depth across sites and agnostic to the direction of allelic bias (excess of reads from the reference or alternative allele). Here, we model allele specific expression of the *g*th locus in the *i*th individual as a squared Z-score of reads containing the alternative allele ($Z^2_{ALT;i,g}$). Under a null model in which read counts follow a Binomial

Under a null model in which read counts follow a Binomial distribution,

$$A_{i,g} \sim \operatorname{Binom}(N_{i,g}, p).$$
 (1)

 $A_{i,g}$ is the number of sampled reads containing the alternative allele, *p* is the underlying proportion of reads that contain the alternative allele, and $N_{i,g}$ is the total number of reads sampled at the locus. The expected number of sampled reads containing the alternative allele is, then,

$$\mathbf{E}[A_{i,g}] = \mathbf{E}[p] \times N_{i,g}.$$
 (2)

In the absence of locus- and allele-specific *cis*-regulation, the expected proportion of reads expressed from the alternative allele is 0.5. However, due to reference mapping bias, the observed proportion of reads from the alternative allele will be slightly lower. This ratio (\hat{p}) was estimated empirically using global reference bias.

$$\hat{p} = \frac{\sum_{(i,g)\in(I,G)} A_{i',g'}}{\sum_{(i,g)\in(I,G)} N_{i',g'}}.$$
(3)

where (I, G) is the set of individual-gene pairs at which we measured ASE. The variance in alternative allele counts is, therefore,

$$\operatorname{Var}[A_{i,g}] = \hat{p}(1-\hat{p}) \times N_{i,g}.$$
(4)

Our ASE statistic is, therefore,

$$Z_{\text{ALT};i,g}^{2} = \frac{\left(A_{i,g} - \mathbb{E}[A_{i,g}]\right)^{2}}{\text{Var}[A_{i,g}]} = \frac{\left(A_{i,g} - (\hat{p} \times N_{i,g})\right)^{2}}{\hat{p}(1 - \hat{p}) \times N_{i,g}}.$$
 (5)

To explore the relationship between ASE and locus-specific regulatory variation, we allow the underlying proportion of

alternative-allele reads to vary across ASE sites. Thus far, we assumed that the underlying proportion of alternative-allele reads at all loci is determined by reference bias alone. We therefore extended our model with the assumption that, within an individual, any heterozygous site in *cis* to an ASE site can alter expression across haplotypes and contribute to allelic imbalance.

Specifically, in each individual *i* at each locus *j*, we assumed the underlying proportion of reads containing the alternative allele $(p_{i,g})$ to be Beta distributed. The mean proportion of alternative allele reads is determined by reference bias, as described above. However, we modeled the variance in the proportion of reads expressed from the alternative allele across individuals as a function of the number of heterozygous sites in *cis* to each measured ASE site.

$$p_{i,g} \sim \text{Beta}(\hat{p}, \sigma_{\text{HET}}^2 \times n_{\text{HET};i,g} + v_p).$$
 (6)

 σ_{HET}^2 is the variance in the proportion of alternative allelereads contributed by a *cis*-heterozygous site, $n_{\text{HET};i,g}$ is the number of *cis*-heterozygous sites at the *g*th locus in the *i*th individual, and v_p is the variance in the proportion of reads expressed from each allele contributed by factors other than *cis*-genetic variation. This could represent expression variance from *trans*-acting or environmental factors.

Note that σ_{HET}^2 is a genome-wide parameter; this assumes that, across loci, variable sites have similar effects on allelic imbalance. This model also assumes that each *cis*-heterozygous site contributes additively to the variance in the underlying proportion of reads expressed from the alternative allele (Var[$p_{i,g}$]).

We then assumed that the number of alternative allelereads sampled in individual *i* at locus $g(A_{i,g})$ results from binomial sampling around the proportion of alternative allele reads at that locus.

$$A_{i,g} \sim \operatorname{Binom}\left(N_{i,g}, p_{i,g}\right).$$
 (7)

In total, the observed number of reads containing the alternative allele will be Beta-Binomially distributed. The variance in alternative-allele counts is, then,

$$\operatorname{Var}[A_{i,g}] = \hat{p}(1-\hat{p}) \times N_{i,g} \times \left(1 + 4(N_{i,g}-1)\operatorname{Var}[p_{i,g}]\right).$$
(8)

Under this model, we can update our squared Z-score of alleleic imbalance (Equation 5) to account for variance contributed by *cis*-regulatory genetic variation.

$$Z_{\text{ALT};i,g}^{*2} = \frac{\left(A_{i,g} - (\hat{p} \times N_{i,g})\right)^2}{\hat{p}(1 - \hat{p})N_{i,g}\left(1 + 4\left(N_{i,g} - 1\right)\left(n_{\text{HET};i,g}\sigma_{\text{HET}}^2 + \nu_p\right)\right)}.$$
(9)

Note that

$$Z_{\text{ALT};i,g}^{*2} = Z_{\text{ALT};i,g}^2 \frac{1}{1 + 4(N_{i,g} - 1)(n_{\text{HET};i,g}\sigma_{\text{HET}}^2 + \nu_p)}.$$
 (10)

When the number of sampled reads at a locus, $N_{i,g}$, is large, $Z^*_{ALT;i,g}$, is standard-normally distributed. Regardless of the number of sampled reads, $E[Z^{*2}_{ALT;i,g}] = 1$. Therefore,

$$E\left[Z_{ALT;i,g}^{2}\right] = 1 + 4(N_{i,g} - 1)(n_{HET;i,g}\sigma_{HET}^{2} + \nu_{p}).$$
(11)

Rearranging Equation 11,

$$\frac{\mathrm{E}\left[Z_{\mathrm{ALT};i,g}^{2}\right] - 1}{4(N_{i,g} - 1)} = n_{\mathrm{HET};i,g}\sigma_{\mathrm{HET}}^{2} + \nu_{p}.$$
 (12)

As $Z^2_{\text{ALT};i,g}$, $N_{i,g}$, and $n_{\text{HET};i,g}$ are measurable in data, we can apply linear regression according to the above model to estimate σ^2_{HET} .

If stabilizing selection acts on gene expression, we would expect rare variants to contribute disproportionately to allelic imbalance. However, the above model assumes that all *cis*heterozygous sites contribute equally to the variance in ASE. We therefore extended our model to allow different values of σ_{HET}^2 for *cis*-heterozygous sites with different allele frequencies. Now,

$$\frac{\mathrm{E}\left[Z_{\mathrm{ALT};i,g}^{2}\right] - 1}{4(N_{i,g} - 1)} = \sum_{b} (n_{\mathrm{HET};i,g})_{b} (\sigma_{\mathrm{HET}}^{2})_{b} + v_{p}.$$
 (13)

where *b* indexes allele frequency bin. $(n_{\text{HET};i,g})_b$ is, for individual *i* at locus *g*, the number of *cis*-heterozygous sites with a population frequency that falls in allele frequency bin *b*, and $(\sigma_{\text{HET}}^2)_b$ is the variance in allelic imbalance explained by each variant in allele frequency bin *b*.

We can then estimate values of $(\sigma_{\text{HET}}^2)_b$ jointly using multiple regression with the counts of *cis*-heterozygous sites in each allele frequency bin as predictors.

Estimating the contribution of cis-regulatory variants to ASE

In this study, we analyzed ASE in 122 self-reported European individuals with RNA sequencing data and genotype calls from whole-genome sequencing from the Genotype Tissue Expression Project (GTEx Consortium 2017). We included the nine best-sampled tissues [whole blood, subcutaneous adipose, tibial artery, heart (left ventricle), lung, skin (not sun exposed), tibial nerve, skeletal muscle, and thyroid] in our analyses.

For an allelic imbalance measurement to be included in our analyses, we required the individual to have at least two reads supporting the reference and alternative alleles, respectively, within a given tissue, and at least five reads supporting each allele across the nine studied tissues. We also required the focal ASE site to be in Hardy-Weinberg equilibrium; determined using a chi-squared test with one degree of freedom and $\alpha = 0.005$. These filters help reduce false signals of ASE resulting from genotyping errors at ASE sites.

For individual-gene pairs with multiple heterozygous sites that passed these filters, the site covered by the largest number of reads was analyzed. Human imprinted genes as listed by *geneimprint* (downloaded from http://www.geneimprint.com/site/genes-byspecies) were excluded from downstream analyses, as were highly polymorphic human leukocyte antigens (HLA) genes (*i.e.*, genes in the extended MHC region; bounded by SNPs rs498548 and rs2772390 plus 2 Mb extensions on both sides).

At each individual-gene pair in each tissue that met our quality control (QC) criteria, we calculated $Z^2_{ALT;i,g}$ as described above. As an example, this resulted in 141,138 measurements of allelic imbalance at 18,307 unique loci in whole blood. We also calculated a combined-tissue ASE, wherein, within an individual, reads containing each allele at a focal ASE site were summed across tissues. This resulted in 343,653 measurements of combined-tissue allelic imbalance at 36,180 unique loci.

To estimate the contributions of *cis*-regulatory variants to ASE, we determined the number of possible gene-regulatory variants at each locus. In each individual, we considered all heterozygous sites in *cis* to an ASE site to have potential effects on gene regulation.

We defined sites in *cis* to be those that lie within 10 kb (or, when noted, 50 kb) of the most upstream TSS of a gene containing an ASE site. TSSs, as annotated in Ensembl, were obtained using biomaRt (Kinsella *et al.* 2011). We filtered sites not in Hardy-Weinberg equilibrium, determined using a chi-squared test with one degree of freedom and $\alpha = 0.005$. We then counted, for each individual, the number of sites in *cis* to each ASE site that were called as heterozygous based on whole-genome sequencing data from the GTEx Project (GTEx Consortium 2017).

For the combined-tissue data, this resulted in 1,183,405 heterozygous sites in *cis* to 12,159 unique genes with measured ASE, with a median of 19 *cis*-heterozygous sites per locus per individual.

We then estimated the average contribution of a *cis*heterozygous site to allelic imbalance using linear regression, as described in Equation 12.

Due to correlation between data points (*e.g.*, ASE was measured at the same gene in many individuals), we estimated 95% confidence intervals for the regression coefficient ($\sigma_{\rm HET}^2$) using a weighted jackknife as described in Busing *et al.* (1999), excluding measurements from all individuals for a single gene in each subsample.

To explore whether stabilizing selection acts on *cis*-regulatory variants in these ASE data, we tested whether there was a relationship between the allele frequency of a *cis*-heterozygous site and its contribution to allelic imbalance.

To do so, we binned *cis*-heterozygous sites by their minor allele frequency in Europeans in GTEx (GTEx Consortium 2017). We divided variants into singletons, doubletons, and spaced the remaining bins such they each contained approximately the same number of sites as the doubleton bin. The resulting bins have the following allele frequency cutoffs: (0.02, 0.04, 0.09, 0.16, 0.27, 0.4, 0.5).

We also repeated this analysis with *cis*-heterozygous sites binned by their minor allele frequency in Europeans in gnomAD (Lek *et al.* 2016). Allele frequencies in gnomAD were extracted using bcftools (Li 2011). Only variants with matching reference and alternative alleles in the GTEx and gnomAD datasets were included. Bins were spaced such that they each contained approximately the same number of sites. The resulting bins have the following allele frequency cutoffs: (0, 0.0002, 0.0013, 0.0047, 0.0125, 0.033, 0.084, 0.18, 0.33, 0.5).

For each ASE site in each individual, we counted the number of *cis*-heterozygous sites in each allele frequency bin. We then estimated the average contributions of *cis*-heterozygous sites in each bin to allelic imbalance using multiple regression, as described in Equation 13.

To explore the confidence level of these estimates, we first permuted allelic imbalance measures across all individuals and genes. Second, we permuted allelic imbalance measures across all individuals within a gene. The first tests for global artifacts of the multiple regression the second tests for variation in allele frequency spectra and allelic imbalance across genes. In all cases, the total number of variants and the number of variants in each allele frequency bin were retained as in the original data. We performed 100 permutations for each of condition and compared the resulting estimates to those obtained in the original data.

Calculating genetic variance of ASE

One way to understand the strength of selection on gene expression is to ask what proportion of the genetic variance of allelic imbalance is explained by rare variants. We therefore calculate, for each gene, the genetic variance of allelic imbalance contributed by variants in each allele frequency bin. We then calculate the total genetic variance of ASE as well as the proportion of that genetic variance attributable to each allele frequency bin.

Each variable position contributes genetic variance to allelic imbalance as follows:

$$2f_i(1-f_i)\big(\sigma_{\rm HET}^2\big)_b,\tag{14}$$

where f_i is the frequency of SNP *i* in allele frequency bin *b* and $(\sigma_{\text{HET}}^2)_b$ is the average variance in ASE contributed by a variant in allele frequency bin *b* (as estimated above).

For a given gene, the genetic variance of ASE contributed by allele frequency bin b is therefore,

$$\left(\sigma_{g;ASE}^{2}\right)_{b} = \sum_{\substack{SNP \ i \\ \text{in AF bin } b}} 2f_{i}(1-f_{i})\left(\sigma_{\text{HET}}^{2}\right)_{b}$$
(15)

To calculate the genetic variance of ASE captured by our model for each gene, we then sum the genetic variance contributed by each allele frequency bin.

$$\sigma_{g;ASE}^2 = \sum_{b} \left(\sigma_{g;ASE}^2 \right)_b.$$
(16)

The total genetic variance of ASE captured by our model can be written as

$$\sigma_{g;ASE}^2 = \sum_b \sum_{\substack{\text{SNP } i \\ \text{in AF bin } b}} 2f_i (1 - f_i) \left(\sigma_{\text{HET}}^2\right)_b.$$
(17)

The proportion of the genetic variance of ASE explained by allele frequency bin *b*, then, is

$$\frac{\left(\sigma_{g;ASE}^{2}\right)_{b}}{\sigma_{g;ASE}^{2}} = \frac{\sum_{\substack{\text{in AF bin } b}} 2f_{i}(1-f_{i})\left(\sigma_{\text{HET}}^{2}\right)_{b}}{\sum_{b}\sum_{\substack{\text{SNP } i \\ \text{in AF bin } b}} 2f_{i}(1-f_{i})\left(\sigma_{\text{HET}}^{2}\right)_{b}}.$$
(18)

Note that we do not directly estimate the heritability of allelic imbalance. However, heritability is simply the proportion of phenotypic variance that can be explained by genetic variance (σ_g^2/σ_p^2) . Therefore, the proportion of heritability explained by variants in a given allele frequency bin is equivalent to the proportion of genetic variance explained by those variants.

Data availability statement

RNA sequencing and genotype data used in eQTL calling were accessed by application through the NIMH Center for Collaborative Genomic Studies on Mental Disorders. Instructions for requesting access to data can be found at https:// www.nimhgenetics.org/access_data_biomaterial.php. Inquiries should reference the "Depression Genes and Networks study (D. Levinson, PI)."

Gene expression measurements (RPKM) across 12 tissues for healthy individuals with CNVs were obtained from version 4 of the GTEx Project (GTEx Consortium 2017, dbGaP accession phs000424.v4.p1). RNA sequencing data for twins discordant for trisomy 21 were accessed from the Gene Expression Omnibus (GEO) data repository (accession GSE55426).

The 1000 Genomes phase 3 data, used in polarizing genotypes to the human ancestral allele, were obtained from ftp:// ftp.1000genomes.ebi.ac.uk/vol1/ftp/release/20130502/ ALL.wgs.phase3_shapeit2_mvncall_integrated_v5b.20130502. sites.vcf.gz. Details regarding the determination of humanchimp ancestral alleles are available from ftp://ftp.1000 genomes.ebi.ac.uk/vol1/ftp/release/20130502/README_ vcf_info_annotation.20141104.

Allele specific expression tables as well as genotype calls from whole genome sequencing, used in estimating the effects of rare regulatory variants on gene expression, were obtained from version 6 of the GTEx Project (dbGAP accession phs000424.v6.p1).

Allele frequencies from the gnomAD dataset (Lek *et al.* 2016) were obtained from VCFs available through the gnomAD browser http://gnomad.broadinstitute.org/downloads. Supplemental material is available at Figshare: https://doi.org/10.25386/genetics.7396673.

Results

CNVs show dosage sensitivity

Gene duplications and deletions are likely to have large effects on gene expression. If expression is under stabilizing selection, we would expect large-effect CNVs to be rare in the population. To test whether human genetic variation is affected by selection against large changes in gene expression, we analyzed the expression levels and allele frequencies of CNVs.

Using whole-genome and transcriptome sequencing of 147 individuals from version 4 of the GTEx Project (GTEx Consortium 2017), we identified 694 genes whose entire coding sequence had been duplicated in 196 polymorphic CNVs, and obtained their expression across 12 tissues.

Despite high variance in expression ratios across genes, when a duplication CNV is rare (present in one individual in this sample), genes in the CNV are expressed at higher levels in heterozygous carriers (with three gene copies) than in noncarriers (with two gene copies; median expression ratio 1.31; Figure 2). By contrast, genes in common CNVs (for which >5% of sampled individuals have a duplicate gene copy) are expressed at similar levels in individuals with two and three copies (median expression ratio is 0.95; Figure 2).

If each gene copy were expressed equally, we would expect the ratio of expression in heterozygous duplication carriers to that in noncarriers to be 1.5. The observed ratio, < 1.5, may result from a cellular buffering mechanism that reduces expression in carriers in an attempt to maintain stable expression levels.

To test for expression buffering, we obtained RNA sequencing data from a set of monozygotic twins discordant for trisomy 21 (Letourneau *et al.* 2014). Importantly, as trisomy 21 is a *de novo* expression-altering event, selection cannot affect the newly introduced expression changes.

We see that the average expression of genes on chromosome 21 is \sim 50% higher in the trisomy 21 individual than in their diploid twin (Figure 2). This suggests that, before selection has time to act, when the entire gene and *cis*-regulatory region are duplicated, cellular buffering is negligible and expression increases proportionally with gene dosage. This is consistent with previous work showing that, for common, multi-allelic CNVs, gene expression scales linearly with copy number (Handsaker *et al.* 2015).

The lack of apparent expression buffering suggests that the negative relationship between the expression of duplicated genes and CNV frequency is driven by constraint. In other words, a gene duplication can become common only when expression in carriers is comparable to that in noncarriers.

Three types of regulatory variation could generate this relationship. First, during gene duplication, damage may occur to *cis*-regulatory elements of the duplicated gene. Damaged duplicates may lead to smaller expression increases and are therefore more likely to survive. Second, CNVs may arise on genetic backgrounds that vary in their expression. In this case, duplicates that arise on low-expression backgrounds (*e.g.*, haplotypes with an expression-decreasing eQTL) are more likely to spread in the population. Third, haplotypes with a duplicate gene may acquire additional genetic variation; haplotypes on which compensatory, down-regulating variants arise can become common.

Regardless of the mechanism, patterns of expression variation at CNVs confirm that constraint on expression affects large-effect regulatory variants.



Figure 2 Expression of heterozygous carriers of a gene duplication (with three gene copies) relative to noncarriers (with two gene copies). On the left, each point corresponds to the expression level (RPKM) of one of 104 genes in an individual with trisomy 21 relative to the expression of the gene in their diploid twin. On the right, each point corresponds to the median expression of heterozygous duplication carriers relative to the median expression of noncarriers for one gene in one tissue. To reduce noise in the expression ratio, gene/tissue pairs with median noncarrier RPKM<1 were excluded (891 gene/tissue pairs retained). Duplicate frequencies obtained from GTEx. Black lines show median expression ratios across genes in each bin.

However, many genetic variants may have smaller effects on expression than a gene duplication. We therefore investigated whether selection on expression is sufficiently strong to affect smaller-effect variants.

Characterizing patterns of cis-regulatory variation using eQTL

First, we carried out eQTL-mapping using genotype and whole-blood RNA sequencing data from 922 European individuals from the Depression Genes and Networks cohort (Battle *et al.* 2014). We called *cis*-eQTLs using stepwise regression in 100 kb windows centered on the TSS of 12,794 autosomal, protein-coding genes (see *Materials and Methods*). This approach allows multiple, independent causal variants per locus. In total, we tested 3,309,888 SNPs and called 6587 significant eQTLs associated with 4734 genes (37% of genes tested).

To preserve interpretability of our effect size estimates, we did not perform any principal component or latent factor correction on our data, nor did we include any covariates in our eQTL mapping. As these additions would have improved our statistical power, the approximately twofold fewer eGenes (genes with a significant eQTL) detected here relative to previous studies is expected (Battle *et al.* 2014).

For 27.33% of eGenes, we called more than one eQTL (to a maximum of 9). This suggests that, at many loci, there may be multiple regulatory variants that would be missed when considering only the most significant eQTL (two such loci are shown in Figure 3).

The median expression of individuals heterozygous for an expression-increasing eQTL was 21% higher than that of homozygotes (-18% for expression-decreasing eQTLs).

When polarizing effect sizes relative to the ancestral allele, we detected similar numbers of eQTLs predicted to increase and decrease expression (3284 expression-increasing and 3303 expression-decreasing eQTLs; not significantly different by binomial test; P = 0.82). Expression-increasing and -decreasing eQTLs had comparable effect size distributions (in terms of fold-change); however, the effects of expressionincreasing eQTLs tended to be slightly larger (Figure 4A; P = 0.0037 by two-sided Kolmogorov-Smirnov test). In particular, we called more large-effect, expression-increasing eQTLs; 243 eQTLs were predicted to double gene expression, 139 to cut expression in half.

There are both technical and biological explanations for this trend. Technically, we may have less power to detect expression-decreasing eQTLs. Biologically, large decreases in gene expression may be less well-tolerated than large increases.

The joint distribution of allele frequency and effect size shows that rare eQTLs tend to have larger effects than common eQTLs (Figure 4C). The median common eQTL [minor allele frequency (MAF) > 0.1, n = 4949] was predicted to increase expression by 18% (-15% for expression-decreasing eQTLs). For rarer eQTLs (MAF < 0.1, n = 1638), the median predicted expression increase was 40% (-25% for expression-decreasing eQTLs). This is consistent with purifying selection acting against *cis*-regulatory variation.

However, eQTL effect sizes can be difficult to interpret. First, previous work has discussed the challenges inherent in estimating eQTL effect sizes when there are multiple causal variants at a locus (Zeng *et al.* 2017). Second, power to map eQTLs of the same effect varies with allele frequency. Third, a statistical phenomenon referred to as "winner's curse" can induce a relationship between allele frequency and estimated effect size (Göring *et al.* 2001; Lohmueller *et al.* 2003; Tung *et al.* 2015). We explored the impacts of each of the above on our effect size estimates.

First, univariate (independent) eQTL effect size estimates were similar to those derived from our stepwise approach (Figure 3). It is therefore unlikely that the presence of multiple causal variants per locus meaningfully impacted our estimates.

Variable eQTL-detection power by allele frequency, however, did impact our calls. One might expect eQTL-based analyses to be limited to relatively common regulatory variants. Indeed, our eQTLs were, on average, more common than candidate SNPs (Figure 4B).

Further, as we lack power to call rare eQTLs of small effect, one might expect the median effect size of rare eQTLs to be



Figure 3 *cis*-eQTLs called using forward-stepwise mapping from wholeblood RNA sequencing in 922 European individuals. (A) eQTL mapping for *ADORA1*. (B) eQTL mapping for *RAP1GAP*. Effect sizes are polarized relative to the ancestral allele. Stepwise effect size estimates (green) are compared to those obtained by testing each SNP independently (orange) at two example loci. Vertical bars mark \pm 2 SE around the estimated effect size for each SNP. Lead eQTLs (smallest *P*-value) from independent testing are marked with asterisks.

inflated relative to common eQTLs. However, when considering only eQTLs with relatively large effects (that could be detected at all frequencies; details in Supplemental Material, Table S1), rare eQTLs were estimated to have larger effects than common ones (Table 1). This suggests that decreased power to detect rare eQTLs is not sufficient to explain the observed relationship between frequency and effect size.

However, this relationship could also result from winner's curse. Conditional on a variant being called as an eQTL, we expect its effect to be overestimated (Göring *et al.* 2001; Lohmueller *et al.* 2003). This is particularly true for rare variants.

To explore the effects of winner's curse, we ascertained eQTLs and estimated their effects in separate subsamples of the DGN data. In the ascertainment set, eQTLs were estimated to have a median effect of 22% (-18% for expression-decreasing eQTLs) on expression. In the validation set, however, the median effect was 18% (-14% for expression-decreasing eQTLs; P = 9.51e - 15 by paired *t*-test; Figure S1). This suggests that winner's curse inflates eQTL effect size estimates. Comparing effect size estimates across rare (0.02 < MAF < 0.1) and common (MAF > 0.1) eQTLs revealed that winner's curse disproportionately inflates estimates at the low end of the allele frequency spectrum (Table 1).

Indeed, effect size estimates from the validation set no longer show any relationship with allele frequency (Figure 4D, further detail in Figure S1). This is consistent with Tung



Figure 4 cis-eQTLs called using forward-stepwise mapping in 100 kb windows centered on the TSS of autosomal, protein-coding genes. Data from whole-blood RNA sequencing in 922 European individuals (DGN). Effect sizes polarized relative to the ancestral allele. (A) Cumulative distributions of estimated eQTL effect sizes, represented as the ratio of eQTL-heterozygotes to eQTL-homozygotes. Expression-increasing eQTLs (derived allele increases expression) shown in dark blue, expressiondecreasing eQTLs in light blue. (B) Allele frequency spectrum of eQTLs (gray) relative to the background of all tested SNPs (white) (C) Joint distribution of eQTL MAF and estimated effect size. Black points show eQTLs with effect sizes that we are powered to detect at all frequencies (estimated effect greater than the minimum effect of eQTLs with MAF<0.02), gray points show eQTLs that are especially rare (MAF<0.02) and/or have effect sizes that we are powered to detect only at higher frequencies. Blue lines show loess-fits of MAF vs. effect size for well-powered expression-increasing and -decreasing eQTLs (black points). (D) eQTLs called in an ascertainment set of 800 individuals, effect sizes estimated in validation set of 122 individuals. Only well-powered eQTLs across allele frequencies and with MAF>0.02 are plotted. Points colored by the direction of effect in the ascertainment set; expression-increasing eQTLs in dark blue, expression-decreasing eQTLs in light blue. Loess-fits of MAF vs. effect size for expression-increasing and -decreasing eQTLs in black.

et al. (2015), who also saw a significant impact of winner's curse on effect size estimates of rare eQTLs. We conclude that eQTL effect size distributions fail to provide evidence for constraint on gene expression.

However, absence of evidence is not necessarily evidence of absence. To more carefully test for a relationship between eQTL effect size and allele frequency, we used an independent dataset of ASE.

eQTL effects on ASE

ASE, or allelic imbalance, is measured using a heterozygous site in a transcript. This site is used to identify reads from, and quantify the expression of, each haplotype within an individual.

Variation in expression across haplotypes captures the regulatory effects of all *cis*-heterozygous sites in an individual, regardless of their frequencies in the population. As a result, analyses of ASE include genetic variants that are too rare to be detected in eQTL studies.

On the other hand, eQTL mapping is better suited to estimate the effects of individual variants on gene regulation. ASE and eQTL mapping are, therefore, complementary tools for measuring *cis*-regulatory variation.

To sidestep statistical challenges in eQTL effect size estimation, we combined our eQTLs with ASE (data from GTEx version 6, GTEx Consortium 2017). We measured ASE using a squared Z-score of reads containing the alternative allele in 343,653 gene-individual-tissue trios (*i.e.*, a gene expressed in a given tissue in a given individual; see *Materials and Methods* for QC filters).

Previous work has demonstrated that ASE measurements are generally consistent with eQTLs (Pickrell *et al.* 2010). To confirm that here, we show that at eGenes, eQTL-heterozygotes (heterozygous for at least one eQTL) tend to have higher allelic imbalance than eQTL-homozygotes (homozygous for all called eQTLs; Figure 5A). In addition, eQTL effect sizes were correlated with allelic imbalance in eQTL-heterozygotes (Figure 5B).

To gain additional insight into the structure of the gene regulatory landscape across tissues, we compared a singletissue analysis of blood to a combined-tissue analysis in which reads spanning an ASE site in an individual were summed across tissues.

In both eQTL-heterozygotes and -homozygotes, combinedtissue ASE tended to be higher than ASE measured in blood (Figure 5A). This shift can be explained by differences in read depth; due to the summation of reads across tissues, average read depth per ASE site was higher in the combined-tissue data (median 130 for combined-tissue, 28 for blood; Figure S7A). Increased read depth reduces sampling variance, thus increasing our ability to detect *bona fide* allelic imbalance (and increasing the resulting ASE Z-score).

However, summing reads across tissues would increase ASE only if allelic imbalance were concordant across tissues. Like many other eQTL and ASE analyses (*e.g.*, Flutre *et al.* 2013; Wheeler *et al.* 2016; GTEx Consortium 2017), our findings suggest that many gene regulatory effects are consistent (or, at least, are unlikely to be inconsistent) across tissues.

Finally, we explored whether ASE provides evidence of selection against eQTLs (Figure 5B). In both combined-tissue

Table 1 Summary of the effects of variable power and winner's curse on eQTL effect size estimates and their relationship with minor allele frequency

	Median eQTL effect				
	Full Data 21% 			Ascertainment (validation) 22% (18%) -18% (-14%)	
Expression increasing Expression decreasing					
	MAF 0.02–0.1	MAF >0.1	MAF 0.02–0.1	MAF >0.1	
Expression increasing—filtered for power Expression decreasing—filtered for power	48% 28%	40% 28%	52% (44%) -29% (-25%)	45% (45%) -29% (-29%)	

Effect sizes reported as percent change of eQTL-heterozygotes relative to the homozygous ancestral. To explore the effects of winner's curse, individuals were split into an eQTL ascertainment set and an effect-size validation set. To explore the impact of variable power to call eQTLs of the same effect across allele frequency bins, eQTLs were filtered to remove those with estimated effects that we would lack power to call at low allele frequencies. Here, we consider eQTLs with estimated effects larger than the minimum magnitude of estimated effect for significant, rare eQTLs (MAF<0.02). To ensure conservative estimates of the relationship between effect size and allele frequency, we also remove rare eQTLs (MAF<0.02) from comparisons across allele frequency bins.

and blood-specific ASE, there is a subtle, but significant, negative correlation between ASE in eQTL-heterozygotes (a proxy for eQTL effect size) and the frequency of the corresponding eQTL. This suggests that selection on eQTLs is present, but weak.

Effects of cis-regulatory variants vary with allele frequency

We next examined constraint on regulatory variants not captured by eQTL mapping. We first sought to relate allelic imbalance to the amount of *cis*-regulatory variation at a locus within an individual. In our model, each *cis*-heterozygous site contributes to the variance in the ratio of reads expressed from each haplotype (detailed in *Materials and Methods*). In this case, we expect the number of *cis*-heterozygous sites to be linearly related to our ASE Z-score.

We then used linear regression to estimate the average contribution of a heterozygous site (across all genes in all individuals) to ASE. In single tissues and in a combined-tissue analysis, we observed significant, positive relationships between genetic variation and ASE (Figure 6). This suggests that variation in allelic imbalance across loci has a genetic basis, rather than being driven solely by sampling noise or environmental factors.

The average effect of a variant on ASE decreases as we increase the *cis*-regulatory window under consideration (Figure 6). This likely reflects the spatial distribution of causal regulatory variants; we and others find that eQTLs are enriched near TSSs (Figure S2; Stranger *et al.* 2007; Veyrieras *et al.* 2008). If this holds for rarer regulatory variants, widening the *cis*-window will decrease the proportion of causal variants included in the model and so decrease the average effect size per variant. For a given window, average per-variant effect size estimates are similar across tissues (Figure 6).

Next, we expanded our model to incorporate allele frequency information. If purifying selection keeps largeeffect regulatory variants rare, we would expect a rare *cis*heterozygous variant to contribute more to allelic imbalance than a common one. For each gene in each individual (individual-gene pair), we counted the number of heterozygous sites in each of nine allele frequency bins. We then used multiple regression to estimate the contribution of an average site in each frequency bin to ASE.

Correlation between the numbers of heterozygous sites across allele frequency bins would make it difficult to accurately estimate average effects for each bin. However, in these data, this correlation is very weak (maximum Pearson correlation across pairs of frequency bins is 0.07; Figure S3).

We find that the average contribution of a singleton in the GTEx dataset to the variance in ASE is $\sim 2.2 \times$ greater than that of the average variant across allele frequency bins (1.8 \times greater than the average common variant (MAF>0.4); Figure 7A). Permutations of ASE measurements across individuals and genes, as well as across genes within an individual, suggest that this relationship between frequency and contribution to ASE is significant.

As this dataset contains only 122 individuals, allele frequency estimates may be noisy. Additionally, singletons in GTEx may not be especially rare in the population. We therefore repeated our analysis with variants binned by their minor allele frequency in the much larger gnomAD dataset (Lek *et al.* 2016; n = 7209 Europeans with whole genome sequencing, Figure 7B). We see similar trends with both binning strategies.

The relationship between allele frequency and contribution to allelic imbalance also persists when considering genetic variants in a much larger candidate *cis*-regulatory region (Figure S5). As for the average per-variant effect across allele frequencies (Figure 6), increasing the window size decreases the estimated effect for variants in each allele frequency bin. However, the average contributions of rare variants (singletons and doubletons) remain greater than those of common variants.

Importantly, this trend is so subtle that it is detectable only when reads are combined across tissues; single-tissue analyses show no clear relationship between allele frequency and estimated effect size (examples whole blood and skeletal



Figure 5 eQTL effects reflected in ASE at eGenes. "Blood" shows ASE in whole blood, "Combined" shows combined-tissue ASE, measured by summing reads spanning an ASE site in the same individual across tissues. (A) Cumulative distributions of ASE measured in whole blood (solid) and combined-tissue ASE (dotted), separated into eQTL-heterozygotes (green), and -homozygotes (homozygous for all called eQTLs, yellow). (B) Rank correlation between allelic imbalance and eQTL effect (left) or minor allele frequency in gnomAD (right). The effect/MAF of the most significant heterozygous eQTL (or, for eQTL-homozygotes, the most significant eQTL) was used. To determine the robustness of these correlations, each point shows the rank correlation in one of 1000 samples generated by bootstrapping over genes. Median correlations of bootstrap samples marked in black, 95% quantiles in white.

muscle shown in Figure S6). This is likely due to the fewer genes, fewer individuals sampled per gene, and lower read depth per individual-gene pair in single tissues as compared to the combined set (for sample size comparisons, see Figure S7; for read depth comparisons, see Figure S8).

From this, we conclude that constraint on gene expression reshapes patterns of regulatory genetic variation. However, the subtlety of this signal suggests that selection on gene expression is weak.

Proportion of heritability (genetic variance) explained by rare variants

Another way to understand the strength of selection on expression is to ask what proportion of the heritability (or, what proportion of the genetic variance σ_g^2) of expression can be explained by rare variants.

Two components determine how much genetic variance is explained by a variant: the variant's squared effect size and its allele frequency (particularly its contribution to heterozygosity, 2pq). When considering the proportion of genetic variance explained by a group of variants at a given allele frequency, the allele frequency spectrum (the proportion of variants in each allele frequency bin) is also important.

Many polygenic trait models assume that all variants, regardless of their allele frequency, contribute equally to genetic variance ($2pq\beta^2$; *e.g.*, Yang *et al.* 2011; Bulik-Sullivan *et al.* 2015). As their low allele frequencies cause rare variants to contribute less to heterozygosity (2pq), this type of model implicitly assumes that rare variants have larger effects (β^2) than common ones.



Figure 6 Average effect of a *cis*-genetic variant on allelic imbalance. Estimates are based on linear regression of an individual's number of *cis*-heterozygous sites within (A) 10 kb and (B) 50 kb of the TSS of a gene and measured ASE for each of the nine best sampled GTEx tissues. Vertical lines show 95% confidence intervals, estimated using a weighted jackknife as described in Busing *et al.* (1999). For reference, the dotted line marks zero estimated effect.

Others (*e.g.*, Speed *et al.* 2012) more explicitly account for the relationship between allele frequency (and corresponding differences in LD) and variance explained. For a more detailed comparison of heritability estimation and variance partitioning methods, see Evans *et al.* (2018).

While these models were not designed with singletons in mind, their varying assumptions about allele frequency, effect size, and heritability led us to consider what impact the observed $2.2 \times$ greater effect size of singletons would have on the proportion of heritability explained by rare variants.

To explore this, we combined our average effect size estimates with allele frequency spectra at each gene to estimate the genetic variance of allelic imbalance captured by our model ($\sigma_{g;ASE}^2$) as well as the proportion of $\sigma_{g;ASE}^2$ explained by variants in each allele frequency bin (summary of allele frequency spectra in Figure S9). Across genes, we find the median heritability explained by singletons (in a sample of 122 individuals) to be a mere 5% (Figure 8). Table 2 shows comparisons of our model to two extreme cases: (1) rare variants (singletons) and common variants (MAF>0.4) contribute equally to genetic variance ($2pq\beta^2$), (2) rare and common variants have equal effects on gene expression (β^2).

Our model suggests that singletons explain more of the heritability of gene expression than expected under neutrality (effect size independent of allele frequency). This is due to singletons' increased average effect size relative to common variants. However, in these data, the relative effect size difference between singletons and common variants is far less



Figure 7 Effects of cis-genetic variants on allelic imbalance given their allele frequencies. Estimates are obtained from multiple regression on allelic imbalance using the number of *cis*-heterozygous sites in each allele frequency bin as predictors. Here, we include sites in a 20-kb window centered on the TSS of a gene with measured allelic imbalance. Estimates from combined-tissue ASE (reads spanning each ASE site in a single individual are summed across all tissues sampled) are shown in black. Colored points represent estimates from 100 permutations of (1) ASE measurements across genes and individuals (red) and (2) ASE measurements across genes within an individual (orange). Horizontal lines mark zero effect (dashed) and the average variant effect estimated by regressing allelic imbalance on the total number of *cis*-heterozygous sites (solid). (A) Estimates with variants binned by minor allele frequency in Europeans in the GTEx data (n = 122). (B) Estimates with variants binned by minor allele frequency in Europeans in gnomAD (n = 7509).

than what would be required for a singleton to contribute as much as a common variant to the heritability of gene expression.

While these findings are consistent with previous evidence of constraint on gene expression (Hernandez et al. 2017; Zeng

Genetic variance by allele frequency 1.00 0.75 0.400.50 0.27 -0.40 0.16 0.09 -0.160.50 0.04 -0.090.02 - 0.04



Figure 8 Partitioning the genetic variance of allelic imbalance by allele frequency. For each gene, we combine the average heterozygosity (2 pg) and number of segregating sites in each allele frequency bin with the estimated average effect size of variants in that bin to calculate the total genetic variance of allelic imbalance captured by our ASE-model ($\sigma_{\alpha;ASE}^2$). We then calculate the proportion of $\sigma_{g;ASE}^{2}$ explained by each allele frequency bin (variants binned by minor allele frequency in GTEx). Each vertical bar represents a single gene for which we measured ASE, colors represent the proportion of genetic variance attributed to variants in each allele frequency bin.

et al. 2018), Hernandez et al. (2017) estimate a much greater contribution of singletons to expression variance, suggesting a much greater role of purifying selection on gene-regulatory variants, than we see here. At this time, we do not know the source of the discrepancy between the studies; however, the two approaches involve different analytical methods, different gene expression measurements (ASE vs. RNASeq), and samples of different sizes.

Future work will be required to understand why different approaches appear to support different conclusions with respect to the importance of rare variants on gene expression. However, in our analysis of allele-specific expression, we do not find support for rare variants being major drivers of expression variance.

Although the median heritability explained by singletons is small, we detect notable variation in singleton-heritability across genes (Figure 8). As we estimate a single, average singleton effect across all genes, this variation is due entirely to differences in allele frequency spectra.

This variation led us to wonder how much of the observed constraint (i.e., relative effect size differences between rare and common variants) is driven by a subset of particularly tightly constrained genes.

Patterns of eQTLs and ASE suggest variable constraint on expression across gene classes

To understand variation in constraint on expression across the genome, we compared patterns of regulatory variation across gene sets.

We expect genes with greater constraint on expression to have lower levels of cis-regulatory variation than genes with

Table 2 Singleton contributions to heritability

Singletons vs. common variants (MAF>0.4)	Estimates	Models	
	$\widehat{eta^2}$ from ASE	$\beta^2 \propto [pq]^{-1}$	β^2 independent of p
Proportion $\sigma_{\alpha \text{ ASF}}^{\mathcal{I}}$ explained by singletons	4.7%	36%	2.4%
Relative squared effect size	~1.8	~60	1
Selection strength	Weak	Strong	None

Estimates based on GTExV6 ASE data (*cis*-regulatory region +- 10kb from TSS) " $\hat{\beta}^2$ from ASE" shows estimates of the median proportion of $\sigma_{g,ASE}^2$ explained by singletons based on effect sizes estimated from our ASE-model. " $\beta^2 \propto [pq]^{-1}$ " shows the median expected per-gene heritability explained by singletons if singletons and common variants contributed equally to genetic variance. This is driven by the fact that 36% of all variants (median 36% of variants per gene) are singletons. The large relative effect size required for singletons to explain this proportion of heritability reflects the low variance contribution of rare variants as a consequence of their low allele frequency (2 *pq*). " β^2 independent of p" shows estimates of the median proportion of heritability explained by singletons if effect size and allele frequency were independent (*i.e.*, singletons and common variants had equal effects on gene expression).

less-constrained expression. To test this, we compared eQTLs across gene sets predicted to have varying tolerance to large changes in gene expression. Specifically, we utilized Probability of Loss-of-Function Intolerance (*pLI*) (Lek *et al.* 2016). *pLI* measures, for each gene, the relative depletion of protein-truncating variants (PTVs) observed in healthy individuals compared to the expectation under a detailed mutation model.

In heterozygotes, PTVs are expected to decrease gene expression by half. Certain genes may therefore be depleted for PTVs because they are intolerant to such large expression changes. We stratified genes into two classes based on their *pLI*-predicted level of constraint on expression (low: *pLI* < 0.1, high: *pLI* > 0.9), and tested for differences in *cis*-regulatory variation.

In total, 4401 eQTLs were mapped around 3103 unique low-*pLI* genes (of 6813 genes tested), and 688 eQTLs were mapped around 511 high-*pLI* genes (of 2576 genes tested). We detected fewer eQTLs per gene for dosage sensitive, high-*pLI* genes than for less constrained, low-*pLI* genes (Figure 9A). This is consistent with prior analysis of eQTLs called in GTEx (Lek *et al.* 2016).

These differences are reflected in the amount of genetic variance captured by eQTLs ($\sigma_{g;eQTL}^2$) for low- and high-*pLI* genes (Figure 9B; P < 2.2e - 16 by two-sided Kolmogorov-Smirnov test). Based on genotypes at called eQTLs, we predicted the genetically regulated component of expression for each individual in the DGN dataset. We then estimated genetic variance as the variance of predicted expression across individuals.

We also used these eQTLs to predict expression and estimate $\sigma_{g;eQTL}^2$ in 122 European individuals from GTEx. The differences in $\sigma_{g;eQTL}^2$ between gene sets are consistent across the two datasets (Figure S10).

To quantify these differences in genetic variance, we compared the median eQTL-estimated genetic variance for genes in each *pLI* class. We assumed log-normally distributed expression values to estimate ranges of gene expression in the population.

Across genes with at least one called eQTL, we estimate that 95% of individuals possess genetic variation resulting in expression levels between 0.83 and $1.21 \times$ the population mean. However, for the median low-*pLI* gene, these ranges

are $0.82 - 1.22 \times$ and, for the median high-*pLI* gene, they are $0.85 - 1.18 \times$. This may suggest that constraint on expression removes more regulatory variation around dosagesensitive high-*pLI* genes than less sensitive low-*pLI* genes.

This observation could also be explained by differences in background selection. High-*pLI* genes experience greater coding sequence constraint than low-*pLI* genes. We might therefore expect background selection to decrease the amount of genetic variation (regulatory or not) around high*pLI* genes.

As shown in Figure S2A, there are fewer common SNPs in *cis* to low-*pLI* genes (MAF>0.05, within 50 kb of the TSS) than to high-*pLI* genes. SNPs around low-*pLI* genes also tend to be more common than those around high-*pLI* genes (Figure S2C). Finally, low-*pLI* eQTLs tend to be closer to the TSS (Figure S2, B and D). These trends suggest that background selection shapes patterns of genetic variation; however, they are unlikely to explain the striking differences in eQTL-based genetic variance across gene sets.

Variation in genetic variance across genes can also be seen in allele-specific expression. As high-*pLI* genes tend to be more highly expressed and have more sampled reads than low-*pLI* genes (read depth information in Figure S8), we might expect to more confidently call ASE (*i.e.*, higher Z-score) in high-*pLI* genes. However, we observed the opposite pattern; ASE Z-scores for high-*pLI* genes tended to be lower than those for low-*pLI* genes (Figure 9D).

In blood, 18.6% of 73,246 individual-gene pairs involving low-*pLI* genes have an ASE Z-score >3. This level of allelic imbalance is unlikely to arise from read sampling. We infer that, in these individual-gene pairs, the two haplotypes are differently *cis*-regulated. By contrast, only 13.3% of 36,457 individual-gene pairs involving high-*pLI* genes have Z-scores >3 (significantly different by binomial test, P < 2.2e - 16). Given the difference in average read depth between high-and low-*pLI* genes, this likely under-represents the difference in expression variance between gene classes.

These differences in expression variance are reflected in genetic variation; high-*pLI* genes tend to have fewer *cis*-heterozygous sites than low-*pLI* genes (Figure 9C). This suggests a link between expression variance and genetic variation.

We also detected differences across gene sets in the genetic variance captured by our ASE-model (calculated according to



Figure 9 Regulatory genetic variation across gene sets with varying levels of constraint on gene expression as predicted by *pLI* class. (A) Histogram of the number of *cis*-eQTLs called per gene by *pLI* class. (B) Cumulative distributions of eQTL-estimated genetic variance by *pLI* class. For each gene in each individual, expression levels were predicted using genotypes and effect size estimates of called eQTLs. Genetic variance was then estimated as the variance of eQTL-predicted expression levels across individuals. (C) Histogram of the number of *cis*-heterozygous sites (per individual-gene pair) within 50 kb of the TSS by *pLI* class. (D) Cumulative distributions of allelic imbalance, measured in whole blood, by *pLI* class. (E) Cumulative distributions of the genetic variance of allelic imbalance captured by our model, estimated using combined-tissue ASE and allele frequencies binned according to GTEx, by *pLI* class. (F) Cumulative distributions of the genetic variance of ASE attributable to singletons by *pLI* class.

Calculating genetic variance of ASE in *Materials and Methods*). The median estimated genetic variance for high-*pLI* genes is 2.0e - 4, for low-*pLI* genes it is 2.4e - 4 (P < 2.2e - 16 by Wilcoxon rank sum test). However, a larger proportion of the genetic variance of high-*pLI* genes is explained by singletons (median 0.053 for high-*pLI* genes, 0.045 for low-*pLI*

genes; P < 2.2e - 16 by Wilcoxon rank sum test). These observations suggest that selection reduces variance in the expression of tightly constrained genes both by reducing the number of segregating *cis*-regulatory sites and by keeping larger-effect regulatory variants more rare.

However, it remains unclear how much of the genome-wide signal of constraint on regulatory variants can be attributed to strong constraint on a subset of genes, like high-*pLI* genes, and how much is due to weak constraint subtly shifting the joint distribution of allele frequency and regulatory effect genome-wide. The extremely small number of genes with large contributions from rare variants (88% of genes have <10% genetic variance explained by singletons, 98% have <20%) may suggest that the bulk of the relationship between allele frequency and effect size is driven by weak selection on many genes, but further work is required to corroborate this interpretation. In particular, larger datasets of paired whole genome and RNA sequencing will increase the sampled genetic diversity between individuals at a locus and provide additional insight into the landscape of selection on gene expression.

Discussion

Our analyses of eQTLs and ASE suggest that selection on gene expression has detectable, but weak, effects on regulatory variants. However, much work remains to understand the connection between expression, complex traits, and fitness.

A central limitation of our approach is that we assume all heterozygous sites in an allele frequency bin have the same effect on allelic imbalance, regardless of the gene they regulate or their position relative to the TSS. In other words, we estimate the genome-wide average effect size of variants at a given allele frequency.

As a result, our model does not capture heterogeneity across regulatory variants at similar frequencies, nor does it reflect heterogeneity in regulation across genes. For example, the expression of a specific gene may be affected by a rare variant of very large effect. However, if most rare variants have negligible effects on the expression of their target genes, the average effect estimated for rare variants will remain moderate.

Our approach cannot, therefore, accurately estimate the effect of a particular variant on gene expression. Nor can we accurately estimate the proportion of genetic variance explained by singletons for a particular gene. What we can conclude is that, in general, much of the variation in gene expression is explained by common variants.

Obtaining per-variant, or average per-gene effect size estimates (rather than genome-wide averages per allele frequency bin) would provide additional insight into the generegulatory landscape and the effects of selection on gene expression. However, we show that statistical limitations decrease the applicability of per-variant effect size estimates from eQTL mapping to questions of constraint. New approaches and larger whole-genome and transcriptome datasets will be required to achieve this additional resolution. Further, in seeming contrast to our findings regarding eQTLs and ASE, analyses of loss-of-function and CNVs suggest that selection on expression changes of $1.5 \times is$, at least in some cases, sufficient to alter patterns of expression and regulatory variation. These results indicate that gene expression has notable fitness consequences.

These observations can be reconciled with the weak selection observed here by arguing that the $1.2 \times$ expression changes caused by the average eQTL and the $1.5 \times$ changes in expression caused by a gene duplication have very different effects on fitness. One might also argue that the effects seen in loss-of-function and copy number variant analyses are driven by a small set of tightly constrained genes, or that loss-of-function and CNVs have effects on fitness that are unrelated to their effects on gene expression.

These arguments might lead us to conclude that gene expression has limited downstream effects on human traits and on fitness. However, if gene regulation is highly polygenic and/or pleiotropic, selection may be unable to cause dramatic changes in the frequencies of regulatory variants (regardless of the fitness consequences of expression changes).

Rampant polygenicity is likely to decrease the effectiveness of selection on individual regulatory variants. If many variants affect the expression of a gene, a new mutation with a large effect may arise on a background with existing, compensatory genetic variation. Such background-effects may explain how the expression of common CNVs is similar between individuals with two and three gene copies.

Additionally, if gene regulation is highly polygenic, an eQTL may not reflect a single causal variant with the effect estimated during mapping. If multiple causal variants with concordant effects are in linkage disequilibrium in a sample, their effects may be aggregated into a single "synthetic" eQTL with a large effect [for more on synthetic associations, see Dickson *et al.* (2010)]. If the variants that comprise such a synthetic eQTL are not in linkage disequilibrium in the population, their effect sizes may individually be sufficiently small as to be nearly neutral. Future work is required to determine to what degree eQTLs represent groups of concordant, small-effect variants.

This challenge of polygenicity is not limited to the regulation of a single gene. If a fitness-relevant trait is affected by the expression of many genes, the fitness consequence of a variant that regulates a single gene is likely to be small. On the other hand, if a variant regulates multiple genes, and the resulting expression changes each affect fitness, the selection experienced by the variant will be a combination of the selection on each expression trait.

Such regulatory pleiotropy may also arise if the expression of a single gene affects multiple fitness-relevant traits. For example, altered gene expression may have different effects in different tissues. Therefore, a variant that affects the expression of a single gene may have multiple (and possibly opposing) effects on fitness. Interestingly, as the polygenicity of fitness-relevant traits (*e.g.*, the number of genes whose expression modulates the trait) increases, the likelihood that a single regulatory variant causes pleiotropic effects on multiple traits also increases.

In summary, a complex, pleiotropic gene expression network may make it difficult for selection to precisely alter the allele frequency of a single regulatory variant, even when its effects might be large and deleterious from the perspective of one gene expression trait in one tissue context. While there is much work to be done to connect gene expression to the one, or many, phenotypic traits seen by selection, we conclude that constraint has subtle, but detectable, effects on the genetic architecture of gene regulation.

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