

Article

Effect of Ho Addition on the Glass-Forming Ability and Crystallization Behaviors of $Zr_{54}Cu_{29}Al_{10}Ni_7$ Bulk Metallic Glass

Shuaidan Lu ¹, Xiaoxiao Li ¹, Xiaoyu Liang ¹, Jiahua He ¹, Wenting Shao ¹, Kuanhe Li ² and Jian Chen ^{1,*}

¹ School of Materials Science and Chemical Engineering, Xi'an Technological University, Xi'an 710021, China; lushuaidan@hotmail.com (S.L.); lixiaoxiao_stu@163.com (X.L.); liangxiaoyu@st.xatu.edu.cn (X.L.); hejiahua@xatu.edu.cn (J.H.); shaowenting@xatu.edu.cn (W.S.)

² School of Metallurgy, Northeastern University, Shenyang 110819, China; kevinlee579@outlook.com

* Correspondence: chenjian@xatu.edu.cn

Abstract: The effect of holmium (Ho) addition on the glass-forming ability (GFA) and crystallization behaviors of $Zr_{54}Cu_{29}Al_{10}Ni_7$ bulk metallic glass (BMGs) were studied by employing differential scanning calorimetry (DSC), X-ray diffraction (XRD), and transmission electron microscopy (TEM). The characteristic temperatures and activation energies of crystallization were obtained from DSC data. Classical kinetic modes were used to evaluate the crystallization processes of $Zr_{54}Cu_{29}Al_{10}Ni_7$ and $Zr_{48}Cu_{29}Ni_7Al_{10}Ho_6$ BMGs. The results showed that Ho addition reduces the activation energy in the original crystallization period of Zr-based BMG and improves the nucleation, which is due to the formation of simpler compounds, such as $CuZr_2$, Cu_2Ho , and Al_3Zr_5 .

Keywords: Zr-based metallic glasses; crystallization kinetic; holmium; activation energy



Citation: Lu, S.; Li, X.; Liang, X.; He, J.; Shao, W.; Li, K.; Chen, J. Effect of Ho Addition on the Glass-Forming Ability and Crystallization Behaviors of $Zr_{54}Cu_{29}Al_{10}Ni_7$ Bulk Metallic Glass. *Materials* **2022**, *15*, 2516.

<https://doi.org/10.3390/ma15072516>

Academic Editor: Philippe Colombari

Received: 15 February 2022

Accepted: 28 March 2022

Published: 29 March 2022

Publisher's Note: MDPI stays neutral with regard to jurisdictional claims in published maps and institutional affiliations.



Copyright: © 2022 by the authors. Licensee MDPI, Basel, Switzerland. This article is an open access article distributed under the terms and conditions of the Creative Commons Attribution (CC BY) license (<https://creativecommons.org/licenses/by/4.0/>).

1. Introduction

Zr-based bulk metallic glasses (BMGs) are considered to possess a widely utilized future as excellent structural materials in consumer electronics for their extraordinary fracture strengths, corrosion, and wear resistance [1–4]. In addition, the good glass-forming ability (GFA) of Zr-based BMGs allows thermoforming production above their glass transition temperature (T_g) [5–10]. However, the plasticity of Zr-based BMGs needs some improvement for commercial applications [11,12]. Recent investigations have reported that the plasticity of BMGs is enhanced in an amorphous composite by separating out micro-nano sized grains, which blocks the development of initial shear bands and forms abundant small-scale shear bands [13–15]. It is well known that crystallization of glasses is a very effective way of getting bulk nanocrystalline materials and crystal/glass composite [16–18]. Therefore, it is necessary to study the crystallization behavior of BMGs for the controllable preparation of crystal/glass composite.

Microalloying is widely used to improve the properties of alloys, especially those of metallic glasses [19–25]. Due to special chemical properties, rare earth elements are usually used as beneficial alloys additives to obtain better performance and are called “industrial monosodium glutamate” [26–29]. In our previous work, 1 at.% addition of rare earth Y was found to improve the GFA of Zr-based BMGs effectively and change the first crystallization phase of $Zr_{53.8}Cu_{29.1}Ni_{7.3}Al_{9.8}$ BMG from $Cu_{10}Zr_7$ to $CuZr_2$, which is beneficial to controlling the crystallization process and preparing bulk nanocrystalline alloys [30]. Microalloying of rare earth holmium (Ho) element was investigated to show beneficial effects on the GFA of Fe-based and Zr-based metallic glasses [26–29,31,32]. However, the addition of Ho in the literature is minimal and displayed limited understanding of microalloying effects of Ho [26–29,32]. In addition, the influence of Ho addition on the crystallization of metallic glasses has not been studied yet.

In this work, metallic glasses with composition of $Zr_{54-x}Cu_{29}Ni_7Al_{10}Ho_x$ ($x = 0, 1, 2, 4, 6$) were prepared and the influence of Ho addition on the GFA and crystallization behavior was systematically investigated. The characteristic temperatures and corresponding activation energies were calculated. Crystallization kinetics equations were fitted to evaluate the crystallization processes, and the phase changes were researched by employing X-ray diffraction (XRD) and transmission electron microscopy (TEM).

2. Materials and Methods

The $Zr_{54-x}Cu_{29}Ni_7Al_{10}Ho_x$ ($x = 0, 1, 2, 4, 6$) master alloy ingots were prepared with purity metals (99.99%), and designated as Zr54, Zr53Ho1, Zr52Ho2, Zr50Ho4, and Zr48Ho6. Each prepared ingot was remelted five times by electric arc melting. The Ti ingot was melted to ensure an oxygen-free atmosphere. Later, as-cast rods (diameter of 3 mm and length of 80 mm) were obtained by suction casting into a water-cooled copper mold following induction smelting. The amorphous structure of these alloys was identified by X-ray diffraction (XRD, Bruker D8, Bruker AXS, Karlsruhe, Germany, Cu-K α radiation). The crystallization peaks were measured by differential scanning calorimetry (DSC, STA449F3, Netzsch, Selb, Germany). The DSC tests of BMGs with different Ho additions were carried at a fixed heating rate of 10 K/min and the non-isothermal tests were carried at various heating rates of 5, 10, 20, 30, 40, and 50 K/min. The crystallization experiments in different duration were carried at 500 °C, and the corresponding phase changes were investigated by XRD and TEM (G20, FEI, Hillsboro, OR, USA). TEM samples were prepared by ion milling with the ion-beam voltage of 3.5 keV under the temperature of -40 °C to avoid structural change.

3. Results and Discussion

3.1. Structure and GFA of Metallic Glasses

Figure 1 is the XRD patterns of as cast $Zr_{54-x}Cu_{29}Ni_7Al_{10}Ho_x$ ($x = 0, 1, 2, 4, 6$) BMGs. All the patterns display the broad diffraction peaks in the range of $2\theta = 30$ – 50° , and there is no sharp peak observed in the patterns, implying the amorphous structure. To study the influence of Ho alloying on the GFA of $Zr_{54}Cu_{29}Ni_7Al_{10}$ BMG, DSC tests were conducted and the resulting curves are displayed in Figure 2. The glass transition temperature (T_g) and initial crystallization temperature (T_x) can be obtained from the DSC curves and summarized in Table 1. The super-cooled liquid region $\Delta T_x (=T_x - T_g)$ can also be calculated and listed in Table 1. It can be found that T_g and T_x both decrease with the increasing Ho addition. However, the drop of T_g is larger than that of T_x , leading to an increase of ΔT_x . The largest ΔT_x value of Zr48Ho6 BMG implies the greatest GFA. Based on the results of GFA, Zr₄₈Ho₆ BMG was selected to carry the further studies about crystallization kinetic of $Zr_{54}Cu_{29}Ni_7Al_{10}$ BMG.

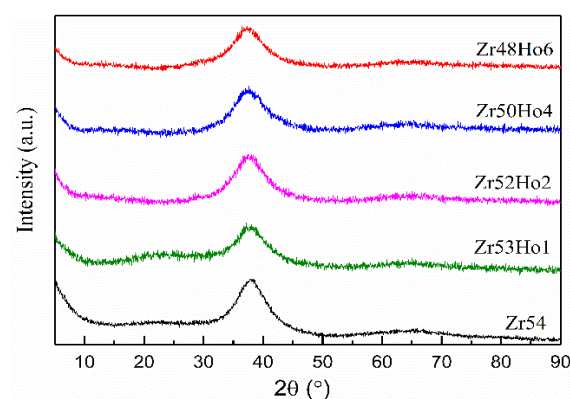


Figure 1. XRD patterns of $Zr_{54-x}Cu_{29}Ni_7Al_{10}Ho_x$ ($x = 0, 1, 2, 4, 6$) BMGs.

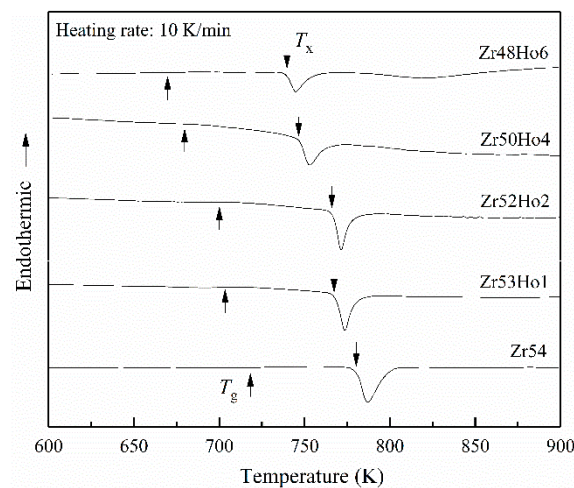


Figure 2. DSC curves of $Zr_{54-x}Cu_{29}Ni_7Al_{10}Ho_x$ ($x = 0, 1, 2, 4, 6$) BMGs.

Table 1. Thermal parameters of $Zr_{54-x}Cu_{29}Ni_7Al_{10}Ho_x$ ($x = 0, 1, 2, 4, 6$) BMGs.

| Composition (in at.%) | T_g (K) | T_x (K) | ΔT_x (K) |
|---------------------------------|-----------|-----------|------------------|
| $Zr_{54}Cu_{29}Ni_7Al_{10}$ | 718.7 | 780.1 | 61.4 |
| $Zr_{53}Cu_{29}Ni_7Al_{10}Ho_1$ | 703.5 | 767.2 | 63.7 |
| $Zr_{52}Cu_{29}Ni_7Al_{10}Ho_2$ | 700.1 | 765.3 | 65.2 |
| $Zr_{50}Cu_{29}Ni_7Al_{10}Ho_4$ | 679.7 | 746.2 | 66.5 |
| $Zr_{48}Cu_{29}Ni_7Al_{10}Ho_6$ | 669.5 | 739.4 | 69.9 |

3.2. Non-Isothermal Crystallization Kinetics

Figure 3 shows the DSC traces of Zr_{54} and $Zr_{48}Ho_6$ BMGs achieved at various heating rates. All the DSC traces show the glass transition characters and exothermic peaks of crystallization. The characteristic temperatures are pointed in Figure 3 and listed in Table 2. As seen in Figure 3, the exothermic peaks move to higher temperatures with the raising heating rate. The characteristic temperatures also become higher at the faster heating rate, indicating an obvious correlation between crystallization and the heating rate, because the crystallization consists of the nucleation and the growth of grains, which are the thermally activated process. In addition, it can also be found in Table 2 that T_g increases more slowly than T_x , leading to the improved ΔT_x .

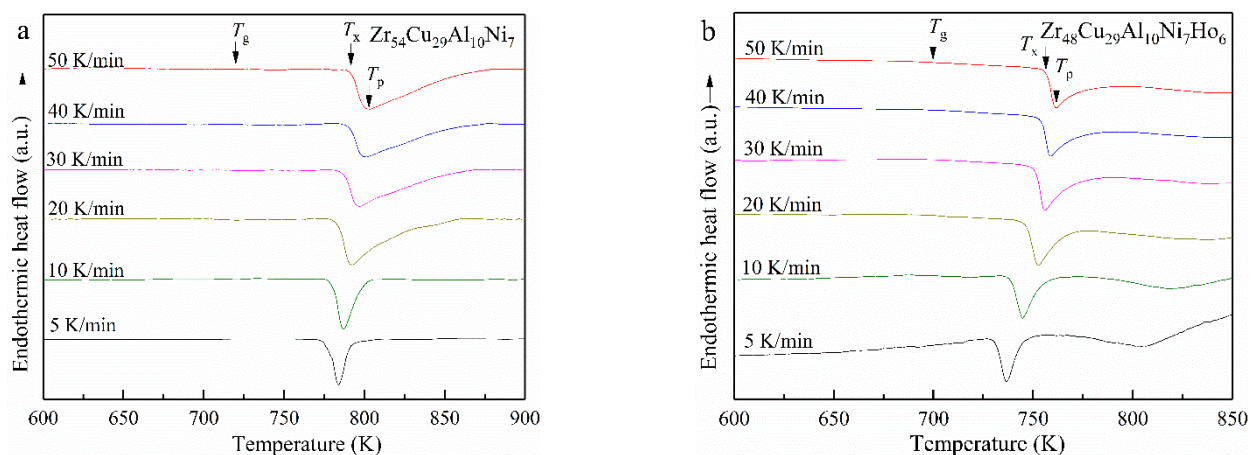
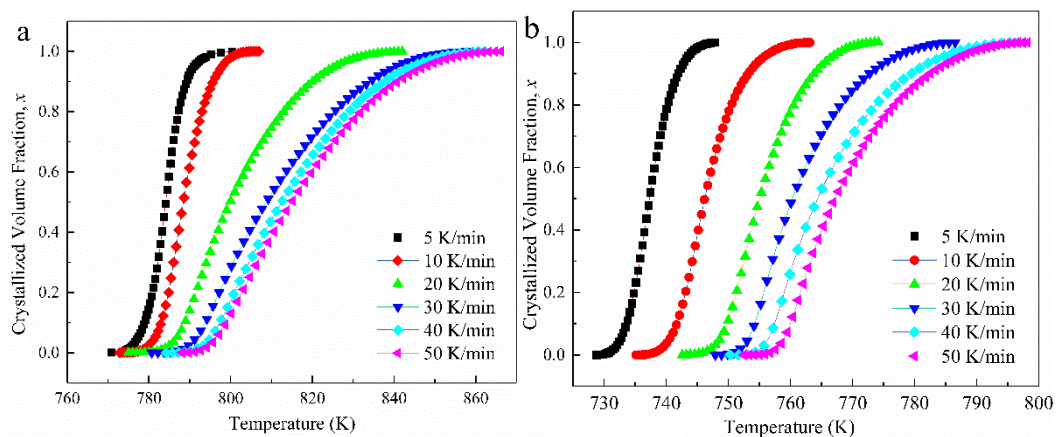


Figure 3. DSC results of Zr_{54} (a) and $Zr_{48}Ho_6$ (b) BMGs at various heating rates.

Table 2. Characteristic temperatures of Zr₅₄ BMG and Zr₄₈Ho₆ BMG at various heating rates.

| Heating Rate (K/min) | Zr ₅₄ Cu ₂₉ Ni ₇ Al ₁₀ | | | | Zr ₄₈ Cu ₂₉ Ni ₇ Al ₁₀ Ho ₆ | | | |
|----------------------|--|--------------------|--------------------|---------------------|--|--------------------|--------------------|---------------------|
| | T _g (K) | T _x (K) | T _p (K) | ΔT _x (K) | T _g (K) | T _x (K) | T _p (K) | ΔT _x (K) |
| 5 | 716.2 | 775.4 | 783.79 | 59.2 | 663.3 | 731.4 | 736.71 | 68.1 |
| 10 | 718.7 | 780.1 | 787.1 | 61.4 | 669.5 | 739.4 | 744.65 | 69.9 |
| 20 | 719.4 | 783.6 | 792.39 | 64.2 | 674.65 | 746.25 | 752.59 | 71.6 |
| 30 | 721 | 787.7 | 796.47 | 66.7 | 677.97 | 751.27 | 755.87 | 73.3 |
| 40 | 722.4 | 791.4 | 800.57 | 69 | 679.39 | 754.89 | 758.51 | 75.5 |
| 50 | 722.5 | 791.6 | 802.93 | 69.1 | 680.04 | 756.84 | 761.51 | 76.8 |

The volume fraction of crystallization, x , could be calculated using DSC results by taking the line integral of the crystallization peak. When temperature T is fixed, the corresponding x can be obtained by $x = S_T/S_p$, where S_p represents the total area of exothermic peak, and S_T represents the area below the peak curve between the initial temperature and the fixed temperature T . The obtained crystallized fraction x is plotted in Figure 4 and displays the classic S-shape, which illustrates the process of non-isothermal crystallization [33–35].

**Figure 4.** Crystallized fraction x corresponding temperature at different heating rates (a) Zr₅₄ BMG and (b) Zr₄₈Ho₆ BMG.

3.3. Effective Activation Energy

The effective activation energy, E , can be calculated from DSC results by using a Kissinger Equation (1) [36] and Ozawa Equation (2) [37]:

$$\ln(\beta/T^2) = -E/RT + C \quad (1)$$

$$\ln \beta = -E/RT + C \quad (2)$$

In the equations, β is the rate of raising temperature, T is characteristic temperature, and R is gas constant. The Kissinger results $\ln(\beta/T^2)$ and Ozawa results $\ln(\beta)$ against $1000/RT$ are shown as scattered points in Figure 5. Each set of data is linearly fitted, and the corresponding results are also displayed in Figure 5. According to the Kissinger and Ozawa equations above, the slope obtained from linear fitting is E/R , and the corresponding activation energies for Zr₅₄ and Zr₄₈Ho₆ BMGs are calculated from the slopes and summarized in Table 3. As seen in Table 3, the values obtained by Ozawa equation are in good agreement with those obtained by a Kissinger equation, and are merely a little bit higher.

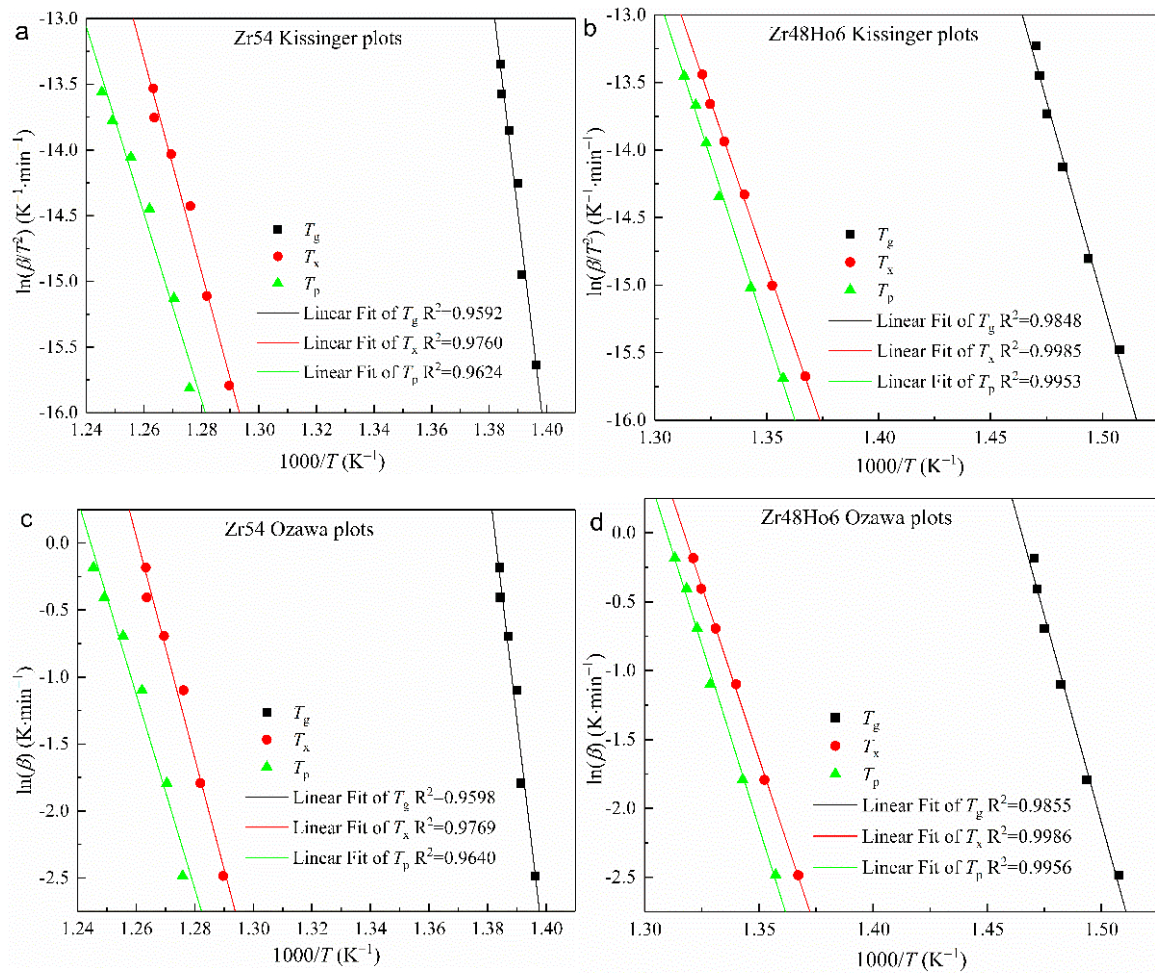


Figure 5. Kissinger and Ozawa plots of (a,c) Zr54 BMG and (b,d) Zr48Ho6 BMG.

Table 3. Activation energies obtained by two equations for Zr54 BMG and Zr48Ho6 BMG.

| Equations | Zr ₅₄ Cu ₂₉ Ni ₇ Al ₁₀ | | | Zr ₄₈ Cu ₂₉ Ni ₇ Al ₁₀ Ho ₆ | | |
|-----------|--|-------------------|-------------------|--|-------------------|-------------------|
| | E_g (kJ/mol) | E_x (kJ/mol) | E_p (kJ/mol) | E_g (kJ/mol) | E_x (kJ/mol) | E_p (kJ/mol) |
| Kissinger | 1525.07 | 675.67 | 590.68 | 488.87 | 402.43 | 427.39 |
| Ozawa | 1537.03 | 688.71 | 603.87 | 500.04 | 414.80 | 439.84 |

It is known that E_g , E_x , and E_p represent the energy barriers to overcome for glass transition, nucleation, and growth of crystal. It can be found in Table 3 that E_g is much greater than others, implying the greater energy barrier to overcome for atomic rearrangement. Comparing with E_g of Zr48Ho6 (488.87 kJ/mol and 500.04 kJ/mol), E_g of Zr54 obtained by Kissinger and Ozawa methods are 1525.07 kJ/mol and 1537.03 kJ/mol, and much larger, implying a more difficult atomic rearrangement. It can also be found that E_x is larger than E_p for Zr54 BMG, indicating the hard nucleation and easy grain growth. However, E_x is smaller than E_p for Zr48Ho6 BMG, implying the easy nucleation and hard growth. The transformation should be attributed to the changes of crystallization products caused by Ho alloying.

3.4. Effective Activation Energy

The activation energy obtained from T_p just roughly evaluates the crystallization process. However, as the nucleation and growth of metallic glass are complicated, the activation energy over the total crystallization process is not fixed. The local activation

energy against crystallized fraction x , $E_c(x)$, was proposed to evaluate the whole crystallization process. It can be calculated by the Doyle–Ozawa isoconversional equation (seen in Equation (3)) [38,39]. The results are displayed in Figure 6 and show two quite different tendencies of $E_c(x)$ for two BMGs. $E_c(x)$ for Zr54 reaches a peak point of 660.40 kJ/mol in the original period and next declines immediately to 600.84 kJ/mol at $x = 1\%$; thereafter, it unceasingly declines with the increasing x and lastly finishes at 174.06 kJ/mol ($x = 99.5\%$). Meanwhile, $E_c(x)$ for Zr48Ho6 drops from the peak point of 412.17 kJ/mol at the original point to 385.50 kJ/mol at x reaches 1%; next, $E_c(x)$ declines continuously in the following process and ends up with 222.92 kJ/mol at $x = 99.4\%$. The mean activation energy for Zr54 and Zr48Ho6 BMGs during the whole crystallization process are 366.43 kJ/mol and 332.33 kJ/mol, respectively, less than the values calculated by the Kissinger and Ozawa equations. Similar results are reported in the crystallization behaviors of some other metallic glasses [38–40]. Comparing with Zr54 BMG, $E_c(x)$ for Zr48Ho6 is smaller in the original period and larger in the second half process, implying an easier nucleation and more difficult development. These are in good agreement with the results obtained from Kissinger and Ozawa methods:

$$\ln \beta = -1.0516E_c(x)/RT + C \quad (3)$$

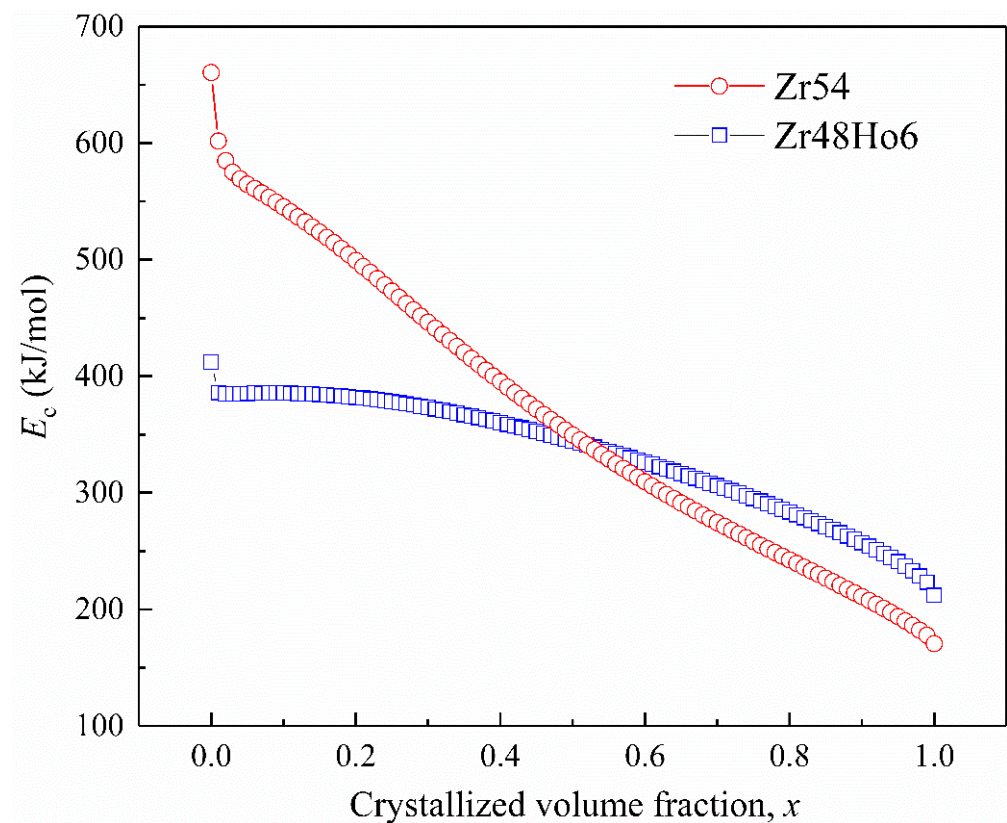


Figure 6. Local activation energies corresponding to crystallized fraction for Zr54 and Zr48Ho6 BMGs.

3.5. Crystallization Mechanism

The solid-state reaction can be described by the following equation:

$$dx/dt = k(T)f(x) \quad (4)$$

where x is the crystallized fraction, t is the duration, T is the reaction temperature, $f(x)$ is set as an expression describing the crystallization process, and $k(T)$ is a constant dependent on temperature and can be obtained by the Arrhenius model [41]:

$$k(T) = A \exp(-E_c/RT), \tag{5}$$

where A is frequency factor, and E_c is crystallization activation energy. Combining Equation (4) with Equation (5), the following equation can be obtained:

$$\ln(dx/dt) + E_c/RT = \ln[Af(x)]. \tag{6}$$

Based on Equation (6), the value of $\ln[Af(x)]$ can be obtained from crystallized fraction and activation energy of T_p (calculated by the Kissinger equation and seen in Table 3). Because the curves of crystallized fraction were varied at various heating rates, the mean values of $\ln[Af(x)]$ were taken to describe the crystallization and plotted as scatters (hollow circles) in Figure 7. The Johnson–Mehl–Avrami (JMA) mode and normal grain growth (NGG) mode in Table 4 were employed to evaluate the experimental data [42,43]. The fitted curves are in red and dotted lines, and the corresponding results are listed in Figure 7.

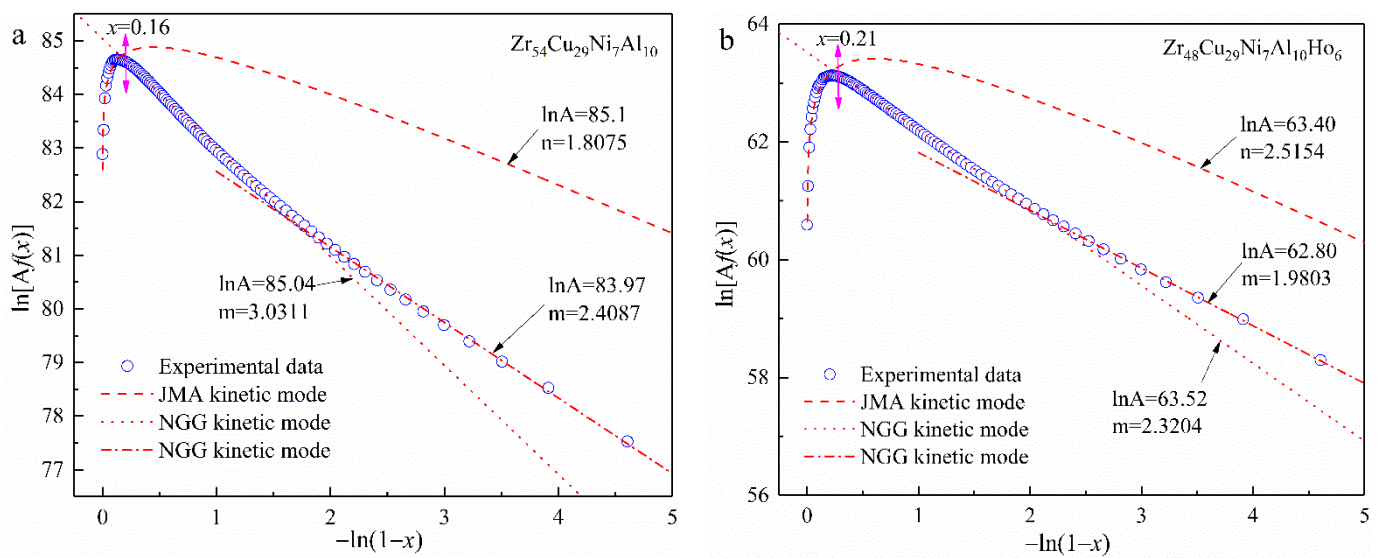


Figure 7. Curves representing crystallization mechanisms of (a) Zr54 BMG and (b) Zr48Ho6 BMG.

Table 4. Theoretical kinetic modes considered.

| Model | $f(x)$ | Label |
|---------------------------|--------------------------------------|-------|
| Johnson–Mehl–Avrami (JMA) | $n(1 - x)[- \ln(1 - x)]^{(n - 1)/n}$ | n |
| Normal grain growth (NGG) | $(1 - x)^{m + 1}$ | m |

As seen in Figure 7a that the crystallization of Zr54 BMG firstly obeys the JMA-mode with $n = 1.8075$ for $x < 0.16$, then the crystallization transforms to obey two NGG-modes ($m = 3.0311$ and 2.4087). As seen in Figure 7b, the crystallization of Zr48Ho6 BMG starts with the JMA-mode with a greater $n = 2.5154$ for $x < 0.21$; later, the remaining crystallization follows two NGG straight lines with less $m = 2.3204$ and 1.9803 , respectively.

As is known to all, the JMA mode describes the precipitation process from nucleation to growth, which commonly takes place in the original period of precipitation. The value of JMA exponent n for Zr54 BMG is <2.5 , suggesting a growth in three dimensions and a lowering nucleation controlled by diffusion [43]. However, the JMA exponent value of Zr48Ho6 BMG is >2.5 , implying a growth in three dimensions and rising nucleation controlled by diffusion. Comparing with Zr54 BMG, the greater JMA exponent of Zr48Ho6 BMG implies a faster nucleation rate. Moreover, the JMA-mode stage of Zr48Ho6 BMG keeps to $x = 0.21$ and is longer than that of Zr54 BMG ($x = 0.16$), suggesting the more nucleation in Zr48Ho6 BMG. This result is consistent with the less E_x for Zr48Ho6 BMG

achieved by the Kissinger method and the Doyle–Ozawa isoconversional method. The developed nucleation should be due to micro-alloying of rare earth, which raises the viscosity of super cooled liquid and lowers the driving force of nucleation [44].

In the follow-up period, the crystallization of Zr54 and Zr48Ho6 BMGs both follow the NGG-mode. Comparing with Zr54 BMG, the lesser NGG exponent of Zr48Ho6 BMG suggests decelerated growth of grain. It indicates that 6 at.% addition of Ho has the tardiness effect on the growth of grain and is beneficial to prepare bulk nanocrystalline alloys by controlling the crystallization process [45].

3.6. Structural Analysis of the Crystallized Alloys

To explain the different crystallization mechanisms of two BMGs, the structure of two alloys annealed at 500 °C was investigated by XRD, and the obtained spectra are analyzed in Figure 8. There is a large amount of CuZr_2 , $\text{Ni}_{10}\text{Zr}_7$, Cu_2Ho , Al_3Zr_5 , and Al_3Zr were formed on Zr48Ho6 BMG annealed at 500 °C for 20 min, while $\text{Cu}_{10}\text{Zr}_7$ and few Al_2Zr were detected on Zr54 BMG after 20 min annealing treatment. The results of 40 min annealing indicate that these primary grains grow up with the continuous annealing. It is obvious that the crystallization processes of two BMGs are essentially different. The formation of Cu_2Ho on Zr48Ho6 BMG is attributed to the addition of Ho, which leads to the reduced Cu atoms combining with Zr atoms, and then causes the precipitation of CuZr_2 , $\text{Ni}_{10}\text{Zr}_7$, and Al_3Zr_5 . The results indicate that Ho tends to combine with Cu rather than other elements. According to the mixing enthalpy between elements in Figure 9, the mixing enthalpies of Ni–Ho and Al–Ho are more negative than that of Cu–Ho, but less negative than those of Ni–Zr, Ni–Al, and Zr–Al. Ni will combine preferentially with Zr and Al, and Al will combine preferentially with Zr and Ni, rather than Ho. Therefore, Ho combined preferentially with Cu to form precipitates. Meanwhile, Zr–Cu, Zr–Ni, and Zr–Al also preferentially form the corresponding compounds, which is consistent with the XRD results.

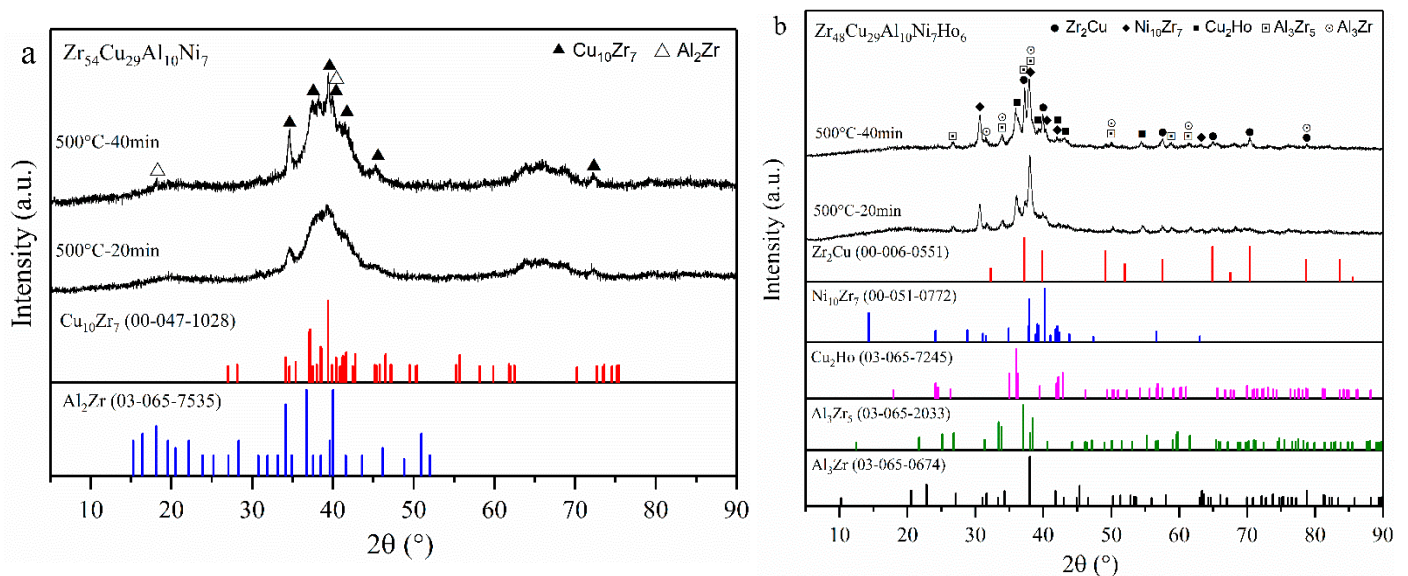


Figure 8. XRD patterns of (a) Zr54 BMG and (b) Zr48Ho6 BMG annealed at 500 °C for various times.

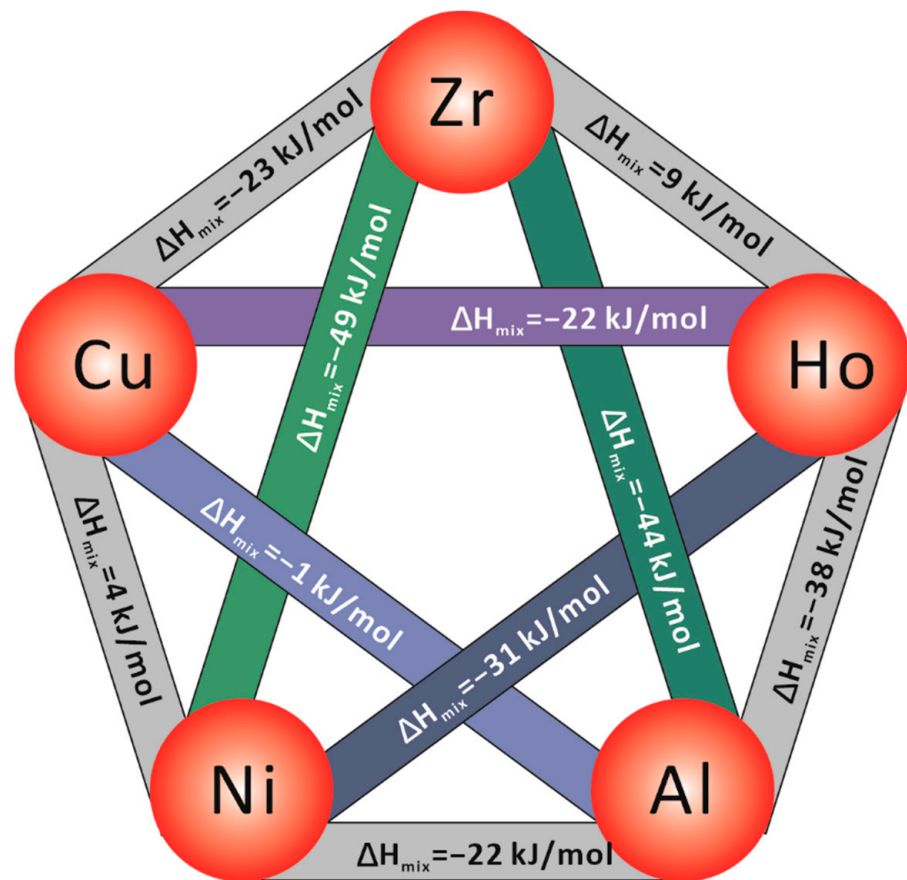


Figure 9. Mixing enthalpy between constituent elements in the Zr-Cu-Ni-Al-Ho system.

Figure 10 exhibits the TEM photographs of Zr₅₄ and Zr₄₈Ho₆ BMGs after 20 min of annealing at 500 °C, and the corresponding selected area electron diffraction (SAED) patterns in the upper right corner. As shown in Figure 10a, there are scattered precipitates, roughly 3050 nm, that appear in Zr₅₄ BMG. The SAED pattern shows many diffraction spots and indicates the formation of Cu₁₀Zr₇ and Al₂Zr. The TEM image of Zr₄₈Ho₆ in Figure 10b also shows a well-ordered polycrystalline structure with immense amounts of precipitates. The SAED pattern indicates the existence of CuZr₂, Ni₁₀Zr₇, and Cu₂Ho phases. Compared with the XRD analysis of annealed alloys, it could be inferred that the crystallization mechanism of Zr₅₄ BMG is changed by Ho addition. It has been found in the nucleation mechanism of Zr-Cu-Al BMGs, which could be divided into two categories: CuZr₂-type and Cu₁₀Zr₇-type [46]. CuZr₂-type represents the lower free energy barrier and easy nucleation, attributing to the simple space unit of CuZr₂. A Cu₁₀Zr₇-type implies a more chemically and topologically disordered crystal structure, resulting in much harder nucleation. The similar result has also been found in our previous work about the influence of Y alloying on the crystallization behavior of Zr-based BMGs [30]. In this work, it is clear that Ho addition reduces the free energy barrier of nucleation and leads to the formation of simple phases, such as CuZr₂ and Cu₂Ho. This is in good agreement with the less activation energy E_x and the improved nucleation in JMA mode obtained above. As the initial crystallized phase is mainly of Cu₁₀Zr₇, the crystallization of Zr₅₄ BMG belongs to Cu₁₀Zr₇-type. Compared with the addition of Y, the alloying of Ho led to the different precipitates Cu₂Ho, which resulted in the difference of crystallized products and the corresponding proportion [30]. Then, the nanocrystalline alloy with different structures and properties can be obtained.

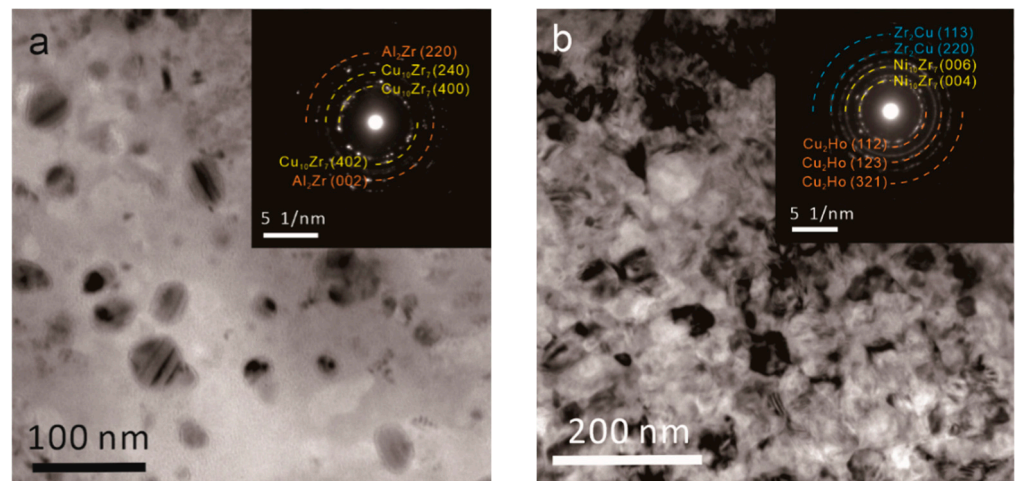


Figure 10. TEM images and the corresponding SAED results of (a) Zr54 BMG and (b) Zr48Ho6 BMG annealed at 500 °C for 20 min.

4. Conclusions

The influences of Ho addition on the GFA and crystallization process of $Zr_{54}Cu_{29}Al_{10}Ni_7$ BMGs were studied. The results were concluded to be as follows:

- (1) The crystallization behavior of Zr54 BMG was changed by Ho addition. The non-isothermal DSC studies showed a good correlation between characteristic temperatures and heating rate.
- (2) The Kissinger, Ozawa, and Doyle–Ozawa isoconversional methods all provided less activation energy at the initial crystallization point of Zr48Ho6 BMG, indicating the much easier nucleation.
- (3) The crystallization of Zr54 and Zr48Ho6 BMG both firstly obeyed the JMA-mode and then changed to obey the NGG-mode. The larger JMA exponent of Zr48Ho6 BMG implies the improved nucleation. The smaller NGG exponents for the following crystallization of Zr48Ho6 BMG mean a slower growth rate of precipitates.
- (4) The XRD and TEM analyses indicated that the initial crystallized products of Zr48Ho6 BMG were simple compounds, such as $CuZr_2$, Cu_2Ho , and Al_3Zr_5 , while the initial crystallization of Zr54 BMG was the formation of $Cu_{10}Zr_7$ with a complex structure.

Author Contributions: Conceptualization, S.L. and J.C.; methodology, X.L. (Xiaoyu Liang); validation, J.H. and W.S.; formal analysis, X.L. (Xiaoxiao Li); investigation, X.L. (Xiaoxiao Li) and X.L. (Xiaoyu Liang); resources, X.L. (Xiaoxiao Li) and X.L. (Xiaoyu Liang); writing—original draft preparation, S.L.; visualization, S.L.; writing—review and editing, K.L.; supervision, J.C.; project administration, J.C. All authors have read and agreed to the published version of the manuscript.

Funding: This work was financially supported by the National Natural Science Foundation of China (Grant Nos. 51931005, 52071251, 52101093), the Shaanxi Outstanding Youth Fund (2020JC-49) and Youth Innovation Team of University in Shaanxi Province, Natural Science Basic Research Program of Shaanxi (Program No. 2021JQ-645), and the Scientific Research Program Funded by the Shaanxi Provincial Education Department (Program No. 20JK0684, 21JP053).

Institutional Review Board Statement: This study did not involve humans or animals and did not require ethical approval.

Informed Consent Statement: The study did not involve humans.

Conflicts of Interest: The authors declare no conflict of interest. The funders had no role in the design of the study; in the collection, analyses, or interpretation of data; in the writing of the manuscript, or in the decision to publish the results.

References

1. Tan, Y.; Wang, Y.W.; Cheng, X.W.; Fu, Q.; Xin, Z.H.; Xu, Z.Q.; Cheng, H.W. Effects of Al replacement on glass forming ability and mechanical properties of Zr-based bulk metallic glasses. *J. Non-Cryst. Solids* **2021**, *568*, 120962. [[CrossRef](#)]
2. Jin, Z.S.; Yang, Y.J.; Zhang, Z.P.; Ma, X.Z.; Lv, J.W.; Wang, F.L.; Ma, M.Z.; Zhang, X.Y.; Liu, R.P. Effect of Hf substitution Cu on glass-forming ability, mechanical properties and corrosion resistance of Ni-free Zr–Ti–Cu–Al bulk metallic glasses. *J. Alloy Compd.* **2019**, *806*, 668–675. [[CrossRef](#)]
3. Gao, W.J.; Zhang, W.W.; Zhang, T.; Yang, C.; Huang, X.S.; Liu, Z.Y.; Wang, Z.; Li, W.H.; Li, W.R.; Li, L.; et al. Large tensile plasticity in Zr-based metallic glass/stainless steel interpenetrating-phase composites prepared by high pressure die casting. *Compos. Part B Eng.* **2021**, *224*, 109226. [[CrossRef](#)]
4. Liu, L.H.; Ma, J.; Yu, C.Y.; Huang, X.S.; He, L.J.; Zhang, L.C.; Li, P.J.; Liu, Z.Y. Determination of forming ability of high pressure die casting for Zr-based metallic glass. *J. Mater. Process. Tech.* **2017**, *244*, 87–96. [[CrossRef](#)]
5. Frey, M.; Wegner, J.; Neuber, N.; Reiplinger, B.; Bochtler, B.; Adam, B.; Ruschel, L.; Riegler, S.S.; Jiang, H.-R.; Kleszczynski, S.; et al. Thermoplastic forming of additively manufactured Zr-based bulk metallic glass: A processing route for surface finishing of complex structures. *Mater. Des.* **2021**, *198*, 109368. [[CrossRef](#)]
6. Monfared, A.; Liu, W.; Zhang, L. On the adhesion between metallic glass and dies during thermoplastic forming. *J. Alloy Compd.* **2017**, *711*, 235–242. [[CrossRef](#)]
7. Li, J.; Li, C.; Wang, S.; Wang, H.; Kou, S. Thermal processing map and thermoplastic forming map of Zr-based bulk metallic glass in the supercooled liquid region. *J. Non-Cryst. Solids* **2021**, *570*, 121008. [[CrossRef](#)]
8. Li, N.; Chen, Y.; Jiang, M.Q.; Li, D.J.; He, J.J.; Wu, Y.; Liu, L. A thermoplastic forming map of a Zr-based bulk metallic glass. *Acta Mater.* **2013**, *61*, 1921–1931. [[CrossRef](#)]
9. Hu, Q.; Fu, M.W.; Zeng, X.R. Evaluation of thermoplastic formability of Zr-based bulk metallic glasses and its correlation with characteristic temperature parameters. *J. Alloy Compd.* **2014**, *602*, 326–330. [[CrossRef](#)]
10. Li, J.B.; Zhang, H.Z.; Jang, J.S.C.; Jian, S.R.; Li, C.; Huang, J.C.; Nieh, T.G. Viscous flow and thermoplastic forming ability of a Zr-based bulk metallic glass composite with Ta dispersoids. *J. Alloy Compd.* **2012**, *536*, S165–S170. [[CrossRef](#)]
11. Wang, F.; Yin, D.; Lv, J.; Zhang, S.; Ma, M.; Zhang, X.; Liu, R. Effect on microstructure and plastic deformation behavior of a Zr-based amorphous alloy by cooling rate control. *J. Mater. Sci. Technol.* **2021**, *82*, 1–9. [[CrossRef](#)]
12. Zhang, L.; Wang, T.; Hou, Q.; Hao, Q.; Qiao, J. Deformation-induced microstructural heterogeneity and rejuvenation in a Zr-based bulk metallic glass. *J. Non-Cryst. Solids* **2021**, *574*, 121148. [[CrossRef](#)]
13. Jia, H.; Wang, G.; Chen, S.; Gao, Y.; Li, W.; Liaw, P.K. Fatigue and fracture behavior of bulk metallic glasses and their composites. *Prog. Mater. Sci.* **2018**, *98*, 168–248. [[CrossRef](#)]
14. Ding, H.; Bao, X.; Jamili-Shirvan, Z.; Jin, J.; Deng, L.; Yao, K.; Gong, P.; Wang, X. Enhancing strength-ductility synergy in an ex situ Zr-based metallic glass composite via nanocrystal formation within high-entropy alloy particles. *Mater. Des.* **2021**, *210*, 110108. [[CrossRef](#)]
15. Duan, G.H.; Jiang, M.Q.; Liu, X.F.; Dai, L.H.; Li, J.X. In-situ observations on shear-banding process during tension of a Zr-based bulk metallic glass composite with dendrites. *J. Non-Cryst. Solids* **2021**, *565*, 120841. [[CrossRef](#)]
16. Czel, G.; Tomolya, K.; Sveda, M.; Sycheva, A.; Kristaly, F.; Rooszy, A.; Janovszky, D. Synthesis and characterization of Zr-based in situ crystal precipitated and liquid phase separated bulk metallic glass composite. *J. Non-Cryst. Solids* **2017**, *458*, 41–51. [[CrossRef](#)]
17. Orava, J.; Kaban, I.; Benkocka, M.; Han, X.; Soldatov, I.; Greer, A.L. Fast-heating-induced formation of metallic-glass/crystal composites with enhanced plasticity. *Thermochim. Acta* **2019**, *677*, 198–205. [[CrossRef](#)]
18. Madge, S.V.; Louzguine-Luzgin, D.V.; Kawashima, A.; Greer, A.L.; Inoue, A. Compressive plasticity of a La-based glass-crystal composite at cryogenic temperatures. *Mater. Des.* **2016**, *101*, 146–151. [[CrossRef](#)]
19. Luo, L.S.; Wang, B.B.; Dong, F.Y.; Su, Y.Q.; Guo, E.Y.; Xu, Y.J.; Wang, M.Y.; Wang, L.; Yu, J.X.; Ritchie, R.O.; et al. Structural origins for the generation of strength, ductility and toughness in bulk-metallic glasses using hydrogen microalloying. *Acta Mater.* **2019**, *171*, 216–230. [[CrossRef](#)]
20. Granata, D.; Fischer, E.; Löffler, J.F. Effectiveness of hydrogen microalloying in bulk metallic glass design. *Acta Mater.* **2015**, *99*, 415–421. [[CrossRef](#)]
21. Gendelman, O.; Joy, A.; Mishra, P.; Procaccia, I.; Samwer, K. On the effect of microalloying on the mechanical properties of metallic glasses. *Acta Mater.* **2014**, *63*, 209–215. [[CrossRef](#)]
22. Wang, W.H. Roles of minor additions in formation and properties of bulk metallic glasses. *Prog. Mater. Sci.* **2007**, *52*, 540–596. [[CrossRef](#)]
23. Xue, L.; Shao, L.; Han, Z.; Luo, Q.; Wang, H.; Huo, J.; Li, Z.; Zhang, B.; Cheng, J.; Shen, B. Tunable magnetocaloric effect in Gd-based metallic glasses microalloying elements with different magnetism. *J. Non-Cryst. Solids* **2022**, *576*, 121222. [[CrossRef](#)]
24. Sohrabi, S.; Gholamipour, R. Effect of Nb minor addition on the crystallization kinetics of Zr–Cu–Al–Ni metallic glass. *J. Non-Cryst. Solids* **2021**, *560*, 120731. [[CrossRef](#)]
25. Cheng, Y.; Chen, C.; Li, X.; Zhang, T. Microalloying-induced large plasticity in La–Al–C bulk metallic glass. *J. Non-Cryst. Solids* **2016**, *447*, 55–58. [[CrossRef](#)]
26. Pang, C.M.; Chen, L.; Xu, H.; Guo, W.; Lv, Z.W.; Huo, J.T.; Cai, M.J.; Shen, B.L.; Wang, X.L.; Yuan, C.C. Effect of Dy, Ho, and Er substitution on the magnetocaloric properties of Gd–Co–Al–Y high entropy bulk metallic glasses. *J. Alloy Compd.* **2020**, *827*, 154101. [[CrossRef](#)]

27. Hu, F.; Yuan, C.; Luo, Q.; Yang, W.; Shen, B. Effects of Ho addition on thermal stability, thermoplastic deformation and magnetic properties of FeHoNbB bulk metallic glasses. *J. Alloy Compd.* **2019**, *807*, 151675. [[CrossRef](#)]
28. Li, J.; Law, J.Y.; Huo, J.; He, A.; Man, Q.; Chang, C.; Men, H.; Wang, J.; Wang, X.; Li, R.-W. Magnetocaloric effect of Fe-RE-B-Nb (RE=Tb, Ho or Tm) bulk metallic glasses with high glass-forming ability. *J. Alloy Compd.* **2015**, *644*, 346–349. [[CrossRef](#)]
29. Pang, C.M.; Yuan, C.C.; Chen, L.; Xu, H.; Guo, K.; He, J.C.; Li, Y.; Wei, M.S.; Wang, X.M.; Huo, J.T.; et al. Effect of Yttrium addition on magnetocaloric properties of Gd-Co-Al-Ho high entropy metallic glasses. *J. Non-Cryst. Solids* **2020**, *549*, 120354. [[CrossRef](#)]
30. Lu, S.; Sun, S.; Li, K.; Li, H.; Huang, X.; Tu, G. The effect of Y addition on the crystallization behaviors of Zr-Cu-Ni-Al bulk metallic glasses. *J. Alloy Compd.* **2019**, *799*, 501–512. [[CrossRef](#)]
31. Luo, C.Y.; Zhao, Y.H.; Xi, X.K.; Wang, G.; Zhao, D.Q.; Pan, M.X.; Wang, W.H.; Kou, S.Z. Making amorphous steel in air by rare earth microalloying. *J. Non-Cryst. Solids* **2006**, *352*, 185–188. [[CrossRef](#)]
32. Zhang, H.; Li, R.; Ji, Y.; Liu, F.; Luo, Q.; Zhang, T. Glass formation, magnetic properties and magnetocaloric effect of ternary Ho-Al-Co bulk metallic glass. *J. Magn. Magn. Mater.* **2012**, *324*, 4064–4067. [[CrossRef](#)]
33. Han, X.; Ding, F.; Qin, Y.; Wu, D.; Xing, H.; Shi, Y.; Song, K.; Cao, C. Compositional dependence of crystallization kinetics in Zr-Ni-Al metallic glasses. *Vacuum* **2018**, *151*, 30–38. [[CrossRef](#)]
34. Jamili-Shirvan, Z.; Haddad-Sabzevar, M.; Vahdati-Khaki, J.; Yao, K.-F. Non-isothermal crystallization kinetics investigation of different zones at the joining area of a bulk metallic glass welded by friction stir spot welding (FSSW). *J. Non-Cryst. Solids* **2020**, *533*, 119904. [[CrossRef](#)]
35. Dołęga, A.; Zieliński, P.M. Kinetics of non-isothermal cold-crystallization of carbamazepine in the glassy state studied by DSC. *J. Non-Cryst. Solids* **2022**, *575*, 121198. [[CrossRef](#)]
36. Kissinger, H.E. Reaction Kinetics in Differential Thermal Analysis. *Anal. Chem.* **1957**, *29*, 1702–1706. [[CrossRef](#)]
37. Ozawa, T. Kinetic analysis of derivative curves in thermal analysis. *J. Therm. Anal.* **1970**, *2*, 301–324. [[CrossRef](#)]
38. Zhuang, Y.; Xing, P.; Duan, T.; Shi, H.; He, J. Kinetic study on the non-isothermal crystallization of Gd₅₃Al₂₄Co₂₀Zr₃ bulk metallic glass. *J. Rear Earth* **2011**, *29*, 793–797. [[CrossRef](#)]
39. Mohammadi Rahvard, M.; Tamizifar, M.; Boutorabi, S.M.A. The effect of Ag addition on the non-isothermal crystallization kinetics and fragility of Zr₅₆Co₂₈Al₁₆ bulk metallic glass. *J. Non-Cryst. Solids* **2018**, *481*, 74–84. [[CrossRef](#)]
40. Yuan, Z.-Z.; Chen, X.-D.; Wang, B.-X.; Wang, Y.-J. Kinetics study on non-isothermal crystallization of the metallic Co₄₃Fe₂₀Ta_{5.5}B_{31.5} glass. *J. Alloy Compd.* **2006**, *407*, 163–169. [[CrossRef](#)]
41. Málek, J. The shape of thermoanalytical curves as a function of the reaction kinetics. *Thermochim. Acta* **1993**, *222*, 105–113. [[CrossRef](#)]
42. Atkinson, H.V. Overview no. 65: Theories of normal grain growth in pure single phase systems. *Acta Metall.* **1988**, *36*, 469–491. [[CrossRef](#)]
43. Málek, J. The applicability of Johnson-Mehl-Avrami model in the thermal analysis of the crystallization kinetics of glasses. *Thermochim. Acta* **1995**, *267*, 61–73. [[CrossRef](#)]
44. Wang, Q.; Liu, C.T.; Yang, Y.; Liu, J.B.; Dong, Y.D.; Lu, J. The atomic-scale mechanism for the enhanced glass-forming-ability of a Cu-Zr based bulk metallic glass with minor element additions. *Sci. Rep.* **2014**, *4*, 4648. [[CrossRef](#)] [[PubMed](#)]
45. Illeková, E. FINEMET-type nanocrystallization kinetics. *Thermochim. Acta* **2002**, *387*, 47–56. [[CrossRef](#)]
46. Lan, S.; Wu, Z.; Wei, X.; Zhou, J.; Lu, Z.; Neuefeind, J.; Wang, X.-L. Structure origin of a transition of classic-to-avalanche nucleation in Zr-Cu-Al bulk metallic glasses. *Acta Mater.* **2018**, *149*, 108–118. [[CrossRef](#)]