

# Regulation of Ion Gradients across Myocardial Ischemic Border Zones: A Biophysical Modelling Analysis

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## Abstract

The myocardial ischemic border zone is associated with the initiation and sustenance of arrhythmias. The profile of ionic concentrations across the border zone play a significant role in determining cellular electrophysiology and conductivity, yet their spatial-temporal evolution and regulation are not well understood. To investigate the changes in ion concentrations that regulate cellular electrophysiology, a mathematical model of ion movement in the intra and extracellular space in the presence of ionic, potential and material property heterogeneities was developed. The model simulates the spatial and temporal evolution of concentrations of potassium, sodium, chloride, calcium, hydrogen and bicarbonate ions and carbon dioxide across an ischemic border zone. Ischemia was simulated by sodium-potassium pump inhibition, potassium channel activation and respiratory and metabolic acidosis. The model predicted significant disparities in the width of the border zone for each ionic species, with intracellular sodium and extracellular potassium having discordant gradients, facilitating multiple gradients in cellular properties across the border zone. Extracellular potassium was found to have the largest border zone and this was attributed to the voltage dependence of the potassium channels. The model also predicted the efflux of  $K^+$  from the ischemic region due to electrogenic drift and diffusion within the intra and extracellular space, respectively, which contributed to  $K^+$  depletion in the ischemic region.

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## Introduction

Myocardial ischemia is caused by reduced perfusion to regions of the heart leading to a localised reduction in supply of metabolites, limited waste removal and compromised ionic homeostasis. The first 10 minutes of ischemia are associated with an increased risk of arrhythmias peaking after 5–6 minutes [1]. During this period arrhythmias are commonly initiated within the border zone (BZ) separating viable, well perfused, tissue and the ischemic, underperfused, region [2–4]. Ischemia causes an increase in extracellular potassium ( $[K^+]_e$ ), intra and extracellular proton concentrations ( $[H^+]_i$  and  $[H^+]_e$ , respectively), intracellular sodium ( $[Na^+]_i$ ) and intracellular calcium ( $[Ca^{2+}]_i$ ) concentrations [5]. The dominant mechanisms for these changes have been attributed to a shift in the ATP/ADP ratio, which inhibits the Sodium-Potassium ATPase pump ( $NaK$ ) and increases the conductance of ATP-inactivated  $K^+$  channels; respiratory acidosis causing an increase in  $CO_2$ ; and metabolic acidosis, where a shift towards anaerobic respiration increases the production of  $H^+$  in the cell [5]. Inherently, these changes in ionic concentrations in the ischemic region lead to gradients in properties across the BZ, creating electrophysiological heterogeneities that are thought to favour the occurrence of arrhythmias [6–8].

Experimentally, the development of gradients of extracellular pH ( $pH_e$ ) and  $[K^+]_e$  [9,10] have been well characterised using ion sensitive electrodes. Intracellular metabolite gradients have been

characterised by fluorescent NADH [11] and biopsy [12] measurements. However, less is known on the gradients of intracellular ions, in particular  $[Na^+]_i$ ,  $[Ca^{2+}]_i$  and  $[H^+]_i$ , nor are the mechanisms that underpin the spatial and temporal evolution of these ion concentration gradients well characterised or understood. This study aims to investigate the spatial-temporal evolution of ion gradients across ischemic BZ and the primary regulators of the BZ size and rate of development.

Previous measurements of ion concentrations and metabolites across the BZ have either been performed at multiple locations but at a limited number of time points [10,12] or have tracked the time evolution of ion concentrations but only from a limited number of locations [13,14]. Furthermore, these measurements have only been able to characterise a subset of ions of interest across the BZ. The need to track the evolution of multiple ionic species in space and time to understand the gradients of cellular electrophysiology across the BZ motivates the use of biophysical computational modelling. Previous models of electrophysiology during acute regional ischemia have simulated the effects of these spatial gradients but have not simulated their time evolution [15–17]. More recent work has simulated the time evolution of  $[K^+]_e$  gradients [18], but have not considered other ionic gradients, the effects of nonlinear interactions between  $K^+$  and other ions, the effect of  $K^+$  diffusion in the intracellular space or the effects of potential gradients on ion diffusion.

In this study a new model of cardiac tissue electrophysiology is developed to investigate the spatial-temporal evolution of ionic concentrations across the ischemic BZ, during the first 5 minutes of reduced perfusion. The proposed model extends the conventional bidomain equations to explicitly link membrane potential to ionic concentrations and enforces ionic species conservation. A model of ion regulation across the cell membrane is then developed, parameterized, validated and coupled to the tissue model. This combined model is then used to investigate the spatial and temporal dispersion of ions across the BZ.

## Methods

To model the evolution of ionic concentrations in the presence of multiple ionic gradients, electric gradients and heterogeneous tissue properties requires the development of a new set of equations for modelling the myocardium. In the next section the equations to model the BZ are derived and a model of passive cell membrane ion regulation is developed and validated. The changes to the cell membrane model to simulate *NaK* inhibition,  $K^+$  channel activation, respiratory acidosis and metabolic acidosis are then described.

### Tissue Model Derivation

Consistent with previous models of cardiac tissue electrophysiology the myocardium is represented as a two phase medium, with each point in the domain containing a fraction of intra and extracellular space. This gives rise to the scaling variables.

$$\alpha_x = \frac{\Omega_x}{\Omega} \quad \chi = \frac{F}{\Omega} \quad (1)$$

where  $\Omega_x$  is the volume of the  $x$  space in a unit of  $\Omega$  myocardium volume,  $\alpha_x$  is the volume fraction of space  $x$  (with  $x$  corresponding to the extra ( $e$ ) or intra ( $i$ ) cellular space),  $\chi$  is the interspace surface area per unit volume myocardium and  $F$  is area of the interspace surface. The intracellular volume fraction ( $\alpha_i$ ) can be separated into sub volume fractions representing the cytosol ( $\alpha_{cvt}$ ), mitochondria ( $\alpha_{mito}$ ) or the sarcoplasmic reticulum ( $\alpha_{SR}$ ) to model distinct subcellular spaces, as described below. At each point in space there exists an intracellular potential ( $\phi_i$ ), an extracellular potential ( $\phi_e$ ), a transmembrane potential ( $V_m$ ) and an intra and extracellular ion concentration for each of the ion species in the model. The movement of each ion species in each domain is driven by diffusion, due to a gradient in ion concentration, and drift, due to a gradient in the electric field. This movement is described by the Nernst-Plank equations

$$\frac{\partial C_x^j}{\partial t} = \nabla \cdot D_x^j \left( \nabla C_x^j + \frac{z^j F}{RT} C_x^j \nabla \phi_x \right) \quad (2)$$

where  $C_x^j$  is the concentration of unbound ion  $j$  in space  $x$ ,  $z^j$  is the charge of ion  $j$ ,  $D_x^j$  is the effective diffusion of ion  $j$  in space  $x$ ,  $F$  is Faraday's constant,  $R$  is the gas constant,  $T$  is the absolute temperature and  $\phi_x$  is the potential in the space  $x$ . The conventional Nernst-Plank equations are adapted to represent the movement of ions across the cell membrane between the intra and extracellular spaces. This gives

$$\frac{\partial C_x^j}{\partial t} = \nabla \cdot D_x^j \left( \nabla C_x^j + \frac{z^j F}{RT} C_x^j \nabla \phi_x \right) + \frac{\chi J_m^j}{\alpha_x} \quad (3)$$

where  $J_m^j$  is the flux of ion  $j$  across the cell membrane.  $J_m^j$  is

defined in units of  $\text{mM ms}^{-1} \text{mm}$ . The surface separating the two regions is modelled as a simple capacitor and defining the transmembrane potential to scale with intracellular charge gives

$$V_m = \frac{Q_i}{C_m} \quad (4)$$

where  $Q_i$  is the intracellular charge per unit cell membrane area and  $C_m$  is the membrane capacitance per unit cell membrane area. The charge on either side of the membrane is assumed to be equal but opposite, giving

$$Q_i = -Q_e \quad (5)$$

Separating the concentration of each ion species in the intra and extracellular space into ions that are membrane bound and make up the membrane charge ( $Q_x^j$ ) and those that are in solution gives.

$$C_x^j = C_{xsol}^j + C_{xQ}^j \quad (6)$$

where  $C_{xsol}^j$  and  $C_{xQ}^j$  are the ions in solution and membrane bound ions, respectively. By assuming charge neutrality for the ions within the solute gives:

$$F \sum z^j C_{xsol}^j = 0 \quad (7)$$

Multiplying Eqn 6 by the ion species charge and Faraday's constant, then summing over all ion species in space  $x$  gives.

$$F \sum z^j C_x^j = F \sum z^j C_{xQ}^j \quad (8)$$

Converting the concentration of ions per unit volume in domain  $x$  to charge per unit cell membrane area and introducing a static charge term ( $\eta_x$ ) that characterises all charge not attributable to  $C_x^j$ , gives

$$Q_x^j = \frac{\alpha_x}{\chi} F \sum z^j C_{xQ}^j + \eta_x \quad (9)$$

Combining with Eqn 8 gives

$$Q_x^j = \frac{\alpha_x}{\chi} F \sum z^j C_x^j + \eta_x \quad (10)$$

This defines the charge on the membrane as equal to the unbalanced charge in space  $x$ . Using the charge balance Eqn 5, gives

$$\alpha_i \sum z^j C_i^j + \alpha_e \sum z^j C_e^j + \eta_i + \eta_e = 0 \quad (11)$$

Differentiating Eqn 11 with respect to time, substituting in Eqn 3 and recognising that all transmembrane fluxes are balanced, provides

$$\alpha_i \sum z^j \nabla \cdot D_i^j \left( \nabla C_i^j + \frac{z^j F}{RT} C_i^j \nabla \phi_i \right) + \alpha_e \sum z^j \nabla \cdot D_e^j \left( \nabla C_e^j + \frac{z^j F}{RT} C_e^j \nabla \phi_e \right) = 0 \tag{12}$$

this ensures that there is no net charge accumulation in any unit volume of myocardium. Defining the relationship between the intra and extracellular potentials gives

$$V_m = \phi_i - \phi_e \tag{13}$$

Using Eqn 4 and the definition of charge (Eqn 10), then gives the algebraic definition of the transmembrane potential:

$$V_m = \frac{F}{C_m \lambda} \alpha_i \left( \sum z^j C_i^j + \eta_i \right) \tag{14}$$

Rearranging Eqn 13 and substituting in the definition of  $V_m$  from Eqn 14 allows  $\phi_i$  to be defined in terms of  $\phi_e$  and  $C_x^j$ . Combining this definition of  $\phi_i$  with Eqns 14, 13, 12, 3 and 2 then represents a closed set of equations. These equations are equivalent to the bidomain equations in the case of a single charge carrier and no gradient in ion concentrations, as shown below.

In cardiac myocytes many important ions, including  $H^+$  and  $Ca^{2+}$  are heavily buffered, both within the cell and the extracellular space. To account for buffering the free and buffer bound fraction of  $C_x^j$  are calculated. In general, as  $C_{xsol}^j > C_{xQ}^j$  the effect of ions bound to the cell membrane will not be included in the buffering equations for simplicity. This gives

$$C_x^j \approx C_{xsol}^j = C_{xfree}^j + C_{xbuff}^j \tag{15}$$

where  $C_{xfree}^j$  are the unbound ions and  $C_{xbuff}^j$  are the ions bound to buffers. At this time all buffers will be treated as rapid and to a single representative buffer species, giving

$$C_x^j = C_{xfree}^j + B_x^j \frac{C_{xfree}^j n_x^j}{C_{xfree}^j n_x^j + K_x^j n_x^j} \tag{16}$$

where  $B_x^j$ ,  $K_x^j$  and  $n_x^j$  are the concentration, binding affinity and Hill coefficient, respectively, for the buffer of ion  $j$  in space  $x$ . Assuming that ions bound to buffers are immobile, only  $C_{xfree}^j$  is used to calculate the diffusion and drift of ions in Eqn 3, and similarly in Eqn 12. As binding of ions to a buffer implicitly removes a charged binding site located on a static protein, Eqn 14 remains unchanged.

Due to the complex anatomy of the cardiac myocyte many sub volumes exist within the cell that affect ionic concentrations. The sum of the volume fraction ( $\alpha_x$ ) values must be less than, but do not have to be equal to, one, allowing the model to represent any volume fractions that are not directly accessible by ions. In particular the  $\alpha_i$  variable can represent all space in the cell or can be substituted for  $\alpha_{cvt}$  representing the volume fraction of the cytosol (a sub volume of  $\alpha_i$ ). This allows the effects of SR,

mitochondrial or other subcellular structure volumes on intracellular ionic concentrations to be accounted for in the model.

**Equation summary.** The modelled equations are given by

$$V_m = \frac{F}{C_m \lambda} \alpha_i \left( \sum z^j C_i^j + \eta_i \right) \tag{17}$$

$$\phi_i = V_m + \phi_e$$

$$C_x^j = C_{xfree}^j + B_x^j \frac{C_{xfree}^j n_x^j}{C_{xfree}^j n_x^j + K_x^j n_x^j}$$

$$\frac{\partial C_i^j}{\partial t} = \nabla \cdot D_i^j \left( \nabla C_{ifree}^j + \frac{z^j F}{RT} C_{ifree}^j \nabla \phi_i \right) - \frac{\lambda J_m^j}{\alpha_i}$$

$$\frac{\partial C_e^j}{\partial t} = \nabla \cdot D_e^j \left( \nabla C_{efree}^j + \frac{z^j F}{RT} C_{efree}^j \nabla \phi_e \right) + \frac{\lambda J_m^j}{\alpha_e}$$

$$0 = \alpha_i \sum z^j \nabla \cdot D_i^j \left( \nabla C_{ifree}^j + \frac{z^j F}{RT} C_{ifree}^j \nabla \phi_i \right) + \alpha_e \sum z^j \nabla \cdot D_e^j \left( \nabla C_{efree}^j + \frac{z^j F}{RT} C_{efree}^j \nabla \phi_e \right)$$

where it is important to note that for non buffered ions  $B_x^j = 0$  and  $C_x^j = C_{xfree}^j$ .

**Consistency with bidomain equations.** Imposing the implicit assumptions of the bidomain equations that charge carriers are not buffered, ion concentrations are homogenous and charge is carried by a single carrier to Eqn 18, the bidomain equations can be derived. Assuming homogenous ion concentrations and considering the case of the intracellular space reduces Eqn 18 to

$$\frac{\partial C_i^j}{\partial t} = \nabla \cdot D_x^j \frac{z^j F}{RT} C_i^j \nabla \phi_i - \frac{\lambda J_m^j}{\alpha_i} \tag{18}$$

Differentiating Eqn 14 for the intracellular space gives

$$\frac{\partial V_m}{\partial t} = \frac{F}{C_m \lambda} \alpha_i \sum \left( z^j \frac{\partial C_i^j}{\partial t} \right) \tag{19}$$

substituting Eqn 18 into Eqn 19 gives

$$\frac{\partial V_m}{\partial t} = \frac{F}{C_m \lambda} \alpha_i \sum z^j \left( \nabla \cdot D_x^j \frac{z^j F}{RT} C_i^j \nabla \phi_i - \frac{\lambda J_m^j}{\alpha_i} \right) \tag{20}$$

As ion concentrations are homogenous conductivity is defined as

$$\sigma_x = \sum D_x^j \frac{z^j F^2 \alpha_x C_x^j}{RT} \quad (21)$$

Then Eqn 20 reduces to

$$C_m \chi \frac{\partial V_m}{\partial t} = \nabla \cdot \sigma_i \nabla \phi_i - F \sum z^j J_m^j \quad (22)$$

Applying the single charge carrier assumption and converting from ionic flux to current gives the first bidomain equation

$$\chi \left( C_m \frac{\partial V_m}{\partial t} + I_{ion} \right) = \nabla \cdot \sigma_i \nabla \phi_i \quad (23)$$

The second bidomain equation is readily derived from applying the homogenous ion concentration assumption to Eqn 12 and multiplying by Faraday's constant (to convert from conserving ion flux to current) giving

$$\nabla \cdot \sum D_i^j \frac{z^j F^2 \alpha_i C_i^j}{RT} \nabla \phi_i + \nabla \cdot \sum D_e^j \frac{z^j F^2 \alpha_e C_e^j}{RT} \nabla \phi_e = 0 \quad (24)$$

Substituting in the definition of conductivity from Eqn 21 then gives the second bidomain equation

$$\nabla \cdot \sigma_i \nabla \phi_i + \nabla \cdot \sigma_e \nabla \phi_e = 0 \quad (25)$$

## Modelling the Membrane Fluxes

Cardiac electrophysiology is predominantly determined by the movement of  $Ca^{2+}$ ,  $Na^+$  and  $K^+$ . For charge neutrality  $Cl^-$  must also be included in the model. To simulate the evolution of acidosis requires the inclusion of  $H^+$ ,  $HCO_3^-$  and  $CO_2$  in the model. All of these ions (and  $CO_2$ ) were modelled in the intra and extracellular space, with  $H^+$  and  $Ca^{2+}$  being buffered. The goal of the model, in this study, was not to track the propagation of the action potential but to simulate the gradients of ions that exist over the BZ. These ion gradients were modelled based on the diastolic properties of the cell. This assumption was also a requirement to enable the simulation of minutes, while remaining computationally tractable.

The membrane ion transport pathways are described first for  $Na^+$ ,  $H^+$  and  $HCO_3^-$ . Ion specific channels are then described that balance the flux of each ion species. The channel and transporter densities were determined by imposing zero net flux for each ion species, using the relative densities of  $Na^+$  and  $H^+$  transporters recorded experimentally, and intra and extracellular ionic concentrations and membrane potential values derived from the literature. Where possible experimental data was taken preferentially from rabbit or guinea pig data at body temperature. This limited number of constraints then allowed the model transporters and channel densities to be uniquely determined.

**Sodium regulation.** The model of  $Na^+$  regulation included representations of the  $NaK$ , sodium calcium exchanger ( $NCX$ ), sodium hydrogen exchanger ( $NHE$ ), sodium bicarbonate co-transporter ( $NBC$ ) and a lumped sodium channel ( $I_{Na}$ ).  $NaK$  was

modelled using the thermodynamically consistent equation set proposed by Smith and Crampin [19]. This model was subsequently revised by Terkildsen et al., [20] and this parameter set that was used here. The model for  $NaK$  was fitted to guinea pig data as limited rabbit data was available. However, the maximum flux was rescaled to match rabbit data, as described below.

The  $NCX$  model was taken from Weber et al., [21]. The model has been fitted to rabbit experimental data at 37°C. The  $NHE$  model was based on the model developed by Crampin and Smith [22] and reparameterized by Niederer and Smith [23]. In this study extracellular  $Na^+$  and  $H^+$  regulation of  $NHE$  were included. This model was fitted predominantly to sheep Purkinje data [24], although the  $H^+$  dependence of  $NHE$  remains relatively consistent between species [25]. The  $NBC$  model was taken from Crampin and Smith [22]. The model assumes  $NBC$  is electro neutral, which is true for only part of the  $NBC$  population [25]. There was not sufficient data to fully characterise the electrogenic and electro neutral forms of  $NBC$ , hence the electro neutral model was used. Background  $Na^+$  flux across residual open fast  $Na^+$  and persistent  $Na^+$  channels is limited when the cell is quiescent. However, some flux is still present [26] and a simple lumped background ionic flux equation was used, given by

$$J_{Na} = g_{Na}(V_m - E_{Na}) \quad (26)$$

to model the residual  $Na^+$  flux across any open  $Na^+$  channels. The same equation form was used for modelling all background ion channels.

**Proton regulation.** In the proposed model  $[H^+]_i$  was regulated by  $NHE$ , described above, chloride-hydroxide exchanger ( $CHE$ ), hydrolysis and buffering. Background  $H^+$  leak or other  $H^+$  exchangers were not considered in the general model of  $H^+$  regulation, described here, but do include models of  $H^+$ -lactate exchange and intracellular metabolism derived  $H^+$  sources in the model of ischemia, described below. The  $CHE$  model comes from Niederer et al., [27] and was fitted to guinea pig data at 37°C. The hydrolysis of  $CO_2$  into  $HCO_3^-$  and  $H^+$  was governed by

$$J_{H_{yd}} = k_f [CO_2] - k_r [H^+] [HCO_3^-] \quad (27)$$

where  $k_f$  and  $k_r$  are the forward and reverse rates of hydrolysis. Hydrolysis occurs in both the intra and extracellular space and the rate constants were assumed to be the same in both domains.  $H^+$  buffering in the intra and extracellular space is due to mobile and static  $H^+$  buffers and  $HCO_3^-$  [28]. The intra and extracellular buffering of  $H^+$  were assumed to be instantaneous and represented by a single population of buffers. To reduce the model size, partial differential equations were only solved for the total concentration of  $[H^+]_i$  or  $[H^+]_e$ . The concentration of free ions were then calculated by

$$[H^+]_{free} = \frac{-K_H - B_H + [H^+]_{total} + \sqrt{(K_H + B_H - [H^+]_{total})^2 - 4[H^+]_{total}K_H}}{2} \quad (28)$$

where  $B_H$  and  $K_H$  represent the concentration of the buffer and the binding affinity, respectively. This buffer model was used for both intra and extracellular  $H^+$ , with a separate set of parameters for each ion.

**Calcium regulation.** A simplified model of intracellular cardiac  $Ca^{2+}$  was developed assuming that  $Ca^{2+}$  in the

intracellular space reaches an approximate equilibrium over the time scales of interest. Furthermore, SERCA ATPase function was modelled with a Hill coefficient of one as opposed to two, to allow the definition of  $Ca^{2+}$  to remain deterministic. The intracellular space was assumed to consist of a sarcoplasmic reticulum (SR) and a cytosolic space. The subsarcolemmal and dyadic space are small and are also likely to be in equilibrium with the cytosolic  $Ca^{2+}$ , so were not included in the model. The  $Ca^{2+}$  dynamics were described by

$$\frac{d[Ca^{2+}]_i}{dt} = -J_{SERCA} + J_{leak} + (I_{CaL} + I_{Cab} - I_{NCX}) \frac{A_m}{FzCa} \quad (29)$$

$$\frac{d[Ca^{2+}]_{SR}}{dt} = (J_{SERCA} - J_{leak}) \frac{\alpha_{SR}}{\alpha_{cyt}} \quad (30)$$

$$J_{SERCA} = V_{SERCA} \frac{[Ca^{2+}]_i^{nH}}{[Ca^{2+}]_i^{nH} + K_{SERCA}^{nH}} \quad (31)$$

$$J_{leak} = P_{leak} ([Ca^{2+}]_{SR} - [Ca^{2+}]_i) \quad (32)$$

$$I_{Ca} = I_{CaL} + I_{Cab} = g_{Ca} (V_m - E_{Ca}) \quad (33)$$

where  $[Ca^{2+}]_{SR}$  is the SR  $Ca^{2+}$ ,  $J_{leak}$  is the flux of calcium out of the SR,  $J_{SERCA}$  is the uptake of  $Ca^{2+}$  by SERCA,  $V_{SERCA}$  is the maximum SERCA flux,  $P_{leak}$  is the diffusion permeability of the SR membrane,  $K_{SERCA}$  is the binding coefficient of  $Ca^{2+}$  to SERCA,  $\alpha_{SR}$  and  $\alpha_{cyt}$  are the volume fractions of the SR and cytosol, respectively,  $I_{CaL}$  is the L-type calcium channel and  $I_{Cab}$  is the background  $Ca^{2+}$  channel. In this model the background and L-type  $Ca^{2+}$  channels were modelled as a single lumped generic  $Ca^{2+}$  channel. Introducing cytosolic buffering, ignoring the effects of SR buffering and setting  $nH$  as one and assuming that the cytosol and the SR are in equilibrium then gives

$$[Ca^{2+}]_{SR} = [Ca^{2+}]_i + \frac{V_{SERCA}}{P_{leak}} \frac{[Ca^{2+}]_i}{[Ca^{2+}]_i + K_{SERCA}} \quad (34)$$

$$\begin{aligned} [Ca^{2+}]_{tot} &= [Ca^{2+}]_i + \frac{\alpha_{SR}}{\alpha_{cyt}} [Ca^{2+}]_{SR} + B_{Ca} \frac{[Ca^{2+}]_i}{[Ca^{2+}]_i + K_{Ca}} \\ &= [Ca^{2+}]_i \left( 1 + \frac{\alpha_{SR}}{\alpha_{cyt}} \right) + \frac{\alpha_{SR} V_{SERCA}}{\alpha_{cyt} P_{leak}} \frac{[Ca^{2+}]_i}{[Ca^{2+}]_i + K_{SERCA}} \\ &\quad + B_{Ca} \frac{[Ca^{2+}]_i}{[Ca^{2+}]_i + K_{Ca}} \end{aligned}$$

defining

$$B_{SERCA} = \frac{\alpha_{SR} V_{SERCA}}{\alpha_{cyt} P_{leak}} \quad (35)$$

$$\gamma_{Ca} = 1 + \frac{\alpha_{SR}}{\alpha_{cyt}} \quad (36)$$

and collecting terms gives

$$A = \frac{\gamma_{Ca} K_{SERCA} + \gamma_{Ca} K_{buff} + B_{buff} + B_{SERCA} - [Ca^{2+}]_{tot}}{\gamma_{Ca}} \quad (37)$$

$$B = \frac{\gamma_{Ca} K_{buff} K_{SERCA} + B_{buff} K_{SERCA} + B_{SERCA} K_{buff} - [Ca^{2+}]_{tot} (K_{SERCA} + K_{buff})}{\gamma_{Ca}} \quad (38)$$

$$C = \frac{-[Ca^{2+}]_{tot} K_{buff} K_{SERCA}}{\gamma_{Ca}} \quad (39)$$

$$0 = [Ca^{2+}]_i^3 + A[Ca^{2+}]_i^2 + B[Ca^{2+}]_i + C \quad (40)$$

As  $C$  is always negative the cubic always has at least one positive real root for possible values of  $[Ca^{2+}]_{tot}$ . The value of  $[Ca^{2+}]_{tot}$  was then found using the root finding method first proposed by Francois Viète in 1600 and reused more recently by Faber and Rudy [29]:

$$\begin{aligned} [Ca^{2+}]_i &= \\ &= \frac{2\sqrt{A^2 - 3B}}{3} \cos \left( \frac{\arccos \left( \frac{9AB - 2A^3 - 27C}{2(A^2 - 3B)^{1.5}} \right)}{3} \right) - \frac{A}{3} \quad (41) \end{aligned}$$

The model of  $Ca^{2+}$  dynamics assumes that all  $Ca^{2+}$  buffers were static and that the transport of ions via mobile buffers was accounted for in the effective diffusion parameters of free  $Ca^{2+}$ . It is possible to extend the proposed model to include mobile buffers but they were assumed to play a secondary role in the current model.  $[Ca^{2+}]_e$  was assumed to be buffered by a single species and was modelled using the same framework described above for  $H^+$  (Eqn 28).

**Chloride regulation.** In this model  $Cl^-$  homeostasis was maintained by the *CHE* and the  $Cl^-$ - $HCO_3^-$  exchanger (*AE*), which bring  $Cl^-$  into the cell, and a  $Cl^-$  channel that allows  $Cl^-$  to flow out of the cell. The *CHE* model is described above. The *AE* model was taken from Crampin and Smith [22] and was developed using guinea pig data at 37°C. The  $Cl^-$  channel uses the conventional background channel formulation. A linear  $H^+$  dependence of the background  $Cl^-$  current was added to the model based on observations from Komukai et al., [30].

**Potassium regulation.** In dynamic action potential models of cardiac electrophysiology there are a large number of  $K^+$  channels [31] that bring  $K^+$  into the cell. This influx was balanced by the *NaK* pump, described above, that extrudes  $K^+$ . For the passive membrane model, all of the  $K^+$  channels were lumped into a single background current ( $I_{Kb}$ ) formulation that was set to balance the flux of  $K^+$  on *NaK*. It was assumed that the

membrane potential and  $K^+$  reversal potential are the dominant factors affecting this channel and other forms of regulation have not been considered.

**Bicarbonate regulation.**  $HCO_3^-$  was assumed to be regulated principally by hydrolysis and through *NBC* and *AE*. All of these components have been described above and it was assumed that there are no other  $HCO_3^-$  pathways across the membrane.

**Carbon Dioxide.**  $CO_2$  is regulated primarily through hydrolysis and can diffuse relatively freely across the membrane. The model of hydrolysis is described above and  $CO_2$  diffusion was assumed to obey Fick's law.

## Model Parameters

For each transmembrane ion pathway described above, all kinetic, binding affinity and membrane potential dependencies were taken from the original models. Here the definition of geometrical parameters, ionic concentrations, buffering parameters and the density/scaling of each transmembrane pathway are motivated from data in the literature.

**Geometrical parameters.** The extracellular space is estimated to be between 17–30% [32–35],  $17.7 \pm 0.6\%$  and  $24.6 \pm 0.6\%$  [33,36] of the volume of the heart in rabbit, cat, and rat hearts, respectively. This gave an  $\alpha_e$  value of 0.2 leading to an  $\alpha_i$  value of 0.8. The surface to volume ratio of a cell is reported as  $0.31–0.35 \mu m^{-1}$  [37,38] in rat and rabbit myocytes, corresponding to a  $\chi$  value of  $264 mm^{-1}$ . The relative SR volume was set to 3% of intracellular volume, giving an  $\alpha_{SR}$  value of 0.024, based on reported values of 1.4–3.5% of cell volume [37,39,40] in mouse, rat and swine. The relative mitochondrial volume ( $\alpha_{mito}$ ) was set to 0.24 based on an estimated mitochondrial cell volume fraction of 30% [37,40]. The cytosol volume fraction was set to 67% of the intracellular space, resulting in an  $\alpha_{cyt}$  value of 0.536. To account for the effects of subcellular domains on intracellular ionic concentrations in the model, all references to  $\alpha_i$  in Eqn 18 were replaced by  $\alpha_{cyt}$ . A summary of geometrical parameters is given in Table 1.

**Intracellular ionic concentrations.**  $[Na^+]_i$  has been measured using SBF1 fluorescence and  $Na^+$  sensitive electrodes. A significant range of values have been reported from 2–10mM [26,41–44] to 20–30mM [34,45,46]. Early measurements of intracellular ionic concentrations were performed using ion sensitive electrodes. These experiments measure ion activity and not ionic concentration and are often performed in multi-cellular preparations, confounding measurements. For these reasons  $[Na^+]_i$  in quiescent myocytes was set to 4mM, consistent with recent calibrated fluorescent measurements in isolated rabbit myocytes [26,44].

No fluorescence dye is routinely used for measuring  $[K^+]_i$ . Using ion sensitive electrodes Lee et al., [45] were able to calibrate

their measurements of ion activity in rabbit myocytes using an estimated  $K^+$  activity coefficient of 0.613, giving a value of 135mM. This compares with a range of 147–236mM calculated by applying the Lee et al.,  $K^+$  ion activity coefficient to ion activity measurements in rabbit, cat and guinea pig [34,43,47,48]. Alternate measurement using flame emission spectrometry by Powell et al., [49] measured  $[K^+]_i$  in rat myocytes, giving a concentration of  $120.8 \pm 1.7$  mM. Given the lower values of the two calibrated measurements,  $[K^+]_i$  was set to 135 mM.

No dye is routinely used for measuring  $Cl^-$  concentration in cardiac cells, however,  $[Cl^-]_i$  can be measured using ion sensitive electrodes.  $Cl^-$  activity has been reported as 14–20 mM [35,48,50,51] in sheep, rabbit and guinea pig heart cells. Estimations of  $[Cl^-]_i$  from total tissue  $Cl^-$  concentrations have resulted in values of  $38.9 \pm 2.5$  mM [35] and 16.2 mM [34] in rabbit cells and  $19.4 \pm 1.2 \mu mol/g$  dry wt (or 9.7 mM using the 0.49 mM per  $\mu mol/g$  dry wt scaling factor from Bers [52]) in rat. The higher value of 39 mM may be attributed to the higher extracellular space used in these calculations (30% as compared to 20%). Considering the relative convergence of values  $[Cl^-]_i$  was set to 18 mM.

Resting free  $Ca^{2+}$  is measured using calibrated fluorescence measurements. These measurements range from 44–100 nM in rabbit and guinea pig preparations [53–57]. Given this consistency the  $[Ca^{2+}]_i$  will be set to 80 nM. SR  $Ca^{2+}$  concentration is calculated from integrating the current across the cell membrane following the release of  $Ca^{2+}$  from the SR in response to caffeine. These measurements show two populations with high values in rat (73–140  $\mu M$  [58–61]), canine (80  $\mu M$  [62]), rabbit (87–106  $\mu M$  [60,61]) and ferret (76  $\mu M$  [63]), compared to lower measurements in guinea pig (17.9–27  $\mu M$  [58,64]). Given that the majority of species have a higher reported concentration, including rabbit, simulations were run with SR  $Ca^{2+}$  load set to 100  $\mu M$ . The buffering of  $Ca^{2+}$  can be described by Hill equation(s), mass action equation(s) or a constant buffering power. To compromise between biophysics and complexity, buffering was modelled by a single Hill equation. Hove-Madsen and Bers [65] fitted  $Ca^{2+}$  buffering in rabbit myocytes using two Hill curves; however, the lower affinity buffer will not play a significant role at passive diastolic  $Ca^{2+}$  concentrations. For this reason the high affinity site, with cooperativity reduced from 1.27 to unity, was used to model  $Ca^{2+}$  buffering, giving a buffer concentration of 208.98  $\mu M$  (converted using a scaling factor of 2.43 from Bers [52]) and an affinity of 0.42  $\mu M$ . This model of  $Ca^{2+}$  buffering in rabbit is similar to the concentration/affinity values of 162/0.63  $\mu M$  [66], 121/0.65  $\mu M$  [67] and 128–162/0.45–0.53  $\mu M$  [68] values measured in other species.

$pH_i$  has been measured using  $H^+$  sensitive electrodes and fluorescence dyes. Measurement of  $pH_i$  consistently falls within the range of 7.0–7.25 [57,69–71] in either HEPES or  $HCO_3^-$  buffered solutions. In the model  $pH_i$  was set to 7.1.  $H^+$  are heavily buffered in the cytosol by intrinsic buffers and  $HCO_3^-$ . Here the buffering of  $H^+$  by  $HCO_3^-$  was modelled explicitly and the intrinsic buffers were assumed to be in rapid equilibrium. Leem et al., [70] measured (and modelled)  $H^+$  buffering by two populations of buffers with binding affinity pK values of 6.03 and 7.57 and concentrations of 84.22mM and 29.38mM. Zamboni et al., [25] differentiated between mobile and fixed buffers and found that the fixed buffers had a consistent concentration of 50–70mM and binding affinity (pK) value of 6.1–6.2 across rat, rabbit and guinea pig, while the mobile buffers had a constant  $\beta$  value of *approx*10. Fitting a single buffering curve to these two

**Table 1.** Geometric variables.

Variable	Value
$\alpha_i$	0.8
$\alpha_e$	0.2
$\chi$	$264 mm^{-1}$
$\alpha_{cyt}$	0.536
$\alpha_{mito}$	0.24
$\alpha_{SR}$	0.024

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**Table 2.** Intra and extracellular free ion concentrations.

Ion	Concentration (mM)	
	Intracellular	Extracellular
$Na^+$	4.0	140
$K^+$	135	4.0
$Cl^-$	18	110
$Ca^{2+}$	$80 \times 10^{-6}$	1.2
$H^+$	$10^{-4.1}$	$10^{-4.4}$
$CO_2$	1.17	1.17

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models over a pH range of 6.5–7.5 gives concentrations of 64–68mM and pK values of 6.45–6.65, which gave a value of 65mM and pK value of 6.5 for this model.

**Extracellular ionic concentrations.** The concentration of the majority of ions in the extracellular space have been measured in canine [46,72], rat [36,73] and cat [74] hearts. These measurements provide a consistent range of ion concentrations for  $Na^+$ ,  $K^+$  and  $Cl^-$ , giving  $[Na^+]_e$  as 134–159mM,  $[K^+]_e$  as 3.3–5.8mM and  $[Cl^-]_e$  as 105–120mM. In the model  $[Na^+]_e$  was set to 140mM,  $[K^+]_e$  was set to 4mM, consistent with measurements in guinea pig hearts [75] and rabbit atrium [76] and  $[Cl^-]_e$  was set to 110mM. The  $[Ca^{2+}]_e$  values reported range from 1.03–5.16mM, however, these values do not differentiate between buffered and ionized  $Ca^{2+}$ . The properties of  $Ca^{2+}$  buffering in the extracellular space are not well characterised and are generally ignored in previous cardiac cell models. To approximate the buffering properties of extracellular  $Ca^{2+}$  using a simple single species steady state mass action model, with no cooperative binding, requires two parameters, the concentration of the buffer and the binding affinity. Assuming the ratio of free  $Ca^{2+}$  in the extracellular space to bound ions is similar to serum [77] and assuming that the primary buffer of  $Ca^{2+}$  in the extracellular space are phospholipids, then extracellular  $Ca^{2+}$  buffering will have a binding affinity of 1.1mM [78], within the range observed across multiple species [79], and a buffer concentration of 2.3mM based on a free  $Ca^{2+}$  concentration of 1.2mM and assuming 50% of  $Ca^{2+}$  are bound to buffers [77].  $pH_e$  was set to 7.4, to be consistent with the majority of experimental studies [57,69–71] and measurements across a range of species [80]. Limited measurements were available to model  $[H^+]_e$  buffering, however, Yan and Kleber [81] reported 39 mM of buffered  $H^+$  in the extracellular space. By assuming similar binding affinities for the intra and extracellular buffers and that  $pH_e$  is 7.4, then gave a concentration of extracellular proton buffers of 350mM. A summary of ion concentrations and buffering parameters are given in Table 2 and Table 3, respectively.

The concentration of  $CO_2$  was calculated using the parameters proposed and measured for guinea pig ventricular myocytes at 37°C by Leem and Vaughan-Jones [82]. The concentration of  $CO_2$  in the extracellular solution was calculated using

**Table 3.** Buffering Parameters.

Parameter	Value (mM)	
	Intracellular	Extracellular
$B_H$	65	350
$K_H$	$10^{-3.5}$	$10^{-3.5}$
$B_{Ca}$	0.209	2.3
$K_{Ca}$	$0.42 \times 10^{-3}$	1.1

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$$[CO_2]_e = \alpha_{CO_2}(\%CO_2)P_{atm} \quad (42)$$

where  $\alpha_{CO_2}$  is the solubility of  $CO_2$ , set to 0.0307 mM mmHg<sup>-1</sup> from human measurements at pH 7.4 and 37°C [83], % $CO_2$  is the fraction of air that is  $CO_2$ , set to 5% at baseline and  $P_{atm}$  is atmospheric pressure, set to 760 mmHg<sup>-1</sup>. This gives a partial pressure of  $CO_2$  ( $P_{CO_2}$ ) of 38 mmHg, consistent with although slightly higher than the  $34 \pm 3$  mmHg measured in rabbit hearts [84]. The hydration of  $CO_2$  was modelled by a mass action reaction (Eqn 27). The  $k_f$  and  $k_r$  values were measured and modelled by Leem and Vaughan-Jones in guinea pig myocytes at 37°C [82], giving values of 0.365s<sup>-1</sup> and  $3.11 \times 10^5$ s<sup>-1</sup>, respectively, resulting in an equilibrium constant of  $10^{-6.2}$ . The rate of hydration of  $CO_2$  was assumed to be similar in both the intra and extracellular space. The movement of  $CO_2$  across the cell membrane was modelled by Fick's law. Previous models have used permittivity values of 0.058mms<sup>-1</sup> [82], based on measurements in red blood cells. This value was reused despite its lack of species and cell type consistency, as there were no recent studies characterising the permeability in cardiac myocytes and the high permeability leads  $CO_2$  to be close to equilibrium between the intra and extracellular spaces.

**Current, exchanger and pump densities.** The model of each transmembrane ion pathway ( $y$ ) was separated into a kinetic regulatory component ( $\gamma_y$ ) dependent on transmembrane potential and ionic concentrations, and a scalar ( $V_y$ ) representing either the maximum flux or channel conduction of the pathway. The flux across a pathway ( $G_y$ ) is then given by

$$G_y = \gamma_y V_y \quad (43)$$

The  $V_y$  values were determined by calculating all of the  $\gamma_y$  values (excluding  $\gamma_{NBC}$ ,  $\gamma_{hyd}$  and  $\gamma_{CO_2}$  as  $[CO_2]_i$  and  $[HCO_3^-]_i$  were unknown) using the ionic concentrations in Table 2 and assuming a membrane potential of -80 mV. The remaining unknown  $V_y$  and ionic concentrations were then determined from a limited number of measurements and by enforcing a zero net flux condition described by

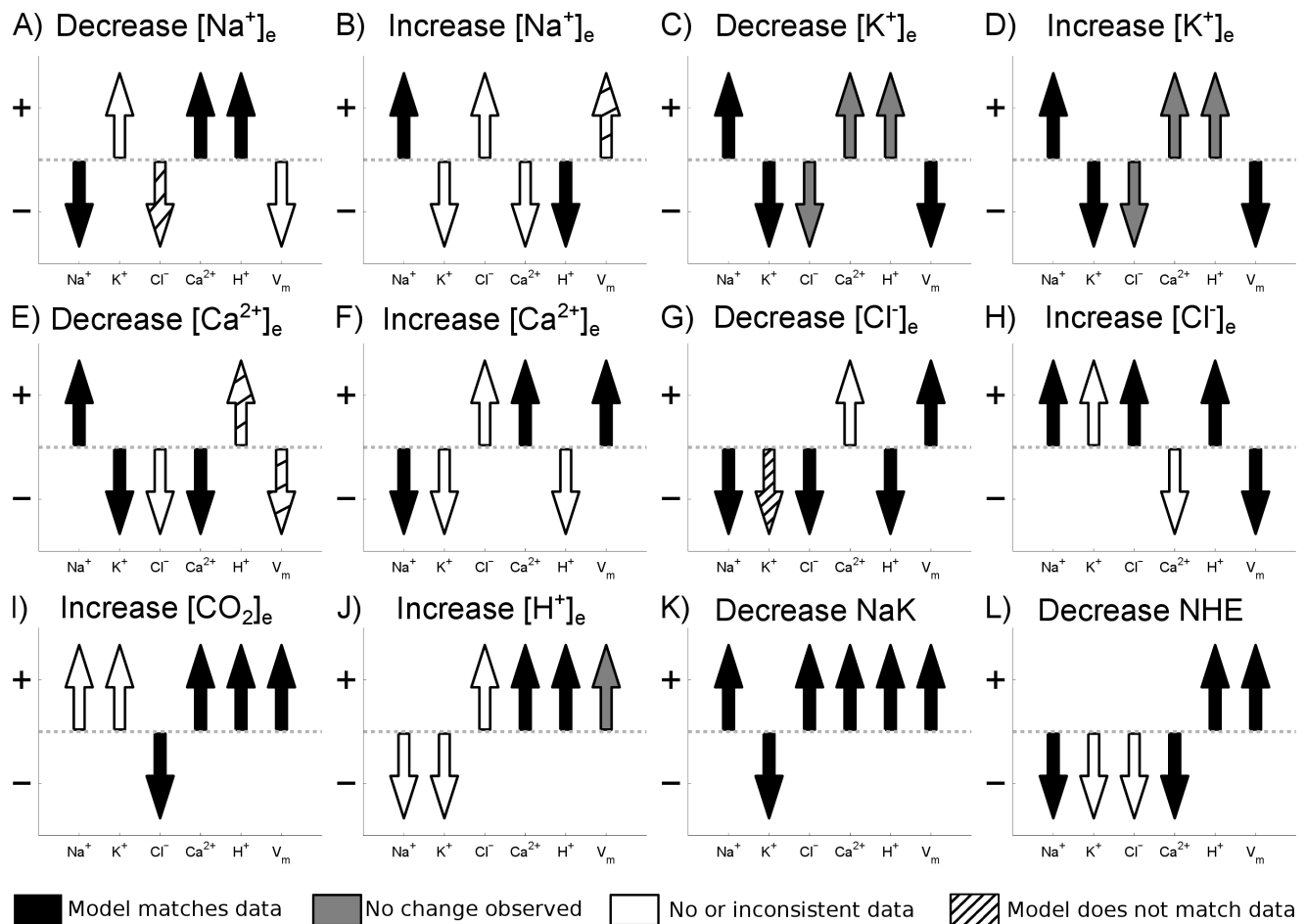




[85]. The  $G_{NaK}$   $Na^+$  flux was assumed to be equal to the sum of all  $Na^+$  influx. As the model does not include  $Na^+-K^+-2-Cl^-$  co-transporter (NaK2Cl) or  $Na^+-Mg^{2+}$  exchanger (NaMg), primarily due to the limited data to constrain the kinetics,  $G_{NaK}$  was reduced from the flux measured by Despa et al., [85] to  $1.13 \times 10^{-5}$  mM  $ms^{-1}$ . Setting these  $G_y$  values defines  $V_{Na}$ ,  $V_{NCX}$ ,  $V_{NHE}$ ,  $V_{NaK}$ ,  $V_{kb}$  and  $V_{Cab}$ . In the experimental and modelling work by the Vaughan-Jones group [70,86] the relative size of  $G_{CHE}$  to  $G_{NHE}$  is 0.12–0.19 at  $pH_i=7.1$ , this gave an estimated ratio of 0.16. Scaling  $G_{NHE}$  determined from [85] by 0.16 provided an estimate of  $G_{CHE}$  of  $0.032 \times 10^{-5}$  mM  $ms^{-1}$ . This allows  $V_{CHE}$  and  $G_{hyd}$  to be defined.  $G_{hyd}$  must be balanced by  $G_{CO2}$  and as  $P_{CO_2}$  and  $[CO_2]_e$  were known, this flux was used to set  $[CO_2]_i$ . Combining the  $pH_i$  and  $[CO_2]_i$  concentrations with the defined hydrolysis parameters and the known value of  $G_{hyd}$

then gave  $[HCO_3^-]_i$ . Knowing  $G_{hyd}$  and  $G_{NBC}$  gave  $G_{AE}$  and hence  $V_{AE}$ . Similarly,  $G_{Cl}$  was calculated from  $G_{AE}$  and  $G_{CHE}$ , which gave  $V_{Cl}$ . Finally,  $V_{NBC}$  was calculated using  $G_{NBC}$  and  $\gamma_{NBC}$ , calculated using the derived  $[HCO_3^-]_i$  value. By automating this parameter derivation process the model parameters could be updated to ensure static ion concentrations, and hence membrane potential, for any perturbation in model parameters or ionic concentrations. Parameters for all simulations in this study were derived following this process.

**Intracellular calcium dynamics.** The intracellular regulation of  $Ca^{2+}$  was treated as an equilibrium system. This resulted in the SR effectively acting as an additional buffer on  $[Ca^{2+}]_i$ . The parameters  $V_{leak}$ ,  $V_{SERCA}$ ,  $K_{SERCA}$ ,  $\alpha_{SR}$  and  $\alpha_{cyl}$  were defined from enforcing a zero net flux constraint and experimental measurements. Measurements of  $K_{SERCA}$  are similar in rat and



**Figure 1. Cell membrane model validation.** Arrow direction shows model prediction for the change in intracellular concentrations and membrane potential for a change in extracellular ion concentrations or inhibition of membrane transporter as indicated by the panel label. The color of the arrow indicates how the model compares with experimental data, summarised in Table 4. Black arrows indicate where the model matches experimental data, white arrows indicate where there is no or inconsistent data, gray arrows indicate where no change was observed experimentally and striped arrows indicate where the model does not match experimental data. Data was considered inconsistent if different studies reported opposite changes in intracellular ion concentration or membrane potential and another found a change, it was assumed that the change was correct (for example the change in  $[K^+]_i$  in response to an increase or a decrease in  $[K^+]_e$ ). For example in panel A) corresponding to a decrease in  $[Na^+]_e$  (as indicated by the panel label), the experimental data comes from row 1 of Table 4. The model predicts that  $[Na^+]_i$  decreases and that  $[Ca^{2+}]_i$  and  $[H^+]_i$  increase, consistent with experimental measurements and the arrows are shaded black. There is no consistent observed change in the transmembrane potential so the  $V_m$  arrow remains white. No data is available for the change in  $[K^+]_i$  in response to a decrease in  $[Na^+]_e$  so the  $K^+$  arrow remains white. The model predicts a decrease in  $[Cl^-]_i$  yet experimental measurements found an increase, hence the  $Cl^-$  arrow is striped.  
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rabbit [65] and have been reported as 0.260–0.350  $\mu\text{M}$  in rabbit [65,87] and 250–280  $\mu\text{M}$  in rat [65,87,88]. A value of 0.3  $\mu\text{M}$  was used in the model.  $J_{Leak}$  is reported as 0.001–0.012  $\mu\text{Mms}^{-1}$  in rabbit, mouse and rat [54,89–91]. A value of 0.01  $\mu\text{Mms}^{-1}$  was used in the model. Enforcing a zero net flux constraint on the SR gave  $J_{SERCA}$  as 0.038  $\mu\text{Mms}^{-1}$ , comparable with values of 0.03–0.08  $\mu\text{Mms}^{-1}$  measured in rabbit [65,87,92] with units converted using scale factors from Bers [52].

### Membrane Model Validation

To validate the passive membrane model, a series of tests based on the response of the cell models intracellular ionic concentrations and transmembrane potential to changes in extracellular ionic concentrations or inhibition of major ion transporters was performed. In order to maximise the number of tests the model was compared against data from cardiac cells, regardless of temperature, species or preparation type. This maximised the number of tests but meant that a quantitative comparison was not valid and so only a qualitative comparison was performed. A summary of experimental data used in the validation is provided in Table 4. Fig. 1 shows the comparison between the model and data. From the 72 simulations performed 43 matched the experimental data, data was not available or was inconsistent for 19, changes were too small to be measured in 5 and the model did not match experiments in 5 cases.

### Diffusion Parameters

The tissue model required the definition of diffusion parameters for each of the ionic species in the intra and extracellular space. The diffusion parameters used in the model were all for the apparent diffusivity of free ions, lumping the effects of any mobile buffers, tortuosity and gap junctions into a single diffusion parameter. Using Eqn 21 the conductivity parameters were shown to be directly related to the conductivity parameters in the bidomain equations. From the review of bidomain conductivities and relative values in the intra and extracellular space by Roth [93] a conductivity value of 0.25  $\text{Sm}^{-1}$  was taken for both the intra and extracellular space. This conductivity, along with the ionic concentrations from Table 2, were used to derive the diffusion parameters. The apparent diffusion of  $H^+$  and  $\text{HCO}_3^-$  are  $1.52 \times 10^{-7} \text{mm}^2 \text{ms}^{-1}$  and  $7.7 \times 10^{-7} \text{mm}^2 \text{ms}^{-1}$  in the >intracellular space [86] and were assumed to be similar in the extracellular space. The apparent diffusion constant of  $\text{Ca}^{2+}$  (including the effects of mobile buffers) has been estimated from experimental measurements in previous modelling studies

as  $0.4 - 3 \times 10^{-7} \text{mm}^2 \text{ms}^{-1}$  [94–96]. Here a value of  $1.5 \times 10^{-7} \text{mm}^2 \text{ms}^{-1}$  [94] was used and the effect of diffusion in the SR was not included, as it was assumed to be non contiguous between cells. It was assumed that  $\text{Ca}^{2+}$  diffusion is limited by buffering, resulting in the same value in the intra and extracellular space.  $\text{Na}^+$ ,  $\text{K}^+$  and  $\text{Cl}^-$  were all assumed to have a common diffusion coefficient in either the intra or extracellular space as these ions are only nominally buffered and are only affected by gap junctions and tortuosity. Diffusion of  $\text{CO}_2$  was estimated from previous modelling/experimental studies of  $\text{CO}_2$  in tissue as  $11.3 \times 10^{-7} \text{mm}^2 \text{ms}^{-1}$  [97], and was assumed to be the same in the intra and extracellular space. Solving Eqn 21 for the diffusion of intra and extracellular  $\text{Na}^+$ ,  $\text{K}^+$  and  $\text{Cl}^-$  gives the diffusion parameters summarised in Table 5.

Finally, the effects of  $[H^+]_i$  on gap junction conductivity were included. Measurements in cell pairs by Swietach et al., [98] have demonstrated that the permeability of gap junctions has a biphasic dependence on the  $[H^+]_i$  concentration. To introduce these effects into the model the intracellular diffusion constants were scaled by

$$\gamma_{diff} = \frac{[H^+]_i^{n1} K_{d2}^{n2}}{[H^+]_i^{n1} + K_{d1}^{n1} K_{d2}^{n2} + [H^+]_i^{n2}} \quad (45)$$

where  $n1/K_{d1}$  and  $n2/K_{d2}$  are the cooperativity and binding affinity for the activation and deactivation of gap junctions by protons, respectively and  $\gamma_{diff}$  scales all intracellular diffusion constants. Using the measured parameters from end-to-end cell pairs in Swietach et al., [98]  $n1 = 2.062$ ,  $n2 = 1.81$ ,  $K_{d1} = 10^{-3.959} \text{mM}$  and  $K_{d2} = 10^{-3.934} \text{mM}$ . In this model of proton effects on gap junction permeability there is an implicit assumption that the gap junction permeability plays a dominant role in defining diffusion. At this stage no other regulators of permeability were included in the model, notably  $\text{Ca}^{2+}$  regulation is absent but this can readily be included in the modelling framework as required.

### Simulating Ischemia

In this study the effect of  $\text{NaK}$  inhibition,  $I_{Kb}$  activation and respiratory and metabolic acidosis during ischemia on cell ionic homeostasis were considered. This list is not exhaustive and absent factors are discussed below. Ischemia was modelled by respiratory acidosis, metabolic acidosis, increased  $\text{K}^+$  channel conductance and decreased  $\text{NaK}$  function. The specific time course of each of these changes is poorly characterised. Previous modelling studies have assumed that changes in cell function with ischemia have evolved linearly [99] or as a nonlinear function of prescribed metabolite concentrations [20]. To avoid any undue bias from the arbitrary selection of a time course, all changes are initially considered instantaneous.

$\text{NaK}$  inhibition and  $\text{K}^+$  channel activation were modelled by scaling the respective fluxes. Respiratory acidosis was assumed to result from an imbalance of production and washout of  $\text{CO}_2$ . To simulate this, an (implicitly electro neutral) intracellular source of  $\text{CO}_2$  was introduced into the ischemic region. There was no flux of  $\text{CO}_2$  out of the extracellular space and this resulted in a build up of  $\text{CO}_2$  in both the intra and extracellular space in the ischemic region.

To model metabolic acidosis required the introduction of an additional intracellular  $H^+$  source. However, introducing a source of cations into the cell compromised the conservation of charge constraint. To provide an electro neutral source of  $H^+$  required

**Table 5.** Effective ion diffusion parameters.

Ion	Diffusion Constant ( $10^{-7} \text{mm}^2 \text{ms}^{-1}$ )	
	Intracellular	Extracellular
$\text{Na}^+$	7.7	12.9
$\text{K}^+$	7.7	12.9
$\text{Cl}^-$	7.7	12.9
$\text{Ca}^{2+}$	1.5	1.5
$H^+$	1.52	1.52
$\text{HCO}_3^-$	7.7	7.70
$\text{CO}_2$	11.3	11.3

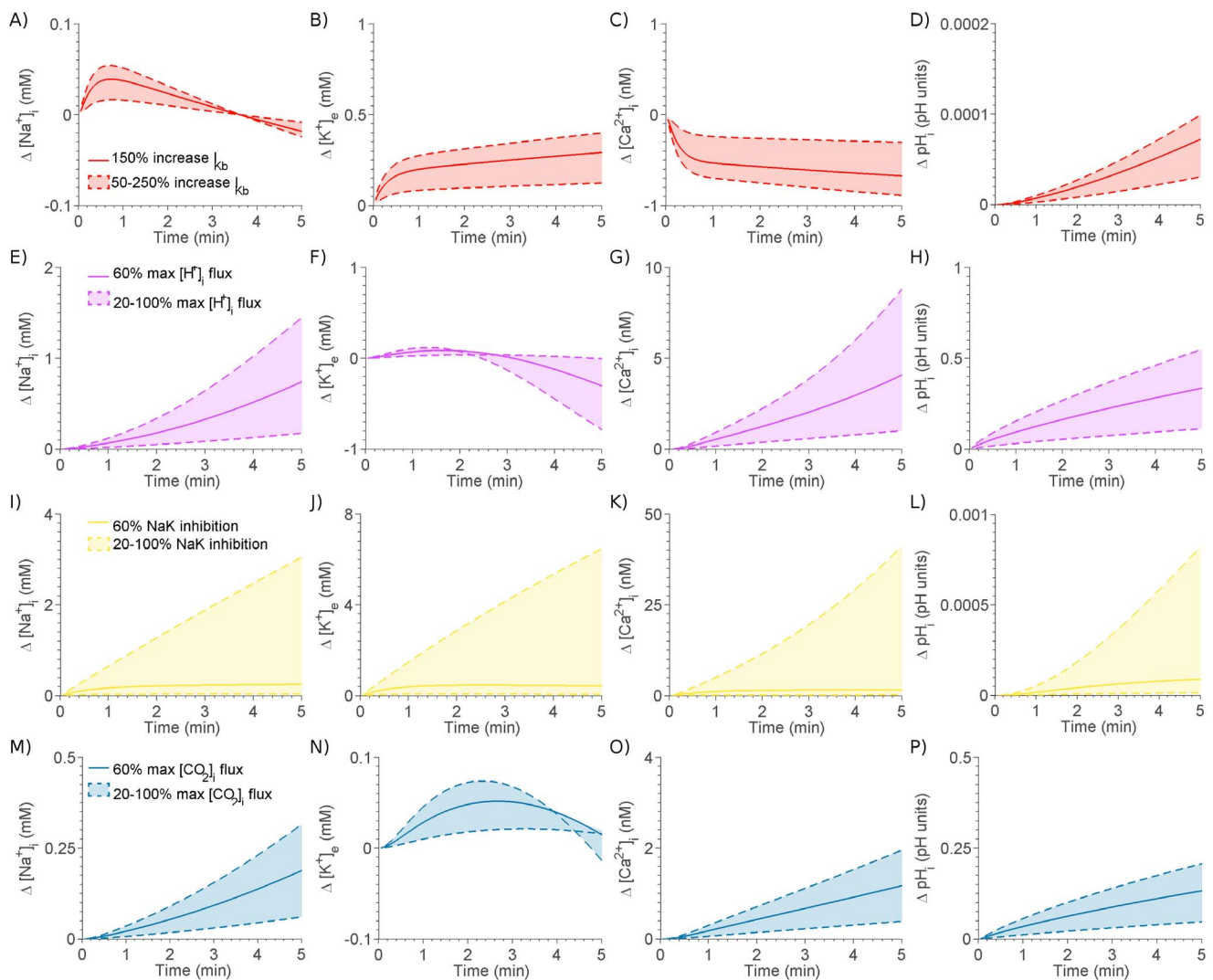
doi:10.1371/journal.pone.0060323.t005

the concurrent introduction of a source of anions that match the production of  $H^+$  inside the cell. It was implicitly assumed that the anions entered the cell in an electro neutral form with an  $H^+$  bound, and the anions and  $H^+$  separate within the cell due to metabolic processes. The source of  $H^+$  in ischemia is likely to be due to increased ATP production through glycolysis [100]; in the absence of oxygen this also results in increased lactate production. As lactate readily dissociates from  $H^+$  it was assumed that the anion source that matches  $H^+$  flux has similar characteristics to lactate including transmembrane regulation via the lactate- $H^+$  membrane exchanger MCT1 [101]. Given the ambiguity in structure, MCT1 was modelled as an ordered exchanger, using the kinetic parameters from Vinnakota and Beard [102] and the maximum influx value of  $4.8 \times 10^{-5} \text{ mMms}^{-1}$  recorded in guinea pig myocytes [103]. In the absence of metabolic acidosis, lactate concentration was assumed to be nominal, consistent with the

small flux of lactate observed in rabbit hearts under normal conditions [104]. Model simulations were performed on a 1D strand with length 32 mm, oriented in the preferred conduction or fibre direction, with a transition between ischemic and viable tissue at 16 mm to ensure the simulation captured the BZ width with nominal boundary condition artefacts. The transition between viable tissue and ischemic tissue was approximated by a Hill equation with a Hill coefficient set to ensure a steep transition between the ischemic region and viable tissue over  $440 \mu\text{m}$ , consistent with the rapid drop in oxygen pressure across the BZ in swine [105].

### Numerical Methods for Tissue Model

The nonlinear equations were solved using a fully implicit finite difference scheme with a line search Newton-Raphson method. The transmembrane flux component of the Jacobian was



**Figure 2. Effect of individual components of ischemia on the change in  $[Na^+]_i$  (column 1),  $[K^+]_e$  (column 2),  $[Ca^{2+}]_i$  (column 3) and  $pH_i$  (column 4).** Effect of 50–250% increase in  $I_{Kb}$  (red shaded region enclosed by dashed line) and a 150% increase in  $I_{Kb}$  (red line) on A)  $[Na^+]_i$ , B)  $[K^+]_e$ , C)  $[Ca^{2+}]_i$ , and D)  $pH_i$ . Effect of 20–100% maximum  $[H^+]_i$  flux (purple shaded region enclosed by dashed line) and 60% maximum  $[H^+]_i$  flux (purple line) on E)  $[Na^+]_i$ , F)  $[K^+]_e$ , G)  $[Ca^{2+}]_i$  and H)  $pH_i$ . Effect of 20–100% NaK inhibition (yellow shaded region enclosed by dashed line) and a 60% NaK inhibition (yellow line) on I)  $[Na^+]_i$ , J)  $[K^+]_e$ , K)  $[Ca^{2+}]_i$  and L)  $pH_i$ . Effect of 20–100% maximum  $[CO_2]_i$  flux (blue shaded region enclosed by dashed line) and a 60% maximum  $[CO_2]_i$  flux (blue line) on M)  $[Na^+]_i$ , N)  $[K^+]_e$ , O)  $[Ca^{2+}]_i$  and P)  $pH_i$ . doi:10.1371/journal.pone.0060323.g002

calculated using finite differencing with the remainder calculated analytically. The Jacobian was inverted directly using MatLab and was only recalculated if the residual fails to decrease or convergence was not reached within 10 Newton-Raphson iterations.

The dependence of the BZ width on the spatial and temporal discretizations was determined to test for numerical convergence. The width of the transition for each ion concentration between the viable and ischemic region, referred to as the BZ width for each ion, was calculated by fitting a Hill curve to each ionic profile. The width of the BZ for each ion was then calculated as the distance between 10 and 90% of the change in concentration.

A convergence analysis was performed and a mesh discretization of 50 $\mu$ m and a time step of 1000ms was used. Increasing the spatial discretization by a factor of 2 results in a maximum change in BZ width of any ion of 0.001mm. Decreasing the time step to 100ms increases the maximum BZ width of any ion by 0.001mm.

## Results

The individual effects of each of the four components of ischemia were first demonstrated. A combined model of ischemia was then developed and the width and magnitude of the changes in ionic concentrations across the ischemic BZ were predicted. The effect of movement of  $K^+$ ,  $Na^+$  and  $Cl^-$  within and between intra and extracellular spaces across the BZ were calculated to show the net movement of ions across the BZ.

### Simulating Individual Components of Ischemia

The level of inhibition of  $NaK$ , the activation of  $I_{Kb}$  and the level of  $CO_2$  and  $H^+$  production in the cell during ischemia is not known. To investigate the effects of each of these aspects of ischemia, they were each individually introduced into the model at five levels of severity, for  $x > 16$ mm along a 32mm strand. Fig. 2 shows the effect of each component on the change in  $[Na^+]_i$ ,  $[K^+]_e$ ,  $[Ca^{2+}]_i$  and  $pH_i$  across the ischemic BZ. The range of alterations in ion concentrations is shown by the shaded regions. The minimum and maximum changes in each component are shown by dashed lines and the mid change is shown by the solid line.  $NaK$  (yellow) was inhibited by up to 100% (no flux) in 20% increments,  $I_{Kb}$  (red) was scaled by up to 250% in 50% increments, metabolic acidosis was simulated by introducing an  $H^+$  flux in five increments up to a maximum value of 0.1 $\mu$ Mms $^{-1}$  and respiratory acidosis (blue) was simulated by a intracellular  $CO_2$  flux increased in five increments up to a maximum value of 0.12 $\mu$ Mms $^{-1}$ .

### Modelling Ischemia

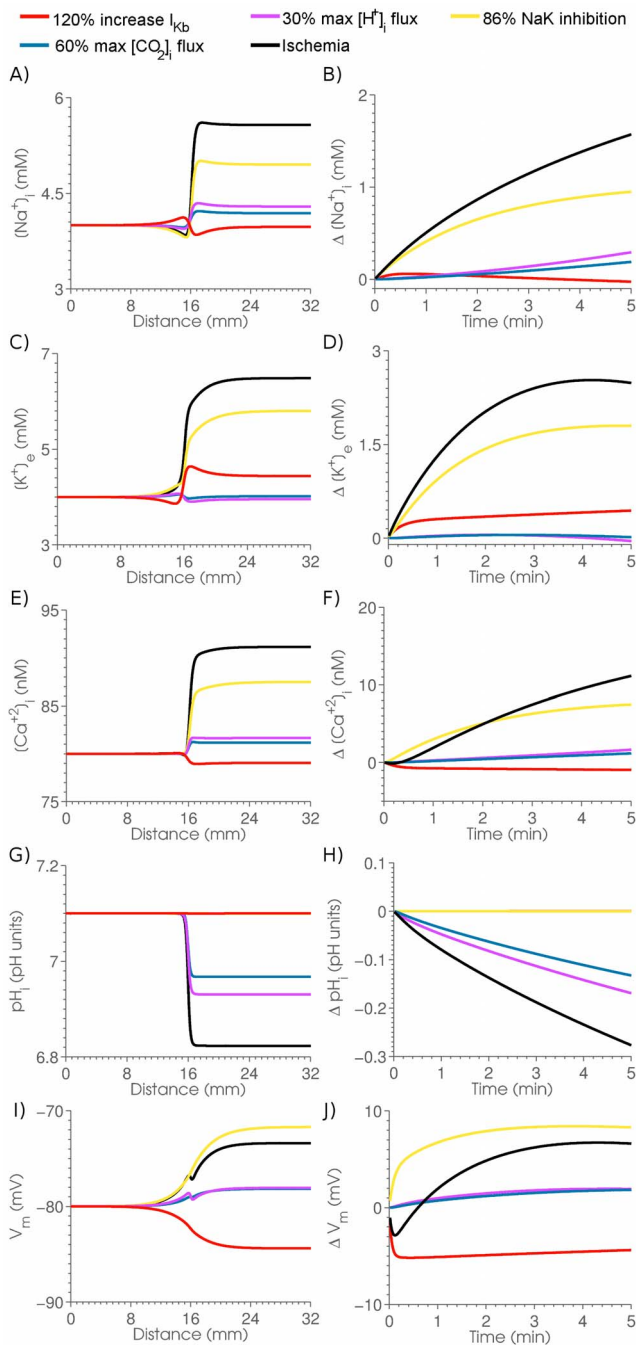
Inherently, there is no single mode of ischemia and the relative contribution of acidosis,  $NaK$  inhibition or  $I_{Kb}$  activation will depend on the residual flow, age, gender, disease state, location of ischemic region and species under study. To provide a representative case to study, 5 minutes of ischemia were simulated in the presence of all four ischemic mechanisms that match representative results from the literature.

Partial pressure measurements of  $CO_2$  in canine ischemic models show a 100–300% increase in  $CO_2$  partial pressure following occlusion, depending on the level of flow inhibition, after 10–15 minutes. The elevation in  $CO_2$  was approximately linear over time and hence in the model it was assumed  $CO_2$  concentration increases by 150% increase in the first 5 minutes of ischemia [106,107]. This corresponded to an increase in the concentration of  $CO_2$  in the model from 1.1mM to 2.8mM. In the

model respiratory acidosis was caused by an increase in  $[CO_2]_i$  flux that cannot be vented from the extracellular space. Although it is recognised that the decrease in  $pH_e$  due to metabolic acidosis will also contribute to elevated  $[CO_2]_e$ , initially the  $CO_2$  flux was set at a 60% level to achieve an increase in  $CO_2$  concentration to 2.2mM, which resulted in a decrease of  $pH_i$  to 7.0. During ischemia  $pH_i$  decreases rapidly before plateauing after approximately 15 minutes. The decrease in the initial 5 minutes has been reported to fall between 0.2 to 0.5 pH units in rat [108], ferret, [109] and guinea pig [110] preparations. Respiratory and metabolic acidosis will both contribute to this drop in  $pH_i$ . In the model setting the level of intracellular  $H^+$  flux to 30% caused a 0.17 pH unit drop and an increase in  $[CO_2]_e$  to 1.6mM. Combined metabolic and respiratory acidosis caused a 0.28 unit drop in pH and an increase in  $[CO_2]_e$  to 2.85mM.

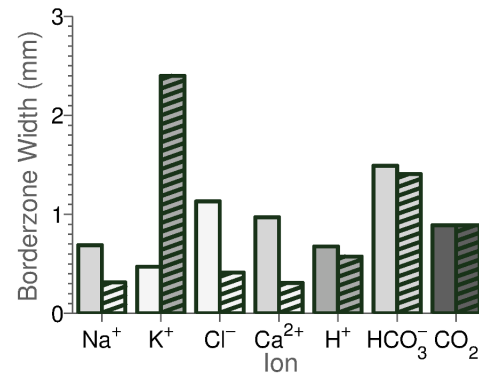
In studies of ischemia  $[Na^+]_i$  tends to increase linearly with time. In the rat heart ischemia caused an increase in  $[Na^+]_i$  by  $78 \pm 8\%$  over 21 minutes [111], by 200% after 40 minutes [112], from 10.5mM to 25mM during 30 minutes ischemia [113], by 170%, 248%, 391% and 405% after 9, 15, 21 and 27 minutes, respectively [114], by two fold over 20 minutes [115], from 6.9mM to 10mM over 30 minutes [116], by 108–120% over 30 minutes [117], by 408% over 27 minutes [118], no change over 10 minutes [108] and by 104–130% over 30 minutes [119]. Changes in  $[Na^+]_i$  in guinea pig hearts during ischemia is controversial with reports of a decrease from 8.8mM to 4.7–7.6mM over 10–15minutes [120] and of an increase of 108% over 15 minutes [121]. Only considering the cases where  $[Na^+]_i$  increases, as these represent a repeatable consensus result, the range of expected increases in  $[Na^+]_i$  over a 5 minute period is 7.5–94%, assuming a linear increase with time. These cluster into two groups with ranges 7.5–38% and 75–94%. In the model reducing the maximum flux of  $NaK$  by 86% caused an increase in  $[Na^+]_i$  to 4.95mM (24%) in the absence of acidosis or 5.57mM (39%) in the presence of the acidotic components of ischemia, described above.

Given the inhibition of  $NaK$  and levels of respiratory and metabolic acidosis a sweep of  $I_{Kb}$  activation values was performed in the presence of these changes to achieve the desired level of extracellular  $K^+$  accumulation. During ischemia,  $[K^+]_e$  increases over three characteristic phases, with the first phase occurring during the initial 5 minutes of ischemia prior to reaching a plateau from minutes 5 to 10, before increasing again. In guinea pigs, ischemia caused  $[K^+]_e$  to increase from 4.2 to 12.6mM over 10 minutes [122] or 4 to 5.8mM over 6 minutes [123]. In swine, ischemia caused  $[K^+]_e$  to increase from 3.3–4.2mM to 10.1–11.5mM after 7–8 minutes [124,125]. In rat, ischemia caused an increase from 4.2mM to 8mM over 5 minutes [110], although other groups have seen a biphasic change in  $[K^+]_e$  in rat with an increase from 5mM to 8.3mM before falling back to 6mM then continuing to rise again, observed over the first 8.2 minutes [126]. In rabbit, ischemia caused  $[K^+]_e$  to increase from 4–4.5mM to 6–9.4mM over 5–10 minutes [10,110,125]. In canine,  $[K^+]_e$  increases from 3.2–4.2mM to 8.1–14.5mM after 6–12 minutes [127,128]. These results indicate an increase in  $[K^+]_e$  from 4mM to 10–14mM after 10 minutes and assuming 80% of this rise occurs in the first 5 minutes [127], and combined with the 5 minute data gives an estimate of  $[K^+]_e$  after 5 minutes of ischemia as 5.5–11mM. In the model an increase in  $I_{Kb}$  of 120% was used to achieve an elevation of  $[K^+]_e$  to 6.5mM, resulting in an increase in the membrane potential of 6.6mV to –73.4mV. This is consistent with measurements in cat (5.4–8.1mV over 10 minutes) [129,130], sheep (5mV over 5 minutes) [131], guinea pigs (13.12mV over 20 minutes) [132] and



**Figure 3. Evolution and profile of A-B)  $[Na^+]_i$ , C-D)  $[K^+]_e$ , E-F)  $[Ca^{2+}]_i$ , G-H)  $pH_i$  and I-J) membrane potential across the BZ due to each component of ischemia.** Complete ischemia,  $NaK$  inhibition,  $I_{Kb}$  inhibition, respiratory acidosis and metabolic acidosis are represented by black, yellow, red, blue and purple lines, respectively. Column 1 shows the profile of ionic concentrations and membrane potential after 5 minutes and column 2 shows the evolution of the change in magnitude in ionic concentrations and potential across the border zone with time.  
doi:10.1371/journal.pone.0060323.g003

mice (16mV over 10 minutes) [133], but less than measurements in rabbit (33mV over 12 minutes [10]) and guinea pig (32.5mV over 15 minutes [120] or 22–29mV over 30 minutes [134–136]). The broad variation in membrane potential changes was not



**Figure 4. Width of ionic BZ.** Gray scale represents magnitude of gradient with white indicating no gradient. Solid bars indicate intracellular gradient and striped bars indicate extracellular gradient.  
doi:10.1371/journal.pone.0060323.g004

unexpected given the range of changes in  $[Na^+]_i$  and  $[K^+]_e$  reported and in simulations an intermediate value has been achieved.

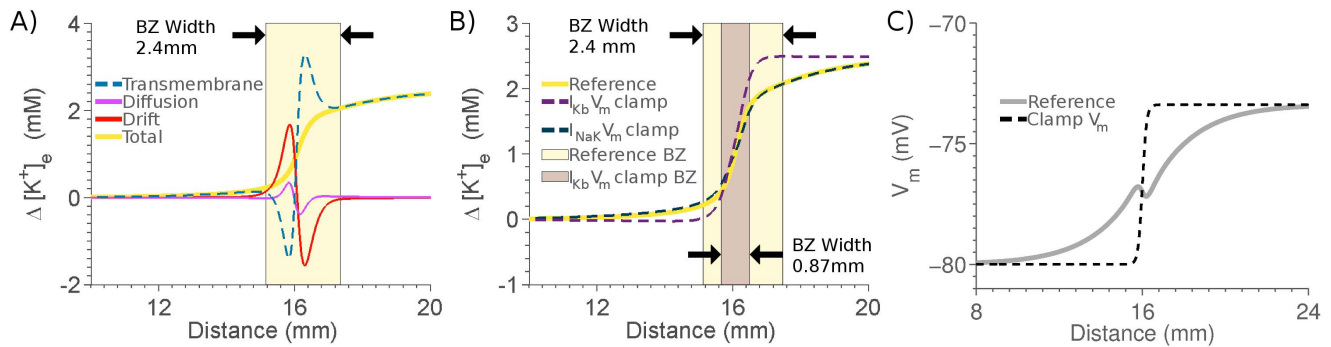
The individual and combined effects of the four components of ischemia on the temporal evolution of the maximum change in ionic concentrations and the spatial concentration and potential distribution profile after 5 minutes of simulated ischemia are shown in Fig. 3. As ischemia progressed,  $[Na^+]_i$  continued to increase. The early rise was attributed to  $NaK$  inhibition; the later increases were due to metabolic and respiratory acidosis. The early rise in  $[K^+]_e$  was significantly affected by  $NaK$  inhibition with  $I_{Kb}$  activation playing a greater role as ischemia progresses and the membrane potential diverges from the  $K^+$  reversal potential. The decrease in  $pH_i$  was solely due to acidosis with no impact from  $I_{Kb}$  activation or  $NaK$  inhibition.  $[Ca^{2+}]_i$  elevation was contributed to principally by  $NaK$  inhibition, while increased  $I_{Kb}$  decreased  $[Ca^{2+}]_i$ . Ischemia caused an initial drop followed by a sustained rise in  $V_m$ .  $I_{Kb}$  activation caused an early hyperpolarisation of the membrane potential, which was subsequently countered by the depolarising effects of  $NaK$  inhibition, with acidosis having a limited effect.

Figure 4 plots the width of the BZ for each ion with striped bars corresponding to extracellular space and the darker the bar the more significant the concentration gradient relative to the initial concentration. This plot shows that  $[K^+]_e$  had a significantly wider BZ with greater magnitude than  $[Na^+]_i$ . For pH regulation,  $H^+$  had a narrower BZ compared to the significantly wider  $HCO_3^-$  BZ, which may indicate the facilitation of proton transport via  $HCO_3^-$  diffusion.

### Extracellular Potassium Gradients

The  $[K^+]_e$  BZ width was significantly wider than other BZ ion widths and notably larger than the  $[Na^+]_i$  BZ width. To determine the cause of this extended  $[K^+]_e$  BZ the source of the cumulative changes in  $[K^+]_e$  due to transmembrane flux, drift or diffusion over the 5 minutes of ischemia were calculated and plotted in Fig. 5. This showed that only the transmembrane flux had a significant gradient across the ischemic region. Separating the transmembrane flux into the  $NaK$  and  $I_{Kb}$  components then identified the  $K^+$  channel, which includes the ATP-inactivated  $K^+$  current, as the cause of this gradient. The gradient of  $I_{Kb}$  was due to the extensive membrane potential gradient into the ischemic region (see Fig. 3). To confirm that this was the cause





**Figure 5. Mechanisms underpinning  $[K^+]_e$  BZ width.** A) Reference change in  $[K^+]_e$  after 5 minutes of simulated ischemia caused by transmembrane flux (blue dashed line), diffusion (purple line), drift (red line) and the total change due to all causes (yellow line). The BZ is indicated by the yellow shaded region. B) Change in  $[K^+]_e$  in the reference model (yellow line) compared with change in  $[K^+]_e$  when  $I_{Kb}$  (purple dashed line) or  $NaK$  (blue dashed line) are exposed to a clamped membrane potential. The reference BZ and BZ when  $I_{Kb}$  is exposed to a clamped membrane potential are indicated by the yellow and purple shaded regions, respectively. doi:10.1371/journal.pone.0060323.g005

of the  $[K^+]_e$  BZ width, the membrane potential was calculated as normal, but an additional clamped membrane potential was calculated at each time step. The clamped membrane potential had the same maximum and minimum values as the correct membrane potential but instead of a smooth gradient across the BZ it had a sharp transition over the BZ. A comparison of this clamped and the control membrane potentials is shown in the Fig. 5C. The effects of using a clamped membrane potential to calculate the  $NaK$  flux or the  $I_{Kb}$  current on the cumulative changes in  $[K^+]_e$  after 5 minutes of simulated ischemia are plotted in Fig. 5B, demonstrating that by removing the gradient in the membrane potential experienced by  $I_{Kb}$  there is a significant narrowing in the  $[K^+]_e$  BZ.

### Drift and Diffusion

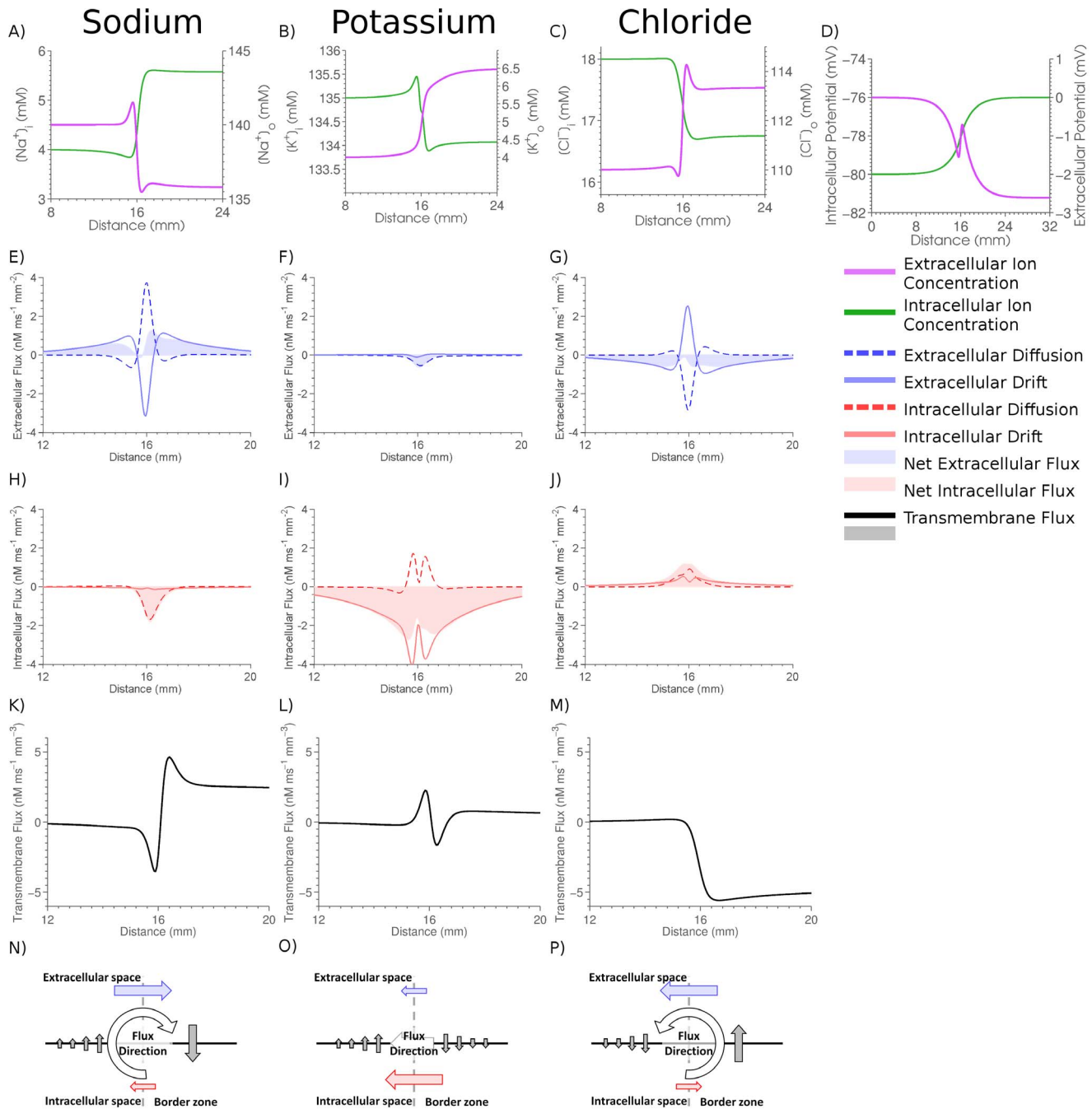
To investigate the relative contribution of drift and diffusion to intra region fluxes (inter or extracellular) the drift and diffusion fluxes in each region were plotted, alongside the transmembrane flux, over the length of the strand after 5 minutes of ischemia. Fig. 6 shows the differences in drift and diffusion between  $Cl^-$ ,  $Na^+$  and  $K^+$ . As expected from the intra and extracellular gradients, intracellular  $K^+$  and  $Cl^-$  diffused into and out of the ischemic region in the intra and extracellular space, respectively. The converse was the case for  $Na^+$ . Due to the decrease in transmembrane potential, characteristic of ischemic regions, there was a convergence of intra and extracellular potentials with the extracellular potential decreasing in the ischemic region and the intracellular potential increasing. This gradient caused positive ions to drift into the ischemic region in the extracellular space and drift out of the ischemic region in the intracellular space. The converse was true for negatively charged ions. As drift is proportional to the ionic concentration,  $Na^+$  drift was significant in the extracellular space and  $K^+$  drift was significant in the intracellular space. For  $Na^+$ , drift and diffusion operated in the same direction in the intra and extracellular space. The result was a cyclical movement of  $Na^+$  moving into the ischemic region in the extracellular space, while moving out of the ischemic region in the intracellular space. The  $Cl^-$  movement was also circular but in the opposite direction (Fig. 6P). However, for  $K^+$  drift and diffusion were in opposite directions. In the extracellular space where the  $K^+$  concentration was low, diffusion dominated and  $K^+$  moved out of the ischemic region. In the intracellular space, where there was a higher concentration of  $K^+$ , drift dominated,

also causing  $K^+$  ions to move out of the ischemic region. Thus ischemia caused a depletion of  $K^+$  in the ischemic region through both the intra and extracellular space and, contrary to previous hypothesis [13], the model suggests that intracellular  $K^+$  movement is the dominant path for  $K^+$  to leave the ischemic region.

### Discussion

In this study a new model of cardiac tissue electrophysiology was developed. The model predicted that the width of the  $[K^+]_e$  gradient across an ischemic BZ would be significantly wider the  $[Na^+]_i$  BZ. The cause of this difference was attributed to the voltage dependence of the  $I_{Kb}$  channel. The model also demonstrated that, due to electrogenic drift,  $K^+$  moved out of the ischemic region in both the intra and extracellular space which will lead to  $K^+$  depletion.

The model of ionic movement and tissue electrophysiology was developed by combining the Nernst-Plank equations with the bidomain framework. No attempt was made to explicitly validate the proposed tissue model equations due to the paucity of experimental data. However, applying simplifying assumptions with regards to ionic or voltage gradients reduces the proposed equations to the well validated bidomain equations [137,138] or coupled reaction-diffusion equations [28,86], respectively, providing support for the validity of the proposed modelling framework. The limited attempts at simulating the spatial temporal evolution of ionic gradients across the ischemic BZ have largely uncoupled the movement of ions and the electric field. Potse et al., [18] demonstrated that measured  $K^+$  gradients across an ischemic BZ could be simulated using a model of  $K^+$  diffusion coupled to a source term. The spatially varying  $[K^+]_e$  gradient could then be included as a boundary condition to models of transmembrane current in the bidomain equations. This model did not include any effect of electric gradients on  $K^+$  movement,  $[K^+]_i$  movement, inter ionic species interactions or the effect of the ischemic region on any other ion gradient. Similar sets of equations to those proposed here have been used for simulating the potential gradient surrounding cells, including the Debye layer [139], electrical propagation along strands of cardiac cells [140,141] and for modelling ion diffusion in the cable equation [142]. These previous models have either explicitly represented the intra and extracellular domains or only considered the intracellular domain



**Figure 6. Regulation of  $Na^+$ ,  $K^+$  and  $Cl^-$  ionic concentrations across the border zone after 5 minutes of ischemia.** Intra and extracellular A)  $Na^+$ , B)  $K^+$  and C)  $Cl^-$  ionic concentrations. D) Intra and extracellular potential. Intracellular drift and diffusion flux of E)  $Na^+$ , F)  $K^+$  and G)  $Cl^-$ . Extracellular drift and diffusion of H)  $Na^+$ , I)  $K^+$  and J)  $Cl^-$ . Transmembrane flux of K)  $Na^+$ , L)  $K^+$  and M)  $Cl^-$ . Schematics showing the general direction of ion movement within and between the intra and extracellular space for N)  $Na^+$ , O)  $K^+$  and P)  $Cl^-$ . doi:10.1371/journal.pone.0060323.g006

but have not modelled the tissue within the bidomain framework, as derived and implemented here.

The proposed equations can be applied generally in three dimensions as opposed to the one dimensional simulations presented here. The current study does not consider the effects of anisotropy on ion or membrane potential gradients across the BZ, however, if implemented in two or three dimensions the model is capable of representing tissue anisotropy and any effects this may have on BZ gradients. By conserving ionic species the

proposed equations provide a more biophysical representation of cardiac electrophysiology than the bidomain equations and can appropriately be applied to simulate a broader range of conditions. However, these benefits come at a cost. Unlike the bidomain equations, with two partial differential equations that can readily be uncoupled and solved as two sets of linear equations [143], the proposed model is nonlinear and contains two parabolic partial differential equations for each ionic species and one elliptic partial differential equation to model the electric potential. This results in

a significant increase both in the complexity and number of equations that must be solved and hence comes at a significant increase in computational cost. The proposed framework can be used to simulate electrically active tissue by introducing a full action potential cell model [31]. This would require identifying and separating out the transmembrane pathways for each ionic species present in the cell model to calculate the net transmembrane flux for each ion or  $J_m^j$  in Eqn 18. The internal cell model state variables, including gating variables, Markov states and intracellular  $Ca^{2+}$  dynamics would also need to be solved, introducing a system of nonlinear ordinary differential equations at each grid point. The small time steps and increased number of degrees of freedom required to simulate electrically active tissue would further increase the computational cost of the proposed model.

A new model of ion movement across the un-stimulated cell membrane was developed. This model has been published online and is available at cellml.org. The model creation approach demonstrated two novel methods. Firstly, the ion transporter densities were uniquely constrained by a small number of experimental data sets and a zero net flux constraint. This provided a repeatable and unique method for determining model parameters under quiescent conditions and could readily be applied to any cardiac electrophysiology model to constrain model parameters. Secondly, in the development of this model a grid of 53 experimental observations were created to provide a comprehensive validation of the model response to changes in ion concentrations and in the presence of blockers of major transporters. Although these observations only provide a qualitative comparison, they do provide a benchmark for quantifying the generality of models. Furthermore, Table 4 identified 19 experiments that do not appear to have been performed or remain controversial, highlighting the potential for additional experiments.

In this study the process of validating the model against 53 experimental observations demonstrated the general capacity of the model to replicate the majority of experimental results. However, the model was unable to match ten of the 53 observations. Five of the experimental observations found no change in a measurement. Due to the numerical nature of the model, even very small changes in a concentration can be observed and without adding in a semi arbitrary threshold that should reflect the variability and confidence of each experimental measurement it was not possible for the model to return no change in a value. In general the five remaining failed observations can be attributed to absent mechanisms in the model or inconsistencies with the model and specific experimental setups. The model did not predict the  $[Cl^-]_i$  response to depressed  $[Na^+]_e$  and the  $[K^+]_i$  response to depressed  $[Cl^-]_e$ . This is potentially due to the absence of NaK2Cl from the model, largely due to the lack of data characterising the transporter. The model was unable to replicate the decrease in  $V_m$  due to elevated  $[Na^+]_e$ . This may be due to the specifics of the experimental protocol. Decreasing  $[Na^+]_e$ , which should have the opposite effect on  $V_m$ , caused both increases and decreases in  $V_m$  in different studies indicating that the  $V_m$  dependence on  $[Na^+]_e$  is sensitive to the specifics of the experimental setup. The model did not predict the change in  $V_m$  or  $H^+$  with a decrease in  $[Ca^{2+}]_e$ . Experimental observations report an increase in  $V_m$  with both a decrease or an increase in  $[Ca^{2+}]_e$ . This may indicate that the  $V_m$  is at some minima with respect to  $[Ca^{2+}]_e$ , although this seems unlikely. It more likely reflects inconsistent data due to differences in experimental setups that were impossible for the model to replicate. In cardiac myocytes it is postulated that  $Ca^{2+}$  and  $H^+$  compete for common

buffering sites [144,145]. The decrease in  $[Ca^{2+}]_e$  may drain the cell of  $Ca^{2+}$ , reducing the  $Ca^{2+}$  bound to buffers that could then be occupied by  $H^+$ , resulting in a decrease in  $[H^+]_i$ . A common pool of  $Ca^{2+}$  and  $H^+$  buffering was not present in the model and this may explain the disparity between model predictions and experimental results. Despite the inability of the model to replicate 5 of the 53 observations, the majority of the absent mechanisms are expected to play a secondary role during ischemia. NaK2Cl is a potential contributor to the elevation in  $[K^+]_e$  [146], although this has been questioned [131], and its absence is unlikely to affect the general model conclusions.

Models simulations found a BZ width for the different ions of between 0.3mm ( $[Na^+]_e$ ) and 2.4mm ( $[K^+]_e$ ). The variation in the width of each ion across the BZ means that there was no single BZ width predicted by the model. The majority of ions transitioned from viable to ischemic concentrations over 0.4–0.8mm, with  $HCO_3^-$  and  $[K^+]_e$  notable outliers. The model predictions are consistent with previous measurements of the BZ between 0.6 and 2mm [10,11,147–149]. However, the model did not include the sharp gradients in metabolites over 0.1mm [11] or the effects of regions of reduced perfusion affecting mechanics over 20 mm distance from the ischemic region [150].

The model predicted that  $[K^+]_e$  and  $[Na^+]_i$  have significantly different BZ widths (Fig. 4). It was expected that the coupling of  $[Na^+]_i$  and  $[K^+]_e$  via NaK would result in concordant gradients in these two ions across the BZ. The extended  $[K^+]_e$  gradient was attributed to the voltage dependence of the  $I_{Kb}$  (Fig 5). Unlike  $[Na^+]_i$ ,  $[K^+]_e$  is regulated by two electrogenic transmembrane pathways  $I_{Kb}$  and NaK, whereas  $[Na^+]_i$  is regulated by multiple exchangers that are electro neutral, or have attenuated voltage dependence, compared to ion channels. This discordance in  $[Na^+]_i$  and  $[K^+]_e$  gradients will have a significant effect on the gradient of action potential morphology across the BZ. Elevation of  $[K^+]_e$  depolarises the cell and shortens the action potential duration, whereas elevation of  $[Na^+]_i$  causes a reduction in action potential duration [151,152]. The combined effect of the two gradients will be a slower change in resting membrane potential on the length scale of the  $[K^+]_e$  gradient and a much more rapid transition in action potential duration due to the faster change in  $[Na^+]_i$  in conjunction with the change in  $[K^+]_e$  over the BZ. The temporal evolution of the two gradients are also distinct, with a sustained constant increase in  $[Na^+]_i$  over the first 5 minutes, while  $[K^+]_e$  increases rapidly for 3 minutes before plateauing (Fig. 3). These simulation results are consistent with experimental measurements of ionic concentrations [111,152] and changes in ECG morphology, which report an early elevation of resting membrane potential, followed by a decrease in action potential duration [153] during early ischemia. These spatial-temporal increases in ion concentrations and secondary effects on electrophysiology will increase tissue heterogeneity and have the capacity to play an important role in the BZ arrhythmogenic substrate.

Experimental measurements have reported a decrease in  $[K^+]_i$  during ischemia [152]. Loss of  $[K^+]_i$  has been attributed to a combination of increased  $I_{Kb}$  conduction and NaK inhibition [152,154]. However, depletion of  $[K^+]_i$  due to transmembrane  $K^+$  movement, in the absence of a potential gradient, would cause an intracellular flux of  $K^+$  into the ischemic zone, due to diffusion, to replenish  $[K^+]_i$ , mitigating the effects of changes of  $K^+$  transmembrane flux on  $[K^+]_i$ . The model proposed here demonstrated that this is not necessarily the case. The model predicted a significant electrogenic  $K^+$  flux in the intracellular space out of the ischemic zone (Fig. 6), resulting in a net efflux of



$K^+$  out of the ischemic zone both in the intra and extracellular space. The movement of  $K^+$  in the intracellular space out of the ischemic zone would further deplete  $[K^+]_i$  in the ischemic region and exacerbate  $[K^+]_i$  loss, but may limit  $K^+$  accumulation in the extracellular space.

### Limitations

The model is inherently an approximation and hence represents a finite set of known cellular properties and changes that occur during ischemia. In particular, the model treated all buffers as static and rapid, the effects of protons on channel, exchanger and co-transporters were not considered, ischemic changes were instantaneous and the model did not include all possible changes or pathways that may affect ionic homeostasis during ischemia.

The tissue model assumed that  $H^+$  and  $Ca^{2+}$  buffers are static, rapid and made up of a single population of binding sites. It is known that some of the buffers for both  $H^+$  and  $Ca^{2+}$  are mobile, these could be introduced into the model framework as an additional concentration but these effects were approximated, without the additional computational cost of adding a additional ionic concentration, by using effective diffusion constants. The equilibrium assumption was likely to be valid in the current model due to the long time scales of interest; however, simulation of cardiac action potentials would require the re-evaluation of this assumption. It is also known that  $H^+$  [28] and  $Ca^{2+}$  [155] are buffered by multiple proteins with distinct binding kinetics but over the range of concentrations simulated these multiple buffer species were unlikely to have significant effects.

The model of intracellular  $Ca^{2+}$  dynamics assumes that the SR and cytosolic  $Ca^{2+}$  concentrations remain in equilibrium, which is clearly not the case during an action potential. The model of intracellular  $Ca^{2+}$  dynamics provided a numerically efficient representation of intracellular  $Ca^{2+}$  buffering and SR  $Ca^{2+}$  uptake. The use of a Hill coefficient of one for SERCA as opposed to the more common and biophysical value of two removed the need for an additional differential equation to model  $[Ca^{2+}]_{SR}$  or the solution of a set of nonlinear equations to model  $Ca^{2+}$  regulation. Furthermore, over the range of  $Ca^{2+}$  values studied it was possible to adjust the maximum SERCA flux to minimize discrepancies between a model with a Hill coefficient of one or two.

It is well recognised that  $H^+$  play an important role in regulating cellular electrophysiology [156]. Experimental and modelling studies have demonstrated the effects of  $H^+$  on ryanodine receptor opening probabilities,  $NCX$ ,  $Ca^{2+}$  channels,  $Ca^{2+}$  buffering and SERCA [22,157]. The majority of the effects of  $H^+$  on  $[Ca^{2+}]_i$  regulation are unlikely to play a significant role in determining the spatial and temporal  $K^+$  and  $Na^+$ . However,

inhibition of  $NCX$  potentially contributes to  $[Na^+]_i$  gradients but this will be secondary to the effects of  $NaK$  inhibition.

The model treats all changes for ischemia as instantaneous. The time dependence of inhibition of  $NaK$ , activation of  $I_{Kb}$ , increased  $[CO_2]_i$  flux or increased  $H^+$  flux are not known and can only be approximated. A linear ramp in ischemic changes has been used previously, but this fails to consider the possibility that changes occur over different time scales. In order to minimise ambiguity in model simulations an instantaneous change in  $NaK$ ,  $I_{Kb}$ ,  $[CO_2]_i$  flux and  $H^+$  flux was chosen.

To limit the scope of this study, the effects of cell swelling and the effects of this on changes in ion concentrations [122] were not included in the model. However, previous, modelling studies have found these effects to not significantly alter  $[K^+]_e$  accumulation and may not fundamentally alter the study conclusions [20]. Mitani and Shattock [146] identified the Na dependent potassium channel as a potential contributor to the elevation of  $[K^+]_e$ . However, the effects of an increase in any  $K^+$  current are captured by the elevation in  $I_{Kb}$  that does not necessarily need to be the sole result of an increase in conduction in the ATP inactivated  $K^+$  channel. Furthermore, the model does not include an increased  $Na^+$  channel conductance during ischemia. This has been reported during ischemia in the form of increased permeability of  $Na^+$  through the persistent  $Na^+$  current [116] and the ATP activated  $K^+$  channel [158]. However, other groups have found a limited impact of the persistent  $Na^+$  channel in  $Na^+$  accumulation during ischemia [159] and previous modelling studies have shown that its inclusion is not required to capture the salient features of ischemia in the single cell [20]. For these reasons a potential increase in the  $Na^+$  channel conductance was not included in this study.

### Summary

A new mathematical framework was derived for simulating cardiac tissue electrophysiology with ion species conservation. The model was used to simulate the movement of ions due to transmembrane channels, pumps and transporters, diffusion and drift in the intra and extracellular space. The model predicted that 1) the sodium BZ is approximately a quarter of the length of the potassium BZ and this is due to the effects of the membrane potential gradient on  $I_{Kb}$  and 2) that during ischemia there is a gross movement of potassium ions out of the ischemic region in both the intra and extracellular space due to the effects of drift, which will lead to a depletion of  $K^+$  from the ischemic region.

### Author Contributions

Conceived and designed the experiments: SAN. Performed the experiments: SAN. Analyzed the data: SAN. Contributed reagents/materials/analysis tools: SAN. Wrote the paper: SAN.

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