OptMAVEn – A New Framework for the *de novo* Design of Antibody Variable Region Models Targeting Specific Antigen Epitopes



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Abstract

Antibody-based therapeutics provides novel and efficacious treatments for a number of diseases. Traditional experimental approaches for designing therapeutic antibodies rely on raising antibodies against a target antigen in an immunized animal or directed evolution of antibodies with low affinity for the desired antigen. However, these methods remain time consuming, cannot target a specific epitope and do not lead to broad design principles informing other studies. Computational design methods can overcome some of these limitations by using biophysics models to rationally select antibody parts that maximize affinity for a target antigen epitope. This has been addressed to some extend by OptCDR for the design of complementary determining regions. Here, we extend this earlier contribution by addressing the de novo design of a model of the entire antibody variable region against a given antigen epitope while safeguarding for immunogenicity (Optimal Method for Antibody Variable region Engineering, OptMAVEn). OptMAVEn simulates in silico the in vivo steps of antibody generation and evolution, and is capable of capturing the critical structural features responsible for affinity maturation of antibodies. In addition, a humanization procedure was developed and incorporated into OptMAVEn to minimize the potential immunogenicity of the designed antibody models. As case studies, OptMAVEn was applied to design models of neutralizing antibodies targeting influenza hemagglutinin and HIV gp120. For both HA and gp120, novel computational antibody models with numerous interactions with their target epitopes were generated. The observed rates of mutations and types of amino acid changes during in silico affinity maturation are consistent with what has been observed during in vivo affinity maturation. The results demonstrate that OptMAVEn can efficiently generate diverse computational antibody models with both optimized binding affinity to antigens and reduced immunogenicity.

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Introduction

Therapeutic antibodies are widely recognized to be among the most promising agents to treat various diseases, including cancers, immune disorders, and infections [1,2]. The earliest used technology for the generation of therapeutic antibodies is raising antibodies against a target antigen in immunized mice. Although widely utilized, the low clinical success rate using mouse antibodies reflects that these foreign proteins can be highly immunogenic in humans, and they typically have weak interactions with human complement and antibody receptors, resulting in inefficient effector functions [3]. These limitations have largely been overcome by grafting the variable domains of a mouse monoclonal antibody to the constant domains of a human antibody, a process known as chimerization [4,5]. Although chimeric antibodies are more human-like and induce considerably less response by the human immune system, they are still not completely human. More recently, complete human antibodies have been designed using directed evolution techniques [6,7] that mimic the natural selection of the process to evolve antibodies towards a desired

property. Among them, phage display [8,9], a technique based on the presentation of peptides or protein fragments on the surface of bacteriophages, is most widely used and offers robust and complementary routes to the generation of potent human antibodies. Despite these advances in the design of antibodies, current experimental methods still have considerable limitations and cannot: (1) target a specific antigen epitope, (2) provide universally applicable structural design routes, and (3) rationally engineer mutations with significantly reduced immunogenicity.

By contrast, computational methods could efficiently overcome some of these shortcomings. For example, a number of successful applications of computational methods have been reported in antibody-antigen recognition [10–13], antibody structure and stability prediction [14–17], design of mutations and antibodyantigen interface [16–22], and immunogenicity prediction [23,24]. However, most of the current examples of computational antibody design have been largely limited to existing antigen–antibody complex structures (i.e. re-designs of antigen–antibody interfaces), and the *de novo* design of antibodies to target a pre-selected antigen epitope has remained elusive.

To address the limitations of current platforms for antibody design, we have developed the OptCDR method that can de novo design an antibody paratope model against any targeted antigen epitope by modeling and optimizing the complementarity determining regions (CDRs) [21]. However, CDRs only capture part of the binding capacity of an antibody and were not constrained to fully human designs. Therefore, in this paper we take the next step and introduce a new computational framework named OptMAVEn for de novo design of not just the CDRs, but fully human, complete antibody variable domain models by expanding the concepts pioneered in OptCDR. OptMAVEn designs antibody models by mimicking the natural evolution of antibody generation and affinity maturation (Fig. S1). In particular, it is implemented as a three-step workflow (Fig. 1). First, for a given antigen, an ensemble of possible antigen binding conformations is generated in a virtual antibody-binding site. This site is defined as a rectangular box that covers all the geometry centers of 750 antigen epitopes with known structures (Fig. 2A-2D). Second, the best scored antigen conformation and combination of six modular antibody parts from the Modular Antibody Parts (MAPs) database [25] are selected using a mixed-integer linear programming (MILP) formulation and the initial antibody structure is predicted by assembling the six MAPs. Third, the antibody model is redesigned and optimized through our Iterative Protein Redesign & Optimization (IPRO) protocol [26].

A new aspect in the last step of OptMAVEn is that we incorporated a 9-mer-sequence-based humanization algorithm to reduce the potent immunogenicity of designed antibody models while optimizing their binding affinity to an antigen. The immunogenicity of an antibody is triggered by molecular recognition of its immunogenic peptides by the major histocompatibility complex (MHC) and/or T cells [27]. A variety of humanization methods such as CDR grafting [28], resurfacing [29], superhumanization [30], framework shuffling [31] and guided selection [32] have produced antibodies more homologous to human sequences, often but not always leading to reductions in immunogenicity to clinically acceptable levels [33]. Our approach is inspired by a humanness score termed "human string content" (HSC) [23] that quantifies a sequence at the level of potential MHC/T cell epitopes. HSC is principally based on the assumption that having more human sequence present in the antibody will reduce its immunogenic potential [34-36].

OptMAVEn aims at designing a diverse library of antibody models that is simultaneously co-optimized on both binding affinity to an antigen epitope and immunogenicity. The resulting computational antibody models are *de novo* designs, probably never seen in nature before, generated *de novo* through



Figure 1. OptMAVEn workflow. Step 1: Antigen positioning. Step 2: Assembly of antibody models targeting the antigen epitope. Step 3: Affinity maturation and humanization of antibody models by redesigning. doi:10.1371/journal.pone.0105954.q001



Figure 2. Illustrations of antibody-binding site and the algorithm of antigen positioning. H and L chains are colored in cyan and green, respectively; epitope is colored in magenta. (A) Database of 750 antibody-antigen structures. H and L chains are colored in cyan and green. Antigens are in different colors. (B) All the complex structures superimposed onto a reference antibody structure whose coordinate center of CDRs attachment points was placed on the origin. (C) A rectangular box that covers all the mean epitope coordinates. Figure S2 shows the distributions for the mean coordinates of all the epitopes along the X, Y, and Z axes. (D) The virtual antibody-binding site. (E) An antigen initial conformation. Epitope is colored in magenta. (F) The rotated antigen conformation having the most negative epitope coordinates. (G) A positioned antigen conformation with epitope's geometry center at one grid point. (H) A rotated antigen conformation around Z axis.

computations. In this study, we benchmarked the corresponding protocols in each step individually and show that OptMAVEn could: (1) efficiently position antigens in the antibody-binding site with a high success rate of 96% using a benchmark set of 120 experimentally determined antigen-antibody complexes (2) rediscover 57.5% of native antibody parts using MILP based optimization for the same benchmark set (3) recapitulate known interactions responsible for affinity maturation using two known germline and affinity maturation antibody pairs as the benchmark set and (4) unambiguously distinguish human antibody sequences from other species (P value <0.000001). As case studies, we applied OptMAVEn to design broadly neutralizing antibody models against two antigens: envelope glycoprotein gp120 (gp120) and hemagglutinin (HA), which are well-known antigens for the HIV-1 and influenza viruses, respectively. The presented designs are diverse in sequence and structure spanning a wide array of affinity maximization interactions. These designed interactions (partially) mimic the geometry of their natural receptors while maintaining the computational humanness of the sequences. Overall, our results demonstrate that OptMAVEn is a computational framework for an open challenge that could make significant contribution to the development of a new generation of therapeutic antibodies and vaccines.

Method

Step 1: Antigen positioning

Antigen positioning starts with the definition of a general antibody-binding site (Fig. 2A-2D), which is represented by a rectangle grid box located close to the origin. This box was obtained by analyzing the locations of known antigen epitopes from a precompiled antibody-antigen crystal structure database consisting of 750 antibody-antigen complexes and sharing three common features: (1) X-ray resolution is better than 2.5 Å, (2) both heavy and light chains are available in the structures, and (3) an antigen is included for each structure. Among the 750 structures, there are 214 hapten, 109 peptide and 427 protein binders. The size of the box was adjusted to include all the mean coordinates of atoms of antigen epitopes, and its X, Y and Z values were within the ranges of (-10 Å, 5 Å), (-5 Å, 10 Å) and (3.75 Å), 16.25 Å), respectively (Fig. 2D). The box was divided into a set of grid points by assigning grid spacing, which is user-defined (default of 2.5, 2.5 and 1.25 Å for X, Y and Z axis, respectively). During the positioning, the coordinate center of an antigen epitope was placed into its corresponding grid box (Fig. 2G) and rotated along the Z coordinate for 360° with an interval of 60° (Fig. 2H) to generate an ensemble of initial antigen positions. Prior to positioning, the antigen was rotated so that the epitope had the most negative Z coordinates (Fig. 2E and 2F), thus ensuring that the target epitope forms the maximum number of interactions with the CDRs. In total, 3234 (7×7×11×6) initial positions of antigens were generated for this study.

Step 2: Assembly of antibody models targeting the antigen epitope

At each position, the interaction energies (IEs), including van der Waals and electrostatic terms, between the antigen and all MAPs were calculated and stored. To avoid detrimental clashes, a "softening" atom van der Waals radius whose value is half of that from the CHARMM force field [37] was used to estimate the hydrophobic interaction. The modular antibody parts were previously constructed in the spirit of template-based modeling, with each part being a prototype structure of the random variable (V), diversity (D), and joining (J) regions in the MAPs database [25]. The recently generated database contains 929 parts constructed from an analysis of 1168 human, humanized, chimeric, and mouse antibody structures and encompasses all currently observed structural diversity of antibodies. Table S1 shows the numbers of antibody parts from the MAPs database. V, CDR3 and I structures can assemble both H and L chains of an antibody. There exist two types of light chain, KAPPA and LAMBDA, which are treated separately. Each MAPs structure was numbered using IMGT's unique numbering [38-41] and consistently placed in the 3D space so that its CDRs attachment points were approximately on the same X-Y plane and centered on the origin with CDRs perpendicularly directed in the positive Z direction.

Once the IEs are calculated, the problem of selecting the best scoring combination of non-clashing antibody parts at each position could be mathematically represented using an MILP representation. requires the definition of the index set IThis $I = \{i | HV, HCDR3, HJ, KV, KCDR3, KJ, LV, LCDR3, LJ\},\$ denoting modular antibody parts. H denotes Heavy, K for KAPPA and L for LAMBDA. V denotes Variable region, CDR3 for Diversity region and J for the Joining region. Also required is the set $P = \{p \mid 1, 2, ..., N_i\}$, which denotes the number of MAPs structures at position *i*. Set *IP*^{clash} contains all pairwise MAPs combinations (*i*1, p1) and (i2, p2) that sterically clash with one another. The binary variables $X_{i,p}$ denotes if antibody part p is selected at position i $(X_{i,p} = 1)$ or not $(X_{i,p} = 0)$. Parameter $E_{i,p}^s$ encodes the calculated energy between structure p at position i and the antigen substrate. Switching parameters H_d and L_d have values of one if a VH or VL respectively, are being designed and zero if they are not chosen. This allows the user to possibly design only a VH or VL, as would be appropriate for a nanobody. The MILP formulation can then be written as follows:

$$Minimize \sum_{i=1}^{9} \sum_{p=1}^{N_i} X_{i,p} E_{i,p}^s$$
(1)

$$X_{i1,p1} + X_{i2,p2} \le 1, \quad \forall (i1,p1,i2,p2) \in IP^{clash}$$
 (2)

$$\sum_{p=1}^{N_i} X_{i,p} = H_d, \qquad \forall i \in \{HV, HCDR3, HJ\}$$
(3)

$$\sum_{p=1}^{N_i} X_{KV,p} = \sum_{p=1}^{N_i} X_{KCDR3,p} = \sum_{p=1}^{N_i} X_{KJ,p}$$
(4)

$$\sum_{p=1}^{N_i} X_{LV,p} = \sum_{p=1}^{N_i} X_{LCDR3,p} = \sum_{p=1}^{N_i} X_{LJ,p}$$
(5)

$$\sum_{p=1}^{N_i} X_{KV,p} + \sum_{p=1}^{N_i} X_{LV,p} = L_d \tag{6}$$

Equation 1, the objective function, entails the minimization of the interaction energy between the antigen and the selected MAPs. The inequality in Equation 2 precludes the simultaneous presence of two antibody part structures that sterically clash. Equation 3 guarantees exactly one part is selected for each heavy chain region when a VH is designed. OptMAVEn defines both KAPPA and LAMBDA light chains and Equations 4-6 make sure that when a VL is being designed, it is composed of parts entirely from one domain type or the other. Equation 4 requires that the same number of KAPPA V, CDR3, and I structures are selected and Equation 5 does the same for the LAMBDA structures. Equation 6 then selects either a KAPPA or LAMBDA V part when a VL domain is being designed, and Equations 4 and 5 together ensure the selection of the proper type of CDR3 and I structures. The optimization formulation described collectively by Equations (1-6) can be solved using CPLEX [42] called directly from Python.

After the MILP selection, the lowest energy solutions (10 in our current study) were selected and submitted to local refinement (i.e., 500 iterations) by randomly moving antigens and reselecting the optimal MAPs. The goal of the refinement is to explore the local conformational space for the antigen and to energetically rescreen the best MAPs. In each iteration, the antigen was randomly translated and rotated for a small distance and angles whose value was generated using a Gaussian distribution centered at zero with a standard deviation of 0.5 Å and 5°, respectively. Subsequently, the IEs between the antigen at this position and the entire MAPs database were reevaluated. A simulated annealing algorithm was used to determine whether or not to retain the results of the iteration.

Step 3: Computational affinity maturation and humanization by redesigning

The refined antibody models were redesigned with IPRO [26] in order to find sequences that maximally improve the binding affinity and possess minimal computational immunogenicity. The standard IPRO design protocol was modified for use in OptMAVEn, which consists of five main steps: sequence design, backbone perturbation, optimal rotamer selection, antigen redocking and energy evaluation. This sequence is carried out iteratively (default max of 10,000 iterations).

Sequence design. For each round, a set of 1–3 continuous residues in either VH or VL is randomly selected for mutation. Residues from CDRs are given 3-fold higher preference over those

from frameworks (FRs) because more mutations are expected in the binding site [25]. A selected residue is allowed to mutate to a set of permitted amino acid types that is site-specific and could be determined according to sequence alignments of relevant antibodies. In this study, the alignments of broadly neutralizing HIV and influenza antibody sequences were used (Data S1 and S2).

At the same time, during the sequence design, a sequence-based humanization algorithm is introduced to guarantee that designed sequences are human. This algorithm starts with constructing a human antibody 9-mer sequences database by splitting 69,032 human antibody sequences (collected from Abysis [43], IMGT [38] and the PDB database [44]) into 1,309,657 unique human 9-mers. For a given test sequence, all the possible 9-mer sequence frames are extracted and the minimum number of mutations between each frame and those from the human 9-mer-sequence database is counted. All frame scores are totaled and defined as the humanness score (HScore, Equation 7).

$$HScore(S) = \sum_{n=1}^{N} M_n^{\min}$$
⁽⁷⁾

S denotes a given antibody sequence, N is the total number of all the possible 9-mers-fragment sequences, and M is the minimum count of the mutations between a 9-mer sequence and those from the human 9-mer fragment database. During each iteration only sequences with HScore equal to or lower than the previous iteration are retained for further optimization.

Backbone perturbation. Once the sequence is designed, the perturbed region, which includes 5 more residues on both sides of the design positions and surrounding residues within 4.5 Å, is subjected to backbone perturbation. For each one of the perturbed residues, the φ and ψ dihedral angles are randomly perturbed using a Gaussian distribution centered at zero degrees with a standard deviation of 1.5°. No modification greater in magnitude than five degrees is permitted. Five residues on each side of the perturbed region are free to move during the perturbation to prevent the dihedral angle changes from causing long-range structural effects. These residues are mutated to glycine and an energy minimization with strong restraints on the perturbed dihedral angles is carried out to make the perturbed structure. All other residues are fixed in place during the process. Different backbone conformations are sampled by iteratively perturbing small regions of the backbone that are randomly chosen during each cycle throughout the variable domains.

Optimal rotamer selection. The following step of IPRO involves the use of a rotamer library and MILP optimization to repack the amino acid side chains in and around the perturbed region. The perturbed residues that are mutated to glycine are always repacked. The residues that are spatially close to the perturbed region are also repacked. Only design positions within the perturbed region are permitted to mutate. The permitted kinds of amino acid mutations for each design position are specified during the sequence design stage. We use the abbreviations R and NR to refer to antibody designed residues (side-chains) and antigen/conserved antibody parts, respectively.

The R–NR (i.e. the antigen and all parts of the antibody that are not being replaced by rotamers) and R-R interaction energies are calculated using the pairwise additive, non-bonded energy terms from the force field (i.e. van der Waals, electrostatics, and implicit solvation). Once all of the R-NR and R-R interaction energies have been calculated, MILP optimization is used to select the minimum energy arrangement of rotamers. The rotamer selection MILP has been previously discussed [26].

Antigen redocking. The fourth step of an IPRO iteration is a local, rigid-body redocking of the antigens. Since docking may take a long time for some antigens, this step is only carried out every third iteration. Docking uses the same pairwise additive energy functions used during the rotamer selection step. During docking, an antigen is randomly perturbed along and around the X, Y, and Z axes. The perturbations are generated using a Gaussian distribution centered at zero, with user-defined standard deviations (defaults of 0.2 Å and 2.0°). After the antigen is perturbed, the net IE is evaluated and the movement of the antigen is sequentially randomly perturbed during an iteration of docking, and a user-defined number of iterations are carried out (default of 500 iterations).

Energy evaluation. The fifth step involves a total energy minimization and complex and interaction energies evaluation. A high-resolution score function that evaluates van der Waals, electrostatics, bonds, angles, dihedral angles, improper dihedral angles, and generalized Born with molecular volume integration implicit solvation energy functions from CHARMM is used. The complex and interaction energies are used in the Metropolis criterion to determine whether or not to retain the results of the IPRO iteration. The user may set the temperature used to make the decision (default is to retain 25% of designs within 10 kcal/mol of the best design).

Benchmark test set

For benchmarking our antigen positioning and MILP selection algorithms, we curated a non-redundant set of bound antibodyantigen complex structures gathered from IMGT [40]. Identical antigens in different binding modes with antibodies were also included. This set includes 120 antibody-antigen complex crystal structures (Table S2) and at present, we only focus on the antigens that are either peptides or small proteins. Amino acid lengths for the antigens range from 4 to 148. This set is used to characterize the distribution of antigen epitopes, verify the initial antigen positioning and adjust the energy function. To test the IPRO design algorithm, we chose two germline (GL) / affinity matured (AM) pairs, all with known X-ray structures. Among them, one antibody pair is broadly neutralizing influenza virus antibody CH65 (AM) [45] and its putative GL precursor [16], and another is broadly neutralizing HIV-1 gp120 antibody VRC01 (AM) [46] and its GL precursor [17]. The influenza HA1 and HIV-1 gp120 antigens were both modeled into the binding sites of their corresponding GL antibodies referencing their positions in the AM complex structures. For testing the proposed HScore, human, mouse, rat and rabbit antibody sequences were collected from Abysis [43] with the number of residues between 90 and 130.

Implementation

OptMAVEn is primarily written in Python and C++ and is available for download on our website, http://maranas.che.psu. edu. The most computationally demanding modules such as energy calculation, antigen positioning and humanness scores calculation are implemented in C++. Parts of OprMAVEn such as energy calculation between antigens and the entire MAPs and computational affinity maturation may use several processors at a time by sharing files. Using its default parameters and 10 processors as an example, a design run against an antigen with 100 amino acids is expected to take no more than three weeks.

| Table 1. Minimu | m RMSDs between the | native and positione | ed poses. | | | | |
|-----------------|---------------------|----------------------|-----------|---------|------|------|------|
| | | | | | | | |
| Peptide | | | | Protein | | | |
| PDB | RMSD | PDB | RMSD | PDB | RMSD | PDB | RMSD |
| 1ACY | 1.79 | 2G5B | 1.86 | 18J1 | 2.11 | 3DVG | 2.71 |
| 1CE1 | 2.35 | 2H1P | 2.98 | 1DZB | 1.35 | 3E8U | 2.40 |
| 1CFS | 2.41 | 2HFG | 2.50 | 1EGJ | 3.74 | 3ETB | 2.35 |
| 1CFT | 1.93 | 2HH0 | 2.30 | 1FBI | 2.76 | 3G6D | 3.23 |
| 1CU4 | 1.99 | 2HKF | 2.17 | 119R | 2.48 | 31U3 | 2.67 |
| 1E4W | 2.35 | 2HRP | 1.69 | 1JHL | 1.55 | 3KS0 | 2.31 |
| 1EJO | 1.47 | 2IGF | 2.48 | 1JRH | 4.68 | 3L5W | 1.80 |
| 1F90 | 1.69 | 2J4W | 1.83 | 1KIQ | 1.86 | 3L5Y | 1.96 |
| 1FPT | 1.61 | 20QJ | 2.62 | 1MLC | 3.42 | 3LQA | 3.88 |
| 1661 | 2.43 | 20R9 | 1.79 | 1NSN | 2.12 | 3NFP | 3.09 |
| 1HH6 | 2.02 | 20SL | 2.85 | 10AZ | 2.28 | 3NH7 | 2.96 |
| 1HIN | 1.86 | 2QHR | 2.77 | 1ORS | 3.23 | 300R | 4.05 |
| 1181 | 1.89 | 2QSC | 2.79 | 1RJL | 1.84 | 3P30 | 3.79 |
| 1JP5 | 1.86 | 2R0W | 2.02 | 1TQB | 2.23 | 3QWO | 1.97 |
| 1KC5 | 2.06 | 2ZPK | 2.19 | 1TZH | 3.89 | 3RKD | 3.24 |
| 1KCR | 3.08 | 3BAE | 1.75 | 1TZI | 3.88 | | |
| 1KTR | 2.13 | 3BKY | 2.61 | 1V7M | 2.82 | | |
| 1MVU | 1.28 | 3CVH | 3.13 | 1W72 | 2.69 | | |
| 1N64 | 1.55 | 3CXD | 2.56 | 1XIW | 2.10 | | |
| 1NAK | 2.57 | 3EYU | 2.42 | 1ZTX | 1.96 | | |
| 10BE | 4.05 | 3F58 | 2.50 | 2BDN | 1.77 | | |
| 1P4B | 2.70 | 3FFD | 2.78 | 2DQJ | 2.03 | | |
| 1PZ5 | 2.31 | 3FN0 | 2.64 | 2FJH | 3.75 | | |
| 1QKZ | 2.03 | 3G5V | 1.75 | 2HVK | 1.44 | | |
| 1QNZ | 2.27 | 3GGW | 2.24 | 2IFF | 3.52 | | |
| 1SM3 | 2.36 | 3GHB | 1.92 | 2JEL | 2.74 | | |
| 1TET | 2.56 | 3GHE | 1.56 | 2QR0 | 4.28 | | |
| 1TZG | 1.69 | 3GJG | 2.91 | 2R29 | 2.28 | | |
| 1U8J | 2.17 | 3HR5 | 2.27 | 2VWE | 4.30 | | |
| 1UWX | 1.74 | 3MLR | 2.16 | ZVXQ | 1.88 | | |
| 1XGY | 2.05 | 3MLS | 1.88 | 2VXS | 3.52 | | |
| 2A6I | 2.33 | 3MLW | 2.37 | 2ZUQ | 2.49 | | |
| 2B1H | 2.14 | 3MLX | 2.08 | 3AB0 | 2.36 | | |
| 2CK0 | 2.82 | 3MLY | 2.48 | 3BDY | 2.94 | | |

| Table 1. Cont. | | | | | | | |
|-------------------------|-----------------|------|------|---------|--------|----------|---------|
| | | | | | | | |
| Peptide | | | | Protein | | | |
| PDB | RMSD | PDB | RMSD | PDB | RMSD | PDB | RMSD |
| 2EH8 | 2.35 | 3QG6 | 2.48 | 3D85 | 2.63 | | |
| | | | | | | | |
| | Average | Std | Min | Max | Medium | Accepted | Failure |
| Peptide | 2.25 | 0.47 | 1.28 | 4.05 | 30% | 69% | 1% |
| Protein | 2.75 | 0.84 | 1.35 | 4.68 | 20% | 72% | 8% |
| doi:10.1371/journal.por | ne.0105954.t001 | | | | | | |
| | | | | | | | |
| | | | | | | | |

Results

Benchmark test of the initial antigen positioning

The starting point for an OptMAVEn design is the positioning of the target antigen in a predefined antibody-binding site in order to obtain the initial antigen conformations. To evaluate whether the positioning protocol is capable of generating near-native poses, we tested it against a benchmark set (Table S2) that contains 120 antigens varying in both length and conformations. As described in the Methods and shown in Fig. 2, each antigen was first rotated to make the epitope have the most negative Z coordinates and then positioned into the binding site box with its mean epitope coordinate placed in every grid point with rotations around Z axis. We used Root Mean Squared Deviation (RMSD) of backbone atoms between an antigen position and its corresponding native conformation as a metric for evaluating the quality of positioning. The quality of a positioning is classified as high (RMSD < 1.0 Å), medium (1.0 Å<RMSD<2.0 Å), and acceptable (2.0 Å< RMSD<4.0 Å) according to CAPRI-defined criteria for protein docking [11]. A successful prediction was described as a positioning run in which at least one of the ensemble members of initial positions has an acceptable RMSD (i.e. <4.0 Å). The benchmark results of antigen positioning are summarized in Table 1. Across the entire benchmark set, OptMAVEn successfully predicted at least acceptable or better quality solutions for 115 targets, representing an overall success rate of 96%, which indicates OptMAVEn could sample the correct antigen orientation and position without any a priori knowledge of antibodybinding site. With respect to antigen type, OptMAVEn successfully predicted near-native structures for 99% of the peptide antigens and 92% of the protein antigens. The slightly better predictions of conformations of peptide antigens are most likely due to their relatively simple and linear epitopes.

Four representative positioning successes of PDB 1MVU, 1NOZ, 1DZB and 2FEL with RMSDs of 1.28, 2.27, 1.35 and 2.74 Å, respectively, are illustrated in Figure 3. As observed, the predicted positions of 1MVU and 1DZB are in close agreement with their corresponding native poses. For 1NQZ and 2FEL, the prediction quality is considered acceptable and further translations and rotations could improve the positions. The predictions for 1OBE and 1JRH serve as representative examples of positioning failures with RMSDs of 4.05 and 4.68, respectively. For 1OBE, the predicted conformation of its L-shaped antigen adopted an almost opposite orientation compared to its native pose; for 1JRH, considerable differences are derived from rotations around the X and Y axes. In both cases, erroneous positioning mainly arise from the approximation of using coordinate centers of antigen epitopes for representing the entire epitopes, and further rigid-body rotations around X and Y axes are required for successful positioning. Extra rotation sampling around the X and Y axes will almost certainly give more accurate predictions, at the expense of longer computational time.

Benchmark test for the MILP based residue design step

In OptMAVEn, the variable domain of an antibody structure is initially predicted by assembling the six best-scoring MAPs (HV, HCDR3 and HJ for VH; KV, KCDR3, KJ or LV, LCDR3, LJ for VL) if both the VH and VL are being designed. For a given antigen conformation, the IE between this antigen and each MAPs is calculated using a pairwise energy functions involving both van der Waals and electrostatic terms (MILP energy). The MILP formulation described in Equations 1–6 is used to select the combination of MAPs structures with the lowest IE. To measure whether the MILP selection could identify native antibody parts



Figure 3. Examples of positioning successes and failures for peptide and protein binders. H and L chains are colored in cyan and green, respectively. Antigens are colored in yellow (native poses) and orange (best positioned poses). doi:10.1371/journal.pone.0105954.q003

efficiently, we tested it on the same benchmark set used to evaluate antigen positioning. Starting with only the native pose of each antigen, the IE to the best MAPs is compared to that to its native antibody part. The results are summarized in Table S3. For each complex, we also performed a further energy minimization and reevaluated the IE using the full CHARMM energy function.

In the majority of cases, calculated MILP IEs were negative, indicating favorable binding between antibodies and antigens. In contrast, for five cases (1KTR, 1OAZ, 1TZH, 2A6I and 2IFF) native antibodies were predicted to disfavor the antigen binding. This could arise from subtle steric clashes or over-approximated MILP energy functions. Therefore, we further minimized each complex and reevaluated the IEs using the full Charmm energy function, including the van der Waals, electrostatics, bonds, angles, dihedral angles, improper dihedral angles and generalized Born with molecular volume integration implicit solvation terms. Using this more detailed description for IE led to negative IEs for all antigen-antibody complexes. This suggests that with a relaxation and energy reevaluation step, it is possible for the MAPs structure selection MILP to design initial antibody models that successfully bind the antigen for favorable initial antigen positions (e.g. native positions).

Of particular note is the fact that for 51/120 cases (i.e. 42.5%), the selected antibody models have better CHARMM IEs than the

native antibodies, by an average of 95.2±90.7 kcal/mol. In the other 69 cases, the native complex is better by an average of 91.8±64.4 kcal/mol. It is not surprising that OptMAVEn identifies initial antibody models in some cases that have higher energy interaction scores than the native antibodies for two reasons. First, at any given moment the immune system will not have all possible naïve antibodies available, so suboptimal antibodies can be expected to be chosen in many cases. In contrast, MILP selection will always be able to pick an optimal combination of MAPs structures. Second, the objective of an immune response is to eliminate a problem as rapidly as possible, not to design optimally binding antibodies. Although strong binding is important, other factors such as stability, concentration, and when an antibody is discovered play a role. Since OptMAVEn is solely trying to design optimal binders, it is to be expected that the designed antibody models would differ from the naturally occurring ones.

Benchmark test of the IPRO design

We next assessed the performance of the computational affinity maturation protocol in IPRO using two experimentally characterized GL and AM antibody pairs against influenza virus (AM antibody CH65) and HIV-1 (AM antibody VRC01), respectively. Structures for each pair of GL and AM structures were available [16,17,45,46]. Experimental data shows that the GL precursor of CH65 possesses 200-fold lower binding affinity to HA1 than the matured CH65 [16], and that VRC01 exhibits no detectable affinity for wild-type gp120 [17]. Two design tests were performed. The first one considered mutations only among the residues that differ between GL and AM and a second where all residues could be mutated. The first test aimed to evaluate whether IPRO could redesign the antibody model to match the amino acid usage patterns in the AM pair starting from the GL sequence. The second test, without specified mutation positions, broadly models affinity maturations aiming to evaluate whether IPRO would independently discover results highly similar to natural affinity maturation.

In the first test, forward and reverse designs were conducted for both systems. Forward design is denoted here as a design starting from a GL structure, while reverse design is the one starting from an AM structure. For each design, mutations along the entire sequence were specified according to their corresponding GL/AM partners. For each design, 25 independent IPRO trajectories were generated and the final IE results are the average of the trajectories, as listed in Table 2. As expected, the IEs indicate that the AM antibodies bind to antigens more tightly than the GL antibodies, which is in agreement with the free energy calculation

Table 2. Forward and reverse designs using IPRO with specified positions for mutations.

| Antibody | Structure ^a | Mutatio | ns ^b | IE | | IE difference ^d | |
|----------------|------------------------|---------|-----------------|------|------|----------------------------|--|
| | | И | VL | GL | АМ | | |
| Influenza CH65 | 4HK0 (GL) | 11 | 6 | -294 | -444 | -150 | |
| | 3SM5 (AM) | | | -295 | -389 | -94 | |
| HIV VRC01 | 4JPK (GL) | 39 | 25 | -167 | -258 | -90 | |
| | 3NGB (AM) | | | -272 | -384 | -111 | |

^aThe starting X-ray structures used for IPRO designs. GL in the parentheses indicate the structure is germline and AM is for affinity maturation.

^bThe number of mutations identified by comparing GL and AM antibody sequences.

^cInteraction energy between an antigen and an antibody. All energies are in kcal/mol.

^dThe IE difference calculated from AM - GL.

| Table 3. Forwar | d designs using IPF | RO without specifi | ed positions for mutations. | | | |
|-----------------|-------------------------|------------------------|--|-----------------|-------|----------------------------|
| Antibody | Structures ^a | Mutations ^b | Native mutations recovery ^c | IE ^d | | IE difference ^e |
| • | | | | GL | АМ | |
| Influenza CH65 | 4HK0 | 17 | 6 | -294 | -1663 | -1359 |
| HIV VRC01 | 4JPK | 64 | 13 | -167 | -1247 | -1080 |

^aThe starting structures used for IPRO designs. GL in the parentheses indicate the structure is germline and AM is for affinity maturation.

^bThe number of mutations identified by comparing GL and AM antibody sequences.

^cThe numbers of designed mutations occurring both in GL and AM antibodies.

^dInteraction energy between an antigen and an antibody. All energies are in kcal/mol.

^eThe IE difference calculated from AM - GL.

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 (ΔG) in Table S4. That this result could be recapitulated in forward and reverse designs for both systems demonstrates the robustness of the sampling and scoring function of IPRO. This is critical for the correct identification of a set of mutations that improve binding to an antigen.

In the second test, only forward designs were performed because the aim is to assess the ability of IPRO to recapitulate the native mutations. The preferred amino acid types for FR residues were assigned according to site-specific amino acid probabilities obtained from the alignments of existing broadly neutralizing influenza and HIV antibodies, respectively (Data S1 and S2). No mutation positions or preferred amino acid types for the CDRs were specified. As seen in Table 3, in the designed sequences 35% and 20% of mutations in the native AM influenza and HIV-1 antibody models, respectively, are recaptured. These percentages are comparable to those from a protein interface design for Ran GTPase with 22-39% native sequence recovery using singleconstraint design strategy and mutating only interface residues [47]. Our design is more challenging because the entire sequence space requires sampling, typically more than 200 positions for paired heavy and light variable domains. In addition, it has been observed that native somatic mutations evolved from the same GL antibody against the same antigen epitope can be quite diverse [43,44,48]. Among the ten VRC01-like HIV broadly neutralizing antibodies isolated by RSC3 binding from different donors, only two residues from the same germline IGHV1-2*02 allele mature to the same amino acids [48]. Therefore, for a given mutation position there exist multiple native mutations. In this test, we used only one AM antibody as the reference for defining the native mutations. The two reported percentages of native mutation recovery would be higher if multiple AM antibodies were used as native references.

Benchmark test for the humanness score

The fundamental assumption of our humanization protocol is that human sequences contain ensembles of local sequences that possess minimal immunogenicity due to a lack of binding to MHC and/or recognition by T cells. Based on this assumption, HScore in OptMAVEn was developed to measure the 9-mer differences of all possible 9-mer frames in a test sequence by comparing them to a precompiled human 9-mer-sequence database. An immunological fragment with size of 9 is chosen because it is the basic peptide unit required for high affinity binding to MHC II [49]. Essentially, an antibody humanness score should have the ability to differentiate human antibody sequences from other species' antibody sequences (e.g. mouse) with high specificity. To meet this end, analysis of the human, mouse, rat and rabbit antibody sequences was performed according to the HScore definition and the results are summarized in Table 4. According to its definition, a lower HScore indicates sequences that are more homologous to human antibody sequences and are predicted to have lower immunogenicity than a higher HScore and vice versa.

Overall, there was a marked difference in HScores between the human and mouse sequences with p < 0.000001. Even better statistical significances were observed for the rat and rabbit antibodies, but the number of sequences evaluated was many

Table 4. Calculated HScores of human, mouse, rat and rabbit sequences.

| Species | Region | Number of sequences | Mean ^a | SD (±) ^b |
|-----------|--------|---------------------|-------------------|---------------------|
| Human | VH | 3000 | 0 | 0 |
| | VL | 3000 | 0 | 0 |
| Synthetic | VH | 720 | 40 | 41 |
| | VL | 599 | 21 | 33 |
| Mouse | VH | 3462 | 54 | 29 |
| | VL | 3480 | 34 | 27 |
| Rat | VH | 1062 | 57 | 42 |
| | VL | 173 | 99 | 49 |
| Rabbit | VH | 244 | 149 | 18 |
| | VL | 244 | 109 | 19 |

^aThe mean of HScore.

^bThe standard deviation of HScore.

fewer than for mouse. It appears that synthetic sequences are more similar to those of human than mouse, rat and rabbit. For example, synthetic VL has a mean lowest mean HScore of 21. The lower HScore of synthetic antibodies are consistent with their sequence contents, which are often created through joining two genes, one of which is human. Conversely, rabbit VH has the highest mean HScore of 149, indicating it has the most different local 9-mer sequences to human VL sequences. Overall, our results demonstrate that HScore is an efficient humanization score for evaluating the predicted immunogenicity of a target antibody sequence by correctly differentiating human sequences from other mammal.

Two case studies: Design of models against influenza hemagglutinin and HIV gp120

We showed that OptMAVEn could accurately position antigens in the predefined antibody-binding site, select appropriate antibody parts from MAPs and identify interaction energy improving mutations while distinguishing human from other mammal sequence. OptMAVEn is carried out by combining antigen positioning, MILP based antibody model assembly and IPRO based *in silico* affinity maturation as a complete pipeline. For demonstration we applied OptMAVEn to design broadly neutralizing antibody models that target HA and gp120, which are well-know antigens for the influenza [45,50–52] and HIV-1 [46,53–55] viruses, respectively.

Identification of epitope

HA proteins, which attach the influenza virus to sialic acid receptors on the cell surface, are a prime drug target. The majority of human antibodies are directed against sites on the head of HA1, in particular the receptor-binding site, to prevent the attachment of virus to target cells. Other antibodies target the stem region to prevent membrane fusion. In this study, we target the receptorbinding site of HA1, the epitope in PDB 3SM5. The B chain and some residues of chain A far from the binding site were ignored to reduce computation time. The receptor-binding site is a broad and shallow pocket framed by three loops and one helix forming the outer ridges, illustrated as the 130-loop (magenta), the 150-loop (yellow), the 190-helix (blue) and the 220-loop (red) in Fig. S3A. The second study involves designing antibody models against the gp120 protein of the human immunodeficiency virus type 1 (HIV-1). Gp120 is a glycoprotein exposed on the surface of the HIV envelope vital for virus entry into a cell. A series of broadly anti-HIV-1 neutralizing antibodies bind to sites located in variable regions of gp120 and help prevent HIV infection. In this study, we designed antibody models targeting the CD4-binding site of gp120 [56]. The gp120 structure was obtained from PDB 3NGB and the epitopes residues are located in CD4-binding-loop, V5-loop and D-loop (Fig. S3B). For each antigen, we chose two targeted epitopes: one includes all the residues in the receptor-binding site (named as HA-all and gp120-all, respectively) and another includes residues that form a loop in the receptor-binding site (i.e., 130-loop for HA1 (HA-130) and CD4-binding-loop for gp120 (gp120-365)).

Assembly of antibody models from MAPs

Table 5 reports the selected best MAPs structures for each epitope before and after a local conformation refinement of the antigen. The negative MILP energies in each case suggest the selected MAPs structures favor antigen binding. Significantly reduced MILP energies were observed after a refinement of the local antigen conformation and a reselection of the best MAPs

| Epitope" Kerinement" | H chain | | | L chain ^c | | | Rmsd ^d | MILP ^e |
|----------------------|---------|------|---|----------------------|---------|-------|-------------------|-------------------|
| | > | CDR3 | ٦ | > | CDR3 | ٦ | | |
| HA-all No | m | 58 | - | 44 (K) | 185 (K) | 1 (K) | I | - 147 |
| Yes | 114 | 428 | 5 | 61 (K) | 147 (K) | 3 (K) | 2.2 | -510 |
| HA-130 No | 123 | 283 | - | 44 (K) | 46 (K) | 1 (K) | | - 263 |
| Yes | 48 | 124 | - | 45 (K) | 199 (K) | 1 (K) | 2.1 | -638 |
| gp120-all No | 29 | 420 | 5 | 15 (K) | 64 (K) | 1 (K) | I | - 448 |
| Yes | 29 | 420 | - | 27 (K) | 7 (L) | 1 (L) | 2.3 | -625 |
| gp120–365 No | 19 | 114 | ε | 2 (K) | 1 (K) | 3 (K) | ı | -402 |
| Yes | 19 | 196 | - | 31 (L) | 32 (L) | 5 (L) | 2.1 | -736 |



Figure 4. Designed antibody model. (A)–(D) Model structures for epitopes of HA-all, HA-130, gp120-all and gp120-365 before (in yellow) and after (in orange) refinements. (E)–(H) MILP reselected best scored MAPs after refinements. H and L chains are colored in cyan and green, respectively. V, CDR3 and J represent corresponding MAPs (See definition in Method). doi:10.1371/journal.pone.0105954.q004

structures. Note that the refinement step was only performed for the antigen position with the best-scored MAPs structures and aims to provide a further local conformational sampling around the best conformation from the initial screen. Comparing the antigen conformations before and after refinement (Fig 4A–D), with all RMSDs higher than 2 Å, confirms that local antigen refinement had a pronounced effect on the antigen conformations and the selection of the best-scored MAPs structures.

Figure 4E-H show the selected MAPs structures. It can be seen that the CDR3s in both VH and VL exhibit considerable diversity, in accordance with their critical roles in recognizing different epitopes. In addition, the V parts exhibit some variability as well, especially in the CDRs. By contrast, there is less variability in the selected J parts. The selection results from these four designs indicate that the MILP could identify promising initial antigen positions. Once the best low energy conformations are identified, an additional refinement step is required to explore the local antigen positions for obtaining the final modular parts.

In silico affinity maturation and humanization

To increase the relevance of the identified designs, the permitted amino acid mutations at each FR position were preselected according to the amino acid frequency of each kind of amino acid at that position in alignments of broadly neutralizing HIV and influenza antibodies (Data S1 and S2). However, the residues in CDRs were allowed to mutate into any of the 20 standard amino acids. Figure 5 depicts the predicted lowest-energy amino acid sequences and corresponding alignments between the initial and designed sequences. The sequence distribution of mutations involved in affinity maturation is very diverse, with no clearly preferred amino acids/positions.

The HA-all and HA-130 antibody models have 10/9 and 11/19 mutations in VH/VL, respectively (Table 6). In contrast, gp120-

all and gp120–365 antibody models have 12/7 and 11/6 mutations in the corresponding domains. Antibodies typically accumulate 5–20% changes in somatic mutations, but in the case of HIV-1-neutralizing antibodies, the level of somatic mutation ranges from 15% to 44% [57]. Our results suggest that the mutation rate from computational affinity maturation is comparable to that of somatic mutations evolved *in vivo*.

For all four designs, the IPRO results show significant energy improvements both in complex and interaction energies, alluding that the designed antibody models are much more stable and could bind to the antigens more tightly (Table 6). Figure 6 shows the amino acid compositions before and after affinity maturation. Interestingly, Glu, Gly, His, Met, Arg and Ser occur more than other amino acids (counts > = 3) in designed sequences, whereas Leu, Pro and Tyr occur less frequently (counts < = 3). Table 7 summarizes the changes of usage during affinity maturation. An apparent trend is that charged residues are favorable in the affinity mature sequences while aromatic residues are disfavored. Despite the importance of aromatic residues in the binding to antigens [31], this finding is in agreement with previous studies that tyrosine and tryptophan are abundant in the germline genes and the degree of aromaticity is typically reduced during affinity maturation [58]. Meanwhile, the number of polar residues is slightly increased. More polar and charged residue occurrences contribute to the improvement of binding affinity and complex stability in the solvent.

Table 6 lists the humanness score for the initial and designed antibody model sequences. Most of the initial sequences, except for the HA-130 light chain and gp120–365 heavy chain possess low humanness scores, indicating they are already human-like sequences and probably have low immunogenicity. The predicted immunogenicity contributions of designed sequences are primarily from CDR3 because the V* and J* model structures in the MAPs



Figure 5. Alignments between designed and initial antibody model sequences for epitopes of HA-all, HA-130, gp120-all and gp120-365. FRs, CDRs regions and the lengths of sequences are indicated on top of each alignment. Yellow shading shows introduced amino acid mutations.

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database are based on human genes whereas CDR3 has some mouse genes to ensure the maximum amount of structural diversity [25]. After the design, as expected, the humanness scores are decreased or maintained at a similar level. For example, the HScore of gp120–365 light chain is reduced to 0 from 4 and that of HA-130 heavy chain is maintained at 0, both predicting no immunogenicity in the final designs. However, it is also noted that the light chain of HA-130 still has a HScore of 32, comparable to a mouse or rat sequence. This shows that upon design the highest binding affinity design may not have low immunogenicity.

The two generated designs against HA1 exhibit highly diverse amino acid sequences, and antigen locations/orientations, but all share the receptor-binding site (Fig. 7A and 7B). Interestingly, the HA-all antibody model possesses a long HCDR3 loop composed of 26 amino acids, which does not bind directly to the epitope residues, but interacts with non-epitope loops on the right side of HA1, as shown in Figure 7A. Such unusually long CDR3s [59] are rarely found in existing HA1 antibodies, and provide a larger antigen-binding surface, potentially introducing more favorable interactions. Moreover, both HCDR1 and HCDR2 insert into the receptor site and interact directly with the 130-loop with four hydrogen bonds (Fig. 7E). In receptor analog LSTc bound to 1934 HA (PDB 1RVZ), the carboxylate group of sialic acid forms two hydrogen bonds with backbone amide of HA1 Ala137, as does the side-chain hydroxyl oxygen of HCDR2 Tyr58 with the backbone amide of HA1 Ala80. The amide of the acetamido group has a hydrogen bond with the backbone oxygen of HCDR1 Val135, as does the backbone oxygen of HA1 with HCDR1 Ser35 (Fig. 7G). In addition, the side-chain carboxyl oxygen of HCDR2 Asp59 of HA-130 antibody model forms the same hydrogen bond with the backbone amide of HA1 Ala80 (Fig. 7F). Thus, the designed HAall and HA-130 antibody models partially mimic the human receptor that interacts with HA1 via insertion of HCDR1 and HCDR2 into the receptor-binding site. This mode of receptor mimicry has also been observed in related broadly neutralizing antibodies CH65 [45] and 5J8 [60], which use HCDR3 insertion, and S139/1, which uses HCDR2 insertion. Significantly, the algorithm automatically generated these results with the only user input being the identification of the epitope as a whole. The recapitulation of this trend suggests that OptMAVEn could reproduce expected antigen binding motifs. The newly designed antibody models are expected to broadly neutralize a large number of strains from a single HA or selected strains from different subtypes and groups of influenza because the epitope in the receptor-bing site is relatively conserved [61].

Both of the designed antibody models against gp120 are predicted to interact directly with the targeted CD4-binding loop. However, they adopt quite different binding modes (Fig. 7C and 7D). The gp120-all antibody model uses the residues where LCDR2 attaches to grasp virtually all surface-exposed portions of the CD4-binding loop. One hydrogen bond is formed: the sidechain guanidinium nitrogen of Arg67 with the backbone oxygen of gp120 Gly228 (Fig 7I). By contrast, the gp120-365 antibody model uses HCDR3 to interact with CD4-binding loop, which involves three hydrogen bonds: the amide nitrogen of HCDR3 Gln108 with the backbone oxygen of gp120 Ser365; the backbone oxygen of Gln108 with the backbone nitrogen of gp120 Gly367; the backbone nitrogen of HCDR3 Gly110 with the carboxyl oxygen of gp120 Asp368 (Fig. 7]). Among CD4-binding sitedirected antibodies, most antibodies (such as the VRC01 class) structurally mimic the CD4 receptor (Fig. 7H, PDB 3JWD) by substantial β -strand contacts to the epitope using HCDR2 [56]. The HCDR3-dominated mode of interaction adopted by the gp120-365 antibody model is similar to a recent isolated broadly neutralizing HIV-1 antibody CH103 [33], which is less mutated than most other CD4-binding site antibodies and reveals a new loop-based mechanism of antibody neutralization.

Summary and Discussion

Previously, we have developed OptCDR for the de novo design of antibody binding pockets composed of CDRs against any specified antigen. We used OptCDR to generate a library of antibody CDRs models against the FLAG antigen (i.e. DYKD) [62] and a preliminary analysis of biological experiments has shown multiple, unique antibody bindings (unpublished data). Here, by expanding the idea of OptCDR, we presented an efficient and general method for de novo design of the computational models of the entire antibody variable domain targeting a specific antigen epitope. Given an antigen, the method entails positioning the antigen in a virtual antibody-binding site, identifying the best modular parts from the MAPs database based on the positioned antigen poses, de novo assembly of these MAPs into the initial antibody model structure, and designing mutations in the antibody model structure to simultaneously improve binding affinity and reduce immunogenicity. For both HA and gp120, novel antibody models with numerous interactions with their target epitopes were generated. The observed rates of mutations and types of amino acid changes are consistent with what has been seen during in vivo affinity maturation. It is especially encouraging that these features were not controlled for in OptMAVEn but were automatically generated. Additionally, in the case of the HA antibody models, a method of antigen binding that has been previously observed in broadly neutralizing anti-influenza antibodies was discovered in both designs.

In OptMAVEn, a pre-generated conformer library was adopted to represent the possible antigen binding poses. Despite success in most of the 120 benchmark cases (success rate of 96%), in some cases, the antigen positioning algorithm still could not sample any conformation having a RMSD within 4 Å of the native. This limitation may have largely been due to the insufficient rotational sampling of antigens around the X and Y axes. Although this limitation could be overcome by adding further sampling around both axes, caution should be taken. For each antigen conformation, its IE to each modular antibody part needs to be precalculated and this computation could quickly become intractable with a significantly increased number of antigen conformations. Therefore, it is suggested to choose an appropriate size of the conformer library by adjusting the parameters of antigen positioning if further sampling is required.

OptMAVEn generates a prototype antibody model that targets an antigen by assembling the six best-scored MAPs structures. This idea is inspired by the natural evolution of an antibody *in vivo*, in that the gene of a germline antibody is initially assembled

| Epitope ^a | Stage ^b | Complex Energy ^c | IEd | Mutation count ^e | | HScore ^f | |
|--|---|---|-------|-----------------------------|----|---------------------|----|
| | | | | т | _ | т | |
| HA-all | Before | - 10588 | -184 | | | 6 | 10 |
| | After | - 12391 | -1495 | 10 | 6 | 5 | 10 |
| HA-130 | Before | -12413 | -99 | 1 | | 0 | 54 |
| | After | - 13965 | -1422 | 11 | 19 | 0 | 32 |
| gp120-all | Before | - 14956 | -131 | | | 5 | 2 |
| | After | -15316 | -898 | 12 | 7 | 4 | ~ |
| gp120-365 | Before | - 14188 | -233 | 1 | 1 | 19 | 4 |
| | After | -14438 | -1106 | 11 | 6 | 19 | 0 |
| ^a The epitope used for designs. See ^b Before or after the design. ^c The entire complex energy. Unit in ^d The interaction energy between th ^e The number of mutations between ^f The humanness score. See the defir doi:10.1371/journal.pone.0105954.t0(| he definition in the meth- kcal/mol. Pantibody and antigen. U the designed sequence a uition in the method. | od. Jnit in kcal/mol. Ind the initial sequence. | | | | | |

6. Summary of

Table (

energies, mutations and HScores of the four best designed antibody models for epitopes of HA-all, HA-130, gp120-all, and gp120-365.



Figure 6. Counts of the type of amino acid mutations before (blue) and after (red) computational affinity maturation from the four best designed antibody models for epitopes of HA-all, HA-130, gp120-all, and gp120-365. doi:10.1371/journal.pone.0105954.g006

by V-(D)-J recombination. Note that the three differing MAPs regions do not match exactly with their V-(D)-J genes because MAPs utilizes CDR3 as a structural component representing the whole diversity region. The primary advantage of using MAPs to assemble an antibody model is that the prediction is fast and there is no need for de novo folding calculations. The computational savings do not come at the expense of accuracy of prediction, as the RMSD of the predicted structures is at least as accurate as earlier methods [25]. In addition, compared to traditional fragment-assembly-based approaches for de novo protein structure prediction, this approach could efficiently sample both local and non-local contacts that are inherently present in the relatively large structural fragments. The designed sequences therefore should have a higher probability of proper folding. It should be also noted that MAPs database includes a considerable amount of information on pairwise clashes between parts. These clashes can thus be avoided by not selecting both members of the pair by the MILP problem in OptMAVEn. The aim of the MILP problem is to find the best combination of the six MAPs with the lowest IEs with the targeted antigen. In its current implementation, it does not explicitly account for the interactions between MAPs except for excluding clashing pairs. In our benchmark test, we found that the selected MAPs have better IEs than native antibodies in 42.5% of 120 cases. While approximations in the energy function may account for some of the improved scores, the general trends allude

that the cohort of designed sequences should bind more tightly than the native ones.

A simplification of the protocol in its described implementation is that it uses IE instead of binding free energy for evaluating the binding affinity of an antigen and antibody model. Although we found that IEs are in good agreement with experimental binding data in two GL-AM antibody pairs, this replacement is still at the expense of an overall bias in energy function, especially in systems where conformational entropy is crucial for the binding interaction. This is supported by the fact that we obtained large negative IEs (Table S3) that are not quantitatively comparable to true experimental binding energies for predicting the binding affinity of native antigens and antibodies. This may have been due to a lack of entropy term in the formulation of IE (Table S4). Effective entropy could quantify the variability of sequence and their rotamer states that are consistent with a target structure and other properties specified as constraints on the properties of the sequences [63]. However, the role of side-chain entropy plays in protein design is still unclear. For example, both Kendra [17] and Daniele et al. [64] demonstrate that changes in protein conformational entropy can contribute significantly to protein sequence design. Conversely, Hu et al. suggest that side-chain conformational entropy has a relatively small role in determining the preferred amino acid at each residue position in a protein except for longer amino acids: methionine and arginine [17]. Neverthe-

Table 7. Statistics of amino acid propensities from the four best designed antibody models for epitopes of HA-all, HA-130, gp120-all and gp120–365.

| Stage ^a | Aliphatic ^b | Aromatic ^b | Polar ^c | Charged ^c |
|--------------------|------------------------|-----------------------|--------------------|----------------------|
| Before | 35 | 7 | 28 | 15 |
| After | 29 | 1 | 31 | 24 |

^aBefore or after the design.

^bThe counts of amino acids belonging to this classification.



Figure 7. Structures and binding modes of designed antibody models for epitopes of HA-all, HA-130, gp120-all, and gp120-365. H and L chains are colored in cyan and green, respectively. Antigens are colored in orange. Hydrogen bonds are highlighted in dashed line and colored in magenta. (A)–(D) Overall complex structures. (E) and (F) Antibody models that recognize 130-loop in the receptor-binding site of HA1. (G) Interaction of receptor analog LSTc in the receptor-binding site of HA1. (H) Interaction of CD4 and CD4-binding loop of gp120. (I) and (J) Antibody models that recognize of CD4-binding loop of gp120. doi:10.1371/journal.pone.0105954.g007

less, future work will consider introducing an appropriate entropy model into the energy evaluation.

Another concern in the energy function is the employed Lazaridis-Karplus implicit solvation model [65] which does not adequately capture charged residue interactions with the solvent. This is reflected by some test designs where charged residues were continually selected without solvent exposure (data not shown). This is a limitation of current implicit solvation models, which yield higher or similar water-to-protein transfer free energies for nonpolar as for many of the polar residues. As a result, they improperly favor the burial of polar amino acids in the protein interior over nonpolar ones [66].

During design runs, we also found that the energy calculations often end up with a local energy minimum instead of the global energy minimum due to the incomplete sampling of the complex energy landscape given the allotted cpu time. This could lead to inconsistent results between different repetitions of the same computational design run. To address this issue, we introduced ensemble structure refinement, which is a refinement carried out by generating an ensemble of structures (default of 10) from the "refinement" iterations (default of 25) of IPRO. A structural refinement has the same steps as a normal IPRO iteration except no mutations are allowed. After all refinement iterations have been completed, the average properties of the refinement ensemble are evaluated to determine whether or not a particular design is actually the best identified so far. This ensemble approach to evaluating structures has given a high correlation ($\mathbb{R}^2 = 0.960$) between calculated IEs and experimentally measured binding affinities in previous work [17].

Another challenge for the *de novo* design is the uncertainty associated with the employed scoring function [63]. For example, energy functions are approximate, side-chain conformations are treated discretely and solvation is represented using simplified models. One solution is to apply site-specific amino acid probabilities, which takes advantage of known inter-atomic interactions and structural features to yield sequence information consistent with naturally folded structures and desired functional properties. It is well known that highly conserved residues are generally distributed in the FRs, whereas the residues in CDRs tend to be considerably diverse. Therefore, in OptMAVEn, we applied two different strategies to determine the permitted amino acid kinds to mutate for residues both from FRs and CDRs. The permitted kinds for FRs residues were site-specific and the probability in each position was obtained from the sequence alignment of broadly neutralizing HIV and influenza antibodies (Data S1 and S2), while those for CDRs residues had no any constraint at all. In both case studies, multiple solutions with quite different sequences and binding modes were identified. Improved mutations were found in both the FRs and the CDRs. The designed antibody models have an apparent trend of obtaining more polar and charged residues while disfavoring aromatic residues.

Designed antibody models could be immunogenic and cause an unexpected and serious immune reaction if applied. To address this issue, we introduced an HScore to evaluate the immunogenicity of designed antibody models in silico. The aim is to limit the sequence design to mutations that either maintain or increase the human-like sequence content. Our algorithm is inspired by a very similar humanization method called HSC [23], which is calculated by determining the maximal identity between a string of test sequence and any sequence in an aligned set of human sequences, and summing theses values over all pertinent sequence positions. Although HScore works well to distinguish human antibody sequences from other species, it should be noted that OptMAVEn does not guarantee the design of antibody models without any immunogenicity (HScore = 0) under the current design parameters. OptMAVEn seeks to design antibody variant models simultaneously having reduced immunogenicity and improved binding in silico, and these two properties are often in inverse proportion (i.e. high affinity binders may possess high immunogenicity and vice versa). This is supported by our case studies, where the designed light chain of HA-130 still has an HScore of 32. This is comparable to what would be expected in a mouse antibody. Also, fewer mutations were found to occur in CDR3, where a considerable amount of energetically favorable mutations were observed in naturally occurring AM antibodies. Parker et al. demonstrated a similar difficulty in optimizing both the stability and immunogenicity of therapeutic proteins by a structure-guided deimmunization strategy [28]. Another probable reason for the failure of deimmunization is that the maximum number of allowed residues (3 under the current study) to mutate and the site-specific amino acid probabilities both impose limits on the number of sequences for immunogenicity evaluation. During some IPRO iterations, few or no mutations are presented for further energy optimization. As a result, in general trade-offs must be made to design antibody models either with predicted moderate binding affinity and lowest immunogenicity or highest binding affinity and moderate immunogenicity.

Supporting Information

Figure S1 The assembly and affinity maturation of gemline antibody. The variable region of the heavy chain is generated from variable (V), diversity (D) and joining (J) gene

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segments, whereas the variable regions of the light chains are generated from V and J gene segments. For the heavy chain, the first two CDRs and three framework regions (FRs) of the variable region are encoded by V gene. CDR3 is encoded by a few nucleotides of V, all of D, and part of J segment, while FR4 is encoded by the remainder of the J segment. For the light chain, V gene segment encode the first two CDRs and three FRs of the V region, plus a few residues of CDR3. J segment encodes the remainder of CDR3 and the fourth FR. (TIF)

Figure S2 The distribution of the mean XYZ coordinates of antigen epitopes. (A) Along X axis. (B) Along Y axis (C) Along Z axis.

(TIF)

Figure S3 The epitopes of influenza HA1 (A) and HIV-1 gp120 (B). H and L chains are colored in cyan and green, respectively. Antigens are colored in yellow and epitopes are colored in blue, magenta and yellow, respectively. (TIF)

Table S1Numbers of antibody modular part structuresin MAPs.

(DOCX)

Table S2Native antibody-antigen structure set.(DOCX)

Table S3 Interaction energies for antibody-antigencomplexes.

(DOCX)

Table S4Binding free energy for forward and reversedesigns using IPRO with specified positions for muta-tions.

(DOCX)

Data S1 The alignments of broadly neutralizing HIV and influenza antibody sequences.

(TXT)

Data S2 The alignments of broadly neutralizing HIV and influenza antibody sequences. (TXT)

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Author Contributions

Conceived and designed the experiments: TL RJP CDM. Performed the experiments: TL RJP. Analyzed the data: TL RJP. Contributed to the writing of the manuscript: TL RJP CDM.

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