Research Article

Analysis of One-Bond Se-Se Nuclear Couplings in Diselenides and 1,2-Diselenoles on the Basis of Molecular Orbital Theory: Torsional Angular Dependence, Electron Density Influence, and Origin in ¹*J*(**Se, Se**)

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Nuclear couplings for the Se-Se bonds, ¹*J*(Se, Se), are analyzed on the basis of the molecular orbital (MO) theory. The values are calculated by employing the triple *ζ* basis sets of the Slater type at the DFT level. ¹*J*(Se, Se) are calculated modeled by MeSeSeMe (**1a**), which shows the typical torsional angular dependence on ϕ (C_{Me} SeSe C_{Me}). The dependence explains well the observed ¹*J*obsd(Se, Se) of small values ([≤] 64 Hz) for RSeSeR (**1**) (simple derivatives of **1a**) and large values (330–380 Hz) observed for 4-substituted naphto[1,8-*c*, *d*]-1,2-diselenoles (**2**) which correspond to *symperiplanar* diselenides. ¹*J* (Se, Se : **2**) becomes larger as the electron density on Se increases. The paramagnetic spin-orbit terms contribute predominantly. The contributions are evaluated separately from each MO (ψ_i) and each $\psi_i \to \psi_a$ transition, where ψ_i and ψ_a are occupied and unoccupied MO's, respectively. The separate evaluation enables us to recognize and visualize the origin and the mechanism of the couplings.

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1. Introduction

Indirect nuclear spin-spin coupling constants (*J*) provide highly important information around coupled nuclei, containing strongly bonded and weakly interacting states, since the values depend on the electron distribution between the nuclei $[1-10]$ $[1-10]$. One-bond $({}^{1}J)$, two-bond (*geminal*) $({}^{2}J)$, three-bond (*vicinal*) $({}^{3}J)$, and even longer coupling constants $\binom{n}{y}$ $(n \geq 4)$ are observed between selenium atoms, which will give important information around the coupled nuclei. The mechanism for $\frac{1}{J}$ must be of the through-bond type; however, that for $\binom{n}{r}$ ($n \geq 2$) would contain through-space interactions, especially for nJ ($n \geq$ 4). Quantum chemical (QC) calculations are necessary for the analysis and the interpretation of the *J* values with physical meanings. Important properties of molecules will be clarified by elucidating the mechanism of spin-spin couplings on the basis of the molecular orbital (MO) theory.

Various ¹*J*_{obsd} (Se, Se) values are reported for alkyl and/or aryl derivatives of dimethyl diselenide (**1a**) (RSeSeR : **1**). They are usually small $({}^{1}J_{\text{obsd}}(Se, Se: 1) \leq 64 \text{ Hz}$; see [Table 1\)](#page-1-0). We examined $\frac{1}{J}$ (Se, Se) of naphto[1,8-c,d]-1,2diselenole $(4-Y-1,8-Se₂C₁₀H₅(2): Y = H (a) [11-15], OMe$ $(4-Y-1,8-Se₂C₁₀H₅(2): Y = H (a) [11-15], OMe$ $(4-Y-1,8-Se₂C₁₀H₅(2): Y = H (a) [11-15], OMe$ (\mathbf{b}) , Me (\mathbf{c}) , Cl (\mathbf{d}) , COOMe (\mathbf{e}) , CN (\mathbf{f}) , and NO₂ (\mathbf{g})), which correspond to the *symperiplanar* diselenides (Figure 1). The 1 *J* (Se, Se) values are measured for 2c, 2d, and 2g, and large 1 *J* _{obsd}(Se, Se) values of 330–380 Hz are detected. [Table 1](#page-1-0) summarizes the ${}^{1}J$ $_{\text{obsd}}$ (Se, Se) values.

Why are $\frac{1}{J}$ _{obsd}(Se, Se: 2) much larger than $\frac{1}{J}$ _{obsd}(Se, Se: 1)? How do $\frac{1}{J}$ _{obsd}(Se, Se: 2) depend on the substituent Y in 2 ? $\frac{1}{2}$ (Se, Se) are analyzed on the basis of the MO theory, as the first step to investigate the nature of the bonded and nonbonded interactions between selenium atoms through *nJ* (Se, Se) [\[18](#page-8-1)]. ¹ *J* (Se, Se) are calculated for **1a** and **2a**–**g**.

According to the nonrelativistic theory, there are several mechanisms contributing to the spin-spin coupling con-stants. As expressed in [\(1\)](#page-1-1), the total value ($^{n}J_{TL}$) is composed

TABLE 1: Observed ¹*J*_{obsd}(Se, Se) values of some selenium compounds.

Compound	$^{1}I_{\rm{obsd}}(Se, Se)$ [Hz]	Comment
tBuSeSeMe	2.7	(a)
nBuSeSeMe	36.3	(a)
MeSeSePh	22	(a)
o -O ₂ NC ₆ H ₄ SeSeCN	64	(b)
$2(Y = Me)$	379.4	This work
$2(Y = Cl)$	375.9	This work
$2(Y = NO_2)$	330.8	This work

(*a*) References [\[9](#page-7-4), [16\]](#page-8-2).

(*b*) References [\[9,](#page-7-4) [17](#page-8-3)].

of the contributions from the diamagnetic spin-orbit (DSO) term ($^nJ_{\text{DSO}}$), the paramagnetic spin-orbit (PSO) term ($^{n}J_{\text{PSO}}$), the spin-dipolar (SD) term ($^{n}J_{\text{SD}}$), and the Fermi contact (FC) term ($^{n}J_{\text{FC}}$),

$$
{}^{n}J_{\text{TL}} = {}^{n}J_{\text{DSO}} + {}^{n}J_{\text{PSO}} + {}^{n}J_{\text{SD}} + {}^{n}J_{\text{FC}} . \qquad (1)
$$

[Scheme 1](#page-2-0) summarizes the mechanism of the indirect nuclear spin-spin couplings. The origin of the terms, $^nJ_{DSO}$, $^nJ_{PSO}$, $^nJ_{SD}$, and $^nJ_{FC}$, is also illustrated, contributing to $^nJ_{TL}$. The ground state of a molecule (*M*) is the singlet state (S_0) if the nuclei (N) in M have no magnetic moments. However, the ground state cannot be the pure S_0 if N possesses magnetic moments, μ_N . The ground state perturbed by μ_N is expressed as follows: DSO arise by the reorganization of *S*0; therefore, they are usually very small. PSO appears by the mixing of upper singlet states (S_1, S_2, S_3, \ldots) . FC and SD originate if admixtures occur from upper triplet states (T_1, T_2, T_3, \ldots) , where only s-type atomic orbitals contribute to FC.

Calculated 1_{TL} values are evaluated separately by the four components as shown in [\(1\)](#page-1-1). The $\frac{1}{I}$ (Se, Se) values are evaluated using the Slater-type atomic orbitals, which are equipped in the ADF 2008 program [\[19](#page-8-4)[–23](#page-8-5)]. Evaluations of the values are performed employing the ADF program, after structural optimizations with the Gaussian 03 program [\[24\]](#page-8-6). Contributions from each ψ_i and each $\psi_i \rightarrow \psi_a$ transition are evaluated separately, where *ψi* and *ψa* denote occupied and unoccupied MOs, respectively. The treatment enables us to recognize and visualize clearly the origin of the indirect nuclear spin-spin couplings.

2. Experimental

2.1. Materials and Measurements. Manipulations were performed under an argon atmosphere with standard vacuumline techniques. Glassware was dried at 130◦C overnight. Solvents and reagents were purified by standard procedures as necessary. Melting points were measured with a Yanaco-MP apparatus of uncorrected. Flash column chromatography was performed on silica gel (Fuji Silysia PSQ-100B), acidic and basic alumina (E. Merck).

NMR spectra were recorded at $297K$ in CDCl₃ and DMSO- d_6 solutions. ¹H, ¹³C, and ⁷⁷Se NMR spectra were measured at 300, 75.5, and 76.2 MHz, respectively. Chemical shifts are given in ppm relative to those of TMS for ¹H and 13 C NMR spectra and relative to reference compound Me₂Se for ⁷⁷Se NMR spectra.

*2.2. Preparation of 4-methylnaphtho[1,8-c,d]-1,2 diselenole (***2b***).* According to a method similar to that previously reported for **2a** [\[11](#page-7-3)[–17\]](#page-8-3) from 1,8-dichloro-4 methylnaphthalene, **2b** was obtained as purple needles in 68% yield, m.p. 127.0–128.0°C. ¹H NMR (CDCl₃, 300 MHz, TMS): *δ* 2.50 (s, 3H), 7.09 (dd, 1H, *J* = 0*.*9 and 7.6 Hz), 7.25 (d, 1H, *J* = 7*.*3 Hz), 7.36 (dd, 1H, *J* = 0*.*6 and 6.9 Hz), 7.55 (dd, 1H, $J = 0.7$ and 8.4 Hz); ¹³C NMR (CDCl3, 75.5 MHz, TMS): *δ* 18.6, 120.4, 120.7, 121.0, 127.4, 128.2, 130.4, 137.0, 137.3, 138.0, 141.1; ⁷⁷Se NMR (CDCl₃, 76.2 MHz, Me₂Se): δ 411.8, 420.6. Anal. Calc. for C₁₁H₈Se₂: C, 44.32; H, 2.70%; found: C, 44.21; H, 2.63%.

*2.3. Preparation of 4-chloronaphtho[1,8-c,d]-1,2-diselenole (***2c***).* According to a method similar to that previously reported for **2a** [\[11](#page-7-3)[–17](#page-8-3)] from 1,4,8-trichloronaphthalene, **2c** was obtained as brown needles in 58% yield, m.p. 155.0– 156*.*0◦C. 1H NMR (CDCl3, 300 MHz, TMS): *δ* 7.24 (d, 1H, *J* = 8*.*1 Hz), 7.30 (d, 1H, *J* = 7*.*9 Hz), 7.34 (t, 1H, *J* = 7*.*7 Hz), 7.39 (dd, 1H, *J* = 1*.*2 and 7.4 Hz), 7.81 (dd, 1H, *J* = 1*.*3 and 7.9 Hz); 13C NMR (CDCl3, 75.5 MHz, TMS): *δ* 120.5, 120.6, 121.9, 127.3, 127.4, 128.6, 135.0, 138.5, 140.0, 141.2; 77Se NMR (CDCl3, 76.2 MHz, Me2Se): *δ* 422.6, 444.6. Anal. Calc. for C₁₀H₅Se₂Cl: C, 37.71; H, 1.58%; found: C, 37.83; H, 1.60%.

*2.4. Preparation of 4-nitronaphtho[1,8-c,d]-1,2 diselenole (***2d***).* According to a method similar to that previously reported for **2a** [\[11](#page-7-3)[–17\]](#page-8-3) from 1,8-dibromo-4 nitronaphthalene, **2d** was obtained as dark purple needles in 28% yield, m.p. 196.0–197.0°C. ¹H NMR (CDCl₃, 300 MHz, TMS): *δ* 7.40 (d, 1H, *J* = 8*.*3 Hz), 7.52 (dd, 1H, *J* = 4*.*1 and 7.6 Hz), 7.53 (s, 1H), 8.18 (d, 1H, *J* = 8*.*3 Hz), 8.51 (dd, 1H, $J = 2.7$ and 4.1 Hz); ¹H NMR (DMSO-d₆, 300 MHz, TMS): *δ* 7.57 (dd, 1H, *J* = 7*.*5 and 8.5 Hz), 7.77 $(d, 1H, J = 8.5 Hz)$, 7.84 (dd, 1H, $J = 0.7$ and 7.5 Hz), 8.20 $(d, 1H, J = 8.5 Hz)$, 8.29 (dd, 1H, $J = 0.7$ and 8.5 Hz); ¹³C NMR (DMSO-d6, 75.5 MHz, TMS): *δ* 118.2, 120.0, 123.4, 127.1, 129.4, 131.1, 139.0, 140.8, 144.2, 155.5; ⁷⁷Se NMR (CDCl3, 76.2 MHz, Me2Se): *δ* 448.8, 474.4. Anal. Calc. for $C_{10}H_5Se_2NO_2$: C, 36.50; H, 1.53; N, 4.26%; found: C, 36.41; H, 1.40; N, 4.19%.

SCHEME 1: How do the indirect nuclear spin-spin couplings originate? Mechanisms for n_{JBSO} , n_{JBSO} , n_{JSD} , and n_{JFC} terms, contributing to $^nJ_{\text{TL}}$.

ϕ	$E_{rel}^{(c)}$	$^1J_{\rm PSO}$	$^{1}J_{\rm SD}$	$^{1}J_{\rm FC}$	$^1J_{\rm SD+FC}$	$1_{f_{\text{TL}}}$
[°]	[kJ mol ⁻¹]	[Hz]	[Hz]	[Hz]	[Hz]	[Hz]
0.0	36.9	447.2	217.8	18.6	236.4	683.7
15.0	33.0	399.2	200.6	15.2	215.8	615.0
30.0	25.3	288.5	163.1	2.7	165.8	454.3
60.0	6.1	76.1	101.4	-43.3	58.1	134.2
75.0	0.9	20.0	87.8	-64.7	23.1	43.1
88.4	0.0	4.1	84.5	-76.7	7.8	11.9
90.0	0.0	4.2	84.6	-77.9	6.7	10.9
105.0	2.3	29.9	91.5	-77.4	14.1	44.0
120.0	7.4	94.7	109.3	-60.5	48.8	143.5
150.0	17.6	291.5	171.7	-8.2	163.5	455.0
165.0	21.5	370.6	201.1	9.0	210.1	580.7
180.0	22.8	400.7	213.4	14.3	227.7	628.4

TABLE 2: 1 *J*(Se, Se) values calculated for $1a^{(a),(b)}$.

(a)For the abbreviation, see text. (b) ¹*J*_{DSO} being less than 0.03 Hz.

^(c)Relative to optimized value (−5267.7384 au) at $\phi = 88.38^\circ$ in kJ mol⁻¹.

2.5. Measurements of $\frac{1}{f}(Se, Se)$. During the measurement of 77 Se NMR spectra for $2g(Y = NO_2)$ in chloroform-*d* solutions (0.050 M) at 297 K, a typical AB quartet pattern of the spectra was observed. After careful analysis of the spectrum for $2g$, $\frac{1}{2}$ (Se, Se) of 330.8 Hz was obtained. The $\frac{1}{f}$ (Se, Se) values are obtained similarly by the careful analysis of the spectra for **2c** and **2d**.

2.6. Calculation Method. Structures of **1a** are optimized employing the $6-311++G(3df,2pd)$ basis sets of the Gaussian 03 program [\[24](#page-8-6)[–28\]](#page-8-7) at the DFT (B3LYP) level [\[29](#page-8-8)[–32\]](#page-8-9). The torsional angle C_{Me} SeSe C_{Me} (ϕ) is 88.38° in the fulloptimized structure of **1a**. Calculations that are further performed on **1a**: **1a** are fully optimized except for *φ*, which are fixed by every 15◦ or 30◦. Optimizations are also performed on **2a–g** using the 6-311+G(3df) basis sets [\[25–](#page-8-10) [28](#page-8-7)] for Se and the 6-311+G(3d,2p) basis sets for other nuclei at the DFT (B3LYP) level $[29-32]$ $[29-32]$. The $C_{2\nu}$ symmetry is assumed for $2a$, C_s for $2b-d$ and $2f$, and the C_1 symmetry for **2e** and **2g**.

The *J*(Se, Se) values are calculated with the triple *ξ* basis sets of the Slater type with two sets of polarization functions (2×1 s, 2×2 s, 2×2 p, 2×3 s, 2×3 p, 3×3 d, 3×4 s, $3\times4p$, $1\times4d$, and $1\times4f$ for Se) at the DFT (BLYP) level of the ADF 2008 program [\[19](#page-8-4)[–23](#page-8-5)], applying on the optimized structures with the Gaussian 03 program [\[24](#page-8-6)]. Calculations are performed at the nonrelativistic level. The scalar ZORA relativistic formulation [\[33](#page-8-11)[–35](#page-8-12)] is also applied to **2a**, for convenience of comparison. The ${}^{n}J$ _{TL} values are evaluated separately by nJ _{DSO}, nJ _{PSO}, nJ _{SD}, and nJ _{FC}, as shown in [\(1\)](#page-1-1). Mechanisms of the nuclear couplings are revealed by

FIGURE 2: Plots of ¹*J*_{DSO} (\blacksquare), ¹*J*_{PSO} (\Box), ¹*J*_{SD} (\blacktriangle), ¹*J*_{FC} (\blacklozenge), ¹*J*_{SD+FC} (\triangle) , and ¹ J_{TL} (\bigcirc) versus ϕ (CSeSeC) in ¹ J (Se, Se: **1a**).

decomposing the contributions to each ψ_i and each $\psi_i \rightarrow \psi_a$ transition [\[36](#page-8-13), [37\]](#page-8-14).

3. Results and Discussion

3.1. Observed ¹*Jobsd(Se, Se).* [Table 1](#page-1-0) collects ¹ *Jobsd* (Se, Se), necessary for discussion. The magnitudes of the ¹J_{obsd} (Se, Se) values are usually small (*<* 64 Hz) for the simple derivatives of MeSeSeMe (**1a**) (RSeSeR : **1**) [\[9,](#page-7-4) [16,](#page-8-2) [17\]](#page-8-3). On the other hand, large $^{1}J_{\text{obsd}}$ (Se, Se) are recorded for **2** (4-Y-1,8-Se2C10H5), which correspond to *symperiplanar* diselenides, although not detected in $2a (Y = H)$ [\[11](#page-7-3)[–15\]](#page-8-0). The values are 379.4 Hz for $2b$ (Y = Me), 375.9 Hz for $2c$ (Y = Cl), and 330.8 Hz for **2d** ($Y = NO_2$). ¹*J* (Se, Se: **2**) becomes smaller as the electron accepting ability of Y increases.

3.2. Mechanism of ¹*J(Se, Se) in* **1a***.* [Table 2](#page-2-1) shows the calculated $^1J_{TL}$ and the components, $^1J_{DSO}$, $^1J_{PSO}$, $^1J_{SD}$, and $^1J_{TC}$ in 1I (Se Se: 1a) $^1J_{LT}$ (Se Se: 1a) is predicted to be less J_{FC} , in ¹*J* (Se, Se: 1a). ¹ J_{TL} (Se, Se: 1a) is predicted to be less than 44 Hz for $\phi = 90^\circ \pm 15^\circ$. Therefore, $^{1}J_{\text{obsd}}$ (Se, Se: 1) is explained substantially and modeled by **1a** with $\phi \approx 90^{\circ}$, although R and R['] in 1 must also affect on the values. $\frac{1}{J}$ (Se, Se: **1a**) is predicted to be very large at $\phi = 0°$ (684 Hz) and 180◦ (628 Hz). Consequently, ¹ *J*obsd (Se, Se: **2**) of 331–379 Hz are essentially explained by ¹*J* (Se, Se: **1a**) with $\phi = 0^\circ$. [Figure 2](#page-3-0) draws the plots of ¹J_{DSO} , ¹J_{PSO} , ¹J_{SD} , ¹J_{FC} , ¹J_{SD+FC} , and ${}^{1}J_{TL}$ versus ϕ in **1a**. It is well demonstrated that ${}^{1}J_{TL}$ changes depending on ϕ , similarly to the case of $\mathrm{^{3}J}$ (H, H), three-bond (*vicinal*) couplings in ¹H NMR spectra [\[1](#page-7-1), [2\]](#page-7-5). 1 *J*_{DSO} are negligible (< 0.03 Hz).

How do ${}^{1}J_{PSO}$ (Se, Se: 1a) and ${}^{1}J_{SD+FC}$ (Se, Se: 1a) $[=$ ¹ J_{SD} (Se, Se: **1a**) + ¹ J_{FC} (Se, Se: **1a**)] contribute to ¹ J_{TL} (Se, Se: **1a**)? ¹*J*_{PSO} (Se, Se: **1a**) and ¹*J*_{SD+FC} (Se, Se: **1a**) are plotted versus $^1J_{\rm TL}$ (Se, Se: 1a), although not shown. The correlations are given in [\(2\)](#page-3-1) and [\(3\)](#page-3-2), respectively. The results exhibit that $\binom{1}{P}$ _{PSO} (Se, Se: 1a) and $\binom{1}{S}$ _{D+FC} (Se, Se: 1a) contribute 65% and 35% to ${}^{1}J_{TL}$ (Se, Se: 1a), respectively, irrespective of the*φ*(CSeSeC) values:

$$
{}^{1}J_{PSO}(\text{Se, Se: } \text{1a})
$$

= 0.651 × ¹J_{TL}(Se, Se: 1a) – 4.1 (r^2 = 0.999),
¹J_{CP, PR}(Se, Se: 1a)

$$
J_{SD+FC}(Se, Se: \mathbf{1a})
$$

= 0.349 × ¹J_{TL}(Se, Se: \mathbf{1a}) + 4.2 (r² = 0.998). (3)

Why does $\frac{1}{f}$ (Se, Se: 1a) show the torsional angular dependence? What orbitals and transitions contribute to the dependence? ¹*J*_{PSO} (Se, Se: 1a) is analyzed next.

3.2.1. Analysis of $\frac{1}{P}$ *P_{SO}*(*Se, Se) in* **1a***.* The mechanism of $^{1}J_{\text{PSO}}$ (Se, Se: 1a) is discussed by analyzing the contributions separately from each ψ_i and each $\psi_i \rightarrow \psi_a$ transition. [Table 3](#page-4-0) lists the ϕ dependence of $^1J_{\rm PSO}$ (Se, Se: 1a) contributed from *ψ*1*–ψ*43, *ψ*1*–ψ*38, *ψ*39*–ψ*43, *ψ*39, *ψ*40, *ψ*41, *ψ*42, and*ψ*43. The contribution from $\psi_{39} - \psi_{43}$ to ${}^{1}J_{PSO}$ (Se, Se: 1a) is large, whereas that from $\psi_1 - \psi_{38}$ is small, although not shown. The plot of the contributions from $\psi_{39} - \psi_{43}$ (*y*) versus those from $\psi_1 - \psi_4$ ³ (*x*) provides an excellent correlation ($y = 0.976x +$ 37.3 : $r^2 = 0.9999$). [Figure 3\(a\)](#page-4-1) shows those from ψ_{39} , ψ_{40} , *ψ*41, *ψ*42, and *ψ*⁴³ and [Figure 3\(b\)e](#page-4-2)xhibits those from *ψ*39*– ψ*₄₁, $ψ$ ₄₂– $ψ$ ₄₃, and $ψ$ ₃₉– $ψ$ ₄₃. Contributions from $ψ$ ₄₂ and $ψ$ ₄₃ exchange with each other at $\phi \approx 90^\circ$. Those of ψ_{39} and ψ_{40} do at $\phi \approx 135^\circ$ [\(Figure 3\(a\)\)](#page-4-1). The contributions from ψ_{42} - ψ_{43} and $\psi_{39} - \psi_{41}$ almost cancel out at $\phi \approx 90^{\circ}$ [\(Figure 3\(b\)\)](#page-4-2).

Magnitudes of the contributions from ψ_{42} and ψ_{43} to $^{1}J_{\text{PSO}}$ (Se, Se: 1a) are very large at 0° and 180° [\(Table 3\)](#page-4-0), although those from ψ_{42} and ψ_{43} are negative and positive directions, respectively. The values amount to −353 to −360 Hz and 753–793 Hz, respectively. The contributions from $\psi_{42} - \psi_{43}$ are 433, 218, and 400 Hz at 0^o, 90^o, and 180o, respectively, and those from *ψ*39–*ψ*⁴¹ are 17, [−]198, and 10 Hz at 0° , 90° , and 180° , respectively. Therefore, the mechanism of $\frac{1}{I}\gamma_{\text{PSO}}(Se, Se: 1a)$ will be clarified by analyzing the contributions from *ψ*⁴² and *ψ*⁴³ at 0o and 180 $^{\circ}$. The mechanism would be complex at 90 $^{\circ}$, since the small magnitude is the results of the total contributions from *ψ*39–*ψ*43.

[Figure 4](#page-5-0) shows the $\psi_{42} \rightarrow \psi_{44}$ and $\psi_{43} \rightarrow \psi_{44}$ transitions at both $\phi = 0^{\circ}$ and 180° which are shown in [Table 3.](#page-4-0) Characters of ψ_{42} (HOMO-1), ψ_{43} (HOMO), and ψ_{44} (LUMO) are *π*(Se–Se), *π*∗(Se–Se), and *σ*∗(Se–Se), respectively, at $\phi = 0^{\circ}$ and 180°. ψ_{42} (HOMO-1) is essentially the same as ψ_{43} (HOMO) at $\phi = 90^{\circ}$. ψ_{42} and ψ_{43} at $\phi = 90^{\circ}$ are also drawn in [Figure 4,](#page-5-0) to show how *ψ*⁴² and *ψ*⁴³ interconvert with each other. Contrary to the case of $\phi \approx 0$ and 180^o, all of ψ_{39} – ψ_{43} contribute to ¹*J* _{PSO}(Se, Se: **1a**) at $\phi \approx 90^\circ$. Contributions from the $\psi_{42} \rightarrow \psi_{44}$ and $\psi_{43} \rightarrow \psi_{44}$ transitions to ¹*J* _{PSO}(Se, Se: **1a**) at 90[°] are almost cancelled by those from the $ψ₃₉ →$ $\psi_{44}, \psi_{40} \rightarrow \psi_{44}$, and $\psi_{41} \rightarrow \psi_{44}$ transitions. In addition, both J $_{\rm SD}$ (Se, Se: 1a) and 1J $_{\rm FC}$ (Se, Se: 1a) substantially contribute at $\phi \approx 90^\circ$. Consequently, it is difficult to specify a few

 (a) In Hz.

(b) For the abbreviation, see text.

 (c) Contribution from the transition.

FIGURE 3: Origin of the torsional angular dependence in 1J _{PSO} (Se, Se: 1a): (a) contributions from each of ψ39, ψ₄₀, ψ₄₁, ψ₄₂, and ψ₄₃ and (b) those from $\psi_{39} - \psi_{41}, \psi_{42} - \psi_{43}$, and $\psi_{39} - \psi_{43}$.

orbitals, together with the transitions, which control $\frac{1}{J}$ (Se, Se: **1a**) at $\phi \approx 90^\circ$. The character of ψ_{44} [LUMO: $\sigma^*(Se-$ Se)] does not change so much depending on *φ*. Therefore, the behavior of *ψ*39–*ψ*⁴³ must be mainly responsible for the *φ* dependence in ¹ *J* (Se, Se: **1a**) (see Figures [3](#page-4-3) and [4\)](#page-5-0). The MO description in [Figure 4](#page-5-0) visualizes the origin of ¹J_{PSO}(Se, Se: **1a**) and helps us to understand the mechanism, especially at $\phi = 0^{\circ}$ and 180^o.

After elucidation of the mechanism for $\frac{1}{J}$ _{PSO}(Se, Se: 1a), next extension is to clarify ¹ *J* (Se, Se: **2**) on the basis of the MO theory.

3.2.2. Evaluation of ¹*J(Se, Se) for* **2***.* [Table 4](#page-5-1) collects the calculated ${}^{1}J_{\text{TL}}$ (Se, Se: 2) values, together with J_{PSO} (Se, Se: **2**), ¹ *J*SD (Se, Se: **2**), ¹ *J*FC (Se, Se: **2**), and ¹ *J*SD+FC (Se, Se: **2**). [Table 4](#page-5-1) also contains the nuclear changes calculated with the natural bond orbital analysis (NBO) method (*Qn*(Se)) [\[38](#page-8-15)[–40](#page-8-16)] for **2** having Y of H (**a**), OMe (**b**), Me (**c**), Cl (**d**), COOMe (**e**), CN (**f**), and NO2 (**g**). The Y dependence of $\frac{1}{2}$ _{lobsd} (Se, Se: 2) is well reproduced by the calculations. 1 *J*_{TL} (Se, Se: 2) are predicted to be larger than the observed values by about 100 Hz. The DFT method overestimates the reciprocal energy differences $(\varepsilon_a - \varepsilon_i)^{-1}$, which would partly be responsible for the larger evaluation. The $\frac{1}{J}$ (Se, Se) values are calculated at both nonrelativistic and scalar ZORA relativistic levels for **2a**. The former is smaller than the latter. The value calculated at the nonrelativistic level seems to be closer to the observed value than that obtained with the scalar ZORA relativistic formulation in our calculation system. Therefore, it would be reasonable to discuss the $nⁿJ$ (Se, Se) value calculated at the nonrelativistic level in this case.

FIGURE 4: Contributions to ¹J_{PSO}(Se, Se: **1a**) from the $\psi_{42} \to \psi_{44}$ and $\psi_{43} \to \psi_{44}$ transitions at $\phi = 0$, 90, and 180°. The interconversion between ψ_{42} and ψ_{43} at $\phi \approx 90^\circ$ is also depicted.

Table 4: ¹*J*(Se, Se) and *Qn*(Se) calculated on the full-optimized structure of **2**(a),(b),(c).

Compound	$V_{PSO}[\text{Hz}]$	$J_{SD}[\text{Hz}]$	$J_{\text{FC}}[\text{Hz}]$	$J_{SD+FC}[\text{Hz}]$	^{1}J TL [Hz]	$Qn({}^{1}Se)$	$Qn(^2$ Se)	Symmetry
$2a(Y = H)$	362.2	195.2	-54.1	141.1	503.3	0.2367	0.2367	$C_{2\nu}$
$2b(Y = OMe)$	394.3	207.5	-54.2	153.3	547.7	0.2256	0.2264	C_{s}
$2c(Y = Me)$	363.6	195.1	-55.3	139.8	503.5	0.2334	0.2296	C_{s}
$2d(Y = Cl)$	360.1	193.4	-53.1	140.3	500.4	0.2448	0.2443	C_{s}
$2e(Y = COOMe)$	324.1	178.2	-55.7	122.5	446.6	0.2593	0.2556	C_1
$2f(Y = CN)$	326.6	180.6	-52.6	128.0	454.6	0.2677	0.2564	C_{s}
$2g(Y = NO_2)$	299.7	167.6	-53.9	113.7	413.4	0.2824	0.2576	C_1
$2a(Y = H)^{(d)}$ $\sqrt{2}$	390.7	206.4	2.6	209.0	599.7	0.2367	0.2367	$C_{2\nu}$

(a)For the abbreviation, see text.

 $^{\rm (b) \ 1}J_{\rm DSO}$ being less than 0.03 Hz.

(c) 1 Se and ²Se being attached to ¹C and ⁸C in 4-Y-1,8-Se₂C₁₀H₅ (2), respectively.

(d) On the basis of scalar ZORA.

Before discussion of $\frac{1}{I}$ (Se, Se: 2), it would be instructive to clarify the behavior of *Qn*(Se: **2**), which changes depending on Y. [Figure 5](#page-6-0) shows the plot of $Qn(^{2}Se: 2)$ versus $Qn(^{1}Se: 2)$. The correlations of the linear type ($y = ax + b$ with *r* (correlation coefficient)) are given in the figure. The results show that $Qn(^{2}Se: 2)$ grows larger as the accepting ability of Y increases for $Y = H$, OMe, Me, Cl, and COOMe then it becomes almost constant for $Y = CN$ and $NO₂$ while $Qn({}^{1}Se: 2)$ grows larger as the accepting ability of Y increases for all Y in [Table 4.](#page-5-1) $Qn(^{2}Se: 2)$ seems saturated for Y of very strong acceptors such as CN and NO₂ while $Qn(^{1}Se: 2)$ will not for all Y.

How do ${}^{1}J_{\text{TL}}$ (Se, Se: 2) being controlled? ${}^{1}J_{\text{TL}}$ (Se, Se: 2) are plotted versus $Qn(^{1}Se)$, $Qn(^{2}Se)$, and $Qn({}^{1}Se)+Qn({}^{2}Se)$. [Figure 6](#page-6-1) shows the plot of ${}^{1}J_{TL}$ (Se, Se: 2) versus $Qn({}^{1}Se)$, which gives best correlation among the three. The correlation is given in the figure. ${}^{1}J_{TL}$ (Se, Se: 2) are confirmed to be controlled by $Qn(^{1}Se)$. One might imagine that ${}^{1}J_{TL}$ (Se, Se: 2) should be controlled by $Qn({}^{1}Se)+Qn({}^{2}Se)$. The saturation in $Qn({}^{2}Se)$ shown in

[Figure 5](#page-6-0) would perturb to give good correlations for $^1J_{\rm TL}$ (Se, Se: **2**) versus $Qn({}^{1}Se) + Qn({}^{2}Se)$. It is demonstrated that ${}^{1}L_{\infty}$ (Se Se: **2**) becomes smaller when $Qn(Se)$ increases J_{TL} (Se, Se: 2) becomes smaller when Qn (Se) increases, experimentally and theoretically.

After clarification of the Y dependence in ${}^{1}J_{TL}$ (Se, Se: 2), next extension is to elucidate the mechanism for ¹*J* (Se, Se: **2**) on the basis of the MO theory.

3.3. Mechanism of ¹*J*(*Se, Se) in* **2a***.* How do ¹*J*_{PSO} (Se, Se: **2**) and ${}^{1}J_{SD+FC}$ (Se, Se: **2**) contribute to ${}^{1}J_{TL}$ (Se, Se: **2**) in the change of Y? $\frac{1}{P}$ _{PSO} (Se, Se: 2) and $\frac{1}{S}$ _{SD+FC} (Se, Se: 2) are plotted versus ${}^{1}J_{TL}$ (Se, Se: 2) for various Y in [Table 4.](#page-5-1) The results for ${}^{1}J_{\text{PSO}}$ (Se, Se: 2) and ${}^{1}J_{\text{SD+FC}}$ (Se, Se: 2) are given in [\(4\)](#page-5-2) and [\(5\)](#page-6-2), respectively. The correlations are very good, which shows that ${}^{1}J_{\text{PSO}}$ (Se, Se: 2) contributes predominantly to $^1J_{\rm TL}$ (Se, Se: **2**) (70%), irrespective of Y:

$$
{}^{1}J_{\text{PSO}} \text{ (Se, Se : 2)}= 0.704 \times {}^{1}J \text{ TL} (\text{Se, Se : 2)} + 8.3 (r^{2} = 0.999),
$$
 (4)

FIGURE 5: Plot of $Qn(^{2}Se)$ versus $Qn(^{1}Se)$ in 2.

FIGURE 6: Plot of ¹*J*(Se, Se: 2) versus $Qn(^1Se)$ in 2.

$$
{}^{1}J_{SD+FC} \text{ (Se, Se : 2)}= 0.295 \times {}^{1}J_{TL} \text{(Se, Se : 2)} - 8.0 \text{ (}r^{2} = 0.994\text{)}
$$
 (5)

The origin of ¹*J* (Se, Se: 2) is elucidated by analyzing $\frac{1}{L}$ $\frac{1}{L}$ (Se, Se: 23) on the basis of the MO theory since $^{1}J_{\text{PSO}}$ (Se, Se: 2a) on the basis of the MO theory, since J_{PSO} (Se, Se) contributes predominantly to ${}^{1}J_{TL}$ (Se, Se)

FIGURE 7: MO analysis of ¹*J*_{PSO} (Se, Se: 2a): (a) contributions from each ψ_i , (b) from each $\psi_{67} \rightarrow \psi_a$ transition, and (c) from each $\psi_{66} \rightarrow \psi_a$ transition.

irrespective of Y. [Figure 7](#page-6-3) depicts the contributions of ¹ $\frac{1}{2}I_{PSO}$ (Se, Se: 2a) separately from each ψ_i and each $\psi_i \rightarrow$ ψ_a transition. (a)–(c) in [Figure 7](#page-6-3) plot the contributions to 1 *J*_{PSO} (Se, Se: 2a) from each ψ_i and each transition of the $\psi_{67} \rightarrow \psi_a$ and $\psi_{66} \rightarrow \psi_a$ types, respectively. In [Figure 7\(a\),](#page-6-4) contributions around $\psi_5 - \psi_{10}$, $\psi_{23} - \psi_{28}$, and $\psi_{53} - \psi_{67}$ originate mainly from atomic $2p(Se)$, $3p(Se)$, and $4p(Se)$ orbitals, respectively. Those caused by 2p(Se) and 3p(Se) are almost cancelled by summarizing over the corresponding orbitals. Therefore, $4p$ (Se) substantially contribute to $\frac{1}{P}$ _{PSO} (Se, Se: **2a**). Especially, ψ_{67} (HOMO) and ψ_{66} (HOMO-1) control J_{PSO} (Se, Se: 2a). ψ_a of ψ_{68} determines ${}^{1}J_{\text{PSO}}$ (Se, Se: 2a), among a lot of $\psi_i \rightarrow \psi_a$ transitions in ψ_i of ψ_{67} and ψ_{66} , as shown in Figures [7\(b\)](#page-6-5) and [7\(c\).](#page-6-6)

[Figure 8](#page-7-6) shows the $\psi_{67} \rightarrow \psi_{68}$ and $\psi_{66} \rightarrow \psi_{68}$ transitions in ¹ *J*PSO (Se, Se: **2a**). The large ¹ *J*PSO (Se, Se: **2a**) value arises from the mixing of *ψ*⁶⁸ [LUMO: *σ*∗(Se–Se)] into $ψ$ ₆₇ [HOMO: $π*(Se-Se)$] and $ψ$ ₆₆ [HOMO-1: $π(Se-Se)$] at the singlet state. The MO presentation in [Figure 8](#page-7-6) is essentially the same as the $\psi_{42} \rightarrow \psi_{44}$ and $\psi_{43} \rightarrow \psi_{44}$ transitions in ¹*J*_{PSO} (Se, Se: **1a**) at $\phi = 0^\circ$ in [Figure 4,](#page-5-0) although ψ_{67} (2a) and ψ_{66} (2a) contain the π (Nap) character. Large $\frac{1}{2}J_{PSO}$ (Se, Se: 2) and small $\frac{1}{2}J_{obsd}$ (Se, Se: 1) are well understood by the ϕ dependence in the calculated $\frac{1}{J}$ (Se, Se: **1a**) values.

4. Conclusion

Nuclear spin-spin coupling constants (*J*) provide highly important information around coupled nuclei, containing

FIGURE 8: MO analysis of ¹J_{PSO} (Se, Se: 2a): main contributions from the ψ_{67} (HOMO) $\rightarrow \psi_{68}$ (LUMO) and $\psi_{66} \rightarrow \psi_{68}$ transitions are depicted.

strongly bonded and weakly interacting states. The ¹J (Se, Se) values are analyzed as the first step to investigate the nature of the bonded and nonbonded interactions between the Se atoms through $\mathrm{^{\textit{n}}J}$ (Se, Se). QC calculations are necessary for the analysis and the interpretation of the *J* values with physical meanings. Calculated $"J_{TL}$ are composed of the contributions from $^nJ_{\text{DSO}}$, $^nJ_{\text{PSO}}$, $^nJ_{\text{SD}}$, and ^{*n*}J_{FC}. The decomposition helps us to consider the mechanisms of the spin-spin couplings, which are closely related to the electronic structures of compounds. Main contributions are evaluated separately from each *ψi* and each $\psi_i \rightarrow \psi_a$ transition, where ψ_i and ψ_a are occupied and unoccupied MO's, respectively. ¹

J (Se, Se) is calculated modeled by MeSeSeMe (**1a**), which shows the typical torsional angular dependence of ϕ (C_{Me}SeSeC_{Me}). The dependence explains well ¹*J*_{obsd} (Se, Se) of small values for RSeSeR' (1) and large values for 4-Y-1,8-Se2C10H5 (**2**) which correspond to *symperiplanar* diselenides. ¹J_{TL} (Se, Se: 2) are confirmed to be controlled by Qn(Se). ${}^{1}J_{TL}$ (Se, Se: 2) are demonstrated to be smaller when *Qn*(Se) becomes larger, experimentally and theoretically. The PSO terms contribute predominantly to $\frac{1}{J}$ (Se, Se). The contributions are analyzed separately from each *ψi* and each $\psi_i \rightarrow \psi_a$ transition. The MO description of each transition enables us to recognize and visualize clearly the origin and the mechanisms of the indirect nuclear spinspin couplings. Important properties of molecules, such as electronic structures, will be clarified by elucidating the mechanisms of the spin-spin couplings on the basis of the MO theory.

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