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# Mathematical modelling of in-situ microaerobic desulfurization of biogas from sewage sludge digestion

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#### ABSTRACT

Microaeration can be used to cost-effectively remove *in-situ* H<sub>2</sub>S from the biogas generated in anaerobic digesters. This study is aimed at developing and validating an extension of the Anaerobic Digestion Model n°1 capable of incorporating the main phenomena which occurs during microaeration. This innovative model was implemented and tested with data from a pilot scale digester microaerated for  $\sim 200$  d. The results showed that despite the model's initial ability to predict the digester's behavior, its predicted performance was improved by calibrating the most influential parameters. The model's prediction potential was largely enhanced by adding retention parameters that account for the activity of sulfide oxidizing bacteria retained inside the anaerobic digester, which have been consistently shown to be responsible for a large share of the H<sub>2</sub>S removed.

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## 1. Introduction

Microaeration, which consists of dosing of a limited amount of air to anaerobic digesters, has emerged as one of the most cost-effective technologies for H<sub>2</sub>S removal from biogas. The microaerophilic conditions created by air supply support the partial oxidation of H<sub>2</sub>S to S° by the action of sulfide-oxidizing bacteria. In Europe, this process is gaining increasing attention and several full-scale plants have already implemented this technology to remove H<sub>2</sub>S from biogas [1]. Indeed, microaeration has been traditionally employed to control H<sub>2</sub>S in full-scale digesters treating agricultural waste. Recently, this technology has been successfully applied to the treatment of a broad range of biogas flow rates  $(7 L d^{-1} - 250 m^3 h^{-1})$ ,  $H_2S$  concentrations (2500 - 67,000 ppm<sub>v</sub>) [2] and substrates (from industrial wastewaters to WWTP sludge) [3,4]. Interestingly, microaeration does not inhibit organic matter removal nor CH4 productivity [5,6]. On the contrary, significant enhancements in organic matter hydrolysis and methanogenic activity have been reported, likely due to the suppression of the inhibition caused by sulfide [1,7,8]. Both air and  $O_2$  can be used to support biogas desulfurization with similar H<sub>2</sub>S removal efficiencies. In this context, the use of concentrated O<sub>2</sub> resulted in lower operating costs when

\* Corresponding author: *E-mail address:* andreseduardo.donoso@cetaqua.com (A. Donoso-Bravo). compared to ferric salt addition for biogas desulfurization in wastewater treatment plants (WWTP) [9].

Mathematical modeling of (bio)chemical processes is nowadays considered of paramount importance for process analysis, control and optimization. Modeling anaerobic digestion (AD) allows us to get more insight on process performance, evaluate different scenarios and hypotheses, facilitates a virtual plant for assessment and training, and represents a valuable tool for process control or experimental design. Therefore, process modelling helps minimize the experimental work needed, which translates into resource savings and risk minimization. Furthermore, modeling is recognized as one the future needs to be addressed in AD [10]. Recent studies have developed models for the microaerobic process in AD, for both liquid effluents and for systems with immobilized biomass, UASB [11] and biotrickling filters [12]. Therefore, to the best of our knowledge, no mathematical model has been so far adapted and implemented for the microaerobic H<sub>2</sub>S removal during sewage sludge AD in a continuous stirred reactor. The anaerobic digestion model 1 (ADM1) developed by the IWA task group [13] is the most recognized and widely used model to describe the AD process. In this context, extensions of the ADM1 have also been published in order to describe particular processes not considered in the original model. These extensions have tackled biological sulfate reduction [14,15], inorganic compounds and solid precipitation [16] and phenolic compounds biodegradation [17], among others.

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This study is aimed at developing, implementing and testing a mathematical model of the microaerobic digestion process based on the ADM1 model using experimental data from pilot-scale anaerobic digesters operated under microaerobic conditions.

## 2. Material and methods

## 2.1. Experimental data

The pilot-plant scale digester (working volume of 200L) was operated under mesophilic conditions with thickened mixed sewage sludge at a hydraulic retention time (HRT) of 20 d. Microaeration was performed in the sludge recirculation line. The O<sub>2</sub> flow rate (Fig. 1a) was manually adjusted to the variable biogas production rate resulting from the unsteady organic load of sludge feeding. Fluctuations in the organic loading rate of anaerobic digesters are inherent to the variations in sludge compositions in WWTPs and were here observed in all parameters monitored, namely, total COD (between 70 and 37  $g_{COD}^{-1}$  L<sup>-1</sup>), soluble COD, TS, VS (Fig. 1b) and VFA concentrations (Fig. 1c). Additionally, Na<sub>2</sub>SO<sub>4</sub> was added to the sludge feed ( $\sim 1090 \text{ mg L}^{-1}$ ) with the aim of increasing the formation of H<sub>2</sub>S during anaerobic digestion. Therefore, the concentration of sulfate and dissolved sulfide were monitored (Fig. 1d). First, the digester was in operation for 70 d in strict anaerobic conditions (data not shown) before the microaerobic period began. More details about the experimental set-up and operation can be found elsewhere [18]. The biogas production was measured by liquid displacement and the biogas composition was determined by GC-TCD. Sulfate concentration was measured by HPLC-IC. VFA concentrations were quantified by GC-FID. Alkalinity, ammonium, TKN, COD, TS, VS, total dissolved sulfide, pH and ORP were determined according to standard methods [19].

#### 2.2. Model description

## 2.2.1. Model implementation and ADM1 modification

ADM1 was implemented and solved in Matlab® 2015b along with the general modification suggested by Rosen and Jeppsson [20]. Suggested parameters by the ADM1 report [21] were maintained, although the minimum and maximum values of the pH inhibition function for H<sub>2</sub> consumers were adapted to the primary sludge. Additionally, a VS output was also included, together with the COD output, by using a conversion COD/mass ratio derived from the generalized mineralization equation [22]. The composite concentration (Xc) was set equal to zero so that the particulate carbohydrates, proteins, lipids and inerts were the input conditions to the ADM1 model. The elimination of the disintegration step originally considered in the ADM1 has been lately suggested as necessary based on the recently reported drawbacks derived from the use of a two-hydrolysis step during the anaerobic digestion of sewage sludge [10]

## 2.2.2. Assumptions and microaeration process rationale

The mathematical description of the sulfide oxidation process involves the following assumptions:

- The levels of dissolved oxygen are always maintained below the inhibition threshold. Therefore, no inhibition function due to the presence of oxygen was added. In fact, the redox potential of the pilot digester cultivation broth remained always below -494 mV under process operation with and without microaeration [23].
- Sulfide oxidizing bacteria X<sub>SOB</sub> is the only microbial community that consumes oxygen.
- The conversion of H<sub>2</sub>S to S° is the only reaction considered. In this context, the conversion of H<sub>2</sub>S to SO<sub>4</sub><sup>2−</sup> requires 4-fold



Fig. 1. Time course of (a) the sludge feeding rates and  $O_2$  flow rate, (b) solids and COD concentrations, (c) VFA concentrations and (d)  $S^{2-}$  and  $SO_4^{2-}$  concentration in the digester.

more  $O_2$  than the oxidation to S°, and therefore the  $O_2$  limiting conditions prevailing in the cultivation broth of the digester do not promote the complete oxidation of H<sub>2</sub>S.

- No spontaneous H<sub>2</sub>S or S° chemical oxidation (redox) reactions occur.
- The dissolved oxygen present in the sludge feeding is negligible compared to the O<sub>2</sub> transferred from the gas phase, which governs the growth of X<sub>SOB</sub>.
- The new process included into the ADM1 along with its stoichiometry are shown in Table 1 based on the findings of [24]. The sulfur oxidation process involves elemental sulfur (S), sulfide oxidizing bacteria (X<sub>SOB</sub>), dissolved oxygen and oxygen in the gas phase as new state variables (ordinary differential equations, ODE). The kinetic parameters of the sulfate reducing bacteria (SRB) were taken from Barrera et al [14].
- An O<sub>2</sub> laden gas stream is injected into the digester and partially transferred to the liquid phase according to Eq. (1), where  $K_H$  stand for the Henrys law constant ( $K_H$  = 0.0013 at 37 °C),  $k_L$ a the volumetric mass transfer coefficient,  $p_{pO2}$  the O<sub>2</sub> partial pressure and S<sub>O2</sub> the dissolved O<sub>2</sub> concentration in the anaerobic broth:

$$O_2 \operatorname{Transfer} rate = k_L a \cdot (K_H \cdot p_{pO_2} - S_{O_2 \perp})$$
(1)

- The value of the volumetric mass transfer coefficient,  $k_{La}$ , depends on reactor design and operating conditions. A unique  $k_{La}$  value was assumed because the HRT and mixing rate were constant in the experimental period considered, so were the temperature and the operating pressure. Changes in mixing conditions, such as switching sludge for biogas recirculation, would result in a different  $k_{La}$  value.
- Two additional ODEs were added to describe the  $O_2$  mass balance in the anaerobic cultivation broth (Eqs. (2), (3)

$$\frac{dS_{02 \, J}}{dt} = O_2 \, Transfer \, rate - SOB_{consumption} - S_{O_2 \, J} \tag{2}$$

Where  $SOB_{consumption}$  stands for the  $O_2$  consumption rate by  $X_{SOB}$  and  $S_{O2}$  \_l the  $O_2$  mass flow rate in the effluent of the anaerobic digestion.

■ Similarly, the O<sub>2</sub> mass balance in the headspace of the digester can be described as follows:

$$\frac{dS_{02\_g}}{dt} = S_{02in\_g} - O_2 \operatorname{Transferrate} - S_{02\_g}$$
(3)

Where  $S_{O2_g}$  represents the  $O_2$  concentration in the gas phase,  $S_{O2in_g}$  the gas phase  $O_2$  mass flow rate supplied to the digester and  $S_{O2_g}$  the gas phase  $O_2$  mass flow rate leaving the digester together with the biogas effluent.

#### 2.3. Model implementation

A manual calibration of the most sensitive model parameters was carried out. Several simulations were performed in order to identify the parameters that would influence the experimental outputs the most. The initial conditions of the model resolution were obtained from simulations until steady state conditions were reached and process parameters (mainly COD concentrations and pH) were similar to the initial values of the experimental data. This is a widely accepted method for estimating the initial conditions in anaerobic digesters [25].

## 2.4. Input conditions

A complete characterization of the sewage sludge was carried out weekly, along with the collection of fresh sludge from Valladolid WWTP. This characterization was assumed to hold until the next characterization and only the inlet flow was measured daily. The concentrations of  $H_2S$  and  $HS^-$  were estimated from the measurement of the total sulfur and the equilibria equation as a function of the pH. The content of carbohydrates, proteins and lipids was assumed to correspond to 20%, 65%, 15% of the degradable organic matter, respectively [26]. Similarly, inerts were assumed to be 30% of the total COD. The dissolved VFAs, inorganic nitrogen, sulfate, sulfide and oxygen concentrations were taken directly from the weekly experimental characterization of the sewage sludge.

#### 3. Results and discussion

#### 3.1. Reactor operation conditions

Fig. 1 shows the characteristics of the feed to the anaerobic digester throughout the period modelled. The sludge flow rate averaged 9 - 12 L  $d^{-1}$ , although significant drops and peaks occurred during digester operation. These fluctuations are necessary in order to test the model's response to transient conditions and unstable reactor loads. Likewise, the solid content and the organic matter concentration inside the digester showed variations during the experimental period. Although the total COD concentration seems to experience the greatest fluctuation, this variability is strongly related to the experimental error of the COD measurement method when analyzing a semi-solid substrate such as sewage sludge. The VS concentration was correlated to the total COD concentration. It is worth stressing that the sewage sludge used in this study exhibited a significant concentration of VFAs and sulfur compounds, which are crucial to generate an adequate environment for SRB bacteria to thrive. Dissolved sulfide was present in the sewage and consequently in the sludge.

#### 3.2. Parameters calibration

The sensitivity analysis (data not shown) indicated that only few parameters could be calibrated in a dependable way. Thus,

#### Table 1

Petersen matrix of the new biochemical reactions added to the ADM1.

Process	S <sub>H</sub> 2S	S <sub>S</sub>	S <sub>02_1</sub>	S <sub>IC</sub>	S <sub>IN</sub>	X <sub>C</sub>	X <sub>SOB</sub>	Rate
Uptake of H <sub>2</sub> S by SOB	-1	(1- Y <sub>SOB</sub> )	- (1-Y <sub>SOB</sub> )/64	- $\Sigma C_i v_i$	$-Y_{SOB}^*N_{BAC}$		Y <sub>SOB</sub>	$k_{mSOB}^{*}(S_{H}2S/(Ks_{H}2S+S_{H}2S))^{*}(S_{02}/(Ks_{O2} + S_{02}))^{*}X_{SOB};$
Decay of SOB				$-C_{BAC}+C_{XC}$	-N <sub>BAC</sub> + N <sub>XC</sub>	1	-1	k <sub>decSOB</sub> * X <sub>SOB</sub>
	Hydrogen	Elemental	Dissolved	Inorganic	Inorganic	Composites	Sulfur oxidizing	
	sulfide	sulfur (S°)	oxygen	carbon	nitrogen	(	bacteria	
	(kmol m <sup>-3</sup> )	(kmol m <sup>-3</sup> )	(kmol m <sup>-3</sup> )	(kmol m <sup>-3</sup> )	(kmol m <sup>-3</sup> )	kg <sub>COD</sub> m <sup>-3</sup> )	$(kg_{COD} m^{-3})$	

some kinetic parameters of  $X_{SOB}$  were set as:  $K_{S\_H2S}$  and  $K_{S\_O2}$ (affinity constants) =  $3 \cdot 10^{-3}$  g L<sup>-1</sup>; Y<sub>SOB</sub> (biomass yield) = 0.25 g g<sup>-1</sup>;  $k_{dec}$  (decay coefficient) = 0.02 d<sup>-1</sup>. These values were chosen based on previous simulations in order to avoid the washout of the SOB from the digester and lied in the same order of magnitude as those microorganisms present in the anaerobic digestion process. Furthermore, these values were in agreement with the fact that a significant fraction of the SOB population was present over the lavers of sulfur accumulated in the digester headspace according to a DGGE analysis [23]. The hydrolysis parameters were optimised by trial and error to minimize the squared value of the difference between predicted and experimental methane production curves. The values of the calibrated parameters are presented in Table 2, which compiles five stoichiometric coefficients and one kinetic parameter calibrated. This difference was induced by the type of experimental data since a continuous operation without controlled changes in the inlet conditions (such as hydraulic or organic overloads) suits better the estimation of stoichiometric parameters compared to that of kinetic parameters [25]. Indeed, a stable continuous operation is basically driven by process stoichiometry rather than by process kinetics.

The calibrated parameter  $k_{m_{SOB}}$ , related to the maximum growth rate of sulfur oxidizing bacteria, showed that this type of microorganism grows 5-6 and 10-12-fold faster than acidogenic and methanogenic communities, respectively, which is in agreement with the difference between the metabolism of aerobic and anaerobic/facultative microorganisms. The stoichiometric value of the methane conversion (C<sub>CH4</sub>) increased by 20% compared to the reference value [20] since a constant bias was observed in regards to the methane composition of the biogas generated in our pilot digesters. The coefficient parameters associated to N metabolism were also calibrated due to different properties of sludge used in this study compared to those used in the original ADM1 model. In fact, several authors recommend the calibration of the stoichiometric parameters associated to the N metabolisms for every substrate fed into the digester [21]. The only physical-chemical parameter calibrated was the pipe resistance coefficient  $(k_{\rm P})$ , which governs the biogas flow estimation and determines the head loss of the outlet gas. This expression, which assumes an overpressure in the headspace of the digester, represents the preferred expression since it yields smoother values of the biogas flow than the original one [20]. The value of this parameter depends on the physical properties of the digester and should be modified according to the specific properties of the target set-up. In our particular case, overpressures ranging from 10 to 20 mbar were recorded throughout the digester's operation, which resulted in a  $k_{\rm P}$  of  $7\times 10^4$  (Table 2).

## 3.3. Model performance

Figs. 2 and 3 show the simulation results of the modified ADM1 model along with the experimental offline (i.e measurements in

Table	2
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Calibrated	parameters	of	the	mode
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Type of parameter	Units	Calibrated value		
Kinetic				
k <sub>m-SOB</sub>	$d^{-1}$	160		
Stoichiometric				
C <sub>ch4</sub>	$\text{kmole}_{\text{C}} \text{kg}_{\text{COD}}^{-1}$	0.0187		
N <sub>xc</sub>	kmole <sub>N</sub> kg <sub>COD</sub> <sup>-1</sup>	0.001		
NI	kmole <sub>N</sub> kg <sub>COD</sub> <sup>-1</sup>	$8  imes 10^{-4}$		
N <sub>aa</sub>	kmole <sub>N</sub> kg <sub>COD</sub> <sup>-1</sup>	$6  imes 10^{-3}$		
N <sub>bac</sub>	kmole <sub>N</sub> kg <sub>COD</sub> <sup>-1</sup>	0.019		
Physical-chemical				
k <sub>P</sub>	$m^3 d^{-1} bar^{-1}$	$7\times 10^4$		

the anaerobic broth) and online data (biogas production and composition data and pH in the anaerobic broth), respectively. The online data corresponds to the composition of the biogas produced and the pH of the anaerobic broth in the digester. Both the methane and CO<sub>2</sub> content simulation matched the experimental data (Figure a,b) as well as the pH value and remained constant because microaeration did not affect them significantly. Even though the pH was slightly overestimated by the model's predictions, it remained at  $\sim$  7.5 (close to the typical pH value of anaerobic digesters) (Fig. 2e). The biogas flow rate was very well predicted by the model's simulation, although there were some random under and overestimation of this variable during digester operations (Fig. 2f). Therefore, the model was able to reproduce the most common on-line variables monitored during AD operation. On the other hand, the average  $H_2S$  and  $O_2$  concentrations predicted in the gas phase was in agreement with the average empirical concentrations measured (Fig. 2c and d). However, the model was not able to reproduce the random H<sub>2</sub>S peaks observed during the period evaluated. Interestingly, those H<sub>2</sub>S peaks did not match any sudden rise in the sulfate inlet concentration or in soluble H<sub>2</sub>S concentrations in the digester broth (Fig. 3). Previous works have hypothesized that the biological oxidation of H<sub>2</sub>S may also occur in the headspace of the digester and in the superior layer of the anaerobic broth based on the high abundance of SOB bacteria recorded by the DGGE analysis [23]. A simple consideration of biomass retention was consequently proposed to partially overcome the limitation identified, while maintaining the model's complexity. The biomass retention approach, which is presented in the next section, separates the hydraulic retention time and the biomass retention time, in this case, for the SOB microorganism.

The decreasing trends in total organic matter (measured as total COD and VS concentrations) observed up to day 115th as well as the slight bounce back from this day onwards were both properly represented by the model (Fig. 3a, c). Likewise, the simulation of the evolution of the soluble COD concentration was in agreement with the empirical values throughout the entire operational time (Fig. 3b). Likewise, the inorganic nitrogen concentration was also properly predicted by the model, thus validating the calibration of the stoichiometric parameters conducted in the previous section. Fig. 3e also confirmed the ability of the ADM1 extension to describe the soluble Sulfate concentration in the anaerobic broth. In contrast, the soluble sulfate concentration in the anaerobic broth was overpredicted and only matched when values were above 0.3 kmol  $L^{-1}$ , which were in agreement with the results reported by [14].

### 3.4. Effect of the biomass retention

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Empirical observations of anaerobic digesters operated under microaerobic conditions have shown that SOB may form a biofilm inside the digester headspace, thus part of H2S oxidation may be carried out at the biofilm surface. Hence, Kobayashi et al [27] identified SOB in microbial mats located on the top of the biodigester, where elemental sulfur accumulated. Therefore, a new parameter in the S mass balance equation was proposed in order to take this biofilm based  $H_2S$  oxidation into account. This parameter, defined as "alpha", multiplies the  $X_{SOB}$  leaving the system and thus modifies the retention time of this microbial population. This is conceptually described in the mass balance shown in Eq. (4)

$$\frac{dX_{SOB}}{dt} = -alpha*D*X_{SOB} + growth \, rate - decay \tag{4}$$

Where D is the dilution rate or the inverse of the hydraulic retention time (HRT)

Fig. 4 depicts the new model predictions of the soluble and gaseous  $H_2S$  as a function of different alpha values compared to the experimental data. The influence of the presence of SOB (blue line)



Fig. 2. Time course of the online measurements of the concentration of methane (a), carbon dioxide (b), hydrogen sulphide (c) and oxygen (d) in the biogas, pH in the anaerobic digestion broth (e) and biogas flow rate (f). Experimental data (circles), model simulation (continuous line).



Fig. 3. Time course of the offline measurements of the total COD (a), soluble COD (b), volatile solids (c), sulfate (d), soluble hydrogen sulfide (e) and inorganic nitrogen (f) in the digester. Experimental data (circles), model simulation (continuous line).



**Fig. 4.** Time course of the H<sub>2</sub>S concentration in the liquid (a) and gas (b) phases at different alpha values. Experimental values (symbols), Black line = No SOB, blue line = alpha 1 (no retention), Green line = alpha 0,4, orange line = alpha 0.25 and grey line = alpha 0.1 (For interpretation of the references to colour in this figure legend, the reader is referred to the web version of this article).

in the anaerobic broth compared to the scenario without these  $H_2S$  oxidizing microorganisms (black line) in both soluble and gas phases was significant. These new simulations also showed the impact of variations in biomass retention on the soluble and gas  $H_2S$ . Model simulation of these two variables improved significantly when the alpha value decreased (= enhanced retention of the SOB in the digester). Hence, the formation of biofilms at the digester headspace maybe partially modeled by adding this biomass retention artifact. This model approach has been successfully performed in anaerobic filters treating vinasse wastewater [28]. In brief, despite more physico-chemical reactions should be considered when describing  $H_2S$  oxidation in anaerobic digesters operated under microaerobic conditions [16,29]; the approach here validated represents a good trade-off between complexity and reality.

### 3.5. Elemental sulfur accumulation

It is known that one of the main shortcomings of the application of microaeration, as a H<sub>2</sub>S removal method, is the accumulation of elemental sulfur in the digester. The build-up of this compound may lead to multiple operational hurdles such as pipeline clogging, hindered mixing or even digester damage due to an excessive weight increase. Based on the negligible aqueous solubility of elemental sulfur, an estimation of the accumulation of this element in the reactor can be carried out using the ADM1 extension developed here. Fig. 5 shows the time course of the mass of S° generated in the pilot reactor during the operational period analyzed here. Five kg of elemental sulfur could have potentially accumulated in the pilot digester over a period of  $\sim 200$  days of operation. This number should be deemed as a theoretical maximum since part of the S° produced was dragged out with the outlet digestate. This estimation of the S° accumulation in the digester can be used to plan the necessary maintenance measures. Therefore, the model developed in this study represents a useful operational tool for AD.

#### 4. Conclusions

An extension of the ADM1 capable of describing  $H_2S$  removal from biogas based on microaeration was developed and evaluated using experimental data from a pilot anaerobic digester. The maximum specific growth rate of the SOB along with four stoichiometric coefficients involved in nitrogen metabolism were estimated during model calibration. The model accurately described the most conventional variables monitored in anaerobic digestion processes (i.e biogas flow,  $CH_4$  and  $CO_2$  concentrations, pH and organic matter removal). The average concentrations of the



**Fig. 5.** Elemental sulfur accumulation in the experimental set-up over the operational period under microaerobic conditions.

S-related compound (i.e. soluble  $SO_4$  and  $H_2S$  in the gas and liquid phase) were properly described. Unfortunately, the model extension provided a poor description of the variations in the concentration of S compounds under transient conditions. Further model improvements may be carried out by separating biological  $H_2S$  oxidation in different sections of the digester or by even considering  $H_2S$  oxidation in the headspace biofilm on top of the digester.

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