

A General Framework of Scanning Tunneling Microscopy Based on Bardeen's Approximation for Isolated Molecules

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states. Numerical results demonstrate that the molecular images under different STM tip states and mapping modes can be quantitatively simulated in the present framework, which paves the avenue for the conclusive investigation of the ground state electronic structures for either neutral or charged molecules.

KEYWORDS: scanning tunneling microscope, general theoretical framework, charged molecules, Bardeen's approximation, analytic algorithm

tilizing quantum tunneling currents between tips and substrates under a certain bias voltage, the invention of the scanning tunneling microscope $(STM)^{1}$ in 1982 opened a door for direct visualizations of the investigated samples at the atomic scale and thus has been extensively applied in physics,² chemistry,³ material science,⁴ and biology.⁵ It is well-known that high-resolution STM images can be associated with the local density of states of the adsorbates, which provides a unique tool for the exploration of the electronic characteristic of the samples.⁶ Although direct adsorption of the sample molecules on prerequisite metallic substrates would inevitably lead to undesired strong perturbations, for instance, energy broadening, charge transfer, and geometrical distortion, on molecular electronic structures, these difficulties have been largely circumvented, and pristine molecular electronic structures can be obtained by using an epitaxial growing of insulating spacers, such as metal oxides,^{7,8} alkali halogenides,^{9–11} two-dimensional materials,¹² and organic layers,^{13,14} on metallic substrates to suppress the undesired dissipation effects (Figure 1a). Therefore, besides the frontier molecular orbitals that can be visualized by STM images,¹⁵ other molecular orbitals at arbitrary energy can also be obtained by the scanning tunneling spectroscopy (STS),^{16,17} i.e., the derivative of tunneling current with respect to the applied bias voltages, providing a powerful technique to precisely understand electronic structures in chemistry.

Accompanying the experimental efforts, developments of theoretical modeling for STM are also indispensable to unambiguously identify the molecular structures from the measurements. The theory of STM can be traced back to Bardeen's seminal work of perturbative treatment for tunneling currents between two separated metal layers.¹⁸ The symmetric current density operator, i.e., the so-called transfer Hamiltonian matrix, was defined.¹⁸ Although theoretical levels beyond perturbation have to be applied in large current regions,¹⁹ Bardeen's approximation is always valid in STM/ STS simulations, as the strong perturbations have to be deliberately suppressed so as to explore the electronic characteristic of the samples. 20 In other words, with the rational control of experimental setups, the tunneling channel that allows the adsorbates to stay in their ground states rather than excited or charging states^{21,22} during STM processes is dominant and thus is the focus of the present work. Assuming a locally spherical potential well, Tersoff and Hamann derived a simple version for the ground state wave function of the tip in the asymptotic region.²³ Substituting this analytic tip's wave function into Bardeen's approximation, the well-known conclusion as mentioned above, i.e., STM/STS images reflect the local density of states of samples,⁶ can be obtained. Later, Chen highlighted that the whole system could be divided into tip and sample regions by a separation plane and modified the tip's potential by truncating it in the sample region (Figure 1a),

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Figure 1. (a) Schematic of the experimental STM setup for investigating electronic structures of a single molecule that is decoupled from the metallic substrate by a thin insulating spacer. The gray-filled circle represents the adatom as in the spherical tip, i.e., a metal atom or an oxygen atom for metallic and CO-decorated tips, respectively. The left panel represents the truncated tip potential in the region of the red-dotted rectangle, where the blue-dotted line indicates the separation plane between the tip and sample regions. (b) The analytical (left) and Gaussian mimicked (right) wave functions of a typical STM tip at the ground state (top) and their derivatives with respect to the z-direction (bottom) on the plane 2.5 Å under the tip.

deriving a general formalism of the tip's wave function.^{6,24,25} Specifically, the radial and angular parts of the tip's wave function in the sample region are spherical modified Bessel functions and spherical harmonics, respectively (Section S1), which was supported by recent numerical simulations at the first-principles level.²⁶ In this context, the Tersoff–Hamann approximation corresponds only to an *s*-wave tip. Chen's results revealed that for the same electronic structure, *p*-wave tips could produce different STM images from *s*-wave, which has been experimentally confirmed by the STM images of pentacene on a bilayer NaCl above Cu(111) with and without CO decorated tip,²⁷ highlighting the symbiotic relationship between experimental measurements and theoretical simulations.^{28,29}

It is straightforward to simulate STM images with the Tersoff-Hamann approximation once the wave functions of samples were obtained.^{28–30} However, the Tersoff–Hamann approximation is only reliable for images with feature sizes well above 1 or 2 Å.²⁰ Besides, extra efforts should be made for the non-s-wave tips that can not only increase the image resolution but also gain new information with important implication for molecular orbital engineering.²⁷ The intrinsic limitations restrict applications of the Tersoff-Hamann approximation in precise determinations of electronic structures, resulting in a demand for the original Bardeen's approximation. In contrast to the Tersoff-Hamann approximation, few implementations of Bardeen's approximation are available even up to date.^{26,31-34} All these realizations are in the framework with periodic boundary conditions (PBCs). This is understandable because there is a naturally defined energy level in PBCs. However, the asymptotic behavior of the tip's wave function that can extend the validation of Bardeen's approximation⁶ was not considered in these implementations.³¹⁻³⁴ More importantly, in PBCs, only neutral systems can be effectively treated because extremely large supercells that bring unnecessarily heavy computational costs have to be adopted to suppress the effects of the inevitable neutralization background charges owing to the long-range characteristic of the electrostatic interaction in charged samples. With suitable spacers, STM/ STS experiments have the ability to visualize the electronic structures of charged systems.^{8,11,17} Recent experiments further revealed that the charged states could facilitate the rational onsurface synthesis under STM tips.³⁵ Thus, accurate simulations of the (charged) isolated molecular systems are starting to play an increasingly important role in chemistry.

In the present work, we proposed a general theoretical framework for STM simulations with Bardeen's approximation for isolated molecules whose wave functions are expanded by Gaussian functions (Section S2), where the asymptotic behavior of the tip's wave function could be taken into account. Specifically, the transfer Hamiltonian matrix element^{18,23}

$$M_{\rm ts} = -\frac{1}{2} \int_{\Sigma} (\Psi_{\rm t}^* \nabla \Psi_{\rm s} - \Psi_{\rm s}^* \nabla \Psi_{\rm t}) \cdot d\mathbf{s}$$
(1)

can be analytically evaluated (Section S3). Here Ψ_t and Ψ_s are quasi-particle wave functions of the tip and sample, respectively, Σ is the separation surface between the tip and sample regions, and s is the vector surface element on Σ .

As noted above, after truncation of the potential, the radial part of analytical Ψ_t is spherical modified Bessel functions (Table S1).^{6,24,25} For example, the wave function of an *s*-wave tip is proportional to $e^{-\kappa r}/r$, where κ is the decay rate and r is the distance from the tip. Owing to the appearance of the Coulomb operator (1/r) in Ψ_t , M_{ts} cannot be factorized,³⁶ which prevents its analytical evaluation.

On the other hand, Gill and Adamson found that the Coulomb operator could be accurately expanded by 37

$$\frac{1}{r} = \frac{\operatorname{erfc}(\omega r)}{r} + \frac{2\omega}{\sqrt{\pi}} \sum_{j=1}^{m} c_j \exp(-\omega^2 \alpha_j^2 r^2)$$
(2)

where erfc is the complementary error function, ω is the shortrange constant, and the coefficients c_j and exponents α_j are dimensionless constants. In the asymptotic region of $\omega r \gg 1$, the erfc part can be naturally dropped. In this context, further expanding the Slater function by Gaussian functions and taking the advantage of the Gaussian product theorem, the spherical modified Bessel functions on Σ can be mimicked solely by Gaussian functions.

As shown in Figure 1b, using only one Gaussian function can well reproduce the analytical s-wave as well as its derivative on Σ except for a slight contraction. More Gaussian functions and allowing different exponents in different directions are expected to further improve the reproduction of the analytical results, which is a direction worth trying in the future. The freely adjustable exponents in Gaussian functions significantly relieve the too-rapid decay feature into the vacuum. Furthermore, incorporating molecular wave functions that are expanded by Gaussian basis sets in the state-of-the-art quantum chemistry codes, the utilization of Gaussian functions allows the factorization of the integral in M_{st} , which thus leads to an analytic and fast recursive evaluation of the desired transfer Hamiltonian matrix for isolated systems. It should be stressed that in the present work, the asymptotic decay of the tip's wave function is implicitly taken into account, which agrees well with the numerical simulations based on the modified potentials.²⁶ We should also emphasize that the current algorithm could be readily extended for accurate simulations of the complex intermedia sates, especially manybody excitations of different charging states, 12,21,22 in STM processes owing to the capacity of the cluster model. In practical calculations, the exponent in the tip's wave function was set to be the same as that in Figure 1b.

To validate the current theoretical framework, we first simulated the STM images of pentacene, which is a widely used benchmark system in experiments.^{15,27,38} The theoretical results of the highest occupied molecular orbital (HOMO) and the lowest unoccupied molecular orbital (LUMO) of an isolated pentacene are depicted in Figure 2a. The measured STM images at negative ion resonance (NIR) at -2.4 V and positive ion resonance (PIR) at 1.7 V in previous experiments (Figure 2b, top panel)¹⁵ nicely resemble the features of native HOMO and LUMO, respectively. As shown in Figure 2b (bottom panel), the calculated STM images with an s-wave tip in the present work are in agreement with their experimental counterparts. The resemblances highlight the ability of the exploration of molecular structures by STM images with swave tips, which is the key conclusion in the Tersoff-Hamann approximation.^{6,23} We should note that although the calculated HOMO-LUMO gap, which is 2.3 eV, is only around half of the experimental results, the insulating spacer helps by suppressing the substrate perturbations on the adsorbates to allow for an accurate assignment as shown in the present work.

For the same molecular electronic structure, different tip's wave functions could lead to different STM images as shown in eq 1. Using a CO-functionalized tip, Gross et al. reported²⁷ that the PIR and NIR STM images (Figure 2c, top panel) have dramatically changed as compared to their counterparts from swave tip states, emphasizing the significant contribution of pwave tip states. Our constant current simulations reveal that the *p*-wave state can reproduce the experimentally measured outer lobes very well, while including some s-wave contribution improves the overall agreement with the experimental observations, especially the corner patterns in the PIR image (Figure S1). Our simulations confirm the previous proposal of using the *sp*-mix tip state for the CO-decorated tip,²⁷ while, at the same time, show the importance of using a suitable mapping mode to discriminate constant height images and constant current images (Figure S2). This conclusion is further



Figure 2. (a) Calculated HOMO (left) and LUMO (right) of isolated pentacene molecule with isovalue of $\pm 2.0 \times 10^{-3}$ au. (b) Top, experimentally measured constant current STM images of a decoupled single pentacene with a pentacene tip at the positive (PIR, left) and negative (NIR, right) ion resonance. Bottom, theoretically simulated constant current STM images for HOMO (left) and LUMO (right) of an isolated pentacene with an *s*-wave tip. (c) Top, experimentally measured constant current STM images of a decoupled single pentacene with a CO-decorated tip at PIR (left) and NIR (right). Bottom, theoretically simulated constant current STM images for HOMO (left) and LUMO (left) and LUMO (right) of an isolated pentacene with a *sp*-mix tip state. Experimental results in (b) and (c) were reproduced from ref 15 and ref 27 (copyright 2005 and 2011 by the American Physical Society), respectively.

validated by comparing the constant height and constant current simulations using the *sp*-mix tip state for the PIR and NIR STM images of naphthalocyanine (Figure S3). The good agreement with the corresponding experimental results has manifested the accuracy of the proposed framework for STM simulations that goes beyond the commonly used Tersoff–Hamann approximation.

We then move on to investigate charged systems that distinguish the new STM framework in the present work from all other implementations currently available. Because the insulating spacer can alter the work function of the substrate, the charge states of adsorbates can be rationally controlled.³⁹ For example, by dragging a ladder phenylene oligomer with



Figure 3. Top, calculated SOMO-1, SOMO, SUMO, and SUMO+1 (from left to right) of an isolated LP_9^+ molecule with an isovalue of $\pm 2.0 \times 10^{-3}$ au. Middle, experimentally measured constant height STS images of a decoupled single LP_9^+ molecule with a metal tip at bias voltages of -0.85, -0.65, +0.5, and +1.05 V (from left to right). Bottom, theoretically simulated constant height STS images for SOMO-1, SOMO, SUMO, and SUMO+1 (from left to right) of an isolated LP_9^+ with an *s*-wave tip. All experimental results were reproduced from ref 17. Copyright 2021 American Chemical Society.



Figure 4. (a) Calculated spin density in anionic water tetramers W_{4,C_4}^- , W_{4,C_s}^- , and $W_{4,C_{4h}}^-$ (from left to right). The isovalue for W_{4,C_4}^- is set to 5.0 × 10⁻⁵ au, while for W_{4,C_4}^- and W_{4,C_4}^- to 5.0 × 10⁻⁴ au. Calculated constant current (top) and constant height (bottom) STM images for SOMO of W_{4,C_4}^- , W_{4,C_s}^- , and $W_{4,C_{4h}}^-$ (from left to right) with an *s*-wave tip (b) and a *p*-wave tip (c). The red solid and dotted lines in (b) and (c) represent the skeleton of the water molecules and the hydrogen bonds between them, respectively.

nine benzene rings and steric methyl substitution groups (LP₉) from Au(111) to NaCl(2 monolayer)/Au(111) via STM tip manipulation, an electron transfer from LP₉ to the substrate automatically occurs, resulting in a positively charged LP₉ (LP₉⁺).¹⁷ It should be noted that this charged state is not the intermedia state during the tunneling processes. Utilizing constant height STS mapping, not only the frontier molecular orbitals, i.e., the singly occupied molecular orbital (SOMO) and singly unoccupied molecular orbital (SUMO), but also the SOMO-1 and SUMO+1 of LP₉⁺ have been recently visualized in experiments.¹⁷

According to the experimentally used tungsten tip with gold coating,¹⁷ an *s*-wave tip was used in the practical calculations. The simulated constant height STS images are in excellent

agreement with the corresponding experimental measurements (Figure 3). For SUMO+1, both experimental and theoretical STS images display six observable patterns along the long axis with an obscure central band, which should be attributed to the contributions from the cyclobutadiene rings in LP₉⁺. Although the cyclobutadiene and fused benzene ring both contribute to SOMO-1, the destructive interferences between them result in an obscure central pattern and two bright patterns located around the outermost benzene groups. Theoretical results reveal that the methyl groups that were deliberately introduced for increasing the selectivity of onsurface synthesis¹⁷ can contribute to the SOMO-1 image despite their effects being underestimated in simulations. Specifically, the fuzzy patterns adjoining the molecular center

moiety should be attributed to the methyl groups therein. In addition, the methyl groups in the outermost benzene can also contribute to the STS image, resulting in two crescent patterns around the molecular ends. It is interesting to note that the calculated images with PBC can also reproduce the SUMO+1 and SOMO-1 measurements of LP_9^+ , indicating that images of some orbitals would suffer less from the artificial extra neutralization background charges.

It was anticipated that STS images of SOMO and SUMO in LP_9^+ would have the same shapes because they are split from the HOMO of neutral LP₉ by removing an electron.¹⁷ Indeed, the calculated results with PBC gave nearly identical STS images of SOMO and SUMO in LP₉⁺ (Figure S4).¹⁷ Nevertheless, the actual experimental measurements showed that the most bright pattern in the SUMO image is located at the molecular center, while in the SOMO image, the terminal patterns become brighter. Besides this remarkable difference, the connection regions between the central and terminal patterns also have noticeable differences, where more diffuse patterns with higher contrast exist in the measured SUMO image. Our calculated constant height STS images for SOMO and SUMO of LP₉⁺ faithfully reflect all the measured differences. As shown in Figure 3, the contributions from the second and third outermost methyl groups in SOMO are suppressed after the relaxation of the electronic structure when removing an electron from LP_{9} (Figure S5), which should be responsible for the compact and low contrast patterns in the connection regions. On the other hand, the brighter central pattern in SUMO should be attributed to the subtle coefficient changes of p_z -orbitals of the conjugated carbon atoms in the positively charged state. It should be stressed that the above electronic relaxations were not observed in the calculations with PBC,¹⁷ which could originate from the indispensable neutralization background charges or plane wave basis sets. It is also noted that in this isolated system, we can correctly assign the high-resolution STS images once the order of energy level maintains (Table S2).

The last examples in the present work are anionic water clusters that are analogies of hydrated electrons.⁴⁰ There are two kinds of localization for the excess electron in anionic water clusters, namely interior and surface.⁴⁰ The visualization of the excess electron by STM would shed light on the precise nature of different local solvation environments as well as the dynamics between them. Although there are no experimental STM measurements for these species, we simulate here the STM images of anionic water tetramers (W_4^- , Figure 4a) to demonstrate the predictive power of the proposed framework. The structures with the C₄ (W_{4,C_4}^-) and C_s (W_{4,C_s}^-) symmetry point groups represent the surface localization. Meanwhile, the structure with the C_{4h} point group $(W_{4,C_{4h}})$ was considered for the interior localization. It should be noted that the prepared precursor observed on NaCl layers⁴¹ would facilitate the formation of $W_{4,C_{4}}$, although it has a very weak binding energy of the excess electron.⁴² The "free" water moiety with the double proton acceptor in the neutral precursor⁴³ would be helpful for the formation of $W_{4,C_{\circ}}^{-}$ since it is the most stable $W_4^{-.44}$ Besides, we also expect that the tetrahedral conformer⁴⁵ would be flattened owing to the substrates, resulting in Kevan structure-like W_{4,C_4}^{-} .

All calculated STM images with the *s*-wave tip for the excess electron in W_4^- were depicted in Figure 4b. All constant current STM images (Figure 4b, top panel) exhibit a quite diffuse pattern, which faithfully reflects the dispersion nature of the extra electron far away from the water molecules either in the surface or in interior structures. The constant height STM images of W_{4,C_s}^- and $W_{4,C_{4h}}^-$ as shown in the bottom panel in Figure 4b present a more focused pattern, indicating the contraction of the extra electron in the vicinity of the molecular kernel. Thus, the electron distributions should be a solid structure in W_{4,C_s}^- and $W_{4,C_{4h}}^-$. On the other hand, the four bright patterns associated with the free O–H bonds and the dim central pattern reveal a hollow structure of the excess electron in W_{4,C_s}^- .

The calculated constant current STM image of W_{4,C_4} with the *p*-wave tip as shown in the top panel in Figure 4c exhibits an obscure central pattern with four fused protrusions along the free O–H bonds, well capturing the hollow feature of the excess electron. Meanwhile, the constant current STM images of W_{4,C_s} and $W_{4,C_{4h}}$ with the *p*-wave tip are similar to their counterparts with the *s*-wave tip except for a slight translation in the W_{4,C_s} image and some minor deformations around the outer region in the $W_{4,C_{4h}}$ image. The single pattern should be attributed to the large curvature of the electron distributions in the central region in W_{4,C_s} and $W_{4,C_{4h}}$.

With the *p*-wave tip, all constant height STM images of $W_4^$ are distinguishable (Figure 4c, bottom panel). Specifically, the W_{4,C_4}^- image displays two ring shape patterns, where the outer ring is brighter. The constructive and destructive interferences inside and between the ring patterns are clearly exhibited in the image. For the W_{4,C_5}^- image, a bright crescent pattern located at the right side of the "free" water moiety and an obscure ring pattern around it are observed. Furthermore, a ring shape with four bright crescent patterns emerges in the $W_{4,C_{4h}}^-$ image. All these results should be attributed to the fact that no matter the surface and interior localizations, the extra electron in anionic water clusters is accommodated by the diffuse atomic orbitals of the hydrogen atoms in the "free" O–H bonds, which can be well characterized via the *p*-wave's quantum interaction.

Therefore, we make a theoretical proposal here. Owing to the extreme diffusion nature of the excess electron in W_4^- , the *s*-wave contributions have to be suppressed as much as possible to observe the above *p*-wave characteristic. Our test calculations indicate that the maximum *s*-wave contribution to distinguish different kinds of W_4^- is ~20% (Figure S6). According to the formation of the d_{π} band when CO adsorbed on metal surfaces,⁴⁷ strong interactions between CO's $1\pi/2\pi^*$ orbitals and metal's *d* orbitals would facilitate the promotion of the *p*-wave contributions.

In summary, we propose a general theoretical framework of STM simulations for isolated molecular systems with different charge states. The effects of different states in functionalized tips can also be accurately considered in the framework. The quantitative agreement between the simulated and experimentally observed STM images for HOMO and LUMO in neutral pentacene under different tip states and mapping modes manifests the accuracy of the proposed framework. Furthermore, the excellent reproduction of the experimentally measured STS images of LP_9^+ , especially the subtle relaxations

in the frontier molecular orbitals after ionization, highlights the advantages of the current framework in the exploration of the electronic structures in charged molecules. Taking W_4^- clusters as an example, our results demonstrate that with the CO-decorated tip, the detailed local solvation environments of different kinds of hydrated electron can be well characterized by STM images. Thus, with the cooperation of high-resolution STM measurements, the present framework provides a unique means for understanding molecular electronic structures and thus would have extensive applications in physics, chemistry, material science, and biology.

ASSOCIATED CONTENT

Supporting Information

The Supporting Information is available free of charge at https://pubs.acs.org/doi/10.1021/jacsau.2c00627.

Summary of tip's asymptotic behavior, theoretical methodology, computational details, and additional calculated results (PDF)

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Notes

The authors declare no competing financial interest.

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