1	A	Distinct Neural Code Supports Prospection of Future Probabilities During Instrumental
2		Information-Seeking
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12

## Abstract

13 To make adaptive decisions, we must actively demand information, but relatively little is known

14 about the mechanisms of active information gathering. An open question is how the brain

15 estimates expected information gains (EIG) when comparing the current decision uncertainty

16 with the uncertainty that is expected after gathering information. We examined this question

17 using fMRI in a task in which people placed bids to obtain information in conditions that varied

18 independently by prior decision uncertainty, information diagnosticity, and the penalty for an

19 erroneous choice. Consistent with value of information theory, bids were sensitive to EIG and its

20 components of prior certainty and expected posterior certainty. Expected posterior certainty was

21 decoded above chance from multivoxel activation patterns in the posterior parietal and

extrastriate cortices. This representation was independent of instrumental rewards and
 overlapped with distinct representations of EIG and prior certainty. Thus, posterior parietal and

extrastriate cortices are candidates for mediating the prospection of posterior probabilities as a

25 key step to estimate EIG during active information gathering.

# Introduction

26 27 In systems neuroscience, decision-making is modeled as a choice between alternative 28 options based on the decision makers' preferences, goals, and knowledge regarding the choice. 29 Traditional decision-making research has typically applied this framework to simple conditions, 30 in which decision-makers are assumed to possess the information relevant to their choice; for 31 example, a participant in a decision-making experiment is typically given a set of relevant 32 stimuli and asked to make a decision based on the stimuli. However, this differs substantially 33 from typical real-life situations in which individuals actively seek out the information that they 34 consider relevant to their choices. When making a natural choice, often one first determines 35 whether and from which source to obtain information (e.g., to which stimulus to attend) and only 36 then decides which action to take based on the information (Raiffa and Schlaifer 1961; S. C.-H. 37 Yang, Wolpert, and Lengyel 2016; Gottlieb 2018; Braunlich and Love 2022). The sampling of 38 decision-relevant (instrumental) information supports adaptive behaviors in humans and other 39 animals (Gottlieb and Oudeyer 2018), and its disturbances are linked to psychopathology 40 (Hauser et al. 2017; Baker et al. 2019), underscoring the importance of understanding its 41 mechanisms. 42 In natural settings, information is gathered through active sensing behaviors—for 43 example, when one attends to or looks at a visual cue (Tatler et al. 2011; S. C.-H. Yang, Wolpert, 44 and Lengyel 2016)—or, alternatively, through explicit purchase decisions—for example, when a 45 firm employs a consultant or a physician orders a medical test. Studies of information demand 46 have primarily tested the latter scenario, using tasks in which participants are given a description 47 of a situation and are asked to make a decision about whether or how much information to 48 request in the situation (Furl and Averbeck 2011; Filimon et al. 2020; Kaanders et al. 2021; 49 Gottlieb 2023). Neuroimaging investigations have focused on the value of information (VOI)— 50 the extent to which obtaining information increases the rewards expected from future actions and choices (Raiffa and Schlaifer 1961; Howard 1966)-and showed that VOI is encoded in value 51 52 and executive areas including the striatum, ventromedial prefrontal cortex, the dorsolateral

53 prefrontal cortex, and the anterior cingulate cortex (Kobayashi and Hsu 2019; Kobayashi et al. 54 2021).

55 An open question, however, concerns the probabilistic computations that precede VOI 56 estimation. In a decision-theoretic framework, VOI depends on both the rewards of a choice and, 57 crucially, on the expected information gain associated with information gathering. Expected 58 information gain, in turn, is the improvement in decision certainty that the decision-maker can 59 expect to obtain by gathering information. A simple measure of expected information gain is 60 probability gain (PG), defined as the difference between the decision maker's prior certainty 61 (PC)—the certainty about making the correct final choice before gathering information—and 62 their *expected posterior certainty* (EPC)—the certainty that is *expected* after gathering 63 information (Raiffa and Schlaifer 1961; Fischhoff and Beyth-Marom 1983; Baron 1985; Braunlich and Love 2022). PG describes humans' demand for instrumental information in two-64 65 alternative inference tasks (Baron 1985; Nelson 2005; Nelson et al. 2010), but its neural mechanisms are not well understood. 66

A particularly challenging step in computing PG is the ability to prospectively reason 67 68 about EPC—i.e., estimate the certainty that one expects to obtain after gathering information 69 (Raiffa and Schlaifer 1961; Braunlich and Love 2022). To understand the neural correlates of 70 EPC and related quantities, we used fMRI in a task in which participants placed bids revealing 71 their willingness to pay for information relevant to a binary choice. On each trial, participants

- 72 were informed about three quantities that were relevant to the normative bid: the prior
- 73 probability that a decision alternative was correct, the diagnosticity of the information (the
- 74 probability that it would correctly specify the correct alternative), and the penalty for an incorrect
- choice. By independently manipulating the three quantities, we distinguished between reward
- value and probabilistic computations of information gains. We show that the participants' bids
- had independent sensitivity to PC and EPC, consistent with normative theories postulating that
- these quantities are combined to estimate PG. We also show that EPC was decoded with above-
- chance accuracy from the multivoxel activity in three regions in the right posterior parietal and
- 80 extrastriate cortices. In these areas, the representation of EPC overlapped anatomically with
- 81 representations of bids, PC, and PG that involved distinct activity patterns. The findings reveal
- 82 candidate neural substrates for encoding expected information gain as a step that precedes but is
- 83 distinct from the assignment of instrumental value to information.

84	Results
85	The Willingness to Pay Task
86	Participants ( $N = 23$ ) underwent fMRI scanning while performing a task in which they
87	bid for information relevant to an incentivized choice (Figure 1A). The task was a modified
88	version of the "beads" task (Huq, Garety, and Hemsley 1988; Furl and Averbeck 2011; van der
89	Leer et al. 2015; Baker et al. 2019), in which participants were told that each trial had a hidden
90	state—a <i>portrait gallery</i> containing more pictures of faces than scenes or a <i>landscape</i> gallery
91	containing more pictures of scenes than faces. Rather than asking participants to infer the
92	gallery's identity on each trial, as is customary, we first presented them with 120 trials in which
93	they bid to receive additional information should they be asked to make the inference. Next, we
94	randomly selected one trial from those the participants bid, delivered information with a
95	probability that was proportional to the bid, asked participants to guess the gallery type, and
96	delivered a payoff that depended on the accuracy of this guess (Figure 1).
	A Trial from the Bidding Stage



97 98 Figure 1. Task A: Structure of a bidding trial. On each trial, participants saw the complementary prior 99 probabilities that the hidden gallery was a portrait or landscape gallery, the diagnosticity of a sample picture from 100 the gallery (i.e., its evidence strength represented by the ratio of majority to minority pictures in the hidden gallery), 101 and the amount the participant would be penalized from their endowment if the trial were realized for payment and 102 they incorrectly guessed the hidden gallery. These quantities could appear in a variety of spatial or temporal orders. 103 The participant then placed a bid for a sample picture from the hidden gallery, followed by a variable 1-10 s 104 intertrial interval. B: The distribution of prior probabilities and diagnosticities shown in the scan session (white 105 dots). The background color indicates PG, which increases with diagnosticity and decreases with PC (i.e., increases 106 as the prior probabilities approach 0.5).

107

108 Our focus was on how the participants' willingness to pay for information varied as a 109 function of the context, as defined by three quantities that were relevant to the normative bid and 110 were conveyed in words and numbers (Figure 1A). One quantity was the *penalty* for making an erroneous guess, a second quantity was the *prior probability* of a gallery type, and the third 111 112 quantity was the *diagnosticity* of the information (the probability that the information, if given, would indicate the correct gallery type, conveyed as the ratio of pictures in the majority versus 113 114 minority category; see Methods, Baker et al. (2019), and Furl and Averbeck (2011)). 115 Importantly, the three quantities were statistically dissociated, allowing us to distinguish their

116 influence on the bids. The penalty was randomly selected to be \$10 or \$20, while prior

**Behavior** 

- 117 probability and diagnosticity were randomized independently to tile the probability space as
- 118 shown in Figure 1B.
- 119
- 120 Our auction and payoff procedures incentivized participants to place a bid commensurate with
- the value of information (VOI), which was positively related to penalty and diagnosticity, and 121
- negatively related to the prior certainty (PC, the greater of the hidden gallery's complementary 122
- 123 prior probabilities; see Methods, Equation 1).

extended model

Strong 10<sup>1</sup> Substantial 101/2 Weak 10<sup>0</sup>





# 144

145 At both the group and individual levels, bids had a significant positive relationship with 146 the normative VOI (Figure S1). A linear mixed-effects model (Equation 14) confirmed this 147 result, yielding fixed-effects (group-level) coefficients that were negative for PC and positive for diagnosticity (Figure 2A, Table 1, the "Base Model"). The results were robust at the individual 148 149 level, as the vast majority of participants had negative coefficients for PC and positive 150 coefficients for diagnosticity and penalty (Figure 2A, gray dots; respectively, 22, 21, and 15 out 151 of 23). These results, which were obtained for the scan session, were consistent with the same 152 participants' behavior during the prescan session and were replicated in two different cohorts 153 who performed the task only outside of the scanner (Figure 2A, triangles, Table 1). The initial 154 slider position was included as a nuisance regressor and produced negligible effects, ruling out 155 sensorimotor artefacts (Figure S2A). Thus, participants understood the task and reliably placed 156 bids that were consistent with normative VOI.

157

158 **Table 1. Fixed-effects regression coefficients for the Base Model of participants' bids (Equation 14)** for every

159 cohort (Main Cohort: N = 23, Cohort 1: N = 21, Cohort 2: N = 15). *DF*: Degree of freedom (from Satterthwaite 160 approximation (Luke 2017)). *p*: *p*-value.

Regressor	Cohort	Coefficient	Standard error	T-statistic	DF	р
	Main, scan	-1.29	0.16	-7.88	23.00	< 0.001
Duion containty	Main, prescan	-1.44	0.16	-9.12	23.00	< 0.001
Prior certainty	2	-1.82	0.14	-14.40	21.00	< 0.001
	3	-1.50	0.19	-7.87	15.00	< 0.001
	Main, scan	0.93	0.19	4.88	23.00	< 0.001
Diagnosticity	Main, prescan	0.94	0.18	5.34	23.00	< 0.001
Diagnosticity	2	0.72	0.18	3.91	21.00	< 0.001
	3	1.17	0.23	5.20	14.99	< 0.001
	Main, scan	0.19	0.11	1.72	23.01	0.098
Donalty	Main, prescan	0.40	0.13	3.11	23.01	0.005
renaity	2	0.44	0.10	2.17	20.97	< 0.001
	3	0.37	0.09	4.08	15.00	< 0.001

161

162 While these results show that participants are sensitive to the information shown on the 163 screen, VOI depends on several quantities that are derived from this information. Specifically,

164 VOI scales with probability gain (PG), which is the difference between PC and expected

165 posterior certainty (EPC) and, in turn, EPC is derived from prior probability and diagnosticity

166 (**Equation 4**). To examine if participants estimated these quantities, we fit their bids to two

additional models: the *Condensed Model* accounting for the effect of PG (**Equation 15**) and the

168 *Extended Model* separately capturing the effects of PC and EPC (**Equation 16**). Consistent with

the Base Model, the Condensed Model produced positive fixed effects for PG (**Figure 2B**), and

the Extended Model yielded positive fixed-effects coefficients for EPC and negative fixedeffects coefficients for PC (Figure 2C). All fixed-effects coefficients were highly significant and

robust across groups (see detailed statistics in **Table 2** and **Table 3**), were highly consistent at

173 the individual level (gray dots in **Figure 2B–C**) and could not be explained by sensorimotor

174 artifacts (see Figure S2 for all the coefficients for all three models).

175

# 176 Table 2. Fixed-effects regression coefficient for the Condensed Model of participants' bids (Equation 15) for

- every cohort (Main Cohort: N = 23, Cohort 1: N = 21, Cohort 2: N = 15). *DF*: Degree of freedom (from
- 178 Satterthwaite approximation (Luke 2017)). *p*: *p*-value.

Regressor	Cohort	Coefficient	Standard error	T-statistic	DF	р
	Main, scan	1.62	0.23	7.18	23.00	< 0.001
Drohohility goin	Main, prescan	1.70	0.19	9.19	22.99	< 0.001
Probability gain	2	1.79	0.16	11.33	21.00	< 0.001
	3	1.99	0.25	8.01	15.00	< 0.001

# 179

180 **Table 3. Fixed-effects regression coefficients for the Extended Model of participants' bids (Equation 16)** for

181 every cohort (Main Cohort: N = 23, Cohort 1: N = 21, Cohort 2: N = 15). DF: Degree of freedom (from

182 Satterthwaite approximation (Luke 2017)). *p*: *p*-value.

Regressor	Cohort	Coefficient	Standard error	T-statistic	DF	р
	Main, scan	-1.84	0.24	-7.75	23.00	< 0.001
Duion containty	Main, prescan	-1.95	0.20	-9.90	22.99	< 0.001
Prior certainty	2	-2.22	0.16	-13.71	21.00	< 0.001
	3	-2.22	0.26	-8.38	15.00	< 0.001
	Main, scan	1.15	0.23	5.05	23.00	< 0.001
Expected posterior	Main, prescan	1.16	0.21	5.55	23.00	< 0.001
certainty	2	0.90	0.20	4.46	21.00	< 0.001
	3	1.49	0.26	5.80	15.00	< 0.001

183

184 Importantly, model comparisons decisively favored the extended model over both the 185 condensed and base models (**Figure 2D**) with Bayes factors far exceeding  $10^3$  in all the cohorts

186 (see legend for specific values). Moreover, in the extended model, the average difference

187 between the absolute value of each participant's coefficients for PC and EPC was significantly

188 positive (scan session: 2.52, T(22) = 2.60, SE = 0.97, p = 0.016, N = 23, paired T-test),

189 suggesting that participants integrated PC and EPC with unequal weights that relatively

190 underweighted EPC. Thus, rather than merely combining the quantities presented on the screen,

191 participants estimated the posterior certainty they expected to have after gathering information

and weighted it separately from their initial uncertainty when they bid for information. This

motivates the investigation of a neural representation of EPC as a neural basis of prospectiveBayesian inference.

195 196

# Neural Representations of Probabilistic Variables Relevant for VOI

To identify neural representations of the variables involved in calculating the bids, we applied multi-voxel pattern analysis (MVPA) to blood-oxygen-level-dependent (BOLD) signals during the response window of each trial in the bidding phase (**Figure 1A**). We used support vector regression and leave-one-run-out (four-fold) cross-validation and measured decoding accuracy for bid, PG, PC, and EPC as the Fisher *z*-transformed correlation between the predicted and actual values of the variable (Fisher 1921; 1915; Görgen and Hebart 2022).

203 Considering that EPC is a numerical representation of prospective Bayesian inference, we 204 first used a whole-brain searchlight analysis to identify clusters that showed significantly above-205 chance decoding of EPC with no cross-decoding of slider displacement or of bid, PG, and PC. 206 This identified three clusters that met these criteria located, respectively, in the right occipital 207 fusiform gyrus, right occipital pole, and right intraparietal sulcus (IPS)/extrastriate cortex

208 (Figure 3A–B, and Table S1). Decoders trained to read out EPC in these clusters produced no

- 209 significant cross-decoding of slider displacement, providing no credible evidence that they
- 210 encoded visual or motor events (Figure 3C). Moreover, the decoders produced no significant
- 211 cross-decoding of bids (**Figure 3D**, left) despite the fact that EPC was correlated with bids as a
- 212 necessary corollary of good task performance (Figure 2C), suggesting that they represented EPC
- 213 independently of information value. The clusters also did not cross-decode PG (Figure 3D,
- 214 middle), despite the fact that PG is the difference between EPC and PC (Equation 5). Finally,
- 215 the clusters also did not decode PC (Figure 3D, right), which, after excluding a small subset of
- 216 high-leverage trials that were high in both variables, was uncorrelated with EPC. Thus, the three
- 217 cortical clusters conveyed information about EPC independent of slider position, PG, PC, or the
- 218 value of information as reflected in bids.



219 220

Figure 3. Distinct multivoxel representations of expected posterior certainty (EPC), probability gain (PG), 221 prior certainty (PC), and bid in the posterior parietal and extrastriate cortices. A: Thresholded T-statistic map 222 of significant clusters of activation in which EPC could be decoded above chance, as identified by a whole-brain 223searchlight analysis (cluster-defining height threshold: p < 0.001; cluster-level familywise error rate correction 224 threshold: p < 0.05). The anatomical template was smoothed at FWHM =  $5 \times 5 \times 5$  mm for visualization purposes 225 (Poldrack, Mumford, and Nichols 2011, 173). B: The labeled significant clusters in which EPC could be decoded: 226 right occipital fusiform gyrus (OFG)/cerebellum, light blue; right occipital pole, green; and right intraparietal sulcus 227 (IPS) and adjacent extrastriate cortex, red. C-E: Decoding results from the 3 clusters. Each panel shows the 228 decoding accuracy of ROI-wise decoders that were trained and tested on the quantities noted in the panel title. Each 229 bar shows the mean decoding accuracy and standard errors across 23 participants. \*\*\*: p < 0.001, \*\*:  $0.001 \le p < 0.001$ 230  $0.01, *: 0.01 \le p < 0.05.$ 

231

We next asked whether these clusters may have had representations of bid, PG, and PC that anatomically overlapped with the representation of EPC but involved distinct activity

- patterns. Indeed, when we trained new decoders to decode bid and PG, we found significant
- above-chance decoding in all 3 ROIs (**Figure 3D**, left, middle) and, when we trained new
- 236 decoders to decode PC, we found significant above-chance decoding in the right IPS/extrastriate
- 237 cluster (Figure 3D, right). The lack of cross-decoding documented in Figure 3C makes it
- 238 unlikely that these results merely reflected correlations between these variables and EPC.
- Therefore, the clusters encoding EPC multiplex distinct neural representations of bid, PC, andPG.
- 241 Separate whole-brain searchlights identified additional clusters that encoded PC and PG
- 242 (Figure S3). These clusters showed no cross-decoding of slider position, showing that they were
- 243 unlikely to reflect sensorimotor confounds, nor significant cross-decoding of EPC (**Figure S3**).
- However, the clusters did show significant cross-decoding between PG and PC and between each
- variable and the participants' bids, making it difficult to pinpoint precisely which variable they encoded toward computing the bid.

## 247

# Discussion

248 We used behavioral testing and fMRI to investigate the mechanisms by which people estimate 249 expected information gain when assigning value to information. We provide evidence that, 250 consistent with value of information (VOI) theory, participants' estimates of VOI were informed 251 by the difference between expected posterior certainty (EPC) and prior certainty (PC). Moreover, 252 we show that portions of the right posterior parietal and extrastriate cortex conveyed distinct 253 multi-voxel representations of EPC and PC, which spatially overlapped with each other, as well 254 as with distinct representations of PG and the participants' bids. The results support the 255 hypothesis that participants prospect about future posterior probabilities and information gains 256 when estimating the instrumental value of information and reveal neural substrates underlying 257 this process.

258 An important feature of our task is that participants did not learn through repeated 259 experience but made one-shot decisions about the value of information based on quantities 260 explicitly shown on the screen: prior probability, diagnosticity, and penalty. While this differs 261 from some studies of Bayesian inference that allow learning based on feedback (Soltani and 262 Wang 2010; Kira, Yang, and Shadlen 2015; Ting et al. 2015; Soltani et al. 2016), it closely 263 follows studies of information gathering that have typically relied on one-shot decisions based on 264 a description of behavioral context (Kobayashi and Hsu 2019; Filimon et al. 2020; Kobayashi et 265 al. 2021; Gottlieb 2023). A second important task feature is that we limited participants to a 266 single additional sample rather than allowing them to request multiple samples. While this 267 distinguishes our approach from studies examining how people terminate sampling (i.e., decide 268 how much information to gather before making a choice (Edwards 1965; Huq, Garety, and 269 Hemsley 1988; Roitman and Shadlen 2002; Furl and Averbeck 2011; Hanks, Kiani, and Shadlen 270 2014; Baker et al. 2019; Kaanders et al. 2021; Ashinoff et al. 2022)), it allowed us to understand 271 with greater experimental control how participants prospect about information gains over a 272 single time step (e.g., avoiding systematic distortions and noise that may gradually accumulate 273 over samples (Ashinoff et al. 2022)).

274 Our results support the idea that participants prospect about future certainty as noted 275 above, and also show that, rather than directly comparing PC to EPC with equal weights, they 276 afforded greater weight to PC relative to EPC. A possible explanation for this differential 277 weighting is that EPC is derived through more complex computations making it more vulnerable 278 to probability underweighting, a known phenomenon during judgments from described 279 probabilities (Gonzalez and Wu 1999; Trepel, Fox, and Poldrack 2005; Garcia, Cerrotti, and 280 Palminteri 2021). Alternatively, participants may underuse EPC because perhaps prospection 281 itself is costly. These factors, in turn, may explain why participants prospect over a limited time 282 horizon when allowed to take sequential samples (Braunlich and Love 2022), as can be 283 examined in future research.

284 Our approach also generated new insights into the neural substrates underlying 285 information gathering. The encoding of probabilistic variables that we found in the posterior 286 parietal cortex is consistent with multiple studies that have implicated this area in probabilistic 287 reasoning. In tasks in which participants make Bayesian inferences based on given (exogenous) 288 information, the human posterior parietal cortex tracks prior probability (Mulder et al. 2012), 289 likelihood (d'Acremont, Fornari, and Bossaerts 2013; d'Acremont, Schultz, and Bossaerts 2013), 290 likelihood uncertainty (Ting et al. 2015), and posterior probability (Singletary, Gottlieb, and 291 Horga 2021), while monkey parietal neurons encode posterior probability or expected rewards 292 (Huk and Shadlen 2005; Kira, Yang, and Shadlen 2015; T. Yang and Shadlen 2007). In tasks in

293 which participants endogenously select information, monkey parietal neurons encode

diagnosticity (Foley et al. 2017) and prior uncertainty (Horan, Daddaoua, and Gottlieb 2019; Li

et al. 2022) and the human parietal cortex tracks the propensity to sample information relevantfor learning a category boundary (Furl and Averbeck 2011).

297 Our findings extend these reports by showing that the human parietal cortex and 298 extrastriate areas multiplex information about probabilistic variables—of EPC, PC, and PG—that

- are distinct from variables representing information value. Thus, our results support the idea that
- 300 information gathering has separate probabilistic and value-based components, as proposed based
- 301 on both behavioral (Braunlich and Love 2022) and neural (Silvetti et al. 2023) results. This result
- 302 is consistent with studies showing that monkey parietal neurons carry dissociable signals of prior
- 303 uncertainty and rewards (Horan, Daddaoua, and Gottlieb 2019; Li et al. 2022). The findings are
- also consistent with previous studies proposing that VOI is encoded in areas that are distinct
- from the EPC clusters we identified here, and include the human striatum, dorsolateral prefrontal cortex, and ventromedial prefrontal cortex (Kobayashi and Hsu 2019; Kobayashi et al. 2021).
- 307 Moreover, our findings that additional clusters non-specifically encode PC, PG, and bids,

308 suggesting the possibility, which can be tested in future research, that probabilistic and value

309 quantities are integrated into a single code for driving the bids. Thus, our results bring granular

insights into the distinct neural mechanisms of probability and reward estimation during active

- 311 information gathering.
- 312

313	Methods
314	Participants
315	Forty-four healthy, right-handed participants (17 female) were recruited through fliers posted on
316	the Columbia University campus and through the recruitment system for the Columbia Business
317	School Behavioral Research Lab. This pool consisted of Columbia University students, other
318	Columbia affiliates, and affiliates of other universities in the New York Metropolitan Area, and
319	they did not report any psychiatric or neurological disorders. Participants first completed a
320	session outside of the scanner (prescan session); 14 participants were not allowed to advance to
321	the scan session because their responses during the prescan session reflected disengagement or
322	lack of comprehension (see "Performance-Based Exclusion Criteria"). Another participant was
323	excluded because of excessive motion inside the MRI scanner, and 6 participants met the
324	advancement criteria but withdrew from the scan session. As a result, the Main Cohort consisted
325	of 23 participants (8 female).
326	We also recruited 19 participants (13 female) through the same methods to complete the
327	experiment outside of the scanner. Fourteen participants (10 female) met the comprehension
328	criteria and were included in the Cohort 2. Added to Cohort 2 were the participant who was
329	excluded because of excessive motion and the 6 participants who withdrew from scanning in the
330	Main Cohort.
331	Before developing the main experimental session, we recruited 23 participants (9 female)
332	through the same methods for a pilot session to be completed outside of the scanner. Fifteen of
333	these participants (7 female) met the comprehension criteria and were included in Cohort 3.
334	Experimental procedures were approved by the Columbia University Institutional Review Board,
335	and all participants provided signed informed consent.
336	Experimental Sessions
337	Prescan Session
338	The prescan session was administered on a computer outside of the scanner. Participants viewed
339	a narrated slideshow on the instructions for the Willingness to Pay (WTP) Task, the main task of
340	the experiment. They were also administered comprehension quizzes on the instructions, which
341	they had to pass before proceeding ( <b>Performance-Based Exclusion Criteria</b> ). After passing the
342	instructions quiz, participants completed 10 practice trials of the WTP Task to familiarize
343	themselves with the relationship between their bids, the receipt of a sample picture, decision
344	accuracy, and ultimately, their earnings, all while avoiding overtraining. Each practice trial was
345	followed by a corresponding mock payout trial to show participants what they could have earned
346	from that trial in the main task based on their submitted bid and their guess of the identity of the
347	hidden gallery if the trial had been chosen for payout; however, these practice trials did not affect
348	the participants' earnings. Then, participants completed the WTP Task. Lastly, their performance
349	was evaluated to determine if they met the remaining performance criteria to advance to the scan
350	session; if not, they were removed from the study.
351	Scan Session
352	Participants watched a summarized version of the instructions slideshow before completing the
353	WTP Task in the MRI scanner.
354	The Willingness to Pay Task
355	The Willingness to Pay (WTP) Task was a modified "bookbag-and-poker-chip" (Peterson and
356	Miller 1965; Phillips and Edwards 1966; Bar-Hillel 1980; Gigerenzer, Hell, and Blank 1988;

- Benjamin 2019) (or "beads" (Huq, Garety, and Hemsley 1988; Furl and Averbeck 2011; van der
- Leer et al. 2015; Baker et al. 2019; Kobayashi et al. 2021)) task developed to measure people's

- demand for instrumental information. On the task, people needed to correctly infer the identity of
- a hidden state depicted as a museum gallery to avoid a penalty. The task consisted of a *Bidding*
- 361 *Stage* followed by a *Payout Stage*. At the beginning of each session, the participant was given a
- 362 \$30 endowment. Then, during the Bidding Stage, the participant placed bids for a sample picture
- 363 from the hidden museum gallery that could increase the accuracy of their inference. During the
- 364 Payout Stage, one bidding trial was drawn at random to be realized to determine the participant's
- 365 payout. The bid on the realized trial was applied to a computer-automated auction that ensured
- that the probability of receiving a sample increased with the bid such that a higher bid
- 367 corresponded to higher demand for the sample (The auction and the expected value–
- 368 **maximizing bid**). The bid would be withdrawn from the endowment if the participant won the 369 auction on the realized trial, and a penalty would be withdrawn if the participant's inference was
- 370 incorrect.
- 371 Bidding Stage
- 372 The Bidding Stage consisted of 120 trials divided evenly into four runs. On each trial,
- 373 participants bid for one sample picture from the hidden gallery that could help them better infer
- 374 whether it was a *portrait gallery* that contained more pictures of faces than scenes or a *landscape*
- 375 gallery that contained more pictures of scenes than faces. Before bidding, participants viewed the
- 376 *prior probability* that the hidden gallery was a portrait or a landscape gallery; the *diagnosticity*,
- 377 or predictive validity, of a sample picture; and the *penalty* that they would lose if the trial were 378 realized for payout and they incorrectly guessed the gallery.
- To prevent behavioral artifacts from serial trial effects, we truthfully told participants that each bidding trial was independent from all other bidding trials, and the identity of a bidding trial's hidden gallery was never revealed during the Bidding Stage.
- *Trial display.* The prior probability of the hidden gallery was displayed as a percentage chance for the portrait and landscape options. The diagnosticity was displayed as the majority-tominority ratio of picture types in the hidden gallery (e.g., 60:40). Participants were also shown the *penalty* that they could lose from the endowment if the trial were chosen for payout (**Payout trial**).
- 387 A trial began with the prior probability, diagnosticity, or penalty appearing (trial 388 components) over a gray background (Figure 1A). The prior probability, diagnosticity, and 389 penalty appeared one at a time with the first component appearing at the instant of trial start and 390 the succeeding components following the previous component by 1 s (Figure 1A). The trial 391 components' spatial order of appearance was stable throughout the prescan and scan sessions but 392 counterbalanced by participant so that participants could expect the information to be in the same 393 place while allowing us to control for potential effects of spatial order. The trial components' 394 temporal order of appearance was randomized by trial to control for potential primacy and 395 recency effects.
- 396 *Response.* Participants completed a trial by reporting their bid for a sample picture from 397 the hidden gallery by using a trackball to move a slider that appeared at the bottom of the screen 398 1 s after the last trial component. The initial slider position was randomized on each trial to 399 reduce the correlation between slider movement and the bid-facilitating the separation of the potentially confounding effect of slider movement from the task variables of interest-and to 400 401 discourage participants from anchoring to any one reported bid. (Randomizing the initial slider 402 position reduces the correlation between slider displacement and bid from nearly 1 to 0.58 across 403 all completed trials in the scan session.) The slider remained on screen for 10 s ("response
- 404 window," Figure 1A). We chose a response window of 10 s because it was the shortest response

405 window that captured approximately 80 percent of responses from 80 percent of participants 406 during piloting. The selected bid was indicated by the amount of the slider from left to right that 407 was highlighted in orange and by an explicit amount in dollars below the slider. Both these 408 indicators were updated in real time. The slider was divided into 77 discrete bins, increasing in 409 steps of \$0.13 from \$0 on the left to \$9.88 on the right. We chose these increments to discourage 410 participants from anchoring to "round" numbers (e.g., multiples of \$1 or \$2.50). The participant 411 confirmed their response by clicking a button on the trackball, after which the highlighted 412 section of the slider would change colors from orange to green to indicate that the response had 413 been recorded. The screen remained unchanged until the end of the response window plus 0.5 s. 414 If the participant did not submit a posterior probability estimate within the 10-s response 415 window, instead, the slider would freeze for 0.5 s and the percentage below the slider would be 416 replaced by text reading, "Bid not submitted." To encourage participants to respond within the 417 response window, participants were truthfully warned that if a response were missing from a trial 418 that happened to be chosen for payout, they would automatically lose that trial's penalty. Across 419 all participants in the Main Cohort during the scan session, only 23 of the 2,760 presented trials 420 (0.8%) had omitted responses, with 7 participants missing one trial, 4 participants missing two 421 trials, 1 participant missing three trials, and 1 participant missing five trials. 422 Intertrial interval. Each bidding trial was followed by an intertrial interval during which a 423 small, black fixation cross appeared over the gray background (Figure 1A). To maximize the 424 efficiency of parameter estimation for the general linear models in the fMRI analysis, the 425 duration of each intertrial interval was drawn from an exponential distribution with mean 3.5 s, 426 truncated with a lower bound of 1 s and an upper bound of 10 s (Hagberg et al. 2001). 427 Selection of parameters for bidding trials. To determine the set of prior probabilities and 428 majority-minority ratios used for the bidding trials in each session, we randomly sampled 60 429 trials from discrete bins that we established for prior probability (0.1, 0.4, 0.5, 0.6, and 0.9, 430 arbitrarily chosen as the prior of the portrait gallery) and majority-minority ratio (60:40, 80:20, 431 and 90:10). Majority–minority ratios represented diagnosticity  $\theta$ , which was defined on the 432 interval  $0.5 < \theta < 1$  and corresponded to the numerator of the majority-minority ratio divided 433 by 100. A random jitter (-0.03, -0.02, -0.01, 0, 0.01, 0.02, or 0.03) was then added to each prior 434 probability and diagnosticity with equal probability. A "true" hidden gallery was assigned to 435 each trial based on the prior probability of the portrait gallery (e.g., if the prior probability was 436 0.6, there was a 60% chance the trial's hidden gallery would be a portrait gallery and a 40% 437 chance it would be a landscape gallery). If the trial were realized for payout, its sample picture 438 was assigned to signal the hidden gallery with a probability equal to the trial's diagnosticity (e.g., 439 on a trial on which the hidden gallery was a portrait gallery and the diagnosticity was 0.6, there 440 was a 60% chance that the sample picture would be a face). These 60 trials were duplicated for 441 each condition of error penalty (\$10 or \$20). The order of the trials was then randomly permuted, 442 and the session was separated into four runs of 30 trials each. Figure 1B displays the prior-443 diagnosticity combinations for the scan session. Every participant within a cohort completed the 444 same session(s). 445 Payout trial

446 After the Bidding Stage was complete, one bidding trial was chosen at random with equal

447 probability to be realized to determine the participant's payment. This trial was displayed along

448 with its submitted bid from the Bidding Stage. If the participant had failed to submit a bid on that

trial, the participant was notified that the error penalty would be automatically subtracted from

450 their endowment, and the session would end.

451 Otherwise, the bid was submitted to an auction for the sample picture. If the participant 452 had bid enough to win the auction, the bid would be subtracted from their endowment, and they 453 would receive one sample picture, randomly drawn from the hidden gallery, to help them decide 454 the hidden gallery's identity (in addition to the prior probability of the hidden gallery and the 455 diagnosticity of a sample picture). If the participant had not bid enough to win the auction, the 456 bid would not be subtracted from their endowment, but they would have to decide using only the 457 prior probability of the hidden gallery.

458 After deciding the identity of the hidden gallery, the penalty would be subtracted from 459 the participant's endowment if and only if their choice was incorrect. Hence, the payment for the 460 WTP Museum Task was the endowment minus the bid (if and only if they received a sample)

461 and minus the penalty (if and only if they chose the incorrect gallery).

462 The auction and the expected value–maximizing bid

463 We elicited participants' valuation of the sample through a first-price auction. On the realized

trial, the computer chose but did not reveal a secret price for the sample picture from

a random uniform distribution between the minimum and maximum possible bids (\$0 and \$9.88,

respectively). If the participant's bid on the realized trial was greater than or equal to the secret

- 467 price, the participant would receive the sample, but their bid would be subtracted from their
- 468 endowment. If the participant's bid was less than the secret price, the participant would not
- 469 receive the sample, but nothing would be subtracted from their endowment. This procedure is
- inspired by the Becker-DeGroot-Marschak auction (Marschak, DeGroot, and Becker 1964) and
- 471 is similar to a traditional auction for an item in which the highest bidder receives the item in472 exchange for their stated price. Hence, the participant must assess the risk of losing the penalty if
- 472 exchange for their stated prec. Hence, the participant must assess the fisk of fosting the penalty i 473 they incorrectly guessed the hidden gallery against the potential cost of a sample picture that
- 474 could decrease the chance of an incorrect guess.

475 This cost-benefit analysis for the WTP Task bids is mathematically tractable for an 476 expected value maximizer. Intuitively, the expected value-maximizing bid in this auction 477 increases with the expected information gain (EIG), or informativeness, of the sample-the 478 greater the sample's EIG, the more an agent should be willing to pay to receive a sample. To 479 express the expected value-maximizing bid in terms of EIG, we measured EIG using probability 480 gain, the extent to which the sample picture would increase the probability of correctly guessing 481 the hidden gallery (Baron 1985; Nelson 2005). We chose probability gain because it has been 482 shown to modulate people's demand for instrumental information (Nelson et al. 2010) and 483 because bids from the auction can be expressed as a simple linear function of it.

484 To estimate probability gain, one needs to compare the probability of correctly guessing 485 the hidden gallery without the sample picture to the expected probability of correctly guessing 486 the hidden gallery with the sample picture. We call the first component of probability gain the 487 *prior certainty* of the hidden gallery (Pr(C)), which is the maximum of the hidden gallery's prior 488 probability distribution (**Equation 1**). Here, Pr(F) is the prior probability of the portrait gallery, 489 and Pr(S) is the prior probability of the landscape gallery.

490

# Equation 1

# $Pr(C) = max(Pr(F), Pr(S)), 0.5 \le Pr(C) \le 1$

491 We call the second component of probability gain the *expected posterior certainty* (EPC) 492 of the hidden gallery. Calculating the expected posterior certainty requires prospecting the future 493 posterior probability distributions for a gallery type (*F* for the portrait gallery, *S* for the 494 landacene cellery) taking the maximum of these posterior distributions conditional on receiving

494 landscape gallery), taking the maximum of these posterior distributions conditional on receiving

495 each type of sample picture (f for a face picture, s for a scene picture), and weighting each maximum by the marginal probability of the respective picture type. 496

497 The posterior probability of gallery H conditional on sample picture D is given by Bayes' 498 theorem in terms of the prior probability of the gallery  $(\Pr(H))$ , the likelihood of receiving 499 sample picture D conditional on the gallery (Pr(H)), and the marginal probability of the sample 500 (Pr(D)) (Equation 2, where H stands for "hypothesis" and D for "data," by convention). The 501 prior probability of each gallery type is explicitly shown on a trial, while the likelihood and 502 marginal probability of a sample type can be calculated from variables that are shown on a trial. 503 The prospected likelihood is the diagnosticity ( $\theta$ ) if the sample picture is prospected to signal 504 gallery H (i.e., when gallery H is the portrait gallery and the sample is prospected to be a face, or 505 when gallery H is the landscape gallery and the sample is prospected to be a scene), while the 506 likelihood is the complement of the diagnosticity  $(1 - \theta)$  if the sample picture is prospected to 507 signal the opposite gallery. The prospected marginal probability of sample D is the product of the diagnosticity of the sample and the prior probability of the gallery signaled by the sample plus 508 509 the product of the complement of the diagnosticity and the complement of the prior probability

- 510 signaled by the sample (Equation 3).
- 511

**Equation 2** 

## 512

# $Pr(D) = \theta Pr(H) + (1 - \theta)(1 - Pr(H))$

 $Pr(H|D) = \frac{Pr(H) Pr(D|H)}{Pr(D)}$ Equation 3

#### 513 Therefore, we can use the marginal probability of each sample type and the posterior 514 probability distribution for each gallery to calculate the expected posterior certainty of the hidden

515 gallery (Equation 4). 516

### **Equation 4**

 $Pr(C)' = Pr(f) \max(Pr(F|f), Pr(S|f)) + Pr(s) \max(Pr(F|s), Pr(S|s))$ 517 This is equivalent to the maximum of the prior certainty and the diagnosticity (Pr(C))' =518  $\max(\Pr(C), \theta)$ ). 519 Therefore, in terms of prospecting the expected certainty after receiving a sample picture,

520 probability gain G is the EPC minus the prior certainty (Equation 5). **Equation 5** 

521

# $G = \Pr(C)' - \Pr(C), \Pr(C)' \ge \Pr(C)$

522 Probability gain can be equivalently expressed as a rectified function of the sample's 523 diagnosticity and the prior certainty of the hidden gallery (Equation 6). 524 **Equation 6** 

 $G = \max(\theta - \Pr(C), 0)$ 

To calculate the bid  $B_{Emax}$  in this auction that maximizes the expected value of a trial, we first 525 526 need to calculate the expected value of a trial  $\mathbb{E}$  in terms of the endowment, the penalty, Pr(C), 527 and Pr(C)'. Expected value is the value of the outcome minus its cost. Since the value and cost 528 of a trial depend on whether the agent receives a sample, which is a random event, let the value 529 be  $\tilde{V}$ , a random variable representing the value of the *outcome*, and let the cost of the outcome be

- C, a random variable representing the price the agent ultimately pays for the sample (Equation 530 531 7).
- 532

## **Equation 7**

- $\mathbb{E} = \tilde{V} C$
- To calculate *E* over all the possible realizations of a trial, let us calculate the probability density 533
- 534 function for receiving a sample. As stated earlier, the computer chooses a random price X in
- 535 dollars from a uniform probability distribution on the interval of possible bids  $0 \le X \le 9.88$ .
- 536 Thus, the probability density function for the random variable X is 537
  - **Equation 8**<sup>1</sup>

$$f(x) = \frac{1}{9.88}, 0 \le x \le 9.88$$

- 538 Now, let us take  $\mathbb{E}$  over all possible realizations of X:
- 539

# **Equation 9** 0.00

$$\mathbb{E} = \int_0^{9.88} (\tilde{V}(x) - C(x)) f(x) dx$$

- 540 Equation 9 can be decomposed into the utility of winning the auction (the left addend in
- 541 **Equation 10**) and the utility of losing the auction (the right addend in **Equation 10**):
- 542

555

556

557 558

559

$$\mathbb{E} = \int_0^B (\tilde{V}(x) - C(x))f(x)dx + \int_B^{9.88} (\tilde{V}(x) - C(x))f(x)dx$$

**Equation 10** 

- Now let us replace the random variables  $\vec{V}$  and C with the exact outcomes that they represent. To 543 544 do so, first let us construct the tree of possible outcomes for a realized trial: at the first step, the 545 agent may win or lose the auction for the sample picture, and at the second step, the agent may 546 correctly or incorrectly guess the identity of the hidden gallery: 547 • When the agent wins the auction 548
  - When the agent correctly guesses the hidden gallery  $\tilde{V} = (C)'$  (because they win the full endowment, which is \$30)
- 549 550 .  $C = \Pr(C)' B$ o When the agent incorrectly guesses the hidden gallerv 551  $\tilde{V} = (1 - \Pr(C)')(30 - W)$ 552 •  $C = (1 - \Pr(C)')B$ 553 When the agent loses the auction 554
  - When the agent correctly guesses the hidden gallery 0
    - $\tilde{V} = 30 \operatorname{Pr}(C)$
    - C = 0
  - o When the agent incorrectly guesses the hidden gallery
    - $\tilde{V} = (1 \Pr(C))(30 W)$ • C = 0

560

<sup>&</sup>lt;sup>1</sup> Letting B be the agent's bid for the sample, the probability of receiving a sample is therefore  $\frac{B}{988}$  because Pr(X < 9.88=0Bfxdx=0B19.88dx=B9.88.

Replacing  $\tilde{V}$ , C, and f(x) in Equation 10 with the above terms yields the expected value of a 561 trial in terms of the endowment, the penalty, Pr(C), and Pr(C)' (Equation 11). 562

$$\mathbb{E} = \int_{0}^{B} \left( \Pr(C)' \left( 30 - B \right) + \left( 1 - \Pr(C)' \right) \left( 30 - B - W \right) \right) \frac{1}{9.88} dx \\ + \int_{B}^{9.88} \left( 30 \Pr(C) + \left( 1 - \Pr(C) \right) \left( 30 - W \right) \right) \frac{1}{9.88} dx \\ \mathbf{Equation 11}$$

563

$$\mathbb{E} = \frac{B(\Pr(C)' W - \Pr(C) W) - B^2}{9.88} + 30 - W(1 - \Pr(C))$$

564 To find the expected value–maximizing bid (Equation 12), let us differentiate E with respect to 565 the bid, set the derivate equal to 0, and solve for the bid  $B_{\mathbb{E}max}$ :

$$\frac{\partial \mathbb{E}}{\partial B} = \frac{W(\Pr(C)' - \Pr(C)) - 2B}{9.88}$$
$$\frac{W(\Pr(C)' - \Pr(C)) - 2B_{\mathbb{E} max}}{9.88} = 0$$
$$\frac{9.88}{\text{Equation 12}}$$

566

$$B_{\mathbb{E} max} = \frac{W(\Pr(C)' - \Pr(C))}{2}$$

567 Note that the endowment does not affect the expected value-maximizing bid.

- Recall that probability gain is the difference between EPC and prior certainty. Therefore, 568
- 569 we can rewrite **Equation 12** in terms of probability gain G (**Equation 13**). We use both this form
- 570 and the form in **Equation 12** to model participants' bids in terms of expected information gain. 571

**Equation 13** 

$$B_{\mathbb{E}\,max} = \frac{WG}{2}$$

- Since the WTP Task only accepts bids in bins (Figure 1A), on the real task, the expected value is 572 573 maximized by submitting a bid as close as possible to the expected value-maximizing bid.
- 574 Performance-Based Exclusion Criteria

575 To ensure participant comprehension and engagement during the scan session, we assessed

576 participants' performance during the prescan session before we allowed them to advance to the

577 scan session. Participants had to meet the following criteria pertaining to the WTP Task to

#### 578 advance to the scan session:

- 579 1. Task comprehension: Participants had to correctly answer at least 80 percent of the 580 questions on a comprehension quiz on the task instructions.
- 2. Task completion: Participants could miss no more than 5 percent of the trials. 581
- 582 3. Minimal dependence of bids on expected information gain (EIG): Bids must have been 583 significantly higher ( $\alpha = 0.05$ , two-sample t-test assuming unknown and unequal 584 variances) on trials with high probability gain ( $\geq 0.33$ ) than on trials with low probability 585 gain ( $\leq 0.1$ ).

586 To measure participants' intrinsic demand for instrumental information without extensive 587 training, the criteria were designed to be lenient enough to respect variation in their pre-task

588 strategies while excluding participants who disengaged from the task or who adopted strategies

589 clearly consistent with misunderstanding the task.

- 590 Image Sets
- 591 Images of faces were selected from the CNBC Faces database by Michael J. Tarr, Center for the
- 592 Neural Basis of Cognition and Department of Psychology, Carnegie Mellon University,
- 593 <u>http://www.tarrlab.org</u>, funded by NSF award 0339122, used in Righi et al. (2012), and are
- 594 available under a Creative Commons Attribution-NonCommercial-ShareAlike 3.0 Unported
- 595 License. Images of scenes were selected from the database for Konkle et al. (2010)), available
- 596 from the Computational Perception and Cognition Lab at MIT
- 597 (http://olivalab.mit.edu/MM/sceneCategories.html).
- 598 Earnings
- 599 Compensation for the prescan session was a show-up fee of \$15 on top of their earnings from the
- 600 prescan session. Compensation for the scan session was a show-up fee of \$20 on top of their
- 601 earnings from the scan session. Participants received an extra \$50 for completing both sessions.
- Therefore, they could earn up to \$145 for completing the entire study.
  - Modeling the Value of (Instrumental) Information
- 604 Our general strategy was to implement linear mixed-effects regression to properly account for
- between-participant variance (fixed effects) and within-participant variance (random effects),
- 606 using the MATLAB function fitlme with maximum likelihood estimation. In all mixed-effects
- models, we used the Satterthwaite approximation to calculate degrees of freedom, which has
- 608 been shown to reduce Type 1 error compared to residual degrees of freedom (Luke 2017). Unless 609 otherwise specified, each predictor was *z*-scored at the group level before the regression model
- 610 was fit.

603

- 611 As a manipulation check, we first modeled participants' bids *B* as a function of the 612 observed variables on a trial: prior certainty (appears on screen as the maximum of the prior 613 probability distribution, **Figure 1A**), diagnosticity, and penalty *W* along with an intercept  $\beta_0$
- 614 (Equation 14, Base Model). To account for the potentially confounding effect of slider
- 615 movement on participants' submissions, we included initial slider position as a nuisance
- 616 regressors. We used fixed-effects terms for each variable and included random-effects terms for
- 617 each variable by participant (**Equation 14**).
- 618

# Equation 14

# $B \sim \beta_0 + \beta_{\Pr(C)} \Pr(C) + \beta_\theta \theta + \beta_W W + \beta_S S$

+  $(\beta_0 + \beta_{\Pr(C)} \Pr(C) + \beta_{\theta} \theta + \beta_W W + \beta_S S | \text{participant})$ 

To model bid in terms of expected information gain (EIG), we developed a *condensed model* in terms of probability gain and an *extended model* decomposing probability gain into its mathematical components of prior certainty and expected posterior certainty. To model bid in terms of probability gain, we included fixed-effects terms for the intercept, probability gain, penalty, the interaction between probability gain and penalty (as suggested by the product of probability gain and penalty in **Equation 13**), and initial slider position, along with the corresponding random-effects terms by participant (**Equation 15**).

626

 $B \sim \beta_0 + \beta_G G + \beta_W W + \beta_{GW} GW + \beta_S S + (\beta_0 + \beta_G G + \beta_W W + \beta_{GW} GW + \beta_S S | \text{participant})$ 627 For the extended model, we replaced probability gain with its mathematical components
628 (**Equation 16**), accounting for the possibility that a participant would not weight prior certainty
629 and expected posterior certainty with equal magnitude when estimating the EIG of a sample.

**Equation 15** 

# 630

## **Equation 16**

 $B \sim \beta_0 + \beta_{\Pr(C)} \Pr(C) + \beta_{\Pr(C)'} \Pr(C)' + \beta_W W + \beta_{W\Pr(C)} W \Pr(C) + \beta_{W\Pr(C)'} W \Pr(C)' + \beta_S S$ +  $(\beta_0 + \beta_{\Pr(C)} \Pr(C) + \beta_{\Pr(C)'} \Pr(C)' + \beta_W W + \beta_{W \Pr(C)} W \Pr(C) + \beta_{W \Pr(C)'} W \Pr(C)' + \beta_S S$  participant) 631 When we compared each participant's coefficient on prior certainty to the coefficient on 632 expected posterior certainty, we fit the extended model without z-scoring the predictors so that 633 any difference between the coefficients was not attributable to a difference in the predictors' 634 standard deviations. 635 fMRI Data Acquisition and Preprocessing 636 Acquisition Whole-brain fMRI data were acquired on a 3-T Siemens MAGNETOM Prisma scanner with a 637 638 64-channel head coil at the Magnetic Resonance Imaging Center at the Zuckerman Mind Brain 639 Behavior Institute of Columbia University. Functional images were acquired with a T2\*-640 weighted, two-dimensional gradient echo spiral in/out pulse sequence (repetition time (TR) =641 1,000 ms; echo time = 30 ms; flip angle =  $52^{\circ}$ , field of view = 230 mm;  $2.4 \times 2.4 \times 2.4$  mm voxels; 642 56 slices; multiband factor = 4). To reduce dropout in central frontal regions, slices were tilted by 643 10° forward from the AC-PC axis. During the scan session, the behavioral tasks were projected 644 onto a mirror attached to the scanner head coil for the participant to see (Hyperion MRI Digital 645 Projection System); participants made responses with the right hand through an MRI-compatible 646 trackball (Current Design). 647 Preprocessing 648 Preprocessing was performed using the *fMRIPrep* pipeline, Version 1.5.0rc1 (Esteban et al. 649 2019) (RRID:SCR\_016216). fMRIPrep uses a combination of tools from well-known software 650 packages, including FSL, ANTs, FreeSurfer, and AFNI, and is based on Nipype 1.2.0 651 (Gorgolewski et al. 2011) (RRID:SCR\_002502). For more details of the pipeline, see the section corresponding to workflows in *fMRIPrep*'s documentation at 652 653 (https://fmriprep.org/en/latest/workflows.html). 654 Anatomical data The T1-weighted (T1w) image was corrected for intensity nonuniformity with 655 N4BiasFieldCorrection (Tustison et al. 2010), distributed with ANTs 2.2.0 (Avants et al. 2008) 656 657 (RRID:SCR 004757). The T1w image was then skull-stripped with a *Nipype* implementation of 658 the antsBrainExtraction.sh workflow (from ANTs), using OASIS30ANTs as target template. 659 Brain tissue segmentation of cerebrospinal fluid, white matter, and gray matter was performed on

- the brain-extracted T1w using fast (Zhang, Brady, and Smith 2001) (FSL 5.0.9,
- 661 RRID:SCR 002823). Volume-based spatial normalization to Montreal Neurological Institute
- 662 (MNI) space (MNI152NLin2009cAsym) was performed through nonlinear registration with
- antsRegistration (ANTs 2.2.0) (Fonov et al. 2009) (RRID:SCR\_008796).
- 664 Functional data
- 665 A skull-stripped susceptibility distortion–corrected BOLD reference was generated using a
- 666 custom methodology of *fMRIPrep*. The BOLD reference was co-registered to the T1w reference
- using bbregister (FreeSurfer), which implements boundary-based registration using six degrees
- of freedom (Greve and Fischl 2009). Head-motion parameters (x, y, z, pitch, roll, and yaw) with
- 669 respect to the BOLD reference were estimated before spatiotemporal filtering using mcflirt (FSL
- 670 5.0.9) (Jenkinson et al. 2002). BOLD runs were slice-time corrected using 3dTshift from AFNI
- 671 20160207 (Cox and Hyde 1997) (RRID:SCR\_005927).

# fMRI Data Acquisition and Preprocessing

- 673 We used multi-voxel pattern analysis (MVPA) methods to identify regions in which the task
- 674 variables were decodable. To do so, first, we used a whole-brain univariate general linear model
- 675 (GLM) to estimate BOLD activation patterns (betas/parameter estimates) associated with each
- 676 task variable. Then, we trained and tested a support vector regression decoder on the voxel-wise
- 677 activation patterns that had been identified by the GLM. Univariate analyses were conducted
- 678 using the GLM framework implemented in SPM12, Version 7487
- 679 (https://www.fil.ion.ucl.ac.uk/spm), convolving boxcar functions within the GLM by the SPM
- 680 canonical hemodynamic response function. MVPA analyses were conducted using The
- 681 Decoding Toolbox (Hebart, Görgen, and Haynes 2015; Görgen and Hebart 2022). Whole-brain
- 682 statistical maps from functional data were overlaid on an average of the 23 participants'
- 683 individual T1-weighted (T1w) maps normalized to Montreal Neurological Institute (MNI) space.
- 684 Since scanning did not occur during the Payout Stage, fMRI activation was only measured
- 685 during the Bidding Stage.

672

- 686 Whole-Brain Analyses to Localize Clusters in Which a Task Variable Was Decodable
- 687 Functional images normalized to MNI space were smoothed with a Gaussian kernel with a
- 688 FWHM of  $5 \times 5 \times 5$  mm. Then, a condensed and an extended GLM was estimated for every
- 689 participant from this normalized, smoothed functional time series. Both GLMs used a variable-
- 690 epoch model (Grinband et al. 2008) using boxcar functions to represent each condition for each
- 691 task variable during the decision period (the period between the beginning of the response
- 692 window and the reaction time on trials that received a response, Figure 1A). The condensed
- 693 GLM contained conditions for probability gain, penalty, bid, and slider displacement (i.e., the
- 694 difference between the initial slider position and the slider position when the bid was submitted). 695 The extended GLM replaced the probability gain conditions with conditions for prior certainty
- 696 and expected posterior certainty. We fit these GLMs separately because probability gain is
- 697 collinear with expected posterior certainty and prior certainty (because probability gain is the
- 698 difference between the latter variables). The conditions for each variable were as follows,
- 699 vielding one parameter estimate per run (four per participant):
- 700 Probability gain: 0, 0.01–0.08, 0.09–0.17, 0.18–0.26, 0.27–0.35, 0.36–0.43 (nearly 701 equally spaced bins on the range of probability gains with a separate category for 0, 702 which was overrepresented)
- 703 • Prior certainty: low (0.5-0.53), medium (0.57-0.63), and high (0.87-0.93) (one for each 704 level of prior certainty, "Selection of parameters")
- 705 • Expected posterior certainty: low (0.57-0.63), medium (0.77-0.83), and high (0.87-0.93)706 (one for each level of expected posterior certainty) 707
  - Penalty: \$10 and \$20 (one for each penalty condition)
- 708 Bid: the bids discretized into 10 equally spaced bins over the available range (\$0 to 709 \$9.88)
- 710 • Slider displacement: the signed slider displacements discretized into 10 equally spaced 711 bins over the range of displacements during the scan session across all the participants
- 712 If the participant failed to respond to at least one trial during a run of the Bidding Stage, an
- 713 additional boxcar function was added to the GLM to model the entire response window for each
- 714 trial that they omitted. Finally, both GLMs also contained fixed-body motion-realignment
- 715 regressors (x, y, z, pitch, roll, and yaw) and their respective first derivatives.
- 716 In the next step, a decoding analysis was performed on the parameter estimates of the
- 717 GLM for each participant. A support vector regression was applied to each task variable of

718 interest, trained and tested on all the variable's conditions (across all the runs). Decoders were

- ross-validated using leave-one-run-out (four-fold) cross-validation. The label for each condition
- was the median value of the variable for the condition within the participant. The support vector
- regression was trained and tested on the same variable using a searchlight approach with a sphere
- of standard radius of 3 voxels (example: Kahnt et al. (2014)). Decoding accuracy for each voxel
- was measured as the Fisher's *z*-transformed correlation coefficient between the decoder's
   prediction and the true label for the variable. The searchlight analysis for probability gain used
- the condensed GLM. The searchlight analyses for prior certainty, expected posterior certainty,
- penalty, bid, and slider displacement used the extended GLM. Searchlight results were broadly
- similar for penalty, bid, and slider displacement between the two GLMs.
- Finally, we identified significant clusters in which each variable of interest was
- decodable by submitting each participant's accuracy map (across all brain voxels) for a variable
- to a second-level *T*-test, applying a cluster-wise correction for multiple comparisons using non-
- parametric permutation tests in SnPM13.1.08 (<u>http://nisox.org/Software/SnPM13/</u>) (Nichols and
- Holmes 2002), which have been shown to be most robust to false positives (Eklund, Nichols, and
- Knutsson 2016; Nichols et al. 2017). Permutation tests were based on a stringent cluster-forming height threshold of p < 0.001 and considered significant at a cluster-wise familywise error rate
- threshold of p < 0.05; we used 10,000 permutations (Holmes et al. 1996; Nichols and Holmes
- 736 2002).
- 737 Region of Interest (ROI) Analyses
- 738 Region-of-interest (ROI) decoding analyses were conducted on each significant cluster. ROI
- decoding was conducted the same way as the whole-brain decoding, except that the decoders
- 740 were trained on all the voxels within a cluster instead of a searchlight sphere, yielding one
- accuracy statistic per ROI. This was done whether the decoder was trained and tested on the
- same variable or trained on one variable and tested on another (cross-decoding). All ROI
- 743 decoding, including cross-decoding, was done with leave-one-run-out cross-validation. In all the
- expected posterior certainty (EPC) clusters, there was "substantial" evidence supporting the null
- hypothesis that cross-decoding accuracy of slider displacement from bid was not different from
- 746 chance (BF >  $10^{1/2}$ ).
- 747

# 748

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- 758

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