

Uncovering the important acoustic features for detecting vocal fold paralysis with explainable machine learning

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Abstract

Objective: To detect unilateral vocal fold paralysis (UVFP) from voice recordings using an explainable model of machine learning.

Study Design: Case series - retrospective with a control group.

Setting: Tertiary care laryngology practice between 2009 to 2019.

Methods: Patients with confirmed UVFP through endoscopic examination (N=77) and controls with normal voices matched for age and sex (N=77) were included. Two tasks were used to elicit voice samples: reading the Rainbow Passage and sustaining phonation of the vowel "a". The 88 extended Geneva Minimalistic Acoustic Parameter Set (eGeMAPS) features were extracted as inputs for four machine learning models of differing complexity. SHAP was used to identify important features.

Results: The median bootstrapped Area Under the Receiver Operating Characteristic Curve (ROC AUC) score ranged from 0.79 to 0.87 depending on model and task. After removing redundant features for explainability, the highest median ROC AUC score was 0.84 using only 13 features for the vowel task and 0.87 using 39 features for the reading task. The most important features included intensity measures, mean MFCC1, mean F1 amplitude and frequency, and shimmer variability depending on model and task.

Conclusion: Using the largest dataset studying UVFP to date, we achieve high performance from just a few seconds of voice recordings. Notably, we demonstrate that while similar categories of features related to vocal fold physiology were conserved across models, the models used different combinations of features and still achieved similar effect sizes. Machine learning thus provides a mechanism to detect UVFP and contextualize the accuracy relative to both model architecture and pathophysiology.

Keywords: vocal fold paralysis, acoustic analysis, voice, speech, biomarkers, explainability, interpretability, machine learning

INTRODUCTION

Voice recordings provide a rich source of information related to vocal tract physiology and human physical and mental health. Given advances in smartphones and wearables, these recordings can be made anytime and anywhere. Thus, the search for disorder-specific acoustic biomarkers has been gaining momentum. Voice biomarkers have been reported for detecting Parkinson's diseases¹ as well as psychiatric disorders including depression, schizophrenia, and bipolar disorder (for a systematic review, see Low et al, 2020²). Given our scientific understanding of the complexity of speech production, multiple acoustic features have been devised for use in machine learning models (see Figure 1 for a schematic of speech production subsystems and acoustic features used in machine learning models; see also Quatieri, 2008³). Despite these advances, robust applications to detect vocal fold paralysis disorders remain limited⁴⁻⁹ (see Supplementary Table S1 for a summary of prior machine learning studies).

Furthermore, complex machine learning can be successful, but they are often treated as "black-boxes" because it can be difficult to determine with precision how the model is making a decision, that is, how it is combining input features for a given patient to output a prediction. This is particularly worrisome given machine learning algorithms can detect and associate unintended or clinically irrelevant relationships and introduce bias that may be difficult to anticipate. Explainable machine learning refers to a series of methods and quantitative analyses for uncovering and "explaining" the rationale behind the decision made by complex algorithms, which is particularly critical in the high-stake decisions of medicine to increase trust among clinicians and patients¹⁰.

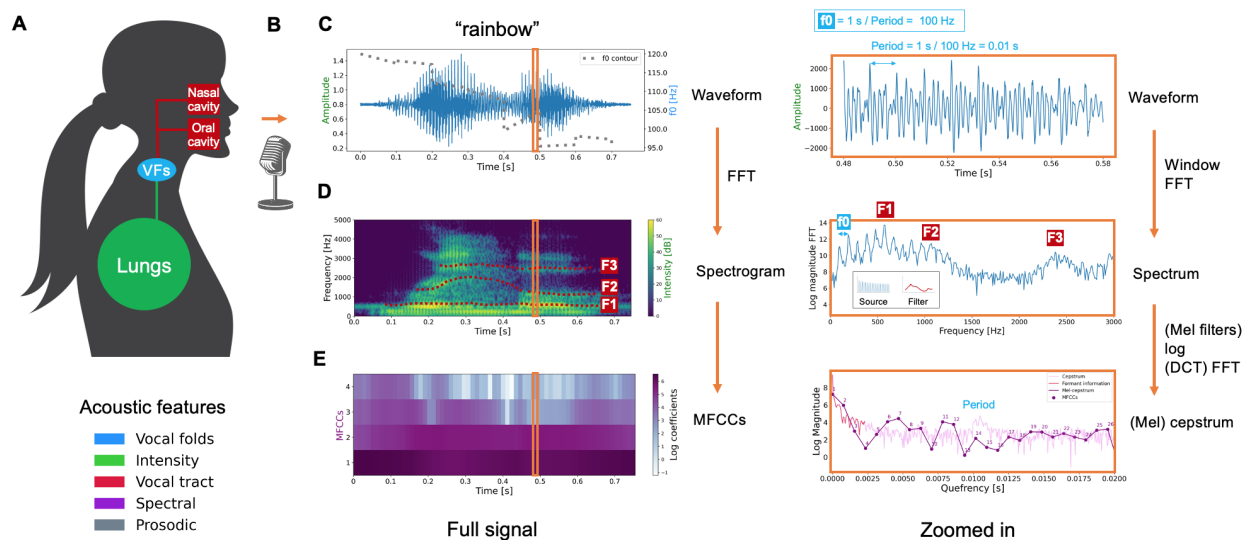


Figure 1. Schematic of speech production and the process of extracting certain acoustic features from an audio signal. (A) Speech is a result of the neural coordination of three subsystems: the respiratory system (lungs), the laryngeal system (vocal folds), and the resonatory system of the vocal tract (pharynx, oral cavity, nasal cavity, articulators, and subglottal effects). Speech production requires air flow from the lungs to generate sound sources that are filtered by the vocal tract. (B) Environmental, microphone, and digital sampling characteristics (e.g., background noise, microphone gain, sampling rate) can affect acoustic features. (C) Waveform of the audio signal, which is the 2D representation of the contraction (positive amplitude) and rarefaction (negative amplitude) of air particles. Higher amplitudes can lead to higher perceived loudness. Prosodic features arise from changes over longer segments of time, which is perceived in the rhythm, stress, and intonation of speech. A segment of the waveform is shown in the right panel, indicating a periodic signal from the vocal folds. (D) For a given time window, a spectrum (right panel) can be obtained through a Fast Fourier Transform (FFT) which represents the magnitude of the frequencies in the signal with peaks (formants F1–F3) due to vocal tract filtering of the source signal produced by the vocal folds. The spectrogram (left panel) is a representation of the spectrum as it varies over time. The approximate location of the F0 and first formants are displayed. (E) To separate source and filter components one can compute the inverse FFT of the log of the magnitude of the spectrum, called the cepstrum (right panel). The peak in the cepstrum reflects the periodic glottal fold vibration while lower quefrequency components reflect properties of the resonatory subsystem. For speech recognition, Mel filters are applied to the spectrum to better approximate human hearing. A conversion of the Mel-spectrum to a cepstrum using a Discrete Cosine Transform (DCT) generates mel-frequency cepstral coefficients (MFCCs). Similar to the cepstrum, lower MFCCs track vocal-tract filter information.

There are many challenges for applying acoustic analysis to detect specific disorders. Voice characteristics are highly varied and change over time. Laryngeal pathology, age, gender, size,

weight, general state of health, smoking/vaping, and medications can impact vocal acoustic characteristics. Diseases in the larynx and phonatory system (i.e., larynx, resonating structures, lungs) and/or neurological system, will also affect voice. Patient compensation and environmental conditions can also change the vocal signal. Furthermore, because hoarseness is such a frequent occurrence and specialty voice centers are rare, vocal fold disorders are often undiagnosed, under-reported, or misdiagnosed¹¹.

Unilateral vocal fold paralysis (UVFP) is an ideal model for demonstrating the explainability of machine learning for several reasons. UVFP occurs when the mobility of a single vocal fold is impaired as a consequence of neurological injury and diagnosis is consistently verified through routine laryngoscopy; therefore, ground truth labels can be obtained. Second, the clinical signs of UVFP are well-described and acknowledged. These characteristics include a weak, breathy voice quality, early vocal fatigue, reduced cough strength, and aspiration with thin liquids^{12,13}. Therefore, the expected acoustic differences between UVFP patients and healthy controls can be interpreted with regards to perceptual symptoms and a well-understood pathophysiology. In contrast, explaining important variables to predict a disorder which is hard to diagnose (e.g., has low inter-rater reliability) and has an unclear pathophysiology would ironically result in a poor explanation, because it would be puzzling how or even if the disorder could modulate the important acoustic variables.

We also chose to examine UVFP because it is clinically important. Vocal fold paralysis may occur due to iatrogenic injury, malignancy, idiopathic, and neurological disease, and impacts quality of life. Overall, surgical iatrogenic injury accounts for 46% of all UVFP in adults and thyroid and parathyroid surgeries are responsible for 32% of postsurgical UVFP¹⁴. There is a significant need for a screening tool for the diagnosis and tracking of UVFP because of the high

impact of this condition on productivity and quality of life. Screening could be done remotely and frequently, especially when surgical specialists and laryngeal exams are not readily accessible due to geographical, financial, and other barriers¹⁵. Using an explainable machine learning model as a screening tool for UVFP can provide greater clarity as to who most needs laryngoscopy and provides insight in the key voice characteristics related to the pathophysiology^{16–20}.

The objectives of our study were: (1) to detect UVFP using machine learning; (2) to evaluate the effectiveness of different models in differentiating the acoustic signals between patients with UVFP and patients with normal functioning vocal folds (i.e., controls); and (3) to explain which features are most important to the diagnostic models and examine the pathophysiological relevance. To achieve these objectives, we evaluated statistical dependencies across voice features in the data, used four different classes of machine learning algorithms to assess classification performance, evaluated the minimal set of features necessary for detection, and identified the most important features for model construction. Ultimately, we wanted to see if the most important features identified by the machine learning models matched clinically-known relevant acoustic changes.

MATERIALS AND METHODS

This study was approved by the Institutional Review Board at Massachusetts Eye and Ear Infirmary and Partners Healthcare (IRB 2019002711).

Participants and voice samples

Through retrospective chart analysis from 2009 to 2019, a total of 1043 patient charts were reviewed from a tertiary care laryngology practice who underwent endoscopic evaluation and voice testing. Of those, 53 patients with confirmed UVFP were identified. They had documented vocal fold paralysis by endoscopic examination and had undergone acoustic analysis as part of routine clinical care. Each patient had four acoustic recordings. These included three sustained vocalizations of the "a" vowel sound (ɑ in the International Phonetic Alphabet) and a reading of the introductory paragraph of the rainbow passage²¹. The acoustic recordings were all taken in an acoustically shielded room. For each of these 53 patients, a board-certified otolaryngologist reviewed their clinical history, video laryngoscopy as well as their audio samples to confirm that they were correctly classified to have UVFP. A separate 24 samples were collected prospectively using a mobile software, OperaVOX™ on an iPad from patients who were currently being treated for UVFP. These patients also had the same four acoustic recordings as the patients from retrospective chart review. This combination of data collection yielded a total of 77 UVFP patients for analysis, of which 48 had left UVFP and 29 right UVFP.

All of the patients were then matched with control samples from a database of patients without UVFP who had also undergone acoustic analysis. Each control was the same sex and had the same smoking status as the UVFP patient and within three years of age, and had documented laryngeal examinations that verified the absence of vocal fold mucosal pathology. The controls were excluded if they had established laryngeal surgery, vocal fold lesions, radiation, head and neck cancer, or neurological disease. The controls had recorded the same four vocal files as the retrospectively gathered UVFP group. A board-certified otolaryngologist confirmed that the voice recordings and video laryngoscopies of these controls matched normal expectancies.

The reading samples were divided in thirds to match the amount of vowel production samples. Reading recordings were not available for three patients and three patient vowel samples were removed due to containing multiple vowel productions or a cough. The final dataset that was analyzed is described in Table 1. Reading+vowel refers to including all samples (i.e., ~6 samples) from the same participant with the goal of either obtaining higher performance or discovering features that show variation in relation to diagnosis consistently across tasks. Mean (SD) audio lengths were 6.81s (5.47) for reading samples and 3.95s (1.00) for vowel samples. The audio samples were processed using OpenSmile with the eGeMAPS configuration file (article²², source code²³) which applies different summarization statistics to the time series depending on the feature resulting in 88 features per sample covering information related to the vocal folds (F0, jitter, shimmer), intensity (loudness, HNR), vocal tract (F1–3 frequency, bandwidth, amplitude), spectral balance (alpha ratio, Hammamberg index, spectral slope, MFCC 1–4, spectral flux), and prosody (voice and unvoiced segments, loudness peaks per second).

	UVFP	Controls	Total
N	77	77	154
Mean age (SD)	56.4 (18.7)	56.6 (18.8)	56.5 (18.7)
Sex (F/M)	39/38	39/38	78/76
Reading	222	231	453
Vowel	227	231	458
Reading+vowel (total)	449	462	911

Table 1. Sample sizes and demographic information. SD: standard deviation; F: female; M: male.

Machine Learning Models of Increasing Complexity

With the goal of classifying voices recording into either UVFP or controls, we used four machine learning algorithms of increasing complexity from the *scikit-learn* using the *pydra-ml* toolbox²⁴ (default parameters were used unless otherwise specified):

(1) Logistic Regression: a simple linear model that is constrained to use few features due to an L1 penalty making it the simplest model (“liblinear” solver was used which is ideal for smaller datasets).

(2) Stochastic Gradient Descent (SGD) Classifier: it is also a linear model but tends to use more features due to an elastic net penalty that was chosen making it slightly more complex (the `max_iter` parameter was set to 5000 and `early_stopping` was set to True).

(3) Random Forest: it is an algorithm that uses simpler decision trees (i.e., weak learners) on feature subsets but then averages the trees' predictions to create a stronger learner, making it harder to interpret which features are important across trees.

(4) Multi-Layer Perceptron: it is a neural network classifier which incorporates, in our case, 100 instances of perceptrons (artificial neurons), which are connected to each input feature through weights with an added nonlinear activation function to capture nonlinear structures in the data. It is not possible to know exactly how the hundreds of internal weights interact to determine feature importance, making the model difficult to interpret directly from its parameters (the `max_iter` parameter was set to 1000; `alpha` or the L2 penalty parameter was set to 1).

To generate independent test and train data splits, a bootstrapped group shuffle split sampling scheme was used. For each iteration of bootstrapping, a random selection of 20% of the participants was used to create a held-out test set. The remaining 80% of participants were used for training. This process was repeated 50 times, and the four classifiers were fitted and tested for each test/train split. The Area Under the Receiver Operating Characteristic Curve (ROC AUC; perfect classification = 1; chance = 0.5) was computed to evaluate the performance of the models on each iteration, resulting in a distribution of 50 ROC AUC scores for each classifier. For each iteration, each classifier was trained with randomized patient/control labelings to generate a null distribution of ROC AUC scores (i.e., a permutation test). Each model's performance was statistically compared to other models and to the null distributions using an empirical p-value, a common and effective measure for evaluating classifier performance (see Definition 1 in Ojala & Garriga, 2010²⁵).

Assessing feature importance

Kernel SHAP (SHapley Additive exPlanations) was used to determine which acoustic features were most important for each model to detect UVFP. This method is model agnostic in that it can take any trained target model (even “black box” neural networks) and compute feature importance²⁶. It does so by performing regression with L1 penalty between different sets of input features and a single prediction made by the target model. It then uses the coefficients of the additional regression model as a measure of feature importance for a single prediction. We took the average of the absolute SHAP values across all test predictions (positive and negative values are both important for classification). We then weighted the average values by the model’s median performance since an important feature for a bad model could be a less important feature for a good model and vice versa. Since we trained each model 50 times (i.e., one for each bootstrapping split), we computed the mean SHAP values across splits for each model. This pipeline (i.e., machine learning models, bootstrapping scheme, SHAP analysis) was done using the *pydra-ml* package.

Reducing redundant features for more explainable models

Highly correlated features can influence model generation and interpretation. Two models may obtain similar performance while using different features or placing different weights on the same features. This makes it difficult to compare algorithmic explanations across models. For instance, mean F1 frequency may be less important to a given model because the model uses mean F2 frequency which happens to capture very similar information in a particular dataset, whereas a different model may use F1 instead of F2 or use both but assign less importance to each. To enforce models to use the same features that capture very similar information and be

able to compare feature importance across models, we kept a single feature out of the sets of features that share similar information above a given threshold. We used a custom algorithm we call Independence Factor (see "Reducing redundant features for more explainable models" section in Supplementary Materials).

RESULTS

Performance with and without redundant features

Given dependent features provide similar information and distort feature importance analyses, we then tested performance after removing redundant features using the Independence Factor method previously described. Supplementary Figure S10 shows performance for different feature set sizes with increasing amounts of redundant features. From this analysis, we selected the feature-set size that resulted in best performance using the least amount of features for subsequent analyses: 39 features (reading), 13 (vowel), 19 (reading+vowel). By removing redundant features (i.e., reducing multicollinearity) from the original 88 features, similar performance was obtained (median ROC AUC = 0.84–0.87) using fewer features.

Supplementary Materials "Feature selection" section describes an analysis of how this method compares to removing features across each train set.

Performance was found to be high across most models both with and without redundant features. The bootstrapped ROC AUC distributions and permutation tests for the reduced (parsimonious) models are shown in Figure 2. Table 2 shows performance using all features

and a subset of features selected by either removing redundant features while maintaining performance (as in Supplementary Figure S10) or using the top 5 most important features.

Studies tend to report and describe the top N features, but it is not clear what performance the model would obtain for those features when used alone since measurement is usually based on models that use additional features with multiple interactions. In contrast, in our study we ran models on the top 5 features together (Table 2), which allowed us to actually demonstrate their predictive capability. The lower performance of these top 5 features relative to a richer feature set helps demonstrate that model performance is dependent on interactions across multiple features. We also ran models without top 5 features to demonstrate that leaving features that are redundant with these top features results in almost equivalent high performance to using all 88 features since the redundant features share information. Given a subset of the UVFP patients were recorded with a different device, we discarded that this could have introduced bias (see analysis in Supplementary section "Performance removing participants that used other recording system").

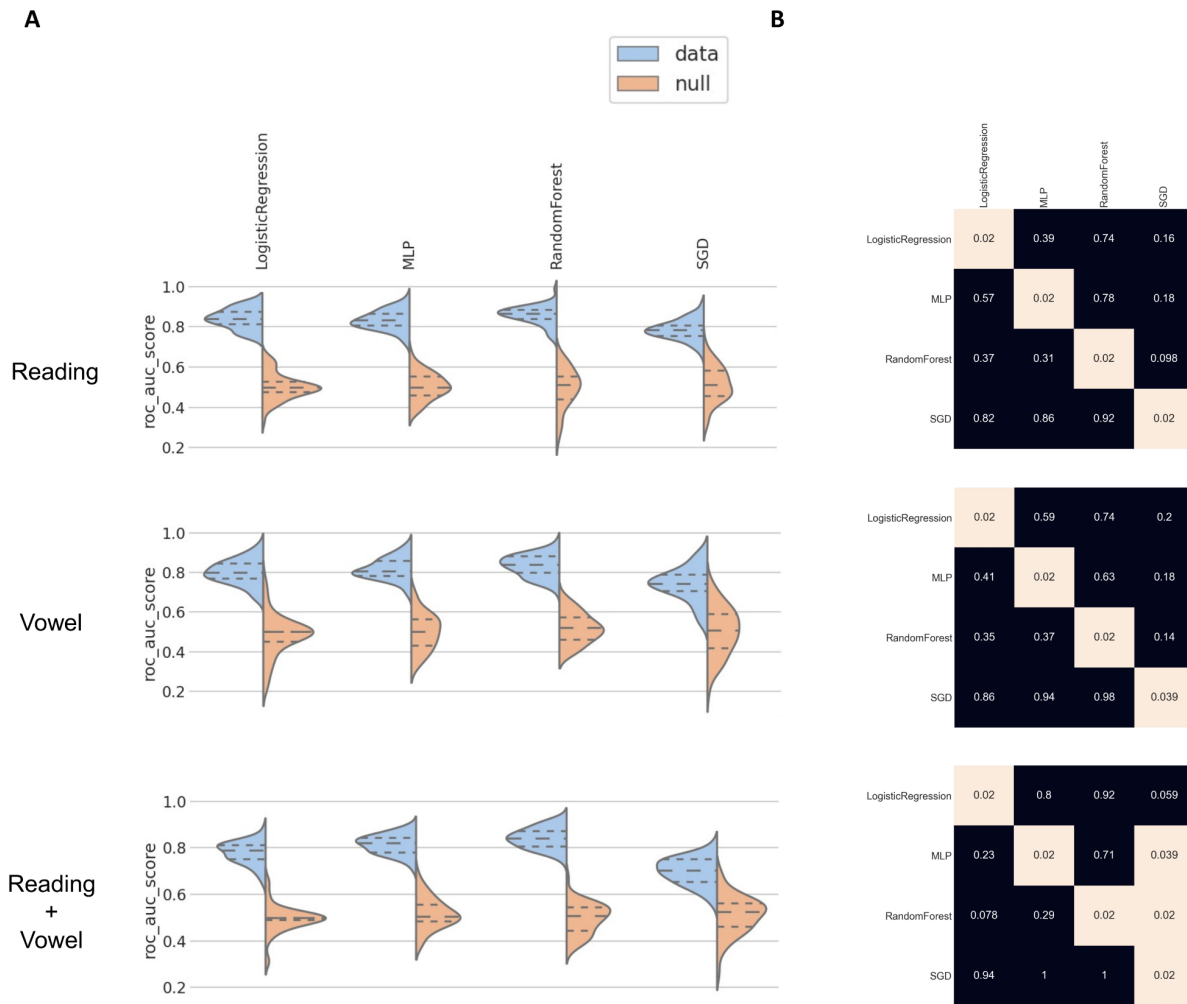


Figure 2. Model performance comparison using non-redundant feature sets. (A) The distribution of scores from models trained on true labels (blue, i.e., data model) and trained on permuted labels (orange, i.e., null model) over 50 bootstrapping splits. **(B)** One tailed statistical comparison (row > column) of models using an empirical p-value, which represents the fraction of column-model scores where the row-model classifier had a higher mean performance (e.g., a p-value of 0.02 indicates that the mean score of a row model is higher than 98% of column-model scores). The diagonal represents a comparison of the model with a null model trained on randomly-shuffled labels. The results that were significant as compared to the alpha value of 0.05 are highlighted.

	Features	LogisticRegression	MLP	RandomForest	SGD
Reading	88	.87 (.78–.93; .50)	.87 (.80–.93; .50)	.87 (.76–.91; .49)	.83 (.76–.89; .50)
Vowel	88	.84 (.77–.89; .50)	.86 (.79–.91; .50)	.86 (.79–.91; .51)	.80 (.72–.87; .50)
Reading+Vowel	88	.84 (.76–.91; .50)	.86 (.74–.92; .48)	.85 (.77–.92; .49)	.79 (.72–.86; .51)
Reading	39	.84 (.76–.92; .50)	.83 (.76–.91; .50)	.87 (.77–.91; .51)	.78 (.71–.86; .51)
Vowel	13	.80 (.70–.90; .50)	.81 (.74–.91; .50)	.84 (.75–.90; .52)	.74 (.58–.87; .51)
Reading+Vowel	19	.79 (.70–.84; .50)	.82 (.75–.88; .51)	.84 (.77–.91; .51)	.70 (.61–.77; .52)
Reading	Top 5	.81 (.73–.89; .50)	.86 (.78–.92; .47)	.85 (.77–.90; .50)	.75 (.56–.87; .57)
Vowel	Top 5	.78 (.67–.87; .50)	.82 (.74–.92; .53)	.81 (.72–.87; .50)	.72 (.57–.82; .49)
Reading+Vowel	Top 5	.80 (.70–.86; .50)	.82 (.74–.88; .50)	.81 (.74–.89; .53)	.72 (.55–.83; .52)
Reading	88 - Top 5	.85 (.76–.92; .50)	.87 (.77–.92; .49)	.85 (.77–.90; .52)	.82 (.71–.89; .51)
Vowel	88 - Top 5	.84 (.75–.93; .50)	.86 (.72–.93; .51)	.84 (.74–.94; .52)	.80 (.70–.90; .48)
Reading+Vowel	88 - Top 5	.84 (.74–.89; .50)	.85 (.76–.91; .50)	.85 (.76–.91; .50)	.79 (.71–.87; .50)

Table 2. Model performance. Performance of models using either all 88 features, non-redundant features (39, 13, 19), top five most important features, and all 88 features minus top 5 most important features. Median ROC AUC score from 50 bootstrapping splits (90% confidence interval; median score of null model). For full distributions of scores see Figure S10 in Supplementary Materials. Removing features is a post-hoc analysis because features were selected based on observing performance on the test sets, and therefore performance might be slightly overly optimistic and would need to be tested on an independent test set for further validation. MLP: Multi-Layer Perceptron; SGD: Stochastic Gradient Descent Classifier.

Assessing feature importance

Figure 3 reports feature importance using SHAP for all models. For further description of features and the chosen classification of features, see Eyben et al. (2015)²² and Low et al. (2020)². To understand the role of the most important features we ran a post-hoc analysis with the top 5 features for each data type (reading, vowel, reading+vowel), performance is shown in Table 2 and we further display the distribution of each top feature and its individual performance

in Figure 4. Figure 5 reports similarity between top 5 features and all original 88 eGeMAPS features.

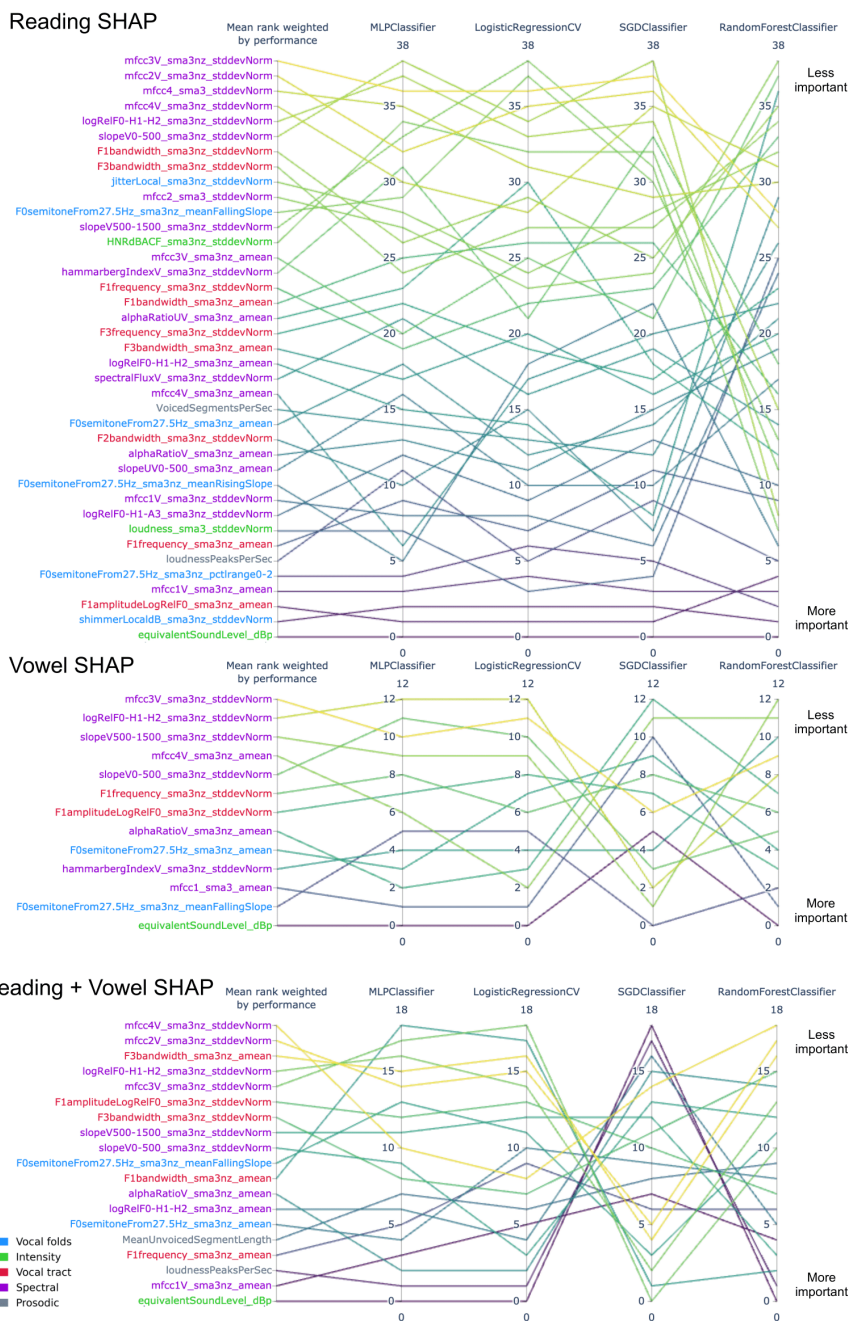


Figure 3. Feature importance parallel coordinate plot. Rank reads from bottom (most important) to top (least important). Mean rank is weighted by performance of each model to avoid a lower performing model biasing the mean rank. When reviewing important features, it is key to note that any of the features with which it is codependent could be a reasonable important feature (see Supplementary Figures S1-S9).

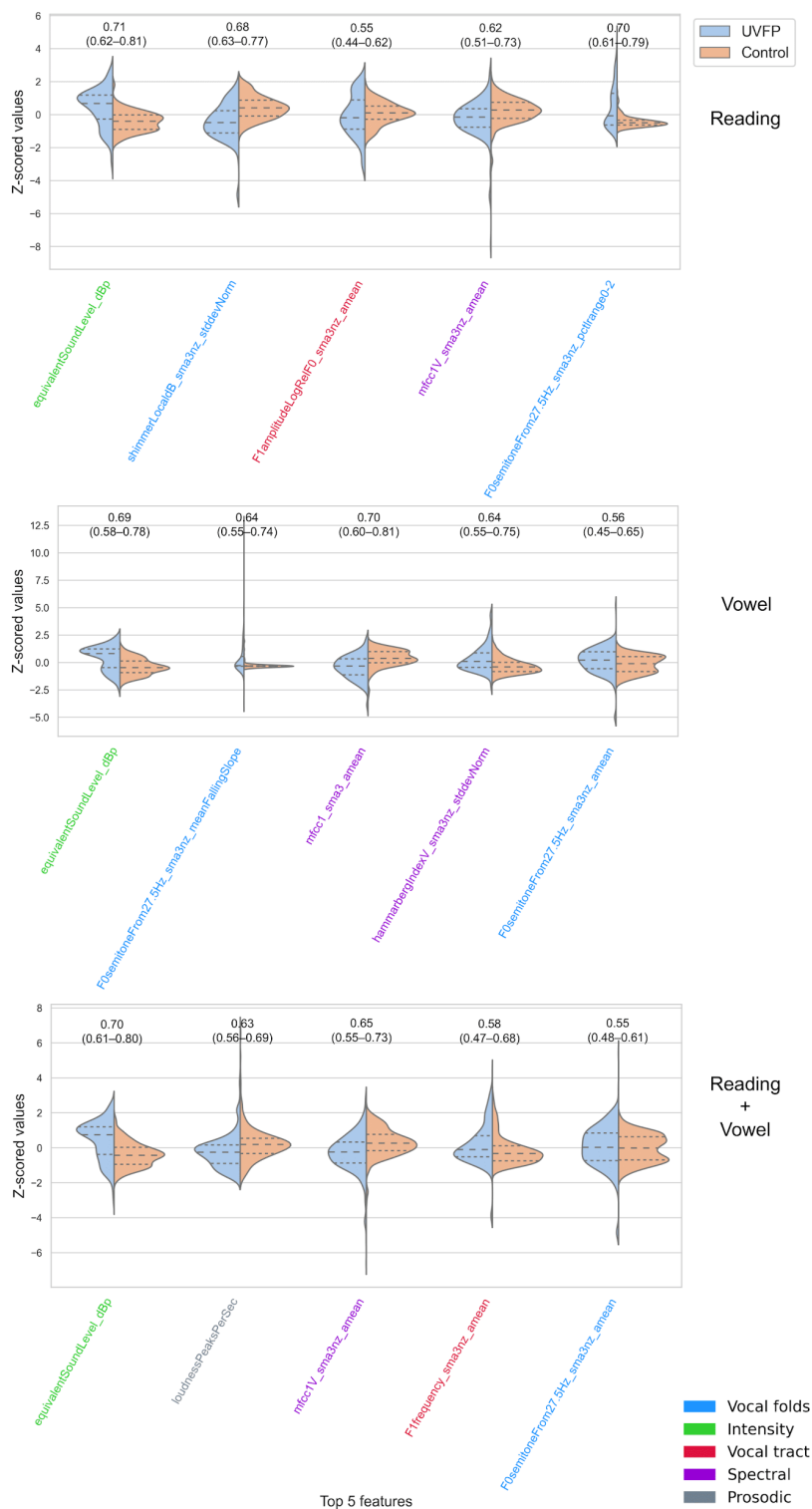


Figure 4. Distributions for top 5 features and corresponding performance for single features using a Logistic Regression with L1 penalty. No single feature is enough to dissociate groups with high performance; high performance is obtained by combining more features as in Figure 2. The median performance of all null models was 0.5.

Figure 5. Feature redundancy with top 5 features highlighted. Top 5 features are highlighted in bold and their rank is displayed before the feature name with the corresponding leaf marked with an "x". Features that have a high distance correlation (i.e., cluster) with top 5 features were not used in models to avoid redundancy, but still share similar information and can therefore be considered important features as well. Squares are clusters of redundant features. Computed with all participants on the reading task. Supplementary Figures S1 to S9 display hierarchically-clustered heatmap for other data types (vowel, reading, both) and groups (UVFP patients, controls, both).

Discussion

This study achieves high performance in dissociating UVFP from healthy voices which could have several clinical applications: (1) postoperative screening for thyroid surgery-related UVFP since after thyroid surgery, UVFP is common, occurring in up to 5 to 10% of cases²⁷.

Furthermore, laryngeal exam is not readily available to all postoperative populations and symptomatic changes are notoriously variable. A machine learning screening could help identify patients needing laryngoscopy and further workup and treatment, and earlier diagnosis is essential to optimize long-term outcomes^{28,29}. (2) Monitoring voice during speech therapy and after surgical treatment for confirmed UVFP to measure when and if the patient's voice is approximating a healthy voice. (3) Preoperative screening prior to surgeries that are at high risk for developing UVFP such as thyroid, head and neck, cardiac, thoracic, esophageal, and cervical spine operations.

We achieve robust classification performance and associate this performance with relevant acoustic features. Critically, we demonstrate that interpreting performance accuracy has to be contextualized with respect to the type of the machine learning model used and the voice-eliciting task.

The need for automated assessments of vocal fold paralysis

We chose vocal fold paralysis as the study cohort for several reasons. The acoustic changes associated with vocal fold paralysis are relatively reliable and consistent. Application of objective acoustic measurements towards differentiating between voice conditions have been limited⁴⁻⁹ (see Supplementary Table S1 for a summary of prior machine learning studies). Our study expands on prior studies which have used pre-existing commercial databases, smaller sample sizes, fewer features, and/or methods for model evaluation that can be biased in small datasets given the test sets may not be representative (for a discussion on bootstrapping for clinical datasets, see 5²). As a clinical entity, UVFP can have detrimental effects on voice, vocation, and quality of life, with resultant morbidity related to respiration, swallowing and aspiration. The costs associated with UVFP not only relate to patient morbidity and diminished quality of life but also to the economic burden placed on our healthcare system. Greater lengths of hospitalization and increased hospital costs have been associated with postsurgical VFP^{27,30}. Access to specialists for diagnosis is limited and early detection and management of UVFP appear to improve length of stay and surgical outcomes³¹.

Explaining acoustic features relevant to detecting vocal fold paralysis

Objective acoustic measurement changes associated with vocal fold paralysis have been described and these changes include reduced loudness and maximum phonation time, higher perturbation measurements such as jitter and shimmer, and increased signal to noise ratio^{13,32,33};

however these were univariate models, and we have demonstrated that using single variables does not seem to provide high predictive performance. While other multivariate machine learning models have been used (see Supplementary Table S1), these used few features and small or undefined samples and only report feature importance results for one model; therefore it is not clear whether the important features reported would hold using larger feature sets or how other models would perform. Using a much larger initial set of acoustic features for analysis, we demonstrate that several machine learning algorithms of increasing complexity (using more parameters) successfully identify vocal fold paralysis from healthy voices. We also report that these models can use different features to achieve similar performance. Different models emphasize different features not simply because of its relevance to a disorder, but because of the mathematics associated with the model^{34,35}. The variability of the ranking of features used by our individual models also illustrates the potential danger of using the single highest performing model, which is commonly seen in published literature.

Instead of reporting the important features from the highest performing model, we analyzed the models to find common features. Some of the most important features across models were: intensity (especially equivalent sound pressure level which was redundant with multiple loudness features and seems to be due to some patients trying to use more breath for projection), Mel Frequency Cepstral Coefficients (especially the first coefficient, which captures spectral envelope or slope), mean F0 semitones (given F0 originates from vocal-fold oscillation, a vocal-fold paralysis is expected to alter F0), mean F1 amplitude and frequency (influenced by how the vocal tract filters F0 and the shape of the glottal pulse which would be affected by UVFP), and voiced and unvoiced segments (prosodic and speech articulation features which may be altered due to changes in the periodicity of F0). Shimmer variability was important just for reading, and it captures variability in glottal pulses and pressure patterns which ultimately

affect F0. When we removed these top 5 features from the full feature set, performance is practically equivalent to using 88 features, as expected, since there are features that are redundant with these top 5 features. Therefore, it is not that only these 5 specific features drive performance, but rather the information they contain, which in this dataset is also captured by other features as shown in Figure 5.

These acoustic features corroborate our clinical understanding of glottal incompetence from UVFP and with common patient complaints of reduced loudness, vocal instability, hoarseness, and rough voice. Uncovering and understanding the basic mechanisms and features that models use to generate predictions and outcomes are important as these tools become part of the clinical decision making process.

Comparing tasks, model complexity, and feature set sizes

In addition to getting a better understanding of features, we explored performance in the context of different vocal tasks. Participants carried out two different tasks to elicit voice, *reading*, which captures more complex speech dynamics, and *sustaining vowels*, which is a simpler measure of vocalization and the respiratory subsystem. Overall, these dynamics from the speech task may have improved model performance as was observed. Comparing simpler and more complex models is important because simpler models such as Logistic Regression could be preferred because they tend to generalize better given they are less at risk for overfitting the training set and they are more interpretable and thus biases can be assessed more directly³⁶.

By removing redundant features, we can concentrate on finding the most useful features for further analysis. Performance decreased only slightly while we made models more parsimonious and explainable. Performance using the top 5 features dropped performance in most cases, with the exception of samples from the reading task which obtained an AUC of 0.85 using just the 5 features (see Figure 4). Using the individual features from within these top 5 one at a time (univariate models) reduced performance significantly to 0.55-0.71. This indicates the need for these models to combine multiple features to achieve high performance and any model evaluation should not focus on only the common or top features without testing their predictive performance.

Limitations and future directions

While it is not clear these models could detect UVFP from other voice disorders, these models could be used to monitor UVFP patients remotely and affordably during treatment or detect risk for UVFP when it is the most likely cause (e.g., dysphonia after thyroid surgery). Larger sample sizes with curated examinations can help increase diverse representation across voice quality and thereby potentially reduce bias in classifier performance. Additional datasets will also help confirm the generalizability of these findings beyond the cross-validation approach used here. Our choice of a standardized feature set worked well in this setting, but may fail to work for differential voice disorder diagnosis or when generalizing to larger datasets, which may bring in additional sources of variance unaccounted for in this dataset. With the availability of more data, additional features could be extracted that better capture changes in coordination (e.g., XCORR³⁷) or vocal fold characteristics (e.g., cepstral peak prominence³⁸). While our feature importance evaluation method, SHAP, shows a certain amount of robustness across models, alternative model-agnostic feature-importance methods (e.g., LIME, permutation importance) as

well as model-specific methods (coefficient values for linear models, mean decrease in impurity for Random Forest) could be compared.

Conclusion

Using the largest dataset to date, our study demonstrates the feasibility and value of testing multiple machine learning algorithms on data obtained from different voice tasks to better understand the process that models use to predict vocal changes associated with laryngeal disease. However, deciphering how these models work, being able to understand strengths and weaknesses of different algorithms, and making sure the training sets are representative of the intended uses are all aspects of machine learning that clinicians need to understand prior to application. We believe that establishing reliable machine learning tools should involve using expertly-curated clinical data, identifying appropriate methods for feature extraction and performance evaluation (e.g., bootstrapping), explaining feature importance which may require understanding redundancy across features (i.e., addressing multicollinearity), and applying multiple models of varying complexity to understand how much feature importance can vary to then make inferences from the features that are important *across* models. With these considerations, machine learning applications can aid in vocal fold paralysis diagnosis, allowing for the potential development of in-home screening assessments and continuous pre- and post-treatment monitoring.

Data availability statement

All data and code are available through Github (<https://github.com/danielmlow/vfp>) and Zenodo (<https://doi.org/10.5281/zenodo.5009208>).

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Supplementary Materials

Introduction

Table S1 lists prior studies and potential limitations¹⁻⁶. Our study expands on prior studies which have used pre-existing commercial databases, smaller sample sizes of UVFP patients, fewer features and models, and/or methods for model evaluation that can be biased in small datasets given the test sets or folds tend to not be representative of the dataset (for a discussion, see recommendation about bootstrapping in clinical datasets⁷).

Study	N	Findings	Potential limitations
Schönweiler et al. (2000). <i>JARO</i> . ¹	112	Accuracy = 65-85% (50-50 train-test split)	Does not specify disorders nor performance per disorder
Godino-Llorente et al. (2004). <i>IEEE Trans Biomed Eng.</i> ²	8 paralysis, 7 paresis (MEEI)	Sensitivity = 95.7%; specificity = 95.9% (70-30 train-test split)	Small N for UVFP; Does not specify performance per disorder
Fraille et al. (2009). <i>Folia Phoniatr Logop.</i> ³	173; does not specify disorders (MEEI)	Mean error = 11.7% (70-30 train-test split)	Does not specify disorders nor performance per disorder
Voigt et al. (2010). <i>Comput Methods Programs Biomed.</i> ⁴	30 (vocal fold paresis)	Mean accuracy = 93% (10-fold CV x 3 initializations)	Small N
Lopes et al (2017). <i>J. Voice.</i> ⁵	257 participants of which 64 have a healthy larynx and 10 have UVFP	Mean accuracy = 79.8% (10-fold CV); Important features: SD F0 and jitter	Small sample of UVFP patients; used only 5 acoustic variables features (SD f0, mean f0, jitter, shimmer, glottal to noise excitation); tested a single model (quadratic discriminant analysis)
Powell et al (2019). <i>Laryng. Inv. Otolaryngol.</i> ⁶	10 (UVFP)	Mean accuracy = 87% (10-fold CV)	Small N; used spectrogram, harder to interpret

Table S1. Prior studies on voice disorders.

N: sample size; MEEI: Kay Electronics Mass. Eye and Ear Infirmary (MEEI) CD-ROM dataset; UVFP: Unilateral Vocal Fold Paralysis; SD: standard deviation; f0: fundamental frequency.

Methods

Reducing redundant features for more explainable models

A post hoc analysis of the smallest sets of features driving a prediction model can be a useful approach to identify clinically meaningful information. We used a custom algorithm we call Independence Factor whereby for each feature in alphabetical (i.e., arbitrary) order, we removed features that show strong dependence above a given threshold. The step was repeated for remaining features. We used distance correlation through the Python *dcor* package to capture linear and nonlinear relationships⁸. We used the following threshold values for the distance correlation [1.0, 0.9, 0.8, 0.7, 0.6, 0.5, 0.4, 0.3, 0.2] to compute the Independence Factor, which removed increasingly more features (i.e., 1.0 keeps all features and 0.2 removes features that have a distance correlation above 0.2). We chose the feature size which contains at least one model that scores within three percentage points of the performance using all features, with the goal of obtaining a more parsimonious model for subsequent explanation while maintaining high accuracy. Thus, removing redundant features makes the models easier to interpret for clinical relevance. To visualize the original redundancy across features, we computed clustermaps using *seaborn* package performing hierarchical clustering with the average-linkage method and Euclidean distance. This was performed on the pairwise distance correlation, computed separately on data from UVFP, controls, UVFP+controls and on reading, vowel, and reading+vowel.

RESULTS

Visualization of Redundant Features

See Figure S1–S9 for a visualization of redundant features for all participants, patients, and controls and for reading, vowel, and reading+vowel tasks. Top 5 features are highlighted in bold and their rank is displayed before the feature name with the corresponding leaf marked with an "x". When stratifying samples by disorder and task, clustering becomes more homogenous (clusters tend to contain a single feature type) in comparison to when all participants or both tasks are included as in Figure S3. Even in Figure S3, the chosen color-coded classification of features appears to be empirically replicated in this dataset given most low-level clusters (i.e., have higher dependency) are for the most part homogenous (i.e., of the same color). This also allows us to observe exceptions (e.g., mean spectral flux clusters with loudness features) which could otherwise be missed if using only a priori theoretical knowledge.

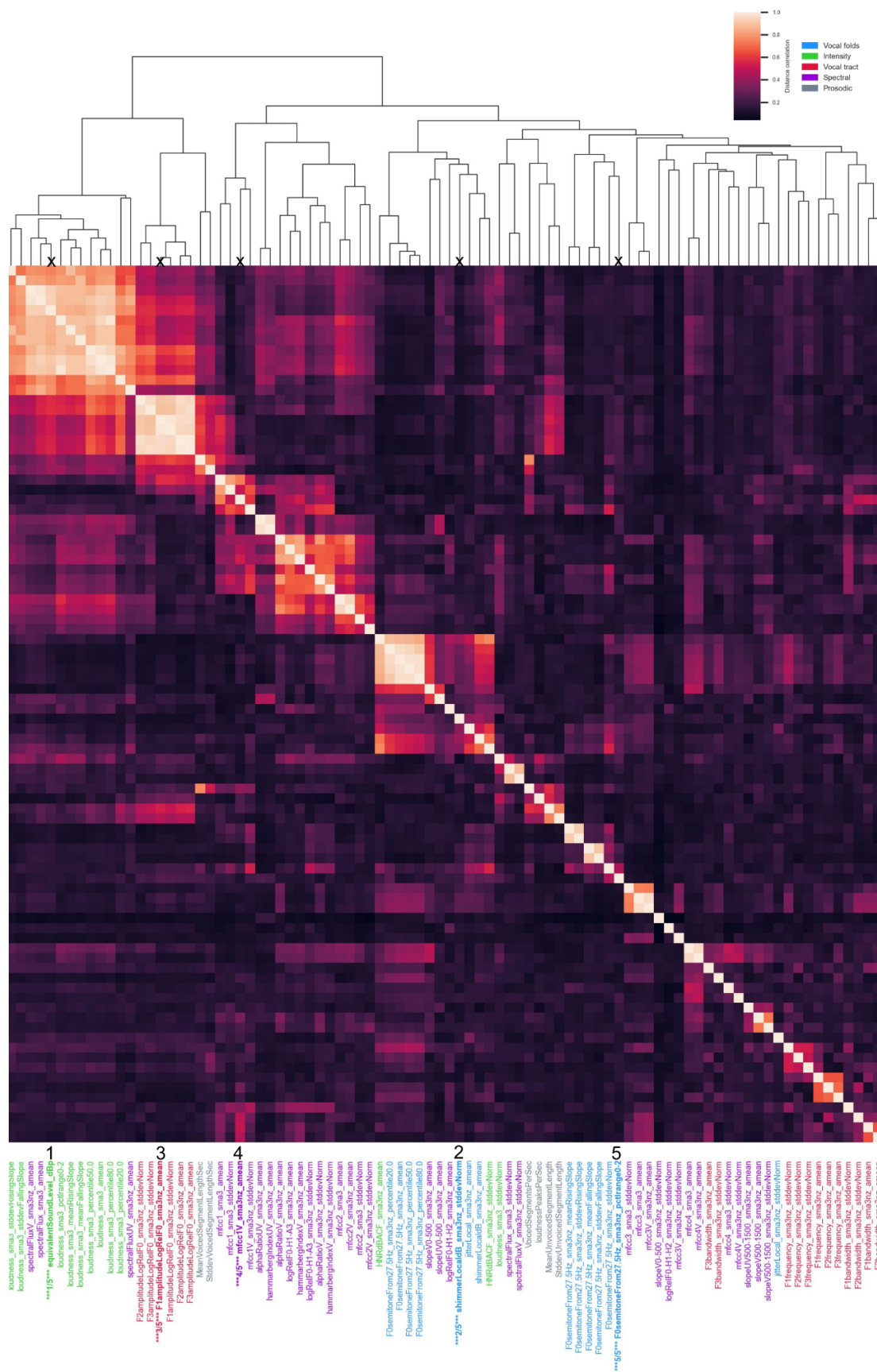


Figure S7. Controls, reading task: Visualization of features with shared information using pairwise distance correlation across the 88 eGeMAPs features. Squares are clusters of redundant features.

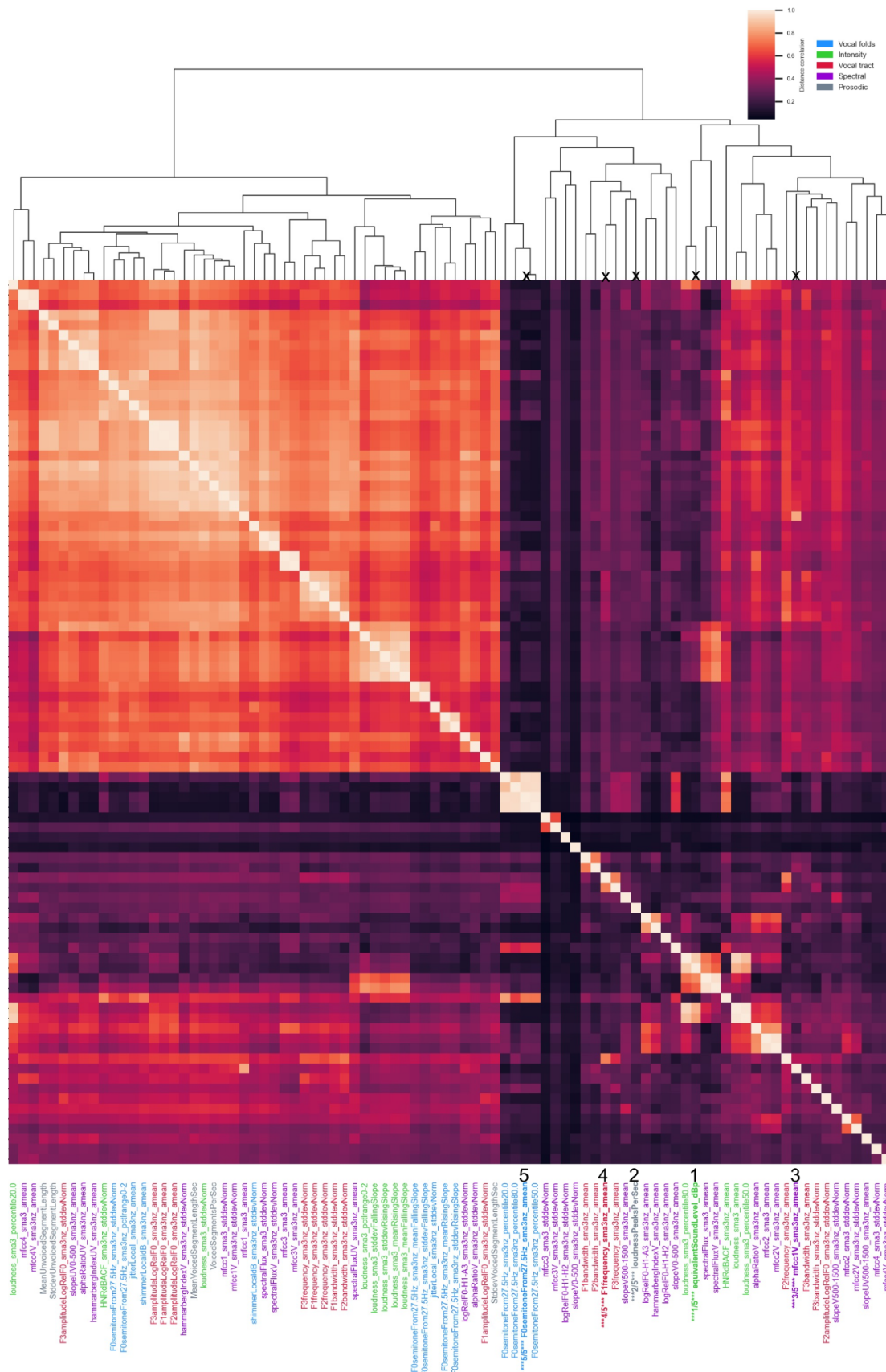


Figure S9. Controls, reading+vowel tasks: Visualization of features with shared information using pairwise distance correlation across the 88 eGeMAPs features. Squares are clusters of redundant features.

Performance with and without redundant features

While removing redundant features is important for explainability, it should not be at the expense of predictive performance. Therefore, we trained and evaluated models and progressively removed redundant features to observe how performance dropped with fewer and fewer features. For each data type (reading, vowel, reading+vowel), through visual inspection of Figure S10, we chose the smaller feature set size that had similar performance to the full feature set size of 88 features: 39 features for reading, 13 features for vowel, and 19 features for reading+vowel.

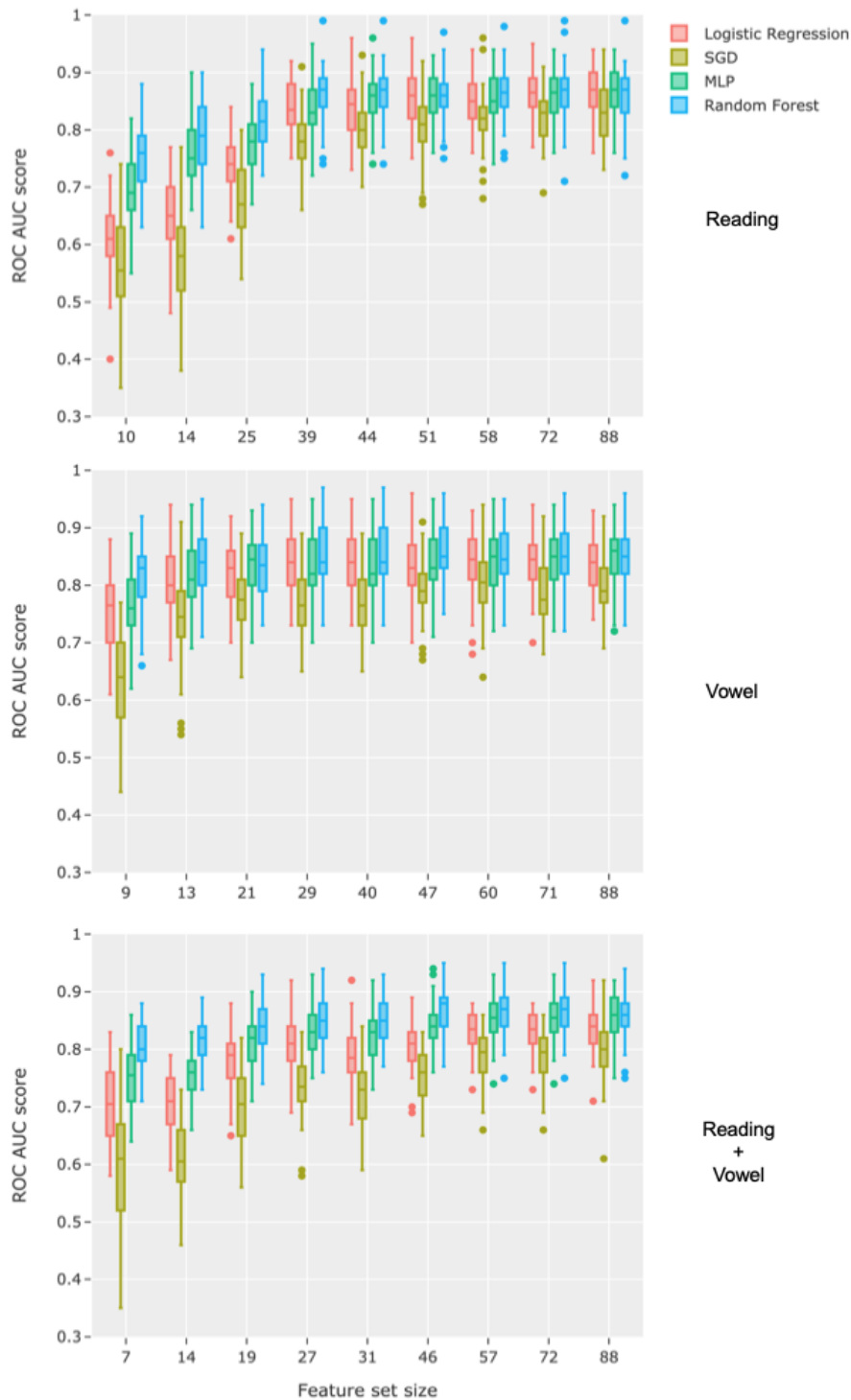


Figure S10. Performance as a function of feature set size using Independence Factor method for reducing feature redundancy. The feature sets remove features with distance correlation ≥ 0.2 up to 1.0 (i.e., keeping all features) in increments of 0.1.

Feature Selection

To make sure information from the test sets is not having a strong influence on feature selection, we tested feature selection on 50 random train sets (80% of samples to match how models were trained) to make sure similar features were selected through this nested approach. If feature selection is relatively consistent across samples, removing features on the entire dataset should not be overfitting and is preferred for the explainability analysis to compare the same features. As seen in Table S2, all or most of the features used by selecting on the data set were also the most common across 50 splits and were selected in 91%, 83% and 76% of splits for reading, vowel and reading+vowel, respectively. Therefore, similar features are selected using both methods, but selecting on the entire dataset is preferred for explainability purposes (i.e., to rank the same features by their importance across all bootstrapping splits).

Selection using		Reading	Vowel	Reading+Vowel
Entire dataset	Optimal threshold and selected features	0.5	0.3	0.4
	Selected features	39	13	19
50 bootstrap train sets	Selected features (mean [95% CI])	35.8 [34–38]	12.3 [11–14]	17.9 [16–20]
	Match between both methods (entire dataset / most common across 50 train sets)	39/39	12/13	16/19
	Selected in percentage of runs	91%	83%	76%

Table S2. Comparison of selecting features on the entire dataset (useful for explainability) versus selecting on 50 bootstrap (80–20) train splits. Original total features are 88. CI = Confidence Interval.

Performance removing participants that used other recording system

Given 24 patients were recorded using an iPad, we trained models without their samples to make sure these differences in recordings were not driving performance. 66, 72, and 138 samples were removed from the reading, vowel, and reading+vowel datasets, respectively. Performance did not drop considerably; changes in performance may also be partly due to reducing sample size (see Supplementary Table S3).

	Features	LogisticRegression	MLP	RandomForest	SGD
Reading	88	.82 (.71–.87; .50)	.82 (.73–.88; .51)	.80 (.72–.88; .53)	.79 (.66–.87; .50)
Vowel	88	.78 (.71–.89; .50)	.79 (.68–.90; .54)	.81 (.73–.90; .52)	.74 (.60–.85; .45)
Reading+Vowel	88	.79 (.70–.87; .50)	.81 (.74–.88; .52)	.81 (.73–.88; .52)	.77 (.67–.84; .50)

Table S3. Performance of models without 24 patients recorded on iPad. Median ROC AUC score from 50 bootstrapping splits (90% confidence interval; median score of null model). The majority class (i.e., controls) represents 60% of the training samples of each dataset. Given the observed performance drop can also be due to removing training samples, the drop is not large enough to suspect that differences in recording are driving performance when using the full datasets. MLP: Multi-Layer Perceptron; SGD: Stochastic Gradient Descent Classifier.

Furthermore, we tested how well a model trained on all participants except those using the iPad and tested on the 24 UVFP patients that used the iPad (see Table S4) to assess generalizability of the model to different recording settings. However, since the iPad recordings were all patients we can therefore only measure false negative rate but not ROC AUC. We used only the controls matched in age and sex to the remaining UVFP patients for training the models to maintain a balanced dataset (i.e., 53 UVFP patients and 53 matched controls).

	Features	LogisticRegression	MLP	RandomForest	SGD
Reading	88	0.08	0.26	0.09	0.39
Vowel	88	0.1	0.11	0.36	0.12
Reading+Vowel	88	0.12	0.2	0.12	0.12

Table S4. False negative rate (FNR) of training on one recording device and testing on 24 UVFP patients that used iPad. FNR is generally quite low. Performance can also be influenced by having a smaller training set in order to balance the classes.

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