

ARTICLE



1

https://doi.org/10.1038/s41467-022-30100-5

OPFN

Structural transition and re-emergence of iron's total electron spin in (Mg,Fe)O at ultrahigh pressure

Han Hsu₁₀ 1⊠ & Koichiro Umemoto²

Fe-bearing MgO [(Mg_{1-x}Fe_x)O] is considered a major constituent of terrestrial exoplanets. Crystallizing in the B1 structure in the Earth's lower mantle, (Mg_{1-x}Fe_x)O undergoes a high-spin (S=2) to low-spin (S=0) transition at ~45 GPa, accompanied by anomalous changes of this mineral's physical properties, while the intermediate-spin (S=1) state has not been observed. In this work, we investigate (Mg_{1-x}Fe_x)O ($x \le 0.25$) up to 1.8 TPa via first-principles calculations. Our calculations indicate that (Mg_{1-x}Fe_x)O undergoes a simultaneous structural and spin transition at ~0.6 TPa, from the B1 phase low-spin state to the B2 phase intermediate-spin state, with Fe's total electron spin S re-emerging from 0 to 1 at ultrahigh pressure. Upon further compression, an intermediate-to-low spin transition occurs in the B2 phase. Depending on the Fe concentration (x), metal-insulator transition and rhombohedral distortions can also occur in the B2 phase. These results suggest that Fe and spin transition may affect planetary interiors over a vast pressure range.

¹ Department of Physics, National Central University, Taoyuan City 320317, Taiwan. ² Earth-Life Science Institute, Tokyo Institute of Technology, Tokyo 152-8550, Japan. [™]email: hanhsu@ncu.edu.tw

e-bearing MgO with the B1 (NaCl-type) structure, also known as ferropericlase (Mg_{1-x}Fe_x)O (0.1 < x < 0.2), is the second most abundant mineral in the Earth's lower mantle (depth 660–2890 km, pressure range 23–135 GPa), constituting ~20 vol% of this region. Experiments and first-principles calculations have shown that B1 MgO remains stable up to ~0.5 TPa and transforms into the B2 (CsCl-type) structure upon further compression^{1–14}. First-principles calculations have also predicted that B2 MgO remains dynamically stable up to at least ~4 TPa^{12,15,16}. MgO has thus been considered a major constituent of terrestrial super-Earths (exoplanets with up to ~10 times of the Earth's mass), where the interior pressure can reach to the tera-Pascal regime^{17,18}.

With the abundance of Fe in the Earth interior, B1 MgO in the Earth's lower mantle contains 10-20 mol% of Fe. Likewise, in terrestrial super-Earths, MgO is expected to contain considerable amount of Fe. With the incorporation of Fe, physical properties of the host mineral can be drastically changed. For example, in B1 (Mg_{1-x}Fe_x)O, Fe undergoes a pressure-induced spin transition (also referred to as spin crossover) from the high-spin (HS, S = 2) to the low-spin (LS, S=0) state at ~45 GPa¹⁹⁻²¹; the intermediate-spin (IS, S = 1) state has never been observed in experiments and has been ruled out by first-principles calculations²². The HS-LS transition of B1 (Mg_{1-x}Fe_x)O is accompanied by anomalous changes of the structural, electronic, optical, magnetic, elastic, thermodynamic, and transport properties of this mineral^{23–36}; it has also been suggested to change the iron diffusion and iron partitioning^{21,23,37–39}, to control the structure of the large low velocity provinces⁴⁰, and to generate the anti-correlation between bulk sound and shear velocities in the Earth's lower mantle⁴¹. Recently, seismological expression of the spin transition of B1 $(Mg_{1-x}Fe_x)O$ has also been reported⁴². Despite extensive studies on B1 $(Mg_{1-x}Fe_x)O$, B2 MgO, and the end member FeO (crystallizing in the B1 structure at pressure $P \lesssim 25$ GPa, undergoing complicated structural transitions upon compression^{43–46}, and stabilizing in the B2 structure at $P \gtrsim 250$ GPa^{47,48}), effects of Fe and spin transition on the properties of B2 MgO and the B1-B2 transition remain unclear, especially for low Fe concentration ($x \le 0.25$) relevant to planetary interiors.

In this work, we study $(Mg_{1-x}Fe_x)O$ at ultrahigh pressure using the local density approximation + self-consistent Hubbard U (LDA+ U_{sc}) method, with the Hubbard U parameters computed self-consistently. So far, LDA+ U_{sc} has been applied to various Fe-bearing minerals of geophysical and/or geochemical importance, including B1 (Mg_{1-x}Fe_x)O, Fe-bearing MgSiO₃ perovskite (bridgmanite) and post-perovskite, ferromagnesite $(Mg_{1-x}Fe_x)CO_3$, and the new hexagonal aluminous (NAL) phase^{22,49–55}. Throughout these works, we have shown that spin-transition pressure determined by LDA+ U_{sc} is typically within 5-10 GPa around the experimental results, and the volume/elastic anomalies obtained by LDA+ U_{sc} are also in great agreement with experiments. With such accuracy, LDA+ U_{sc} has been established as a reliable approach to study Fe-bearing minerals at high pressure and is therefore adopted in this work. Further details of the computation and modeling are described in the Methods Section and Supplementary Information. To investigate the effects of Fe concentration, we perform calculations on $(Mg_{1-x}Fe_x)O$ with x = 0.125 and 0.25 using 16 and 8-atom supercells, respectively (Fig. 1). For B2 IS (Mg_{0.75}Fe_{0.25})O, we find ferromagnetic (FM) order more energetically favorable than antiferromagnetic (AFM) order; we therefore present the FM results in this paper.

Results and discussion

Self-consistent Hubbard *U* **parameters.** Within LDA+ U_{sc} , both the IS and LS states of B2 (Mg_{1-x}Fe_x)O can be obtained at

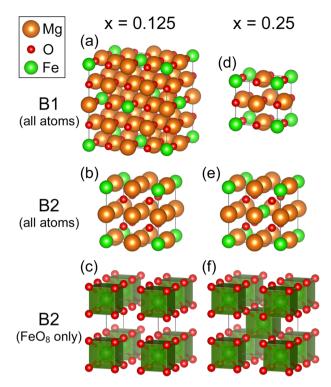


Fig. 1 Supercells of B1 and B2 (Mg_{1-x}Fe_x)O. For x = 0.125 (**a-c**) and x = 0.25 (**d-f**), 16- and 8-atom supercells are adopted, respectively. For the B2 phase, FeO_8 polyhedra are also plotted (**c**, **f**). In B2 ($Mg_{0.75}Fe_{0.25}$)O, a 3D network of corner-sharing FeO_8 cubes is formed (**f**).

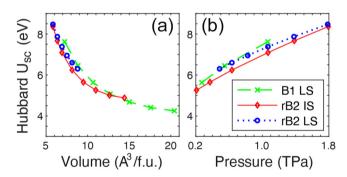


Fig. 2 Self-consistent Hubbard $U(U_{sc})$ **of Fe at ultrahigh pressure. a** U_{sc} of intermediate-spin (IS) and low-spin (LS) Fe in B1 and rB2 (Mg_{0.875}Fe_{0.125})O at various volumes. **b** U_{sc} plotted with respect to pressure in the region of 0.2–1.8 TPa.

ultrahigh pressure, while the HS state can only be obtained at $P \lesssim 0.29$ TPa. The Hubbard U_{sc} of Fe in (Mg_{0.875}Fe_{0.125})O at various volume/pressure are shown in Fig. 2. Note that B2 (Mg_{0.875}Fe_{0.125})O is stabilized via rhombohedral distortion (as further discussed in Figs. 3 and 4), hence referred to as rB2 hereafter. At ultrahigh pressure (0.5 < P < 1.8 TPa), as shown in Fig. 2b, U_{sc} is mainly affected by pressure (increasing with P by ~2.5 eV) and marginally affected by the Fe spin state and crystal structure (by ~0.5 eV). In contrast, at P < 0.15 TPa, Fe spin/valence state affects U_{sc} by up to ~2 eV, while pressure affects U_{sc} by up to ~0.5 eV²²,49⁻⁵⁴.

Soft phonons in cubic B2 ($Mg_{0.875}Fe_{0.125}$)**O.** Fe spin states in B1 and B2 ($Mg_{1-x}Fe_x$)O exhibit distinct properties, due to the host minerals' distinct crystal structures. In the B1 phase, Fe substitutes Mg in the 6-coordinate octahedral site (Fig. 1a, d), forming FeO₆ octahedra (Supplementary Fig. 1a and Note 1). In

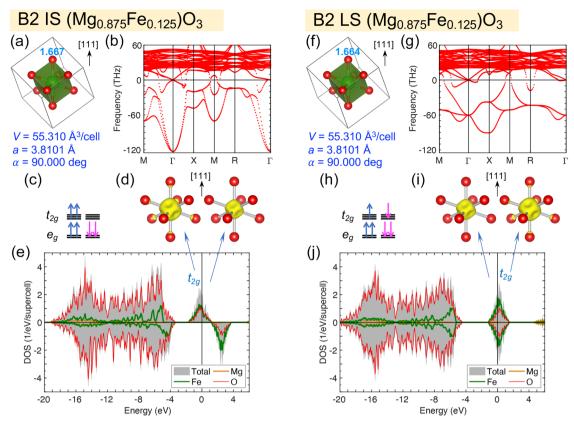


Fig. 3 Atomic structure, stability, and electronic structure of cubic B2 (Mg_{0.875}Fe_{0.125})O. Here, the intermediate-spin (IS, **a-e**) and low-spin (LS, **f-j**) states at volume $V = 55.310 \text{ Å}^3/\text{cell}$ (6.914 Å³/f.u., pressure $P \approx 1.07 \text{ TPa}$) are shown. **a, f** FeO₈ cubes in the supercell, with the Fe-O bond lengths (in Å) indicated by the numbers next to the oxygen atoms, and the lattice parameters (a and a) listed below; **b, g** phonon dispersion; **c, h** orbital occupation; **d, i** integrated local density of states (ILDOS) of the filled and empty t_{2g} states; **e, j** total and projected DOS, with the Fermi energy set as the reference (0 eV). In panels **a, d, f**, and **i**, the [111] direction is pointing upward.

FeO₆ octahedra, the t_{2g} orbitals have lower energy than the e_g orbitals; the orbital configurations of HS and LS Fe²⁺ are $t_{2q}^4 e_q^2$ and $t_{2g}^6 e_g^0$, respectively (Supplementary Fig. 1b and Note 1). In the B2 phase, Fe substitutes Mg in the 8-coordinate site (Fig. 1b, e), forming FeO₈ polyhedra (Fig. 1c, f). For cubic B2 $(Mg_{1-x}Fe_x)O$ with x = 0.125, after structural optimization, FeO₈ polyhedra remain cubic (O_h symmetry), with all eight Fe-O bonds in the same length. Expectedly, the Fe-O bonds of the IS state are slightly longer than those of the LS state (Fig. 3a, f). Remarkably, cubic B2 (Mg_{0.875}Fe_{0.125})O is dynamically unstable, regardless of the Fe spin state, as indicated by the soft phonon modes (negative phonon frequencies) shown in Fig. 3b, g. Nevertheless, the electronic structure of cubic B2 (Mg_{0.875}Fe_{0.125})O still provides valuable insights. In FeO₈ cubes, the t_{2g} orbitals have higher energy than the e_g orbitals, and the orbital configurations of IS and LS Fe²⁺ are both $e_g^4 t_{2g}^2$ (Fig. 3c, h). For the IS state, the e_g orbitals are fully occupied, while the t_{2g} orbitals are partially occupied by two spin-up electrons (Fig. 3c). A partially filled t_{2g} band in the spin-up channel is thus formed, spanning across the Fermi energy (set as the reference, 0 eV) from -1.7 to 1.3 eV, as indicated by the density of states (DOS) shown in Fig. 3e. The t_{2g} characteristic of the t_{2g} band can be visualized via the integrated local density of states (ILDOS) over the energy intervals -1.7 <E < 0 and 0 < E < 1.3 eV for the filled and empty t_{2g} states, respectively (Fig. 3d). For the LS state, the t_{2g} orbitals are partially occupied by one spin-up and one spin-down electron (Fig. 3h), forming a partially filled t_{2g} band in the interval of -1.2 < E <1.6 eV (Fig. 3j). The ILDOS of the filled and empty t_{2g} states (Fig. 3i) resemble those of the IS state (Fig. 3d). For both spin

states, the completely filled e_g bands are embedded in the oxygen band spanning over $-20 \lesssim E \lesssim -4$ eV (Fig. 3e, j). Evidently, the partially filled t_{2g} band and thus the metallicity of cubic B2 (Mg_{0.875}Fe_{0.125})O are the direct consequences of the cubic symmetry.

Rhombohedrally distorted rB2 (Mg_{0.875}Fe_{0.125})O. Depending on the Fe spin state, dynamically unstable cubic B2 (Mg_{0.875}Fe_{0.125})O is stabilized via rhombohedral compression or elongation. As shown in Fig. 4a/f, the IS/LS state is rhombohedrally compressed/elongated, with shortened/stretched Fe-O bonds along the [111] direction and rhombohedral angle α larger/ smaller than 90°. The resultant rB2 structures for both spin states are dynamically stable with no soft phonon mode (Fig. 4b, g). With rhombohedral distortion, the FeO₈ cubes become FeO₈ dodecahedra (D_{3d} symmetry), and the three t_{2g} orbitals split into a singlet (a_{1g}) , which is a d_{z^2} -like orbital along the [111] direction, and a doublet (e'_g) . For the IS state, with shortened Fe-O bonds along the [111] direction, the a_{1g} orbital has higher energy than the e'_{σ} orbitals; the four spin-up electrons occupy the e_{g} and e'_{σ} orbitals, and the two spin-down electrons occupy the e_g orbitals (Fig. 4c). With the splitting of t_{2g} orbitals, an energy gap (~0.3 eV) is opened between the e_g' and $\overline{a_{1g}}$ bands, as indicated by the DOS (Fig. 4e). The e'_{g} and a_{1g} characteristics of these bands can be visualized via the ILDOS (Fig. 4d). For the LS state, with stretched Fe-O bonds along the [111] direction, the a_{1g} orbital has lower energy than the e'_{g} orbitals (Fig. 4h); the three spin-up and three spin-down electrons fully occupy the e_g and a_{1g} orbitals, with the e_g' orbitals left unoccupied, resulting in a gap (~2.0 eV) between

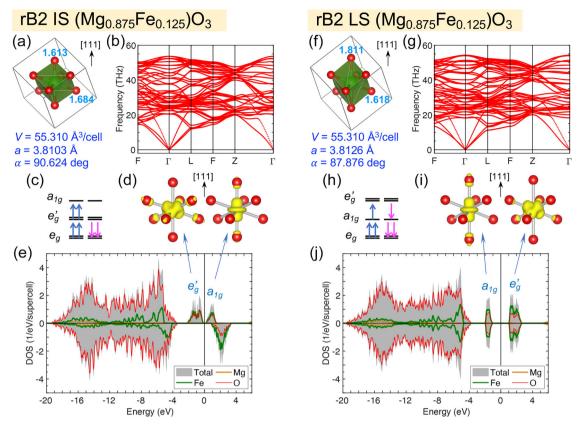


Fig. 4 Atomic structure, stability, and electronic structure of rhombohedrally distorted rB2 (Mg_{0.875}Fe_{0.125})O. Here, the intermediate-spin (IS, **a-e**) and low-spin (LS, **f-j**) states at volume $V = 55.310 \text{ Å}^3/\text{cell}$ (6.914 Å³/f.u., pressure $P \approx 1.07 \text{ TPa}$) are shown. **a, f** FeO₈ dodecahedra in the supercell, with the Fe-O bond lengths (in Å) indicated by the numbers next to the oxygen atoms, and the lattice parameters (a and a) listed below; **b, g** phonon dispersion; **c, h** orbital occupation; **d, i** integrated local density of states (ILDOS) of the e' and a_{1g} bands; **e, j** total and projected DOS, with the Fermi level set as the reference (0 eV). In panels **a, d, f,** and (i), the [111] direction is pointing upward.

the a_{1g} and e'_g bands (Fig. 4j). The a_{1g} and e'_g characteristics of these two bands can also be visualized via the ILDOS (Fig. 4i). For both spin states, the completely filled e_g bands are embedded in the oxygen bands spanning over $-20 \lesssim E \lesssim -4$ eV (Fig. 4e, j).

Cubic B2 (Mg_{0.75}Fe_{0.25})O remaining stable. When the Fe concentration increases to x = 0.25, a three-dimensional (3D) network of corner-sharing FeO₈ cubes is formed in B2 (Mg0.75Fe0.25)O (Fig. 1f), while for $x \le 0.125$, the FeO₈ polyhedra are isolated/ unconnected (Fig. 1c). For isolated FeO₈ polyhedra, rhombohedral distortion is allowed and favored, as observed in rB2 (Mg_{0.875}Fe_{0.125})O (Fig. 4). In contrast, connectivity of the 3D FeO₈ network in B2 (Mg_{0.75}Fe_{0.25})O suppresses the rhombohedral distortion and further stabilizes the cubic structure: Starting the structural optimization with rhombohedrally compressed/elongated rB2 IS/LS (Mg_{0.75}Fe_{0.25})O, the crystal structure and FeO₈ polyhedra resume cubic symmetry within a few steps. Within $LDA+U_{sc}$, the LS state of cubic B2 (Mg_{0.75}Fe_{0.25})O can be obtained throughout 0.2-1.8 TPa, while the IS state can only be obtained at P < 1.1 TPa and is subject to magnetic collapse: The total magnetization (M) decreases from $2\mu_B/\text{Fe}$ to 0 in the region of 0.6 < P < 1.1 TPa and vanishes at P > 1.1 TPa (Fig. 5a). (Note: For x = 0.125, the IS state retains $M = 2\mu_B/\text{Fe}$ up to 1.8 TPa.) Regardless of the spin state and magnetization, cubic B2 (Mg_{0.75}Fe_{0.25})O is dynamically stable with no soft phonon mode, even during the magnetic collapse (Fig. 5b-d). With FeO₈ cubes $(O_h \text{ symmetry}), \text{ cubic B2 } (Mg_{0.75}Fe_{0.25})O \text{ and } (Mg_{0.875}Fe_{0.125})O$ have the same 3d orbital occupations and similar electronic structures. For cubic B2 IS $(Mg_{0.75}Fe_{0.25})O$ with $M = 2\mu_B/Fe$

(before the magnetic collapse), the spin-up t_{2g} band spans across the Fermi energy (0 eV) while the spin-down t_{2g} band lies above the Fermi energy (Fig. 5e), showing the same characteristic as cubic B2 IS (Mg_{0.875}Fe_{0.125})O (Fig. 3e). Likewise, for cubic B2 LS (Mg_{0.75}Fe_{0.25})O (Fig. 5g) and (Mg_{0.875}Fe_{0.125})O (Fig. 3j), the t_{2g} bands in both spin channels align, spanning across the Fermi energy. During the magnetic collapse (0 < M < 2 μ_B /Fe), the t_{2g} bands in the spin-up and spin-down channels are shifted upward and downward, respectively (Fig. 5f).

Complicated transitions of $(Mg_{1-x}Fe_x)O$. To analyze the structural and spin transition of $(Mg_{1-x}Fe_x)O$, we compute the equations of state (EoS) of the B1 LS, (r)B2 IS, and (r)B2 LS states (Supplementary Fig. 2 and Note 2); the relative enthalpies (ΔH) of these states with respect to the (r)B2 IS state are plotted in Fig. 6. For x = 0.125 (Fig. 6a), (Mg_{0.875}Fe_{0.125})O transforms from the B1 LS state into the rB2 IS state at 0.642 TPa. Upon further compression, the rB2 IS state undergoes a spin transition to the rB2 LS state at 1.348 TPa. Throughout these transitions, (Mg_{0.875}Fe_{0.125})O remains insulating (see Supplementary Fig. 1 and Note 1 for the insulating B1 LS state). Remarkably, in the simultaneous structural (B1-rB2) and spin (LS-IS) transition at 0.642 TPa, Fe's total electron spin S re-emerges from 0 to 1, opposite to the perception that S decreases upon compression. Furthermore, the IS state is energetically favorable over a wide pressure range (0.612-1.348 TPa), despite that IS state has never been observed in the Earth's lower-mantle minerals, including B1 (Mg_{1-x}Fe_x)O, Fe-bearing MgSiO₃ bridgmanite and post-perovskite, ferromagnesite $(Mg_{1-x}Fe_x)CO_3$, and the NAL

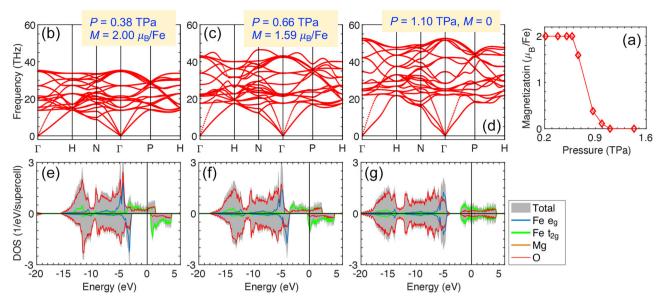


Fig. 5 Stability, electronic structure, and magnetic collapse of cubic B2 intermediate-spin (IS) ($Mg_{0.75}Fe_{0.25}$)O. a Total magnetization (M); b-d phonon dispersion; e-g total and projected density of states (DOS), with the Fermi energy set as the reference (0 eV). Panel (a) indicates that the IS state retains M > 0 at P < 1.1 TPa. At $P \ge 1.1$ TPa, only the nonmagnetic low-spin (LS) state (M = 0) can be obtained. Panels (d) and (g) thus also indicate the LS results.

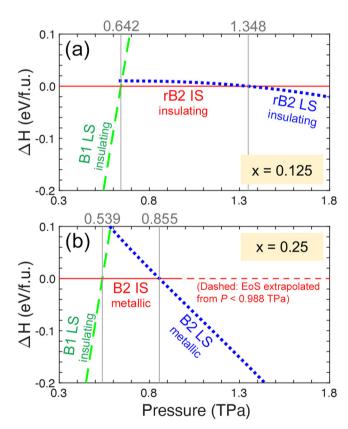


Fig. 6 Relative enthalpies of $(Mg_{1-x}Fe_x)O$ in various structural phases and spin states. a x=0.125, with the rB2 intermediate-spin (IS) state as the reference; b x=0.25, with the B2 IS state as the reference. The vertical lines and the numbers above indicate the enthalpy crossings and transition pressures, respectively.

phase^{22,49–54}. For x = 0.25 (Fig. 6b), a simultaneous structural, spin, and metal–insulator transition occurs at 0.539 TPa, from the insulating B1 LS state to the metallic B2 IS state (notice that *S* increases). Upon further compression, an IS–LS transition occurs

in metallic B2 (Mg_{0.75}Fe_{0.25})O at 0.855 TPa. From Fig. 6, effects of Fe concentration on the B1–(r)B2 transition pressure ($P_T^{B1/B2}$) can also be inferred. For Fe-free MgO (x=0), we find $P_T^{B1/B2}=0.535$ TPa (Supplementary Fig. 3 and Note 3), in agreement with other calculations^{3–14}. As x increases, $P_T^{B1/B2}$ first increases to 0.642 TPa at x=0.125 (Fig. 6a) and then decreases to 0.539 TPa at x=0.25 (Fig. 6b), indicating a trend of decreasing $P_T^{B1/B2}$ in the region of $0.125 \lesssim x \le 1$, consistent with experiments: $P_T^{B1/B2}$ of FeO (~0.25 TPa)^{47,48} is much lower than that of MgO (~0.5 TPa)^{1–4}. [Note: (1) For x=0.25 (Fig. 6b), the EoS of the B2 IS state is fitted using the data points at P < 0.988 TPa (where M > 0). (2) To examine the robustness of the LDA+ U_{sc} results shown in Fig. 6, we perform extensive test calculations using various methods. Similar results are obtained, as shown in Supplementary Figs. 4, 5, and Note 4].

In the Earth's mantle condition, Fe partitioning between B1 (Mg_{1-x}Fe_x)O, Fe-bearing MgSiO₃ bridgmanite, and postperovskite varies with pressure, temperature, and even the Fe valence/spin state^{21,23,37–39}. Likewise, in exoplanet interiors, Fe concentration in B2 (Mg_{1-x}Fe_x)O may vary with the depth or the interior region, due to the variation of Fe partitioning between B2 (Mg_{1-x}Fe_x)O and other minerals phases, including postperovskite and/or high-pressure silicates 15,16. Evident by comparing Fig. 6a and b, spin, structural, and metal-insulator transition of B2 (Mg_{1-x}Fe_x)O can also be induced by the change of Fe concentration (x). In the depth/region with pressure of 0.642-0.855 TPa, if x increases from 0.125 to 0.25, a simultaneous structural and metal-insulator transition occurs [insulating rB2 IS $(Mg_{0.875}Fe_{0.125})O \rightarrow metallic \ B2 \ IS \ (Mg_{0.75}Fe_{0.25})O];$ in the depth/ region with pressure of 0.855–1.348 TPa, if x increases from 0.125 to 0.25, a simultaneous structural, spin, and metal-insulator transition occurs [insulating rB2 IS $(Mg_{0.875}Fe_{0.125})O \rightarrow metallic$ B2 LS $(Mg_{0.75}Fe_{0.25})O$]. Even in the depth/region of P > 1.348TPa, where only LS Fe²⁺ exists, if x increases from 0.125 to 0.25, a simultaneous structural and metal-insulator transition occurs [insulating rB2 LS $(Mg_{0.875}Fe_{0.125})O \rightarrow metallic$ B2 LS $(Mg_{0.75}Fe_{0.25})O]$. On the other hand, if x decreases from 0.25 to 0.125, the aforementioned transitions would be reversed. Based on the above analysis, metal-insulator transition is always included in the composition-induced transitions of the B2 phase, suggesting that variation of Fe partitioning can significantly change the electrical and thermal transport properties of exoplanet interiors.

Implications of spin transition in the B2 phase. At temperature $T \neq 0$, spin transition goes through a mixed-spin (MS) phase/ state, in which different spin states coexist. For B2 $(Mg_{1-x}Fe_x)O$, only the IS and LS states are relevant. Within the thermodynamic model detailed in Supplementary Note 5, the LS fraction (n_{LS}) in the MS phase can be written $n_{LS} = 1/[1 + 3 \exp(\Delta H/k_B Tx)]$, where $\Delta H \equiv H_{LS} - H_{IS}$, and the IS fraction $n_{IS} = 1 - n_{LS}$. Despite that lattice vibration is not considered, the results obtained from this approach have been shown in great agreement with roomtemperature experiments^{22,50,53,54,56}. In Fig. 7, the LS and IS fractions, compression curves, and bulk modulus of B2 $(Mg_{1-x}Fe_x)O$ at T=300 K are shown. For x=0.125, the IS-LS transition is smooth and spans over a wide pressure range (Fig. 7a), due to the small enthalpy difference (ΔH) between the rB2 IS and LS states (Fig. 6a). The compression curves V(P) of the MS, IS, and LS states are nearly the same (Fig. 7b); their difference is barely noticeable even by plotting the relative volume difference with respect to pure $\dot{B2}$ MgO, namely, $(V-V_{\rm MgO})/V_{\rm MgO}$ (Fig. 7c). As a consequence, the bulk modulus $K \equiv -V\partial P/\partial V$ barely changes during the spin transition (Fig. 7d). For x = 0.25, the spin transition is more abrupt (Fig. 7e), due to the larger ΔH between the B2 IS and LS states (Fig. 6b). With increased Fe concentration, the volume difference between the LS and IS states increases (Fig. 7f), resulting in prominent volume reduction (~0.5%) (Fig. 7g) and bulk modulus softening (~22%) (Fig. 7h). While the full elastic tensor (C_{ij}) and shear modulus (G) are not computed, the volume and elastic anomalies shown in Fig. 7g and h clearly indicate anomalous softening of bulk sound velocity $v_{\Phi} = \sqrt{K/\rho}$ (ρ : density) and compressional wave velocity $v_p = \sqrt{\left(K + \frac{4}{3}G\right)/\rho}$. Furthermore, within the phonon gas model, lattice thermal conductivity $\kappa \approx (1/3)C_V v_P^2 \tau$ (C_V : heat capacity; τ : average phonon scattering time)⁵⁷, suggesting that anomalous change of v_P may play a role in the anomalous change of thermal conductivity. In the B1 phase, anomalous v_{Φ} , $v_P^{20,28-33}$ and $\kappa^{35,36}$ have all been observed. The volume/elastic anomalies accompanying the spin transition of the B2 phase may thus be a possible source of seismic and thermal anomalies in exoplanet interiors.

Experiments and computations have confirmed that HS–LS transitions in B1 ($Mg_{1-x}Fe_x$)O and ferromagnesite ($Mg_{1-x}Fe_x$)CO₃ are accompanied by anomalous changes of major thermal properties, including thermal expansivity, heat capacity, Grüneisen parameter, thermal conductivity, and thermoelasticity^{20,28–33,35,36,55}. As the temperature increases, the spin-transition pressure increases, and the transition is broadened^{29,55}. Remarkably, for ($Mg_{0.75}Fe_{0.25}$)CO₃, the anomalous increase of heat capacity retains its magnitude (~12%) without smearing out, even at high temperature⁵⁵. Likewise, for the B2 phase, anomalous changes of thermal properties accompanying the spin transition can be expected. To investigate such anomalies at high P-T conditions, vibrational free energy must be included. Thermal calculations are thus highly desirable and will be left for future studies.

In summary, we have investigated $(Mg_{1-x}Fe_x)O$ ($x \le 0.25$) at ultrahigh pressure up to 1.8 TPa via first-principles calculations. Our calculations indicate that Fe greatly affects the properties of $(Mg_{1-x}Fe_x)O$. For x=0.125, insulating $(Mg_{0.875}Fe_{0.125})O$ undergoes a simultaneous structural and spin transition (B1 LS \rightarrow rB2 IS) at 0.642 TPa, followed by a spin transition (rB2 IS–LS) at 1.348 TPa. For x=0.25, $(Mg_{0.75}Fe_{0.25})O$ undergoes a simultaneous

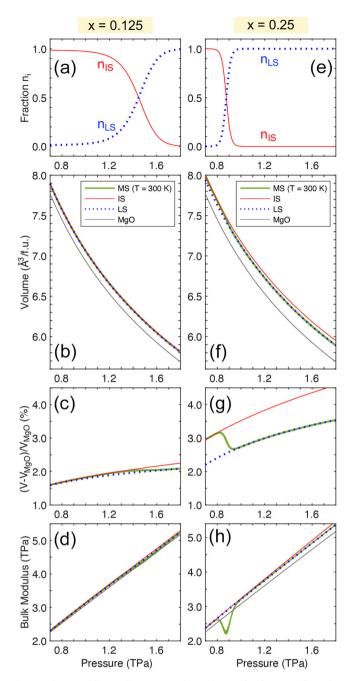


Fig. 7 Spin transition and accompanying volume/elastic anomalies of (r)B2 (Mg_{1-x}Fe_x)O at room temperature. a-d rB2 (Mg_{0.875}Fe_{0.125})O; e-h B2 (Mg_{0.75}Fe_{0.25})O. a, e Fractions of the intermediate-spin (IS) and low-spin (LS) states; b, f compression curves; c, g relative volume difference with respect to pure B2 MgO; d, h isothermal bulk modulus.

structural, spin, and metal-insulator transition (insulating B1 LS \rightarrow metallic B2 IS) at 0.539 TPa, followed by a spin transition (metallic B2 IS-LS) at 0.855 TPa. Remarkably, Fe's total electron spin S re-emerges from 0 to 1 in the B1-(r)B2 transition. In addition, structural, spin, and metal-insulator transitions of B2 (Mg_{1-x}Fe_x)O can also be induced by the change of Fe concentration (x). These results suggest that Fe and spin transition may greatly affect planetary interiors over a vast pressure range, considering the anomalous changes of elastic, transport, and thermal properties accompanying the spin and/or metal-insulator transition.

Methods

Computation. In this work, all major calculations are performed using the QUAN-TUM ESPRESSO codes⁵⁸. We use ultrasoft pseudopotentials (USPPs) generated with the Vanderbilt method⁵⁹. The valence electron configurations for the generations are $2s^22p^63s^23p^03d^0$, $3s^23p^63d^{6.5}4s^14p^0$, and $2s^22p^43d^0$ for Mg, Fe, and O, respectively; the cutoff radii are 1.4, 1,8, and 1.0 a.u. for Mg, Fe, and O, respectively. The aforementioned USPPs of Mg and O have been used in refs. ¹⁵, 16, and the USPP of Fe has been used in refs. ^{22,49–54}. To properly treat the on-site Coulomb interaction of the Fe 3d electrons, we adopt the local density approximation + self-consistent Hubbard U (LDA+ U_{sc}) method, with the Hubbard U parameters computed self-consistently^{60–63}. Briefly speaking, we start with an LDA+U calculation with a trial U (the "input U_{in} ") to obtain the desired spin state for $(Mg_{1-x}Fe_x)O$. For this LDA $+U_{in}$ state, we compute the second derivative of the LDA energy with respect to the 3d electron occupation at the Fe site (d^2E_{LDA}/dn^2) via a density functional perturbation theory (DFPT) approach⁶³ implemented in QUANTUM ESPRESSO. This second derivative, d^2E_{LDA}/dn^2 , is considered as the "output U_{out} " and will be used as U_{in} in the next iteration. Such a procedure is repeated until self-consistency is achieved, namely, $U_{in} = U_{out} \equiv U_{sc}$. Phonon calculations are performed using the Phonopy code⁶⁴, which adopts the finite-displacement (frozen phonon) method. The third-order Birch-Murnaghan equation of state (3rd BM EoS) is used for the EoS fitting.

Thermodynamic model. In this work, analysis for the IS–LS transition in (r)B2 $(Mg_{1-x}Fe_x)O$ at room temperature (300 K) is based on the thermodynamic model detailed in Supplementary Note 5. Plotted in Fig. 7, the IS/LS fractions and the EoS of the MS phase are given by Supplementary Eqs. 9 and 10, respectively.

Data availability

The authors declare that the main data supporting the findings of this study are contained within the paper and its associated Supplementary Information. Example input and output files of our calculations (using QUANTUM ESPRESSO) have been deposited at Zenodo (https://doi.org/10.5281/zenodo.6283200). All other relevant files are available from the corresponding author upon reasonable request.

Code availability

In this work, all major calculations are performed using the QUANTUM ESPRESSO (QE) codes, and phonon calculations are performed using Phonopy, as described in the Methods Section. Both QE and Phonopy are open-source packages; they can be downloaded for free from http://phonopy.github.io/phonopy/, respectively. Detailed information for the compilation and installation of these codes are contained in their own websites.

Received: 1 December 2020; Accepted: 6 April 2022; Published online: 19 May 2022

References

- McWilliams, R. S. et al. Phase transformations and metallization of magnesium oxide at high pressure and temperature. Science 338, 1330 (2012).
- Coppari, F. et al. Experimental evidence for a phase transition in magnesium oxide at exoplanet pressures. *Nat. Geosci.* 6, 926 (2013).
- Miyanishi, K. et al. Laser-shock compression of magnesium oxide in the warm-dense-matter regime. Phys. Rev. E 92, 023103 (2015).
- Root, S. et al. Shock response and phase transitions of MgO at planetary impact conditions. *Phys. Rev. Lett.* 115, 198501 (2015).
- Karki, B. B. et al. Structure and elasticity of MgO at high pressure. Am. Mineral. 82, 51 (1997).
- Mehl, M. J., Cohen, R. E. & Krakauer, H. Linearized augmented plane wave electronic structure calculations for MgO and CaO. J. Geophys. Res. 93, 8009 (1008)
- Oganov, A. R., Gillan, M. J. & Price, G. D. Ab initio lattice dynamics and structural stability of MgO. J. Chem. Phys. 118, 10174 (2003).
- 8. Alfe, D. et al. Quantum Monte Carlo calculations of the structural properties and the B1-B2 phase transition of MgO. *Phys. Rev. B* **72**, 014114 (2005).
- Belonoshko, A. B., Arapan, S., Martonak, R. & Rosengren, A. MgO phase diagram from first principles in a wide pressure-temperature range. *Phys. Rev.* B 81, 054110 (2010).
- Boates, B. & Bonev, S. A. Demixing instability in dense molten MgSiO₃ and the phase siagram of MgO. Phys. Rev. Lett. 110, 135504 (2013).
- 11. Cebulla, D. & Redmer, R. Ab initio simulations of MgO under extreme conditions. *Phys. Rev. B* **89**, 134107 (2014).

- Taniuchi, T. & Tsuchiya, T. The melting points of MgO up to 4 TPa predicted based on ab initio thermodynamic integration molecular dynamics. J. Phys. Condens. Matter 30, 11400 (2018).
- Bouchet, J. et al. Ab initio calculations of the B1-B2 phase transition in MgO. Phys. Rev. B 99, 094113 (2019).
- Soubiran, F. & Militzer, B. Anharmonicity and phase diagram of magnesium oxide in the megabar regime. Phys. Rev. Lett. 125, 175701 (2020).
- Umemoto, K., Wentzcovitch, R. M. & Allen, P. B. Dissociation of MgSiO₃ in the cores of gas giants and terrestrial exoplanets. *Science* 311, 983 (2006).
- Umemoto, K. et al. Phase transitions in MgSiO₃ post-perovskite in super-Earth mantles. *Earth Planet. Sci. Lett.* 478, 40 (2017).
- Duffy, T., Madhusudhan, N. & Lee, K. K. M. Mineralogy of super-Earth planets. In *Treatise on Geophysics*, 2nd edition, Vol. 2, pp. 149 (2015).
- van den Berg, A. P., Yuen, D. A., Umemoto, K., Jacobs, M. H. G. & Wentzcovitch, R. M. Mass-dependent dynamics of terrestrial exoplanets using ab initio mineral properties. *Icarus* 317, 412 (2019).
- Hsu, H., Umemoto, K., Wu, Z. & Wentzcovitch, R. M. Spin-state crossover of iron in lower-mantle minerals: Results of DFT. U investigations. Rev. Miner. Geochem. 71, 169 (2010).
- Lin, J.-F., Speziale, S., Mao, Z. & Marquardt, H. Effects of the electronic spin transitions of iron in lower-mantle minerals: Implications for deep mantle geophysics and geochemistry. Rev. Geophys. 51, 244 (2013).
- Badro, J. Spin transitions in mantle minerals. Annu. Rev. Earth Planet. Sci. 42, 231 (2014).
- Hsu, H. & Wentzcovitch, R. M. First-principles study of intermediate-spin ferrous iron in the Earth's lower mantle. Phys. Rev. B 90, 195205 (2014).
- Badro, J. et al. Iron partitioning in Earthas mantle: toward a deep lower mantle discontinuity. Science 300, 789 (2003).
- Lin, J.-F. et al. Spin transition of iron in magnesiowüstite in the Earthas lower mantle. *Nature* 436, 377 (2005).
- Tsuchiya, T., Wentzcovitch, R. M., daSilva, C. R. S. & de Gironcoli, S. Spin transition in magnesiowüstite in Earth's lower mantle. *Phys. Rev. Lett.* 96, 198501 (2006).
- Goncharov, A. F., Struzhkin, V. V. & Jacobsen, S. D. Reduced radiative conductivity of low-Spin (Mg, Fe)O in the lower mantle. *Science* 312, 1205 (2006)
- Lin, J.-F. et al. Spin transition zone in Earth's lower mantle. Science 317, 1740 (2007).
- Crowhurst, J., Brown, J. M., Goncharov, A. F. & Jacobsen, S. D. Elasticity of (Mg,Fe)O through the spin transition of iron in the lower mantle. *Science* 319, 451 (2008).
- Wu, Z., Justo, J. F., daSilva, C. R. S., de Gironcoli, S. & Wentzcovitch, R. M. Anomalous thermodynamic properties in ferropericlase throughout its spin crossover transition. *Phys. Rev. B* 80, 014409 (2009).
- Wentzcovitch, R. M. et al. Anomalous compressibility of ferropericlase throughout the iron spin cross-over. *Proc. Natl Acad. Sci. USA* 106, 8447 (2009)
- Marquardt, H. et al. Elastic shear anisotropy of ferropericlase in Earthas lower mantle. Science 324, 224 (2009).
- 32. Antonangeli, D. et al. Spin crossover in ferropericlase at high pressure: a seismologically transparent transition? *Science* **331**, 64 (2011).
- Wu, Z., Justo, J. F. & Wentzcovitch, R. M. Elastic anomalies in a spincrossover system: ferropericlase at lower mantle conditions. *Phys. Rev. Lett.* 110, 228501 (2013).
- Holmström, E. & Stixrude, L. Spin crossover in ferropericlase from firstprinciples molecular dynamics. *Phys. Rev. Lett.* 114, 117202 (2015).
- Ohta, K., Yagi, T., Hirose, K. & Ohishi, Y. Thermal conductivity of ferropericlase in the Earth's lower mantle. *Earth Planet. Sci. Lett.* 465, 29 (2017).
- Hsieh, W.-P., Deschamps, F., Okuchi, T. & Lin, J.-F. Effects of iron on the lattice thermal conductivity of Earth's deep mantle and implications for mantle dynamics. *Proc. Natl Acad. Sci. USA* 115, 4099 (2018).
- Kobayashi, Y. et al. Fe-Mg partitioning between (Mg,Fe)SiO₃ post-perovskite, perovskite, and magnesiowüstite in the Earth's lower mantle. *Geophys. Res.* Lett. 32, L19301 (2005).
- 38. Irifune, T. et al. Iron partitioning and density changes of pyrolite in Earthas lower mantle. *Science* **327**, 193 (2010).
- Piet, H. et al. Spin and valence dependence of iron partitioning in Earth's deep mantle. Proc. Natl Acad. Sci. USA 113, 11127 (2016).
- Huang, C., Leng, W. & Wu, Z. Iron-spin transition controls structure and stability of LLSVPs in the lower mantle. *Earth Planet. Sci. Lett.* 423, 173 (2015).
- Wu, Z. & Wentzcovitch, R. M. Spin crossover in ferropericlase and velocity heterogeneities in the lower mantle. *Proc. Natl Acad. Sci. USA* 111, 10468 (2014).
- Shephard, G. E. et al. Seismological expression of the iron spin crossover in ferropericlase in the Earth's lower mantle. Nat. Commun. 12, 5905 (2021).

- Ohta, K., Hirose, K., Shimizu, K. & Ohishi, Y. High-pressure experimental evidence for metal FeO with normal NiAs-type structure. *Phys. Rev. B* 82, 174120 (2010).
- Ozawa, H. et al. Spin crossover, structural change, and metallization in NiAstype FeO at high pressure. Phys. Rev. B 84, 134417 (2011).
- Fischer, R. A. et al. Phase transition and metallization of FeO at high pressures and temperatures. *Geophys. Rev. Lett.* 38, L24301 (2011).
- 46. Hamada, M. et al. Magnetic and spin transitions in wüstite: a synchrotron Mössbauer spectroscopic study. *Phys. Rev. B* **93**, 155165 (2016).
- Ozawa, H., Takahashi, F., Hirose, K., Ohishi, Y. & Hirao, N. Phase transition of FeO and stratification in Earthas outer core. Science 334, 792 (2011).
- Coppari, F. et al. Implications of the iron oxide phase transition on the interiors of rocky exoplanets. Nat. Geosci. 14, 121 (2021).
- Hsu, H., Umemoto, K., Blaha, P. & Wentzcovitch, R. M. Spin states and hyperfine interactions of iron in (Mg,Fe)SiO₃ perovskite under pressure. *Earth Planet. Sci. Lett.* 294, 19 (2010).
- Hsu, H., Blaha, P., Cococcioni, M. & Wentzcovitch, R. M. Spin-state crossover and hyperfine interactions of ferric iron in MgSiO₃ perovskite. *Phys. Rev. Lett.* 106, 118501 (2011).
- Hsu, H., Yu, Y. G. & Wentzcovitch, R. M. Spin crossover of iron in aluminous MgSiO₃ perovskite and post-perovskite. *Earth Planet. Sci. Lett.* 359-360, 34 (2012).
- Yu, Y. G., Hsu, H., Cococcioni, M. & Wentzcovitch, R. M. Spin states and hyperfine interactions of iron incorporated in MgSiO₃ post-perovskite. *Earth Planet. Sci. Lett.* 331-332, 1 (2012).
- Hsu, H. & Huang, S.-C. Spin crossover and hyperfine interactions of iron in (Mg,Fe)CO₃ ferromagnesite. *Phys. Rev. B* 94, 060404(R) (2016).
- 54. Hsu, H. First-principles study of iron spin crossover in the new hexagonal aluminous phase. *Phys. Rev. B* **95**, 020406(R) (2017).
- Hsu, H., Crisostomo, C., Wang, W. & Wu, Z. Anomalous thermal properties and spin crossover of ferromagnesite (Mg,Fe)CO₃. Phys. Rev. B 103, 054401 (2021).
- Hsu, H. & Huang, S.-C. Simultaneous metal-half-metal and spin transition in SrCoO₃ under compression. *Phys. Rev. Mater.* 2, 111401(R) (2018).
- 57. Hofmeister, A. M. & Branlund, J. M. Thermal conductivity of the Earth. In *Treatise on Geophysics*, 2nd edition, Vol. 2, pp. 583 (2015).
- Giannozzi, P. et al. Advanced capabilities for materials modelling with Quantum ESPRESSO. J. Phys. Condens. Matter 29, 465901 (2017).
- Vanderbilt, D. Soft self-consistent pseudopotentials in a generalized eigenvalue formalism. *Phys. Rev. B* 41, 7892(R) (1990).
- Cococcioni, M. & de Gironcoli, S. Linear response approach to the calculation of the effective interaction parameters in the LDA+U method. *Phys. Rev. B* 71, 035105 (2005).
- Kulik, H. J., Cococcioni, M., Scherlis, D. A. & Marzari, N. Density functional theory in transition-metal chemistry: a self-consistent Hubbard *U* approach. *Phys. Rev. Lett.* 97, 103001 (2006).
- Himmetoglu, B., Floris, A., de Gironcoli, S. & Cococcioni, M. Hubbardcorrected DFT energy functionals: the LDA+U description of correlated systems. *Int. J. Quantum Chem.* 114, 14 (2014).
- Timrov, I., Marzari, N. & Cococcioni, M. Hubbard parameters from densityfunctional perturbation theory. *Phys. Rev. B* 98, 085127 (2018).

 Togo, A. & Tanaka, I. First principles phonon calculations in materials science. Scr. Mater. 108, 1 (2015).

Acknowledgements

H.H. acknowledges support from the Ministry of Science and Technology of Taiwan under Grant Numbers MOST 107-2112-M-008-022-MY3, 107-2119-M-009-009-MY3, and 110-2112-M-008-033. K.U. acknowledges support from the JSPS Kakenhi Grant Numbers 17K05627 and 21K03698. Calculations were performed at National Center for High-performance Computing, Taiwan, and the Global Scientific Information and Computing Center at Tokyo Institute of Technology, Japan.

Author contributions

Both authors designed and planned this research. K.U. initiated the work by performing preliminary calculations. H.H. performed the major calculations. Both authors analyzed the calculation results. H.H. wrote the manuscript.

Competing interests

The authors declare no competing interests.

Additional information

Supplementary information The online version contains supplementary material available at https://doi.org/10.1038/s41467-022-30100-5.

Correspondence and requests for materials should be addressed to Han Hsu.

Peer review information Nature Communications thanks Jung-Fu Lin and the anonymous reviewer(s) for their contribution to the peer review of this work. Peer reviewer reports are available.

Reprints and permission information is available at http://www.nature.com/reprints

Publisher's note Springer Nature remains neutral with regard to jurisdictional claims in published maps and institutional affiliations.

Open Access This article is licensed under a Creative Commons Attribution 4.0 International License, which permits use, sharing,

adaptation, distribution and reproduction in any medium or format, as long as you give appropriate credit to the original author(s) and the source, provide a link to the Creative Commons license, and indicate if changes were made. The images or other third party material in this article are included in the article's Creative Commons license, unless indicated otherwise in a credit line to the material. If material is not included in the article's Creative Commons license and your intended use is not permitted by statutory regulation or exceeds the permitted use, you will need to obtain permission directly from the copyright holder. To view a copy of this license, visit https://creativecommons.org/licenses/by/4.0/.

© The Author(s) 2022