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OPEN Design Principles of Inert **Substrates for Exploiting Gold Clusters' Intrinsic Catalytic** Reactivity

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Ultralow stability of gold clusters prohibits the understanding of their intrinsic reactivity (that is vital for revealing the origin of gold's catalytic properties). Using density functional theory including many-body dispersion method, we aim to ascertain effective ways in exploiting gold clusters' intrinsic reactivity on carbon nanotubes (CNTs). We find that the many body van der Waals interactions are essential for gold clusters' reactivity on CNTs and even for O, activation on these supported clusters. Furthermore, curvature and dopant of CNTs are found to qualitatively change the balance between physisorption and chemisorption for gold clusters on CNTs, determining the clusters' morphology, charge states, stability, and reactivity, which rationalize the experimental findings. Remarkably, N doped small curvature CNTs, which effectively stabilize gold clusters and retain their inherent geometric/electronic structures, can be promising candidates for exploiting gold clusters' intrinsic reactivity.

As catalysts, gold nanoparticles have attracted great interest over past decades, due to its unexpected activity and high selectivity towards many reactions 1-4. In particular, gold clusters with a few atoms Au_n exhibit unusual intrinsic reactivity because of their geometric and electronic structures⁵⁻¹⁰. The understanding of Au_n clusters' intrinsic reactivity is of great importance, both for revealing the origin of gold's catalytic properties and for applying gold cluster catalysts⁵⁻⁷. Gold clusters thus have been extensively studied in gas phase experimentally and theoretically^{5,6,9-19}, showing that Au_n clusters adopt planar structures up to Au₁₂18,19, while their reactivity is sensitive to size, shape, and charge states. However, the nature of catalytic properties of gold clusters is still ambiguous, since gold clusters suffer issue of ultralow stability, which leads to their short lifetimes in free states that hampers the understanding of their intrinsic reactivity practically. Many attempts have been made to stabilize metal nanoparticles by protecting them with coordinating ligands or depositing them on active substrates²⁰⁻²⁷. Although ligand-protection and active substrates support yielded some stable and active gold cluster catalysts^{22–27}, these catalysts are entangled with the gold-ligand/gold-substrate covalent bonding, the saturation of clusters' low-coordinate atoms, and the substantial change of clusters geometry, which blur the intrinsic reactivity of gold clusters. Therefore, it is essential to achieve the long-term stable gold clusters that retain their inherent geometric and electronic structures.

Carbon materials as inert substrates are advantageous over active substrates and have also been widely used for growing metal nanoparticles $^{28-31}$. The studies by Corma *et al.* have synthesized Au_{5-10} on functions. tionalized carbon nanotubes (CNTs) that are highly active for the aerobic oxidation of thiophenol with O₂ but are unfortunately passivated rapidly by forming larger and inactive nanoparticles, meanwhile the Au₄ clusters are found to be inactive on CNTs⁸. In addition, the morphology and catalytic mechanism of the supported Au₄₋₁₀ are still unclear because of the limit of experimental detection, substantially

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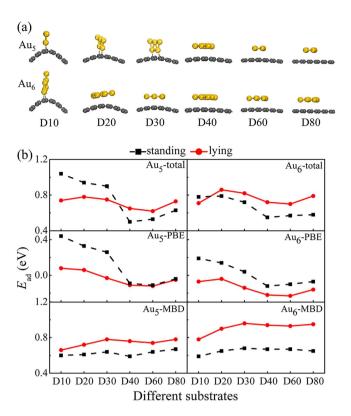


Figure 1. Adsorption properties of the Au_{5-6} clusters on $D10 \sim D80$. (a) Configurations of the optimal Au_{5-6} clusters on $D10 \sim D80$. (b) Adsorption energies of the standing and lying modes for the Au_{5-6} clusters on $D10 \sim D80$. The lines guide the eye. With decreasing of the curvature (from D10 to D80), Au_{5-6} gradually transform from the standing mode to the lying mode, which are determined by the competition of chemisorption and physisorption.

prohibiting the attempt to improve the stability of these catalysts. Density functional approximations (DFA) with (semi-)local functionals, which miss long-range van der Waals (vdW) interactions for non-homogeneous electron gas, cannot be applied to nanomaterials either. The main challenge for theoretically accurate determination of adsorption properties of nanomaterials originates from their nonlocal anisotropic polarization that is coupled with a pronounced contribution of many-body electronic correlations³². This contribution is missed in the pairwise approximation for dispersion forces too.

To reveal the properties of Au_n clusters on CNTs, we employ DFA augmented with accurate description of nonlocal many-body dispersion interactions (DFA+MBD) to study the configurations of $Au_n^{32,33}$, which should be affected by both chemisorption and physisorption. The possible contributions consist of covalent bonding, electrostatic interactions, Pauli repulsions, and vdW interactions. Therefore, we focus on the influence of CNTs' curvature on Au_n , which are accompanied by different chemical reactivity and electrodynamic response effects depending on the diameters of CNTs³⁴, corresponding to distinct chemisorption and physisorption. Indeed, the curvature effect is a rather general phenomenon: Graphene often experiences curl or bending in reality due to tensions, defects, and so on³⁵, intrinsically exhibiting part of CNTs.

Next, we attempt to improve the stability of Au_n clusters by doping CNTs (with different substitution dopants). We propose a design basis that the optimal dopant should enlarge the electrostatic attractions (but avoid forming covalent bonding) between gold clusters and substrates. Furthermore, to retain the intrinsic reactivity of gold clusters on CNTs, the candidate dopant should remain the clusters' geometric and electronic properties unchanged compared to the isolated cases'. By investigating the influences of different dopants, we find that nitrogen dopant combined with curvature control, which perfectly meets the above requirements, can effectively accelerate the exploitation of gold clusters' intrinsic reactivity on CNTs. In addition, our DFA + MBD calculations also provide fundamental insights into catalytic mechanism of gold clusters on CNTs.

Results and Discussions

We first study the influence of curvature on the morphology of the gold clusters, showing the optimal configurations and adsorption energies in Fig. 1 (more results are referred to Figure S1 and Table S1 in Supplementary Information). To simulate CNTs and curved-graphene, we use the bending graphenes, with six kinds of curvature denoted as Dm (m = 10, 20, 30, 40, 60, and 80), corresponding to the different

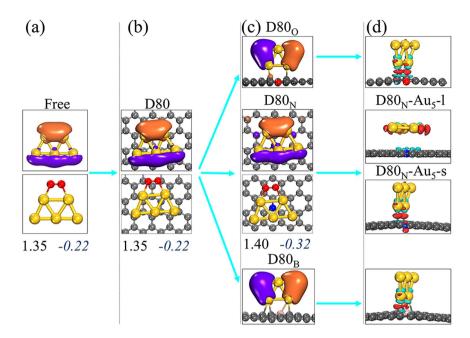


Figure 2. Electronic and geometric properties of the Au_5 clusters. (a,b) Atomic distribution of the HOMOs of the isolated Au_5 clusters and those supported on D80, with the optimal configurations of the adsorption of O_2 on these clusters. (c) HOMOs of the Au_5 clusters on D80_N, D80_O, and D80_B where the subscript N, O, B denote the doping element. (d) The electron density difference of the Au_5 clusters on these doped D80 (both lying and standing modes for D80_N). The different colours of HOMOs represent opposite signs of wavefunctions. LUMOs of O_2 are not shown for simplification. For the electron density difference, blue-green (red) indicates the deletion (accumulation) of electron density. The numbers in bold are the bond lengths of adsorbed O_2 , while those in italic are the charges on O_2 Q (e) with Hirshfeld definition.

diameters of CNTs 10 Å, 20 Å, 30 Å, 40 Å, 60 Å, and 80 Å. In addition, we choose the Au_n clusters with $4 \le n \le 7$ that are in the range of experimental Au_{3-10}^8 . To better understand the adsorption properties of Au_n , we separate the contribution of vdW interactions ($E_{ad,MBD}$) from the total adsorption energy by Perdew-Burke-Ernzerhof³⁶ combined with MBD method (PBE+MBD). The rest is PBE contribution ($E_{ad,PBE}$).

We find that the Au_{4-7} clusters on the substrates resemble the geometry of the isolated Au_n clusters, with planar structures more stable than three-dimensional ones^{5-10,18,19}. These clusters experience two interesting adsorption modes — lying and standing — depending on the curvature of substrates (Fig. 1 and S1). We expect the further experimental studies with IR spectroscopy to identify these two modes. The Au₄ cluster always stands on D10~D80 regardless of the curvature, while Au₅₋₇ gradually transform from the standing mode to the lying mode on D10 ~ D80 with decreasing of the curvature (Fig. 1 and S1), which are determined by the competition of chemisorption and physisorption (mainly the competition of covalent bonding and vdW interactions. see Table S1). The standing mode of gold clusters forms stronger chemical bonds with substrates than the lying mode does, by optimizing the overlap of gold clusters' the highest occupied molecular orbtials (HOMO) and substrates' the lowest unoccupied molecular orbtials (LUMO). In contrast, the lying mode of gold clusters is conducive to maximize vdW interactions with substrates by minimizing the distance between the gold atoms and the substrates. With decreasing of the curvature, chemical reactivity of substrates gradually decreases, while vdW interactions play an increasingly important role in the adsorption of the Au₄₋₇ clusters, forcing the transformation of the Au₄₋₇ clusters from the standing mode to the lying mode. As the Au_n size increases, vdW interactions grow with $0.13 \sim 0.20 \, \text{eV/atom}$ and favor the lying mode. In particular, the lying mode Au_{5-7} experience pure physisorption on CNTs, where these clusters are anchored by vdW interactions, electrostatic interactions, and Pauli repulsions.

To elucidate the reactivity of the Au_n clusters, we study the O_2 activation that is crucial for plenty of reactions^{7–10,12–17,37}. Our calculations demonstrate that the HOMOs of the lying mode Au_{5-7} have lobes exclusively localized on the low-coordinated Au atoms (Fig. 2 and S2), which are all accessible to the LUMO of O_2 (LUMOs_{O2}), since no covalent bonding is formed between the clusters and the substrates. As O_2 adsorbs on these clusters, the charge states of O atoms and the lengths of O-O bond (E) are similar with those on the isolated E0, showing that the substrates greatly preserve the reactivity of the lying mode E1. In contrast, the standing modes E1 and the

Species		Free		D40		$\mathrm{D40_{N}}$	
		PBE	HSE	PBE	HSE	PBE	HSE
Au ₅	Q_{Au5}	0	0	0.03	0.13	-0.33	-0.31
O ₂ /Au ₅	Q_{Au5}	0.22	0.40	0.35	0.38	0.19	0.30
	Q _{O1}	-0.11	-0.20	-0.11	-0.13	-0.17	-0.16
	$Q_{\rm O2}$	-0.11	-0.20	-0.11	-0.13	-0.17	-0.16
Au ₆	Q_{Au6}	0	0	0.17	0.16	0.05	0.14
O ₂ /Au ₆	Q_{Au6}	0.07	0.03	0.17	0.17	0.02	0.13
	Q _{O1}	-0.03	-0.01	-0.05	-0.01	-0.10	-0.04
	Q_{O2}	-0.04	-0.02	-0.06	-0.02	-0.12	-0.05

Table 1. Hirshfeld charges Q (e) of the Au₅, Au₆, O₂/Au₅, and O₂/Au₆ complexes on D40 and D40_N where the subscript N denotes the doping element, compared to the corresponding results on the isolated gold clusters. O1 and O2 indicate the oxygen atom of adsorbed O₂. Both PBE and HSE results are shown for comparison purpose.

standing modes Au_5 on $D10 \sim D30$) bind to the substrates with covalent bonding, which saturates the low-coordinated Au atoms, making their HOMOs be partially inaccessible for LUMOs_{O2} and limiting the adsorption of other reactants (Fig. 1, S1, and S2). These results reveal the importance of taking the lying mode for the supported Au_n clusters to exhibit intrinsic reactivity.

On the lying modes, O_2 activation follows the same manner as on the isolated gold clusters: O_2 is likely activated by gold clusters with an odd (not even) number of electrons (Figure S2)^{7-10,15,16}. In addition, the electron density, which is transferred to the π^*_{OO} molecular orbital of O_2 , is originally from the Au_n clusters, while the substrates act as an electron reservoir that exchanges electrons with adsorbates during catalytic process (Tables 1 and S2). To mitigate the impact of DFT electron self-interaction error on the description of electronic properties, we adopted hybrid functional Heyd-Scuseria-Ernzerhof (HSE)³⁸ to study the electron transfer among the substrates, Au_n clusters, and O_2 . We find that the HSE results are compatible with the PBE ones (Table 1), confirming the independence of our results on exchange-correlation functional and further supporting our conclusions. It is noteworthy that the contribution of vdW interactions to O_2 adsorption increases from $0.06\,\text{eV}$ on Au_4/Dm to $0.44\,\text{eV}$ on Au_7/Dm with increasing of the Au_n size. The maximum contribution is up to 58% ($0.34 \sim 0.44\,\text{eV}$) on $Au_7/\text{Dm} \sim D80$ for the lying mode gold clusters, although it is negligible to that on the isolated gold clusters ($\leq 0.06\,\text{eV}$) and the bare $D10 \sim D80$ ($\leq 0.1\,\text{eV}$). The synergy effects of gold clusters and CNTs make vdW interactions be essential even for activating small molecules like O_2 .

The stability of the supported Au_n clusters is critical to the application of these clusters as catalysts, which can be evaluated from their diffusion barriers. Herein, we compute the diffusion barriers using the adsorption energy difference of the Au_n clusters at different adsorption sites, which are consistently less than $0.2\,eV$ on all considered substrates $(0.05\,\sim\,0.1\,eV$ for the lying modes), indicating a quick migration of the supported Au_n clusters even at low temperature. The tiny diffusion barriers are due to the dominant role of vdW interactions in the adsorption of the Au_n clusters.

Overall, our results explain the experimental findings on the CNTs (the sizes correspond to D40) that the Au_{5-7} clusters are highly active for O_2 activation but quickly aggregate into larger and inactive nanoparticles, while the Au_4 clusters present negligible reactivity⁸. This strongly confirms the promise of our bending-graphene models in studying the properties of CNTs.

To improve the catalytic performance of the Au_n clusters on CNTs, we consider the role of doping in stabilizing these clusters. Elements N, O, B, P, Li, Be, Cr, and Ag are implanted into substrates respectively by replacing one C atom with one impurity atom (the concentration of 1/90). Taking $Au_5/D80$ as an example, none but D80 doped with N (D80_N) surprisingly remain the lying mode of the Au_5 clusters (D80_N-Au₅-I in Fig. 2 and S2). N dopant, which is sp^2 hybridization (see electron density difference of D80_N-Au₅-s in Fig. 2d), perfectly saturates the dangling bonds as one C atom is replaced. Therefore, the lying mode Au_5 cluster does not form any covalent bonding with D80_N, with the distance between D80_N and Au atoms around 3.36 Å. Nevertheless, the amount of electron-density 0.32e is transferred from D80_N to the Au_5 cluster towards N doping (Table S2), significantly increasing electrostatic attractions (monopole-monopole and multipole-multipole interactions) between D80_N and Au_5 . The resulting adsorption energies for the Au_5 cluster are $E_{ad,PBE} = 0.19 \, \text{eV}$ and $E_{ad,MBD} = 0.81 \, \text{eV}$, being larger than those on D80 ($E_{ad,PBE} = -0.05 \, \text{eV}$ and $E_{ad,MBD} = 0.78 \, \text{eV}$). Clearly, the N dopant stabilizes the lying mode Au_5 on D80 by 0.27 eV without forming any covalent bonding, which remarkably meets the design basis we proposed.

In D80_N, each N dopant contributes two p electrons to the π system and leaves the p orbital of N dopant unoccupied, while these two electrons are partially localized in the p orbital of the N dopant's neighboring C atoms. Therefore, the standing mode Au₅, which needs the electron-density donation from binding atoms, binds with the N dopant's neighboring C atoms rather than the N dopant itself. In

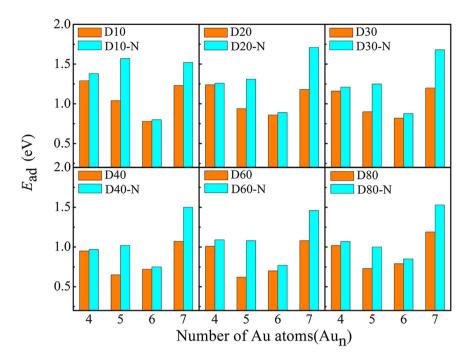


Figure 3. The comparison of adsorption energy for the Au_{4-7} clusters on the substrates of D10 ~ D80 and (D10 ~ D80)_N. Adsorption energies of the Au_{4-7} clusters are overall increased towards Nitrogen doping.

this case, electron-density is also transferred from the Au_5 cluster to the unoccupied p orbital of the N dopant as shown in the $D80_N$ -Au $_5$ -s of Fig. 2d. The N dopant can hardly modify the nature of sp^2 hybridization for its neighboring C atoms. Thus, the overlap of Au $_5$ and C-2p orbitals yields weak covalent bonding between Au_5 and $D80_N$ for the standing mode, having $E_{ad,PBE} = 0.27 \, eV$ ($E_{ad,MBD} = 0.64 \, eV$) and $L_{C-Au} = 2.36 \, Å$. As results, the Au_5 cluster lies on $D80_N$.

In the case of the O doped D80 (D80_O), O dopant is sp^3 hybridization and has two unpaired electrons that cannot fully saturate its neighboring C atoms. Thus these C atoms undergo sp^3 hybridization, leading to the overlap of Au-5d and C-s p^3 orbitals that makes the Au₅ cluster strongly bind with D80_O ($E_{\rm ad,PBE} = 1.32\,{\rm eV}$). Regarding the B, Li, and Be dopants, dangling C atoms cannot be fully saturated either, which form strong covalent bonding with the Au₅ clusters ($E_{\rm ad,PBE} = 1.38 \sim 2.43\,{\rm eV}$). The sizes of P, Cr, and Ag atoms are much larger than that of C atom, making the dopants locate outside CNTs by altering bond angles of C-dopant-C rather than shortening bond lengths of C-dopant, which consequently enable forming covalent P-Au, Cr-Au, and Ag-Au bonds with $E_{\rm ad,PBE}$ of $1.14 \sim 2.20\,{\rm eV}$.

More importantly, the optimal ${\rm Au}_5$ cluster on ${\rm D80}_{\rm N}$ exhibits the identical atomic distribution of the HOMOs compared to the isolated case (Fig. 2 and S2), implying that N doped substrates retain not only the geometry but also the electronic structure of the supported clusters, which is critical for the application of gold clusters' intrinsic reactivity. We thus adopt N as the dopant to stabilize gold clusters on CNTs.

As N is implanted into D10 ~ D80, the geometries of the supported Au_{4-7} are not changed. Importantly, the adsorption energies of Au_{4-7} are overall increased at doped sites (Fig. 3), especially, those of the lying modes Au_5 and Au_7 are increased by $0.27 \sim 0.53\,\text{eV}$. The resulting diffusion barriers of the Au_5 and Au_7 clusters are in the range of $0.35 \sim 0.63\,\text{eV}$ on $(D10 \sim D80)_N$ [2.5 ~ 10 times larger than those on $(D10 \sim D80)_I$, indicating a significantly improved stability of the Au_5 and Au_7 clusters even at elevated temperature of $200 \sim 350\,\text{K}$. The increase of adsorption energy exhibits an odd-even alteration depending on the number of gold atoms, which reflects the redistribution of electron density towards N doping. The open-shell Au_5 and Au_7 , which can readily accept more electrons from the substrates than the close-shell Au_4 and Au_6 do, effectively stabilize $Au_5/(D10 \sim D80)_N$ and $Au_7/(D10 \sim D80)_N$. This stabilization can hardly change the vdW interactions between Au_{4-7} and substrates $(\Delta E_{ad,MBD} \approx 0.05\,\text{eV})$ in Table S1). If the N concentration is increased to 1/45, the diffusion barrier of the lying mode Au_5 is further increased to $0.76\,\text{eV}$ on $D80_N$ ($0.35\,\text{eV}$ at concentration of 1/90).

The $Au_{4-7}/(D10 \sim D80)_N$ are more active in activating O_2 compared to $Au_{4-7}/D10 \sim D80$: more electrons $(0.02 \sim 0.12\,e)$ are transferred to O_2 and the bond length of adsorbed O_2 are elongated further by $0.01 \sim 0.05\,\text{Å}$ towards N doping (Fig. 2 and S2). Namely, nitrogen dopants effectively improve the reactivity of the supported Au_n clusters by making the substrates donate more electrons for activating O_2 . Furthermore, our HSE calculations predict the same trend as PBE calculations for the electron transfer among O_2 , Au_5/Au_6 , and $D40_N$ (Table 1). In addition, HSE functional also identifies a comparable diffusion barrier for the Au_5 cluster on $D40_N$ as PBE functional $(0.42\,eV)$ vs $0.47\,eV$ at concentration of 1/90). Clearly, our results are independent on exchange-correlation functionals, explicitly confirming

that N dopant is able to promote both reactivity and stability of the gold clusters on CNTs. In addition, the dispersed N dopant can also enhance the dispersion of the gold clusters. Recalling that the experiments of the aerobic oxidation of thiophenol with O₂ were carried out at 300 K⁸, we also performed *ab inito* molecular dynamics simulations for Au₅/D40_N and Au₇/D40_N at 300 K, finding slight change of the adsorption position of the Au₅ and Au₇ clusters during 10 ps runs. Therefore, we conclude that the N doped CNTs largely mitigate the problem of low stability of the gold clusters on CNTs⁸ and serve as promising substrates for the application of the gold clusters' intrinsic reactivity.

It is gratifying that CNTs and graphene exhibit sufficient flexibility towards doping functionalization^{39,40}, while the N doped CNTs and graphene have been synthesized experimentally and exhibit remarkable reactivity for variant reactions^{41–43}. In particular, negatively charged 10 nm gold nanoparticles were successfully anchored to the N doped CNTs⁴³, while the Au_{3–10} clusters have been synthesized on CNTs⁸. These encouraging results show robust prospects for growing gold clusters on the N doped CNTs and graphene.

By comparing the MBD results to those by the pairwise approximation of Tkatchenko-Scheffler (TS)⁴⁴ method (Table S1), we find that many body effects are essential for the lying mode Au_n (20~35% contribution) not for the standing mode, reflecting the highly anisotropic polarization of gold clusters and CNTs. In the case of O_2 adsorption on these gold clusters, many body effects can critically affect O_2 activation with up to 41% contribution on $\mathrm{Au}_7/\mathrm{D80}$ (Table S3). In particular, these effects first reduce and then enhance the adsorption energy with decreasing of the curvature, indicating the significant influence of anisotropic polarization of nanomaterials on O_2 activation. Recalling the dominant role of MBD force in anchoring gold clusters on CNTs and activating O_2 on $\mathrm{Au}_n/\mathrm{CNTs}$, DFA+MBD methods are thus essential for accurate prediction of properties of gold clusters on nanomaterials as well as catalysis on these catalysts.

Conclusions

In conclusions, our DFA+MBD results reveal the fundamental mechanism of $\mathrm{Au_{4-7}}$ in activating $\mathrm{O_2}$ on CNTs, where $\mathrm{Au_{4-7}}$ catalytic properties are determined by the balance of chemisorption and physisorption. We find that curvature and dopant of CNTs combined with the clusters size qualitatively change this balance, determining clusters' morphology, charge states, stability, and reactivity. Remarkably, N doped small curvature CNTs, which effectively promote gold clusters' stability by enlarging electrostatic attractions (without forming covalent bonding), retain gold clusters' inherent geometric and electronic structures. These results enable us to explain the experimental findings of gold clusters on CNTs⁸ and to predict N doped CNTs as promising substrates for exploiting gold clusters' intrinsic reactivity. The methodologies we employed, including the DFA+MBD method and the principles of tuning substrates for gold clusters, can serve as a tool to engineer other clusters (*i.e.* Pt_n) supported on nanomaterials where strong covalent bonding ought to be avoided.

Methods

vdW interactions were calculated in the scheme of non-local MBD method on top of DFA (DFA+MBD) 32,33 , using the FHI-aims all electron code with "tight" settings⁴⁵. The DFA+MBD approaches add the vdW energy given as a sum of C_6R^{-6} terms to the DFA total energy. The DFA+MBD methods compute the long-range correlation energy through the coupled harmonic oscillator model Hamiltonian^{32,33,46-48}, which is an effective random phase approximation-like treatment of many body effect, going beyond the pairwise vdW approaches. In addition, the MBD approach, which avoids the explicit use of single-electron orbitals, allows for a favorable N^3 scaling (N is the number of atoms) and a negligible computational cost relative to a self-consistent DFA calculation. More importantly, The MBD methods has been found to be highly accurate for many molecular and solid-state systems^{32,33,46-48}.

All geometries were obtained using CASTEP⁴⁹ code with Vanderbilt-type ultrasoft pseudopotentials⁵⁰ and the PBE+TS method^{36,44}. Forces and stresses for TS calculations were calculated numerically and used to obtain fully consistent TS geometries for all calculations⁴⁴: the normal self-consistency cycle is first completed for PBE; second, the resulting self-consistent electron density is used to create the vdW energy; After adding this vdW energy to PBE total energy, one can effectively compute the forces of PBE+TS. The PBE+TS method has been found to yield the interlayer distance of 3.34 Å for graphite⁵¹, in perfect agreement with the experimental value 3.34 Å. The careful convergence tests allow us to adopt a cutoff energy of 400 eV and a k-point mesh of $2 \times 2 \times 1$ for 90 atoms supercell of graphene (5×9). All calculations are spin unrestricted. The DFA + MBD calculations are shown to converge MBD energy to a meV/atom level. To explicitly elucidate the interplay between substrates and gold clusters, we also compute the electronic structures of considered systems using hybrid HSE functional³⁸.

To obtain the most stable structures of gold clusters on substrates, we defined adsorption energy of gold clusters (E_{ad}) as:

$$E_{\rm ad} = -\left(E_{\rm total} - E_{\rm sub} - E_{\rm gold}\right),\tag{1}$$

where E_{total} is the energy of the bound Au_{n} /substrates, E_{sub} is the energy of the substrates, and E_{gold} is the energy of the isolated, fully relaxed Au_{n} clusters. Since the vdW energy is added as an additional term to the PBE total energy, it is thus convenient to separate the vdW contribution (by MBD) from the total adsorption energy.

References

- 1. Hughes, M. D. *et al.* Tunable gold catalysts for selective hydrocarbon oxidation under mild conditions. *Nature* **437**, 1132–1135 (2005).
- 2. Corma, A. & Garcia, H. Supported gold nanoparticles as catalysts for organic reactions. Chem. Soc. Rev. 37, 2096-2126 (2008).
- Corma, A. & Serna, P. Chemo selective hydrogenation of nitro compounds with supported gold catalysts. Science 313, 332–334 (2006).
- 4. Grirrane, A., Corma, A. & García, H. Gold-catalyzed synthesis of aromatic azo compounds from anilines and nitroaromatics. *Science* 322, 1661–1664 (2008).
- 5. Wang, L.-M. & Wang, L.-S. Probing the electronic properties and structural evolution of anionic gold clusters in the gas phase. *Nanoscale* **4**, 4038–4053 (2012).
- 6. Gruene, P. et al. Structures of neutral Au₇, Au₁₉, and Au₂₀ clusters in the gas phase. Science 321, 674-676 (2008).
- Boronat, M., Leyva-Pérez, A. & Corma, A. Theoretical and experimental insights into the origin of the catalytic activity of subnanometric gold clusters: Attempts to predict reactivity with clusters and nanoparticles of gold. Acc. Chem. Res. 47, 834–844 (2014).
- 8. Corma, A. et al. Exceptional oxidation activity with size-controlled supported gold clusters of low atomicity. Nat. Chem. 5, 775–781 (2013).
- 9. Yoon, B., Häkkinen, H. & Landman, U. Interaction of O₂ with gold clusters: Molecular and dissociative adsorption. *J. Phys. Chem.* A 107, 4066–4071 (2003).
- 10. Huang, W., Zhai, H.-J. & Wang, L.-S. Probing the interactions of O_2 with small gold cluster anions (Au_n^- , n=1-7): Chemisorption vs physisorption. *J. Am. Chem. Soc.* **132**, 4344–4351 (2010).
- 11. Li, J., Li, X., Zhai, H.-J. & Wang, L.-S. Au₂₀: A tetrahedral cluster. Science 299, 864-867 (2003).
- 12. Pal, R., Wang, L.-M., Pei, Y., Wang, L.-S. & Zeng, X. C. Unraveling the mechanisms of O₂ activation by size-selected gold clusters: Transition from superoxo to peroxo chemisorption. *J. Am. Chem. Soc.* **134**, 9438–9445 (2012).
- 13. Zhai, H.-J., Kiran, B., Dai, B., Li, J. & Wang, L.-S. Unique CO chemisorption properties of gold hexamer: $Au_6(CO)_n^-$ (n=0–3). *J. Am. Chem. Soc.* 127, 12098–12106 (2005).
- Fielicke, A. et al. Gold cluster carbonyls: Saturated adsorption of CO on gold cluster cations, vibrational spectroscopy, and implications for their structures. J. Am. Chem. Soc. 127, 8416–8423 (2005).
- 15. Woodham, A. P., Meijer, G. & Fielicke, A. Charge separation promoted activation of molecular oxygen by neutral gold clusters. J. Am. Chem. Soc. 135, 1727–1730 (2013).
- 16. Woodham, A. P., Meijer, G. & Fielicke, A. Activation of molecular oxygen by anionic gold clusters. *Angew. Chem. Int. Ed.* 51, 4444-4447 (2012).
- 17. Woodham, A. P. & Fielicke, A. Superoxide formation on isolated cationic gold clusters. *Angew. Chem. Int. Ed.* **53**, 6554–6557
- 18. Furche, F. et al. The structures of small gold cluster anions as determined by a combination of ion mobility measurements and density functional calculations. J. Chem. Phys. 117, 6982–6990 (2002).
- Häkkinen, H. et al. On the electronic and atomic structures of small Au_N⁻ (N=4-14) clusters: A photoelectron spectroscopy and density-functional study. J. Phys. Chem. A 107, 6168–6175 (2003).
- 20. Häkkinen, H. The gold-sulfur interface at the nanoscale. Nat. Chem. 4, 443-455 (2012).
- 21. Desireddy, A. et al. Ultrastable silver nanoparticles. Nature 501, 399-402 (2013).
- Farmer, J. A. & Campbell, C. T. Ceria Maintains smaller metal catalyst particles by strong metal-support bonding. Science 329, 933–936 (2010).
- 23. Lopez-Acevedo, O., Kacprzak, K. A., Akola, J. & Häkkinen, H. Quantum size effects in ambient CO oxidation catalysed by ligand-protected gold clusters. *Nat. Chem.* **2**, 329–334 (2009).
- 24. Yang, H. et al. All-thiol-stabilized Ag₄₄ and Au₁₂Ag₃₂ nanoparticles with single-crystal structures. Nat. Comm. 4, 2422 (2013).
- 25. Yoon, B. et al. Charging effects on bonding and catalyzed oxidation of CO on Aug clusters on MgO. Science 307, 403-407 (2005).
- Herzing, A. A., Kiely, C. J., Carley, A. F., Landon, P. & Hutchings, G. J. Identification of Active Gold nanoclusters on iron oxide supports for CO oxidation. Science 321, 1331–1335 (2008).
- 27. Lu, J., Aydin, C., Browning, N. D. & Gates, B. C. Imaging isolated gold atom catalytic sites in zeolite NaY. Angew. Chem. Int. Ed. 51, 5842–5846 (2012).
- Joo, S. H. et al. Ordered nanoporous arrays of carbon supporting high dispersions of platinum nanoparticles. Nature 412, 169–172 (2001).
- Gao, W., Mueller, J. E., Anton, J., Jiang, Q. & Jacob, T. Ni cluster growth on defect sites of graphene: A computational study. Angew. Chem. Int. Ed. 52, 14237–14241 (2013).
- 30. Rinaldi, A. et al. Dissolved carbon controls the initial stages of nanocarbon growth. Angew. Chem. Int. Ed. 50, 3313-3317 (2011).
- 31. Sanz-Navarro, C. F. et al. Molecular dynamics simulations of carbon-supported Ni clusters using the reax reactive force field. J. Phys. Chem. C 112, 12663–12668 (2008).
- 32. Tkatchenko, A., DiStasio, R. A., Jr., Car, R. & Scheffler, M. Accurate and efficient method for many-body van der Waals interactions. *Phys. Rev. Lett.* **108**, 236402 (2012).
- 33. Ambrosetti, A., Reilly, A. M., DiStasio, R. A., Jr. & Tkatchenko, A. Long-range correlation energy calculated from coupled atomic response functions. *J. Chem. Phys.* **140**, 18A508 (2014).
- Gobre, V. V. & Tkatchenko, A. Scaling laws for van der Waals interactions in nanostructured materials. Nat. Comm. 4, 2341 (2013).
- 35. Thompson-Flagg, R. C., Moura, M. J. B. & Marder, M. Rippling of graphene. EPL 85, 46002 (2009).
- 36. Perdew, J. P., Burke, K. & Ernzerhof, M. Generalized gradient approximation made simple. Phys. Rev. Lett. 77, 3865-3868 (1996).
- 37. Turner, M. et al. Selective oxidation with dioxygen by gold nanoparticle catalysts derived from 55-atom clusters. Nature 454, 981–984 (2008).
- 38. Heyd, J., Scuseria, G. E. & Ernzerhof, M. Erratum: "Hybrid functionals based on a screened Coulomb potential" [J. Chem. Phys. 118, 8207 (2003)]. J. Chem. Phys. 124, 219906 (2006).
- 39. Zhao, Y.-L. & Stoddart, J. F. Noncovalent functionalization of single-walled carbon nanotubes. Acc. Chem. Res. 42, 1161–1171 (2009)
- 40. Dreyer, D. R., Todd, A. D. & Bielawski, C. W. Harnessing the chemistry of graphene oxide. Chem. Soc. Rev. 43, 5288-5301 (2014).

- 41. Gong, K., Du, F., Xia, Z., Durstock, M. & Dai, L. Nitrogen-doped carbon nanotube arrays with high electrocatalytic activity for oxygen reduction. *Science* 323, 760–764 (2009).
- 42. Qu, L., Liu, Y., Baek, J.-B. & Dai, L. Nitrogen-doped graphene as efficient metal-free electrocatalyst for oxygen reduction in fuel cells. ACS Nano 4, 1321–1326 (2010).
- 43. Jiang, K., Eitan, A., Schadler, L. S., Ajayan, P. M. & Siegel, R. W. Selective attachment of gold nanoparticles to nitrogen-doped carbon nanotubes. *Nano Lett.* 3, 275–277 (2003).
- 44. Tkatchenko, A. & Scheffler, M. Accurate molecular van der Waals interactions from ground-state electron density and free-atom reference data. *Phys. Rev. Lett.* **102**, 073005 (2009).
- 45. Blum, V. et al. Ab initio molecular simulations with numeric atom-centered orbitals. Comput. Phys. Commun. 180, 2175–2196 (2009).
- 46. Ambrosetti, A., Alfè, D., DiStasio, R. A., Jr. & Tkatchenko, A. Supporting information for "Hard numbers for large molecules: Toward exact energetics for supramolecular systems". *J. Phys. Chem. Lett.* 5, 849–855 (2014).
- 47. Reilly, A. M. & Tkatchenko, A. Role of dispersion interactions in the polymorphism and entropic stabilization of the aspirin crystal. *Phys. Rev. Lett.* **113**, 055701 (2014).
- 48. Tkatchenko, A. Current understanding of van der Waals effects in realistic materials. Adv. Funct. Mater. 25, 2054-2061 (2015).
- 49. Segall, M. D. et al. First-principles simulation: Ideas, illustrations and the CASTEP code. J. Phys.: Condens. Matter 14, 2717–2744 (2002).
- 50. Vanderbilt, D. Soft self-consistent pseudopotentials in a generalized eigenvalue formalism. Phys. Rev. B 41, 7892-7895 (1990).
- 51. Gao, W. & Tkatchenko, A. Sliding mechanisms in multilayered hexagonal boron nitride and graphene: The effects of directionality, thickness, and sliding constraints. *Phys. Rev. Lett.* **114**, 096101 (2015).

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Author Contributions

W.G. and Q.J. conceived and designed the research. W.G. and T.T.C. perforemed calculations. W.G., T.T.C. and Q.J. wrote the paper, Y.F.Z., Z.W., M.Z. and J.C.L. discussed the results and commented on the manuscript.

Additional Information

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