



Geometry Design Optimization of Functionally Graded Scaffolds for Bone Tissue Engineering: A Mechanobiological Approach

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Citation: Boccaccio A, Uva AE, Fiorentino M, Mori G, Monno G (2016) Geometry Design Optimization of Functionally Graded Scaffolds for Bone Tissue Engineering: A Mechanobiological Approach. PLoS ONE 11(1): e0146935. doi:10.1371/journal. pone.0146935

Editor: Jie Zheng, University of Akron, UNITED STATES

Received: November 2, 2015

Accepted: December 25, 2015

Published: January 15, 2016

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Data Availability Statement: All relevant data are within the paper.

Funding: The authors have no support or funding to report.

Competing Interests: The authors have declared that no competing interests exist.

Abbreviations: t, length of the side of the basis of the scaffold prismatic model; h, height of the scaffold prismatic model; V_{TOT} , total volume of the scaffold model; $\overline{F_V}$, compression force acting on the scaffold

Abstract

Functionally Graded Scaffolds (FGSs) are porous biomaterials where porosity changes in space with a specific gradient. In spite of their wide use in bone tissue engineering, possible models that relate the scaffold gradient to the mechanical and biological requirements for the regeneration of the bony tissue are currently missing. In this study we attempt to bridge the gap by developing a mechanobiology-based optimization algorithm aimed to determine the optimal graded porosity distribution in FGSs. The algorithm combines the parametric finite element model of a FGS, a computational mechano-regulation model and a numerical optimization routine. For assigned boundary and loading conditions, the algorithm builds iteratively different scaffold geometry configurations with different porosity distributions until the best microstructure geometry is reached, i.e. the geometry that allows the amount of bone formation to be maximized. We tested different porosity distribution laws, loading conditions and scaffold Young's modulus values. For each combination of these variables, the explicit equation of the porosity distribution law-i.e the law that describes the pore dimensions in function of the spatial coordinates-was determined that allows the highest amounts of bone to be generated. The results show that the loading conditions affect significantly the optimal porosity distribution. For a pure compression loading, it was found that the pore dimensions are almost constant throughout the entire scaffold and using a FGS allows the formation of amounts of bone slightly larger than those obtainable with a homogeneous porosity scaffold. For a pure shear loading, instead, FGSs allow to significantly increase the bone formation compared to a homogeneous porosity scaffolds. Although experimental data is still necessary to properly relate the mechanical/biological environment to the scaffold microstructure, this model represents an important step towards optimizing geometry of functionally graded scaffolds based on mechanobiological criteria.



and producing a vertical distributed load; $\overline{F_H}$, shear force acting on the scaffold and producing a horizontal distributed load; $\overline{F_M}$, mixed compressionshear force acting on the scaffold; poore, pore pressure acting on the outer surfaces of the granulation tissue; E, scaffold Young's modulus; A, pore radius; A_i (i = 1, 2, 3, 4), pore radius at specific ylocations; y_{max} , y_{min} , y_{int} , y_{int1} , y_{int2} , specific ylocations where the pore radius was determined; m, m_i (i = 1, 2, 3), gradient of porosity distribution laws; S, biophysical stimulus regulating the differentiation process; χ, octahedral shear strain; υ, interstitial fluid flow; $\varepsilon_{\textit{I}}, \, \varepsilon_{\textit{II}}, \, \varepsilon_{\textit{III}},$ principal strains; a, empirical constant a = 3.75%; b, empirical constant $b = 3 \mu ms^{-1}$; n_{resorb} , n_{mature} , c, boundaries of the mechano-regulation diagram; Alower, lower bound of the pore radius variability range; A_{upper}, upper bound of the pore radius variability range; $V_{i\ bone}$, volume of the generic element where the formation of mature bone is predicted to take place; n_b, number of elements where the formation of mature bone is predicted to take place; V_{BONE}, total volume of the elements where the formation of mature bone is predicted to take place; $BO_{\%}$, percentage of scaffold volume that is occupied by bone; Ω , objective function to optimize; PVPD, Percent Variation of the Pore Dimension; A_H , A_L , highest and lowest value of A along the y-axis, respectively; BO_{% tri-linear}, percentage of volume occupied by bone predicted for the tri-linear porosity distribution law; $\mathsf{BO}_{\%_constant}$, percentage of volume occupied by bone predicted for the constant porosity distribution law; iBO_%, increment of BO_%.

Introduction

Functionally Graded Scaffolds (FGSs) for bone tissue engineering are porous biomaterials where the porosity changes with a specific gradient in space. The gradation of porosity enables FGSs to combine together the best mechanical properties of the denser material with those of the more porous one and the resulting material exhibits performances higher than those of the single constitutive materials. Low porosity regions offer high mechanical strength, high porosity regions promote, instead, cell adhesion and support cell growth, proliferation and differentiation [1-2].

Such scaffolds have been successfully utilized in the most variegated domains including the repair of long bone [1,3] and osteochondral [4–5] defects, the maxillofacial [6–7] and the spinal [8] surgery, the cranial reconstruction [9] and the drug delivery systems [1,10]. A large number of studies [11–13] are reported in the literature on the manufacturing processes that can be adopted to fabricate these biomaterials. Among the others, the strategy based on the integration of additive manufacturing or rapid prototyping techniques with computer-aided design models seems to be one of the most efficient [2,14]. The possibility of building any scaffold architecture with any type of porosity gradation and the experimental evidence that the geometry of porous scaffolds significantly influences the cellular response and the rate of bone tissue regeneration [15–17] led research community to find the possible models that relate the scaffold gradient to the mechanical and biological requirements for the regeneration of the bony tissue [2]. However, to date such models have not been developed yet.

In this article, we attempt to bridge the gap and propose a mechanobiology-driven optimization algorithm that, based on the boundary and loading conditions acting on the scaffold, identifies the best porosity distribution that allows the bone formation to be maximized. Other studies reported in the literature utilized optimization techniques to determine the best scaffold geometry [18–23] but none of them adopted mechanobiological criteria and determined the optimal porosity gradient in FGSs. In a previous study [24], the algorithm was utilized to determine the optimal pore dimension in regular structured open-porous scaffolds with homogeneous porosity. In the present study, the model was further developed to include a functionally graded porosity. In particular, three different variables have been investigated: the porosity distribution law, the loading conditions and the scaffold Young's modulus; for each combination of the three variables, the algorithm determines the explicit equation of the porosity distribution law (i.e. the law that describes the pore dimensions in function of the spatial coordinate), that allows the largest volume of the scaffold to be occupied by bone.

Materials and Methods

Parametric model of an open-porous functionally graded scaffold

The parametric finite element model of an open-porous functionally graded scaffold was created in ABAQUS CAE® Version 6.12 (Dassault Systèmes, France). The model has a prismatic geometry with a square $t \times t = 2548 \ \mu m \times 2548 \ \mu m$ base and a $h = 3822 \ \mu m$ height. The scaffold (represented in yellow, Fig 1A) includes circular pores with a parametric radius A that was assumed to change only along the y direction and remain constant along x and z direction (Fig 1A and 1B). According to Byrne et al. [25], the scaffold pores were hypothesized to be occupied by granulation tissue (represented in red, Fig 1B). The finite element mesh includes tetrahedral biphasic poro-elastic elements. 4-node linear coupled pore pressure elements (C3D4P) available in ABAQUS were utilized to model both, the scaffold (Fig 1C) and the granulation tissue (Fig 1D). The approximate element size was fixed equal to 40 μ m.



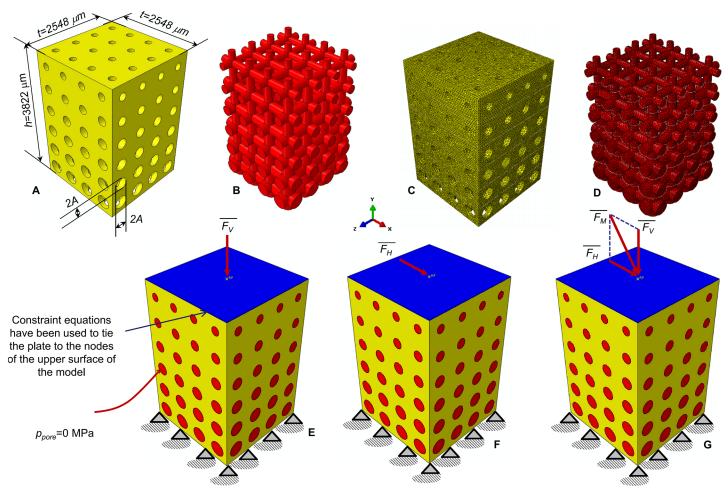


Fig 1. Parametric finite element model of the functionally graded scaffold utilized in the study. CAD model (A-B) and finite element mesh (C-D) of the scaffold (A, C) and granulation tissue (B, D). Circular pores with variable radius A have been modelled. The nodes of the bottom surface of the model were clamped (E-G) while those of the upper surface were tied to a rigid plate (represented in blue). Three different loading conditions were hypothesized: a compression force $\overline{F_V}$ (E); a shear force $\overline{F_H}$ (F); a mixed compression-shear force $\overline{F_M}$ (G). The pore pressure p_{pore} on the outer surfaces of the granulation tissue was set equal to zero to simulate the free exudation of fluid.

Material properties implemented in the finite element model of the granulation tissue are the same as those utilized in previous studies [$\underline{24}$, $\underline{26}$ – $\underline{27}$]. In detail, the Young's modulus was set equal to 0.2 MPa; the permeability to 1×10^{-14} m⁴/N/s; the Poisson's ratio to 0.167; the porosity to 0.8; the bulk modulus grain to 2300 MPa; the bulk modulus fluid to 2300 MPa. In order to evaluate the effect of the scaffold mechanical properties on the optimal porosity distribution, three different values of the Young's modulus *E* were hypothesized: 500, 1000 and 1500 MPa which are the same as those utilized in a previous study [$\underline{24}$].

The nodes of the bottom surface of the model were clamped (Fig 1E, 1F and 1G) while those of the upper surface were tied to a rigid plate (represented in blue, Fig 1E, 1F and 1G). For the outer nodes of the granulation tissue the pore pressure was fixed equal to 0 MPa which indicates that the liquid can freely exudate while applying the load. Three different loading conditions were hypothesized in the study: (a) a compression force \overline{F}_V producing a vertical distributed load of $F_V/(t \times t) = 1$ MPa (Fig 1E); (b) a shear force \overline{F}_H producing an horizontal distributed load of $F_H/(t \times t) = 0.5$ MPa (Fig 1F); (c) a mixed compression-shear force \overline{F}_M



given by the sum $\overline{F}_M = \overline{F}_V + \overline{F}_H$ (Fig 1G). The choice of setting $F_H = 0.5 \times F_V$ was done because scaffolds are primarily designed to undergo to compression loading [25]. In all the hypothesized loading conditions, force was ramped over a time period of 1 s that is the possible time in which, a human body motion (such as to assume the erect position or to perform any motion of anatomical regions where a FGS can be implanted), can be completed. The same time interval was utilized in previous studies [24, 28–29].

Porosity distribution laws

The dimension of the circular pores was controlled by the parametric radius *A* (Fig 1) that was hypothesized to change along the *y*-direction according to different porosity distribution laws. The coefficients of these distribution laws and hence their gradients were determined via the optimization algorithm described below. The porosity distribution laws considered in the study are the following: constant, linear, bi-linear and tri-linear.

- Constant law. All the pores have the same dimensions (<u>Fig 2A</u>). In this case, the optimization algorithm determines just one coefficient, i.e. A_I, that is the pore radius of all the scaffold pores.
- Linear law. The dimensions of pore change linearly with y. Two coefficients have to be determined by the optimization algorithm: A_1 and A_2 that are the pore radii at $y = y_{min}$ and $y = y_{max}$ respectively (Fig 2B).
- Bi-linear law. The pore radius A changes in the ranges $[y_{min} y_{int}]$ and $[y_{int} y_{max}]$ with two different linear laws that assume the same value for $y = y_{int}$. The coefficients to optimize are three: A_1 , A_2 and A_3 (Fig 2C).
- Tri-linear law. The dimensions of the pore change in the intervals $[y_{min} y_{int1}]$, $[y_{int1} y_{int2}]$, $[y_{int2} y_{max}]$ with three different linear laws. The laws defined in the first and second and those defined in the second and third interval assume the same value for $y = y_{int1}$ and for $y = y_{int2}$, respectively. In this case, the optimization algorithm determines four coefficients: A_1 , A_2 , A_3 and A_4 (Fig 2D).

The specific values of y_{max} , y_{min} , y_{int} , y_{int1} and y_{int2} are reported in Fig 2. It is worthy to note that, once the coefficients A_i (i = 1, 2, 3, 4) have been determined, the explicit equation of the best porosity distribution, i.e. the equation that describes how the pore radius A changes with y, can be obtained by simply implementing the obtained coefficients in the relationships reported in Table 1.

Computational mechano-regulation model

Once the mesenchymal stem cells invade the scaffold and spread through its pores, the bone regeneration process starts. After dispersal, cells will differentiate. The biophysical stimulus S that regulates the differentiation process was hypothesized to be a function of the octahedral shear strain γ and interstitial fluid flow ν in the extracellular environment of the cells. In detail, let ε_I , ε_{II} , and ε_{III} be the principal strains, the octahedral shear strain γ can be defined as:

$$\gamma = \frac{1}{2}\sqrt{(\varepsilon_{I} - \varepsilon_{II})^{2} + (\varepsilon_{II} - \varepsilon_{III})^{2} + (\varepsilon_{III} - \varepsilon_{I})^{2}}$$
(1)

Calling *a* and *b* two empirical constants defined as in Huiskes et al. [30], and given by a = 3.75% and $b = 3 \mu ms^{-1}$, the biophysical stimulus *S* can be expressed, according to



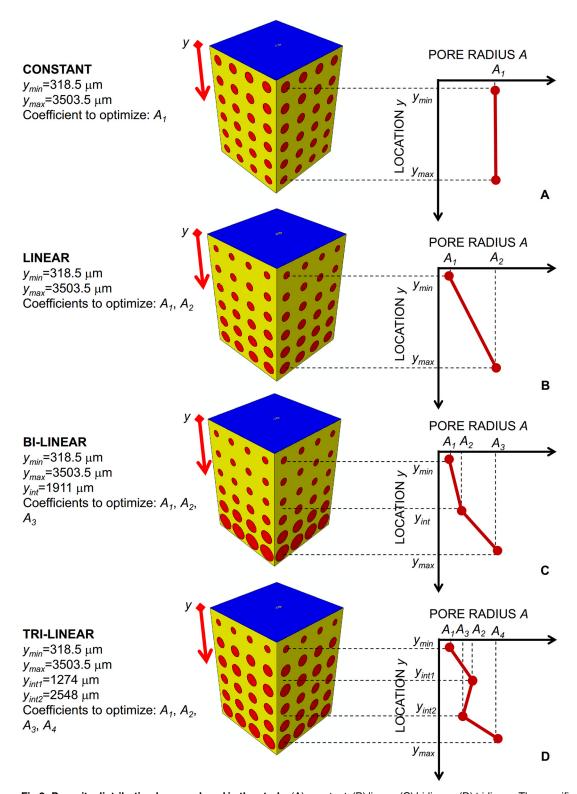


Fig 2. Porosity distribution laws analyzed in the study. (A) constant; (B) linear; (C) bi-linear; (D) tri-linear. The specific coefficients A_i (i = 1, 2, 3, 4) of these laws were determined via the optimization algorithm.



Table 1. Porosity distribution laws implemented in the study	Table 1. Porosit	v distribution laws	s implemented in the study
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Porosity distribution	Coefficients to optimize	Equation	Gradient
Constant law	A ₁	$A = A_1$	0
Linear law	A_{1},A_{2}	$A = A_2 + m(y - y_{\text{max}})$	$m=rac{A_2-A_1}{y_{max}-y_{min}}$
Bi-linear law	A_{1},A_{2},A_{3}	for $y \in [y_{\min} y_{int}] \Rightarrow A = A_2 + m_1(y - y_{int})$ for $y \in [y_{\min} y_{int}] \Rightarrow A = A_3 + m_2(y - y_{\max})$	$m_1 = \frac{A_2 - A_1}{y_{int} - y_{min}}$
			$m_2 = \frac{A_3 - A_2}{y_{max} - y_{int}}$
Tri-linear law	$A_{1,}A_{2,}A_{3,}A_{4}$	for $y \in [y_{\min} y_{\text{int1}}] \Rightarrow A = A_2 + m_1 \times (y - y_{\text{int1}})$ for $y \in [y_{\text{int1}} y_{\text{int2}}] \Rightarrow A = A_3 + m_2 \times (y - y_{\text{int2}})$	$m_1 = \frac{A_2 - A_1}{y_{int1} - y_{min}}$
		for $y \in [y_{int2} y_{max}] \Rightarrow A = A_4 + m_3 \times (y - y_{max})$	$m_2 = \frac{A_3 - A_2}{y_{int2} - y_{int1}}$
			$m_3 = \frac{A_4 - A_3}{y_{max} - y_{int2}}$

Prendergast et al. [31], as:

$$S = \frac{\gamma}{a} + \frac{\nu}{b} \tag{2}$$

Mesenchymal stem cells differentiate into different cell phenotypes according to the following inequalities:

(if
$$S > c \Rightarrow fibrogenesis \Rightarrow fibroblasts \Rightarrow fibrous tissue formation$$
if $1 < S < c \Rightarrow condrogenesis \Rightarrow chondrocytes \Rightarrow cartilagineous tissue formation$
if $n_{mature} < S < 1 \Rightarrow osteogenesis \Rightarrow osteoblasts \Rightarrow immature bone tissue formation$
(3)
if $n_{resorb} < S < n_{mature} \Rightarrow osteogenesis \Rightarrow osteoblasts \Rightarrow mature bone tissue formation$
(if $0 < S < n_{resorb} \Rightarrow osteoclasts \Rightarrow bone resorbtion$

where $n_{resorb} = 0.01$, $n_{mature} = 0.53$ and c = 3 represent boundaries of the mechano-regulation diagram the values of which are the same as those utilized in other studies [28, 32–33].

Optimization algorithm

The FGS parametric finite element model, the computational mechano-regulation model above described and a numerical optimization routine were combined together in an algorithm written in Matlab (v. R2011b) (Fig 3) that aims to determine, for each of the hypothesized scaffold Young's moduli, loading conditions and porosity distribution laws, the equations of the best porosity distribution that allows the bone formation to be maximized. Considering that 3 scaffold Young's modulus values (i.e. 500, 1000 and 1500 MPa), 3 loading conditions (i.e. \overline{F}_V , \overline{F}_H , and \overline{F}_M) and 4 porosity distribution laws (i.e. constant, linear, bi-linear and tri-linear) have been hypothesized, it follows that a total of $3 \times 3 \times 4 = 36$ optimization analyses have been performed in the study.

As a first step, the algorithm requires to select (Block [1]) one of the porosity distribution laws (Block [2]). The initialization of coefficients A_i follows (Block [3]), the user can assign to A_i initial values that fall within the interval [$A_{lower} A_{upper}$], where $A_{lower} = 5 \, \mu m$ and $A_{upper} = 300 \, \mu m$ have been taken the same as those utilized in a previous study [24]. The algorithm implements the specified initial values of A_i into a PYTHON script (Block [4]) that is given in input to ABAQUS. The PYTHON script, based on the values A_i , defines in function of the coordinate location y the



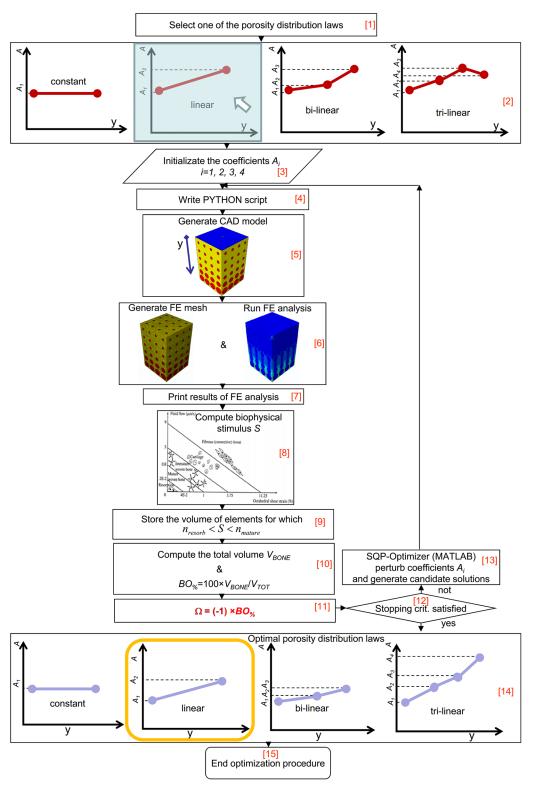


Fig 3. Schematic of the algorithm implemented in Matlab environment to optimize the porosity distribution law in functionally graded scaffolds.



dimension of each pore. The module ABAQUS CAE builds the CAD model of the functionally graded scaffold (Block [5]) with the computed pore dimensions, and after applying the boundary and (one of) the (three) loading conditions above described, generates the finite element mesh (Block [6]). The finite element analysis follows that accounts for geometrical and material nonlinearities (Block [6]). For each element occupying the scaffold pores, i.e. the elements represented in red in Fig 1D, ABAQUS prints (Block [7]) the values of the principal strains ε_I , ε_{II} and ε_{III} and of the interstitial fluid flow D that the algorithm utilizes to compute, through the eqs (1) and (2), the magnitude of the biophysical stimulus S (Block [8]). Then, the relationships eq (3) are implemented and for those elements for which the inequality

$$n_{resorb} < S < n_{mature}$$
 (4)

is satisfied, i.e. for those elements where the formation of mature bone is predicted to take place, the volume V_{i_bone} is stored (Block [9]). If n_b is the number of elements where inequality eq (4) is satisfied, the algorithm calculates the total volume of these elements as:

$$V_{BONE} = \sum_{i=1}^{nb} V_{\underline{\iota}bone} \tag{5}$$

If V_{TOT} is the total volume of the scaffold model $V_{TOT} = t \times t \times h = 2548 \ \mu\text{m} \times 2548 \ \mu\text{m} \times 3822 \ \mu\text{m} = 24.814 \ \text{mm}^3$, the algorithm determines the percentage of scaffold volume $BO_{\%}$ that is occupied by bone as (Block [10]):

$$BO_{\%} = \frac{V_{BONE}}{V_{TOT}} \times 100 \tag{6}$$

and calculates the value of the objective function Ω as (Block [11]):

$$\Omega = (-1) \times BO_{\omega} \tag{7}$$

At this point, the algorithm formulates an optimization problem that includes the coefficients A_i as design variables and that aims to minimize the value of the objective function Ω or, equivalently, to maximize the percentage $BO_{\%}$ of volume occupied by bone. It can be claimed, in fact, that the greater the efficiency of the scaffold, the larger the amount of bone produced by the scaffold itself. In an ideal scaffold, 100% of its volume is occupied by bone. The inverse problem described with the eqs (6) and (7) was solved with the Sequential Quadratic Programming (SQP) method available in Matlab, an iterative method for nonlinear optimization. The number of iterations performed by the method can be controlled by means of specific stopping criteria that can be selected by the user and that include a number of tolerances. As one of these stopping criteria is meet, the optimization process ends and after implementing the optimal coefficients A_i in the relationships of Table 1, the optimal porosity distributions are traced in function of y (Blocks [14] and [15]). If no stopping criteria are satisfied, the optimization algorithm assigns new values to A_i thus generating new candidate solutions (Block [13]). The optimization process terminates when one of the selected stopping criteria is satisfied (Block [12]).

The biophysical stimulus S on which the objective function Ω depends, was computed based on the hypothesis that the dispersal of mesenchymal stem cells has already taken place and that the only granulation tissue, with the mechanical properties above described, occupies the scaffold pores.

All the computations were performed on a HP Z620- Intel[®] Xeon[®] Processor E5-2620—16Gb RAM. The most expensive optimization analyses were those implementing the tri-linear law that took around 300 hours of computations.



Results

In the case of the compression loading F_V the predicted pore dimension experiences small changes (Fig 4A, 4C and 4E) along the y-axis and is almost constant. Independently from the scaffold Young's modulus E, A does not change by more than 15 μ m. The general trend (with the exception for the porosity distribution obtained implementing the constant law) that can be observed is that the pore radius in the vicinity of the clamps (i.e. for high values of y) and of the load (i.e. for small values of y) slightly decreases. For increasing values of E, the pore radius, on average, increases. For instance, in the case of E = 500 MPa, the average pore radius is about 190 μ m, for E = 1500 MPa, instead, becomes about 220 μ m. The percentage of volume occupied by bone $BO_{\%}$ increases as we move from the constant to the tri-linear porosity distribution (Fig 4B, 4D and 4F). Furthermore, increasing values of $BO_{\%}$ were predicted for increasing values of the scaffold Young's modulus (Fig 4B, 4D and 4F).

More interesting appears the porosity distribution predicted by the algorithm in the case of the shear load F_H (Fig 5) where important changes of the pore dimensions are predicted along the y-axis (Fig 5A, 5C and 5E). The highest values of A are predicted in the vicinity of the load (i.e. for small values of y) while the pore dimensions tend to decrease as we move towards the clamped region. Also in this case $BO_{\%}$ increases as we move from the constant to the tri-linear porosity distribution, however, the change of $BO_{\%}$ is more significant than in the case of compression load. For increasing levels of E, the average value of $BO_{\%}$ increases too (Fig 5B, 5D and 5F).

In the case of mixed load F_M , the pore radius A experiences changes that are less important than those predicted in the case of shear load F_H but that are certainly larger than those computed in the case of compression load F_V (Fig 6A, 6C and 6E). As in the previous case, the pore dimension decreases for increasing values of y. $BO_{\%}$ increases as we move from the constant to the tri-linear law and its average value increases for increasing values of the scaffold Young's modulus E (Fig 6B, 6D and 6F). For a fixed value of E and porosity distribution law, the values of E0% predicted in the case of mixed load E10 are smaller than those predicted for the other hypothesized loading conditions (Figs 4B, 4D, 4F, 5B, 5D, 5F, 6B, 6D and 6F).

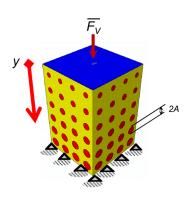
In order to quantify (i) the change of the pore dimensions with *y* and (ii) the "usefulness" of utilizing a functionally graded scaffold instead of a scaffold with a homogenous porosity distribution we introduced two parameters. The first one, denoted as *PVPD*, represents the Percent Variation of the Pore Dimension and is defined as:

$$PVPD = \frac{(A_H - A_L)}{A_L} \times 100 \tag{8}$$

where A_H and A_L are the highest and the lowest value of A along the y-axis, respectively (Fig 7A). In general, the higher the PVPD, the larger are the changes of the pore dimension A. The highest values of PVPD have been found in the case of the shear loading F_H (Fig 7) where changes of A also by more than 25–30% were predicted (Fig 7C). Slightly lower are the values of PVPD found in the case of the mixed load F_M (Fig 7D) and yet less significant those computed in the case of the compression load F_V (Fig 7B). Averagely, it appears that PVPD does not depend neither on the scaffold Young's modulus E, nor on the porosity distribution law but does depend on the loading conditions. For the constant law, regardless of the type of load considered, the value of PVPD is zero and is not shown in Fig 7.

In general, it appears that as we move from the constant to the linear, bi-linear and, finally, tri-linear porosity distribution law the percentage of volume occupied by bone $BO_{\%}$ increases (Figs 4B, 4D and 4F, 5B, 5D and 5F, 6B, 6D and 6F). In particular, the highest values of $BO_{\%}$ have been found for the tri-linear law while the lowest ones for the constant law. Therefore, it





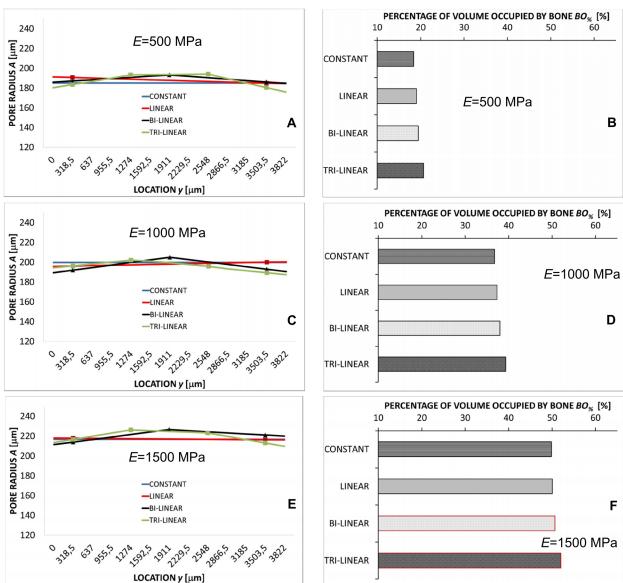
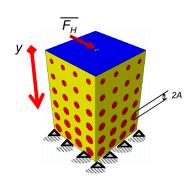


Fig 4. Computed values of A and $BO_{\%}$ in the case of compression loading. Pore radius A (A, C, E) (vs. location y) and percentages of the scaffold volume occupied by bone $BO_{\%}$ (B, D, F) predicted by the optimization algorithm in the case of compression loading F_V for different scaffold Young's moduli and after implementing different porosity distribution laws. The schematic figure shown on the top indicates the loading condition to which the diagrams refer. All the values of $BO_{\%}$ reported in the diagrams refer to the optimal configuration, i.e. the configuration for which Ω reaches its minimum value.





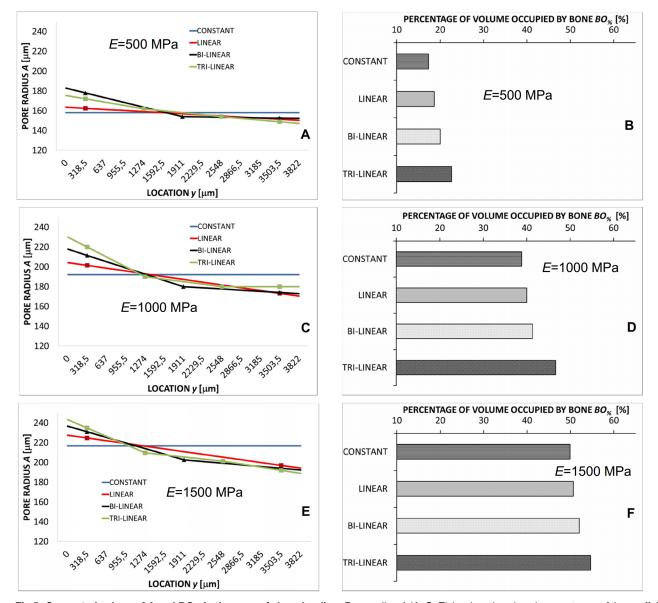
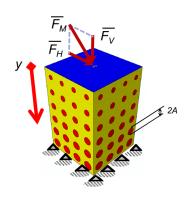
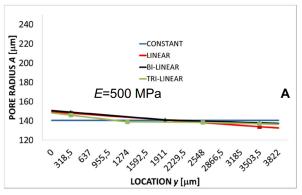
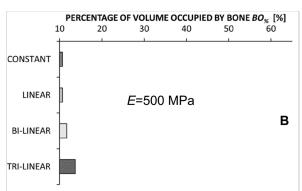


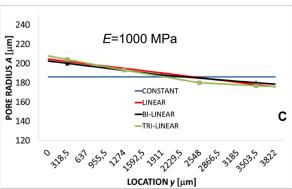
Fig 5. Computed values of A and $BO_{\%}$ in the case of shear loading. Pore radius A (A, C, E) (vs. location y) and percentages of the scaffold volume occupied by bone $BO_{\%}$ (B, D, F) predicted by the optimization algorithm in the case of shear loading F_H for different scaffold Young's moduli and after implementing different porosity distribution laws. The schematic figure shown on the top indicates the loading condition to which the diagrams refer. All the values of $BO_{\%}$ reported in the diagrams refer to the optimal configuration, i.e. the configuration for which Ω reaches its minimum value.

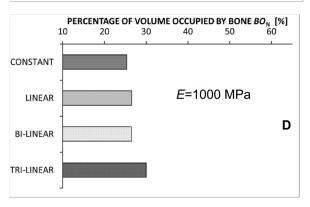


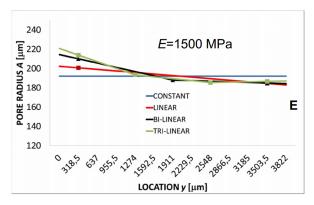












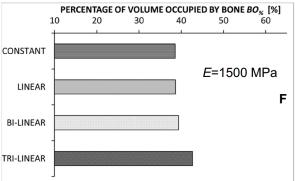


Fig 6. Computed values of A and $BO_{\%}$ in the case of mixed load. Pore radius A (a, c, e) (vs. location y) and percentages of the scaffold volume occupied by bone $BO_{\%}$ (b, d, f) predicted by the optimization algorithm in the case of mixed load F_{M} for different scaffold Young's modulus values and after implementing different porosity distribution laws. The schematic figure shown on the top indicates the loading condition to which the diagrams refer. All the values of $BO_{\%}$ reported in the diagrams refer to the optimal configuration, i.e. the configuration for which Ω reaches its minimum value.



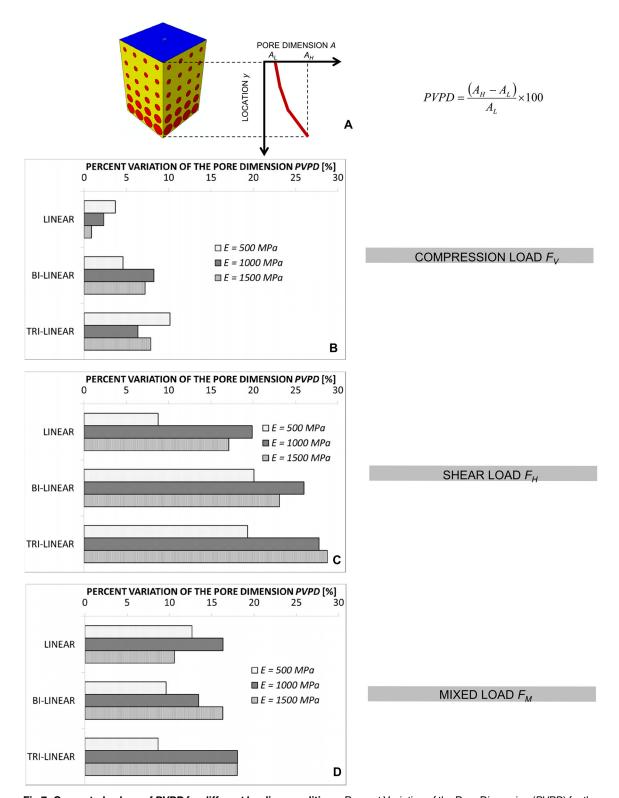


Fig 7. Computed values of *PVPD* for different loading conditions. Percent Variation of the Pore Dimension (PVPD) for the compression F_V (B), the shear F_H (C) and the mixed F_M (D) load and for all the hypothesized scaffold Young's modulus values. (A) reference schematic utilized to calculate the parameter PVPD. Note: A_H and A_L are the highest and lowest value of A that can be located in correspondence of any value of y and not necessarily, as reported in the figure, of the furthest values $y = 0 \mu m$ and $y = h = 3822 \mu m$.



makes sense to introduce the second parameter, denoted as $iBO_{\%}$ and defined as the increment of $BO_{\%}$ when we move from the constant to the tri-linear law. If $BO_{\%_tri-linear}$ is the percentage of volume occupied by bone predicted for the tri-linear porosity distribution and $BO_{\%_constant}$ the percentage predicted with the constant one, $iBO_{\%}$ can be expressed as:

$$iBO_{\%} = BO_{\%_tri-linear} - BO_{\%_constant}$$
 (9)

As is clear, the higher the values of $iBO_{\%}$, the more "useful" is the utilization of a functionally graded scaffold instead of a homogeneous porosity scaffold. In the limit case where $iBO_{\%} = 0\%$, the use of a FGS does not make sense and a homogeneous porosity scaffold has the same potentialities of generating bone as the FG one. On average, the highest values of $iBO_{\%}$ were computed in the case of shear loading F_H followed by the mixed load F_M and the compression load F_V , respectively (Fig. 8). In particular, among the hypothesized scaffold Young's moduli, the highest values of $iBO_{\%}$ were predicted for E = 1000 MPa.

A three-dimensional view of the optimal scaffold geometry predicted for the tri-linear porosity distribution (that is the law with which the highest values of $BO_{\%}$ have been obtained) and the shear loading F_H is shown in Fig 9. As it can be seen, the pore dimensions change significantly along the *y*-axis and, on average, increase for increasing values of E.

Discussion

This article presented an optimization algorithm based on mechanobiological criteria and aimed to determine the best porosity distribution in functionally graded scaffolds for bone tissue engineering.

Four *porosity distribution laws*, three *loading conditions* and three *scaffold Young's moduli* were hypothesized. For each combination of these three variables, the optimal microstructure geometry was determined. It was shown that all these variables have a critical effect on the amounts of bone predicted to form within the scaffold pores.

Regarding the *porosity distribution law*, it was found that designing FGSs with a tri-linear law allows the largest amounts of bone to be generated (Figs 4–6) compared to bi-linear, linear and constant laws. In general, the use of porosity distribution laws with increasing complexity level (i.e. with increasing number of coefficients A_i) leads the scaffold geometry to be better tailored to the specific boundary and loading conditions acting on the construct thus allowing the bone formation to be maximized. Increasing the complexity level of a porosity distribution means, in other words, to include a larger number of design variables and hence, to increase the probability that the optimizer will find a geometry that allows larger amounts of bone to be generated.

More critical appears the effect of the *loading conditions*. For a pure compression loading, the changes of the pore dimension A are marginal (Figs 4, 7 and 9) and using a FGS allows the formation of amounts of bone slightly larger than those obtainable with a homogeneous porosity scaffold (Fig 8). For a pure shear loading, instead, FGSs allow to significantly increase the bone formation compared to a homogeneous porosity scaffolds (Figs 5B, 5D, 5F and 8) and the pore dimensions change (vs. y) also by more than 20-25% (Figs 7 and 9). This behavior can be justified with the following argument. In the case of pure shear loading, strains increase as we move from the loaded towards the clamped region and hence, the stimulus S, that is a function of the strain, changes in the same manner. In order to maximize the number of elements for which inequality eq (4) is satisfied, the optimization solver tends to reduce the dimension of the pores subjected to higher strain and increase that of the pores subjected to lower strain. In the case of pure compression, instead, (from the macroscopic point of view) the scaffold model is subjected to an uniaxial stress state (with the only exception of the regions close to the loaded



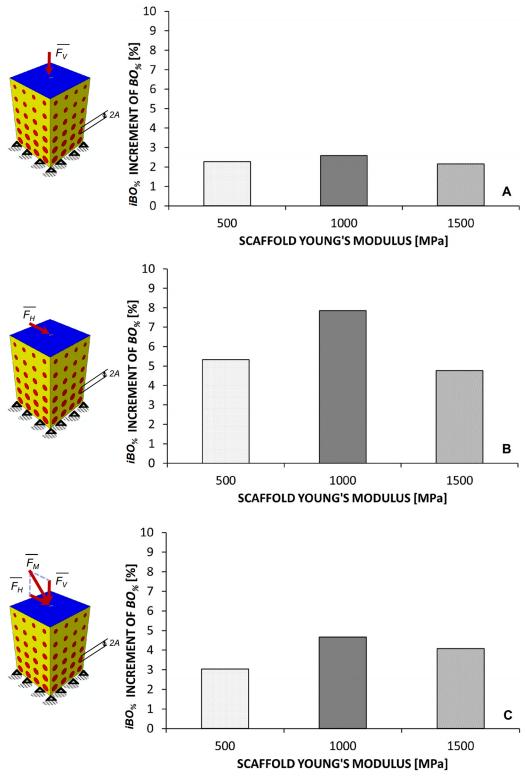


Fig 8. Computed values of $iBO_{\%}$ for compression (A), shear (B) and mixed (C) load.



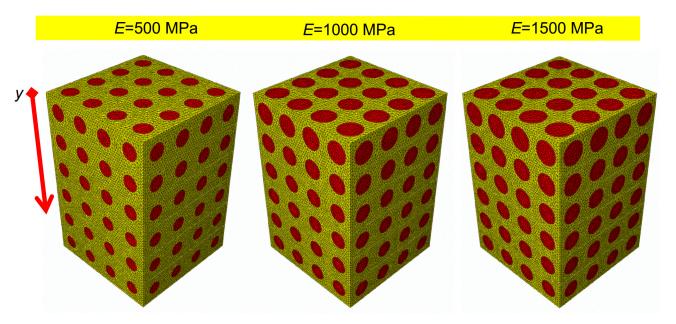


Fig 9. 3D view of the best geometrical configurations (tri-linear porosity distribution) predicted by the optimization algorithm for the shear loading condition.

and the clamped surfaces where the stress state becomes tri-axial) and then to a more or less uniform distribution of the stimulus S, which explains the approximately uniform dimensions of the pores. The mixed load F_M leads to an intermediate situation between the pure compression and the pure shear. Changes of A as well increments of $BO_{\%}$ are more important than those predicted in the case of compression force F_V but less relevant than those computed with the shear load F_H (Figs 6–8).

Finally, regarding the *scaffold Young's modulus* it appears that the average pore dimension A increases for increasing values of E (Fig 9). This can be justified with the argument that as the Young's modulus increases, the global scaffold stiffness increase too and the optimizer tends to increase the dimensions of the pores to include larger amounts of bone.

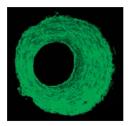
To determine the optimal porosity distribution in FGSs some assumptions were made. First of all, the temporal variable was neglected. It was assumed that the scaffold pores are occupied only by granulation tissue, the processes of diffusion of the mesenchymal stem cells and of tissue differentiation were not simulated and the optimization of the porosity distribution was carried out based on the values of the biophysical stimulus registered at the initial time instant. Furthermore, the algorithm does not include scaffold resorption potential [25].

Including the time variable would certainly allow to carry out more accurate predictions on the best porosity distribution but would lead to a dramatic increase of the computational time thus making the algorithm practically not implementable in a "clinical" context. Other aspects such as angiogenesis [34–36] and growth factors [37] involved in the process of bone regeneration were not modelled. This model neglects the effect of loads during the initial development of a tissue on a scaffold, i.e. during the phase in which cell attach to the scaffold surface. The scaffold surface is a 2D environment while the model utilized in this study is based on volumetric strains. A model to predict the effect of mechanical signals on cells seeded on the surface of a scaffold has been reported [38]. Another limitation of the model is that a deterministic approach was adopted to determine the biophysical stimulus *S*, —on the definition of which the optimal porosity distribution law is calculated,—which neglects any possible genetic



variability in animal populations. A more general and complete approach would be the probabilistic one and would take into account this variability.

However, despite these limitations, the predictions of the model are consistent with the results of experimental studies. For instance, the patterns of bony tissue predicted in the case of a pure compression load, constant porosity distribution, E = 1000 MPa, are consistent with those of new tissue generated in circular matrix channels observed in histological analyses [39]. In vitro, it was found that, bone forms from the channel walls and tends to growth towards the center of the pore. This same behavior was observed in the numerical model (Fig 10). The grey



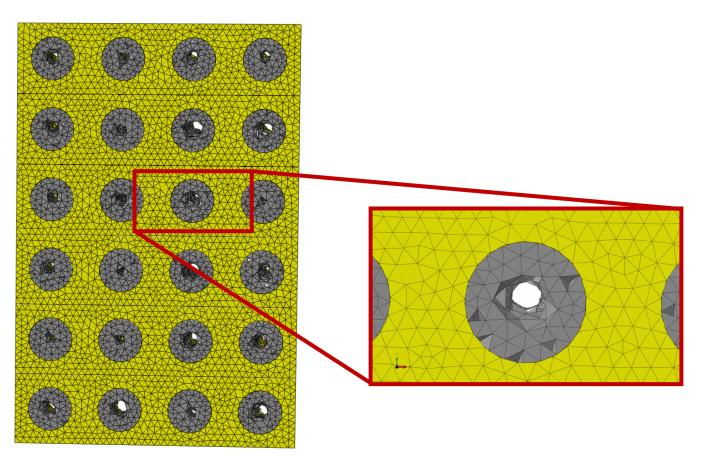


Fig 10. Patterns of bone predicted in the case of: (i) compression loading; (ii) scaffold Young's modulus *E* = 1000 MPa; (iii) porosity distribution law: constant. Elements in gray are representative of the regions within the scaffold pores where the algorithm predicts bone formation. Interestingly, the predicted bony tissue patterns appear consistent with those of new tissue formed in three-dimensional matrix channels observed in an in vitro study [39]. Bone formation starts from the pore walls and propagates towards the pore center.



elements shown in Fig 10 represent the volumes of the model where the mechano-regulation model predicts the formation of bone. Furthermore, as demonstrated in previous studies a minimum pore size of about 100 μ m is required to guarantee a successful bone regeneration process in scaffolds [40]. The pore dimensions predicted by the model are all above this threshold value and well fall within the range of the typical dimensions of the pores of scaffolds for bone tissue engineering [41]. Other studies report that the rate of bone regeneration in scaffold is a function of the scaffold mechanical properties [42]. This is also consistent with the predictions of the present model where the amounts of bone $BO_{\%}$ change for changing values of the scaffold Young's modulus (Figs 4–6 and 9).

Conclusions

A mechanobiology-driven optimization algorithm was presented to determine the optimal porosity distribution in functionally graded scaffolds. The results presented in this paper show that the loading conditions are pivotal in determining optimal porosity distribution. For a pure compression loading, it was predicted that the changes of the pore dimension are marginal and using a FGS allows the formation of amounts of bone slightly larger than those obtainable with a homogeneous porosity scaffold. For a pure shear loading, instead, FGSs allow to significantly increase the bone formation compared to a homogeneous porosity scaffold. Increasing pore dimensions are predicted for increasing values of the scaffold Young's modulus. Increasing the number of coefficients that define a porosity distribution law allows to design more performing scaffolds capable of generating larger amounts of bone.

The model predictions appear reasonably consistent with what is observed in vitro. Although experimental data is still necessary to properly relate the mechanical/biological environment to the scaffold microstructure geometry, this model represents an important step towards optimizing geometry of functionally graded scaffolds and/or stimulation regimes based on mechanobiological criteria.

Author Contributions

Conceived and designed the experiments: AB AEU MF. Wrote the paper: AB. Conceived and designed the algorithm: AB. Edited the algorithm: AEU MF. Wrote the paper: AB. Edited the manuscript: AEU MF G. Mori. Supervised the study and the article writing: G. Monno.

References

- 1. Mia X, Sun D. Graded/Gradient Porous Biomaterials. Materials. 2010; 3: 26–47.
- Leong KF, Chua CK, Sudarmadji N, Yeong WY. Engineering functionally graded tissue engineering scaffolds. J Mech Behav Biomed Mater. 2008; 1: 140–152. doi: 10.1016/j.jmbbm.2007.11.002 PMID: 19627779
- 3. Tampieri A, Celotti G, Sprio S, Delcogliano A, Franzese S. Porosity-graded hydroxyapatite ceramics to replace natural bone. Biomaterials. 2001; 22: 1365–1370. PMID: 11336309
- Pan Z, Duan P, Liu X, Wang H, Cao L, He Y, et al. Effect of porosities of bilayered porous scaffolds on spontaneous osteochondral repair in cartilage tissue engineering. Regenerative Biomaterials. 2015: 9– 19.
- Bailey BM, Nail LN, Grunlan MA. Continuous gradient scaffolds for rapid screening of cellmaterial interactions and interfacial tissue regeneration. Acta Biomater. 2013; 9: 8254–8261. doi: 10.1016/j.actbio. 2013.05.012 PMID: 23707502
- 6. Yang J, Kang Y, Browne C, Jiang T, Yang Y. Graded Porousβ-Tricalcium Phosphate Scaffolds Enhance Bone Regeneration in Mandible Augmentation. J Craniofac Surg. 2015; 26: e148–e153. doi: 10.1097/SCS.000000000001383 PMID: 25675019
- Giannitelli SM, Basoli F, Mozetic P, Piva P, Bartuli FN, Luciani F, et al. Graded porous polyurethane foam: A potential scaffold for oro-maxillary bone regeneration. Mater Sci Eng C Mater Biol Appl. 2015; 51: 329–335. doi: 10.1016/j.msec.2015.03.002 PMID: 25842142



- Lu WW, Zhao F, Luk KDK, Yin YJ, Cheung KMC, Cheng GX, et al. Controllable porosity hydroxyapatite ceramics as spine cage: fabrication and properties evaluation. J Mater Sci Mater Med. 2003; 14: 1039– 1046. PMID: <u>15348496</u>
- Pompe W, Worch H, Epple M, Friess W, Gelinsky M, Greil P, et al. Functionally graded materials for biomedical applications. Mat Sci Eng A Struct. 2003; 362: 40–60.
- Rodríguez-Lorenzo LM, Ferreira JMF. Development of porous ceramic bodies for applications in tissue engineering and drug delivery systems. Mater Res Bull. 2004; 39: 83–91.
- Muthutantri A, Huang J, Edirisinghe M. Novel preparation of graded porous structures for medical engineering. J R Soc Interface. 2008; 5: 1459–1467. doi: 10.1098/rsif.2008.0092 PMID: 18426768
- Lee BT, Kang IC, Gain AK, Kim KH, Song HY. Fabrication of pore-gradient Al₂O₃–ZrO₂ sintered bodies by fibrous monolithic process. J Eur Ceram Soc. 2006; 26: 3525–3530.
- Macchetta A, Turner IG, Bowen CR. Fabrication of HA/TCP scaffolds with a graded and porous structure using a camphene-based freeze-casting method. Acta Biomater. 2009; 5: 1319–1327. doi: 10.1016/j.actbio.2008.11.009 PMID: 19112055
- Chua CK, Leong KF, Sudarmadji N, Liu MJJ, Chou SM. Selective laser sintering of functionally graded tissue scaffolds. Mater Res Bull. 2011; 36: 1006–1014.
- Zadpoor AA. Bone tissue regeneration: the role of scaffold geometry. Biomater Sci. 2015; 3: 231–245. doi: 10.1039/c4bm00291a PMID: 26218114
- Bidan CM, Kommareddy KP, Rumpler M, Kollmannsberger P, Bréchet YJ, Fratzl P, et al. How linear tension converts to curvature: geometric control of bone tissue growth. PLoS ONE. 2012; 7: e36336 doi: 10.1371/journal.pone.0036336 PMID: 22606256
- 17. Feng YF, Wang L, Li X, Ma ZS, Zhang Y, Zhang ZY, et al. Influence of Architecture of β-Tricalcium Phosphate Scaffolds on Biological Performance in Repairing Segmental Bone Defects. PLoS ONE. 2012; 7: e49955 doi: 10.1371/journal.pone.0049955 PMID: 23185494
- 18. Guyot Y, Papantoniou I, Chai YC, Van Bael S, Schrooten J, Geris L. A computational model for cell/ ECM growth on 3D surfaces using the level set method: a bone tissue engineering case study. Biomech Model Mechanobiol. 2014; 13: 1361–1371. doi: 10.1007/s10237-014-0577-5 PMID: 24696122
- 19. Rainer A, Giannitelli SM, Accoto D, De Porcellinis S, Guglielmelli E, Trombetta M. Load-Adaptive Scaffold Architecturing: A Bioinspired Approach to the Design of Porous Additively Manufactured Scaffolds with Optimized Mechanical Properties. Ann Biomed Eng. 2012; 40: 966–975. doi: 10.1007/s10439-011-0465-4 PMID: 22109804
- Dias MR, Guedes JM, Flanagan CL, Hollister SJ, Fernandes PR. Optimization of scaffold design for bone tissue engineering: A computational and experimental study. Med Eng Phys. 2014; 36: 448–457. doi: 10.1016/j.medengphy.2014.02.010 PMID: 24636449
- Coelho PG, Hollister SJ, Flanagan CL, Fernandes PR. Bioresorbable scaffolds for bone tissue engineering: optimal design, fabrication, mechanical testing and scale-size effects analysis. Med Eng Phys. 2015; 37: 287–296. doi: 10.1016/j.medengphy.2015.01.004 PMID: 25640805
- Boccaccio A, Ballini A, Pappalettere C, Tullo D, Cantore S, Desiate A. Finite Element Method (FEM), Mechanobiology and Biomimetic Scaffolds in Bone Tissue Engineering. Int J Biol Sci. 2011; 7: 112– 132. PMID: 21278921
- Wieding J, Wolf A, Bader R. Numerical optimization of open-porous bone scaffold structures to match the elastic properties of human cortical bone. J Mech Behav Biomed Mater. 2014; 37: 56–68. doi: 10.1016/j.jmbbm.2014.05.002 PMID: 24942627
- Boccaccio A, Uva AE, Fiorentino M, Lamberti L, Monno G. A Mechanobiology-based Algorithm to Optimize the Microstructure Geometry of Bone Tissue Scaffolds. Int J Biol Sci. 2016; 12: 1–17. doi: 10.7150/ijbs.13158 PMID: 26722213
- **25.** Byrne DP, Lacroix D, Planell JA, Kelly DJ, Prendergast PJ. Simulation of tissue differentiation in a scaffold as a function of porosity, Young's modulus and dissolution rate: application of mechanobiological models in tissue engineering. Biomaterials. 2007; 28: 5544–5554. PMID: 17897712
- Boccaccio A, Pappalettere C, Kelly DJ. The influence of expansion rates on mandibular distraction osteogenesis: a computational analysis. Ann Biomed Eng. 2007; 35: 1940–1960. PMID: <u>17768683</u>
- Boccaccio A, Prendergast PJ, Pappalettere C, Kelly DJ. Tissue differentiation and bone regeneration in an osteotomized mandible: a computational analysis of the latency period. Med Biol Eng Comput. 2008; 46: 283–298. PMID: 17899238
- Boccaccio A, Kelly DJ, Pappalettere C. A Mechano-Regulation Model of Fracture Repair in Vertebral Bodies. J Orthop Res. 2011; 29: 433–443. doi: 10.1002/jor.21231 PMID: 20886646
- Boccaccio A, Kelly DJ, Pappalettere C. A model of tissue differentiation and bone remodelling in fractured vertebrae treated with minimally invasive percutaneous fixation. Med Biol Eng Comput. 2012; 50: 947–959. doi: 10.1007/s11517-012-0937-1 PMID: 22752875



- Huiskes R, van Driel WD, Prendergast PJ, Søballe K. A biomechanical regulatory model of periprosthetic tissue differentiation. J Mater Sci Mater Med. 1997; 8: 785–788. PMID: 15348791
- Prendergast PJ, Huiskes R, Søballe K. Biophisical stimuli on cells during tissue differentiation at implant interfaces. J Biomech. 1997; 30: 539–548. PMID: 9165386
- Lacroix D, Prendergast PJ. A mechano-regulation model for tissue differentiation during fracture healing: analysis of gap size and loading. J Biomech. 2002; 35: 1163–1171. PMID: 12163306
- Boccaccio A, Lamberti L, Pappalettere C. Effects of aging on the latency period in mandibular distraction osteogenesis: a computational mechano-biological analysis. J Mech Med Biol. 2008; 8: 203–225.
- Checa S, Prendergast PJ. A mechanobiological model for tissue differentiation that includes angiogenesis: A lattice-based modeling approach. Ann Biomed Eng. 2009; 37: 129–145. doi: 10.1007/s10439-008-9594-9 PMID: 19011968
- Sandino C, Checa S, Prendergast PJ, Lacroix D. Simulation of angiogenesis and cell differentiation in a CaP scaffold subjected to compressive strains using a lattice modeling approach. Biomaterials. 2010; 31: 2446–2452. doi: 10.1016/j.biomaterials.2009.11.063 PMID: 19969348
- Mehdizadeh H, Sumo S, Bayrak ES, Brey EM, Cinar A. Three-dimensional modeling of angiogenesis in porous biomaterial scaffolds. Biomaterials. 2013; 34: 2875–2887. doi: 10.1016/j.biomaterials.2012.12. 047 PMID: 23357368
- Bailón-Plaza A, Van Der Meulen MCH. A mathematical framework to study the effects of growth factor influences on fracture healing. J Theor Biol. 2001; 212: 191–209. PMID: https://doi.org//recommons.org/linearing-nch/
- 38. Hendrikson WJ, van Blitterswijk CA, Verdonschot N, Moroni L, Rouwkema J. Modeling Mechanical Signals on the Surface of µCT and CAD Based Rapid Prototype Scaffold Models to Predict (Early Stage) Tissue Development. Biotechnol Bioeng. 2014; 111: 1864–1875. doi: 10.1002/bit.25231 PMID: 24824318
- 39. Rumpler M, Woesz A, Dunlop JW, van Dongen JT, Fratzl P. The effect of geometry on three-dimensional tissue growth. J. R. Soc. Interface. 2008; 5: 1173–1180. doi: 10.1098/rsif.2008.0064 PMID: 18348957
- Karageorgiou V, Kaplan D. Porosity of 3D biomaterial scaffolds and osteogenesis. Biomaterials. 2005; 26: 5474–5491. PMID: 15860204
- Yang SF, Leong KF, Du ZH, Chua CK. The design of scaffolds for use in tissue engineering. Part 1, traditional factors. Tissue Eng. 2001; 7: 679–689. PMID: <u>11749726</u>
- 42. Yavari SA, van der Stok J, Ahmadi S, Wauthlé R, Schrooten J, Weinans H, et al. Mechanical analysis of a rodent segmental bone defect model: The effects of internal fixation and implant stiffness on load transfer. J Biomech. 2014; 47: 2700–2708. doi: 10.1016/j.jbiomech.2014.05.006 PMID: 24882739