

1 **Title (15/15 words):** Mean daily temperatures can predict the thermal limits of malaria  
2 transmission better than rate summation

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18 **Abstract (200/200 words)**

19 Temperature shapes the distribution, seasonality, and magnitude of mosquito-borne disease  
20 outbreaks. Mechanistic models predicting transmission often use mosquito and pathogen thermal  
21 responses from constant temperature experiments. However, mosquitoes live in fluctuating  
22 environments. Rate summation (nonlinear averaging) is a common approach to infer performance  
23 in fluctuating environments, but its accuracy is rarely validated. We measured three mosquito traits  
24 that impact transmission (bite rate, survival, fecundity) in a malaria mosquito (*Anopheles*  
25 *stephensi*) across temperature gradients with three diurnal temperature ranges (0, 9 and 12°C). We  
26 compared thermal suitability models with temperature-trait relationships observed under constant  
27 temperatures, fluctuating temperatures, and those predicted by rate summation. We mapped results  
28 across *An. stephensi*'s native Asian and invasive African ranges. We found: 1) daily temperature  
29 fluctuation significantly altered trait thermal responses; 2) rate summation partially captured  
30 decreases in performance near thermal optima, but also incorrectly predicted increases near  
31 thermal limits; and 3) while thermal suitability characterized across constant temperatures did not  
32 perfectly capture suitability in fluctuating environments, it was more accurate for estimating and  
33 mapping thermal limits than predictions from rate summation. Our study provides insight into  
34 methods for predicting mosquito-borne disease risk and emphasizes the need to improve  
35 understanding of organismal performance under fluctuating conditions.

## 36 **Introduction**

37 Malaria remains one of the biggest global public health burdens, despite substantial control efforts.  
38 In 2022 alone, there were 249 million cases and 580,000 deaths worldwide, mostly of children  
39 under five years of age (76% of deaths) and occurring in Africa (94% of cases)<sup>1</sup>. Further, global  
40 climate change and land use change are altering the environments where malaria is transmitted,  
41 shifting the times of year and geographic regions that are environmentally suitable for malaria  
42 transmission<sup>2-7</sup>. Over the past 20 years, we have gained substantial mechanistic insight into how  
43 key abiotic environmental variables—including temperature—shape malaria risk<sup>2,6,8-12</sup>. Because  
44 mosquitoes are ectothermic, temperature has strong effects on the vital rates of both the mosquito  
45 and the parasite. These effects shape mosquito population dynamics, the ability of the mosquito to  
46 become infected and transmit, and the parasite development rate, all of which in turn influence  
47 malaria transmission dynamics. Thus, a mechanistic determination of how temperature will alter  
48 the distribution and abundance of mosquito vectors, as well as people's potential exposure to  
49 malaria-infectious mosquitoes, will be critical for accurately anticipating how the environmental  
50 suitability for malaria transmission will respond to current and future global change.

51 Previous empirical work has focused on characterizing the effects of temperature on  
52 mosquito and parasite traits that are relevant for transmission across a diversity of mosquito-borne  
53 disease systems<sup>4</sup>. In general, temperature-trait relationships have a kinetic profile akin to an  
54 enzymatic reaction<sup>13,14</sup>. Performance is constrained by a lower and upper temperature threshold  
55 ( $T_{min}$  and  $T_{max}$ , respectively) and gradually increases with temperature to an optimal value ( $T_{opt}$ ) as  
56 enzymatic and biochemical processes become more efficient. Performance then declines as  
57 temperatures warm away from the  $T_{opt}$ , presumably because enzymatic reactions become less  
58 efficient as protein stability declines, followed by performance failure or organism death as

59 temperatures approach the  $T_{max}$ <sup>15–18</sup>. Collectively, these responses give us temperature-trait  
60 relationships known as thermal performance curves (TPCs) that have been used extensively across  
61 diverse organisms to infer ecological and evolutionary outcomes. These TPCs are typically  
62 characterized by estimating a trait (e.g. bite rate, mortality rate, development rate) across a gradient  
63 of constant temperatures in a controlled laboratory study<sup>13</sup>. For modeling mosquito-borne diseases,  
64 the TPCs are then often incorporated either into standard formulae for the pathogen’s basic  
65 reproduction number ( $R_0$ ; defined as the number of secondary cases arising from a primary case  
66 introduced into a fully susceptible population) to predict overall thermal suitability for  
67 transmission<sup>2,8,9,19</sup>, or into mechanistic dynamical models used to predict human incidence or the  
68 final epidemic size<sup>20,21</sup>. These approaches have generated many important insights, including: 1)  
69 warming at northern latitudes or high elevations has increased and will continue to increase  
70 suitability for transmission due to longer and more intense transmission seasons, resulting in the  
71 potential for large epidemics<sup>3,7</sup>; 2) areas of the world that are currently suitable for transmission  
72 may become less environmentally suitable as temperatures warm beyond the optimum<sup>3,22</sup>; 3)  
73 disease intervention efforts (e.g. vector control, vaccination, drug coverage) will need to be more  
74 expansive in areas of the world and times of year that are most suitable for transmission<sup>3,23,24</sup>; and  
75 4) climate change could shift disease burden from malaria to arboviruses in Africa<sup>25</sup>.

76         Although controlled laboratory studies have provided insight into the effects of temperature  
77 on mosquito life history, mosquito-pathogen interactions, and overall transmission potential, the  
78 temperatures that organisms experience in the field are highly variable, fluctuating diurnally,  
79 seasonally, annually, and on other timescales<sup>26</sup>. A consequence of the mathematical fact known  
80 as ‘Jensen’s inequality’ is that when temperature impacts performance non-linearly, then the time-  
81 average of performance across a thermally fluctuating environment is not equal to the performance

82 measured at the average temperature<sup>27–29</sup>. Specifically, thermal fluctuations should increase  
83 performance in accelerating (convex) portions of a TPC and decrease performance in decelerating  
84 (concave) portions (**Figure 1B**), simply based on the time spent at each temperature and the  
85 associated performance predicted by the TPC. This theoretical prediction is supported by a  
86 growing body of empirical research across diverse taxa<sup>30–34</sup>, including mosquitoes<sup>35–37</sup>,  
87 demonstrating that trait performance under fluctuating temperatures can differ substantially from  
88 performance at constant temperatures.

89 Unfortunately, it is logistically infeasible to experimentally evaluate every possible  
90 fluctuating temperature regime that an organism might experience. Accordingly, studies typically  
91 use ‘non-linear averaging’ or ‘rate summation’ to quantitatively predict the average trait  
92 performance as temperature fluctuates over time<sup>27,30,38–41</sup> (**Equation 1**).

$$\langle f \rangle = \frac{1}{n} \sum_{t=1}^n f [T [t]]$$

Eq. 1

93 Here,  $\langle f \rangle$  is the average performance of a trait, and is calculated from  $f$ , the trait performance as  
94 a function of temperature ( $T$ ), which in turn is a function of time ( $t$ ) from  $t=1$  to  $t=n$ . This  
95 approach has been adopted widely to account for the impact of temperature variation on the  
96 thermal suitability of transmission in many vector-borne disease systems<sup>10,35,42–48</sup>.

97 However, rate summation makes two simplifying assumptions that are likely to be  
98 violated in many biological systems: 1) traits always exhibits the same value at a given  
99 temperature in both fluctuating and constant environments; and 2) performance changes  
100 instantaneously with temperature (i.e., no acclimation period). First, performance in fluctuating  
101 environments can differ from in the equivalent constant temperatures due to the inherent effects  
102 of thermal fluctuations on organismal performance<sup>49</sup>, including acclimation to thermal  
103 stress<sup>13,50,51</sup>, accumulation of damage associated with thermal stress<sup>52,53</sup>, and processes to repair  
104

105 damage incurred at extreme low or high temperatures during time spent at more favorable  
106 temperatures (e.g. production of heat shock proteins) that cause hysteresis effects<sup>51,54,55</sup>. Second,  
107 time lags and other thermal acclimation effects are common and varied in their impact on  
108 performance<sup>56</sup>. Although the accuracy of rate summation has been assessed in other  
109 organisms<sup>28,30,39,49</sup>, it has not been evaluated for vector-borne disease systems. Furthermore,  
110 because rate summation has mixed success in predicting performance of traits, it is unclear  
111 whether rate summation can accurately predict suitability for mosquito-borne disease  
112 transmission. Evaluating the ability of rate summation to capture the thermal suitability of  
113 realistically fluctuating conditions has important implications for understanding how mosquito  
114 populations and their transmission dynamics will play out in natural field settings, as well as in  
115 response to future climate change.

116 In this study, we use experimental data and modeling (**Figure 1**) to better understand the  
117 use of rate summation to predict the thermal suitability for malaria transmission by *Anopheles*  
118 *stephensi*, an important mosquito vector of urban malaria in South Asia and now Africa.  
119 Specifically, we ask: 1) Do field-relevant diurnal temperature fluctuations alter the relationships  
120 between temperature and adult mosquito life history traits compared to those characterized across  
121 constant temperatures? 2) Can rate summation accurately predict these temperature-trait  
122 relationships in environments that diurnally fluctuate? 3) How do these various temperature-trait  
123 relationships scale up to impact predicted thermal suitability for malaria transmission? Our results  
124 show that temperature fluctuations significantly alter the thermal responses of adult mosquito  
125 traits, that rate summation largely fails to predict the performance of these traits, and that this  
126 discrepancy impacts the predicted thermal limits for malaria transmission. We discuss reasons for  
127 why rate summation might fail to predict performance in a fluctuating environment and the

128 implications for using this technique in mechanistic modeling frameworks that predict vector-  
129 borne disease transmission.

130

## 131 **Study and Suitability Model Overview**

132 We modeled the effects of diurnal temperature fluctuation on predicted thermal suitability  
133 for transmission of malaria,  $S(T)$ , using a trait-based mechanistic model based on a standard  
134 derivation of  $R_0$  for malaria (**Equation 2**, see *Methods*). We focused on the impacts of three adult  
135 mosquito traits that we directly measured across temperature gradients in both constant and  
136 fluctuating conditions: daily female bite rate ( $a$ ), lifetime egg production ( $B$ ), and lifespan ( $lf$ ).  
137 Data for other traits required to calculate  $S(T)$ —larval survival ( $p_{EA}$ ), development rate ( $MDR$ ),  
138 vector competence ( $bc$ ), and extrinsic incubation period ( $EIP$ )—were taken from previous  
139 experimental studies with constant temperature gradients<sup>19,36</sup>. Trait thermal performance curves  
140 (TPCs) were fitted using either a symmetric (quadratic) or asymmetric (Brière) function, chosen  
141 by comparing Deviance Information Criteria (DIC)<sup>67</sup>.

142 We generated five versions of the  $S(T)$  model (**Figure 1**) parameterized with TPCs for traits  
143 either fit to data from three different temperature fluctuation regimes (diurnal temperature range  
144 [DTR] = 0, 9, or 12°C) or calculated via rate summation (RS).

- 145 1. TPCs fit to trait data from across a range of constant temperatures ('constant').
- 146 2. TPCs fit to trait data from fluctuating conditions for the focal traits with empirical data ( $a$ ,  $B$ ,  
147 and  $lf$ ), combined with TPCs fit to trait data from constant temperatures for traits measured in  
148 other studies ( $p_{EA}$ ,  $MDR$ ,  $bc$ , and  $EIP$ ; 'empirical fluctuating').

- 149 3. TPCs generated by applying rate summation to the TPCs from constant temperatures for the  
150 focal traits ( $a$ ,  $B$ , and  $lf$ ); as in version 2, other traits ( $p_{EA}$ ,  $MDR$ ,  $bc$ , and  $EIP$ ) used unmodified  
151 TPCs from constant temperatures ('trait-level RS - 3 traits').
- 152 4. Similar to version 3 above, but rate summation was applied to the TPCs from constant  
153 temperatures for all traits ('trait-level RS - all traits').
- 154 5. Rate summation applied to the TPC for  $S(T)$  generated from traits measured across a range of  
155 constant temperatures (i.e, the output of constant model 1 above) to generate a new TPC for  
156  $S(T)$  (' $S(T)$ -level RS').

157 We used these five versions of  $S(T)$ , generated for both fluctuating DTRs (9 and 12°C) where  
158 applicable, to assess the following questions: A) how thermal suitability is likely affected by  
159 temperature fluctuations (model 1 versus model 2); B) if rate summation can adequately predict  
160 suitability in fluctuating temperature regimes (model 2 versus model 3); and C) how the level at  
161 which rate summation is calculated (on the component traits or on suitability itself) impacts  
162 predictions (model 4 versus model 5).

163

## 164 **Results**

### 165 **Diurnal fluctuation alters the thermal responses of mosquito traits**

166 All three focal traits (bite rate [ $a$ ], lifespan [ $lf$ ], and lifetime egg production [ $B$ ]) responded  
167 strongly to mean temperature (**Figure 2**). The shape of the thermal response was relatively  
168 consistent for each trait across fluctuation treatments (diurnal temperature range [DTR] = 0, 9, or  
169 12°C). Lifespan ( $lf$ ) always responded symmetrically and was best fit with a quadratic function,  
170 while bite rate ( $a$ ) always responded asymmetrically and was best fit with a Brière function.  
171 Lifetime egg production ( $B$ ) was fit similarly by both functions ( $\Delta\text{DIC} < 2.0$  for all fluctuation

172 treatments); we elected to always use a quadratic function to be consistent and because it had a  
173 slightly lower DIC for two of three fluctuation treatments (**Table S1**).

174 Fluctuating temperatures significantly altered the thermal performance curves (TPCs) for  
175 each trait (**Figure 2, Tables 1, S2, and S3**). These changes were reflected by shifts in TPC  
176 characteristics as well as the magnitude of performance in each environment. Diurnal temperature  
177 fluctuations caused downward shifts in three key TPC parameters ( $T_{opt}$ ,  $T_{max}$ , and  $T_{breadth}$ ) and the  
178 magnitude of these shifts depended on the trait. For all three parameters, the shifts were largest for  
179 bite rate ( $a$ ), followed by lifespan ( $lf$ ), and then lifetime egg production ( $B$ ). TPCs characterized  
180 under temperature fluctuations resulted in cooler predicted thermal optima ( $T_{opt}$ ), ranging from  
181 1.2-4.2°C cooler, and thermal maxima ( $T_{max}$ ), ranging from 2.5-5.2°C cooler, depending on the  
182 trait. We were unable to detect any shifts in the thermal minima ( $T_{min}$ ). Consequently, we also  
183 observed a narrowing in thermal breadth ( $T_{breadth}$ ) that ranged from from 2.3-4.5°C depending on  
184 the trait. Differences in TPCs based on the magnitude of fluctuation (i.e., DTR 9°C vs. DTR 12°C)  
185 were only significant for lifespan ( $lf$ ).

186 Fluctuating temperatures also decreased absolute performance for all traits at their thermal  
187 optima and warmer temperatures, relative to trait performance at constant temperatures (**Figure 2,**  
188 **Table 1**). Maximum predicted performance [i.e., trait value at the thermal optimum,  $f(T_{opt})$ ]  
189 decreased more for bite rate ( $a$ ; 23.5-25.1% lower) than for lifespan ( $lf$ ; 2.7% lower to 10.7%  
190 higher) or egg production ( $B$ ; 7.9-14.8% lower). For lifespan ( $lf$ ), fluctuating temperatures  
191 increased performance relative to constant temperatures at 16°C, which increased the maximum  
192 predicted performance for DTR 12°C only.

193

194 **Rate summation fails to predict thermal responses in fluctuating environments**

195 Overall, rate summation failed to accurately predict trait performance in a diurnally  
196 fluctuating thermal environment. Rate summation did not predict the observed shifts in three TPC  
197 parameters ( $T_{opt}$ ,  $T_{max}$ , and  $T_{breadth}$ ) or the maximum predicted performance (**Figure 3, Table 1**). In  
198 fact, for two of the parameters ( $T_{max}$ , and thus also  $T_{breadth}$ ), rate summation predicted that  
199 temperature fluctuations would change performance in a different direction than what was  
200 observed (i.e., it predicted warmer/wider shifts instead of cooler/narrower shifts relative to  
201 performance in constant temperature conditions). Rate summation also predicted small decreases  
202 in  $T_{min}$  under fluctuations, which we did not detect in the TPCs fit to empirical data from fluctuating  
203 conditions.

204 Rate summation overestimated the  $T_{max}$  for bite rate ( $a$ ), lifespan ( $lf$ ), and to some degree  
205 lifetime egg production ( $B$ , for DTR 12°C) (**Figure 3, Table 1**). It predicted increases in the  
206 thermal maxima ( $T_{max}$ ) for all three traits relative to mosquitoes housed in constant temperatures  
207 (2.6-5.4°C warmer). In contrast, mosquitoes housed in fluctuating conditions had cooler  $T_{max}$  for  
208 all traits relative to those housed under constant temperature conditions (2.5-5.2°C cooler). As a  
209 result, rate summation overpredicted the overall thermal breadth ( $T_{breadth}$ ) of trait performance  
210 relative to mosquitoes housed in constant temperatures (5.0-12.0°C warmer), instead of the more  
211 constrained thermal breadth observed for mosquitoes in thermally fluctuating environments (2.3-  
212 4.5°C cooler).

213 Rate summation generally overestimated the  $T_{opt}$  in mosquitoes housed in fluctuating  
214 environments and failed to predict differences compared to those housed in constant temperature  
215 conditions (**Figure 3, Table 1**). This trend was strongest (minimal overlap in credible intervals)  
216 for the daily bite rate ( $a$ ) at DTR 9°C and lifespan ( $lf$ ) for both DTR 9°C and 12°C treatments. For  
217 bite rate ( $a$ ), rate summation underestimated the decrease in the  $T_{opt}$  that was observed in

218 mosquitoes housed under fluctuating thermal conditions relative to constant temperature  
219 conditions (1.0-1.8°C cooler predicted by rate summation vs. 2.4-4.2°C cooler from empirical  
220 data). For lifespan ( $lf$ ) and lifetime egg production ( $B$ ), rate summation predicted essentially no  
221 change in the  $T_{opt}$  from mosquitoes housed at constant temperatures, in contrast to observed  
222 decreases in the  $T_{opt}$  in mosquitoes housed under temperature fluctuations (1.2-2.1°C cooler).

223 In many cases, rate summation also failed to accurately predict absolute trait performance  
224 in fluctuating environments (**Figure 3, Table 1**). In the most extreme example, for daily bite rate  
225 ( $a$ ), rate summation predicted substantially higher maximum trait performance [ $f(T_{opt})$ ] for both  
226 DTR treatments (predictions 16.1-21.1% higher than empirical observations). For lifetime egg  
227 production ( $B$ ) and lifespan ( $lf$ ) in DTR 9°C, rate summation was fairly accurate at predicting small  
228 decreases in maximum trait performance [ $f(T_{opt})$ ; predictions all within 3.7% of empirical  
229 observations]. However, for lifespan ( $lf$ ) in DTR 12°C, rate summation predicted small decreases  
230 in absolute trait performance at cooler temperatures, when TPCs fit to observations yielded  
231 increases in absolute trait performance relative to constant temperatures.

232

### 233 **Diurnal temperature fluctuation impacts the predicted suitability for transmission**

234 The effects of fluctuating temperatures on the three adult mosquito traits measured here  
235 lowered the predicted suitability for transmission,  $S(T)$ , at warmer temperatures (**Figure 4A, Table**  
236 **2**). As a result, model 2 (empirical fluctuating) lowered the predicted  $T_{opt}$  by 1.2-1.4°C,  $T_{max}$  by  
237 0.8-1.8°C, thermal breadth by 0.8-1.2°C, and predicted amount of suitability at  $T_{opt}$  by 32.0-33.8%  
238 (**Table 2**) compared to model 1 (constant). Applying rate summation to the trait TPCs to predict  
239 performance of the three adult mosquito traits in thermally fluctuating environments (model 3:  
240 trait-level RS - 3 traits) did not capture these effects (**Figure 4B**). This model predicted much

241 smaller changes in  $T_{opt}$  (0.1-0.2°C lower), no change in  $T_{max}$  or the thermal breadth, and smaller  
242 reductions in suitability at  $T_{opt}$  (10.0-17.1% lower) (**Table 2**), therefore overestimating suitability  
243 near and above the thermal optimum compared to model 2 based on empirical observations.  
244 Finally, the level at which the rate summation calculation was performed (on all seven traits prior  
245 to calculating suitability [model 4: Trait-level RS - all traits] or directly on the suitability curve  
246 [model 5:  $S(T)$ -level RS]) visually impacted the curves for predicted suitability (**Figure 4C**), but  
247 had little impacts on the key values of the TPCs ( $T_{min}$ ,  $T_{opt}$ ,  $T_{max}$ ,  $T_{breadth}$ ) or the predicted reduction  
248 in suitability at  $T_{opt}$  (18.1-32.0% lower) (**Table 2**). Performing rate summation on the  $S(T)$  curve  
249 yielded a TPC that was wider and predicted higher suitability at temperatures near the thermal  
250 margins (**Figure 4C**). However, this difference was not reflected in the values for  $T_{min}$  or  $T_{max}$ ,  
251 which were identical for a given level of diurnal temperature variation (DTR), because the  
252 suitability curves for model 5 approached the x-axis extremely gradually. Additionally, the  
253 predicted optimum ( $T_{opt}$ ) and the magnitude of transmission near the optimum was very similar  
254 for both versions of suitability (Trait-level RS: 0.2-0.4°C cooler than constant temperatures,  $S(T)$ -  
255 level RS: 0.1°C warmer or cooler than constant temperatures; **Figure 4C, Table 2**).

256 The sensitivity and uncertainty analyses provide insight into which traits determine key  
257 characteristics of the TPC for suitability ( $T_{min}$ ,  $T_{opt}$ , and  $T_{max}$ ) and drive uncertainty across the  
258 temperature gradient (**Figures S1, S2 and S3**). For all suitability models, as temperature increases,  
259 lifespan ( $lf$ ) is most important for lowering  $T_{opt}$  while bite rate ( $a$ ) and development rate ( $MDR$ )  
260 are most important for raising  $T_{opt}$  (**Figures S1 and S2**). Together, these traits most strongly  
261 influence the optimal temperature for transmission ( $T_{opt}$ ), consistent with previous studies<sup>4</sup>. In  
262 model 1 (constant),  $T_{min}$  and  $T_{max}$  are both determined by larval traits not measured in this study  
263 (larval survival [ $p_{EA}$ ] and development rate [ $MDR$ ], respectively). The TPC for development rate

264 [MDR] has very little uncertainty in its  $T_{max}$ , which leads to similarly low uncertainty for the  $T_{max}$   
265 of suitability. Most of the uncertainty in model 1 is generated by lifetime egg production ( $B$ ) near  
266  $T_{opt}$  and by vector competence ( $bc$ ) near both thermal margins (**Figure S3**).

267 By contrast, in model 2 (empirical fluctuating),  $T_{max}$  for suitability is determined primarily  
268 by the effects of temperature on mosquito lifespan ( $lf$ ), and then lifetime egg production ( $B$ ), as the  
269  $T_{max}$  for both of those traits decrease below the  $T_{max}$  for development rate (MDR; **Figures S1** and  
270 **S2**). Larval survival ( $p_{EA}$ ) still determines  $T_{min}$  and uncertainty in vector competence and lifetime  
271 egg production ( $B$ ) are still most important near the lower thermal limit and optimum, respectively.  
272 However, near the upper thermal limit, most of the uncertainty is now due to lifetime egg  
273 production ( $B$ ) and lifespan ( $lf$ ; **Figure S3**). Model 3 (trait-based RS - 3 traits) retains the effects  
274 of the unmodified TPCs for larval survival ( $p_{EA}$ ) and development rate (MDR) from model 1  
275 (constant), which again determine  $T_{min}$  and  $T_{max}$ , respectively (**Figures S1** and **S2**). Models 4 (trait-  
276 level RS - all traits) and 5 (S(T)-level RS) preserve the importance of these two larval traits for  
277 determining  $T_{min}$  and  $T_{max}$ , but the rate summation calculation changes the specific temperature at  
278 which  $T_{min}$  and  $T_{max}$  occur. Models 3, 4, and 5 also retain the uncertainty patterns from model 1:  
279 lifetime egg production ( $B$ ) is most important near  $T_{opt}$  and vector competence ( $bc$ ) is most  
280 important near both thermal margins (**Figure S3**).

281

## 282 **Mapping predicted suitability for transmission**

283 Differences in the predicted thermal suitability can be visualized on maps showing the  
284 number of months predicted to have temperatures suitable for transmission,  $S(T) > 0.001$ , in both  
285 the native zone (Central and South Asia; **Figure 5** left column) and introduced zone (Africa;  
286 **Figure 6** left column) for *An. stephensi*. The constant temperature model for suitability (model 1),

287 predicts that India is suitable for malaria transmission year round (**Figures 5A**), as is much of  
288 Africa (**Figure 6A**). The empirical fluctuations model for suitability (model 2) shows a slightly  
289 shorter transmission season in Northern India and Pakistan (**Figure 5B**) and in Northern Africa  
290 (**Figure 6B**), due to its cooler  $T_{max}$  value (**Table 3**). Both suitability models based on rate  
291 summation calculations (model 4: trait-level RS and model 5:  $S(T)$ -level RS) yielded  $T_{min}$  values  
292 that were much cooler than models 1 and 2 (**Table 3**), and thus produced maps with predicted  
293 year-round transmission across all of India (**Figure 5C-D**) and nearly all of Africa (**Figure 6C-**  
294 **D**). Compared to the constant and empirical fluctuating models, both rate summation models  
295 predicted much longer transmission seasons in Northern India, Pakistan, and Iran (**Figure 6C-D**),  
296 as well as in Northern and Southern Africa (**Figure 7C-D**). Overall, the predictions from the  
297 constant temperature model were more like those from the empirical fluctuating model, while the  
298 predictions from both rate summation models diverged more (**Figures 5 and 6 left columns, Table**  
299 **3**).

300 Both suitability models based on rate summation calculations (model 4: Trait-level RS and  
301 model 5:  $S(T)$ -level RS) yielded nearly identical results for  $S(T) > 0.001$  (**Figures 5 and 6**).  
302 However, even though the  $T_{min}$  and  $T_{max}$  of thermal suitability is predicted to be the same across  
303 both models, there are clearly differences in the rate at which temperatures increase from or  
304 decrease toward the  $T_{min}$  and  $T_{max}$ , respectively, across models. When we use a higher threshold  
305  $S(T) > 0.5$ , for where the thermal suitability is relatively high (**Figures 5 and 6 right columns**),  
306 performing rate summation on the TPC for suitability (model 5, **Figure 5D and 6D**) predicts more  
307 areas with relatively high thermal suitability year-round than performing rate summation on the  
308 TPCs of the component traits (model 4, **Figure 5C and 6C**). For this higher threshold, performing  
309 rate summation at the trait-level produced maps that were quite like both empirical models

310 (constant and fluctuating), while performing rate summation directly on the suitability TPC did  
311 not (**Figures 5 and 6** right columns, **Table 3**).

312

## 313 **Discussion**

314 This study measured and analyzed adult mosquito life history traits (lifespan, bite rate, and  
315 lifetime reproductive output) for the urban Asian malaria vector *Anopheles stephensi* across a  
316 temperature gradient under three daily temperature range (DTR) regimes (0, 9, and 12°C). We  
317 used these data to determine if standard modeling techniques could accurately predict the impact  
318 of biologically relevant daily temperature fluctuations on mosquito performance and  
319 environmental suitability for malaria transmission. We found that: 1) daily temperature fluctuation  
320 significantly altered the thermal responses for these critical mosquito traits involved in pathogen  
321 transmission; 2) rate summation (RS), a non-linear averaging approach used to estimate the effect  
322 of temperature fluctuations using thermal performance curves (TPCs) characterized in constant  
323 temperature environments, did not accurately predict trait thermal responses in diurnally  
324 fluctuating temperature environments; and 3) while thermal suitability predictions constructed  
325 with responses from constant temperature conditions did not capture the impact of real-world  
326 temperature variation on mosquito traits, they were substantially more accurate for predicting and  
327 mapping the thermal limits of malaria transmission than predictions constructed using rate  
328 summation calculations. This result stems from a general property of performing rate summation  
329 on TPCs that cut-off at the x-axis, as is often the case for biological traits that cannot take negative  
330 values. Thus, we conclude that while daily-scale temperature fluctuations have important impacts  
331 on organismal performance, for some applications it may be better to use thermal responses fit  
332 under constant temperature environments than to try to incorporate the impact of fluctuating

333 temperatures using non-linear averaging. Additionally, it is vital to improve methods of estimating  
334 the physiological effects of temperature fluctuation in real-world situations to accurately predict  
335 the thermal suitability for transmission of vector-borne diseases under realistic temperature  
336 regimes.

337         Daily temperature fluctuations significantly altered the thermal responses for all three adult  
338 mosquito traits studied here, primarily by reducing performance at temperatures near and above  
339 the thermal optimum. The reduced performance at warmer temperatures resulted in cooler upper  
340 thermal limits ( $T_{max}$ ) and thermal optima ( $T_{opt}$ ), and narrower thermal breadths, without a detectable  
341 impact on lower thermal limits ( $T_{min}$ ) (**Figure 2, Table 1**). Fluctuations also increased lifespan in  
342 our coldest mean temperature treatment (16°C). Our results contribute to a growing body of  
343 literature demonstrating that daily temperature fluctuations affect the life history of ectothermic  
344 organisms in ways not captured by constant mean temperature gradients<sup>28,30–32,39,49,51,57–59</sup>,  
345 including for mosquitoes and their associated pathogens<sup>26,35–37,60–62</sup>. The effect of temperature  
346 fluctuations on performance depends strongly on the mean temperature over which the fluctuation  
347 is occurring. Typically, fluctuations impair processes at the warmer end of the reaction norm and  
348 boost processes at the cooler end, resulting in cooler temperatures for both the  $T_{opt}$  and  $T_{max}$ , similar  
349 to our results. This general pattern is supported by three meta-analyses<sup>28,57,58</sup> and frequently  
350 observed (albeit with some exceptions) in studies from medically important mosquitoes<sup>35–37,61</sup> and  
351 other host-parasite systems<sup>31,47</sup> (see **Table 4**). Collectively, these results suggest that whether  
352 fluctuations rescue or decrease performance is dependent on the mean temperature and the duration  
353 of time an organism remains beyond its thermal limits. Overall, our findings reinforce the pattern  
354 found in these previous studies: while fluctuations often reduce performance at warmer  
355 temperatures and increase it at cooler temperatures, there are also frequent exceptions to this rule.

356 Rate summation (RS) did not accurately predict trait values in diurnally fluctuating  
357 temperature environments in our study. Rate summation did predict reductions in performance  
358 near the thermal optima, but in many cases only captured a small proportion of the observed  
359 decrease (i.e. the direction of the effect was correct, but the magnitude was too small) (**Figure 3,**  
360 **Table 1**). Rate summation also predicted increases in performance near the thermal margins,  
361 yielding wider thermal breadths than what was observed, with both warmer  $T_{max}$  and cooler  $T_{min}$   
362 values (i.e., the wrong direction of effect on  $T_{max}$ ). Finally, for our coldest mean temperature (16°C)  
363 and highest DTR (12°C), we observed lifespans that were higher than the maximum value  
364 observed for constant temperatures (i.e., at the  $T_{opt}$ ), something that is impossible to occur using  
365 rate-summation predictions. Few studies have quantitatively tested the predictions made by rate  
366 summation for how temperature fluctuation will alter organismal performance. One study using a  
367 green alga found that rate summation accurately predicted population growth rates in fluctuating  
368 conditions<sup>30</sup>. However, three studies on animals found that nonlinear averaging did not accurately  
369 predict performance of larval development and growth in frogs<sup>39</sup>, of short-term and long-term  
370 growth rates in tobacco hornworms<sup>49</sup>, and of development rate in coffin flies<sup>28</sup>. Alternatively, some  
371 studies compare their results qualitatively (i.e., did fluctuations increase or decrease performance)  
372 with general predictions based on Jensen's Inequality and the concavity of the TPC. These studies  
373 typically find that the predicted change in trait value successfully matches the observed direction  
374 of trait change<sup>51,63</sup> (but there are exceptions<sup>59</sup>). Thus, our findings once again reinforce general  
375 patterns from the literature: trait values measured under fluctuating conditions often qualitatively  
376 match the predicted changes compared to constant temperatures based on Jensen's Inequality and  
377 the concavity of TPCs, but they rarely quantitatively match the specific values predicted by rate  
378 summation calculations.

379 Predicted thermal suitability for malaria transmission varied substantially among our four  
380 models (**Figure 4, Table 3**). These differences mirrored the trait-level results: empirical  
381 fluctuations (model 2) decreased  $T_{opt}$  and  $T_{max}$  compared to constant temperatures (model 1), while  
382 rate summation (models 4 and 5) predicted little change in  $T_{opt}$ , increases in  $T_{max}$ , and decreases in  
383  $T_{min}$ . Although rate summation appeared to predict the decrease in suitability at  $T_{opt}$  quite accurately  
384 (**Table 3**), we note that our empirical model only accounts for the impact of fluctuations on our  
385 three focal traits, while the rate summation models simulate the impact of fluctuations on all seven  
386 traits. Thus, rate summation may still be only partially capturing the impact of fluctuating  
387 temperatures near the thermal optimum. We also found that the level at which rate summation was  
388 conducted had a large impact on predicted suitability near both thermal limits (i.e., on component  
389 traits versus on the TPC for suitability, model 4 versus model 5, respectively; **Figure 4C**). Studies  
390 on mosquito-borne disease generally perform rate summation on component traits<sup>42–44,46</sup> or have  
391 ambiguously written methods<sup>48</sup>, but a recent study on temperature-dependent transmission of  
392 schistosomiasis performed rate summation directly on the TPC for  $R_0$ <sup>47</sup>.

393 The variation in the suitability models' thermal limits generated substantial differences in  
394 the predicted length of transmission seasons and geographic areas predicted to be suitable for year-  
395 round transmission (**Figures 5 and 6**, left columns). For our main mapping approach (number of  
396 months with  $S(T) > 0.001$ ), constant temperatures (model 1) approximated empirically fluctuating  
397 temperatures (model 2) extremely well, since those models had the same thermal minima ( $T_{min}$ ).  
398 By contrast, both rate summation models (4 and 5) overpredicted the geographic area with year-  
399 round suitability for transmission due to their much cooler  $T_{min}$ . The models' upper thermal limits  
400 ( $T_{max}$ ) were not important here, since current monthly mean temperatures did not exceed them;  
401 however, they could begin to limit suitability under future climate change projections.

402 To our knowledge, this study is the first to attempt to validate the accuracy of rate  
403 summation in predicting the effects of thermal variation on mosquito and pathogen life history,  
404 and to explore the implications for predicted transmission. Unfortunately, our results suggest that  
405 these studies are likely overestimating transmission near  $T_{max}$ , and possibly near  $T_{min}$  as well. These  
406 areas of the TPC correspond to locations where the impacts of climate change on transmission are  
407 predicted to be felt most strongly, as cooler areas become newly suitable and hotter areas become  
408 unsuitable<sup>3,7</sup>. We found two studies that used rate summation to estimate the thermal response of  
409 transmission under multiple diurnally fluctuating conditions. Similar to our study, one predicted  
410 that fluctuations would increase the  $T_{max}$  of transmission<sup>48</sup>, contrary to the decreases in  $T_{max}$   
411 observed in our study and that better correspond to the broader literature (**Table 4**). The other  
412 study provided results for a limited range of temperatures that stopped well below  $T_{max}$  (at 28°C)  
413 and could not be compared<sup>10</sup>.

414 Overall, our suitability results are concerning: they demonstrate that rate summation  
415 calculations can systematically distort the thermal limits of TPCs and increase their thermal  
416 breadth, and yet many predictive models for mosquito-borne diseases use it to account for the  
417 impacts of temperature fluctuations on mosquito and pathogen traits that are important for  
418 transmission<sup>10,35,42–46,48</sup>. We recommend caution when applying rate summation to organismal  
419 performance and models for disease transmission (or other processes) in cases where empirical  
420 responses to fluctuating temperatures are not available. Rate summation more accurately estimates  
421 absolute levels of performance or transmission near the thermal optimum, which can be important  
422 for capturing the overall intensity of transmission. However, TPCs measured in constant  
423 temperature conditions may provide more accurate estimates of the thermal limits, which is

424 important for estimating seasonality and the current and future geographic areas suitable for  
425 transmission. (This accuracy likely depends on the specific TPC function used: see below).

426 Many different factors could affect the accuracy of rate summation for predicting  
427 performance under fluctuating temperature conditions. First, the function chosen to fit the TPC  
428 over the constant temperature gradient will strongly influence any predictions from rate summation  
429 because the calculations are very sensitive to the shape and concavity of the thermal response, as  
430 illustrated by Jensen's Inequality<sup>27,40</sup>. Many thermal responses are truncated at zero (including the  
431 quadratic and Brière responses used here) because negative values for traits like lifespan and  
432 fecundity are not biologically meaningful. This truncation, however, inherently creates  
433 accelerating (i.e., convex) portions of the curve, that in turn leads to higher predicted performance  
434 in fluctuating versus constant temperatures for mean temperatures near the thermal margins. TPCs  
435 that are not truncated below zero, such as the Eppley curve used in the study on population growth  
436 for a green alga, do not always predict an increase at the thermal margins using rate summation<sup>30</sup>.  
437 Second, traits that are rate-based (i.e., measured per unit time like development rate, foraging rate,  
438 daily fecundity, etc.) are more likely to show an asymmetrical thermal response<sup>4</sup> and may be more  
439 likely to match the assumptions required for rate summation than traits that are integrated over an  
440 organism's lifetime (e.g., longevity or lifetime fecundity). Third, traits that depend on discrete  
441 events may be determined by the temperatures an organism experiences shortly after those events  
442 occur. For example, the time of day mosquitoes are exposed to *Plasmodium falciparum* parasites  
443 and the portion of the DTR experienced after this exposure significantly alters the proportion of  
444 *Anopheles* mosquitoes that become infectious with malaria<sup>60</sup>. Finally, certain taxa may more  
445 closely match predictions from rate summation than others. For instance, rate summation may  
446 work better in single-celled organisms<sup>30</sup> than in larger, multicellular organisms with more complex

447 tissue-specific responses to temperature stress<sup>32</sup>. From a molecular and cellular biology  
448 perspective, discrepancies between observed performance and predictions from rate summation  
449 may occur due to acclimation/hardening processes or the accumulation of thermal stress and the  
450 energetic costs of repairing damage from extreme hot or cold temperatures<sup>32,50,52,54</sup>.

451 Organismal performance is consistently observed to differ in thermally fluctuating  
452 environments relative to constant temperature environments, thus developing a validated  
453 predictive framework that can accurately approximate trait performance in a fluctuating  
454 environment is essential. Future work should continue characterizing organismal responses in  
455 thermally fluctuating environments, in order to uncover potential patterns related to the type of  
456 trait and organism under study<sup>26</sup>. Additionally, we need more work that integrates phenomena  
457 across biological scales to mechanistically understand the cellular and molecular responses to  
458 thermal acclimation and stress that dictate the temperature constraints on organismal performance.  
459 Finally, while this study investigated the impact of thermal fluctuations on a single strain of  
460 mosquitoes in the adult stage, more work is needed to investigate how other environmental factors  
461 (e.g., food resources, competition, humidity) and genetic variation (e.g., thermal plasticity) affect  
462 organismal performance in thermally variable environments<sup>6,50,64,65</sup>.

463 In conclusion, realistic temperature fluctuations over the daily cycle can have significant  
464 impacts on organismal performance, including for mosquito vectors of human parasites like  
465 malaria. However, current approaches for quantitatively modeling the effect of temperature  
466 fluctuations using nonlinear averaging often fail to adequately predict performance under  
467 fluctuating conditions. Our thermal suitability model based on data from constant temperatures  
468 was more accurate for mapping the thermal limits for malaria transmission than the model  
469 parameterized via rate summation. Thus, for some applications it may be better to simply use

470 thermal responses fit under constant temperature environments than to try to incorporate the impact  
471 of fluctuating temperatures using non-linear averaging. Future studies should carefully consider  
472 whether nonlinear averaging is likely to improve the accuracy of their results based on their  
473 specific goals. Meanwhile, more work is needed to improve methods for estimating the  
474 physiological effects of temperature fluctuation in real-world situations to more accurately predict  
475 organismal performance and disease transmission under realistic temperature regimes.

476

## 477 **Materials & Methods**

### 478 **Mosquito husbandry**

479 *Anopheles stephensi* mosquitoes (urban type form originally sourced from Walter Reed  
480 Army Institute of Research, Silver Spring, MD, USA) were reared at standard insectary conditions  
481 ( $27^{\circ}\text{C} \pm 0.5^{\circ}\text{C}$ ,  $80\% \pm 5\%$  relative humidity, and a 12L:12D photoperiod) prior to the life table  
482 experiment, as described previously<sup>8</sup>. Briefly, we hatched immature mosquito larvae from eggs  
483 and placed 110 individuals into plastic trays (6 Qt., 12.4 cm x 34.6 cm x 21.0 cm) containing  
484 500mL of distilled water. Food (100mg ground TetraMin fish flakes) was provided daily until  
485 most individuals reached the pupal stage. Pupae were rinsed and transferred to water-containing  
486 cups placed inside adult mosquito mesh cages for eclosion. For adult colony maintenance, *An.*  
487 *stephensi* were provided 5% dextrose and 0.05% para-amino benzoic acid (PABA) and fed whole  
488 human blood (O+, healthy male < 30 years, Interstate Blood Bank, TN, USA) via water-jacketed  
489 hog intestine membrane feeders to support reproduction.

490

### 491 **Experimental design**

492 We adopted a similar experimental design as in <sup>8</sup>, where we previously measured *An.*  
493 *stephensi* (urban type form) life history traits at six constant temperatures (16°C, 20°C, 24°C, 28°C,  
494 32°C, and 36°C). Here, we programmed incubators (Percival; Perry, Iowa) to follow a Parton-  
495 Logan model <sup>66</sup> for hourly diurnal temperature ranges (DTR) that are relevant for *P. falciparum*  
496 transmission in a natural setting (DTR of 9°C or 12°C) around five of the mean temperatures  
497 (16°C, 20°C, 24°C, 28°C, 32°C ± 0.5°C) explored previously <sup>8</sup> (see **SI Methods**). All other  
498 incubator settings (80% ± 5 RH, and 12L:12D photoperiod) and experimental procedures were the  
499 same to allow for direct comparison between results. All experimental work for both studies was  
500 conducted during 2016-2018 at the University of Georgia (USA).

501 To generate a cohort of age-matched individuals, we collected pupae present at day nine  
502 post-hatch (when most immature mosquitoes reached the pupal stage) and placed them in an  
503 eclosion container within an adult cage for 24hr. We provided a sugar solution (5% dextrose and  
504 0.05% para-amino benzoic acid) to co-housed age-matched adults for three days prior to starting  
505 the lifetable experiment to permit mating. The lifetable experiment was initiated by providing  
506 females with an initial blood meal for 15 min, randomly sorting 300 blood-fed females into  
507 individual housing (16oz. paper cup with mesh top), and then randomly assigning 30 individuals  
508 to each temperature treatment.

509 Each day until found dead, individuals were provided with a whole human blood meal for  
510 15 minutes and inspected visually for imbibed blood. Oviposition sites (secured petri dish  
511 containing water saturated cotton and filter paper) within each individual housing were rehydrated  
512 and checked daily for eggs; if present, eggs were removed and counted. We terminated the  
513 experimental block when either all mosquitoes had died or when at most four mosquitoes remained  
514 alive at 16°C. The life table experiment for each fluctuation regime was performed two

515 independent times resulting in data from a total of 600 individuals. Life table data collected across  
516 constant temperatures from the previous study by our group consisted of 390 individuals across  
517 six constant temperatures <sup>8</sup>.

518

### 519 **Fitting Thermal Performance Curves (TPCs)**

520 For each combination of trait (lifetime measures of bite rate [ $a$ ], lifespan [ $lf$ ], and egg  
521 production [ $B$ ]) and fluctuation regime (constant, DTR 9°C, and DTR 12°C), we used a Bayesian  
522 framework to fit either a symmetric (quadratic:  $-c(T-T_{min})(T-T_{max})$ ) or an asymmetric (Brière:  $cT(T-$   
523  $T_{min})(T_{max}-T)^{1/2}$ ) non-linear unimodal function to generate a TPC predicting trait values across  
524 temperature ( $T$ , in degrees Celsius). From these functions, we can compare the predicted thermal  
525 limits ( $T_{min}$ ,  $T_{max}$ ) and optimum temperature ( $T_{opt}$ ) for each trait among the different DTR  
526 treatments, with  $c$  as a shape fit parameter. Both functions were restricted from becoming negative  
527 by assuming a trait value to be zero if  $T < T_{min}$  or  $T > T_{max}$ . The previous study<sup>8</sup> analyzed only the  
528 constant temperature treatments and fit trait thermal responses to means from each experimental  
529 block using a truncated normal distribution. Here, we used the full dataset of three DTR treatments  
530 and fit the trait thermal responses to individual-level data, using different probability distributions  
531 for each trait based on the data type and observed distribution. For bite rate ( $a$ ), we used a normal  
532 distribution truncated at zero; for lifespan ( $lf$ ), we used a gamma distribution; for lifetime egg  
533 production ( $B$ ), we used a negative binomial distribution (see **SI Methods** for model  
534 specifications).

535 For each trait, we selected the best-fitting functional form (quadratic or Brière) using the  
536 Deviance Information Criterion (DIC)<sup>67</sup>. For each parameter in the mean response function (i.e.,  
537  $c$ ,  $T_{min}$ ,  $T_{max}$ ) and the additional parameter required to specify each probability distribution (i.e.,

538 the variance for the truncated normal distribution, the rate parameter for the gamma distribution,  
539 and the  $r$  parameter for the negative binomial distribution), we assumed low-information uniform  
540 priors ( $T_{min} \sim \text{uniform}(0, 20)$ ,  $T_{max} \sim \text{uniform}(28, 45)$ ,  $c \sim \text{uniform}(0, 10)$ , variance  $\sim \text{uniform}$   
541  $(0, 1000)$ , rate  $\sim \text{uniform}(1, 100)$ ,  $r \sim \text{uniform}(1, 100)$ ) that restricted the range of parameters to  
542 biologically or statistically meaningful values. TPCs were fitted in R using JAGS/R2jags<sup>68,69</sup>,  
543 which implements Markov Chain Monte Carlo (MCMC). Posterior draws were obtained from  
544 three concurrent Markov chains. In each chain, a 5,000-step burn-in phase was followed by 20,000  
545 samples of the stationary chain, for a total of 60,000 posterior samples. These samples were thinned  
546 by saving every eighth sample (yielding 7,500 samples) to reduce autocorrelation in the chain. For  
547 each TPC, we used the posterior distributions for the parameters to generate posterior distributions  
548 over a temperature gradient from 0-45°C at 0.1°C intervals, which we then used to calculate the  
549 mean, median, and 95% credible intervals.

550 To test for the statistical significance of fluctuation treatment, we used the Deviance  
551 Information Criterion (DIC) output from JAGS. For each trait, we compared: 1) the sum of DIC  
552 values for the three models fit separately to data from each treatment (constant, DTR 9°C, and  
553 DTR 12°C) and 2) the DIC of a model fit to the combined data from all treatments. Fluctuation  
554 treatment is significant if the sum of the separate models is  $\geq 2$  DIC units lower than the DIC  
555 value for the combined model.

556

### 557 **Generating TPCs with rate summation**

558 To calculate the trait thermal responses predicted by rate summation (**Equation 1**) we used  
559 the 7,500 posterior samples from the Bayesian fitted TPCs for each trait measured at constant  
560 temperatures. First, we used a Parton-Logan model<sup>66</sup> to calculate a temperature profile for each

561 mean temperature spanning 0-50°C with 0.1°C increments, assuming a DTR of 9 or 12°C across  
562 a 24-hour period (see **SI Methods**). Second, we calculated predicted trait values at each hour using  
563 the TPC for trait performance at constant temperatures. Third, a daily mean value for each trait  
564 was calculated by averaging the predicted hourly values for that trait over the 24-hour period for  
565 each mean temperature. When fluctuating temperatures extended beyond the range of our constant  
566 temperature TPCs ( $0^{\circ}\text{C} \geq T \leq 45^{\circ}\text{C}$ ), we used the trait value predicted at the corresponding edge  
567 temperature, which was always equal or approximately equal to zero. Lastly, since rate summation  
568 was conducted for each posterior sample, we calculated the mean, median, and 95% credible  
569 interval of the resulting rate summation estimates for each mean temperature.

570

### 571 **Predicting thermal suitability, $S(T)$**

572 Following previous work<sup>8</sup>, we use a modified expression for the relative pathogen basic  
573 reproductive number (relative  $R_0$ ), a metric of pathogen transmission potential in a given thermal  
574 environment. This metric incorporates the thermal responses of mosquito and parasite traits to  
575 evaluate the combined effects of temperature and temperature fluctuation on the predicted thermal  
576 suitability [ $S(T)$ , **Equation 2**] of *An. stephensi* to transmit *Plasmodium falciparum*<sup>8</sup>. A scaled  
577 version of  $R_0(T)$ , called  $S(T)$ , is proportional to the number of new cases expected to arise from a  
578 single case assuming a fully susceptible population, and is dependent on environmental  
579 temperature,  $T$  (°C). Further, because values for mosquito life history traits change as mosquitoes  
580 age, we have adopted the use of the  $S(T)$  expression that more precisely captures lifetime  
581 transmission potential<sup>8</sup> (**Equation 2**).

$$582 \quad S(T) = \sqrt{a(T)^2 bc(T) \gamma(T) B(T) p_{EA}(T) MDR(T) lf(T)^2} \quad \text{Eq. 2}$$

583           The parameters of  $S(T)$  include: daily per capita bite rate ( $a$ ), vector competence ( $bc$ ; the  
584 proportion of infectious mosquitoes), lifetime egg production ( $B$ ), probability of egg-to-adult  
585 survival ( $p_{EA}$ ), mosquito development rate ( $MDR$ ), and adult mosquito lifespan ( $lf$ ). Further, the  
586  $S(T)$  formulation uses the Gompertz function over daily adult survival and the extrinsic incubation  
587 period ( $EIP$ , the inverse of the parasite development rate [ $PDR^{-1}$ ]) to calculate the proportion of  
588 mosquitoes surviving the latency period ( $\gamma$ ) as described in <sup>8</sup>. We fit thermal responses for these  
589 additional traits ( $p_{EA}$ ,  $MDR$ , and  $bc$ ) using previously published data measured across constant  
590 temperature gradients <sup>19,36</sup>. For  $\gamma$ , we combined data for  $PDR$  measured across a constant  
591 temperature gradient <sup>19</sup> with our new lifespan ( $lf$ ) data in constant and fluctuating conditions, and  
592 fit a TPC for each of our three fluctuation treatments (DTR = 0, 9, and 12°C). In all cases, we used  
593 the same methods as for the focal trait data collected here (described above), with a truncated  
594 normal distribution. We calculated thermal suitability using the full posterior distributions for each  
595 trait TPC over the temperature gradient from 0-45°C at 0.1°C intervals, yielding posteriors for  
596 suitability over that same gradient, with the same number of samples (7500). We then used these  
597 distributions to calculate the mean, median, and 95% credible intervals.

598           Absolute  $R_0(T)$  is influenced by additional factors that we do not incorporate in this study  
599 including rainfall, humidity, mosquito habitat quantity and quality, infection status, and  
600 heterogeneity in contact rates, individuals, or genotypes. Thus, we instead describe the thermal  
601 suitability of pathogen transmission,  $S(T)$ , where  $S(T)$  is scaled to range between 0 and 1 at the  
602 respective minimum and maximum values for the median thermal response. We scaled all  
603 versions of the  $S(T)$  model using the maximum value from model version 1 ('constant', see  
604 *Suitability Model Overview*) in order to be able to visually compare differences in the predicted  
605 magnitude of thermal suitability between model versions. The additional  $R_0$  parameters  $r$  (human

606 recovery rate) and  $N$  (density of humans) are evaluated as arbitrary constants, as they are  
607 assumed to be temperature independent. Thus, a threshold of  $S(T) > 0$  implies that the thermal  
608 conditions are suitable for the transmission of *P. falciparum* based solely on the temperature-  
609 dependent physiological responses of *An. stephensi*. Differences in the predicted critical  
610 temperatures at which  $S(T)$  reaches 0 ( $T_{min}$  and  $T_{max}$ ) and 1 ( $T_{opt}$ ) can then be compared across  
611 diurnal temperature ranges.

612

### 613 **Sensitivity and uncertainty analysis**

614 We performed two types of sensitivity analysis and an uncertainty analysis on each version  
615 of the suitability model to determine which traits were most important for determining the thermal  
616 optimum and limits for transmission and how each trait contributed to the uncertainty in  $S(T)$ .  
617 First, we used a partial derivative approach, calculating  $\partial S / \partial x \cdot \partial x / \partial T$  across the temperature ( $T$ )  
618 gradient for each trait ( $x$ ). This approach only works for the models without rate summation (i.e.,  
619 model 1: constant and model 2: empirical fluctuating) because it uses the derivatives of the  
620 quadratic and Brière functions and their fitted parameters ( $T_{min}$ ,  $T_{max}$ , and  $q$ ) for each trait. Second,  
621 we held each trait constant while allowing all others to vary with temperature. Finally, we  
622 calculated the HPD interval (highest posterior density interval, the smallest interval of predicted  
623 trait value encompassing 95% of the probability density in the posterior distribution) across the  
624 temperature gradient for  $S(T)$  using the full posterior distributions for all traits (i.e. full uncertainty)  
625 and for  $S(T)$  with each trait given its mean value (i.e. removing the uncertainty for one trait at a  
626 time). We then compared the relative size of the HPD in both conditions for each trait.

627

### 628 **Mapping thermal suitability predictions**

629 We created maps to compare the spatial distribution of months of thermal suitability for  
630 transmission predicted by the different versions of our model,  $S(T)$ . For simplicity, we only  
631 mapped model versions 1, 2, 4, and 5 (constant, empirical fluctuating, trait-level RS fluctuating -  
632 all traits, and  $S(T)$ -level RS fluctuating, respectively) for one level of DTR (12°C) where  
633 applicable. As with previous mapping for thermal suitability of transmission<sup>5,8,23,42,70</sup>, for each  
634 version of  $S(T)$  we determined the temperature range (at 0.1°C resolution) where  $S(T) > 0.001$   
635 with a posterior probability  $>97.5\%$ . This conservative threshold minimizes type I error  
636 (inclusion of unsuitable areas). Here, we also calculated the temperature range at which each  
637 model exceeded an additional threshold of suitability,  $S(T) > 0.5$ . This threshold shows where  
638 thermal suitability is relatively high (rather than simply *present*), and allows us to illustrate  
639 quantitative differences between model versions 4 and 5 (i.e. rate summation performed on the  
640 trait TPCs versus on the suitability TPC), which had similar  $T_{min}$  and  $T_{max}$  but different shapes  
641 otherwise. For calculating the mapping thresholds, we scaled the 97.5% lower CI prediction from  
642 each model between 0 and 1 so that relative suitability was based on the maximum predicted  
643 suitability for that specific model.

644 Global gridded long-term average modeled baseline monthly mean temperatures at a 5  
645 arcminute resolution (approximately 10 km<sup>2</sup> at the equator), were downloaded from  
646 WorldClim.org (version 1.0). The number of months (0-12) of thermal suitability under each  
647 combination of model and suitability threshold was calculated at the pixel level, and masked to  
648 countries described as the ‘endemic’ range for *An. stephensi* (India, Pakistan, Iran, Kuwait,  
649 United Arab Emirates, and Oman), and for all countries in the continent of Africa, where it is  
650 currently invading and establishing. All raster calculations and mapping output were conducted

651 in R (version 4.3.1), using packages ‘raster’ ‘terra’ ‘sf’ ‘tidyverse’ ‘ggplot2’ ‘maptools’  
652 ‘mapdata’ ‘ggthemes’, in RStudio 2024.04.0 Build 735.

653

## 654 **Data Availability**

655 The mosquito trait data are currently available on the project GitHub repository:  
656 <https://github.com/JoeyBernhardt/anopheles-rate-summation>. Upon acceptance, these data will  
657 also be submitted to Dryad Data Repository, and the associated citation will be provided here.

658

## 659 **Code Availability**

660 The code for this analysis is available on the project GitHub repository:  
661 <https://github.com/JoeyBernhardt/anopheles-rate-summation>.

662

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671

## 672 **Author Contributions**

673 KLM and CCM designed the study, with input from RJH. KLM and ARO performed the  
674 experiments. KLM performed the first analysis and wrote the first manuscript. MSS and JRB  
675 revised the analysis, with input from CCM and VMS. SJR performed the mapping analysis. MSS  
676 and CCM revised the manuscript, with input from SJR and VMS. All authors read and approved  
677 the final manuscript.

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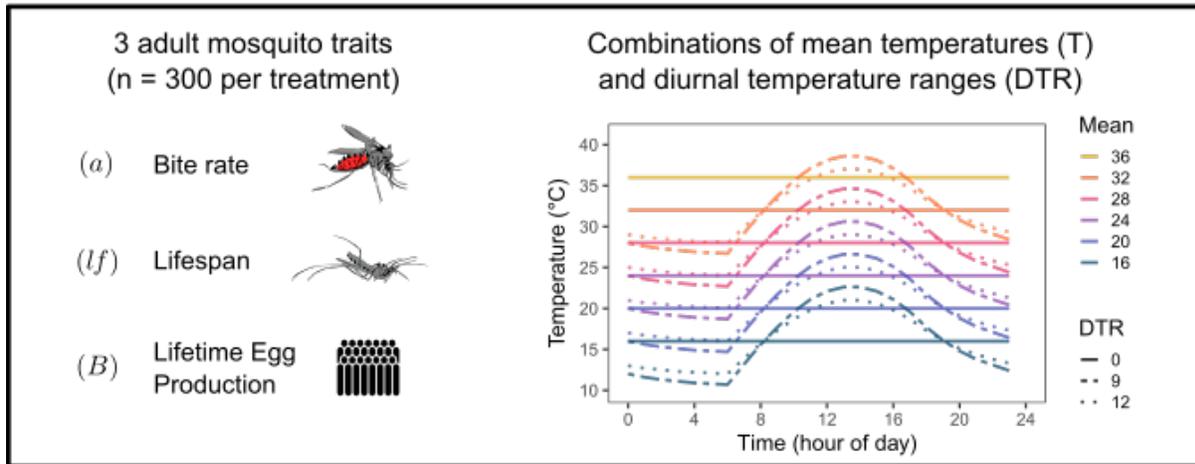
678

679 **Figure Captions (max 350 words each)**

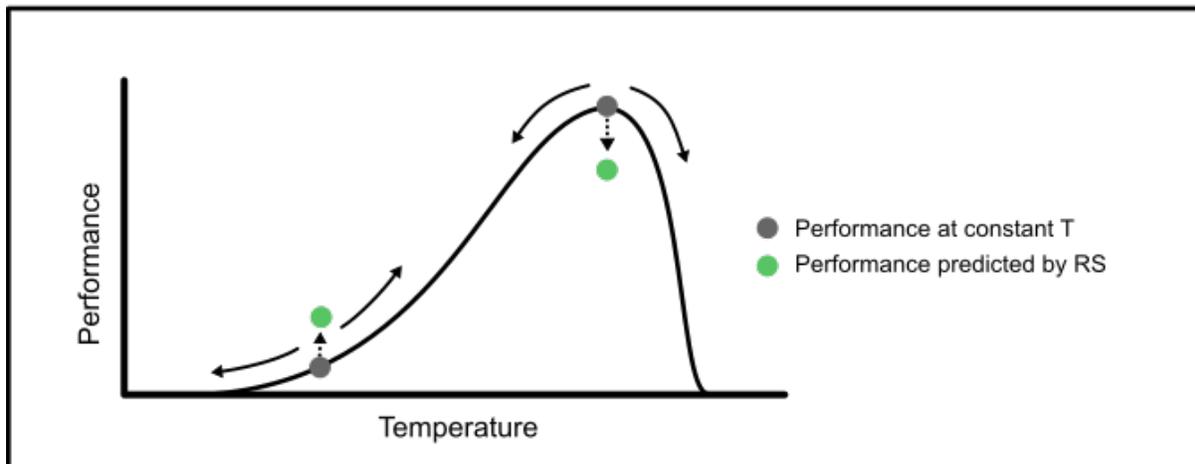
680 **Figure 1: Conceptual figure summarizing the study.** A) We measured three adult mosquito  
681 traits (bite rate [a], lifespan [lf], and lifetime egg production [B]) in constant and fluctuating  
682 conditions (diurnal temperature range [DTR] = 0, 9, and 12°C) across a range of mean  
683 temperatures (mean temperatures = 16, 20, 24, 28, and 32°C for all DTR treatments; 36°C for DTR  
684 = 0°C only). B) For each trait, we fit thermal response curves (TPCs) to the data from each DTR  
685 treatment. Additionally, we used rate summation (RS) to predict performance in fluctuating  
686 environments based on the TPC fitted to data from constant environments. Compared to constant  
687 temperatures with the same mean (dark gray points), in fluctuating temperatures (solid arrows)  
688 rate summation will predict a decrease in performance over decelerating portions of a TPC (e.g.,  
689 near the optimum) and an increase in performance over accelerating portions of a TPC (dashed  
690 arrow and green points). C) We compared five versions of a model predicting thermal suitability  
691 for transmission,  $S(T)$ , parameterized with different trait TPCs. Model 1 ('Constant T') used TPCs  
692 fit to trait data from constant temperatures. Model 2 ('Empirical Fluctuating T') used TPCs fit to  
693 trait data from fluctuating temperatures. Models 3 and 4 used TPCs generated by applying rate  
694 summation to constant temperature TPCs for either the 3 focal traits measured here (model 3:  
695 'Trait-level RS Fluctuating T - 3 traits') or all traits in the model (model 4: 'Trait-level RS  
696 Fluctuating T - all traits'). Model 5 ('S(T)-level RS Fluctuating T') applied rate summation directly  
697 to the TPC for suitability generated in model 1. Dashed arrows denote RS calculations and solid  
698 arrows denote parameterizing the suitability model with trait TPCs.  
699

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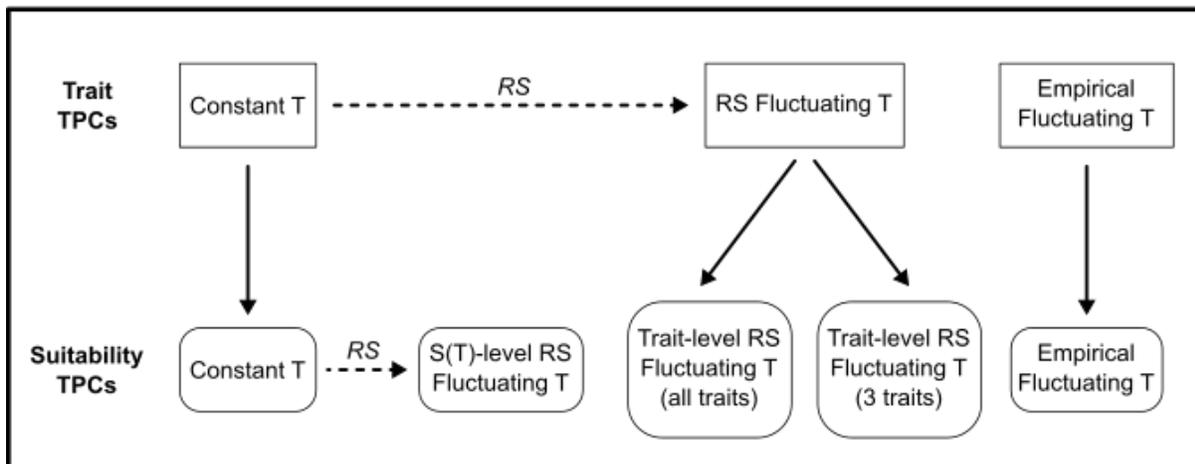
## A) Measure traits in constant & fluctuating conditions



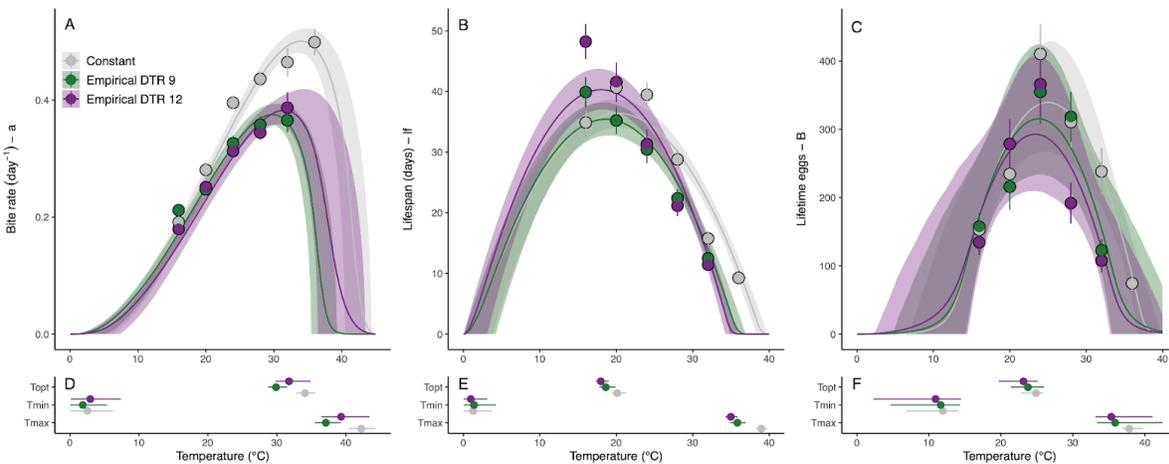
## B) Fit trait TPCs & use rate summation (RS) to predict performance in fluctuating conditions



## C) Model thermal suitability for malaria transmission – $S(T)$

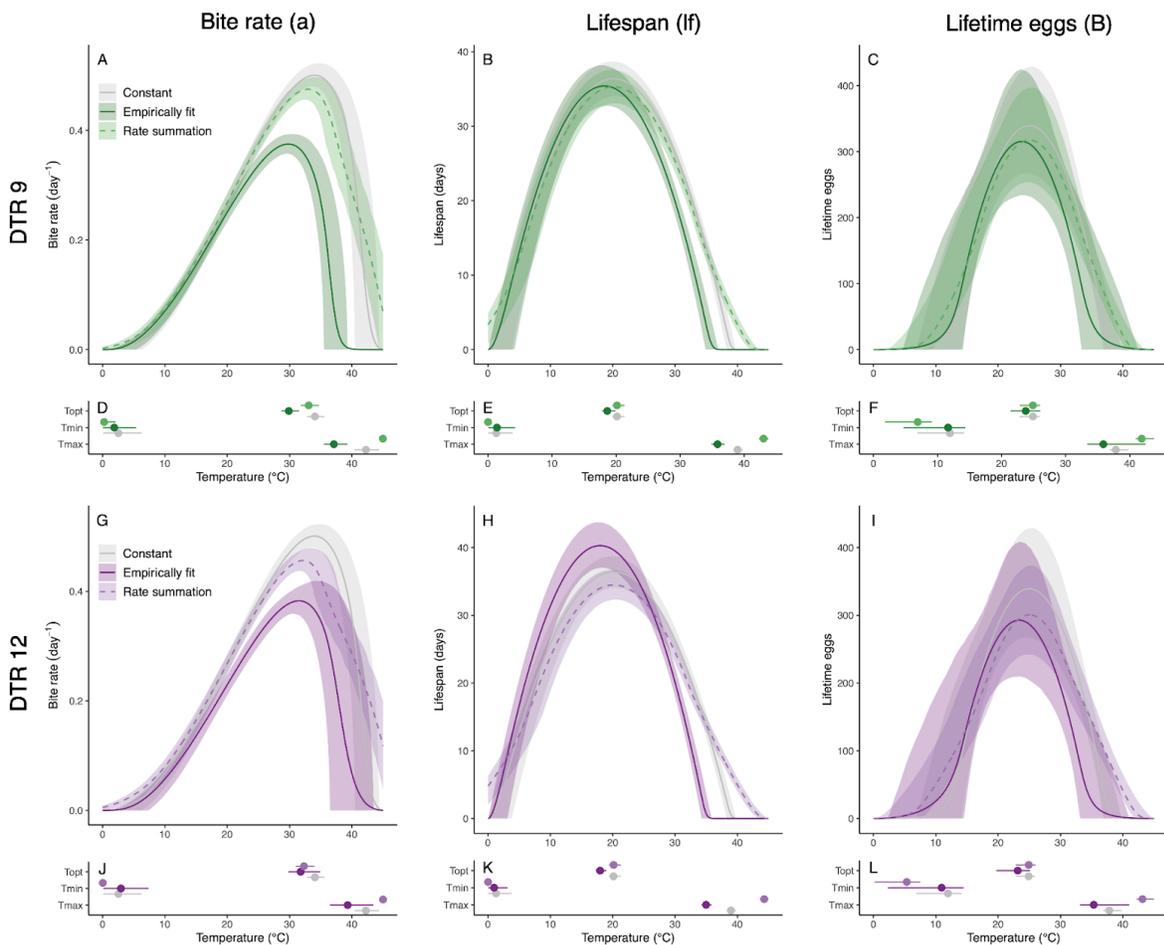


701 **Figure 2: Empirically measured thermal responses for three adult *Anopheles stephensi* traits**  
702 **in constant and diurnally fluctuating temperatures.** Traits include: bite rate (a, left column),  
703 lifespan (lf, center column) and lifetime egg production (B, right column). Colors denote daily  
704 temperature range (DTR) treatment: 0°C (gray), 9°C (green), and 12°C (purple). A-C)  
705 Summarized data and thermal performance curves (TPCs). TPC contours show posterior  
706 distribution medians, with 95% credible intervals as shaded areas. Points and error bars display  
707 block means and standard errors for visual comparison between treatments. (TPCs were fit to  
708 individual-level data.) D-F) Key temperature values from the TPCs: thermal optimum (Topt),  
709 thermal minimum (Tmin), and thermal maximum (Tmax). Points display posterior distribution  
710 medians and error bars display 95% credible intervals.  
711



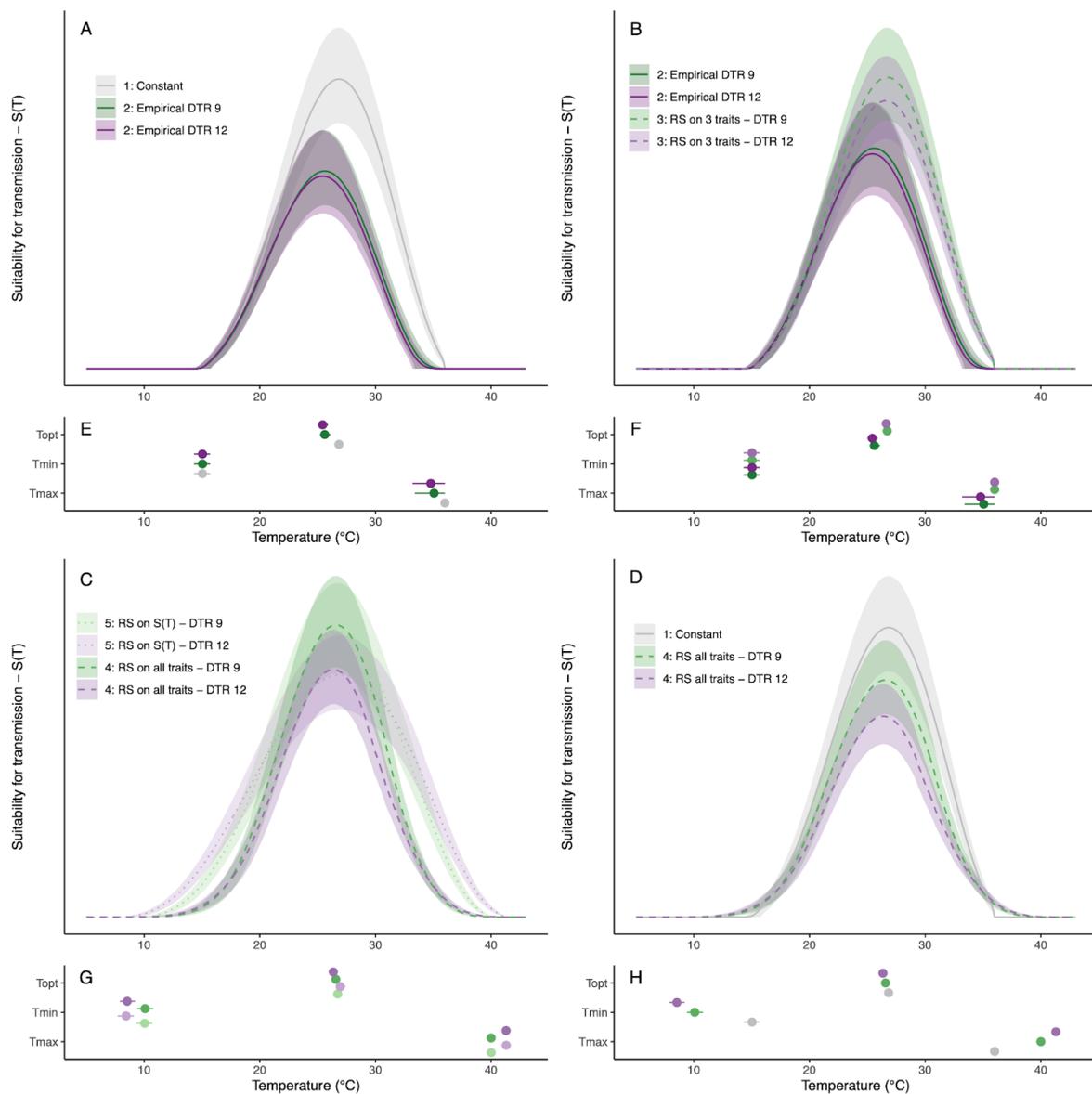
712

713 **Figure 3: Thermal performance based on empirical observations or predictions generated**  
714 **by rate summation for *Anopheles stephensi* performance in diurnally fluctuating**  
715 **temperature environments.** Left column: bite rate (a), center column: lifespan (lf), right column:  
716 lifetime egg production (B). Top row (green): daily temperature range (DTR) 9°C, bottom row  
717 (purple): DTR 12°C. Darker hues and solid lines show thermal performance curves (TPCs) fit to  
718 empirical data collected from mosquitoes housed in diurnally fluctuating temperature conditions.  
719 Light hues and dashed lines show predictions generated by rate summation. TPCs fit to empirical  
720 data collected from mosquitoes housed across constant temperature conditions shown in gray for  
721 comparison.  
722

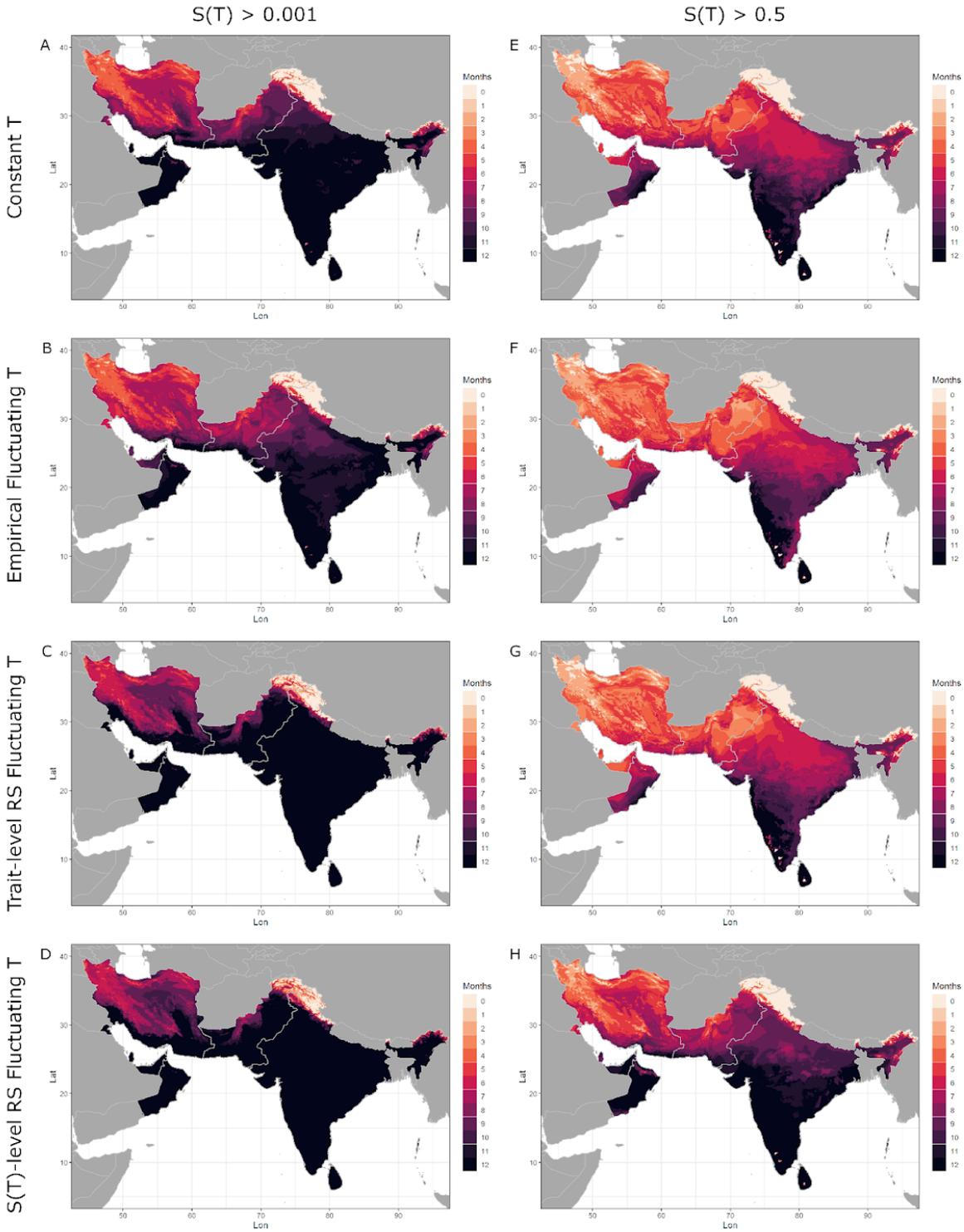


723  
724

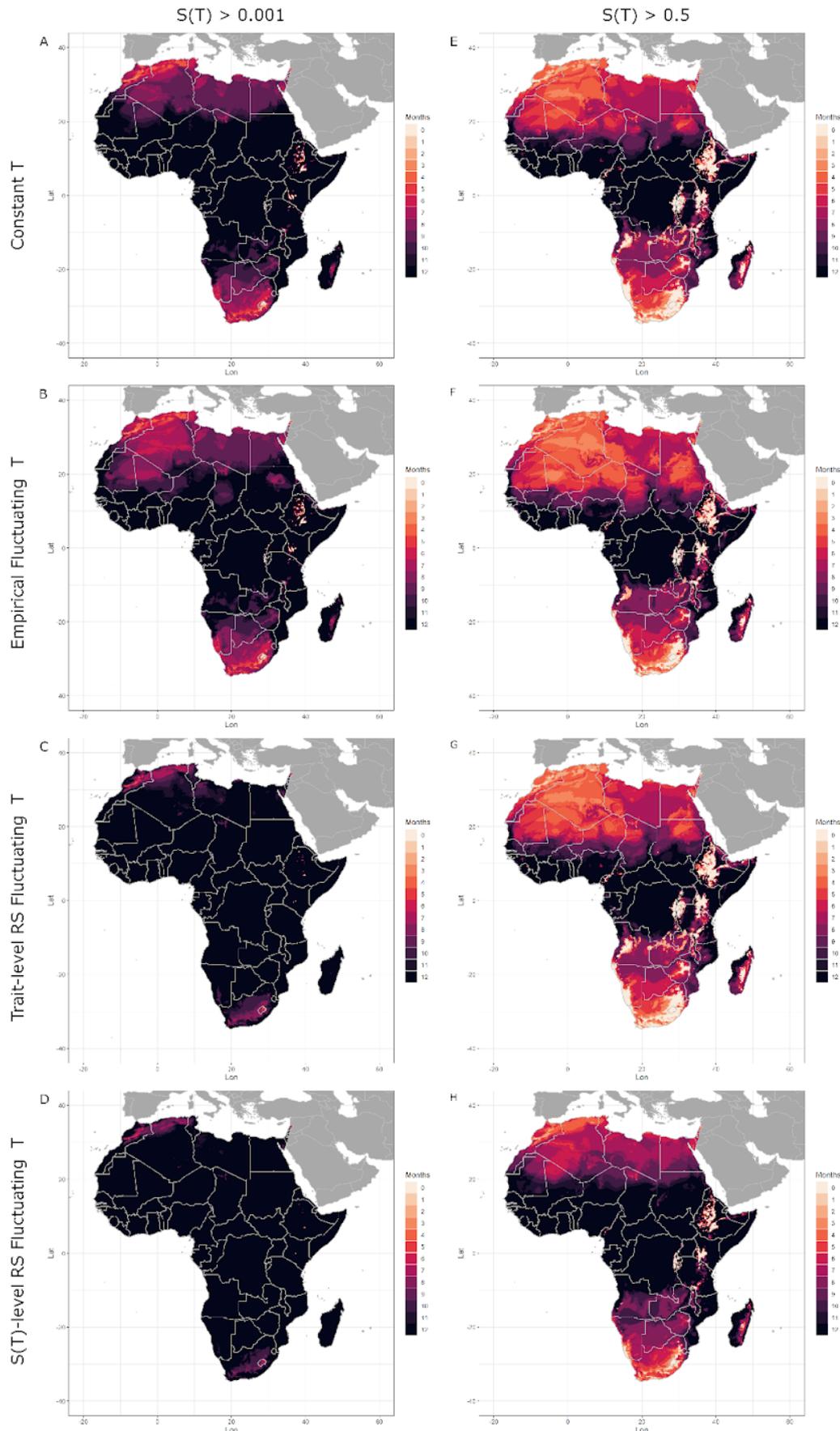
725 **Figure 4: Thermal suitability for transmission of malaria by *Anopheles stephensi* predicted**  
726 **for constant and diurnally fluctuating temperature conditions.** A) Model versions  
727 parameterized with TPCs fit to empirical data collected from constant temperature (T) conditions  
728 (model 1, constant T) and fluctuating conditions (model 2, empirical fluctuating T). B) Model  
729 versions parameterized with TPCs fit to empirical data collected from fluctuating conditions  
730 (model 2, empirical fluctuating T) and TPCs predicted by rate summation performed on trait TPCs  
731 for focal traits only (model 3, trait-level RS - 3 traits). C) Model versions comparing rate  
732 summation performed on the TPCs for traits (model 4, trait-level RS - all traits) and on the TPC  
733 for suitability itself (model 5,  $S(T)$ -level RS). The numbers in the legends below refer to model  
734 numbers, see *Methods* for model details.  
735



737 **Figure 5: Months of thermal suitability,  $S(T)$ , for transmission of malaria by *Anopheles***  
738 ***stephensi* in its native range in Central and South Asia predicted by models parameterized**  
739 **using constant and fluctuating temperatures.** Left column: total months where  $S(T)$  is predicted  
740 to exceed 0.001 (i.e. when transmission is possible). Right column: total months where  $S(T)$  is  
741 predicted to exceed 0.5 (i.e. when transmission is relatively favored by temperature). Darker hues  
742 indicate more months. Top row: model 1 (constant T) uses trait TPCs fit to data across a range of  
743 constant temperatures; second row: model 2 (empirical fluctuating T) uses trait TPCs fit to data  
744 across a range of fluctuating temperatures; third row: model 4 (trait-level RS - all traits), uses trait  
745 TPCs generated by applying rate summation to TPCs fit to data from constant temperatures for all  
746 traits; bottom row: model 5 ( $S(T)$ -level RS), applies rate summation to the TPC for suitability  
747 generated from traits measured across a range of constant temperatures (i.e. the output of version  
748 1). Fluctuating temperature models used a daily temperature range (DTR) = 12°C.  
749



751 **Figure 6: Months of thermal suitability,  $S(T)$ , for transmission of malaria by *Anopheles***  
752 ***stephensi* in its invading range in Africa predicted by models parameterized using constant**  
753 **and fluctuating temperatures.** Left column: total months where  $S(T)$  is predicted to exceed 0.001  
754 (i.e. when transmission is possible). Right column: total months where  $S(T)$  is predicted to exceed  
755 0.5 (i.e. when transmission is relatively favored by temperature). Darker hues indicate more  
756 months. Top row: model 1 (constant T) uses trait TPCs fit to data across a range of constant  
757 temperatures; second row: model 2 (empirical fluctuating T) uses trait TPCs fit to data across a  
758 range of fluctuating temperatures; third row: model 4 (trait-level RS - all traits), uses trait TPCs  
759 generated by applying rate summation to TPCs fit to data from constant temperatures for all traits;  
760 bottom row: model 5 ( $S(T)$ -level RS), applies rate summation to the TPC for suitability generated  
761 from traits measured across a range of constant temperatures (i.e. the output of version 1).  
762 Fluctuating temperature models used a daily temperature range (DTR) = 12°C.  
763



765 **Table 1. Shifts in properties of thermal performance curves (TPCs) for adult mosquito**  
 766 **traits due to temperature fluctuations.** Differences in thermal optimum ( $T_{opt}$ ), thermal  
 767 maximum ( $T_{max}$ ), and thermal breadth ( $T_{breadth}$ ), and percent change in the predicted trait value at  
 768  $T_{opt}$  [ $f(T_{opt})$ ]. TPCs fit to empirical data from fluctuating temperatures (Emp.) and TPCs  
 769 calculated using rate summation (RS) are both compared to TPCs fit to data from constant  
 770 temperatures. Diurnal temperature ranges (DTR) = 9 and 12°C. Differences calculated using  
 771 median values. See **Table S2** for the original parameter values for each model.  
 772

Trait & Fluctuation Regime	Emp. $T_{opt}$ (°C)	Emp. $T_{max}$ (°C)	Emp. $T_{breadth}$ (°C)	Emp. $f(T_{opt})$	RS $T_{opt}$ (°C)	RS $T_{max}$ (°C)	RS $T_{breadth}$ (°C)	RS $f(T_{opt})$
Bite rate ( $a$ )								
<i>DTR 9</i>	-4.2	-5.2	-4.5	-25.1%	-1.0	+2.6	+5.0	-5.1%
<i>DTR 12</i>	-2.4	-3.1	-3.4	-23.5%	-1.8	+2.6	+5.0	-8.9%
Lifespan ( $lf$ )								
<i>DTR 9</i>	-1.5	-3.1	-3.2	-2.7%	0.0	+4.1	+5.1	-3.0%
<i>DTR 12</i>	-2.1	-3.9	-3.7	10.7%	+0.1	+5.4	+6.4	-5.2%
Lifetime eggs ( $B$ )								
<i>DTR 9</i>	-1.2	-2.5	-2.3	-7.9%	+0.1	+4.0	+6.7	-6.5%
<i>DTR 12</i>	-1.6	-2.9	-2.4	-14.8%	+0.1	+5.3	+12.0	-11.5%

773

774 **Table 2: Shifts in properties of thermal performance curves (TPCs) for models of predicted**  
 775 **suitability of malaria transmission,  $S(T)$ , due to temperature fluctuations.** Differences in  
 776 thermal optimum ( $T_{opt}$ ), thermal maximum ( $T_{max}$ ), and thermal breadth ( $T_{breadth}$ ), and the percent  
 777 change in median  $S(T)$  predicted at  $T_{opt}$ , compared to the constant temperature model (model 1).  
 778 Fluctuating models are parameterized with trait TPCs fit from empirical data (model 2:  
 779 “Empirical fluctuating”) or are calculated using rate summation (RS). Rate summation was used  
 780 only for the three traits with empirical data (model 3: “Trait-level RS - 3 traits”), for all traits  
 781 (model 4: “Trait-level RS - all traits”), or directly on the TPC for suitability,  $S(T)$ , at constant  
 782 temperatures (model 5: “ $S(T)$ -level RS”). Diurnal temperature ranges (DTR) = 9 and 12°C.  
 783 Differences calculated using median values. See **Table S3** for original parameter values for each  
 784 model.  
 785

<b>Model &amp; Fluctuation Regime</b>	$T_{opt}$ (°C)	$T_{max}$ (°C)	$T_{breadth}$ (°C)	$S(T_{opt})$
2) Empirical fluctuating - 3 traits				
<i>DTR 9</i>	-1.2	-0.8	-0.8	-32.0%
<i>DTR 12</i>	-1.4	-1.8	-1.2	-33.8%
3) Trait-level RS - 3 traits				
<i>DTR 9</i>	-0.1	0.0	0.0	-10.0%
<i>DTR 12</i>	-0.2	0.0	0.0	-17.1%
4) Trait-level RS - all traits				
<i>DTR 9</i>	-0.2	+4.0	+9.0	-18.1%
<i>DTR 12</i>	-0.4	+5.3	+11.9	-30.6%
5) $S(T)$ -level RS				
<i>DTR 9</i>	-0.1	+4.0	+9.0	-19.9%
<i>DTR 12</i>	+0.1	+5.3	+11.9	-32.0%

786

787 **Table 3: Temperature thresholds used for mapping four models of thermal suitability.** Four  
788 versions of the model for thermal suitability,  $S(T)$ , parameterized with different trait TPCs or  
789 calculated using rate summation (RS): trait TPCs fit from empirical data under constant  
790 temperatures (model 1: “Constant”), trait TPCs fit from empirical data under fluctuating  
791 temperatures (model 2: “Empirical Fluctuating”), RS at the trait-level for all traits (model 4:  
792 “Trait-level RS - all traits”), or RS directly on the TPC for suitability,  $S(T)$ , parameterised under  
793 constant temperatures (model 5: “ $S(T)$ -level RS”). All fluctuating models were for Diurnal  
794 temperature ranges (DTR) = 12°C only. Units are in °C.  
795

<b>Model</b>	<b>Range where <math>S(T) &gt; 0.001</math> (°C)</b>	<b>Range where <math>S(T) &gt; 0.5</math> (°C)</b>
Constant (1)	15.8 - 35.8	21.1 - 31.9
Empirical Fluctuating (2)	15.8 - 33.1	20.3 - 30.2
Trait-level RS - all traits (4)	10.9 - 40.1	21.2 - 31.1
$S(T)$ -level RS (5)	9.3 - 41.1	18.7 - 34.7

796

797

798 **Table 4: Summary of selected previous studies analyzing empirical data on the impact of**  
 799 **temperature fluctuations on performance.** When relevant, results include whether they match  
 800 the general pattern of fluctuations improving performance at cooler temperatures and reducing  
 801 performance at warmer temperatures.  $T_{mean}$  = mean temperature,  $T_{min}$  = lower thermal limit,  $T_{opt}$   
 802 = thermal optimum, DTR = diurnal temperature range.  
 803

Study description and citation	Key results or traits measured (matches general pattern)
<i>Meta-analyses</i>	
Meta-analysis of 24 studies on development rate in all taxa <sup>28</sup>	Fluctuations that went below $T_{min}$ all increased performance; fluctuations that went above $T_{opt}$ reduced performance, with one exception (yes); other studies were highly variable (unclear)
Meta-analysis of 22 studies on egg incubation traits in reptiles <sup>57</sup>	Fluctuations increased performance at cooler $T_{means}$ and decreased performance at warmer $T_{means}$ (yes); fluctuation size increased effect size
Meta-analysis of 75 studies on all traits in all taxa <sup>58</sup>	Fluctuations reduced performance at all temperatures, but reduction was greater at warmer temperatures (partial)
<i>Studies in medically important mosquitoes</i>	
Larval, adult, and infection traits for rodent malaria in <i>Anopheles stephensi</i> at $T_{mean} = 18^{\circ}\text{C}$ and $24^{\circ}\text{C}$ <sup>37</sup>	Parasite development rate (yes), vector competence (yes), larval development rate (yes), larval survival (yes), gonotrophic cycle duration (yes), adult survival (no: fluctuations changed survival curve shape at cool $T_{mean}$ and increased survival at warm $T_{mean}$ )
Adult survival and vector competence for dengue virus in <i>Aedes aegypti</i> at $T_{mean} = 26^{\circ}\text{C}$ <sup>35</sup>	Adult survival (yes), vector competence (partial: reduced for % infection but no effect for % dissemination)
Larval and adult traits in <i>Aedes aegypti</i> at $T_{mean} = 16^{\circ}\text{C}$ and $35\text{-}37^{\circ}\text{C}$ <sup>61</sup>	Larval development rate (yes), larval survival (partial: increased at both $T_{means}$ ), proportion blood feeding (yes)
Larval traits in <i>Anopheles stephensi</i> at various $T_{means}$ <sup>36</sup>	Larval development rate (yes), larval survival (yes); for survival, larger DTRs increased effect size at $T_{mean} = 35^{\circ}\text{C}$
<i>Studies in other host-parasite systems</i>	
Parasitoid wasps in drosophila hosts at $T_{mean} = 20^{\circ}\text{C}$ <sup>31</sup>	Parasite development rate (yes), infestation rate (no effect), parasite success (yes)
Snail hosts and schistosome parasites at $T_{mean} = 25^{\circ}\text{C}$ <sup>47</sup>	Fluctuations up to 2x typical DTR: snail egg production (no effect), snail growth (no effect), and parasite production (no effect).

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