

# Electrostatic Effect on Core–Shell Micro-spheres with Mixed Charges as Adaptive Plugging Agents for Enhanced Oil Recovery

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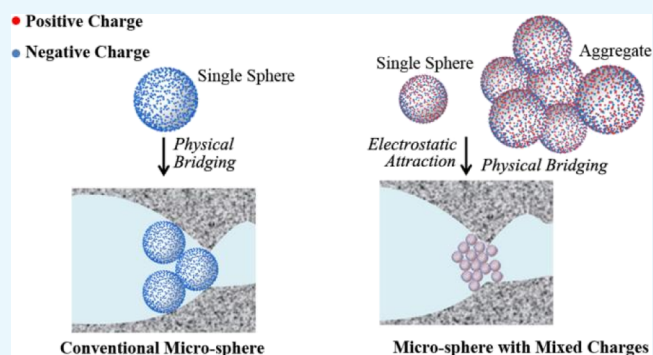
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**ABSTRACT:** Core–shell micro-spheres (MS) with both negative and positive charges in the core and only negative charges in the shell were developed as adaptive plugging agents for in-depth conformance control for enhanced oil recovery. The MS were designed to propagate deeply into the reservoir due to the small particle size and electrostatic repulsion between the MS and the sandstone at the initial stage of injection and form aggregates by electrostatic attraction between the cores with mixed charges when the shells degraded at a given time during transportation, leading to an effective plugging of the highly permeable layers with low residual oil saturation. The self-assembling and plugging behaviors of the MS have been studied by Monte Carlo simulation. The results show that charge density ( $D_{\text{charge}}$ ), fraction of positive charge ( $F_p$ ), MS concentration, temperature, and salinity are the key factors influencing the self-assembling behaviors. The electrostatic interaction would become stronger with the increase in  $D_{\text{charge}}$  when it is larger than 0.5. The MS are more likely to form aggregates when  $F_p$  approaches 0.5. The higher the concentration of the MS, the stronger the electrostatic interaction between the MS. In addition, electrostatic interactions between the MS become stronger with the increase in temperature and decrease in salinity. Simulation results prove that the MS with mixed charges can effectively and adaptively plug highly permeable layers with low residual oil saturation through self-assembling by combination of electrostatic interactions along with physical bridging, leading to the improvement of oil recovery. Furthermore, block charge distribution will be helpful for the MS with mixed charges to form larger aggregates than that of the random mode to effectively plug the highly permeable layers.



## 1. INTRODUCTION

More and more mature oilfields in China become seriously heterogeneous<sup>1,2</sup> with high water cut in the extraction fluid,<sup>3,4</sup> resulting in low oil production and high costs. Currently, extensive chemicals have been adopted in the oilfields for profile control to reduce the water cut and improve the oil production, including foam agents<sup>5,6</sup> and cross-linked polymers,<sup>7–13</sup> such as preformed particle gels, polyacrylamide micro-spheres (MS), and underground delayed cross-linking systems.<sup>14–16</sup> Plugging behavior of conventional cross-linked polymers is based on the mechanism of physical bridging at reservoir pore throats, the narrowest parts where the fluid transports, depending on the size matching relationship<sup>17–19</sup> between the plugging agents, which are used to plug the highly permeable zones of the reservoir by physical bridging, and the reservoir pore throats. Usually, the reservoir can be effectively plugged when the sizes of plugging agents ranged from 1/3 to 1 times of reservoir pore throats in the homogeneous reservoirs,<sup>17,19</sup> no matter the MS is in the small initial sizes or in the big expansion sizes.<sup>20–22</sup> However, it is challenging to find suitable plugging agents for heterogeneous reservoirs with poly-dispersed pore throat sizes.<sup>23,24</sup> Therefore, it is necessary

to do more research from both practical and fundamental viewpoints to design a new adaptive plugging agent for in-depth conformance control in heterogeneous reservoirs with various permeabilities.

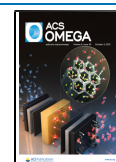
Core–shell MS with positively and negatively charged cores wrapped by negatively charged shells were developed recently by multi-stage emulsion or micro-emulsion polymerization with different ionic monomers,<sup>25</sup> aiming to form aggregates adaptively for plugging highly permeable layers by electrostatic attraction along with the conventional physical bridging, as shown in Figure 1.

The mechanism of self-assembling and plugging behavior of the MS was studied by Monte Carlo simulation in this paper.

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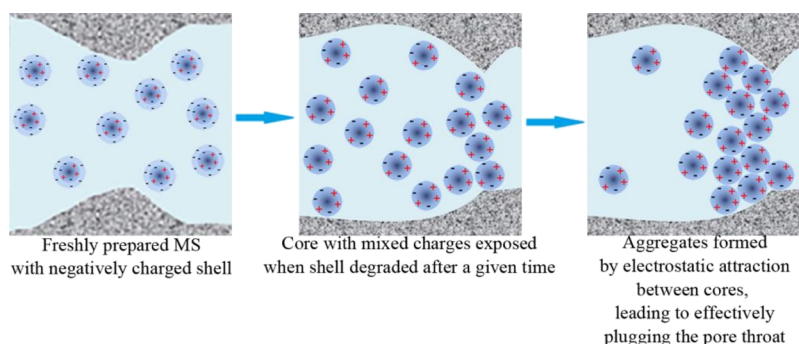


Figure 1. Scheme of the plugging process of the MS.

## 2. SIMULATION METHODOLOGY

Monte Carlo Simulation<sup>26</sup> with the canonical ensemble<sup>27</sup> was conducted in a two-dimensional lattice mode<sup>28</sup> space with either periodic or uncharged hard-wall boundary conditions. All MS moved randomly in the space. Importance sampling<sup>29</sup> of simulation was based on the electrostatic interaction calculated by Ewald sum adhering to Debye–Hückel theory<sup>30</sup> and the solvating effect described by the Flory–Huggins factor.<sup>31</sup>

**2.1. Modeling.** As hard spheres, the diameter of the MS was 24 units in the calculation cell, and each unit represented 12.5 nm in length. The MS with a diameter about 300 nm occupied 480 lattices, and each MS occupied 75 lattices on average. To simplify and speed up the simulation processes, only the MS surfaces were charged. Each lattice of the MS surface was set at most one charge by obeying the principle<sup>32,33</sup> that it will inhibit the ionization of the surrounding groups when one ionizable group of the polymer is ionized. Each charge on the MS surface was established as the dipole-lattice model,<sup>34</sup> and the length between two charges was calculated by their positions.

$D_{\text{charge}}$  and  $F_p$ , which represented charge density and fraction of the positive charge on the MS surface, respectively, both ranged from 0 to 1. The MS surfaces were uncharged at  $D_{\text{charge}} = 0$  and fully charged at  $D_{\text{charge}} = 1$ . There were only negative charges on the MS surface at  $F_p = 0$  when  $D_{\text{charge}}$  was not zero, which could be used for representing MS wrapped by negatively charged shells. Positive and negative charges on the MS surface were distributed randomly when  $D_{\text{charge}}$  and  $F_p$  were determined except noted elsewhere. The number of charges on the surface of each MS was calculated using eq 1

$$\begin{aligned} N_{\text{charge}} &= D_{\text{charge}} \cdot N_{\text{lat-surface}} \\ N_p &= F_p \cdot N_{\text{charge}} = F_p \cdot D_{\text{charge}} \cdot N_{\text{surface}} \\ N_n &= N_{\text{charge}} - N_p \end{aligned} \quad (1)$$

where  $N_{\text{charge}}$  was the total number of charges,  $N_{\text{lat-surface}}$  was the number of the lattice occupied by the surface of each MS,  $N_p$  was the number of positive charges, and  $N_n$  was the number of negative charges. When the results of  $N_{\text{charge}}$  and  $N_p$  were not an integer, they were round to the largest integer less than the results, respectively.

The concentration of the MS in the calculation cell,  $C_{\text{ms}}$ , was calculated using eq 2

$$C_{\text{ms}} = N_{\text{lat-ms-total}} / N_{\text{lat-cell}} = N_{\text{ms}} \cdot N_{\text{lat-ms-one}} / N_{\text{lat-cell}} \quad (2)$$

where  $N_{\text{lat-ms-total}}$  was the total number of lattices occupied by all MS in the calculation cell,  $N_{\text{ms}}$  was the number of MS in the

calculation cell,  $N_{\text{lat-ms-one}}$  was the number of lattices occupied by one MS, and  $N_{\text{lat-cell}}$  was the total number of lattices of the calculation cell.  $N_{\text{lat-cell}}$  was about  $4.19 \times 10^6$  by periodic boundary condition representing the MS solution with lengths of calculation cell ( $L_{\text{cell}}$ ) in both horizontal and vertical direction equaled 2048 units. The hard-wall boundary condition in the vertical direction was used to represent the pore, and the vertical length ( $L_{\text{cell-y}}$ ), which represented the diameter of the pore, was set to be a multiple of the MS diameter and equaled  $24 \times M$ , where  $M$  is the multiple of the pore size to the MS diameter.  $N_{\text{cell}}$  of the hard-wall boundary condition was  $2048 \times L_{\text{cell-y}}$  since the horizontal length of the calculation cell ( $L_{\text{cell-x}}$ ) obtained by the periodic boundary condition remained 2048 units. The minimum number of MS for forming an entire plugging structure in the pore was defined as  $N_{\text{min}}$ . The amount of  $N_{\text{min}}$  was used to describe not only the number of MS in the pore but also the size of the aggregate which could entirely plug the pore either.

**2.2. Sampling and Calculation.** To estimate state  $\Phi$  from state  $\Psi$  by importance sampling, the probability in simulation ( $P_{\text{acc}}$ ) was expressed as eq 3<sup>29</sup>

$$P_{\text{acc}}(\Psi \rightarrow \Phi) = \min[c_r, \exp(-\beta\Delta E)] \quad (3)$$

where  $\Delta E$  was the change in potential energy from state  $\Psi$  to state  $\Phi$ ,  $c_r$  was a random number ranging from 0 to 1, and  $\beta$  was Boltzmann constant normalized to 1 by Lennard-Jones (LJ) units, a method to set the fundamental quantities to 1 without loss of generality in simulation.

Potential energy  $E$  was separated into three independent parts: interactions between MS, interactions between MS and water, and electrostatic energy. The state change would be accepted when all three parts satisfied with the condition that the result of eq 3 was  $c_r$ .

In the hard-sphere model, the interaction energy between MS,  $E_{\text{MS}}$ , was calculated using eq 4, where  $L(ij)$  was the Euclidean distance between the centers of  $i$ th and  $j$ th MS

$$E_{\text{MS}} = \begin{cases} \infty & L(ij) < 24 \\ 0 & L(ij) \geq 24 \end{cases} \quad (4)$$

Flory–Huggins factor  $\chi$ , in the range of 0–1, was used to estimate the interaction between the MS and water according to eq 5<sup>31</sup>

$$E_{\text{sol}} = \chi \cdot Z \quad (5)$$

where  $E_{\text{sol}}$  stood for the interaction energy between MS and water and  $Z$  represented the number of lattices surrounding the MS which were occupied by the solvent. Considering that

the MS were highly hydrophilic in the experiment,  $\chi$  was fixed at 0 in simulation.

Electrostatic energy ( $E_{\text{ele}}$ ) in a lattice-mode space could be obtained using eq 6 by Fourier transform<sup>35</sup>

$$E_{\text{ele}} = \frac{1}{2} \sum_{i,j=1}^{N_{\text{ele}}} \sum_{\mathbf{n} \in \mathbb{Z}^3} \frac{q_i q_j}{|\mathbf{r}_{ij} + \mathbf{n} \cdot \xi^* \cdot \xi_0|} \quad (6)$$

where  $N_{\text{ele}}$  was the number of charges in the calculation cell,  $q_i$  and  $q_j$  ( $i, j = 1 \sim N_{\text{ele}}, i \neq j$ ) represented the  $i$ th or the  $j$ th charge, respectively.  $\xi^*$  was the relative permittivity of solution, and  $\xi_0$  was the vacuum dielectric constant.  $\mathbf{r}_{ij}$  was the real space vector from  $i$ th charge with vector  $\mathbf{r}_i$  to  $j$ th charge with vector  $\mathbf{r}_j$ .

$E_{\text{ele}}$  would be negligibly small when  $|\mathbf{r}_{ij}| > r_{\text{max}}$  and  $r_{\text{max}}$  was calculated using the Ewald parameter  $\alpha$ ,<sup>35,36</sup> as shown in eq 7

$$\alpha = \pi^{1/2} N_{\text{ele}}^{1/6} L_{\text{ele}}^{-1} \\ r_{\text{max}} \approx \pi / \alpha \quad (7)$$

where  $N_{\text{ele}}$  was the number of charge in the calculation cell and  $L_{\text{ele}}$  was the length of the calculation cell used in the calculation of  $E_{\text{ele}}$  which was 2048 with the periodic boundary condition and  $(2048 \times L_{\text{cell}})^{0.5}$  with the hard-wall boundary condition.

The value of  $N_{\text{ele}}$  in eq 7 was related to two parts: charges on the MS surface, which equaled  $N_{\text{ms}} \cdot N_{\text{charge}}$ , and ions in the solution. The number of salt ions could not be precisely set because salt ions could not be seen as a result of the high coarsening degree in simulation. Therefore, it should be unreachable to revise the data of  $N_{\text{ele}}$ , with the result that  $N_{\text{ele}}$  in eq 7 remained  $N_{\text{ms}} \cdot N_{\text{charge}}$  in simulation. Besides, surface charge density and the electrical potential of the MS would be changed by salt ions,<sup>37,38</sup> and the influence would become stronger with higher ion concentrations. Therefore, it was necessary to revise the activity of charges on the MS surface in electrostatic energy calculation to calculate the influence of salinity in simulation considering the calculation efficiency. Assuming that there was only NaCl in the solution, the activity of surface charge,  $a(S)$ , was calculated using eq 8<sup>39</sup>

$$a(S) = 1 - \frac{S/(1000 \times 58.5)}{1 + S/(1000 \times 58.5)} \quad (8)$$

where  $S$  was the salinity of the MS solution, mg/L.

The electrical property of aqueous solution with salt ions was simulated as the continuum model<sup>34</sup> and was corrected by temperature ( $T$ ) and salinity ( $S$ ), as shown in eq 9<sup>40</sup>

$$\xi^*(T, S) = \xi^*(T, 0) \times (1 - 0.2551 \cdot f(S) \\ + 5.15 \times 10^{-2} \cdot f(S)^2 - 6.889 \times 10^{-3} \cdot f(S)^3) \quad (9)$$

where  $T$  was the temperature of the MS solution and  $\xi^*(T, 0)$  reflected the influence of temperature on  $\xi^*$  in deionized (DI) water according to eq 10<sup>41</sup>

$$\xi^*(T, 0) = 87.740 - 0.4008T \\ + 9.398 \times 10^{-4} T^2 - 1.410 \times 10^{-6} T^3 \quad (10)$$

The correction function  $f(S)$  was related to the salinity of the MS solution ( $S$ , mg/L), according to the eq 11<sup>40,42</sup>

$$f(S) = (S/1000) \times [1.070 \times 10^{-2} \\ + 1.205 \times 10^{-5} \times (S/1000) + 4.058 \times 10^{-9} \\ \times (S/1000)^2] \quad (11)$$

By the normalization of  $\xi_0$  to 1 according to LJ units, along with the correction of  $S$  and  $T$ , eq 6 would be revised to eq 12 to calculate in simulation

$$E_{\text{ele}} = \frac{1}{2} \sum_{i,j=1}^{N_{\text{ele}}} \sum_{\mathbf{n} \in \mathbb{Z}^3} \frac{q_i^* \cdot q_j^*}{|\mathbf{r}_{ij} + \mathbf{n} \cdot \xi^*(T, S)|} \\ q_i^* = q_i \cdot a(S); \quad q_j^* = q_j \cdot a(S) \quad (12)$$

where  $a(S)$  and  $\xi^*(T, S)$  were obtained using eqs 8 and 9, respectively.

**2.3. Statistics.** To further investigate the self-assembling and motion behaviors of the MS, two series of factors, series L and series D, were considered, respectively.

Series L was based on the distribution of the MS in the calculation cell.  $L(ij)$  was the Euclidean distance, as shown in eq 4.  $L_{\text{ave}}$ ,  $L_{\text{min}}$ , and  $CV_L$  were the average value, the minimum value, and the coefficient variation of all  $L(ij)$  in one calculation cell, respectively. With less  $L_{\text{ave}}$  or  $L_{\text{min}}$  and greater  $CV_L$ , the distribution of the MS in the calculation cell becomes more uneven, and the self-assembling behavior of MS should be more obvious.

Series D was used to estimate the motion behavior of the MS.  $D(i)$  represented the contour length of the motion trajectory from the initial position to the final position of  $i$ th MS, which described the moving distance of  $i$ th MS.  $D_{\text{ave}}$  was the average value of all  $D(i)$  in one calculation cell. The MS had better motility with a higher value of  $D_{\text{ave}}$ .

### 3. RESULTS AND DISCUSSION

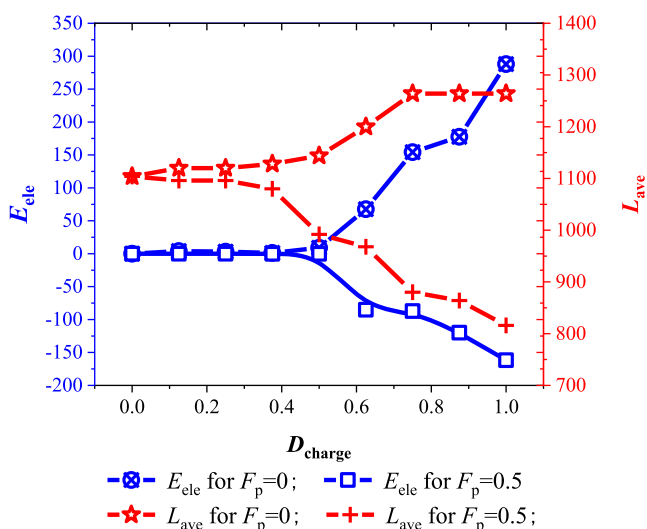
**3.1. Influence Factors of Self-Assembling.** The influence factors of the self-assembling behaviors of the MS were studied in the MS solution using periodic boundary conditions.

**3.1.1. Charge Density.** The dependence of self-assembling factors on  $D_{\text{charge}}$  is shown in Figure 2.

The absolute values of  $E_{\text{ele}}$  are very small and changes little when  $D_{\text{charge}}$  is less than 0.5, implying that there is little electrostatic interaction between MS. Correspondingly,  $L_{\text{ave}}$  is almost unchanged. The absolute values of  $E_{\text{ele}}$  increase sharply with the increase in  $D_{\text{charge}}$  when  $D_{\text{charge}}$  is greater than 0.5, implying that the electrostatic interaction between MS strengthens dramatically with the increase in charge density.

At  $F_p = 0$ , as MS with like-charged surface repel each other, the MS separate from each other as far as possible in the limited simulation cell, leading to a disequilibrium system with  $E_{\text{ele}} > 0$  at any  $D_{\text{charge}}$  and  $L_{\text{ave}}$  reaches maximum at about  $D_{\text{charge}} = 0.75$  by the limitation of the fixed concentration. The further increase in  $D_{\text{charge}}$  above 0.75 does not change the value of  $L_{\text{ave}}$  but increases the value of  $E_{\text{ele}}$  because of its non-equilibrium state.

At  $F_p = 0.5$ , which means the ratio of the positive charge to negative charge is 1:1 on the MS surface,  $E_{\text{ele}}$  is less than 0 at any  $D_{\text{charge}}$ . It indicates that there is electrostatic attraction between MS which dominates the self-assembling of the MS. In addition,  $E_{\text{ele}}$  increases with the increase in  $D_{\text{charge}}$  showing that electrostatic attraction becomes stronger. Therefore the



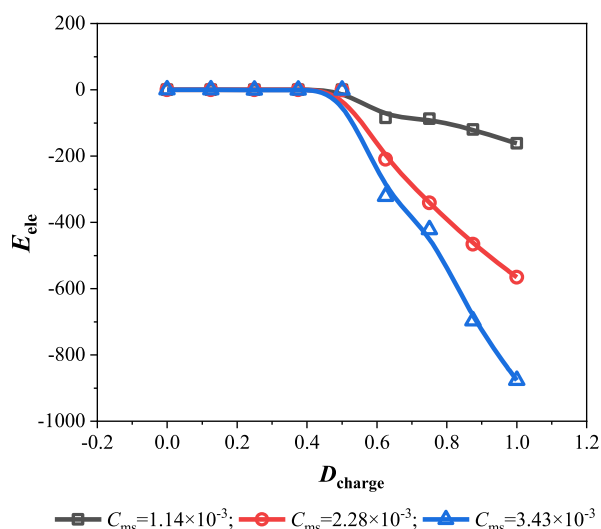
**Figure 2.** Dependence of  $E_{\text{ele}}$  and  $L_{\text{ave}}$  on  $D_{\text{charge}}$  at  $C_{\text{ms}} = 1.14 \times 10^{-3}$  with  $F_p = 0$  or  $F_p = 0.5$ .

MS become more inclined to assemble, resulting in the decrease in  $L_{\text{ave}}$ .

**3.1.2. Fraction of Positive Charge.** Figure 3 shows the dependence of self-assembling factors on  $F_p$ .

$E_{\text{ele}}$  is below zero when  $F_p$  is between 0.3 and 0.7 and reaches the minimum at  $F_p = 0.5$  and  $L_{\text{ave}}$ , while  $CV_L$  reaches the maximum, indicating that electrostatic attraction dominates in this range. It will lead to the self-assembling of the MS, which makes the distribution of the MS more and more uneven in the calculation cell until the number of positive charges equals to negative charges on the MS surface. The distribution of the MS varies with the change in the electrostatic interaction, depending on the value of  $F_p$ . When the fraction of either charge is below 0.3, the electrostatic repulsion will dominate the separation of the MS; hence, it is hard to form aggregates.

**3.1.3. MS Concentration.** Figure 4 shows the influence of charge density on  $E_{\text{ele}}$  with different MS concentrations at  $F_p = 0.5$ .



**Figure 4.** Dependence of  $E_{\text{ele}}$  on  $D_{\text{charge}}$  with different  $C_{\text{ms}}$  at  $F_p = 0.5$ .

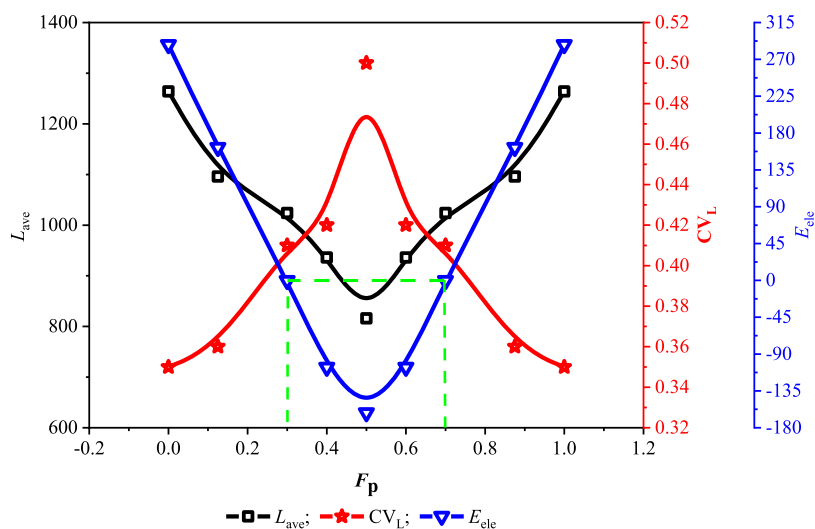
The turning points of drastic change appear at about  $D_{\text{charge}} = 0.5$  at all concentrations, indicating that the MS concentration does not change the electrostatic properties, which are determined by the charge density on the MS surface, but only changes the absolute value of  $E_{\text{ele}}$ . The absolute value of  $E_{\text{ele}}$  becomes larger with the increase in  $C_{\text{ms}}$  at any  $D_{\text{charge}}$ , though the difference is tiny when  $D_{\text{charge}} < 0.5$ .

Figure 5 shows the influence of  $F_p$  on  $E_{\text{ele}}$  with different MS concentrations at  $D_{\text{charge}} = 1$ .

$E_{\text{ele}}$  is less than 0 when  $F_p$  is in the range of 0.3–0.7 at any  $C_{\text{ms}}$ , and the increase in  $C_{\text{ms}}$  increases the absolute values of  $E_{\text{ele}}$ , making the self-assembling behavior of the MS more obvious when there is electrostatic attraction between MS. The attraction or repulsion between MS depends on the charge ratio on the MS surface.

**3.1.4. Temperature.** Figure 6 shows the dependence of  $\xi^*$  and  $E_{\text{ele}}$  on temperature ( $T$ ) in DI water at  $D_{\text{charge}} = 1$ .

It is shown that  $\xi^*$  decreases with the increase in  $T$ ,<sup>41</sup> and the absolute values of  $E_{\text{ele}}$  of MS at both  $F_p = 0$  and  $F_p = 0.5$  increase with the increase in  $T$ . The results for  $E_{\text{ele}}$  and  $\xi^*$  are in accordance with eq 12 which shows that  $E_{\text{ele}}$  is inversely



**Figure 3.** Dependence of self-assembling factors on  $F_p$  at  $D_{\text{charge}} = 1$  and  $C_{\text{ms}} = 1.14 \times 10^{-3}$ .



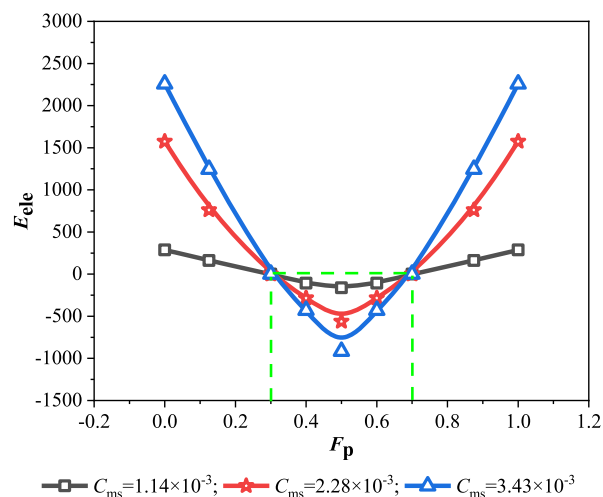


Figure 5. Dependence of  $E_{\text{ele}}$  on  $F_p$  with different  $C_{\text{ms}}$  at  $D_{\text{charge}} = 1$ .

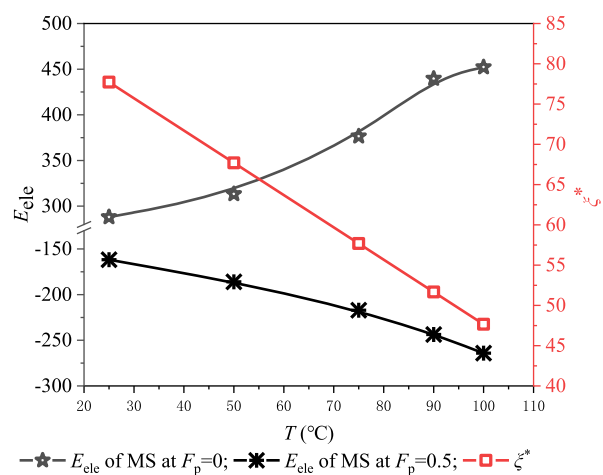


Figure 6. Dependence of  $\xi^*$  and  $E_{\text{ele}}$  on  $T$  at  $C_{\text{ms}} = 1.14 \times 10^{-3}$ ,  $S = 0$  mg/L.

proportional to  $\xi^*$ . It is implied that the electrostatic interaction of either  $F_p$  enhances with the increase in  $T$ , which is helpful for the MS with mixed charges to form aggregates to plug highly permeable layers, and is crucial for enhanced oil recovery (EOR) since it is much more difficult to find suitable plugging agents for high-temperature reservoirs.<sup>43</sup>

**3.1.5. Salinity.** Since there is a wide range of salinity used in EOR, such as river water with low salinity and formation water with high salinity,<sup>44,45</sup> it is necessary to study the influence of salinity ( $S$ ) on the electrostatic interaction and self-assembling behavior of the MS with mixed charges. Figure 7 shows  $\xi^*$ ,  $a(S)$ ,  $E_{\text{ele}}$ , and  $L_{\text{ave}}$  as functions of  $S$  at  $T = 95$  °C and  $F_p = 0.5$ .

$\xi^*$  and  $a(S)$  decrease with the increase in  $S$  when the salinity is greater than 1000 mg/L. It has been discussed previously that  $E_{\text{ele}}$  is inversely proportional to  $\xi^*$ , but  $E_{\text{ele}}$  decreases as  $\xi^*$  decreases, as shown in Figure 7, which might be the result of the decrease in  $a(S)$ .  $a(S)$  decreases with the increase in  $S$ , which simulates the increase in the charge shielding effect<sup>46,47</sup> and the decrease in the ionization possibility of charged groups on the MS surface. As a result, the absolute values of  $E_{\text{ele}}$  decrease apparently by orders of magnitude, indicating that the electrostatic attraction between MS weakens significantly with the increase in salinity, causing the decrease in self-assembling that  $L_{\text{ave}}$  grows with the increase in  $S$ , as shown in Figure 7.

### 3.2. Plugging Behavior of the MS in Porous Media.

The plugging behaviors of the MS were studied in porous media using hard-wall boundary conditions at  $D_{\text{charge}} = 1$ ,  $S = 9000$  mg/L, and  $T = 95$  °C.

Figure 8 shows the minimum plugging structure in the pore. The data of  $N_{\text{min}}$  are numerically the same as  $M$ . It is found that there should be at least  $1N_{\text{min}}$  MS in porous media to form an entire plugging structure, and  $C_{\text{ms}}$  should be higher than the critical concentration  $8.78 \times 10^{-3}$  by eq 2, otherwise the plugging behavior of the MS would not occur. Thus, the self-assembling and plugging behavior of the MS in porous media were studied when  $C_{\text{ms}}$  was higher than the critical concentration.

**3.2.1. Influence of Pore Diameter on MS Size.** Self-assembling behaviors of the MS in porous media at  $C_{\text{ms}} = 1.32 \times 10^{-2}$  are shown in Figure 9. Though the MS concentration is higher than the critical concentration, it is still not high enough to form an aggregate for plugging.

It can be seen that the MS show the similar behaviors at  $F_p = 0.5$  and at  $F_p = 0$  when  $M$  equals 3, implying that physical bridging caused by geometric configuration of pores could counteract the effect of the electrostatic interaction at  $M = 3$ , no matter whatever  $F_p$  is. It is confirmed that it is the upper limit of physical bridging when the size of pore is three times that of the conventional MS.<sup>17,19</sup>

When the size of pores increases, MS at  $F_p = 0.5$  could form aggregates by electrostatic attraction, while MS at  $F_p = 0$  are likely to separate from each other and distributed in the entire space of the calculation cell. The simulation results prove that MS wrapped by negative shells could transport in the porous media.

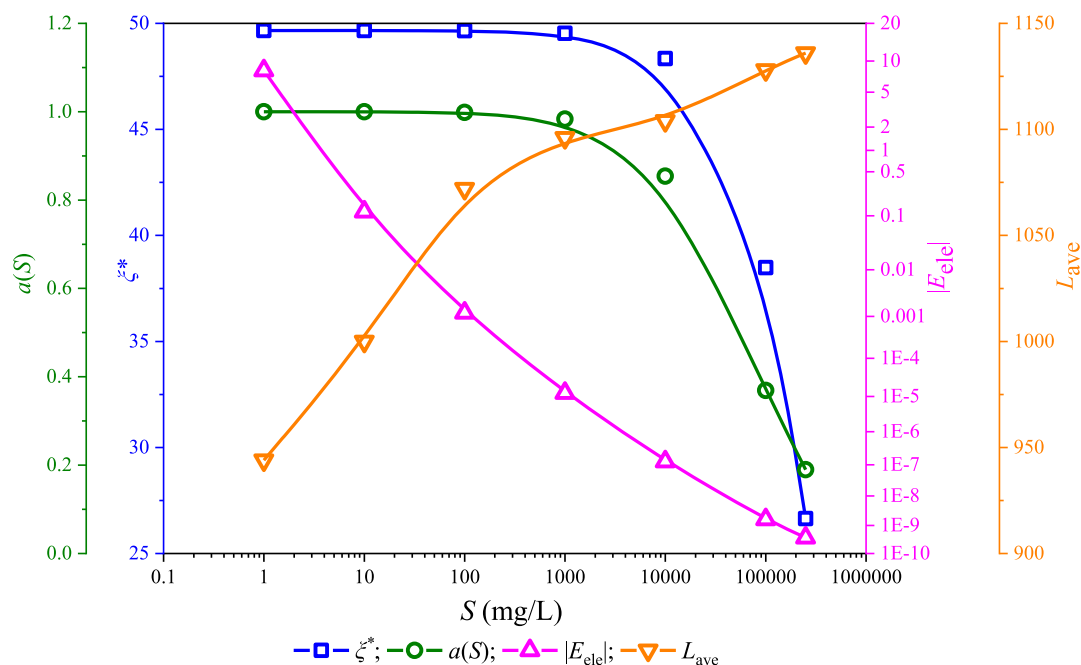
**3.2.2. Influence of the MS Concentration.** To investigate the plugging behaviors of the MS at  $F_p = 0.5$ , a series of simulations have been carried out and are shown in Figure 10 with different MS concentrations.

It can be seen that even the number of the MS is larger than the least needed to form an entire plugging structure at  $C_{\text{ms}} = 2.20 \times 10^{-2}$  ( $2.5N_{\text{min}}$ ), which is higher than the critical concentration, it is still difficult to form at least one entire plugging structure in porous media with different sizes. However, there are some small aggregates formed which may change the flow in porous media.

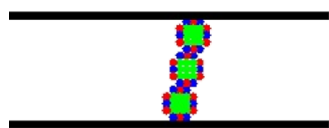
When the concentration of the MS reaches  $4.39 \times 10^{-2}$  ( $5N_{\text{min}}$ ), the entire plugging structures occur at  $M = 3$  and  $M = 8$ , though they seem to be different. As highlighted by red circles in Figure 10 at  $C_{\text{ms}} = 4.39 \times 10^{-2}$ , the number of MS for forming the plugging structures at  $M = 3$  is  $1N_{\text{min}}$ , while the number of which at  $M = 8$  is about  $1.5N_{\text{min}}$ .

When pore diameter increases to  $M = 16$ ,  $5N_{\text{min}}$  is not enough to form an entire plugging structure. By increasing the MS concentration to  $6.59 \times 10^{-2}$  ( $7.5N_{\text{min}}$ ), an entire plugging structure occurs in the calculation cell, and the number of MS for forming the structure highlighted by red circle at  $C_{\text{ms}} = 6.59 \times 10^{-2}$  is about  $2N_{\text{min}}$ , larger than that at  $C_{\text{ms}} = 4.39 \times 10^{-2}$  at  $M = 3$  or 8. At  $C_{\text{ms}} = 6.59 \times 10^{-2}$  in the small pores, more plugging structures are formed as a result of the increased number of MS at  $M = 3$ , and the size of the plugging structure at  $M = 8$  becomes larger, as 1.5 or 2 times of which at  $C_{\text{ms}} = 4.39 \times 10^{-2}$ .

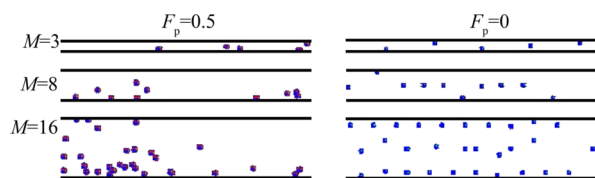
The plugging behaviors, as shown in Figure 10, have proved that the MS with mixed charges could improve the upper limit of physical bridging for conventional MS, which is triple of the MS diameter,<sup>17,19</sup> and break through the pore throat matching



**Figure 7.** Dependence of  $\xi^*$ ,  $a(S)$ ,  $E_{\text{ele}}$  and  $L_{\text{ave}}$  on  $S$  at  $C_{\text{ms}} = 1.14 \times 10^{-3}$ ,  $T = 95$  °C, and  $F_p = 0.5$ .



**Figure 8.** Scheme of the minimum plugging structure at  $M = 3$ .



**Figure 9.** MS in porous media with different pore sizes at  $C_{\text{ms}} = 1.32 \times 10^{-2}$ .

theory,<sup>17–19</sup> which can be adopted to plug larger pores by electrostatic interaction rather than physical bridging. To avoid plugging near the injection well, the MS will be wrapped by negatively charged shell to move deeply into the reservoir. Moreover, to achieve adaptive in-deep conformation control in the heterogeneous reservoir, it should be mentioned that the higher MS concentration is also important to efficiently plug high permeability reservoirs with low oil saturation.

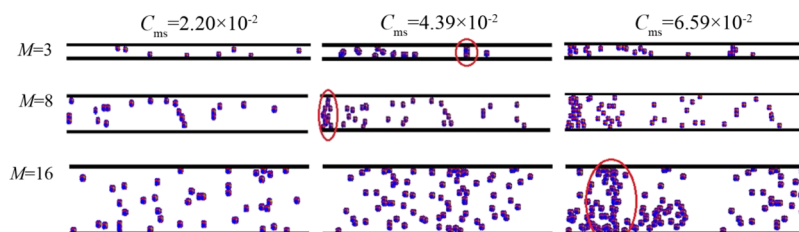
**3.3. Charge Distribution.** All the discussion above are about the random distribution of charges on the MS surface,

but different modes of charge distribution on the MS surface would influence the electrostatic interaction between MS. Two models of charge distribution, block mode and random mode, are discussed in this section at  $F_p = 0.5$ . Figure 11 schematically shows these two models, where positive and negative charges are drawn as red and blue spots, respectively, on the MS surface.

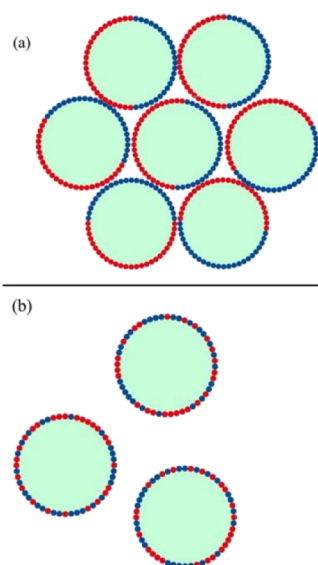
The most extreme block charge distribution on the MS surface is charged Janus particle,<sup>48–50</sup> as shown in Figure 11a that there are only two segments on the MS surface, one is positively charged, and the other is negatively charged. All charges face opposite ones on the nearby MS surface at an appropriate position when electrostatic attraction reaches its maximum, as shown in Figure 11a, which is thermodynamically favorable to induce the MS to form large aggregates. On the other hand, at a random mode, as shown in Figure 11b, it is hard to match all positive and negative segments. Consequently, electrostatic attraction could be much stronger at the block mode than that at the random mode.

The assembling behaviors of MS at  $F_p = 0.5$  with different charge distribution modes at  $C_{\text{ms}} = 3.43 \times 10^{-3}$  are shown in Figure 12.

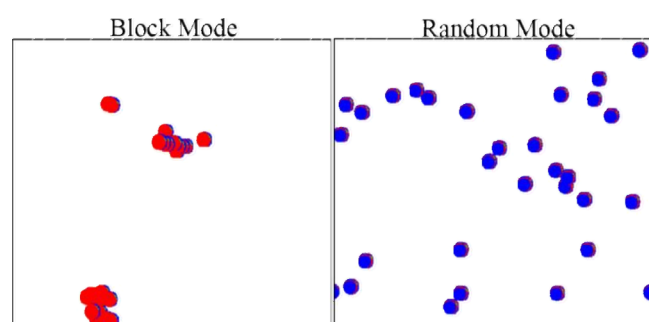
MS at the block mode show stronger electrostatic attraction, leading to larger aggregates than that at the random mode. For the block mode, aggregates are formed by 7–10 MS. Because of the small screening length between aggregates,<sup>48,49</sup> the



**Figure 10.** Self-assembling and plugging behavior of MS at  $F_p = 0.5$  in porous media.



**Figure 11.** Scheme of different charge distribution: (a) block mode and (b) random mode ○ (red): positive charge; ○ (blue): negative charge.



**Figure 12.** Self-assembling behaviors of MS at  $F_p = 0.5$  with different charge distribution modes at  $C_{ms} = 3.43 \times 10^{-3}$ .

electrostatic interaction between these aggregates is screened. Therefore, further simulation will not yield larger aggregates but the phase separation.<sup>50</sup> MS at the random mode are separated and distributed all over the space in the calculation cell and form small aggregates by 2–3 MS, less than that at the block mode.

All the self-assembling factors based on Figure 12 are shown in Table 1. It can be seen that  $L_{min}$  and  $L_{ave}$  at the block mode

**Table 1.** Self-Assembling Factors of MS at Different Charge Distribution Modes at  $F_p = 0.5$

charge distribution	$L_{ave}$	$L_{min}$	$CV_L$	$D_{ave}$
block mode	737	24.0	0.78	66
random mode	881	65.6	0.40	19,520

are significantly less than that at the random mode, and the values of  $CV_L$  show opposite trends, which confirms that MS at the block mode are distributed more unevenly by stronger self-assembling than at the random mode.

It is shown in Table 1 that  $D_{ave}$  at the block mode is significantly less than that at the random mode. MS at the block mode are unlikely to move in water solution by strong electrostatic interactions, which is at a disadvantage in simulation for its strong initial state dependence, but will be

helpful for plugging the highly permeable layers for adaptable profile control and improving oil recovery because MS at the block mode would stop at a fixed point after degrading shells and form aggregates for effective plugging as the result of their less motility.

#### 4. CONCLUSIONS

Monte Carlo simulation was used to systematically study the self-assembling and plugging behavior of core–shell MS with both negative and positive charges on the core surface and only negative charges on the shell surface.

- (1)  $D_{charge}$  and  $F_p$  are the key factors in influencing the self-assembling behavior of the MS along with concentration, temperature, and salinity. The increase in  $D_{charge}$  would enhance the electrostatic interaction between the MS. Aggregates were formed when  $F_p$  was in the range of 0.3–0.7 by electrostatic attraction, and the largest aggregates were found when  $F_p$  equaled 0.5. High concentration, high temperature, and low salinity would increase the electrostatic interaction between the MS.
- (2) It is confirmed that the MS with mixed charges could break through conventional size matching theory and conduct an effective plugging performance in highly permeable layers with low oil saturation by electrostatic attraction along with physical bridging for EOR.
- (3) It is helpful for the MS with mixed charges to form large aggregates to plug the highly permeable layers when charges are block distributed on the MS surface.

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