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Investigation of carbon dioxide solubility in various families of deep eutectic solvents by the PC-SAFT EoS

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Having been introduced in 2003, Deep Eutectic Solvents (DESs) make up a most recent category of green solvents. Due to their unique characteristics, and also their tunable physical properties, DESs have shown high potentials for use in various applications. One of the investigated applications is CO₂ absorption. The thermodynamic modeling of CO₂ solubility in DESs has been pursued by a number of researchers to estimate the capacity and capability of DESs for such tasks. Among the advanced equations of state (EoSs), the Perturbed Chain-Statistical Associating Fluid Theory (PC-SAFT) is a well-known EoS. In this study, the performance of the PC-SAFT EoS for estimating CO₂ solubility in various DESs, within wide ranges of temperatures and pressures, was investigated. A large data bank, including 2542 CO₂ solubility data in 109 various-natured DESs was developed and used for this study. This is currently the most comprehensive study in the open literature on \mbox{CO}_2 solubility in DESs using an EoS. For modeling, the DES was considered as a pseudo-component with a 2B association scheme. CO₂ was considered as both an inert and a 2Bcomponent and the results of each association scheme were compared. Considering the very challenging task of modeling a complex hydrogen bonding mixture with gases, the results of AARD% being lower than 10% for both of the investigated association schemes of CO₂, showed that PC-SAFT is a suitable model for estimating CO2 solubilities in various DESs. Also, by proposing generalized correlations to predict the PC-SAFT parameters, covering different families of DESs, the developed model provides a global technique to estimate CO₂ solubilities in new and upcoming DESs, avoiding the necessity of further experimental work. This can be most valuable for screening and feasibility studies to select potential DESs from the innumerable options available.

KEYWORDS

association schemes, DES (deep eutectic solvents), $\rm CO_2$, vapor-liquid equilibria (VLE), phase behavior

Introduction

Global warming is one of the most important issues of this century. Since 1980, an increase of about 0.6 C in the mean temperature of the globe (both the northern and southern hemispheres) has been reported (Florides and Christodoulides, 2009). The emissions of greenhouse gases, such as carbon dioxide, methane, and nitrous oxide into the atmosphere have their impact on this environmental crisis. Among the greenhouse gases, CO₂ plays a major role (Yamasaki, 2003; Florides and Christodoulides, 2009; Ali et al., 2014). Over the past decades, the concentration of carbon dioxide in the atmosphere has increased, partly because of industrial activities. Particularly, the burning of fossil fuels such as natural gas, petroleum, and coal in various industries causes CO₂ emissions (Yamasaki, 2003; Li et al., 2019). Therefore, the absorption of this gas is a serious concern (Mulia et al., 2017). One of the commonly used methods is absorption by conventional solvents. However, most conventional solvents are not sustainable and have, themselves, caused environmental damage in the recent decades. Finding sustainable and environmentally-friendly solvents, which have the desired properties for CO₂ absorption, is vital. In this respect, Deep Eutectic Solvents (DESs) are recently proposed green solvents which have also been investigated by researchers for CO2 absorption (Abbott et al., 2003; Koel, 2005; Wells and Coombe, 2006; Hasib-ur-Rahman et al., 2010; Vega et al., 2010; Haghbakhsh et al., 2019).

A DES is a mixture, consisting of at least two components that have the ability to establish new hydrogen bonds between the constituents. They are usually created by mixing a hydrogen bond acceptor (HBA), commonly a quaternary ammonium or phosphonium salt, and a hydrogen bond donor (HBD), such as metal salts or organics acids. DESs possess a number of desirable properties, such as having low vapor pressure, as well as being task-specific, easy to synthesize, cheap, non-flammable, sustainable, and biodegradable (Smith et al., 2014; Altamash et al., 2017; Ma et al., 2017; Haghbakhsh et al., 2019; Haider et al., 2020; Khajeh et al., 2020).

These interesting properties have led to significant investigations on DESs in various fields. Researchers have studied DES applications covering, for example, nanotechnology (Smith et al., 2014), gas absorption (Mirza et al., 2017; Marcus, 2018; Li et al., 2019), catalytic reactions (Ilgen et al., 2009), purification of biodiesels (Abbott et al., 2007), biomass treatment (Xia et al., 2014) electrochemistry (Abbott et al., 2011), and drug solubilization (Morrison et al., 2009).

Regarding the field of gas absorption, up to now, researchers have focused on the absorption of CO_2 more than on other gases. Various DESs, having different chemical natures, have been considered for CO_2 absorption, and wide ranges of pressures and temperatures have been studied (Li et al., 2008; Zhang et al., 2012; Leron and Li, 2013a; Leron and Li, 2013b; Francisco et al., 2013; Leron et al., 2013; Chen et al., 2014; Li et al., 2014; Zubeir et al., 2014; Lu et al., 2015; Mirza et al., 2015; Deng et al., 2016; Ji et al., 2016; Zubeir et al., 2016; Altamash et al., 2017; Ghaedi et al., 2017; Liu et al., 2017; Sarmad et al., 2017; Altamash et al., 2018; Haider et al., 2018; Li et al., 2018; Zubeir et al., 2018; Liu et al., 2019; Wang et al., 2019). These studies have accumulated a data bank for CO₂ absorption by DESs, providing vital information for pilot or industrial planning. Although many DESs have been investigated, their number is insignificant compared to the number of DESs remaining uninvestigated. There are countless DESs and they differ greatly in nature and variation. But the experimentation process is time-consuming and enatils high expenses, and so, investigating CO2 solubility for all is not possible. Therefore, developing global thermodynamic models for the estimation of CO₂ solubility in various DESs is a recommended procedure to overcome the mentioned limitations.

Besides, since DESs have been introduced only recently, few thermodynamic models have been investigated for their phase behavior with CO₂ (Florides and Christodoulides, 2009; Zubeir et al., 2014; Mirza et al., 2015; Zubeir et al., 2016; Animasahun et al., 2017; Dietz et al., 2017; Haghbakhsh and Raeissi, 2017; Lloret et al., 2017). Simple cubic equations of state (EoSs), such as the Peng-Robinson (PR) and modified Peng-Robinson have been considered by some researchers (Florides and Christodoulides, 2009; Zubeir et al., 2014; Mirza et al., 2015). In these studies, a DES was considered as a pseudo-pure compound whose critical properties were calculated using a group-contribution procedure, namely, the modified Lyderson-Joback-Reid model (Joback and Reid, 1987). To achieve more reliable results, some researchers considered more complex models. Haghbakhsh and Raeissi (2017) used the cubic plus association (CPA) equation of state to model the solubility of CO2 in various DESs. They also investigated different association schemes of CO2 and found that the inert scheme, with fewer fitting parameters, is the most accurate. Lloret et al. (2017) applied the Soft-SAFT (Soft-Statistical Associating Fluid Theory) EoS, to describe the density, surface tension, viscosity, and phase behavior of CO2 with several tetraalkylammonium chloride-based DESs. They explored the two approaches of either describing the DESs as pseudocompounds or treating them as combinations of their two independent constituents of HBA and HBD. Further, the effort was made to model CO2 solubility in DES systems using the PC-SAFT (Perturbed Chain-Statistical Associating Fluid Theory) EoS, as a well-known version of the SAFT type family (Zubeir et al., 2016; Dietz et al., 2017; Animasahun et al., 2017; Aminian, 2021; Cea-Klapp et al., 2020). For the first time, Zubeir et al. (2016) used the PC-SAFT to peruse the phase behavior of a few DES + CO₂ mixtures at a temperature range between 298.15 and 318.15 K and pressures up to 2 MPa. They presented two strategies for calculating CO₂ + DES phase behavior, where the DES was either considered as a pseudo-pure component, in which the pure parameters were

calculated based on density data, or it was treated as two individual components (HBA and HBD). Dietz et al. (2017) applied the pseudo-pure approach for PC-SAFT modeling of CO₂ phase behavior for a few hydrophobic DESs, and reported reliable results with respect to the experimental data. Animasahun et al. (2017) also used the PC-SAFT, as well as two different cubic EoSs (Peng-Robinson and Soave-Redlich-Kwong) to estimate CO2 solubilities in some DESs. They investigated 20 different CO2 + DES systems, in which choline chloride was considered as the HBA in 16 of the systems. Only the association scheme of 2B was considered for carbon dioxide. Further, Aminian (Aminian, 2021) studied the phase behavior of systems containing ionic liquids (ILs) and DESs using the PC-SAFT EoS. Their investigated DESs were tetrabutylammonium based on chloride and tetrabutylammonium bromide (as the HBA), and levulinic acid and diethylene glycol (as the HBD) at two different molar ratios. Their phase equilibrium results by PC-SAFT were compared to the COSMO-RS model. Cea-Klapp et al. (2020) also applied the PC-SAFT EoS for calculating the phase equilibria of DES systems. By using temperaturedependent binary interaction parameters, they succeeded to present more reliable results, especially in the case of liquidliquid equilibria in ternary systems.

Despite the advancements in DES modeling, there is still the need for further studies to improve the phase behavior modelling of such complex hydrogen-bonding components with CO2. In this study, the largest and most comprehensive data bank of CO₂ solubility in various families of DESs was developed, which is much more extended and generalized than any previous study. The experimental densities of DESs are used to optimize the pure PC-SAFT parameters of the DESs with different chemical natures. The phase behavior of carbon dioxide with various DESs is then modelled with the PC-SAFT EoS over wide ranges of pressures and temperatures. Two feasible association schemes of inert and 2B are considered for carbon dioxide, which has not yet been investigated for the PC-SAFT EoS. Furthermore, to make the model predictive, and so, suitable for feasibility and screening studies on DESs for carbon capture applications, generalized correlations are proposed for estimation of the PC-SAFT parameters.

Theoretical background

The perturbed-chain SAFT (PC-SAFT) equation of state

Gross and Sadowski (Gross and Sadowski, 2001; Gross and Sadowski, 2002) proposed the PC-SAFT equation of state based on the combination of different terms of the reduced Helmholtz energy. These terms are the reduced residual Helmholtz energy (\tilde{a}^{res}), the reduced hard-chain Helmholtz energy (\tilde{a}^{hc}), the

reduced dispersion Helmholtz energy (\tilde{a}^{disp}) , and the reduced associating contribution Helmholtz energy (\tilde{a}^{assoc}) , which is presented as follows.

$$\tilde{a}^{res} = \tilde{a}^{hc} + \tilde{a}^{disp} + \tilde{a}^{assoc} \tag{1}$$

The reduced hard-chain Helmholtz energy is expressed through (Eqs 2–(4) (Gross and Sadowski, 2001; Gross and Sadowski, 2002; Parvaneh and Shariati, 2017; Haghbakhsh et al., 2018a; Haghbakhsh et al., 2018b).

$$\tilde{a}^{hc} = \bar{m}\tilde{a}^{hs} - \sum_{i} x_{i} (m_{i} - 1) \ln g_{ii}^{hs}$$
(2)

$$\tilde{a}^{hs} = \frac{1}{\zeta_0} \left[\frac{3\zeta_1 \zeta_2}{1 - \zeta_3} + \frac{\zeta_2^3}{\zeta_3 (1 - \zeta_3)^2} + \left(\frac{\zeta_2^3}{\zeta_3^2} - \zeta_0 \right) \ln\left(1 - \zeta_3\right) \right]$$
(3)

$$g_{ij}^{hs} = \frac{1}{1-\zeta_3} + \frac{d_i d_j}{d_i + d_j} \frac{3\zeta_2}{(1-\zeta_3)^2} + \left(\frac{d_i d_j}{d_i + d_j}\right)^2 \frac{2\zeta_2^2}{(1-\zeta_3)^3}$$
(4)

where \tilde{a}^{hs} , m_i , x_i , and g_{ij}^{hs} are the reduced Helmholtz energy of the hard sphere, the number of segments, chain mole fraction, and radial pair distribution function, respectively. d_i is the temperature-dependent hard segment diameter for component *i*, which is calculated using the following equations (Gross and Sadowski, 2001; Gross and Sadowski, 2002; Parvaneh and Shariati, 2017; Haghbakhsh et al., 2018a; Haghbakhsh et al., 2018b).

$$d_i = \sigma_i \left[1 - 0.12 \exp\left(-\frac{3\varepsilon_i}{k_B T} \right) \right]$$
(5)

$$\zeta_n = \frac{\pi}{6} \rho \sum_i x_i m_i d_i^n \ n \in \{0, 1, 2, 3\}$$
(6)

where m_i (number of the segment), σ_i (segment diameter), and ε_i/k_B (segment energy) are the pure component parameters that should be optimized based on experimental data.

The functionality of the dispersion (\tilde{a}^{disp}) and associating (\tilde{a}^{assoc}) contributions are given through the following equations (Gross and Sadowski, 2001; Gross and Sadowski, 2002; Parvaneh and Shariati, 2017; Haghbakhsh et al., 2018a; Haghbakhsh et al., 2018b).

$$\tilde{a}^{disp} = -2\pi\rho I_1 \overline{m^2 \varepsilon \sigma^3} - \pi\rho \overline{m} C_1 I_2 \overline{m^2 \varepsilon^2 \sigma^3}$$
(7)

$$\tilde{a}^{assoc} = \sum_{i} x_i \sum_{A_i} \left(\ln X^{A_i} - \frac{X^{A_i}}{2} + \frac{M_i}{2} \right)$$
(8)

$$X^{A_i} = \left(1 + \rho \sum_j x_j \sum_{B_j} X^{B_j} \Delta^{A_i B_j}\right)^{-1} \tag{9}$$

$$\Delta^{A_i B_j} = g_{ij}^{seg} \kappa^{A_i B_j} \sigma_{ij}^3 \left(\exp\left(\frac{\varepsilon^{A_i B_j}}{kT}\right) - 1 \right)$$
(10)

where X^{Ai} , M_{i} , and Δ^{AiBj} are the mole fraction of component *i* that is not bonded at site *A*, the number of association sites, and the association strength, respectively. In addition to m_i , σ_i , and ε_i/k_B , the effective association volume (κ^{AiBi}) and association energy TABLE 1 The values of optimized PC-SAFT parameters for the investigated DESs in this study and carbon dioxide^b.

Abbr.	m _i	σ_i (Å)	ε_i/k (K)	AARD %
DES1	3.6803	3.6018	420.74	0.26
DES2	9.4497	2.6755	309.65	0.28
DES3	8.9837	2.7142	327.52	0.23
DES4	7.0125	2.9335	340.12	0.23
DES5	10.3775	2.4586	343.99	0.44
DES6	9.3189	2.4892	336.29	0.4
DES7	8.7806	2.4332	339.50	0.53
DES8	9.7048	2.6265	318.15	0.09
DES9	3.2933	3.1822	381.91	0.15
DES10	3.4444	3.2491	355.21	0.17
DES11	3.4128	3.8870	335.16	0.05
DES12	3.4170	3.6864	358.76	0.02
DES13	3.3869	3.6223	354.27	0.03
DES14	3.5068	3.8034	332.58	0.06
DES15	3.4600	3.6919	332.86	0.13
DES16	3.5507	4.1042	327.82	0.05
DES17	3.5021	3.9730	327.72	0.02
DES18	3.4751	3.9429	332.31	0.03
DES19	7.5169	2.7308	359.28	0.69ª
DES20	6.9359	2.8935	349.74	0.67ª
DES21	7.1671	2.8281	342.91	0.59ª
DES22	6.6122	2.8056	380.24	0.57ª
DES23	5.7468	3.04907	407.43	0.63ª
DES24	3.1064	3.4753	387.70	0.15
DES25	3.4218	3.4959	395.86	0.12
DES26	3.3837	3.3711	348.92	0.05
DES27	4.3270	3.0785	350.00	0.11
DES28	4.3312	3.2648	391.45	0.17
DES29	3.6904	3.4178	390.63	0.17
DES30	4.6418	3.2047	393.62	0.10
DES31	5.3061	3.0173	332.52	0.10
DES32	6.6024	3.1179	348.71	0.70ª
DES33	7.8434	2.6487	356.71	0.66ª
DES34	6.3107	2.9103	345.30	0.30
DES35	4.6314	3.2144	361.14	0.22
DES36	3.7883	3.1277	320.39	0.30
DES3/	6.2709	3.1457	368.99	0.69
DE536	5.4619 7.5212	2.5881	343.22	0.14
DE339	/.5215	2.6746	254.00	0.08
DES40	5 3 4 0 6	2.7601	310.00	0.07
DE\$41	0.1060	2.9241	310.00	0.42
DES42	7.000	2.8825	352.35	0.21
DES44	5 5588	3 1125	341.30	0.08
DESH	6 1204	2 9585	396.20	0.60ª
DES46	5.1851	2.9327	284.13	0.62
DES47	5.4774	3.0834	323.72	0.10
DES48	3.7486	3.4475	291.86	0.08
DES49	3.0017	3.6851	280.52	0.09
DES50	6.3275	3.0243	377.26	0.66ª
DES51	7.1170	2.8502	347.81	0.62ª
DES52	7.1606	2.845	355.33	0.62ª
DES53	6.3374	2.8215	257.25	0.24

(Continued on following page)

ABLE 1 (Continued) The values of	optimized PC-SAFT parameters	for the investigated DESs	in this study and carbon dioxide ^b

Abbr.	m _i	σ_i (Å)	ε_i/k (K)	AARD %
DES54	5.3589	2.9327	241.00	0.26
DES55	5.1909	2.9327	229.25	0.24
DES56	9.0710	2.8000	330.58	0.15
DES57	8.7878	2.8324	317.32	0.24
DES58	3.4365	3.2789	353.06	0.49ª
DES59	3.3586	3.1858	360.18	0.27
DES60	3.3674	3.1902	383.90	0.68ª
DES61	10.5724	2.5122	323.10	0.15
DES62	10.5806	2.5346	362.07	0.17
DES63	10.5485	2.5390	361.91	0.19
DES64	11.0243	3.3621	304.89	0.07
DES65	11.0359	3.3701	305.57	0.07
DES66	6.3126	3.0152	372.90	0.64ª
DES67	6.0238	2.9766	358.31	0.61ª
DES68	6.8842	2.9122	387.74	0.24
DES69	9.5777	2.6250	347.43	0.26
DES70	6.7541	3.2009	342.42	0.67ª
DES71	6.3977	3.1206	378.56	0.54ª
DES72	7.8481	3.5327	337.11	0.06
DES73	11.7300	2.6760	303.76	Zubeir et al. (2016)
DES74	10.5328	2.6760	338.00	Zubeir et al. (2016)
DES75	8.7261	2.9327	266.40	0.08
DES76	8.9204	2.8600	330.34	0.61ª
DES77	7.2637	3.0673	366.66	0.60ª
DES78	6.8383	2.9416	341.56	0.60ª
DES79	6.4777	2.9094	387.90	0.60ª
DES80	6.1411	3.0882	357.80	0.61ª
DES81	9.5816	2.9376	321.28	0.65ª
DES82	8.3764	2.9603	339.72	0.64ª
DES83	7.2833	3.0302	357.95	0.63ª
DES84	6.4463	2.7725	356.45	0.58ª
DES85	6.4289	2.7432	382.36	0.58ª
DES86	8.6644	2.9327	252.88	0.14
DES87	3.9823	3.7122	365.60	0.02
DES88	4.0299	3.7590	364.79	0.06
DES89	8.0400	2.5831	329.75	0.57ª
DES90	7.2645	2.5935	365.81	0.56ª
DES91	3.2607	3.7539	599.88	Zubeir et al. (2016)
DES92	5.5147	3.1379	280.15	0.10
DES93	8.8536	2.8989	344.45	0.60ª
DES94	5.2004	3.2659	350.74	0.05
DES95	4.9495	2.7400	379.67	0.48ª
DES96	2.9824	3.5678	506.01	Zubeir et al. (2016)
DES97	15.4820	3.1583	317.42	Dietz et al. (2017)
DES98	14.8000	3.2400	382.09	Dietz et al. (2017)
DES99	15.3220	3.1533	307.11	Dietz et al. (2017)
DES100	7.2315	2.5414	359.78	0.58ª
DES101	6.1747	2.7751	352.67	0.55 ^b
DES102	5.8932	2.6729	340.80	0.56ª
DES103	6.5848	2.7365	369.45	0.53ª
DES104	6.2763	2.7635	364.94	0.55ª
DES105	6.8388	2.7936	353.41	0.63ª
			(Continued on following page)

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Abbr.	m_i	σ_i (Å)	ε_i/k (K)	AARD %
DES106	6.2883	2.9043	396.64	0.60ª
DES107	6.7412	2.9691	359.07	0.60^{a}
DES108	3.7112	3.3667	404.08	0.29
DES109	8.9137	2.6324	335.54	0.10
CO ₂ (inert)	2.0729	2.7852	169.21	Gross and Sadowski, (2001)
CO ₂ (2B) ^c	2.1051	2.7841	162.08	Baramaki et al. (2019)

TABLE 1 (Continued) The values of optimized PC-SAFT parameters for the investigated DESs in this study and carbon dioxide^b.

^aDensity data was obtained according to Haghbakhsh et al.'s density model (Haghbakhsh et al., 2019).

^bThe values of the ($\kappa^{A(B)}$) and ($\varepsilon^{A(B)/k}$) parameters were considered as 0.1 and 5,000, respectively, for all of the investigated DESs (Zubeir et al., 2016; Dietz et al., 2017).

^cThe values of the (κ^{AiB}) and (ϵ^{AiB}/k) parameters of CO₂ for the association schemes of 2B are 0.03318 and 576.7, respectively (Baramaki et al., 2019).

 (ε^{AiBi}/k) are also pure compound constants that must be considered for associating compounds.

Investigated compounds

In this research, the largest data bank, up to date, of CO₂ solubility in DESs, consisting of 109 various natured DESs, was collected from the open literature. This data bank consists of 2,542 data points, covering wide ranges of pressures and temperatures. Supplementary Table S1 (Supplementary Material) presents the pressure, temperature, and CO2 solubility ranges of the investigated DESs in this study. The corresponding literature reference of each DESs is also given in Supplementary Table S1 (Li et al., 2008; Leron and Li, 2013a; Leron and Li, 2013b; Francisco et al., 2013; Leron et al., 2013; Chen et al., 2014; Li et al., 2014; Zubeir et al., 2014; Lu et al., 2015; Mirza et al., 2015; Deng et al., 2016; Ji et al., 2016; Zubeir et al., 2016; Altamash et al., 2017; Ghaedi et al., 2017; Liu et al., 2017; Sarmad et al., 2017; Altamash et al., 2018; Haider et al., 2018; Li et al., 2018; Zubeir et al., 2018; Liu et al., 2019; Wang et al., 2019). In the case of those limited DESs for which solubility data were presented by more than one research group, no discriminations were carried out and all of the data by all groups were considered in the development of the model.

Results and discussion

The pseudo-component approach was used for modeling $CO_2 + DES$ systems, which is a well-known model having been used for various DESs (Zubeir et al., 2016; Dietz et al., 2017; Lloret et al., 2017). The association scheme of 2B, as presented by Huang and Radosz (Huang and Radosz, 1990; Huang and Radosz, 1991), was considered for the pseudo-component DESs. The reason for considering the pseudo-component approach, and also choosing the 2B association scheme for DESs is by following the recommendations of many published

studies (Zubeir et al., 2016; Haghbakhsh and Raeissi, 2017; Lloret et al., 2017; Dietz et al., 2017; Animasahun et al., 2017; Aminian, 2021; Cea-Klapp et al., 2020). Almost all of the literature that have used the PC-SAFT EoS for modeling of DESs, have recommended the 2B association scheme for a pseudo-component DES. The schematic representation of the considered association schemes of the investigated systems are presented as Figure S1 of the Supplementary Material. For CO_2 , the inert and 2B association schemes are the most commonly used association schemes in the literature, as indicated by the studies of Haghbakhsh and Raeissi, and also Baramaki et al. (Haghbakhsh and Raeissi, 2017; Baramaki et al., 2019). Therefore, we chose to investigate and compare both of these schemes in this study.

To model the phase behavior of CO₂ + DES systems, the first calculation step was to estimate the PC-SAFT pure parameters of m_i (segment number), σ_i (segment diameter), u_i/k (segment energy parameter), $\kappa^{A_{iBj}}$ (effective association volume), and $\varepsilon^{A_{iBj}}/k$ (association energy). These five parameters are optimized to the liquid density data of the DESs based on Eq. (11) as the objective function.

$$OF = \sum_{i}^{Np} \left(\frac{\rho_{i}^{\exp \cdot} - \rho_{i}^{calc.}}{\rho_{i}^{\exp \cdot}} \right)^{2}$$
(11)

in which, $\rho_i^{exp.}$ and $\rho_i^{calc.}$ are the experimental and calculated density, respectively, and *Np* is the number of the data points.

However, in order to reduce the number of adjustable parameters of the PC-SAFT EoS for DESs, the effective association volume (κ^{AiBj}) and association energy (ε^{AiBj}/k) parameters were considered as 0.1 and 5,000, respectively (Zubeir et al., 2016; Dietz et al., 2017).

The number of literature density data for each DES, the range of liquid densities, and the corresponding reference are given in Supplementary Table S2. However, for some of the investigated DESs, no density data have been reported in the open literature. Thus, for those DESs, distinguished in Supplementary Table S3, the general density model of Haghbakhsh et al. (Haghbakhsh et al., 2019) was used to generate the density data. Haghbakhsh et al.'s density model (Haghbakhsh et al., 2019) is a function of



temperature, critical volume, critical temperature, and acentric factor of the DES pseudo-component. The modified Lydersen-Joback-Reid approach (Valderrama and Robles, 2007; Valderrama et al., 2008) and the Lee-Kesler mixing rules, which were presented by Knapp et al. (1982), were used to calculate the critical properties and acentric factors of the DESs that lacked density data. The results are presented in Supplementary Table S4 of the Supplementary material.

The three pure component parameters of PC-SAFT, optimized to the collected density data of the investigated DESs, are presented in Table 1. For some of the investigated DESs, the values of the PC-SAFT parameters were previously given in published studies, and in these cases, the literature values were considered, as reported in Table 1. For CO₂, the values of the three pure component PC-SAFT parameters for both the association schemes of 2B and inert have been reported in Table 1. Furthermore, the effective association volume (κ^{AiBj}) and association energy (ε^{AiBj}/k) parameters of CO₂ for the association schemes of 2B are 0.03318 and 576.7, respectively (Baramaki et al., 2019).

In order to check the consistency of the values of the calculated critical properties and the optimized PC-SAFT parameters for the investigated DESs, the thermodynamic evaluation of the global map of Polishuk et al. (2013) has been carried out. For this purpose, values for the reduced critical temperatures have been calculated according to Eq. (12). Since these values were calculated to be greater than 1 for all of the DESs, according to the thermodynamic analysis of Polishuk et al. (2013), no unrealistic values have been found for the calculated critical properties and optimized PC-SAFT parameters. The details of this evaluation are given in Supplementary Table S5 of the Supplementary Material.







$$T_c^* = \frac{T_c}{\left(\varepsilon/k\right)} \tag{12}$$

Also, in order to have a more comprehensive investigation and provide predictive ability for the PC-SAFT model, a generalized correlation for the estimation of the PC-SAFT pure component parameters of the studied DESs was developed in this work, as presented by Eq. (13).

$$m\sigma^3 = 1.6773MW - 38.764 \tag{13}$$

where is *m* is the segment number and σ is the segment diameter, which are related to the molecular weight, *MW*, of the DES. The graphical behavior of the developed generalized correlation for the studied DESs is depicted in Figure 1. In this figure, the relations of $m\sigma^3$ of the PC-SAFT

Inert (CO₂)+ 2B (DES) 2B (CO₂) + 2B (DES) Predictive Correlative Predictive Correlative k_{ij=}a+b.T $\mathbf{k}_{ij} = \mathbf{0}$ $\mathbf{k}_{ij} = \mathbf{0}$ k_{ij=}a+b.T AARD% AARD% b AARD% AARD% b a a DES1 0.00013 1.53×10^{-4} 0.00015 91.22 44.48 126.56 44.48 2.19×10^{-4} -0.11915 2.22×10^{-4} -0.11216 2.35×10^{-4} DES2 64.98 1.61 55 74 1.57 DES3 74.24 1.87 -0.11839 1.75×10^{-4} 67.35 1.85 -0.11027 1.84×10^{-4} DES4 -0.07758 1.43×10^{-4} 1.57 -0.06605 1.51×10^{-4} 47.11 1.62 30.64 DES5 96.54 7.35 -0.27373 $4.27\,\times\,10^{-4}$ 95.75 7.37 -0.27141 4.43×10^{-4} DES6 94.78 4.50 -0.26806 4.49×10^{-4} 93.38 4.56 -0.26533 4.70×10^{-4} DES7 97.22 8.75 -0.30329 4.97×10^{-4} 96.40 8.85 -0.30089 5.19×10^{-4} DES8 3.03 -0.28205 6.06×10^{-4} 80.35 3.07 -0.27692 6.22×10^{-4} 84.25 DES9 50.18 15.13 0.18890 -7.15×10^{-4} 23.12 15.10 0.21407 -7.15×10^{-4} DES10 0.22557 -7.79×10^{-4} 17.02 -7.91×10^{-4} 35.17 16.54 27.00 0.25662 DES11 12.60 0.01029 0 11.99 0.03583 0 15.97 36.44 DES12 14.13 9.89 -0.01059 0 18.28 9.17 0.01403 0 DES13 -0.00483 12.19 0 11.50 0.02027 12.62 28.35 0 DES14 23.36 8.22 0.00028 6.12×10^{-5} 59.81 7.97 0.00017 1.37×10^{-4} DES15 10.69 4.84 0.02300 -4.94×10^{-5} 46.84 4.78 0.04894 -4.82×10^{-5} DES16 29.48 10.83 0.03073 0 55.82 10.33 0.05537 0 DES17 40.11 8.17 0.03675 0 75.15 4.64 0.06205 0 DES18 58.86 11.08 0.04603 0 100.48 10.60 0.07128 0 DES19 9.00 -0.09664 0 85.68 8.62 -0.08488 0 89.24 DES20 0.01535 0 0.02943 0 47.49 46.35 51.00 46.26 DES21 75.08 5.62 -0.06410 0 66.55 5.43 -0.05068 0 DES22 21.23 -0.11819 0 20.76 90.35 -0.105130 92.91 DES23 90.59 17.11 -0.10412 0 87.14 16.58 -0.09010 0 0.22373 DES24 27.27 13.94 -6.74×10^{-4} 69.48 13.93 0.25247 -6.81×10^{-4} 10.08 -7.41×10^{-4} -7.77×10^{-4} DES25 14.51 0.23499 31.66 10.15 0.27122 DES26 242.5 6.73 0.00015 2.53×10^{-4} 401.24 5.85 0.00017 3.41×10^{-4} DES27 41 47 3 69 -0 16969 6.13×10^{-4} 105 49 3 63 -0.15445 6.33×10^{-4} DES28 2.35 -0.08064 3.33×10^{-4} 105.76 2.38 -0.06356 3.41×10^{-4} 46.44 DES29 0.00023 2.00×10^{-4} 292.64 0.00466 2.57×10^{-4} 175.43 3.72 3.59 DES30 10.77 2.37 0.01453 -3.14×10^{-5} 54.45 2.35 0.03053 -2.42×10^{-5} DES31 7.95 2.54 -0.00028 1.50×10^{-5} 50.52 2.51 0.00026 7.44×10^{-5} DES32 65.88 11.30 0.13579 -6.05×10^{-4} 55.84 11.70 0.16771 -6.54×10^{-4} DES33 96.49 12.59 -0.14354 0 95.36 12.43 -0.13270 0 DES34 $4.35\,\times\,10^{-4}$ 4.55×10^{-4} 42.47 4.26 -0.1632822.15 4.19 -0.15409DES35 -0.10102 $4.04\,\times\,10^{-4}$ 51.48 3.98 111.83 3.89 -0.08494 4.16×10^{-4} DES36 -0.2015469.60 14.24 7.22×10^{-4} 150.62 13.36 -0.17527 7.21×10^{-4} DES37 70.39 12.11 0.00014 -1.99×10^{-4} 60.92 12.61 0.01277 -1.88×10^{-4} DES38 -0.19128 2.78×10^{-4} 87.24 -0.18509 2.92×10^{-4} 90.09 1.64 1.64 $2.60\,\times\,10^{-4}$ DES39 86.14 1.87 -0.17459 81.77 1.84 -0.16806 2.77×10^{-4} DES40 81.74 1.32 -0.13052 1.52×10^{-4} 75.6 1.28 -0.12166 1.67×10^{-4} DES41 6.93×10^{-4} 38.08 4.69 -0.2540316.00 5.85 -0.21010 6.25×10^{-4} DES42 -0.20774 3.74×10^{-4} -0.20266 3.88×10^{-4} 87.82 1.63 84.68 1.62

TABLE 2 The values of optimized parameters and AARD% for the two predictive and correlative modes of PC-SAFT EoS by considering two association schemes for CO₂.

(Continued on following page)

	Inert (CO_2)+ 2B (DES)				$2B (CO_2) + 2B (DES)$			
	Predictive	Correlative			Predictive	Correlative		
	$\mathbf{k_{ij}} = 0$	k _{ij=} a+b.T			$\mathbf{k}_{ij} = 0$	k _{ij=} a+b.T		
	AARD%	AARD%	a	b	AARD%	AARD%	a	b
DES43	60.82	1.46	-0.12685	2.59×10^{-4}	48.62	1.45	-0.11834	2.75×10^{-4}
DES44	17.08	2.00	-0.06124	2.28×10^{-4}	58.75	1.95	-0.04801	2.43×10^{-4}
DES45	90.95	14.08	$1.07 \times 10-5$	-3.51×10^{-4}	87.80	14.17	0.03143	-4.06×10^{-4}
DES46	92.22	1.95	-0.12822	5.24×10^{-4}	173.20	2.12	-0.12631	5.90×10^{-4}
DES47	8.23	2.17	-0.13986	4.49×10^{-4}	41.11	2.13	-0.12790	4.70×10^{-4}
DES48	183.48	2.90	-0.07176	4.90×10^{-4}	291.85	2.91	-0.04673	4.98×10^{-4}
DES49	268.21	1.56	-0.06274	5.73×10^{-4}	408.56	1.51	-0.03684	5.94×10^{-4}
DES50	80.55	16.73	-0.08185	1.16×10^{-6}	74.09	17.04	-0.05477	-3.92×10^{-5}
DES51	93.37	10.13	-0.13390	0	91.19	10.45	-0.12079	0
DES52	95.00	2.95	-0.14492	0	93.37	2.70	-0.13232	0
DES53	59.52	13.15	0.09203	-1.99×10^{-4}	123.75	12.14	0.08996	-1.24×10^{-4}
DES54	148.94	10.05	-0.03571	3.35×10^{-4}	253.23	9.19	-0.01823	3.59×10^{-4}
DES55	179.70	11.61	0.00036	2.54×10^{-4}	298.03	10.60	0.00030	3.45×10^{-4}
DES56	62.22	4.11	-0.18903	4.56×10^{-4}	52.72	4.03	-0.18175	4.68×10^{-4}
DES57	43.85	5.20	-0.15278	3.96×10^{-4}	29.18	5.14	-0.14439	4.08×10^{-4}
DES58	65.43	9.33	-0.06193	3.09×10^{-4}	146.66	11.14	$1.35 \times 10-4$	2.06×10^{-4}
DES59	31.56	16.34	0.00023	-6.22×10^{-5}	20.99	18.70	0.10159	-2.87×10^{-4}
DES60	9.61	9.17	5.31 × 10-5	-3.67×10^{-6}	45.95	10.70	$3.12 \times 10-4$	7.80×10^{-5}
DES61	91.19	1.83	-0.15568	1.72×10^{-4}	89.07	1.86	-0.15005	1.81×10^{-4}
DES62	97.44	1.42	-0.20506	1.96×10^{-4}	96.89	1.38	-0.20029	2.02×10^{-4}
DES63	97.47	1.05	-0.20657	1.98×10^{-4}	96.92	1.06	-0.20309	2.08×10^{-4}
DES64	39.39	0.98	-0.02250	1.52×10^{-4}	59.71	0.98	-0.00839	1.38×10^{-4}
DES65	38.21	1.47	0.00616	5.60×10^{-5}	57.72	1.47	0.01427	6.30×10^{-5}
DES66	44.22	30.06	-0.03073	0	34.47	29.77	-0.01633	0
DES67	77.22	28.16	-0.06353	0	68.69	27.76	-0.04826	0
DES68	73.02	9.81	-0.05605	0	64.25	9.98	-0.04362	0
DES69	78.22	39.33	-0.04963	0	72.55	39.23	-0.04048	0
DES70	125.55	45.05	0.07112	0	192.68	44.96	0.08641	0
DES71	67.71	4.10	-0.05765	0	57.26	3.72	-0.04374	0
DES72	41.75	1.00	-0.02222	1.52×10^{-4}	68.61	1.17	-0.01099	1.57×10^{-4}
DES73	74.86	2.56	-0.13172	2.05×10^{-4}	69.74	2.32	-0.12671	2.17×10^{-4}
DES74	89.89	2.33	-0.16478	1.98×10^{-4}	87.67	2.08	-0.15906	2.07×10^{-4}
DES75	15.98	2.77	-0.13366	453×10^{-4}	44 26	2.78	-0.12424	4.71×10^{-4}
DE\$76	69.09	10.47	-0.06013	0	60.87	10.34	-0.04888	0
DE\$77	40.12	4 27	-0.02607	0	23.16	4 17	-0.01340	0
DES78	45.95	4.68	-0.03197	0	26.96	4.61	-0.01747	0
DF\$79	81 79	1.70	-0.07782	0	75.60	1.58	-0.06490	0
DES80	67.29	9.38	-0.05996	0	56.25	9.26	-0.04474	0
DES81	40.80	12 19	-0.02841	0	27.18	12 11	-0.01752	0
DES82	61 42	9.00	-0.04033	0	51 33	8 89	-0.03764	0
DES92	71.14	3.95	-0.06241	0	62.79	3.78	-0.04075	0
DES84	95.41	14.63	-0.13919	0	93.64	14.61	-0 12222	0
DE004	22.41	14.05	-0.13010	U	23.04	14.01	-0.12323	U

TABLE 2 (Continued) The values of optimized parameters and AARD% for the two predictive and correlative modes of PC-SAFT EoS by considering two association schemes for CO₂.

(Continued on following page)

	Inert (CO ₂)+ 2B (DES)				2B (CO ₂) + 2B (DES)			
	Predictive	Correlative k_ij=a+b.T			Predictive k _{ij} = 0	Correlative k_ij=a+b.T		
	$\mathbf{k_{ij}} = 0$							
	AARD%	AARD%	a	b	AARD%	AARD%	a	b
DES85	98.21	13.43	-0.16905	0	97.53	13.69	-0.15537	0
DES86	45.79	1.75	-0.11529	4.44×10^{-4}	82.85	1.77	-0.10450	4.61×10^{-4}
DES87	17.84	7.31	$7.42 \times 10-5$	4.00×10^{-5}	52.84	7.08	0.00426	9.32×10^{-5}
DES88	15.82	10.54	0.10802	-3.10×10^{-4}	44.85	10.29	0.13815	-3.39×10^{-4}
DES89	91.90	3.87	-0.10463	0	89.12	3.54	-0.09300	0
DES90	96.84	18.06	-0.13761	0	95.70	17.60	-0.12629	0
DES91	8.68	2.86	-0.04545	1.58×10^{-4}	50.73	2.92	-0.03230	1.70×10^{-4}
DES92	73.21	2.78	-0.09120	4.09×10^{-4}	132.18	2.80	-0.07432	4.23×10^{-4}
DES93	78.21	10.00	-0.07712	0	72.60	9.57	-0.06653	0
DES94	19.71	2.07	-0.10140	3.56×10^{-4}	59.39	2.12	-0.08789	3.71×10^{-4}
DES95	92.74	14.00	-0.11066	0	89.09	13.41	-0.09404	0
DES96	46.50	3.16	$3.20 \times 10-5$	6.47×10^{-5}	113.55	3.12	0.02309	5.85×10^{-5}
DES97	27.87	0.59	-0.05763	1.20×10^{-4}	21.06	0.62	-0.05198	1.20×10^{-4}
DES98	72.06	1.83	-0.11720	1.51×10^{-4}	69.84	2.03	-0.11460	1.54×10^{-4}
DES99	17.67	0.70	-0.04276	9.70×10^{-5}	9.53	0.58	-0.03989	1.08×10^{-4}
DES100	98.39	4.34	-0.15918	0	97.79	4.26	-0.14756	0
DES101	89.66	7.78	-0.09991	0	85.44	7.94	-0.08463	0
DES102	97.06	20.36	-0.16026	0	95.72	21.77	-0.14326	0
DES103	92.33	10.77	-0.10894	0	89.43	10.33	-0.09581	0
DES104	90.17	13.43	-0.10066	0	86.31	13.51	-0.08664	0
DES105	55.88	23.02	-0.03057	0	40.09	22.88	-0.01694	0
DES106	83.20	5.12	-0.07731	0	77.19	5.11	-0.06412	0
DES107	64.43	3.60	-0.05155	0	52.60	3.75	-0.03774	0
DES108	21.75	5.60	0.01153	0	83.18	4.95	0.03643	0
DES109	87.83	2.98	-0.09378	0	84.13	2.20	-0.08230	0
Total	63.77	8.08			84.65	8.12		

TABLE 2 (Continued) The values of optimized parameters and AARD% for the two predictive and correlative modes of PC-SAFT EoS by considering two association schemes for CO₂.

EoS with respect to the molecular weight are shown for all 109 investigated DESs. As can be seen, $m\sigma^3$ has an increasing behavior with increasing molecular weight. Despite the simplicity, this correlation succeeds to consider various DESs, having very different natures, with high accuracy.

Although the above correlation is global and can be used for all the DESs, we have also provided two family-specific correlations for higher accuracy. For the families of 1-choline chloride + n-levulinic acid (n = 3, 4, 5) and 1-tetrabutyl ammonium bromide + n-diethylene glycol (n = 2, 3, 4) specific correlations were developed and presented as Eqs (14), (15), respectively.

$$m\sigma^3 = 5.3361MW - 490.57 \tag{14}$$

$m\sigma^3 = 1.3983MW - 6.3921 \tag{15}$

Figures 2, 3 present the graphical behavior of these two specific family correlations with respect to molecular weight. As one would expect, one single generalized equation, correlated with only the molecular weight for all types of DESs with different natures and different molar ratios, is not as accurate (Figure 1) as the family-specific correlations, with constants that are fine-tuned to the particular structural family (Figures 2, 3).

Also, in order to investigate the predictive ability of the PC-SAFT model, CO_2 solubilities were calculated according to the two modes of prediction and correlation of PC-SAFT. In the prediction mode, the solubilities were achieved without considering any binary interaction parameters (k_{ij}), while in



the correlation mode, binary interaction parameters were considered according to the following equation, with the purpose to correct the segment-segment interactions of dissimilar chains (Gross and Sadowski, 2001).

$$\varepsilon_{ij} = \sqrt{\varepsilon_i \varepsilon_j} (1 - k_{ij}) \tag{16}$$

To involve the effect of temperature on the binary interaction parameters, the temperature functionality of Eq. (17) was taken into account.

$$k_{ij} = a + b \times T \tag{17}$$

The two adjustable parameters (*a* and *b*) were optimized based on the CO_2 solubility data in various DESs using the following objective function, and the values are reported in Table 2.

$$OF = \sum_{i}^{N_{P}} \left(\frac{x_{i}^{Exp.} - x_{i}^{Calc.}}{x_{i}^{Exp.}} \right)^{2}$$
(18)

The results of PC-SAFT modeling for CO_2 solubilities in the investigated DESs were estimated and the errors were calculated by calculating *AARD*%, as given by Eq. (19).

$$AARD\% = \frac{100}{Np} \sum_{i}^{N_{p}} \left| \frac{x_{i}^{Exp.} - x_{i}^{Calc.}}{x_{i}^{Exp.}} \right|$$
(19)

in which $x_i^{Exp.}$ and x_i^{Calc} are the experimental and calculated carbon dioxide solubilities, respectively, and N_P is the total number of data. Table 2 presents the calculated *AARD*% values for both the correlative and predictive modes, each also considering both the association schemes of 2B and inert for CO₂.

Based on the results of Table 2 for CO_2 + DES, the predictive PC-SAFT EoS had a total *AARD*% of 63.77 and 84.65% for the inert-2B and 2B–2B modes, respectively. Therefore, on the average, the inert association scheme for CO_2 results in lower



AARD% than the 2B association scheme, most particularly, for DESs with choline chloride or tetrabutylphosphonium bromide as their HBA. However, for the majority of DESs whose, pure PC-SAFT parameters were optimized based on the density data generated by Haghbakhsh et al.'s density model (Haghbakhsh et al., 2019), the results of the 2B association scheme had slightly lower *AARD*% values. But all in all, the results are not acceptable in these predictive modes of calculations. By considering adjusted binary interaction parameters, both of the association schemes improve significantly and produce acceptable errors. The inert-2B and 2B–2B cases resulted in total *AARD*% of 8.08% and 8.12%, respectively.

The trends between the calculated CO_2 solubility values by the PC-SAFT versus the corresponding experimental values are presented in Figure 4 for all of the investigated DESs, using both the association schemes of inert-2B and 2B–2B. A normal behavior is observed for the PC-SAFT by noticing that most of the results are located very close to the diagonal line. Also, this figure shows that the accuracy of PC-SAFT generally decreases in the region of high CO_2 absorption.

Figures 5–7 show pressure vs. CO_2 solubility for three random DESs at various temperatures. These three DESs are considered as representatives, applying the different methods of obtaining the pure PC-SAFT parameters. In Figure 5, the pure PC-SAFT parameters of choline chloride + diethylene glycol (1:4) were optimized based on its experimental density data, while in Figure 6, the pure PC-SAFT parameters of benzyltriethylammonium chloride (BTEAC) + acetic acid (1:2) were optimized based on the general density model of Haghbakhsh et al. (Haghbakhsh et al., 2019). Figure 7 represents the phase behavior of CO_2 with tetraethylammonium chloride (TEAC) + L-lactic acid (1:2), whose PC-SAFT parameters were taken from the literature. Figures 5–7 compare the trends of PC-SAFT



FIGURE 6

Comparison of two association schemes of PC-SAFT (inert-2B and 2B-2B) for solubility of CO₂ in benzyltriethylammonium chloride + acetic acid (1:2) (Sarmad et al., 2017) at the temperature of 298.15 K. The pure compoent PC-SAFT parameters of the DES were optimized using the density model of Haghbakhsh et al. (2019).



calculated phase behavior using both association schemes of inert and 2B to represent CO_2 . In all three figures, both the correlative and the predictive PC-SAFT results showed CO_2 solubility to have a linear function of pressure, consistent with the linear trend of the experimental data. This shows that PC-SAFT, even in its predictive mode, could successfully predict the solubility trends in the presented systems, however, it does need adjustment by including binary interaction parameters in order to produce



more reliable results with respect to the experimental values. The predictive PC-SAFT in Figure 6 shows overestimations of CO_2 solubility at fixed pressures, while it shows underestimations in Figures 5, 7. This shows a normal behavior for the predictive PC-SAFT, i.e., there is no systematic underestimation or overestimation by the model, as both cases are observed. Furthermore, these three figures show that the correlative PC-SAFT presents reliable agreement with the experimental values and trends for both the carbon dioxide association schemes of 2B and inert.



ammonium bromide (TBAB) + n-diethylene glycol (Haider et al., 2018) (n = 2, 3, and 4) by the correlative mode of PC-SAFT, at the temperature of 303.15 K.



For further details, the solubility of CO_2 in different HBAs (choline chloride, allyltriphenyl phosphonium bromide, and tetrabutyl ammonium bromide) with different HBDs and various molar ratios are presented in the Supplementary section (Supplementary Figures S2–S4). It can be seen from these Supplementary figures that upon increasing the molar ratios of the glycols (ethylene glycol, diethylene glycol or triethylene glycol) as the HBD components of the investigated DESs, the CO_2 solubility decreases. The developed PC-SAFT models, in all cases, could follow these trends quite well.

Figures 8–10 aim to compare members of the same family of DESs (identical HBA and HBD but various molar ratios). By increasing the molar ratio (HBA with respect to HBD) in each family, the DESs show different capacities and trends for CO_2

absorption. Figure 8 presents the correlative mode of the PC-SAFT model for choline chloride + n-furfuryl alcohol (n = 3, 4, and 5) at various molar ratios at a temperature of 333.15 K. As can be seen, the phase behavior of CO₂ with the chosen family of DES can be calculated precisely by both of the investigated schemes. In Figure 9, the phase behavior representations of CO₂ with 1-tetrabutyl ammonium bromide (TBAB) + n-diethylene glycol (n = 2, 3, and 4) are given at the temperature of 303.15 K. In this figure, by increasing the molar ratio of the HBD (diethylene glycol), CO2 absorption increases. The experimental trends are very well followed by both of the investigated association schemes. Figure 10 exhibits the CO₂ solubility in 1-allyltriphenyl phosphonium bromide + n-diethylene glycol family (n = 4, 10, and 16) at the temperature of 303.15 K. Opposite to the DES family of Figure 9, in Figure 10, by increasing the molar ratio of diethylene glycol in this family, the solubility of CO₂ is decreasing, which is also followed by the correlative mode of PC-SAFT with good agreement.

Based on the achieved results, the inert scheme for CO_2 , in general, shows better results compared to the 2B scheme when the predictive mode is considered (when neglecting binary interaction parameters). Despite this, the predictive mode does not give acceptable results with either of the schemes. However, when considering binary interaction parameters, both association schemes of inert and 2B for CO_2 show trustworthy estimations with respect to the experimental trends.

Conclusion

In contrast to previous studies focusing on a very limited number of DESs, in this study, the PC-SAFT EoS has been chosen as an associating EoS to estimate carbon dioxide solubilities in 109 deep eutectic solvents having different chemical natures over wide ranges of temperatures and pressures. This is indeed a thermodynamic challenge, considering that the DESs consist of various types of HBDs and HBAs, and at different molar ratios, resulting in complex interactions. High pressures further add to the challenge of thermodynamic modelling. Therefore, for the first time, this study gives an overview of the capabilities of this sophisticated model, as a tool for the general modelling of DES + CO₂ phase behavior. A large and most-recent data bank, consisting of 2,542 solubility data points, is used. To obtain the pure component parameters of PC-SAFT, which are not reported in the literature, a data bank of experimental densities was also collected, consisting of a total of 62 various DESs, with 656 density data points.

The pseudo-component approach was used in this study. The association scheme of 2B was considered for the DES pseudocomponents, while the association schemes of inert and 2B were both investigated for carbon dioxide. For a more extensive investigation on the capability of the PC-SAFT EoS, predictive and correlative modes were both studied. In the predictive mode, the CO₂ solubility was calculated without considering any binary interaction parameters (k_{ij}) , while in the correlative mode, a binary interaction parameter was considered as a function of temperature.

One of the greatest challenges in using associating equations of state, and thus limiting their use by researchers, is the determination of the pure component parameters. This is a cause of regret, because DESs are truly associating compounds, and only models that do consider these associations are theoretically sound models for such complex systems. To assist in the more widespread use of the PC-SAFT by researchers, a simple generalized correlation is proposed in this study to estimate the PC-SAFT pure component parameters of DESs. This generalized correlation is only a function of molecular weight, and so, easily applicable to any DES. In this way, the challenging step of parameter optimization by users is eliminated. The PC-SAFT, in the predictive mode, showed total AARD% of 63.77 and 84.65% for the inert-2B and 2B-2B modes, respectively. But in the correlative calculations, the inert-2B and 2B-2B modes, led to total AARD% of 8.08% and 8.12%, respectively. The calculated solubilities by the predictive mode showed that the inert scheme for CO₂ leads to less errors than the scheme of 2B, however, both schemes are inaccurate. By considering adjusted binary interaction parameters, the results improve significantly, with both the inert-2B and 2B-2B calculations showing reliable results with respect to the experimental trends. In its current state, DESs can still be considered as novel solvents with much unknowns. These limits also have their impact on the thermodynamic modelling of systems involving DESs. For accurate modelling, the number and strength of association bonds between carbon dioxide and the HBA or HBD molecules must be known. For example, performing NMR tests on these systems can provide valuable information. This is because systems of carbon dioxide with DESs are very complex, and in order to succeed in very accurate modeling, all the established associations in the mixture should be involved in the thermodynamic model. However, in this way, the model will become more complicated and time-consuming, but this is the cost of greater accuracy.

Data availability statement

The original contributions presented in the study are included in the article/Supplementary Material, further inquiries can be directed to the corresponding author.

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Writing—original draft, conceptualization, formal analysis, data curation, software, KP; methodology, writing—review and editing, conceptualization, formal analysis, validation, RH; funding acquisition, supervision, writing—review and editing, AD; supervision, validation, writing - review and editing, SR.

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Conflict of interest

The authors declare that the research was conducted in the absence of any commercial or financial relationships that could be construed as a potential conflict of interest.

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Supplementary material

The Supplementary Material for this article can be found online at: https://www.frontiersin.org/articles/10.3389/fchem. 2022.909485/full#supplementary-material

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