### RESEARCH



**Open Access** 

# Effect of tumor shape, size, and tissue transport properties on drug delivery to solid tumors

Mostafa Sefidgar<sup>1</sup>, M Soltani<sup>1,2\*</sup>, Kaamran Raahemifar<sup>3</sup>, Hossein Bazmara<sup>1</sup>, Seyed Mojtaba Mousavi Nayinian<sup>1</sup> and Majid Bazargan<sup>1</sup>

#### Abstract

**Background:** The computational methods provide condition for investigation related to the process of drug delivery, such as convection and diffusion of drug in extracellular matrices, drug extravasation from microvessels or to lymphatic vessels. The information of this process clarifies the mechanisms of drug delivery from the injection site to absorption by a solid tumor. In this study, an advanced numerical method is used to solve fluid flow and solute transport equations simultaneously to investigate the effect of tumor shape and size on drug delivery to solid tumor.

**Methods:** The advanced mathematical model used in our previous work is further developed by adding solute transport equation to the governing equations. After applying appropriate boundary and initial conditions on tumor and surrounding tissue geometry, the element-based finite volume method is used for solving governing equations of drug delivery in solid tumor. Also, the effects of size and shape of tumor and some of tissue transport parameters such as effective pressure and hydraulic conductivity on interstitial fluid flow and drug delivery are investigated.

**Results:** Sensitivity analysis shows that drug delivery in prolate shape is significantly better than other tumor shapes. Considering size effect, increasing tumor size decreases drug concentration in interstitial fluid. This study shows that dependency of drug concentration in interstitial fluid to osmotic and intravascular pressure is negligible.

**Conclusions:** This study shows that among diffusion and convection mechanisms of drug transport, diffusion is dominant in most different tumor shapes and sizes. In tumors in which the convection has considerable effect, the drug concentration is larger than that of other tumors at the same time post injection.

Keywords: Drug concentration, Solid tumor, Tumor shape and size, Tissue transport properties

#### Background

Cancer, the main cause of death in developed countries, is the second leading cause of death in developing countries [1]. Solid tumors account for 85% of human cancers [2]. Chemotherapy is one of the ways widely used for cancer treatment. Based on the findings from clinical applications, most cancer treatments with drugs fail to eliminate solid tumors completely [3]. The computational method can investigate why systemic administration cannot distribute drug uniformly in tumors. The drug exchange between microvessels and extracellular matrices, drug removal by lymphatic system, drug diffusion and convective transport in extracellular matrices should be included by mathematical simulation. Computational fluid dynamics (CFD) can model the whole drug delivery process and clarify the mechanisms of drug delivery from the injection site to absorption by a solid tumor.

Baxter and Jain, based on the theoretical framework in their 1D mathematical method, found the effective factors on drug delivery such as microvessel permeability, interstitial fluid pressure (IFP), and interstitial fluid velocity (IFV) [4-7].

Improving the 1D model of Baxter et al. [5,6,8] and Saltzman et al. [9], Wang et al. [10-12] developed a simulation framework of drug delivery to tumors by



© 2014 Sefidgar et al.; licensee BioMed Central Ltd. This is an Open Access article distributed under the terms of the Creative Commons Attribution License (http://creativecommons.org/licenses/by/4.0), which permits unrestricted use, distribution, and reproduction in any medium, provided the original work is properly credited. The Creative Commons Public Domain Dedication waiver (http://creativecommons.org/publicdomain/zero/1.0/) applies to the data made available in this article, unless otherwise stated.

<sup>\*</sup> Correspondence: msoltani@jhu.edu

<sup>&</sup>lt;sup>1</sup>Department of Mechanical Engineering, K. N. T. University of Technology, Tehran, Iran

<sup>&</sup>lt;sup>2</sup>Division of Nuclear Medicine, Department of Radiology and Radiological Science, School of Medicine, Johns Hopkins University, Baltimore, MD, USA Full list of author information is available at the end of the article

considering the complex 3D geometry. Wang and Li [10] used modified MRI images for tumor geometry. They considered interstitial fluid flow with blood and lymphatic drainage in their model. Wang et al. [11] studied the effect of elevated interstitial pressure, convective flux, and blood drainage on the delivery of specified solute to brain tumors.

The study of tissue transport property effect on drug delivery is considered in recent studies. Zhao et al. [13] used a 3D computational model to predict the distribution of IFV, IFP, and solute transport through a tumor. Arifin et al. [14] studied the sensitivity of drug distribution to physiochemical properties in realistic models of brain tumors. A specific tumor captured by MRI is used by Pishko et al. [15] for modeling drug distribution in tissue with spatially-varying porosity and vascular permeability. The sensitivity of solute distribution to tumor shape and size is not considered in above mentioned works.

In our previous work [2], tumor shape and size effect on drug delivery is investigated by modeling interstitial fluid flow and assuming that drug particles flow with the interstitial fluid. In the present work, by adding the solute transport equation to the previous developed model in our group [16-20], new governing equations are investigated to find drug concentration in interstitial fluid (DCIF). Solving fluid flow and solute transport equations simultaneously, the effects of tumor shape, size, and tissue transport properties on drug delivery to solid tumor are also investigated.

Spherical and non-spherical tumors and their surrounding normal tissue are modeled with assumption of rigid porous media. The vasculature as a source term and lymphatic vessel as a sink term vary spatially. In the following parts of this paper, the sensitivity analysis provides a better understanding of the effects of tissue transport parameters on drug delivery.

#### Results

Simulation of interstitial fluid flow for baseline values (Table 1) predicts that IFP has its greatest value in the tumor center. IFP is non-dimensionalized by effective pressure. The effective pressure,  $P_{eff}$  is a parameter defined by intravascular pressure, plasma osmotic pressure, and interstitial osmotic pressure by Equation (1). The non-dimensionalized pressure is defined by Equation (2)

$$P_{eff} = P_B^t - \sigma_s^t \left( \pi_B^t - \pi_i^t \right) \tag{1}$$

$$P_n = \frac{P_i}{P_{eff}} = \frac{P_i}{P_b^t - \sigma_s^t \left(\pi_b^t - \pi_i^t\right)}$$
(2)

where t stands for tumor tissue. Parameters used in Equation (1) and (2) are introduced in the method section.

Page	2	of	13
------	---	----	----

Table	1 Interstitia	l transport	properties	used	in n	umerical
simula	ations					

Parameter	Baseline value	Reference
L <sub>P</sub> [cm/mmHg s]		
Normal	$0.36 \times 10^{-7}$	[16]
Tumor	$2.80 \times 10^{-7}$	
K[cm²/mmHg s]		
Normal	$8.53 \times 10^{-9}$	[16]
Tumor	$4.13 \times 10^{-8}$	
S/V[cm <sup>-1</sup> ]		
Normal	70	[16]
Tumor	200	
P <sub>B</sub> [mmHg]		
Normal	15.6	[16]
Tumor	15.6	
π <sub>B</sub> [mmHg]		
Normal	20	[16]
Tumor	20	
π <sub>i</sub> [mmHg]		
Normal	10	[16]
Tumor	15	
σ		
Normal	0.91	[16]
Tumor	0.82	
P <sub>L</sub>		
Normal	0	[15]
L <sub>PL</sub> S <sub>L</sub> /V [1/mmHg s]		
Normal	$1.33 \times 10^{-5}$	[15]

Non-dimensionalized IFP along transverse and vertical lines (shown in Figure 1), are illustrated in Figures 2 and 3. The maximum value of IFP occurs in the tumor center (Figure 2). This value is equal to  $P_{eff}$  1.53 kPa, except for the case of  $\lambda = 0.1$  (Prolate shape). IFP has uniform distribution at tumor region and in the inner boundary (for more detail see Figure 1 and boundary condition section) IFP falls down sharply to around 150 Pa as shown in Figure 2 for all shapes except for prolate one  $(\lambda = 0.1)$ . In normal tissue, pressure has uniform distribution close to outer boundary (for more detail, see Figure 1 and boundary condition section) then it decreases smoothly to peripheral pressure. For prolate shape as shown in Figure 2, IFP reduces smoothly from tumor center to the outer boundary, and IFP has a non-zero gradient in whole domain. Figure 2 shows the IFP along vertical line. Results are very similar to IFP results in Figure 2. Only for a prolate shape IFP has different pattern from what is observed in Figure 2. Maximum value of IFP in the prolate shape does not occur in the tumor



center and takes place somewhere between the tumor center and tumor periphery.

IFV distribution along the vertical and transverse lines is presented in Figures 4 and 5. Maximum value of IFV occurs close to the inner boundary. Also, in normal tissue, IFV reaches zero far from the inner boundary. However, for the prolate shape, velocity is not zero, especially along transvers line (Figure 4).

DCIF is simulated in two cases of injection. In the first case, the continuous injection which leads to constant plasma concentration ( $C_p$  = constant) is considered and in the second case, the bolus injection in which the plasma concentration decreases with time exponentially ( $C_p = C_p^0 e^{-\ln(0.5)t/\tau}$ ) is studied, in which  $\tau$  is the drug half-life in plasma (Table 2). DCIF are non-dimensionalized by  $C_p$  for continuous injection and  $C_p^0$  for bolus injection,





respectively. Average of non-dimensionalized DCIF for two injection cases in different times is shown in Figures 6 and 7. DCIF of prolate shape ( $\lambda = 0.1$ ) has the maximum value and DCIF of oblate shape ( $\lambda = 10$ ) has the minimum value. Other considered shapes show the similar transient behavior.

Non-dimensionalized DCIF along two lines (transverse and vertical) is illustrated in Figures 8 and 9. The bolus injection results are presented in 8 hr post injection in which the concentration is maximum based on Figure 7 and for continuous injection is presented at final time of simulation, in 72 hr post injection. The profiles of two types of injections are similar in spite of different values of DCIF. As observed in IFV and IFP profiles, the prolate



λ=0.1

λ=0.5 λ=1

2=2

 $\lambda = 10$ 

25

0.05

0.045

0.04

0.035

0.03

0.025

0.015

0.005

0.5

IFV(µm/s)

shape is different from the other shapes in DCIF distribution. A bump is observed in DCIF curves at the inner boundary of all tumor shapes. The normal tissue has uniform distribution of DCIF except near the boundaries (inner and outer). DCIF distribution in normal tissue is the same for all tumor shapes.

Figure 5 Interstitial fluid velocity profile along vertical line. The

1 in "x" axis shows the boundary of tumor (inner boundary).

15

Non-dimensionalized radius

2D contours of DCIF in tumor region for bolus injection in 8 hr post injection are shown in Figure 10 for all tumor shapes. Results show that DCIF for tumors with  $\lambda = 0.1$  and  $\lambda = 10$  has different distributions. Generally, in the inner boundary, DCIF has its maximum value. In Figures 11 and 12, Peclet number distribution along two lines for continuous injection is shown. Peclet number demonstrates the ratio of convection to diffusion across the microvessel

Table 2 Parameters of solute transport model used innumerical simulations

Parameter	Baseline value	Reference
Øf		
Normal	0.9	[8]
Tumor	0.9	
D <sub>eff</sub> [m²/s]		
Normal	0.16× 10 <sup>-12</sup>	[8]
Tumor	2.0× 10 <sup>-12</sup>	
P[m/s]		
Normal	2.2× 10 <sup>-10*</sup>	[8]
Tumor	17.3× 10 <sup>-10*</sup>	
τ [hr]**		
Plasma	6.1	[8]

\*- the microvessel permeability coefficient is 10% of effective permeability introduced in [8].

\*\*- the drug half-life in plasma introduced in results section.



wall. Results show that in the tumor region Peclet number is zero except for prolate shape. Peclet number for the prolate shape especially along short radius (transverse line) is greater than zero.

Some of tissue transport parameters mentioned (effective pressure, hydraulic conductivity, and tumor size) in Table 1 are investigated for sensitivity analysis. The values of these parameters are selected near the ranges reported in the literature [2,15,21].

Figure 13 shows the influence of changing effective pressure,  $P_{eff}$  on numerical results of tumor shapes with the same volume. Maximum value of IFP in tumor region (Figure 13a) linearly increases when  $P_{eff}$  increases. Only in





the prolate shape the pressure increases more than other tumor shapes. Average of IFV on inner boundary also has the same pattern and linearly changes with  $P_{eff}$  (Figure 13b). The changes in average of DCIF in tumor region for two cases of injection are shown in Figure 13c and d. For these two cases of injection, the prolate shape is more sensitive to  $P_{eff}$  changes than other tumor shapes and DCIF changes around 20% when the  $P_{eff}$  changes from 500 Pa to 2500 Pa. The other shapes do not show significant variations in DCIF for these ranges of  $P_{eff}$ .

Different tumor sizes are studied with changes in their volume. One of important metric of disease development and response to tumor therapy with drug is volume of tumors [22-25]. To quantify response to therapeutic regimens and also assess disease progression, tumor volume is used as a metric in many studies, such as Char et al. [26], Jensen et al. [27] and Gass et al. [28].

As shown in Figure 14a, IFP has less value than  $P_{eff}$  when the tumor volume is smaller than 1 cm<sup>3</sup>. When the tumor volume is in the order of 1 cm<sup>3</sup>, IFP reaches  $P_{eff}$ 

and by increasing the tumor radius, IFP remains constant. Average of IFV on the inner boundary generally decreases with increasing tumor size, Figure 14b. Only in prolate shape in small radii, IFV increases with the tumor size. As shown in Figure 14c and d, the mean values of DCIF have the greatest value in the smallest tumor. Also, the prolate shape has the highest value of DCIF in all studied tumors.

Figure 15 shows the sensitivity of IFF parameters and DCIF to hydraulic conductivity changes. Results show that in all tumor shapes, if hydraulic conductivity increases, the maximum value of IFP remains constant and then decreases sharply. Average of IFV increases by increasing hydraulic conductivity. DCIF increases by increasing hydraulic conductivity and then reaches a constant value in spite of increasing hydraulic conductivity.

#### Discussion

This study presents DCIF, IFP, and IFV in solid tumors surrounded by normal tissue in two types of injection; bolus and continuous one. The model used in this study





investigates the effect of two characteristics of tumors on concentration distribution; tumor shape and size.

Results of high IFP in tumors are discussed in our previous studies [2,16,17] and in the experimental results of Arifin et al. [29] and Huber et al. [30]. Maximum value of IFP in spherical tumors (1 cm radius) for baseline values in Table 1 is 1529.5 Pa which is close to the studies of Jain et al. [31], Chauhan et al. [32], and Arfin et al. [33]. The current results are verified by experimental data of IFP measured by Nielsen et al. [34]. In their work, the wick-in-needle technique is used to measure IFP in two types of tumors with the same volume as tumors in the current study. They found IFP in the range of 1400 Pa to 1600 Pa.

IFV on tumor boundary in spherical tumors with baseline values is around 0.05  $\mu$ m/s which is at the same order of the prediction of Jain et al. [31] and experimental observation of Hompland et al. [35]. Also, the profile of drug concentration for simulation with baseline values for spherical tumor in different times (Figures 6 and 7) agrees well with Baxter and Jain's predictions [8]. Results show that DCIF for prolate shape ( $\lambda = 0.1$ ) always has the greatest value. Results of transient DCIF (Figures 6 and 7) show that drug delivery is much easier in the prolate tumors. Also, the oblate shape ( $\lambda = 10$ ) has the most resistance to drug delivery. Following of this section, the reason of these phenomena is investigated.

The uniform values of IFP for all tumor shapes except prolate one (Figures 2 and 3) is equal to  $P_{eff}$  Non-uniform IFP in prolate shape results in the maximum value of







DCIF among other tumor shapes with the same volume. Equation (17) is able to legitimize this behavior of tumor shapes. The source term (the last term in the right hand side of Equation (17)) includes diffusion and convection terms. The convection term depends on the differences between IFP and  $P_{eff}$  based on starling's law. This pressure difference is close to zero (Figures 2 and 3) for all tumor shapes except for the prolate one and therefore the convection term only for prolate shape has non-zero value. Because of the non-zero values of Peclet number for prolate shape in tumor region (Figures 11 and 12), the concentration for this shape is affected not only by diffusion rate from vessels but also by convection rate from vessels. The convection rate leads to higher level of DCIF in prolate shape than that of other tumor shapes (Figures 6, 7, 8, 9 and 10). The non-zero values of Peclet number for prolate shape are seen in an image based work of Zhao et al. as well [13]. In normal tissue, Peclet number shows that drug delivery from microvessel to tissue is done by both mechanisms of transfer, convection and diffusion.

The other effect of uniform pressure is zero pressure gradients in all tumor shapes except for prolate one. Because of zero IFP gradient and based on Darcy's equation, IFV is close to zero in tumor tissue except for prolate shape. The close to zero value of IFV is predicted in a few numerical studies such as Welter and Rieger [36]; Roy and Riahi [37]; and experimental results of Hompland et al. [35]. Zero IFV results in a negligible convection transport (the second term of the right hand side of Equation (17)) and consequently the convection transport does not affect drug distribution; and the diffusion transport (the first term of the right hand side of Equation (17)) is the only reason of drug transport in all tumor shapes except for prolate one. Therefore, non-zero IFV in prolate shape, also seen in Zhao et al. [13], is another reason of higher DCIF values in this tumor shape with respect to other shapes.

The sharp pressure gradient (Figures 2 and 3) and highest value of IFV (Figures 4 and 5) in the inner boundary for all tumor shapes increases drug transport and make a bump at this boundary for DCIF.

The sensitivity analysis of effective pressure shows that the effective pressure does not have too much effect on DCIF. In all tumor shapes, DCIF for a wide range of effective pressure changes smoothly; however, in prolate shape, this change is sharper and increases by effective pressure (Figure 13c and d). As mentioned, in the tumor region for all tumor shapes except for prolate one the convection rate, which depends on  $P_{eff}$  has a negligible role



on drug distribution; therefore,  $P_{eff}$  cannot have significant effect on drug concentration. However, in prolate shape, increasing  $P_{eff}$  increases pressure difference between IFP and  $P_{eff}$  and consequently the convection rate from vessels in the tumor region; therefore, DCIF in prolate shape is sensitive to  $P_{eff}$  changes.

The tumor volume shows more effects on IFP, IFV, and DCIF than other investigated parameters such as effective pressure and hydraulic conductivity. The increasing tumor volume increases significantly IFP (Figure 14a). The dependency of IFP to tumor volume is observed in experimental study of Gutmann et al. [38], Hompland et al. [39], and Leguerney et al. [40], as well. When the tumor volume is in the order of 1 cm<sup>3</sup>, the sensitivity of IFP to tumor size decreases. The independency of IFP to tumor volume in in large tumors is observed in the study of Leguerney et al. [40], as well. In their work, IFP changes very slowly with tumor volume. Since the high IFP is introduced as the main barrier of drug delivery to tumors, IFP increasing with tumor volume leads to DCIF decrease in these tumors. This reduction of DCIF with tumor size is observed in Au et al. [41], as well. Since IFP reaches around the effective pressure with increasing tumor volume, the convection rate is vanished and the diffusion rate reaches a constant value, and consequently the sensitivity of DCIF to tumor size reduces. Lower IFP in the small tumor sizes leads to increase the convection rate of source term in Equation (17). Therefore, it is expected to have a better drug distribution in small tumors.

Results show that IFV, IFP, and DCIF are sensitive to tissue hydraulic conductivity changes. The hydraulic conductivity is appeared only in Darcy's law. This parameter has a direct effect on IFF and indirect effect on DCIF. Theoretical analysis shows that the  $\frac{P_i}{P_{eff}}$  in tumor region is proportional to  $1 - \frac{1}{\sqrt{\kappa}} / \sinh\left(\frac{1}{\sqrt{\kappa}}\right)$  [8] ( $\kappa$  is hydraulic conductivity, see material section). In low values of  $\kappa$ , the  $\frac{1}{\sqrt{\kappa}}/\sinh\left(\frac{1}{\sqrt{\kappa}}\right)$  is negligible and  $P_i$  is close to  $P_{eff}$ (Figure 15a). Increasing  $\kappa$ , increases the  $\frac{1}{\sqrt{\kappa}}/\sinh\left(\frac{1}{\sqrt{\kappa}}\right)$ and leads to sharp decrease in IFP. This dependency is also observed by McCarty and Johnson [42]. For high values of  $\kappa$ , IFP is very low and negligible in comparison to  $P_{eff}$ . IFP reduction from effective pressure increases IFV around 5 times (Figure 15b). The hydraulic conductivity affects DCIF by convection rate from vessels (as mentioned this value depends on difference between IFP and  $P_{eff}$ ). In low values of  $\kappa$ , since IFP is equal to  $P_{eff}$ , the

effect of convection rate is not significant and DCIF remains constant. Increasing  $\kappa$  increases the convention rate and consequently DCIF.

When hydraulic conductivity increases two to three orders of magnitude, the mean values of DCIF are two times greater than the average of DCIF for baseline values in Table 1. However, after a specific value of hydraulic conductivity, DCIF changes smoothly and reaches a constant value because IFP is very low and convection rate only depends on  $P_{eff}$ .

#### Conclusions

A numerical approach which couples the mathematical model of the lymphatic system and the interstitial flow with the mathematical model of solute transport demonstrates that DCIF is affected by two transport mechanisms, convection and diffusion.

Drug convection and drug transport from microvessel to tumor are blocked by high interstitial pressure (IFP) which is uniformly distributed in most part of the tumor. The large pressure gradient results in an outward convective flow that washes out the drug extravasated from microvessels at the tumor periphery. This study shows that when there is IFP gradient in the tumor region instead of uniform IFP distribution which occurs in some tumor shapes, DCIF is greater than that of the uniform one.

As the effects of osmotic and intravascular pressure on convection rate are negligible in most of tumor shapes, the dependency of DCIF to these parameters is very low.

The hydraulic conductivity which is another considered parameter in sensitivity analysis has significant effect on drug distribution since it increases the convection rate from vessels.

#### Method

#### Mathematical model of interstitial fluid transport

This section introduces the mathematical model of interstitial fluid transport in macroscopic scale [2,16]. Since normal and tumor tissue have characteristics the same as porous media, fluid flow behavior is defined by coupling the fluid flow governing equations. The mass balance or continuity equation for steady state incompressible fluid in the porous media with source and sink of mass is [16]:



$$\nabla . \nu_i = \phi_B - \phi_L \tag{3}$$

where

 $v_i$ : The interstitial fluid velocity,

 $\phi_{\!B\!}$  : The source term, extravasation from microvessels, and

 $\phi_L$ : The drainage term, elimination by lymphatic system. In biological tissues, the fluid source is evaluated through Starling's law as follows [16]:

$$\phi_B = \frac{L_P S}{V} \left( P_B - P_i - \sigma_s (\pi_b - \pi_i) \right) \tag{4}$$

where

 $P_i$ : Interstitial fluid pressure,

 $P_B$ : Blood pressure in microvessel,

 $\frac{S}{V}$ : The surface area per unit volume of tissue for transport in the interstitium,

 $\pi_{B}$ : Microvessel oncotic pressure,

 $\pi_i$ : Interstitial oncotic pressure,

 $L_p$  : The hydraulic conductivity of the microvessel wall, and

 $\sigma_s$ : Osmotic reflection coefficient.

and the lymphatic system is related to the pressure difference between the interstitium and the lymphatic vessels and is considered only for normal tissues [43]:

$$\phi_{L}(r) = \begin{cases} \frac{L_{PL}S_{L}}{V}(P_{i}-P_{L}) & Normal tissue\\ 0 & Tumor tissue \end{cases}$$
(5)

where

 $\phi_L$ : The volumetric flow rate into the lymphatic,

 $\frac{L_{PL}S_L}{V}$ : The lymphatic filtration coefficient, and

 $P_L$ : The hydrostatic pressure of the lymphatic.

The momentum balance equation in its general form can be written as Equation (6) [44]:

$$\rho\left(\frac{\partial \mathbf{v}_{i}}{\partial t} + (\mathbf{v}_{i}.\nabla)\mathbf{v}_{i}\right) = \nabla \cdot \left[-P_{i} + \mu\left(\nabla \mathbf{v}_{i} + (\nabla \mathbf{v}_{i})^{T}\right) - \frac{2\mu}{3}(\nabla \cdot \mathbf{v}_{i})\right] - \left(\frac{\mu}{K}\right)\mathbf{v}_{i} + F$$
(6)

where

K: The permeability of the porous medium,

 $\rho$  : The density,

μ: The viscosity, and

F: The volume forces.

Since interstitial fluid is a Newtonian fluid and has low velocity through the tissues, Equation (6) in the steady state condition is simplified to Darcy's law [16]:

$$\nabla P_i = -\left(\frac{\mu}{K}\right) \mathbf{v}_i \tag{7}$$

The K/ $\mu$  is defined as hydraulic conductivity of the interstitium,  $\kappa$ :

$$\mathbf{v}_i = -\kappa \nabla P_i \tag{8}$$

Combination of momentum equation (Equation (8)) and the continuity equation (Equation (3)) results in

$$-\nabla \cdot (\kappa \nabla P_i) = \phi_B - \phi_L \tag{9}$$

When  $\kappa$  is constant, the interstitial pressure can be expressed by

$$-\kappa \nabla^2 P_i = \phi_B - \phi_L \tag{10}$$

By substituting Equations (4) and (5) into Equation (10):

$$-\kappa \nabla^2 p = \begin{cases} \frac{L_P S}{V} (P_B - P_i - \sigma_s(\pi_b - \pi_i)) - \frac{L_{PL} S_L}{V} (P_i - P_L) & \text{Normal tissue} \\ \frac{L_P S}{V} (P_B - P_i - \sigma_s(\pi_b - \pi_i)) & \text{Tumor tissue} \end{cases}$$
(11)

#### Macroscopic solute transport

Molecular transport in tumors is based on the conservation laws for mass and momentum. The interstitial transport of drug is governed by the convection diffusion equation; therefore, the general equation for the mass balance of solutes can be written as:

$$\frac{\partial C}{\partial t} = \nabla \cdot \left( D_{eff} \cdot \nabla C \right) - \nabla \cdot \left( \nu_i C \right) + \left( \Phi_B - \Phi_L \right)$$
(12)

where

*C* : The solute concentration based on tissue volume,

 $\Phi_B$ : The rate of solute transport per unit volume from microvessel into the interstitial space,

 $\Phi_L$ : The rate of solute transport per unit volume from the interstitial space into lymphatic vessels, and

 $D_{eff}$ : The effective diffusion tensor.

For an isotropic and uniform diffusion in tissues, equation (12) can be written as:

$$\frac{\partial C}{\partial t} = D_{eff} \nabla^2 C - \nabla \cdot \left( \nu_f C \right) + \left( \Phi_B - \Phi_L \right)$$
(13)

The solute transport rate across the lymphatic vessels can be considered as [15]

$$\Phi_L = \begin{cases} \phi_L C & Normal \ Tissue \\ 0 & Tumor \ Tissue \end{cases}$$
(14)

The solute transport rate across the microvessel can be represented by Patlak equation [45]:

$$\Phi_B = \phi_B (1 - \sigma_f) C_P + \frac{PS}{V} (C_P - C) \frac{Pe}{e^{Pe} - 1}$$
(15)

where



$$Pe = \frac{\phi_B (1 - \sigma_f) V}{PS} \tag{16}$$

 $\phi_B$ : The fluid flow rate per unit volume of tissue across the microvessel wall,

 $\sigma_f$ : The filtration reflection coefficient,

*P* : The microvessel permeability coefficient,

S/V: The microvessel surface area per unit volume of tissue,

 $C_p$ : Solute concentration in the plasma.

By substituting Equations (15) and (14) in to Equation (13):



$$\begin{cases} \frac{\partial C}{\partial t} = D_{eff} \nabla^2 C - \nabla \cdot (v_i fC) \\ + \left( \phi_B (1 - \sigma_f) C_P + \frac{PS}{V} \left( C_P - \frac{C}{K_{AV}} \right) \frac{Pe}{e^{Pe} - 1} - \phi_L C \right) \text{ Normal region} \\ \frac{\partial C}{\partial t} = D_{eff} \nabla^2 C - \nabla \cdot (v_i fC) \\ + \left( \phi_B (1 - \sigma_f) C_P + \frac{PS}{V} \left( C_P - \frac{C}{K_{AV}} \right) \frac{Pe}{e^{Pe} - 1} \right) \text{ Tumor region} \end{cases}$$

$$(17)$$

#### **Boundary conditions**

A tumor surrounded by normal tissue is considered in this study. The tumor shape is considered ellipsoid. A 2D section of the geometry and boundaries are shown in Figure 1. The three boundaries are indicated for geometry: a) the center of tumor, b) the boundary between tumor and normal tissue, named inner boundary, c) the boundary at the outer edge of geometry, named outer boundary. The appropriate boundary conditions are implemented for Equations (11) and (17). The no flux boundary condition is applied at the center of the tumor; i.e. [16],

$$\nabla P_i = 0 \text{ for } r = 0 \tag{18}$$

$$D_{eff}\nabla C + v_i C = 0 \text{ for } r = 0 \tag{19}$$

The continuity of pressure and velocity for Equation (11) and concentration and its flux for Equation (17) are considered as appropriate boundary conditions for inner boundary:

$$\begin{aligned} -\kappa_t \nabla P_i|_{\Omega^-} &= -\kappa_n \nabla P_i|_{\Omega^+} \\ P_i|_{\Omega^-} &= P_i|_{\Omega^+} \end{aligned}$$
 (20)

$$\begin{pmatrix} D_{eff}^t \nabla C + \nu_i C \end{pmatrix} |_{\Omega^-} = \begin{pmatrix} D_{eff}^n \nabla C + \nu_i C \end{pmatrix} |_{\Omega^-}$$

$$C |_{\Omega^-} = C |_{\Omega^+}$$

$$(21)$$

where  $\Omega^-$  and  $\Omega^+$  indicate the tumor and normal tissue at the inner boundary.

For outer boundary, that the interstitial pressure is constant; the Dirichlet type of boundary condition must be applied [16]:

$$P_i = for outer region \tag{22}$$

And for concentration, the open boundary condition is used in the outer region [46]. The Open Boundary is used to set up mass transport across boundaries where both convective inflow and outflow can occur and defined by Equation (23):

$$-\mathbf{n} \cdot \nabla \mathbf{C} = 0 \tag{23}$$

where **n** is the normal vector.

#### Geometry

To investigate the effect of tumor shape on drug delivery, 5 different shapes are considered. The 3D fundamental shape of tumors is assumed to be an ellipsoid in different studies. The assumption of considering ellipsoid tumor shape is investigated in many research such as breast cancer [47], prostate cancer [48,49] cervical cancer [50], glioma cancer [51], and others [52]. Based on this mentioned reason, ellipsoidal shapes of tumors are considered in this study. Different shapes are produced by changing ratio of two radii of ellipsoid shown in Figure 1. This ratio  $(\lambda = b/a)$  is changed from 0.1 (prolate) to 10 (oblate). In all shapes shown in Figure 16 the volume of the tumor is remained constant and equal to the volume of spherical tumor with radius R. The baseline value of R is 1 cm. The values of R used in sensitivity analysis are changed from 0.1 cm to 2.5 cm. This range is obtained from the literature and is close to the experimental observations [40].

#### Model parameterization

The interstitial transport properties for normal and tumor tissue are listed in Table 1. These values are used as baseline and some of them are investigated and changed in specified ranges for sensitivity analysis.

The parameters of solute transport model taken from Baxter and Jain [8] are listed in Table 2. Although, the numerical model is applicable for any type of solute, in present study the properties of Fragment antigen-binding  $(F(ab')_2)$  as a sample is used.

#### Numerical solution

A systematic flow chart is illustrated in Figure 17 to clarify the computational techniques involved in this paper. The criterion for the convergence of iterative solution based on element–based finite volume (EB-FV) method is to reduce the residual by 6 orders of magnitudes. The details of numerical method is mentioned in our previous works [2,16,53].

#### Abbreviations

CFD: Computational fluid dynamics; IFP: Interstitial fluid pressure; IFV: Interstitial fluid velocity; DCIF: Drug concentration in interstitial fluid; EB-FV: Element based- finite volume.

#### **Competing interests**

The authors declare that they have no competing interests.

#### Authors' contributions

MS and MS carried out the numerical simulations and drafted the manuscript. HB participated in the numerical simulations. MM and MB and KR helped to draft the manuscript and discussed the results. MS and MS conducted the numerical simulation, discussed the results and reviewed the manuscript. All authors read and approved the final manuscript.

#### Author details

<sup>1</sup>Department of Mechanical Engineering, K. N. T. University of Technology, Tehran, Iran. <sup>2</sup>Division of Nuclear Medicine, Department of Radiology and Radiological Science, School of Medicine, Johns Hopkins University, Baltimore, MD, USA. <sup>3</sup>Electrical & Computer Department of Ryerson University, Toronto, Ontario.

#### Received: 24 February 2014 Accepted: 30 May 2014 Published: 12 June 2014

#### References

- Siegel R, Naishadham D, Jemal A: Cancer statistics. A Cancer J Clin 2013, 63:11–30.
- 2. Soltani M, Chen P: Effect of tumor shape and size on drug delivery to solid tumors. J Biol Eng 2012, 6:4.
- Blakeslee S: Impenetrable tumors found to block even the newest cancer agents. In [http://www.nytimes.com/1989/06/27/science/impenetrabletumors-found-to-block-even-the-newest-cancer-agents.html]
- Baxter LT, Jain RK: Transport of fluid and macromolecules in tumors IV: A microscopic model of the perivascular distribution. *Microvasc Res* 1991, 41:252–272.
- Baxter LT, Jain RK: Transport of fluid and macromolecules in tumors (II): role of heterogeneous perfusion and lymphatics. *Microvasc Res* 1990, 40:246–263.
- 6. Baxter LT, Jain RK: Transport of fluid and macromolecules in tumors (iii): role of binding and metabolism. *Microvasc Res* 1991, **41**:5–23.
- Jain RK, Baxter LT: Mechanisms of heterogeneous distribution of monoclonal antibodies and other macromolecules in tumors: significance of elevated interstitial pressure. *Cancer Res* 1988, 48:7022–7032.
- Baxter LT, Jain RK: Transport of fluid and macromolecules in tumors (I): role of interstitial pressure and convection. *Microvasc Res* 1989, 37:77–104.
- 9. Saltzman WM, Radomsky ML: Drugs released from polymers: diffusion and elimination in brain tissue. *Chem Engng Sci* 1991, **46**:2429–2444.
- 10. Wang CH, Li J: Three-dimensional simulation of IgG delivery to tumors. Chem Eng Sci 1998, 53:3579–3600.
- Wang CC, Li J, Teo CS, Lee T: The delivery of BCNU to brain tumors. J Control Release 1999, 61:21–41.
- 12. Tan WHK, Wang F, Lee T, Wang C-H: Computer simulation of the delivery of etanidazole to brain tumor from PLGA wafers: comparison between linear and double burst release systems. *Biotechnol Bioeng* 2003, **82**:278–288.
- Zhao J, Salmon H, Sarntinoranont M: Effect of heterogeneous vasculature on interstitial transport within a solid tumor. *Microvasc Res* 2007, 73:224–236.
- 14. Arifin DY, Lee KYT, Wang C-H: Chemotherapeutic drug transport to brain tumor. J Control Release 2009, 137:203–210.
- Pishko GL, Astary GW, Mareci TH, Sarntinoranont M: Sensitivity analysis of an image-based solid tumor computational model with heterogeneous vasculature and porosity. Ann Biomed Eng 2011, 39:2360–2373.
- Soltani M, Chen P: Numerical modeling of fluid flow in solid tumors. PLoS One 2011, 6:1–15.

- Soltani M, Chen P: Numerical modeling of interstitial fluid flow coupled with blood flow through a remodeled solid tumor microvascular network. *PLoS One* 2013, 8:e67025.
- Soltani M: Numerical modeling of drug delivery to solid tumor microvasculature. Waterloo, Ontario, Canada: PhD thesis, Chem. Eng. (Nanotechnology); 2012.
- Sefidgar M, Soltani M, Bazmara H, Mousavi M, Bazargan M, Elkamel A: Interstitial flow in cancerous tissue: effect of considering remodeled capillary network. J Tissue Sci Eng 2014, 4:1–8.
- Sefidgar M, Raahemifar K, Bazmara H, Bazargan M, Mousavi SM, Soltani M: Effect of remodeled tumor-induced capillary network on interstitial flow in cancerous tissue. In 2nd Middle East Conf:17-20 February 201;Doha, Qatar. Biomed. Eng. IEEE; 2014:212–215.
- Netti PA, Berk DA, Swartz MA, Grodzinsky AJ, Jain RK: Role of extracellular matrix assembly in interstitial transport in solid tumors. *Cancer Res* 2000, 60:2497–2503.
- Mayr NA, Yuh WTC, Zheng J, Ehrhardt JC, Sorosky JI, Magnotta VA, Pelsang RE, Hussey DH: Tumor size evaluated by pelvic examination compared with 3-D MR quantitative analysis in the prediction of outcome for cervical cancer. *Int J Radiat Oncol Biol Phys* 1997, 39:395–404.
- Kim HJ, Kim W: Method of tumor volume evaluation using magnetic resonance imaging for outcome prediction in cervical cancer treated with concurrent chemotherapy and radiotherapy. *Radiat Oncol J* 2012, 30:70–77.
- Ayers GD, Mckinley ET, Zhao P, Fritz JM, Metry RE, Deal BC, Adlerz KM, Coffey RJ, Manning HC: Volume of preclinical xenograft tumors is more accurately assessed by ultrasound imaging than manual caliper measurements. J Ultrasound Med 2010, 29:891–901.
- 25. Narayan K, Fisher R, Bernshaw D: Significance of tumor volume and corpus uteri invasion in cervical cancer patients treated by radiotherapy. Int J Gynecol Cancer 2006, **16**:623–630.
- 26. Char D, Kroll S, Phillips T: Uveal melanoma: growth rate and prognosis. Arch Ophthalmol 1997, 115:1014–1018.
- Jensen PK, Hansen MK: Ultrasonographic, three-dimensional scanning for determination of intraocular tumor volume. *Acta Ophthalmol* 1991, 69:178–186.
- 28. Gass J, Donald M: Comparison of uveal melanoma growth rates with mitotic index and mortality. *Arch Ophthalmol* 1985, **103**:924–931.
- Arifin DY, Lee LY, Wang C-H: Mathematical modeling and simulation of drug release from microspheres: implications to drug delivery systems. *Adv Drug Deliv Rev* 2006, 58:1274–1325.
- Huber PE, Bischof M, Heiland S, Peschke P, Saffrich R, Gro H, Lipson KE, Abdollahi A: Trimodal cancer treatment: beneficial effects of combined antiangiogenesis, radiation, and chemotherapy. *Cancer Res* 2005, 65:3643–3655.
- Jain RK, Tong RT, Munn LL: Effect of vascular normalization by antiangiogenic therapy on interstitial hypertension, peritumor edema, and lymphatic metastasis: insights from a mathematical model. *Cancer Res* 2007, 67:2729–2735.
- Chauhan VP, Stylianopoulos T, Martin JD, Chen O, Kamoun WS, Bawendi MG, Fukumura D, Jain RK: Normalization of tumour blood vessels improves the delivery of nanomedicines in a size-dependent manner. *Nat Nanotechnol* 2012, 7:383–388.
- Arifin DY, Wang C, Smith KA: Patient-specific chemotherapeutic drug delivery to brain tumors. *Mimics Innov Award* 2007, 1:1–9.
- Nielsen T, Murata R, Maxwell RJ, Stødkilde-Jørgensen H, Ostergaard L, Ley CD, Kristjansen PEG, Horsman MR: Non-invasive imaging of combretastatin activity in two tumor models: association with invasive estimates. *Acta Oncol* 2010, 49:906–913.
- Hompland T, Ellingsen C, Øvrebø KM, Rofstad EK: Interstitial fluid pressure and associated lymph node metastasis revealed in tumors by dynamic contrast-enhanced MRI interstitial fluid pressure and associated lymph node. *Cancer Res* 2012, **72**:4899–4908.
- 36. Welter M, Rieger H: Interstitial fluid flow and drug delivery in vascularized tumors: a computational model. *PLoS One* 2013, 8:e70395.
- Roy R, Riahi DN: Modeling blood flow in a brain tumor treated concurrently with radiotherapy and chemotherapy. *Appl Math Phys* 2013, 1:67–77.
- Gutmann R, Leunig M, Feyh J, Goetz AE, Messmer K, Kastenbauer E, Jain RK: Advances in brief interstitial hypertension in head and neck tumors in patients: correlation with tumor size. *Cancer Res* 1992, 52:1993–1995.

- Hompland T, Ellingsen C, Rofstad EK: Preclinical evaluation of Gd-DTPA and gadomelitol as contrast agents in DCE-MRI of cervical carcinoma interstitial fluid pressure. *BMC Cancer* 2012, 12:2–10.
- Leguerney I, Lassau N, Koscielny S, Rodrigues M, Massard C, Rouffiac V, Benatsou B, Thalmensi J, Bawa O, Opolon P, Peronneau P, Roche A: Combining functional imaging and interstitial pressure measurements to evaluate two anti-angiogenic treatments. *Invest New Drugs* 2012, 30:144–156.
- Au JL, Jang SH, Zheng J, Chen CT, Song S, Hu L, Wientjes MG: Determinants of drug delivery and transport to solid tumors. J Control Release 2001, 74:31–46.
- 42. Mccarty WJ, Johnson M: The hydraulic conductivity of Matrigel. *Biorheology* 2007, 44:303–317.
- Wu M, Frieboes HB, McDougall SR, Chaplain MAJ, Cristini V, Lowengrub J: The effect of interstitial pressure on tumor growth: coupling with the blood and lymphatic vascular systems. J Theor Biol 2013, 320:131–151.
- 44. Vafai K: Porous Media, Application in Biological systems and biotechnology. Boca Raton: CRC Press; 2011.
- Curry F: Mechanics and thermodynamics of transcapillary exchange, Handbook of Physiology, Section 2: The Cardiovascular System. Bethesda: Amer Physiol Soc; 1984.
- 46. Orlanski I: A simple boundary condition for unbounded hyperbolic flows. *J Comput Phys* 1976, **21:**251–269.
- Wapnir IL, Barnard N, Wartenberg D, Greco RS: The inverse relationship between microvessel counts and tumor volume in breast cancer. Breast J 2001, 7:184–188.
- Sosna J, Rofsky NM, Gaston SM, DeWolf WC, Lenkinski RE: Determinations of prostate volume at 3-Tesla using an external phased array coil: comparison to pathologic specimens. Acad Radio 2003, 10:846–853.
- Egorov V, Ayrapetyan S, Sarvazyan AP: Prostate mechanical imaging: 3-D image composition and feature calculations. *IEEE Trans Med Imaging* 2008, 25:1329–1340.
- Mayr NA, Taoka T, Yuh WTC, Denning LM, Zhen WK, Paulino AC, Gaston RC, Sorosky JI, Meeks SL, Walker JL, Mannel RS, Buatti JM: Method and timing of tumor volume measurement for outcome prediction in cervical cancer using magnetic resonance imaging. *Int J Radiat Oncol Biol Phys* 2002, 52:14–22.
- Schmidt K, Ziu M, Ole Schmidt N, Vaghasia P, Cargioli T, Doshi S, Albert M, Black P, Carroll R, Sun Y: Volume reconstruction techniques improve the correlation between histological and in vivo tumor volume measurements in mouse models of human gliomas. J Neurooncol 2004, 68:207–215.
- James K, Eisenhauer E, Christian M, Terenziani M, Vena D, Muldal A, Therasse P: Measuring response in solid tumors: unidimensional versus bidimensional measurement. J Natl Cancer Inst 1999, 91:523–528.
- 53. Soltani M, Chen P: Shape design of internal flow with minimum pressure loss. *Adv Sci Lett* 2009, **2**:347–355.

#### doi:10.1186/1754-1611-8-12

**Cite this article as:** Sefidgar *et al.*: **Effect of tumor shape**, **size**, **and tissue transport properties on drug delivery to solid tumors**. *Journal of Biological Engineering* 2014 **8**:12.

## Submit your next manuscript to BioMed Central and take full advantage of:

- Convenient online submission
- Thorough peer review
- No space constraints or color figure charges
- Immediate publication on acceptance
- Inclusion in PubMed, CAS, Scopus and Google Scholar
- Research which is freely available for redistribution

) BioMed Central

Submit your manuscript at www.biomedcentral.com/submit