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1. Introduction

The physical properties of materials, such as structural, electronic, optical and mechanical are studied in depth to gain deep knowledge of their uses. The analysis of a material's physical properties can be done by both experimental¹⁻⁵ and theoretical investigations.6-10 Theoretical studies aid experimental work in gaining a better understanding of physical properties.^{1,6} The physical properties of materials are associated with crystal structure.11-15 Perovskite compounds comprise conductors, insulators, semiconductors, and superconductors;¹⁶⁻²⁰ therefore, they are considered the most important materials among various types of crystal structures in terms of uses.²¹⁻²³ Because of their immense physical properties, such as photocatalytic, dielectric, ferroelectric, pyroelectric, piezoelectric, magnetic, superconductivity, and ionic conductivity.²⁴⁻³¹ perovskites are often referred to as "the department store of physical properties".32 The simple cubic perovskite with space group $Pm\bar{3}m$ (#221) could be oxide based (general formula ABO₃)³³ or halide based (general formula ABX₃),³⁴ where A and B are cations, while X is a monovalent halogen anion.35 The first-principle calculations were successfully implemented to cubic perovskite compounds to analyze different physical properties.35-54 The substitution of element,^{35,36} doping,^{10,37,38} or applying hydrostatic pressure³⁹⁻⁵³ can change the physical properties of cubic perovskites.

Ultra-violet to visible band gap engineering of cubic halide KCaCl₃ perovskite under pressure for optoelectronic applications: insights from DFT

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Density functional theory is utilized to explore the effects of hydrostatic pressure on the structural, electrical, optical, and mechanical properties of cubic halide perovskite KCaCl₃ throughout this study. The interatomic distance is decreased due to the pressure effect, which dramatically lowers the lattice constant and unit cell volume of this perovskite. Under pressure, the electronic band gap shrinks from the ultra-violet to visible region, making it easier to move electrons from the valence band to the conduction band, which improves optoelectronic device efficiency. Furthermore, the band gap nature is switched from indirect to direct around 40 GPa pressure, which is more suitable for a material to be exploited in optoelectronic applications. The use of KCaCl₃ in microelectronics, integrated circuits, QLED, OLED, solar cells, waveguides, solar heat reduction materials, and surgical instruments has been suggested through deep optical analysis. The use of external hydrostatic pressure has a considerable impact on the mechanical properties of this material, making it more ductile and anisotropic.

Linh et al.³⁵ found that substituting of bigger ionic radius alkali metals (M = Li, Na, and K) to $(Bi_{0.5}M_{0.5})TiO_3$ increased its direct band gap. The substitution of K to Cs site in $MCaF_3$ (M = K, Cs) improved the optical characteristics by altering the band gap from indirect to direct.36 Gillani et al. also reported that the doping of alkaline earth metals (Mg, Ca, Ba) into SrZrO₃ shifted the band gap from indirect to direct.37,38 Furthermore, using hydrostatic pressure to alter the band gap from indirect to direct proved beneficial, as seen in a number of cubic perovskites.39-44 The band gap of halide cubic perovskites $CsBX_3$ (B = Sn, Ge; X= Cl, Br) was decreased to zero by applying external pressure, resulting in a semiconductor to metallic transition.45-49 The first-principle investigations under hydrostatic pressure have also been done for Ca based cubic alkali halide perovskites $KCaX_3$ (X = F, Cl)^{50,51} and $ACaF_3$ (A = Rb, Cs).^{52,53} The band gap of KCaF₃ and RbCaF₃ were shifted from indirect to direct by applying hydrostatic pressure of 13.5 and \geq 14 GPa, respectively.^{51,53} Furthermore, $ACaF_3$ (A = K, Rb, Cs) exhibited improved mechanical properties under increased hydrostatic pressure.51,53 The photoluminescence of another halide perovskite RbCaCl₃ phosphor activated with 3d elements Cu⁺ and Mn²⁺ was discussed in the reported literature.54 The investigations of physical properties and structural stability have been done at ambient pressure50,55,56 for experimentally synthesized Ca based alkali halide perovskite KCaCl₃,⁵⁷ but the attempt of applying pressure on this perovskite has yet to be done. As a result, the goal of this research is to use the first-principles calculations to examine the geometric structure, electronic, optical, and mechanical properties of non-toxic cubic halide perovskite KCaCl₃ under hydrostatic pressure and assess the results to explore the effects of pressure.

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Fig. 1 Crystal structure of cubic perovskite KCaCl_3 with crystallographic sites.

2. Computational method

The first-principle calculations are carried out with the Cambridge Serial Total Energy Package (CASTEP) code,⁵⁸ which is an implementation of the plane-wave pseudo-potential total energy approach based on density functional theory (DFT). The Vanderbilt-type ultrasoft-pseudopotential is used to model the interaction of valence electrons with ion cores.59 The generalized gradient approximation (GGA) suggested by Perdew-Burke-Ernzerhof (PBE) is used to treat the exchange-correlation effect.⁶⁰ The plane-wave basis set cut-off is fixed to 900 eV to distinguish core states from valence ones. The Monkhorst-Pack method61 with 12 \times 12 \times 12 k-point mesh is used to integrate special points sampling over the Brillouin zone. In geometry optimization, the Broyden-Fletcher-Goldfarb-Shanno (BFGS) minimization technique⁶² is used, which allows quick search for the lowest energy structure. The convergence factors are set as the difference in total energy within 5×10^{-6} eV per atom, maximum ionic Hellmann– Feynman force within 0.01 eV $Å^{-1}$, maximum displacement within 5×10^{-4} Å, and maximum stress within 0.02 GPa. In this study, the hydrostatic pressure up to 120 GPa with an interval of 40 GPa is used. The optimized crystal structure is visualized by using VESTA software.⁶³ The two-dimensional (2D) and three-dimensional (3D) anisotropic contour plots of Young's modulus, shear modulus, and Poisson's ratio are constructed by using the ELATE program.⁶⁴

3. Result and discussion

3.1 Structural properties

The halide perovskite compound KCaCl₃ is crystallized in cubic structure with the space group $Pm\bar{3}m$ (#221).^{50,55} The optimized crystal structure of KCaCl₃ with crystallographic sites is represented in Fig. 1. The unit cell of KCaCl₃ is made up of five atoms, which has one formula unit. In the structure, K atom occupies the corner with 1a Wyckoff position (0, 0, 0), Ca atom locates at the body center with 1b Wyckoff position (0.5, 0.5, 0.5), and Cl atom holds the face center with 3c Wyckoff position (0, 0, 5, 0.5).

Table 1 summarizes the pressure-dependent simulated values of the lattice constant and unit cell volume of KCaCl₃ in comparison to experimental and theoretical data. The estimated data are clearly in agreement with the experimental⁵⁷ and available theoretical results.^{50,55} The calculated lattice parameter is slightly larger than the experimental data due to the general tendency of GGA functional.⁴⁵ At 0 GPa, the computed lattice constant differs from the experimental value by only 0.60%, indicating that the present simulation is valid. Fig. 2(a) and (b) illustrates the effects of applied hydrostatic pressure (0–120 GPa) on the lattice constant and unit cell volume, respectively. As the pressure rises, both the lattice constant and unit cell volume are found to be reduced, indicating that the distance between atoms is getting decreased as represented in Table 2.

3.2 Electronic properties

The investigation of electronic properties including band structure, density of states, and electronic density map is crucial to get a clear idea about the optical properties. The band structure variations of KCaCl₃ under various hydrostatic pressures calculated by GGA-PBE functional are displayed in Fig. 3. The band structure configuration ranging from -4 to +8 eV is displayed. The Fermi level (E_F) is displayed at zero photon energy indicating by horizontal dashed line. The band structure at 0 GPa pressure reveals the wide band gap (E_g) of KCaCl₃ with a value of 4.75 eV. Since, the valence band maximum (VBM) and conduction band minimum (CBM) are located at *R* and *F* point, respectively, indicating indirect band gap of KCaCl₃. The equivalent band gap of 4.76 eV⁵⁰ and 4.811 eV⁵⁴ was also found in the previous investigations using the same functional

Table 1 The simulated and the available experimental with theoretical values of lattice constant, and unit cell volume of $KCaCl_3$ at different hydrostatic pressure

	Lattice constant, <i>a</i> (Å)			
Pressure (GPa)	This work (GGA-PBE)	Theoretical study (GGA-PBE)	Experimental	Volume, $V(Å^3)$
00	5.397	5.410 (ref. 50) 5.407 (ref. 55)	5.365 (ref. 57)	157.20
40	4.537			93.39
80	4.269	_	_	77.78
120	4.101	—	_	69.00



Fig. 2 Variation of (a) lattice constant and (b) unit cell volume of KCaCl₃ with pressure.

Table 2 The calculated bond lengths in halide perovskite KCaCl_3 under different pressure

	Bond length (Å)						
Bonds	0 GPa	40 GPa	80 GPa	120 GPa			
K–Cl Ca–Cl	3.81626 2.69850	3.20811 2.26848	3.01834 2.13429	2.90029 2.05082			

showing the authenticity of the present calculations. The applied pressure shows a major impact on the energy band gap and its nature. The value of $E_{\rm g}$ becomes significantly reduced from ultra-violet (4.75 eV) to visible (2.71 eV) region under pressure up to 120 GPa (Fig. 4), which allows electrons easily transport from valence band (VB) to conduction band (CB). Thus, the optical absorption and conductivity becomes higher, which is advantageous for optoelectronic applications. It is well-known that there exists an inverse relationship between the band



Fig. 3 Band structure of KCaCl₃ under various applied pressures.



Fig. 4 Variation of band gap of KCaCl_3 under various applied pressures.

gap and external applied pressure.⁶⁵ By applying the external pressure, the potential between the electron-ion is enhanced and hence the lattice parameters are reduced (Table 1). Due to this reduction in lattice parameters the band gap is reduced at the Brillouin zone symmetry points. Moreover, the nature of band gap is switched from indirect to direct after the application of 40 GPa pressure, as VBM is shifted from *R* to Γ point.

The applied external pressure elongates the VB that shows a linear extension to higher energies at the Γ point. Such states shifting in energy induce specific rearrangement of states, resulting in an indirect to direct band gap transformation. The transition of band gap from indirect to direct under pressure was also observed for cubic halide perovskites $ACaF_3$ (A = K, Rb).^{51,53} This transition reduces the energy required for electrons to move from the VB to the CB, which may improve device performance.^{45,46} Since the VBM and CBM move forward to the E_F under pressure, the separation between certain VBs as well as certain CBs is increased. The prominent feature is observed at *R* and Γ points of the Brillouin zone.

For more clarification the partial density of states (PDOS) of KCaCl₃ at various applied pressures are plotted in Fig. 5. The vertical dashed line at 0 eV represents the Fermi level $(E_{\rm F})$. The reducing tendency of E_{g} under pressure is also observed in the PDOS diagram, as the VBs and CBs move towards the $E_{\rm F}$. By increasing external pressure the hybridization between K-3p and Cl-3p is enhanced, which lifts the CBs towards the $E_{\rm F}$ and hence the band gap is reduced. Moreover, the reduction in K-Cl bond length under pressure (Table 2) would enhance the hybridization between the K-3p and Cl-3p orbitals. The increased hybridization lifts up the VBM and down the CBM at Γ point of the Brillouin zone (Fig. 3), consequently reducing the band gap from 4.75 eV to 2.17 eV. This phenomenon is supported by the band diagrams. The VB of both non-pressurized and pressurized system is originated mostly from Cl-3p state with negligible share of K-3p and Ca-3p states. On the other hand, the CB is dominated by 4s, 3p orbitals of K atoms with small contribution of Cl-3p state.

The charge density mapping is also studied in order to understand the behavior of chemical bonding. Fig. 6 shows the charge density distribution of KCaCl_3 at 0 and 120 GPa pressure along the crystallographic planes (100) and (200). The intensity of charge (electron) density is represented by the scale on the



Fig. 5 The partial density of states of cubic perovskite KCaCl₃ under pressure.

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right side of the density map. At ambient pressure the electron charge distributions of K and Cl atoms are not overlapped along (100) plane, representing ionic bonding of K–Cl (Fig. 6(a)). In contrast, a slight overlapping of Ca and Cl atoms is observed along (200) plane (Fig. 6(b)), indicating covalent nature of Ca–Cl bonds. However, the spacing between K and Cl atoms reduces and begins to overlap along (100) plane (Fig. 6(c)) under pressure (120 GPa), converting the ionic character of K–Cl to covalent. Furthermore, the overlapping between Ca and Cl atoms increases along (200) plane (Fig. 6(d)) under hydrostatic pressure, intensifying the covalent nature of Ca–Cl bonds.

3.3 Optical properties

Due to the large band gap (4.75 eV) in the ultra-violet range, halide perovskite KCaCl₃ is not suited for optoelectronic applications. As a result, more advancement is required for improved performance in solar cell and other optoelectronic applications. The application of hydrostatic pressure might be a simple and effective approach to reduce the band gap for this purpose.^{45–49} The exploration of optical profiles is a high-impact criterion for obtaining suitable concept about a material's compatibility in order to improve device efficiency. Therefore, the optical functions, namely absorption (α), conductivity (σ), reflectivity (R), refractive index (η), and dielectric function (ε) of KCaCl₃ are studied under induced pressure ranging from 0 to 120 GPa. The absorption coefficient (α) is a critical measure for determining a material's ability to absorb light energy and gives essential information on solar energy conversion efficiency.⁴⁸ Fig. 7(a) shows the variation of α of KCaCl₃ as a function of photon energy under pressure up to 120 GPa. It begins at band gap due to the absorption of ultra-violet radiation at 0 GPa, which causes transition of charges from VB to CB. Consequently, the optical conductivity also starts at band gap value because of the availability of charges in the CB. As the pressure increases the fundamental absorption shifts from ultra-violet to visible range of the electromagnetic spectrum. With the rise in pressure, the edge of α has clearly migrated to the low energy zone known as red shift⁴⁵⁻⁴⁹ that is consistent to the pressuredependent band gap variation. Moreover, the calculated α of KCaCl₃ shows linear increase due to the illustrated direct band gap after the increasing application of pressure that is better than that of indirect band gap nature at 0 GPa. The induced pressure dramatically boosts the absorption, implying that applying pressure significantly improve the potentiality of KCaCl₃ perovskite in solar cell or other optoelectronic devices. Furthermore, KCaCl₃ can be an efficient material for sterilizing the surgical instruments due to the wide absorption peak in the ultra-violet region. The optical conductivity or photoconductivity (σ) of KCaCl₃ under pressure is displayed in Fig. 7(b). The σ spectrum exhibits the similar pattern of α spectrum (Fig. 7(a) and (b)), as a material releases free carriers for conduction during photon absorption. However, both α and σ are not started at 0 eV for the system under pressure from 0-120 GPa, reconfirming the insulating/semiconducting nature of $KCaCl_3$. It can be seen from Fig. 7(b) that at zero pressure the σ starts from 4.75 eV and moves towards lower energies, as



Fig. 6 The electron density map of KCaCl₃ (a) and (b) at 0 GPa and (c) and (d) at 120 GPa along the crystallographic planes (100) and (200).



Fig. 7 The pressure-induced (a) absorption and (b) conductivity spectra of KCaCl₃.

the pressure is increased. It is also observed that the σ shows maximum value when KCaCl₃ stabilizes direct band gap after the pressure being applied, which has a linear increasing tendency with increased pressure. Because of its improved conductivity under pressure, KCaCl₃ is expected to be an effective halide perovskite for improving optoelectronic device efficiency.

The surface nature of the KCaCl₃ perovskite can be determined in relation to the reflected light energy from the surface.⁶⁶ The reflectivity (R) spectrum of KCaCl₃ as a function of photon energy under pressure is displayed in Fig. 8(a). The studied compound shows the best reflecting behavior in the energy range of 13–16 eV. It can be clearly seen from Fig. 7(a) and 8(a) that when the α edge is at 0 eV then at the same energy point the R has some value, which reveals the inverse relationship of absorption and reflectivity. Therefore, it is required to have high absorption and low reflectivity at low energy region for high performance photovoltaic devices. However, the R increases at low energy region with applied pressure, which may decrease the effectiveness of the photovoltaic efficiency. Therefore, further research should be done to reduce the R, which can increase absorption and photovoltaic performance. Importantly, as the *R* increases under pressure in the high energy zone, the titled material appears to be more promising for reducing solar heating. The refractive index (η) describes the speed with which light passes through a material⁶⁷ and also provides information about a material's suitability for device applications.⁶⁸ It is seen from Fig. 8(b) that at 0 eV, with the increase of pressure from 0.0–10 GPa, the $\eta(0)$ increases from 1.55 to 2.15. The increased, $\eta(0)$ under pressure can make KCaCl₃, more appropriate for application in QLED, OLED, solar cells, and waveguides.^{69,70} The trend of η is similar to the real part of dielectric function ε_1 (Fig. (8b) and (c)). It starts with a static value of 1.55 at 0 GPa and reaches to a maximum of 2.15 at \sim 7 eV energy, which increases with increase in pressure. However, the η decreases below unity in energy range 25–35 eV. In this region, the group velocity of incident radiations is greater than the velocity of light because the η is less than unity.^{71,72} As a result, the group velocity transfers to the negative domain and the nature of medium changes from linear to nonlinear.

The rate of charge-carrier recombination is governed by the dielectric function, which is a crucial optical parameter.45-49,73 It provides a clear picture of optoelectronic device performance.74 Solar cells with a higher static dielectric constant have lower recombination rates.⁷⁵ Fig. 8(c) and (d) show the real (ε_1) and imaginary (ε_2) part of dielectric constant of non-toxic KCaCl₃ under applied pressure, respectively. Pressure causes a higher static dielectric function, $\varepsilon_1(0)$ of KCaCl₃ than that of nonpressurized system (Fig. 8(c)), which could improve device efficiency. It can be seen that the value of $\varepsilon_1(0)$ increases with increasing pressure, viewing the band gap is inversely associated to $\varepsilon_1(0)$; a smaller energy gap results in a higher $\varepsilon_1(0)$ value. Moreover, the pressure-induced KCaCl₃ exhibits higher ε_1 in the visible region. The ε_2 is also linked to the optical absorption and the band gap of a material. Similar to the optical absorption, the applied pressure raises ε_2 in the visible region, and the peaks transfer to a low photon energy area, which concludes that KCaCl₃ is a good absorber of visible light under pressure. The ε_2 drops to zero as the photon energy increases because the absorption under all applied pressures is very low in the high photon energy region. Furthermore, the higher ε_1 and ε_2 at low photon energy as well as lower ε_1 and ε_2 at high energy region explicit the potential of KCaCl₃ in microelectronics and integrated circuits10

3.4 Mechanical properties

Elastic constants (C_{ij}) are a crucial element in calculating mechanical properties, such as brittleness, ductility, stiffness, and anisotropy.^{45–49} C_{ij} can be used to identify mechanical stability and internal forces in solids.^{45–49} The finite strain theory⁷⁶ is used to determine the mechanical properties in this study. Because the lattice parameters of KCaCl₃ decrease with induced pressure (Fig. 2), it is critical to understand how pressure affects the C_{ij} in order to gain better understanding of the mechanical properties. The three independent elastic constants of cubic KCaCl₃ perovskite are C_{11} , C_{12} , and C_{44} . The calculated



Fig. 8 The pressure-induced (a) reflectivity, (b) refractive index, (c) real part of dielectric function, and (d) imaginary part of dielectric function of KCaCl₃.

Table 3	The calculated elastic constants (C_{ij}) and Cauchy pressure ($C_{12} - C_{44}$) of KCaCl ₃ at various applied pressures compared with	i previously
reported	d data of halide perovskites CsXCl ₃ (X = Sn,Ge,Ca)	

Compound	Pressure (GPa)	<i>C</i> ₁₁	C_{12}	C_{44}	$C_{12} - C_{44}$	Ref.
CsSnCl ₃	0	50.66	8.71	6.01	2.70	45
CsGeCl ₃	0	54.86	12.95	12.00	0.95	48
CsCaCl ₃	0	56.905	9.692	10.233	_	80
KCaCl ₃	0	54.06	9.26	7.80	1.46	This work
	40	356.87	67.29	8.17	59.12	This work
	80	606.10	120.29	7.40	112.89	This work
	120	818.07	170.96	6.82	164.14	This work

Table 4 The calculated bulk modulus *B* (GPa), shear modulus *G* (GPa), Young's modulus *E* (GPa), Poisson's ratio (ν), Pugh's ratio (*B*/*G*), and elastic anisotropy (*A*) of KCaCl₃ at different applied pressures compared with previously reported data of halide perovskites CsXCl₃ (X = Sn, Ge, Ca)

Compound	Pressure (GPa)	В	G	Ε	B/G	ν	A	Ref.
CsSnCl ₃	0	22.70	10.20	26.61	2.22	0.300	_	45
CsGeCl ₃	0	26.92	15.03	38.01	1.79	0.265	_	48
CsCaCl ₃	0	25.430	14.406	36.353	1.765	0.363	0.433	80
KCaCl ₃	0	24.20	12.10	31.11	2.00	0.285	0.35	This work
U	40	163.81	37.97	105.74	4.31	0.392	0.06	This work
	80	282.23	56.85	159.81	4.96	0.405	0.03	This work
	120	386.66	72.36	204.33	5.34	0.411	0.02	This work



Fig. 9 Variation of (a) Poisson's ratio and (b) Pugh's ratio of KCaCl₃ under pressure.

 C_{ij} at various applied pressure are listed in Table 3. The mechanical stability of cubic crystals is determined by the Born stability criterion⁷⁷ listed below.

 $C_{11} > 0, C_{44} > 0, (C_{11} - C_{12}) > 0, (C_{11} + 2C_{12}) > 0$

The calculated elastic constants meet the aforementioned criteria over the whole pressure range, confirming structural stability of KCaCl₃ at high pressure. Since, the reported elastic constants are not available; this study cannot compare the present results. However, the calculated elastic constants at 0 GPa are comparable with the halide perovskites CsXCl₃ (X = Sn,



Fig. 10 The anisotropic 2D and 3D representation of (a) Young's modulus, (b) shear modulus, and (c) Poisson's ratio of KCaCl₃ at 0 and 120 GPa pressure.

Ge, Ca).^{45,48,80} The difference between C_{12} and C_{44} is known as Cauchy pressure and it can be used to determine whether a material is ductile (positive value) or brittle (negative value).^{45–49} Under all applied pressures, the KCaCl₃ possesses positive Cauchy pressure, indicating its ductile character and the ductility becomes intensive with increased pressure (Table 3).

The elastic moduli, such as bulk modulus (B), shear modulus (G), Young's modulus (E) can be determined using Voight-Reuss-Hill approximation (VHR).78 The fundamental mechanical properties, namely Pugh's ratio (B/G), Poisson's ratio (ν) , and anisotropy factor (A) are calculated using the expressions in the previous literature.⁷⁹ The calculated $B, G, E, B/G, \nu$, and A are listed in Table 4 having almost similar values with previously studied halide perovskites CsXCl₃ (X = Sn, Ge, Ca).^{45,48,80} The value of B, G, and E increase as the applied pressure is increased, indicating that applying hydrostatic pressure incorporates the hardness, stiffness, and higher resistance to KCaCl₃ against tensile deformation under high pressure.45,48 Unfortunately, there is no literature data of elastic moduli to compare with the pressure induced results. To the best of our knowledge, this is the first theoretical work on this compound under high pressure. Therefore, this study can serve as a prediction for future works. Pugh's ratio (B/G) and Poisson's ratio (ν) are crucial parameters to investigate the ductile/brittle character of a material.

The critical value of B/G and ν to recognize the brittle/ductile nature of a material is 1.75 and 0.26, respectively.^{45–49} A material is termed as ductile if the B/G and ν surpass the critical value, otherwise it is brittle. According to the computed B/G and ν , KCaCl₃ is a ductile material that becomes more ductile when the applied pressure is raised, as seen in Fig. 9(a) and (b), respectively. The increased ductility of KCaCl₃ under pressure makes it more suitable for use in optoelectronic devices.⁸¹ Moreover, the value of ν should be in the range of 0.25–0.50 to detect the presence of central force within a crystal.⁸² It is seen from Table 4 that the value of ν lies within 0.25–0.50 over the entire pressure range, confirming the presence of central force inside KCaCl₃.

The Zener anisotropy index (*A*) indicates whether a substance is isotropic or anisotropic. It is calculated by using the following Zener equation^{83,84} and listed in Table 4.

$$A = \frac{2C_{44}}{C_{11} - C_{12}}$$

The compound is classified as isotropic when the value of A is unity; however, the deviation from unity reflects the degree of anisotropy.⁸³ The value of A manifests the anisotropic nature of KCaCl₃, which become more anisotropic under pressure.

In order to visually explore the anisotropic nature of KCaCl₃, the 2D and 3D anisotropic contour plots of Young's modulus (*E*), shear modulus (*G*), and Poisson's ratio (ν) at 0 and 120 GPa pressure are presented in Fig. 10(a) and (b), respectively. The 2D plots are constructed along the *xy*-, *yz*-, and *xz*-planes, but the projections are taken on the *xy*-plane. The isotropy of a material is represented by the circular 2D and spherical 3D plots, whereas the departure from those reveals anisotropy.^{47,48} The 2D and 3D contour plots clearly show that the investigated $KCaCl_3$ has anisotropic character in all directions. However, the deviation of circular 2D and spherical 3D is more intensive in the case of 120 GPa than that of 0 GPa pressure, implying that pressure induces more anisotropy in $KCaCl_3$.

4. Conclusions

For the first time, a DFT-based simulation was used to examine the effect of pressure (up to 120 GPa) on the structural, electronic, optical, and mechanical properties of the cubic halide perovskite KCaCl₃. The optimized lattice parameters demonstrate good agreement with reported experimental and theoretical evidences, but being reduced under pressure. According to the examination of electronic behavior, the band gap of KCaCl₃ can be tuned by applying pressure. The band gap narrows dramatically from ultra-violet to visible light under pressure, which is advantageous for solar cell applications. The indirect band gap is also found to be converted into a direct band gap, which is helpful for optoelectronic applications. The pressure-induced optical functions are also studied, yielding some intriguing results as well as a variety of feasible applications. The estimated elastic constants maintain the Born stability criterion, ensuring the mechanical stability of KCaCl₃ over the whole pressure range. The application of pressure makes the compound more ductile and anisotropic.

Data availability

The datasets generated and/or analyzed in this study are available from the corresponding author upon reasonable request.

Author contributions

Muhtasim Ali Haq: investigation, methodology, data curation, writing original draft; Md Saiduzzaman: formal analysis, conceptualization, supervision, writing original draft, reviewing and editing; Tariqul Islam Asif & Ismile Khan Shuvo: formal analysis, investigation; Khandaker Monower Hossain: formal analysis, validation, supervision, writing the original draft, reviewing and editing.

Conflicts of interest

There is no conflict of interest to declare.

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