



# Article An Effective Shrinkage Control Method for Tooth Profile Accuracy Improvement of Micro-Injection-Molded Small-Module Plastic Gears

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**Abstract:** An effective method to control the non-linear shrinkage of micro-injection molded smallmodule plastic gears by combining multi-objective optimization with Moldflow simulation is proposed. The accuracy of the simulation model was verified in a micro-injection molding experiment using reference process parameters. The maximum shrinkage ( $Y_1$ ), volume shrinkage ( $Y_2$ ), addendum diameter shrinkage ( $Y_3$ ), and root circle diameter shrinkage ( $Y_4$ ) were utilized as optimization objectives to characterize the non-linear shrinkage of the studied gear. An analysis of the relationship between key process parameters and the optimization objectives was undertaken using a secondorder response surface model (RSM-Quadratic). Finally, multi-objective optimization was carried out using the non-dominated sorting genetic algorithm-II (NSGA-II). The error rates for the key shrinkage dimensions were all below 2%. The simulation results showed that the gear shrinkage variables,  $Y_1$ ,  $Y_2$ ,  $Y_3$ , and  $Y_4$ , were reduced by 5.60%, 8.23%, 11.71%, and 11.39%, respectively. Moreover, the tooth profile inclination deviation ( $f_{H\alpha T}$ ), the profile deviation ( $f_{f\alpha T}$ ), and the total tooth profile deviation ( $F_{\alpha T}$ ) were reduced by 47.57%, 23.43%, and 49.96%, respectively. Consequently, the proposed method has considerable potential for application in the high-precision and high-efficiency manufacture of small-module plastic gears.

**Keywords:** micro-injection molding; small-module gear; plastic gear; non-linear shrinkage; tooth profile accuracy

## 1. Introduction

In recent decades, with the rapid development of high-performance engineering plastics [1,2], small-module plastic gear has been widely applied in cutting-edge fields, such as aerospace [3], medical devices [4], and automobiles [5]. Compared with small-module metal gear, small-module plastic gear has obvious advantages, such as self-lubrication, strong shock and vibration resistance, and low noise [6,7]. Micro-injection molding is likely to become the main processing method for small-module plastic gear in the future because it enables production in large quantities [8,9]. However, because of the high shrinkage of engineering plastics and the irregular surface shape of gear teeth, plastic gear can undergo significant non-linear shrinkage during micro-injection molding [10–13]. Moreover, the specific surface area of small module gear teeth is small, which leads to complex and changeable interface heat transfer events during the cooling process [14,15]. Hence, the non-linear shrinkage of micro-injection molded small-module plastic gears is difficult to control.

Because of the small size of the small-module gear itself, the non-linear shrinkage phenomenon during the micro-injection molding greatly influences the tooth profile accuracy of small-module plastic gears [16]. In addition to the rational design of the mold



Citation: Wu, W.; He, X.; Li, B.; Shan, Z. An Effective Shrinkage Control Method for Tooth Profile Accuracy Improvement of Micro-Injection-Molded Small-Module Plastic Gears. *Polymers* 2022, *14*, 3114. https:// doi.org/10.3390/polym14153114

Academic Editor: Yi-Je Juang

Received: 11 July 2022 Accepted: 27 July 2022 Published: 30 July 2022

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**Copyright:** © 2022 by the authors. Licensee MDPI, Basel, Switzerland. This article is an open access article distributed under the terms and conditions of the Creative Commons Attribution (CC BY) license (https:// creativecommons.org/licenses/by/ 4.0/). structure and the selection of materials, the scientific selection of injection molding process parameters is an effective way to control shrinkage. There are many process parameters that affect the molding quality of small-module plastic gears. There is a complex, time-varying, nonlinear and strong coupling relationship between process the parameters and molding quality goals [17,18]. For this reason, it is particularly difficult to find a reasonable set of optimal process parameters. The traditional optimization method involves the constant adjustment of process parameters by injection molding personnel, based on experience, to obtain ideal parameter combinations. However, the traditional method is unable to achieve global optimal parameters, which greatly prolongs trial time, increases trial cost, and wastes raw materials [19,20]. Therefore, determining how to quickly obtain the optimal process parameters for micro-injection molding on a scientific basis is of great practical significance for the high-precision and high-efficiency manufacture of small-module plastic gears.

The problem highlighted has attracted the attention of many researchers. In recent years, computer-aided engineering (CAE) technology and optimization design theory have been continuously developed [21,22]. CAE simulation technology has been used to replace the traditional continuous mode test method [23]. Combined with optimal design theory, it has been used in the optimization of injection molding process conditions, not only to improve the quality of plastic parts, but also to shorten the molding cycle [24]. Hakimian et al. simulated and analyzed the micro-injection molding process of 0.6 mmtooth-thickness micro-gear based on Moldflow and optimized the process of maximum warpage and shrinkage using the Taguchi method [25]. Combining grey relational analysis and simulation analysis, Mehat et al. studied the influence of process parameters on the warping deformation of plastic gears [26].

In general, most current research considers warpage deformation and maximum shrinkage to be the process optimization goals of the gear when applying simulation models [25–28]. It is difficult to directly assess the degree of optimization of gear tooth profile accuracy. Optimization results deviate significantly from those observed in actual industrial production if optimization is based on simulation which is unverified by experiments. In many studies, the test samples are mainly subjected to orthogonal tests [15,25,29,30]. However, in orthogonal tests, problems of sample point accumulation can occur, and the test samples may not adequately represent all the important variables. Therefore, it is necessary to combine simulation with experiment, and to use CAE simulation and multi-objective optimization to control the non-linear shrinkage of small-module plastic gears. In addition, it is impossible to directly characterize and optimize tooth profile accuracy through simulation results. Therefore, it is important to identify optimization objectives that can be easily characterized and which fully reflect tooth profile accuracy.

This paper focuses on the challenge of low tooth profile accuracy caused by non-linear shrinkage associated with the micro-injection molding of small-module plastic gears. We propose a novel method for shrinkage control that combines multi-objective optimization with Moldflow simulation to improve tooth profile accuracy, as shown in Figure 1. Local shrinkage, overall shrinkage, and key dimension shrinkage of small-module plastic gears are the main factors affecting tooth profile accuracy [15]. We use the maximum shrinkage  $(Y_1)$ , volume shrinkage  $(Y_3)$ , addendum diameter shrinkage  $(Y_3)$ , and root circle diameter shrinkage ( $Y_4$ ) as the optimization objectives for characterizing the non-linear shrinkage of the studied gear. Approximation surrogate models representing the relationships between the process parameters and the optimization objectives were established. The four optimization objectives were optimized in a non-normalized approach using the non-dominated sorting genetic algorithm-II (NSGA-II). Finally, micro-injection molding experiments on the studied gears were carried out using reference and optimal process parameters. As a result, shrinkage of the studied gear was well controlled. Measurements of size and tooth profile accuracy indicated that key dimension shrinkage errors between the simulation and experimental tests were less than 2%. Moreover, tooth profile inclination deviation  $f_{H\alpha T}$ , tooth profile deviation  $f_{f\alpha T}$  and total tooth profile deviation  $F_{\alpha T}$  were reduced by

47.57%, 23.43%, and 49.96%, respectively. Consequently, the proposed method can inform the high-precision and high-efficiency manufacture of small-module plastic gears.



**Figure 1.** The tooth profile accuracy improvement method for micro-injection molded small-module plastic gears.

## 2. Materials and Methods

## 2.1. 3D model and Material of Studied Gear

In this study, small-module involute cylindrical gear (module = 0.5 mm) was studied. A three-dimensional (3D) model and the dimension parameters of the studied gear are shown in Figure 2. Polyformaldehyde (POM) is most commonly used for production of plastic gears. It is a thermoplastic crystalline polymer with high strength and good wear resistance. The studied gear was made from POM-100 P, produced by DuPont, US, which is the most used high-performance crystalline engineering plastic for small-module plastic gears [31–33]. The physical properties of the materials used are shown in Table 1.



**Figure 2.** The 3D model and dimension parameters of the studied gear: Module (m) = 0.5 mm; number of teeth (*z*) = 20; modification coefficient ( $\chi$ ) = 0; pressure angle ( $\alpha$ ) = 20 °.

Parameters	Test Method	Value
Water absorption (%)	ASTM D-570	0.25
Hardness (R)	ASTM D-785	120
Tensile strength (MPa)	ASTM D-638	69
Elasticity coefficient (MPa)	ASTM D-638	3360
Deflection coefficient (MPa)	ASTM D-790	3090
Shear strength (MPa)	ASTM D-732	66
Tensile impact strength $(kJ/m^2)$	ASTM D-1822	420
Thermal expansion coefficient ( $10^{-5} \text{ m /m}^{\circ}\text{C}$ )	ASTM D-696	12.2

Table 1. Properties of DuPont POM-100 P.

## 2.2. Moldflow Simulation

Autodesk Moldflow Insight (AMI) 2021 software, US, [34,35] was used for the simulation of small-module plastic gear micro-injection molding. For small-module gears, the polymer filling process is extremely short, and the process cannot be observed visually, so it is difficult to characterize experimentally. However, the polymer flow molding process can be studied visually using Moldflow. To facilitate later extraction of the 3D shrinkage gear model, a built 3D model of the studied gear was imported into the Moldflow software using an .stp extension. The gating system of the simulation model was established according to the actual forming gating system. A double-layer mesh was used for meshing, and the global edge length was 0.15 mm. The mesh chord angle was 20 degrees. The minimum curvature size was 10% of the global size. The mesh model was optimized by reducing the aspect ratio through operations such as merging nodes and integrating nodes. The injection gate position was then set according to the actual micro-injection molding. The gear simulation model is shown in Figure 3.



Figure 3. Simulation model of the studied gear.

The analysis type chosen for this study was "thermoplastic injection molding". The analysis sequence was "Filling + Packing + Warpage". Then, POM 100-P from DuPont was selected in the software material library. Parallel computing was specified to improve the computing speed.

# 2.3. Experimental Design

Studies have found that the local shrinkage, overall shrinkage and key dimension shrinkage of plastic gears directly affect the tooth accuracy [25]. For this reason, the maximum shrinkage ( $Y_1$ ), volume shrinkage ( $Y_2$ ), addendum diameter shrinkage ( $Y_3$ ) and root circle diameter shrinkage ( $Y_4$ ) were taken to be optimization objectives for multi-objective optimization. The maximum shrinkage ( $Y_1$ ) and volume shrinkage ( $Y_2$ ) were obtained directly from the simulation results. The key dimension shrinkage was also assessed to verify the accuracy of the simulation model. The 3D model of the gear after shrinkage was extracted through Moldflow simulation. The diameter of the addendum and root circle were measured by CAD software. The addendum diameter shrinkage ( $Y_3$ ) and the root circle diameter shrinkage ( $Y_4$ ) were calculated using Equations (1) and (2).

$$Y_3 = \frac{d_a - d'_a}{d_a} \times 100\tag{1}$$

$$Y_4 = \frac{d_f - d'_f}{d_f} \times 100\tag{2}$$

where  $d_a$  and  $d'_a$  are the addendum circle diameters of the studied gear and the shrinkage gear, and  $d_f$  and  $d'_f$  are the root circle diameters of the studied gear and the shrinkage gear.

Based on previous research and long-term practical experience in the production of small-module plastic gears, the mold temperature, melt temperature, packing pressure, packing time, and cooling time were selected as input factors. Compared to traditional single-factor experimental designs and orthogonal experimental designs, the Box–Behnken design (BBD) method facilitates the analysis of individual and interactional effects of parameters on responses with fewer experiments and lower computational cost [36,37]. Thus, the BBD method was utilized to quantitatively analyze the influence of key process parameters on the shrinkage of small-module plastic gear. The micro-injection molding process levels were selected according to the range of process parameters recommended by the Moldflow material library, and production experience, as shown in Table 2. The 46 groups of BBD simulation results are shown in Table 3. It was found that the optimal results for  $Y_1$ ,  $Y_2$ ,  $Y_3$  and  $Y_4$  appeared in 39, 13, 12 and 41 groups of trials, respectively. Therefore, the interaction between the objectives was substantial, and the four objectives could not be minimized at the same time through conventional single-objective optimization.

Table 2. Factors and levels of key process parameters.

	Factors	Minimum Level	Intermediate Level	Maximum Level
A	Mold temperature (°C)	60	80	100
В	Melt temperature (°C)	190	210	230
С	Packing pressure (MPa)	60	70	80
D	Packing time (s)	1	3	5
Ε	Cooling time (s)	10	20	30

#### 2.4. Approximate Surrogate Model

An approximate surrogate model can effectively save time required for CAE simulation. If the accuracy of the established model is reliable, the model can be applied to predict the properties of unknown points in space. In this study, Kriging models [38], radial basis function (RBF) models [39], linear response surface models (RSM) [40], RSM-Quadratic, RSM-Cubic and RSM-Quartet models between process parameters, and optimization objectives, were established using the Isight platform, US [41,42].

D			Factor	Response of			onse of Op	nse of Optimize Objectives		
Kun#	A (°C)	B (°C)	C (MPa)	D (s)	<i>E</i> (s)	<i>Y</i> <sub>1</sub> (mm)	Y <sub>2</sub> (%)	Y <sub>3</sub> (%)	Y <sub>4</sub> (%)	
1	80	210	80	3	10	0.1452	13.16	6.07273	6.33143	
2	80	230	70	3	10	0.1452	14.37	6.01818	6.35429	
3	80	210	70	3	20	0.1483	13.49	6.12727	6.40000	
4	100	190	70	3	20	0.1553	13.55	6.45455	6.67429	
5	80	230	60	3	20	0.1479	14.59	6.16364	6.42286	
6	100	230	70	3	20	0.1536	16.35	6.30909	6.69714	
7	80	210	80	1	20	0.1687	17.18	6.89091	6.97143	
8	100	210	70	3	10	0.1519	13.78	6.25455	6.51429	
9	60	210	70	3	30	0.1453	13.49	5.98182	6.21714	
10	80	210	60	1	20	0.1711	17.38	6.96364	7.04000	
11	80	190	70	1	20	0.1726	15.86	7.05455	7.15429	
12	60	210	70	5	20	0.1431	13.33	5.70909	5.96571	
13	80	190	80	3	20	0.1486	12.21	6.09091	6.40000	
14	60	190	70	3	20	0.1494	12.75	6.10909	6.46857	
15	80	190	70	3	30	0.1523	12.68	6.29091	6.60571	
16	80	230	70	5	20	0.1433	14.40	5.81818	6.08000	
17	60	210	70	1	20	0.1681	16.96	6.83636	6.92571	
18	100	210	80	3	20	0.1484	13.64	6.16364	6.40000	
19	80	210	70	1	30	0.1699	17.27	6.94545	6.99429	
20	100	210	70	5	20	0.1507	13.81	6.21818	6.42286	
21	80	210	70	3	20	0.1483	13.49	6.14545	6.46857	
22	80	190	60	3	20	0.1560	13.08	6.43636	6.62857	
23	100	210	70	3	30	0.1515	13.78	6.29091	6.58286	
24	60	210	70	3	10	0.1453	13.49	5.96364	6.21714	
25	80	210	80	3	30	0.1448	13.16	5.96364	6.21714	
26	80	230	80	3	20	0.1422	14.18	5.87273	6.17143	
27	80	210	60	3	10	0.1516	13.81	6.23636	6.46857	
28	80	210	70	3	20	0.1483	13.49	6.05455	6.37714	
29	80	210	60	3	30	0.1516	13.81	6.16364	6.49143	
30	80	210	70	3	20	0.1483	13.49	6.10909	6.44571	
31	80	190	70	3	10	0.1523	12.68	6.25455	6.53714	
32	80	210	70	3	20	0.1483	13.49	6.18182	6.46857	
33	80	210	60	5	20	0.1498	13.89	6.05455	6.33143	
34	80	210	70	5	10	0.1463	13.51	5.90909	6.26286	
35	100	210	70	1	20	0.1711	17.47	7.00000	7.08571	
36	80	230	70	3	30	0.1449	14.49	5.98182	6.37714	
37	80	210	70	3	20	0.1483	14.83	6.07273	6.46857	
38	80	190	70	5	20	0.1493	12.65	6.00000	6.14857	
39	60	230	70	3	20	0.1416	14.04	5.83636	6.12571	
40	60	210	80	3	20	0.1418	13.02	5.78182	6.17143	
41	80	210	80	5	20	0.1426	13.18	5.76364	5.94286	
42	80	210	70	5	30	0.1462	13.51	5.92727	6.17143	
43	100	210	60	3	20	0.1543	13.93	6.34545	6.56000	
44	80	210	70	1	10	0.1699	17.27	6.94545	7.01714	
45	60	210	60	3	20	0.1483	13.72	6.05455	6.33143	
46	80	230	70	1	20	0.1660	18.39	6.78182	6.85714	

Table 3. Box-Behnken experimental design and simulation results.

To determine if a model is representative, it is necessary to verify the convergence accuracy of the model through error analysis. The method used to verify the accuracy of the surrogate model involves comparison of the approximation of the predicted value and the test sample. This study mainly used R-square ( $R^2$ ) to evaluate the accuracy of the built surrogate model. The most suitable surrogate model was selected through error analysis to predict the shrinkage of the gear more accurately. Moreover, the approximate surrogate model was suitable for further multi-objective optimization to minimize the shrinkage of the small-module plastic gear.

#### 2.5. Multi-Objective Optimization

Since practical engineering problems are complex and involve uncertain factors, most problems can be studied with multi-objective optimization strategies. Multi-objective optimization algorithms provide more satisfactory solutions than single-objective optimization methods [43,44]. Multi-objective optimization methods have attracted the attention of researchers in different disciplines and fields. Many population-based algorithms have been proposed which have been used to solve the multi-objective optimization problem (MOP) in engineering applications.

The improved non-dominated sorting genetic algorithm, NSGA-II [45,46], has good exploration performance and an efficient sorting process. The principle of the NSGA-II algorithm is shown in Figure 4. The algorithm not only uses crowding degree and a crowding degree comparison operator to replace the fitness sharing strategy under the control of sharing radius, but also introduces an elite strategy to ensure that the best individual is not lost. Therefore, in this study, the NSGA-II multi-objective optimization algorithm was selected to optimize gear shrinkage. For the algorithm settings, the population side was set to 12, the number of generations was set to 20, and the number of samples was 240, which meets the recommended value of between 20 and 200. The crossover probability crossover rate was set to 0.9, the recommended value was 0.6~1, and the remaining settings were set by default.



Figure 4. Schematic diagram of NSGA-II algorithm.

The mathematical model of the process optimization problem of gear shrinkage in this study was expressed as Equation (3).

$$\begin{cases} F = \min[Y_1(\text{mm}), Y_2(\%), Y_1(\%), Y_1(\%)] \\ & \begin{cases} 60 \le A \le 100(^{\circ}\text{C}) \\ 190 \le B \le 230(^{\circ}\text{C}) \\ 60 \le C \le 80(\text{MPa}) \\ 1 \le D \le 5(\text{s}) \\ 10 < E < 30(\text{s}) \end{cases}$$
(3)

### 2.6. Experimental Verification of Simulation Model and Optimization Method

First, the reliability of the gear simulation model required to be verified through micro-injection molding pre-testing with reference process parameters. The self-built micro-injection molding experiment platform is shown in Figure 5a, and the mold structure is shown in Figure 5b. Figure 5c is the actual mold of the studied gear. According to the recommended process for assessing materials, the reference process parameters are shown in Table 4. The diameter of the addendum circle and root circle were measured using a

digital super-depth microscope (KEYENCE VHX-1000C, US). The addendum diameter shrinkage ( $Y_3$ ) and the root circle diameter shrinkage ( $Y_4$ ) of the gear samples were calculated using Equations (1) and (2), respectively. The reliability of the simulation model was verified by comparing the key dimensions shrinkage between the simulation and experiment under reference process parameters.



**Figure 5.** (**a**) Micro-injection molding experiment platform of small-module plastic gears. (**b**) Cavity layout of the mold. (**c**) The actual mold of the studied gear.

Table 4. Reference process parameters.

Parameters	Value
Mold temperature (°C)	80
Melt temperature (°C)	210
Packing pressure (MPa)	70
Packing time (s)	3
Cooling time (s)	20

The results of multi-objective optimization require to be verified, and injection molding experiments were carried out under the obtained optimal process parameters. The optimization results of the NSGA-II algorithm were verified by Moldflow simulation. The accuracy of the optimized method was verified by comparing the key dimensions shrinkage and the tooth profile accuracy of the gear from the micro-injection molding experiments under reference and optimal process parameters. The tooth profile accuracy was automatically measured using an FPG 3002B small-module gear measuring machine [47]. Tooth profile accuracy [48,49] includes the deviation of tooth profile inclination ( $f_{H\alpha T}$ ), tooth profile deviation ( $f_{f\alpha T}$ ) and total tooth profile deviation ( $F_{\alpha T}$ ). The gear clamping and specific clamping method for the small-module gear are shown in Figure 6.



**Figure 6.** FPG 3002B small-module gear measuring machine and clamping method of small-module gear.

#### 3. Results and Discussion

#### 3.1. Simulation Model Accuracy

Since the flow channel was injected symmetrically, the shrinkage of the two gears was basically the same. For this reason, we only selected a single gear for analysis. The shrinkage results of the studied gear obtained by Moldflow analysis are shown in Figure 7. From Figure 7a, it can be seen that the shrinkage of the gear was different at different positions. The tooth part of the gear shrank the most. During the cooling process, the cooling rate indicated by the gear teeth was very high due to the large temperature difference between the mold and the polymer melt. Accordingly, the gear teeth measurements indicated that the volume of the polymer molecular chain changed greatly. The degree of shrinkage near the addendum and the root circle of the studied gear was the largest, which is consistent with previous research findings [15,25]. In addition, the shrinkage of the part where the gear shrank the most was 0.4183 mm. The test results for the key dimensions of the gear obtained by simulation are shown in Figure 7b. The volume shrinkage of the gear obtained by simulation was 13.49% (Figure 7c).

The teeth morphology of the gear simple under reference process parameters was observed using a 200- $\times$  microscope, as shown in Figure 8a. It can be seen that the forming quality of the gear teeth was intact, so the gear samples could be adopted to verify the simulation model. The addendum and root circle diameters of the gear samples measured under the 50- $\times$  microscope are shown in Figure 8b. The key dimension shrinkage of the gear derived through simulation and experiment was calculated using Equations (1) and (2), as shown in Table 5. It was found that the errors between the experiment and the simulation were all less than 2 %. Therefore, the simulation model was able to accurately simulate the shrinkage of the studied gear.



**Figure 7.** Simulation results under the reference parameters. (**a**) Shrinkage cloud diagram. (**b**) Volume shrinkage. (**c**) Addendum diameter and root circle diameter.



**Figure 8.** (a) The tooth morphology of the gear sample. (b) Key dimension results of experiment under reference process parameters.

	Y <sub>3</sub> (%)	Y <sub>4</sub> (%)
Simulation	6.363	6.503
Experiment	6.334	6.571
Ērror (%)	0.300	1.035

Table 5. Comparison of key dimension shrinkage rates obtained by simulation and experiment.

#### 3.2. Approximate Surrogate Models and Effect Analysis of Process Parameters

The data in Table 2 was input into Isight software. The Approximate module was used to build the approximate surrogate models. Since the input factors are different types of physical quantities, the adaptation type was selected as anisotropic. To select the approximate surrogate model with the highest accuracy, the accuracy of the established five typical approximate surrogate models was compared; the results are shown in Table 6. It was found that the accuracy of the RSM-Linear model was clearly lower, and the accuracy of the optimization objectives was less than 85%. This indicated that there was a strong non-linear relationship between the optimization objectives and the process parameters. It was found that that the accuracy of volume shrinkage ( $Y_2$ ) in the Kriging models and the RBF models was below 90%. The RSM-Quadratic, RSM-Cubic, and RSM-Quartet models all achieved the required accuracy. However, compared with the RSM-Quadratic model, the accuracy improvement using the RSM-Cubic and RSM-Quartet models was not very significant; however, the computational complexity increased substantially. Accordingly, the RSM-Quadratic model was applied to represent the response relationship between the process parameters and the optimization objectives of the studied gear. The RSM-Quadratic coefficients of the optimization objectives are shown in Table 6.

Accuracy (%) **Approximation Surrogate Model**  $Y_1$  $Y_2$  $Y_3$  $Y_4$ 94.734 Kriging 81.693 93.985 90.850 RBF 94.638 87.661 95.089 91.870 RSM-Linear 67.662 52.482 74.930 80.850 98.229 RSM-Quadratic 92.838 98.031 94.562 **RSM-Cubic** 92.037 97.856 95.086 98.151 **RSM-Quartet** 98.015 91.609 97.660 94.590

**Table 6.** The accuracy of the Kriging models, RBF models, and the RSM-Linear, RSM-Quadratic, RSM-Cubic and RSM-Quartet models.

Therefore, the following RSM-Quadratic model was employed to represent the relationship between the input factors and the responses:

$$f = a_0 + \sum_{i=1}^k a_i x_i + \sum_{i=1}^k a_{ii} x_i^2 + \sum_{i=j}^k a_{ij} x_i x_j, i < j$$
(4)

where *f* is the output response,  $a_i = 0, 1, ..., k$  are coefficients of regression, and  $x_i, i = 0, 1, ..., k$  are input factors. The RSM-Quadratic coefficients of the optimization objectives are shown in Table 7.

The significance of the RSM-Quadratic coefficients was evaluated, as shown in Table 8. The *p*-value for  $Y_1$ ,  $Y_2$ ,  $Y_3$ , and  $Y_4$ , as a function of  $D^2$ , was 0.000. Therefore, besides *A*, *B*, *C* and *D*, there was a strong interaction between *D* and *D*. To simplify the RSM-Quadratic, only *A*, *B*, *C*, *D*, *E* and  $D^2$  were considered in the regression equations for the optimization objectives. The regression equations for  $Y_1$ ,  $Y_2$ ,  $Y_3$ , and  $Y_4$  are Equations (5)–(8).

$$Y_1(mm) = 0.37925 - 0.00094A - 0.00116B - 0.00445C - 0.01898D + 0.00024D^2$$
(5)

$$Y_2(\%) = 33.06385 - 0.26211A - 0.10297B - 0.03879C - 1.97750D + 0.42343D^2$$
(6)

$Y_3(\%) = 14.13387 - 0.02770A - 004364B - 0.00744C - 0.81237D + 0.07602E$	$)^2$ (7)
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$$Y_4(\%) = 11.46747 - 0.04402A - 0.04514B - 0.08270C - 0.59975D + 0.03973D^2$$
(8)

Table 7. RSM-Quadratic coefficient table.

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Polynomial Term	$Y_1$	<i>Y</i> <sub>2</sub>	<i>Y</i> <sub>3</sub>	$Y_4$
Constant	0.37925	33.06385	14.13387	11.46747
Α	-0.00094	-0.26211	-0.02770	-0.04402
В	-0.00116	-0.10297	-0.04364	-0.04514
С	-0.00445	0.03879	-0.00744	0.08270
D	-0.01898	-1.97750	-0.81237	-0.59975
Ε	0.00018	0.01842	0.02115	0.03480
$A^2$	1.12500	0.00029	0.00003	-0.00002
$B^2$	1.29167	0.00011	0.00006	0.00005
$C^2$	-1.16667	-0.00150	-0.00012	-0.00049
$D^2$	0.00024	0.42343	0.07602	0.03973
$E^2$	0.00000	-0.00123	2.66667	0.00009
AB	0.00000	0.00094	0.00008	0.00023
AC	0.00000	0.00051	0.00011	-0.00003
AD	0.00000	-0.00019	0.00216	0.00186
AE	0.00000	0.00000	0.00002	0.00009
BC	0.00000	0.00057	0.00007	-0.00003
BD	0.00000	-0.00487	0.00057	0.00143
BE	0.00000	0.00015	-0.00009	-0.00006
CD	0.00000	-0.00638	-0.00273	-0.00399
CE	0.00000	-3.73429	-0.00009	-0.00034
DE	0.00000	-2.61961	0.00023	-0.00086

**Table 8.** The estimated regression coefficients for  $Y_1$ ,  $Y_2$ ,  $Y_3$ , and  $Y_4$ .

Polynomial Tarm	<i>p</i> -Value						
r orynomiai term	<i>Y</i> <sub>1</sub>	<i>Y</i> <sub>2</sub>	<i>Y</i> <sub>3</sub>	$Y_4$			
Constant	0.000	0.000	0.000	0.000			
Α	0.000	0.001	0.000	0.000			
В	0.000	0.000	0.000	0.000			
С	0.000	0.006	0.000	0.000			
D	0.000	0.000	0.000	0.000			
Ε	0.736	0.936	0.567	0.837			
$A^2$	0.143	0.371	0.468	0.649			
$B^2$	0.095	0.726	0.124	0.292			
$C^2$	0.699	0.245	0.440	0.015			
$D^2$	0.000	0.000	0.000	0.000			
$E^2$	0.978	0.338	0.869	0.649			
AB	0.002	0.053	0.188	0.003			
AC	0.736	0.586	0.343	1.000			
AD	0.015	0.968	0.001	0.012			
AE	0.822	1.000	0.848	0.538			
BC	0.343	0.541	0.567	0.837			
BD	0.736	0.304	0.343	0.048			
BE	0.866	0.873	0.447	0.681			
CD	0.012	0.499	0.029	0.007			
CE	0.822	1.000	0.702	0.223			
DE	0.955	1.000	0.848	0.538			

Figure 9 shows the error analysis results of the RSM-Quadratic of the Gaussian spatial correlation function. The abscissa is the predicted value of the RSM-Quadratic and the ordinate is the actual measured value. The blue horizontal line is the average response value of the model, and the white background indicates that the model has high accuracy. The black line with a slope of 1 represents the ideal model. The closer the red dot is to the black slash, the more accurate and representative the surrogate model is. The red dots in the figure are evenly distributed on both sides of the black line and are very close. This indicates that the fitting accuracy of the RSM-Quadratic established in this study was very high. Therefore, the RSM-Quadratic established in this study can be used to predict the shrinkage of the studied gear micro-injection molding. It will save time spent on multiple Moldflow simulation attempts.



**Figure 9.** Residual analysis diagram of each response target of the RSM-Quadratic. (a) Maximum shrinkage ( $Y_1$ ). (b) Volume shrinkage ( $Y_2$ ). (c) Addendum diameter shrinkage ( $Y_3$ ). (d) Root circle diameter shrinkage ( $Y_4$ ).

Then, the main effect diagram and variance analysis were used to analyze the influence of the process parameters on the optimization objectives. The main effect diagram is shown in Figure 10. Figure 10a,c,d are the main effect diagrams of maximum shrinkage, addendum diameter shrinkage and root circle diameter shrinkage, respectively. It was found that there was a positive correlation between the mold temperature and the maximum shrinkage, the addendum diameter shrinkage and the root circle diameter shrinkage. However, there was a negative correlation between the melt temperature, packing pressure and packing pressure and the maximum shrinkage, addendum diameter shrinkage and root circle diameter shrinkage. The maximum shrinkage, addendum diameter shrinkage and root circle diameter shrinkage increased first and then decreased with increase in cooling time. Figure 10b is the main effect diagram of the volume shrinkage. It can be seen that the



volume shrinkage of the studied gear first increased and then decreased with increase in the packing pressure.

**Figure 10.** Main effect diagram: (a) Maximum shrinkage  $(Y_1)$ . (b) Volume shrinkage  $(Y_2)$ . (c) Addendum diameter shrinkage  $(Y_3)$ . (d) Root circle diameter shrinkage  $(Y_4)$ .

Table 9 is the variance analysis table of the maximum shrinkage in which the contribution ratio of the mold temperature and the dwell time is shown to be 5.05% and 81.61%. Table 10 is the variance analysis table of volume shrinkage in which the contribution ratio of the melt temperature and packing time is shown to be 13.68% and 73.71%. Table 11 is the variance analysis table of the addendum diameter shrinkage in which the contribution ratio of the mold temperature and the packing time is shown to be 7.99% and 80.59%. Table 12 is the variance analysis table of root circle diameter shrinkage in which the contribution ratio of the mold temperature and the packing time is shown to be 9.81% and 75.44%. Therefore, it can be concluded that the packing pressure had the greatest influence on the non-linear shrinkage of the small-module plastic gears.

Source	DF	Sum of Squares	Mean Square	F-Value	<i>p</i> -Value	Contribution (%)
Α	2	0.000183	0.000092	78.80	0.000	5.05
В	2	0.000166	0.000083	71.14	0.000	4.58
С	2	0.000146	0.000073	62.71	0.000	4.03
D	2	0.002958	0.001479	1271.16	0.000	81.62
E	2	0.000000	0.000000	0.04	0.962	0.00
Error	35	0.000041	0.000001			
Total	45	0.003624				

Table 9. ANOVA for maximum shrinkage.

Source	DF	Sum of Squares	Mean Square	F-Value	<i>p</i> -Value	Contribution (%)
A	2	2.012	1.0060	8.12	0.001	1.87
В	2	14.744	7.3719	59.53	0.000	13.68
С	2	1.450	0.7248	5.85	0.006	1.35
D	2	79.427	39.7137	320.71	0.000	73.71
Е	2	0.133	0.0664	0.54	0.590	0.12
Error	35	4.334	0.1238			
Total	45	107.751				

Table 10. ANOVA for volume shrinkage.

Table 11. ANOVA for addendum diameter shrinkage.

Source	DF	Sum of Squares	Mean Square	F-Value	<i>p</i> -Value	Contribution (%)
Α	2	0.47856	0.23928	77.67	0.000	7.99
В	2	0.23341	0.11671	37.88	0.000	3.90
С	2	0.20798	0.10399	33.75	0.000	3.47
D	2	4.82563	2.41281	783.21	0.000	80.59
Е	2	0.00081	0.00040	0.13	0.878	0.01
Error	35	0.10782	0.00308			
Total	45	5.98814				

Table 12. ANOVA for root circle diameter shrinkage.

Source	DF	Sum of Squares	Mean Square	F-Value	<i>p</i> -Value	Contribution (%)
А	2	0.39574	0.19787	39.07	0.000	9.81
В	2	0.15007	0.07504	14.82	0.000	3.72
С	2	0.19460	0.09730	19.21	0.000	4.82
D	2	3.04317	1.52158	300.43	0.000	75.44
E	2	0.00077	0.00039	0.08	0.927	0.02
Error	35	0.10782	0.00308			
Total	45	4.03381				

Then, the interactive effects of the micro-injection molding process parameters on the shrinkage of the small-module plastic gears was further investigated. The interaction effect plots for the maximum shrinkage ( $Y_1$ ), volume shrinkage ( $Y_2$ ), addendum diameter shrinkage ( $Y_3$ ) and root circle diameter shrinkage ( $Y_4$ ) were obtained, as shown in Figure 11. If the two straight lines are not parallel or intersect, there is an interaction effect between the process parameters; the greater the degree of non-parallelism, the stronger the interaction effect. It can be seen that there was a large interaction between the process parameters, so the optimal combination of process parameters cannot be determined using a traditional single factor design.

# 3.3. NSGA-II Algorithm Optimization Results

The optimal process parameters obtained by NSGA-II were a mold temperature of 61.44 °C, a melt temperature of 193.64 °C, a packing pressure of 79.84 MPa, a packing time of 4.48 s and a cooling time of 20 s. Figure 12 shows the simulation results under the optimal parameters. The maximum shrinkage of the studied gear was 0.1400 mm (Figure 12a), which was reduced by 5.60% compared to the shrinkage of the gear under the reference process parameters. The volume shrinkage of the studied gear was 12.38% (Figure 12b), which was reduced by 8.23% compared to the shrinkage of gear under the reference process parameters. The addendum diameter shrinkage ( $Y_3$ ) and root circle diameter shrinkage ( $Y_4$ ) calculated according to Figure 12c were 5.618% and 5.762%, which were reduced by 11.71% and 11.39%, respectively. Compared with the optimization objectives predicted by



the approximate surrogate models, the relative errors were all less than 5%, as shown in Table 13.

**Figure 11.** Interaction effect plot: (a) Maximum shrinkage  $(Y_1)$ . (b) Volume shrinkage  $(Y_2)$ . (c) Addendum diameter shrinkage  $(Y_3)$ . (d) Root circle diameter shrinkage  $(Y_4)$ .



**Figure 12.** Simulation results under the optimal parameters. (**a**) Shrinkage cloud diagram. (**b**) Volume shrinkage. (**c**) Addendum diameter and root circle diameter.

	Y <sub>1</sub> (mm)	Y <sub>2</sub> (%)	Y <sub>3</sub> (%)	Y <sub>4</sub> (%)
Prediction	0.1409	11.92	5.631	5.885
Actual	0.1400	12.38	5.618	5.762
Error (%)	0.643	3.715	0.231	2.134

Table 13. Simulation results and prediction results.

#### 3.4. Optimization Method Validation

The measurement results for the key dimension shrinkage of the gear samples in the micro-injection molding experiment under reference and optimal process parameters are shown in Figure 13a. It was found that the addendum diameter shrinkage ( $Y_3$ ) and the root circle diameter shrinkage ( $Y_4$ ) decreased by 9.44% and 9.91%, respectively. Moreover, the tooth profile inclination deviation ( $f_{H\alpha T}$ ), tooth profile deviation ( $f_{f\alpha T}$ ) and total tooth profile deviation ( $F_{\alpha T}$ ) were reduced by 47.57%, 23.43%, and 49.96%, respectively (Figure 13b). Figure 13c shows the tooth profile deviation curve of the gear sample with the highest tooth profile accuracy under optimal process parameters. It can be seen that the deviation near the addendum circle and the root circle was larger, while the deviation near the graduation circle was smaller, which was also close to the simulation results. Consequently, the tooth profile accuracy of the small-module plastic gears could be significantly improved using the proposed method.



**Figure 13.** (a) Key dimensions' shrinkage in the experiment under optimal process parameters. (b) Optimization results of tooth profile accuracy. (c) Tooth profile deviation curve of gear sample with the highest tooth profile accuracy under optimal parameters.

### 4. Conclusions

In summary, this paper has proposed an effective method to improve the tooth profile accuracy of micro-injection molded small-module plastic gears. First, based on the Box–Behnken design method, a simulation of the micro-injection molding of the studied gear was carried out. Next, the response relationship between the process parameters and the optimization objectives was analyzed using the RSM-Quadratic. The optimization objectives were non-normalized optimized using the NSGA-II algorithm. Finally, an experimental analysis of the micro-injection molding of the studied gear was carried out under reference and optimal process parameters to verify the optimization method. The main conclusions of this study are as follows.

- 1. The shrinkage of the gear was different at different positions. The tooth part of the gear shrank the most. Moreover, the shrinkage degree near the addendum and the root circle of the small-module plastic gear was the largest. The relative errors of the key dimension shrinkage between the micro-injection molding experiment and simulation were all less than 2%.
- 2. The factor that had the greatest influence on the shrinkage of the small-module plastic gears was the packing time, and there was a complex interaction between the process parameters. The accuracy of the RSM-Quadratic for the optimization objectives reached more than 92 %.
- 3. The simulation results showed that the  $Y_1$ ,  $Y_2$ ,  $Y_3$ , and  $Y_4$  values of the studied gear were reduced by 5.60%, 8.23%, 11.71%, and 11.39%, respectively. Moreover, the tooth profile inclination deviation ( $f_{H\alpha T}$ ), tooth profile deviation ( $f_{f\alpha T}$ ) and total tooth profile deviation ( $F_{\alpha T}$ ) were reduced by 47.57%, 23.43%, and 49.96%, respectively.

**Author Contributions:** Conceptualization, W.W.; data curation and formal analysis, X.H.; methodology, X.H. and Z.S.; investigation, X.H. and B.L.; writing—original draft, X.H. and W.W.; writing review and editing, W.W.; supervision, W.W.; project administration, W.W.; funding acquisition, W.W.; resources, W.W. All authors have read and agreed to the published version of the manuscript.

**Funding:** This research was funded by [National Key Research and Development Program of China] grant number [2020YFB2008200], [National Natural Science Foundation of China] grant number [51875582], [Huxiang Young Talents Program] grant number [2019RS2003], and [Graduate Research and Innovation Project of Central South University] grant number [2022ZZTS0787].

Institutional Review Board Statement: Not applicable.

Informed Consent Statement: Not applicable.

Data Availability Statement: Not applicable.

Acknowledgments: The authors would like to acknowledge the financial support from the National Key Research and Development Program of China, grant number 2020YFB2008200; the National Natural Science Foundation of China, grant number 51875582; the Huxiang Young Talents Program, grant number 2019RS2003; and the Graduate Research and Innovation Project of Central South University, grant number 2022ZZTS0787. The helpful comments of anonymous reviewers are gratefully acknowledged.

**Conflicts of Interest:** The authors declare that they have no known competing financial interest or personal relationships that could have appeared to influence the work reported in this paper.

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