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Competition of Several Energy-Transport Initiation Mechanisms Defines the Ballistic Transport Speed

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ABSTRACT: The ballistic regime of vibrational energy transport in oligomeric molecular chains occurs with a constant, often high, transport speed and high efficiency. Such a transport regime can be initiated by exciting a chain end group with a mid-infrared (IR) photon. To better understand the wavepacket formation process, two chemically identical end groups, azido groups with normal, ¹⁴N₃-, and isotopically substituted, ¹⁵N₃-, nitrogen atoms, were tested for wavepacket initiation in compounds with alkyl chains of n = 5, 10, and 15 methylene units terminated with a carboxylic acid (-a) group, denoted as ¹⁴N₃Cn-a and ¹⁵N₃Cn-a. The transport was initiated by exciting the azido moiety stretching mode, the $\nu_{N\equiv N}$ tag, at 2100 cm⁻¹ (¹⁴N₃Cn-a) or 2031 cm⁻¹ (¹⁵N₃Cn-a). Opposite to the expectation, the ballistic transport speed was found to



decrease upon ${}^{14}N_3 \rightarrow {}^{15}N_3$ isotope editing. Three mechanisms of the transport initiation of a vibrational wavepacket are described and analyzed. The first mechanism involves the direct formation of a wavepacket via excitation with IR photons of several strong Fermi resonances of the tag mode with the $\nu_{N=N} + \nu_{N-C}$ combination state while each of the combination state components is mixed with delocalized chain states. The second mechanism relies on the vibrational relaxation of an end-group-localized tag into a mostly localized end-group state that is strongly coupled to multiple delocalized states of a chain band. Harmonic mixing of $\nu_{N=N}$ of the azido group with CH₂ wagging states of the chain permits a wavepacket formation within a portion of the wagging band, suggesting a fast transport speed. The third mechanism involves the vibrational relaxation of an end-group-localized mode into chain states. Two such pathways were found for the $\nu_{N\equiv N}$ initiation: The $\nu_{N=N}$ mode relaxes efficiently into the twisting band states and low-frequency acoustic modes, and the $\nu_{\rm N-C}$ mode relaxes into the rocking band states and low-frequency acoustic modes. The contributions of the three initiation mechanisms in the ballistic energy transport initiated by $\nu_{N\equiv N}$ tag are quantitatively evaluated and related to the experiment. We conclude that the third mechanism dominates the transport in alkane chains of 5-15 methylene units initiated with the $\nu_{N\equiv N}$ tag and the wavepacket generated predominantly at the CH₂ twisting band. The isotope effect of the transport speed is attributed to a larger contribution of the faster wavepackets for ${}^{14}N_3Cn$ -a or to the different breadth of the wavepacket within the twisting band. The study offers a systematic description of different transport initiation mechanisms and discusses the requirements and features of each mechanism. Such analysis will be useful for designing novel materials for energy management.

1. INTRODUCTION

Ballistic energy transport via acoustic phonons is prevalent in ordered materials such as crystals and can occur to large distances. The amount of energy transferred via wavepackets made of acoustic phonons is limited by the thermal energy, $k_{\rm B}T$, which is too small to significantly influence chemical processes. In recent studies, ballistic energy transport via covalent bonds of linear oligomeric chains was discovered to occur via optical chain bands, thus delivering substantially larger energy quanta to distances exceeding 60 Å¹⁻⁴ and featuring much higher efficiency compared with that in diffusive energy transport.⁵⁻⁸ Oligomeric chains feature a range of chain bands differing in energy and bandwidth. The bandwidth of a chain band determines the mean group velocity of the wavepacket supported by the band.⁹ The ballistic through-chain transport was initiated via excitation with a mid-IR photon, a vibrational mode at the end group, which then transferred its energy into the chain, initiating the transport. The energies of the end-group modes tested for ballistic transport range from 2100 cm⁻¹ (azido group stretch)¹ to 1650-1750 cm⁻¹ (carbonyl groups in carboxylic acid, ester,

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succinimide ester, and amide),^{9,10} 1500 cm⁻¹ (amide II mode of an amide),¹⁰ and ~1300 cm⁻¹ (azido group stretch).⁹ It was found that the selection of the end-group mode used to initiate the transport determines which chain band transfers energy, thus determining the transport speed and efficiency. For example, ballistic transport via alkane chains, initiated by an azido-group stretching mode at 2100 cm⁻¹, occurs with a speed of 14.5 Å/ps (1.45 km/s), whereas the speed is 8.0 Å/ps when initiated by a carbonyl stretching mode at 1710–1820 cm⁻¹⁹ and only 4.2 Å/ps when initiated with the amide-I mode of an amide end group.¹⁰ Previous reports by the Troe^{11,12} and Dlott^{13,14} groups indicated the presence of ballistic transport via alkane chains.

Although ballistic transport was reported via several oligomeric chains, PEG,¹⁵ alkane,^{9,12} perfluoroalkane,¹⁶ and *p*-phenylene,¹⁷ the transport initiation mechanisms were not discussed systematically. At the same time, the central role of the transport initiation process became apparent, as the endgroup properties define which band or portion of the band is involved in the through-chain transport, thus defining the transport speed and efficiency. This study is inspired by the interest in designing molecular systems with faster and more efficient energy transport. Such systems have high potential as novel materials suitable for energy management, for delivering energy to remote regions, including energy transport against a thermal gradient, and as materials for molecular electronics. The energy quanta delivered via optical chain bands are large enough to be used for remotely initiating low-barrier chemical reactions. Approaches to direct and alternate ballistic transport by external stimuli^{10,17} may result in creating energy-transport switches.

Instead of changing the nature of the end group, drastically changing its properties, in this study, we vary the frequency of the end-group vibrational mode via isotope editing of the end-group atoms, ${}^{14}N_3 \rightarrow {}^{15}N_3 -$, targeting different portions of the alkane chain bands and thus expecting different transport speeds. Using the previously reported dispersion curves for alkane chains (Figure S2A in the Supporting Information (SI)),⁹ a higher transport speed was expected for the ${}^{15}N_3 -$ initiation.

The Article reports the experimental results of energy transport via linear alkyl chains of 5, 10, and 15 methylene groups terminated with an isotopically edited azido group and a carboxylic acid group, ${}^{15}N_3Cn$ -a (Section 3.1). The experiments were performed using relaxation-assisted twodimensional infrared (RA 2DIR) spectroscopy, where the excess energy arrival from the initially excited end-group mode (tag) to the site of the end group at the opposite chain end (reporter) was recorded as a time dependence of the tagreporter cross-peak amplitude.⁷ A systematic description of the ballistic transport initiation mechanisms is given in Section 3.2. Sections 3.3-3.6 discuss different mechanisms of transport initiation in N₃Cn-a, describing vibrational relaxation pathways of the tag and its relaxation daughter modes and the coupling strength among the end-group and chain states. In the Discussion section, we compare different mechanisms of transport initiation, offering strategies to design compounds to achieve high efficiency of energy delivery and high transport speed.

2. EXPERIMENTAL DETAILS

2.1. 2DIR Measurements. A comprehensive description of a fully automated dual-frequency three-pulse echo 2DIR

instrument with heterodyne detection is presented elsewhere.¹⁸ In brief, a Ti:sapphire laser producing 1.5 W power at 1 kHz repetition rate, 800 nm wavelength, and 80 fs pulse duration (Libra, Coherent) was used to pump a computercontrolled dual optical parametric amplifier (OPA, Palitra-duo, Quantronix). Two pairs of signal and idler pulses generated by the OPA were directed to two computer-controlled difference frequency generation (DFG) units (NIR Quantronix) to generate mid-IR pulses tunable in the frequency range from 500 to 5000 cm^{-1} , featuring a pulse energy ranging from 1.0 to 10 μ J. A fully automated 2DIR instrument features a sensitivity of better than 10^{-4} cm⁻¹ in measured anharmonicities, which is achieved by a combination of a closed-loop phase stabilization of better than 70 as, phase cycling, and spectral interferometry. The automatic frequency tuning from 800 to 4000 cm^{-1} is achieved by implementing a mid-IR beam direction stabilization schematic (<50 μ rad deviations)¹⁹ and a schematic for setting the phase-matching geometry for mid-IR beams at the sample.¹⁸ The spectral width of the mid-IR pulses was ~150 cm⁻¹, and the instrument response function was ~140 fs. The 2DIR measurements were performed by scanning the delay between the first two mid-IR pulses τ of the same DFG unit at a fixed waiting time T, which is the delay between the second and third pulses, and recording the heterodyned spectrum in the frequency range of interest $(\lambda \rightarrow \omega_t)$ for every τ . Fourier transformation along τ results in the ω_{τ} axis in the 2DIR spectrum, shown as the ordinate. A typical 2DIR spectrum contained ~250 points along the τ direction and took 1–3 min to acquire. For the RA 2DIR measurements, the 2DIR spectra were recorded for each waiting time, which was scanned with nonconstant delay steps ranging from 100 fs at small waiting times up to 5 ps at large waiting times. Typical waiting-time dependences contain 40-50 points along T, which take 1 to 2 h to acquire.

2.2. Sample Preparation. A series of compounds featuring an isotopically edited azido end group, an alkyl chain of three lengths of n = 5, 10, and 15, and a carboxylic-acid-terminating moiety, denoted as ${}^{15}N_3Cn$ -a (Figure 1A), were prepared according to the procedure previously reported for ${}^{14}N_3Cn$ -a, except isotopically labeled sodium azide (Na ${}^{15}N_3$, 97% ${}^{15}N$, Berry & Associates/ICON Isotopes) was used as the reagent.² Fourier transform infrared (FTIR) and 2DIR measurements of N₃Cn-a compounds dissolved in CDCl₃ were performed in a sample cell made of 1 mm thick CaF₂ windows and a 50 μ m Teflon spacer at room temperature, 22 \pm 0.5 °C.

2.3. Density Functional Theory Calculations. Density functional theory (DFT) calculations were performed using the Gaussian 09 suite. Geometry optimization, vibrational mode analysis, and anharmonicity calculations were executed using the B3LYP functional and the 6-311+G(d,p) basis set in dichloromethane (DCM) solvent described with a polarized continuum model (PCM) method. Vibrational relaxation pathways of the end-group states were computed using the theoretical approach reported in refs 20 and 21. The method uses DFT-computed anharmonic coupling constants of an isolated molecule to compute third-order relaxation pathways. The relaxation pathways from several excited azido-group states were performed for compounds with n = 1 and 5 and terminated with a hydrogen atom of 2000 amu instead of the carboxylic acid moiety, denoted as ${}^{15}N_3Cn$ and ${}^{14}N_3Cn$.

Vibrational couplings between the modes of the azido moiety and chain states were evaluated for both ${\rm ^{14}N_3C}n$ and



Figure 1. (A) Molecular structure of the used compounds. (B) Linear absorption spectra of the ¹⁵N₃C5-a, ¹⁵N₃C10-a, ¹⁵N₃C15-a, and ¹⁴N₃C5-a in CDCl₃, normalized for the carbonyl peak at $\nu_{C=O}$ at ca. 1709 cm⁻¹. Two azido-group vibrational modes denoted as $\nu_{N\equiv N}$ (2100 cm⁻¹ in ¹⁴N₃C*n*-a and 2031 cm⁻¹ in ¹⁵N₃C*n*-a) and $\nu_{N=N}$ (~1250 cm⁻¹) are labeled. The inset shows the $\nu_{N\equiv N}$ difference spectrum ¹⁵N₃C5-a – ¹⁴N₃C5-a and its fit with two Gaussian functions. (C) 2DIR spectrum showing the $\nu_{N\equiv N}/\nu_{C=O}$ cross-peak for ¹⁵N₃C15-a at *T* = 3.1 ps. (D,E) Waiting-time dependences for the $\nu_{N\equiv N}/\nu_{C=O}$ cross-peak for (D) ¹⁴N₃C*n*-a² and (E) ¹⁵N₃C*n*-a for *n* = 5, 10, and 15. Notice that the graphs are spaced vertically, and zero horizontal lines are shown with matching colors. Fitting curves with an asymmetric double-sigmoidal function are shown with red lines.

¹⁵N₃*Cn* compounds with n = 1 and 5 using the previously reported approach where the atomic masses of the end-group atoms are smoothly changed, causing the end-group frequency change, and the Hessian matrix is diagonalized for each mass point.⁹ As the end-group frequency passes the resonance with a chain state, a frequency jump occurs that is equal to 2β , where β is the interaction energy of the end-group and the chain state.⁹

3. RESULTS

3.1. 2DIR Measurements of the Energy Transport. Both high-frequency modes of the azido moiety, denoted as $\nu_{N\equiv N}$ and $\nu_{N=N}$, are significantly affected by the ${}^{14}N_3 \rightarrow {}^{15}N_3 -$ isotope editing. (See Section S1 in the SI.) The frequency of the $\nu_{N\equiv N}$ mode, found at 2100 cm⁻¹ in ${}^{14}N_3Cn$ -a, is red-shifted in $^{15}N_3Cn$ -a by 69.2 cm⁻¹ (Figure 1B). The frequency of the N=N mode, found at ca. 1270 cm⁻¹ in $^{14}N_3Cn$ -a, is also red-shifted in $^{15}N_3Cn$ -a by ca. 45 cm⁻¹ (Figure 1B, inset).

2DIR cross-peak spectra, focusing at the $\nu_{N\equiv N}/\nu_{C=O}$ crosspeak, were measured for ¹⁵N₃Cn-a by tuning the first two IR pulses to excite the $\nu_{N\equiv N}$ tag mode at 2031 cm⁻¹ and the third and local oscillator (LO) pulses to access the $\nu_{\rm C=O}$ reporter mode at 1709 cm^{-1} (Figure 1C). The cross-peak spectra were measured for a range of waiting times, T, and waiting-time kinetics were constructed by integrating the 2DIR spectra over the cross-peak area and plotting the resulting amplitude as a function of the waiting time (Figure 1E). The results for ¹⁴N₃Cn-a are shown in Figure 1D, reported in ref 2. The traces show a rise with an increase in the waiting time associated with the energy transport from the tag to the reporter site. The maximum in the kinetic trace, occurring at T_{max} corresponds to the maximum energy delivered; the following decrease in the cross-peak amplitude is associated with the cooling of the reporter site in the solvent, occurring with the characteristic time of ca. 14 ps. To determine the T_{max} value for each compound, the traces were fitted with an asymmetric doublesigmoidal function. (See Figure S1 in the SI for details.) Mean $T_{\rm max}$ values were determined by averaging three measurements per compound. (See Section S2 in the SI.) The resulting T_{max} values were plotted as a function of the through-bond chain length, determined as a sum of all C-C bond lengths of the chain (Figure 2A). The dependence was fitted with a linear function, and the transport speed, V, was evaluated as an inverse slope of the fit function. The energy-transport speed along the chain in ${}^{15}N_3Cn$ -a was found to be 11.0 \pm 1.5 Å/ps, which is slower than the 14.5 \pm 0.5 Å/ps reported for ¹⁴N₃Cna (Figure 1D).²

Note that this result is opposite to the prediction of a higher speed with ${}^{15}N_3$ - transport initiation. The expectation was based on the calculations in which $\nu_{N=N}$, a daughter mode of $\nu_{N\equiv N}$ relaxation, matched the portion of the dispersion curves of both the CH₂ wagging and twisting chain bands, which feature higher group velocities. (See Section S3 in the SI.)

It is also notable that longer $T_{\rm max}$ times are observed for ${}^{15}{\rm N}_{3}{\rm Cn}$ -a compared with ${}^{14}{\rm N}_{3}{\rm Cn}$ -a (Figure 2A); the $T_{\rm max}$ values obtained from linear extrapolation to zero chain length differ by ca. 0.5 ps. The increase in $T_{\rm max}$ suggests that the energy injection into the chain occurs slower in ${}^{15}{\rm N}_{3}{\rm Cn}$ -a.

The presence of different wavepackets featuring different speeds is expected for both isotopes. Faster moving wavepackets contribute the most at the rising portion of the waiting-time trace. To inspect the contributions of faster wavepackets, the transport speed was also evaluated based on the initial portion of the waiting-time traces, the $T_{0.8}$ values, determined as the time in which the trace reached the 0.8 fraction of its maximum amplitude (Figure 2B).^{17,22} The obtained speed is higher than the T_{max} -based speed (Figure 2B inset) by a factor of 1.6 to 1.8.

A theoretical analysis of the energy injection process was performed for both end groups. The analysis focused on the relaxation channels of the tag $(\nu_{N\equiv N})$ and its relaxation daughter modes $(\nu_{N=N} \text{ and } \nu_{N-C})$, coupling the daughter modes and the chain states, and Fermi resonances (FRs) of the tag. We first present a general description of different mechanisms of wavepacket initiation.

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Figure 2. (A) T_{max} and (B) $T_{0.8}$ values as a function of chain length for the two series of compounds, ¹⁴N₃Cn-a and ¹⁵N₃Cn-a, with n = 5, 10, and 15. Linear fit lines are shown in red, and the corresponding transport speeds obtained from the fits are shown in data-matching colors.

3.2. Mechanisms of Wavepacket Formation. Wavepacket initiation by an excited end-group-localized mode requires energy transfer from the end group to the chain states. Excitation of a single-exciton coherent superposition of chain states, a wavepacket, can occur directly from the excited tag mode or from the daughter modes of the tag relaxation. Different mechanisms of wavepacket excitation rely on different extents and orders of interaction between the end-group modes and the chain states, as shown in Figure 3.



Figure 3. Mechanisms of ballistic transport initiation by an excited end-group-localized vibrational mode. Magenta boxes indicate the couplings required for wavepacket initiation.

Without losing generality, we consider the tag that is endgroup-localized and frequency-isolated, so it is not harmonically mixed with any chain state. Nevertheless, the tag mode can be anharmonically coupled to other states via FRs. If a strong FR occurs among the tag and a combination band involving chain-band states, then the combination band will gain IR intensity through intensity borrowing from the tag (Figure 3A). It is possible to have multiple FRs involving a range of chain states, as reported for the azido end group.²³ Such combination bands can be directly excited with a photon and can, under certain conditions, form a wavepacket within the chain states.

Another mechanism of wavepacket formation involves vibrational relaxation of the tag into daughter states, at least one of which is strongly (harmonically) coupled to the chain states, $\beta_{end gr.}$ (Figure 3B). Strong coupling among a daughter mode and a few chain states results in their mixing. Vibrational relaxation, local in nature, excites, in this case, a superposition of delocalized chain states, such that they involve local motion at the sites nearest to the end group, a wavepacket. The spectral width of the wavepacket is defined by the coupling strength between the end-group daughter mode and the chain

state localized at the adjacent methylene site, $\beta_{\rm end\,gr./ch.}$ in relation to the coupling within the chain, $\beta_{\rm ch.}$. If the coupling strength is comparable to or larger than the chain bandwidth, $\beta_{\rm end\,gr.} \geq \beta_{\rm ch.}$ then all states of the band will be involved in the wavepacket. The transport speed of such a wavepacket corresponds to the mean speed of the chain band. If $\beta_{\rm end\,gr.} < \beta_{\rm ch.}$ only the chain states that are resonant with the end-group mode will participate in the wavepacket. Such a wavepacket will feature a group velocity that is characteristic of a specific portion on the chain band dispersion curve at the frequency of the chain state, not the mean speed supported by the whole band. The spatial size of any wavepacket is defined by the number of chain states involved in the superposition. For the cases with smaller $\beta_{\rm end\,gr./ch.}$ longer chains are required to achieve a spatially sharp wavepacket.

Another mechanism of wavepacket formation involves the vibrational relaxation of the end-group mode into chain states (Figure 3C). The local nature of the relaxation process is derived from the spatial proximity of the involved states for strong coupling.^{24–26} Therefore, strong anharmonic coupling of the end-group mode and the local mode at the first chain site is require for efficient relaxation. Anharmonically driven relaxation will excite a local chain mode, which represents a wavepacket on the basis of delocalized chain states. The strength of the anharmonic coupling determines the spectral width of the wavepacket and its spatial sharpness, similar to case B.

In the next section, we will consider the transport initiation with $\nu_{N\equiv N}$ in ${}^{14}N_3Cn$ -a and ${}^{15}N_3Cn$ -a to identify which mechanism is contributing the most. To identify the differences and similarities in the transport, computational results are presented for compounds with both isotopes. First, we consider a possibility of mechanism B, inspecting the relaxation pathways of the tag and the extent to which the daughter modes of the tag relaxation involve the chain states.

3.3. Vibrational Relaxation Pathways for the $\nu_{N\equiv N}$ **Tag.** We computed the rates of the intramolecular vibrational energy redistribution (IVR) pathways using a recently developed theoretical approach.^{20,21} To determine the vibrational frequencies and anharmonic force constants, DFT anharmonic computations were performed using the Gaussian-09 suite²⁷ for the ^{14/15}N₃-(CH₂)₅-²⁰⁰⁰H compounds, denoted as ¹⁴N₃C5 and ¹⁵N₃C5, where a large mass for the chain-terminating hydrogen was used to decouple its motion from other motions in the compounds. In agreement with previous reports for ¹⁴N₃- initiation,^{2,2,3} the $\nu_{N\equiv N}$ relaxation

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Figure 4. Relaxation pathways for the tag mode, $\nu_{N\equiv N}$, computed for (A) ¹⁴N₃C5 and (B) ¹⁵N₃C5. (C) $\nu_{N=N}$ mode frequency of ¹⁴N₃C5 (blue) and ¹⁵N₃C5 (green) as a function of the mass scaling factor for the N atoms of the azido group. Horizontal red lines show the frequencies of the wagging chain states. The inset shows the ν_{N-C} mode frequency as a function of the mass scaling factor, indicating its coupling to the rocking state at 815 cm⁻¹.

predominantly populates a combination band of modes $\nu_{\rm N=N}$ and $\nu_{\rm N-C}$ (Figure 4A,B), which accounts for >90% of all relaxation channels for both isotopes. To efficiently create a wavepacket in the chain upon the tag relaxation, the relaxation daughter states need to be harmonically mixed with more than one chain state of the same chain band (mechanism B). The $\nu_{\rm N=N}$ daughter state frequency matches the CH₂ wagging (W) and twisting (Tw) chain bands (Figure S2 in the SI), whereas $\nu_{\rm N-C}$ is located within the rocking (Ro) band (Figure S4 in the SI).

To evaluate the coupling strength of the $\nu_{N=N}$ mode with the wagging and twisting modes of the chain, we scanned the masses of the nitrogen atoms of the azido moiety in increments of 0.01 amu and computed the normal modes for every mass using the Hessian matrix obtained via DFT normal-mode analysis.⁹ When, as a result of mass change, the frequency of $\nu_{\rm N=N}$ passes that of the chain state, W or Tw, a jump of the mode predominantly residing on the azido group $(\nu_{N=N})$ occurs. The magnitude of the frequency jump is equal to $2\beta_{N=N/W}$ or $2\beta_{N=N/Twt}$ where β is the respective interaction energy. The computations performed for N₃C1 resulted in $\beta_{14N=N/W} = 10 \text{ cm}^{-1}$, $\beta_{15N=N/W} = 8.4 \text{ cm}^{-1}$, and $\beta_{N=N/TW} < 0.1$ cm⁻¹ for both isotopes. Similar results were obtained for N₃C5, although the observed coupling was different for different wagging states (Figure 4C) correlating with a contribution of the first methylene site in different wagging normal modes; this contribution is the highest at ca. $1/\sqrt{n}$ for the normal modes featuring the highest wave vectors, where n is the number of sites. Note that equal site contributions require cyclic boundary conditions.

Therefore, $\nu_{N=N}$ is harmonically mixed with wagging modes but only within a rather narrow resonance window of about $\pm 2\beta_{N=N/W}$. The pattern of $\nu_{N\equiv N}$ relaxation pathways confirms the result: In addition to the relaxation pathway to $\nu_{N=N}$ (Figure 4A), there is a pathway in ¹⁵N₃C5 to a single wagging state, which is shifted by ca. 15 cm⁻¹ from $\nu_{N=N}$, and two pathways in ¹⁵N₃C5 to wagging states that are shifted by ca. 25 cm⁻¹ from $\nu_{N=N}$. These pathways gain their efficiencies due to the mixing of $\nu_{N=N}$ with formalwagging states of the chain. Because the site energy gap is larger than $\beta_{N=N/W}$, the mixing is partial. The other wagging states of the chain are further away from $\nu_{N=N}$ and do not feature significant $\nu_{N=N}$ contributions. As a result of the small density of chain states in N₃C5, the $\nu_{\rm N\equiv N}$ relaxation mostly populates the end-grouplocalized $\nu_{N=N}$, although a small amplitude wavepacket is also created on the wagging states. The chain-state density increases with the increase in chain length. For the efficient formation of the wavepacket, at least two wagging states need to be found within the $2\beta_{N=N/W} \approx 20 \text{ cm}^{-1}$ window at the frequencies around $\nu_{\rm N=N}$. To satisfy this requirement, the chain length should be ca. 22 and 19 units long for normal and isotopically substituted compounds. Even for the longest experimentally assessed chain of N₃C15-a, two wagging states will not be efficiently excited via mechanism B, suggesting that the influence of such a wavepacket will likely be small for the overall energy-transport process. A rather high speed is expected for such a wavepacket, reaching 40 Å/ps for $^{14}N_3C5$, as the fastest portion of the wagging band will be involved, not the whole band. Essentially the same speed is predicted for ¹⁵N₃C5 for the wagging band constructed of either harmonic or anharmonic chain states. (See Section S3 in the SI.)

The coupling between $\nu_{\rm N-C}$ and the rocking band states, $\beta_{\rm N-C/Ro}$, evaluated in a similar way to $\beta_{\rm N=N/W}$, was found to be ~8 cm⁻¹ (Figure 4C, inset). The density of the rocking states at ca. 900 cm⁻¹ is the smallest within the band, corresponding to the highest group velocity of the rocking band, exceeding 65 Å/ps. To have two rocking states separated by $2\beta_{\rm N-C/Ro} \approx 16$ cm⁻¹ for their efficient mixing with $\nu_{\rm N-C}$, the chain should consist of 44 methylene units. The longest experimentally assessed chain, N₃C15-a, is almost three times shorter, which allows us to conclude that the formation of a wavepacket on rocking states via mechanism B in negligible for these chains. Therefore, the vibrational relaxation of $\nu_{\rm N=N}$ remains mostly local to the azido moiety and will not efficiently create a wavepacket on wagging, twisting, or rocking states via mechanism B.

Next, we consider relaxation pathways of the first-tier daughters, $\nu_{N=N}$ and ν_{N-C} , and the possibility of wavepacket formation via their relaxation into chain states (mechanism C).

3.4. Vibrational Relaxation Pathways of $\nu_{N=N}$. The $\nu_{N=N}$ mode lifetime, computed for both isotopes in N₃C5, is very short at 0.20 (¹⁴N) and 0.18 ps (¹⁵N). Three groups of daughter modes account for 95% of all pathways: all CH₂

The Journal of Physical Chemistry B Article pubs.acs.org/JPCB 0.8 1400 ¹⁴N₃C5 0.8 k-mode # $v_{N=N}$ relaxation ¹⁴N₃C5 С ¹⁵N₂C5 D k-mode # - 45 $v_{N=N}$ -**---** 45 Τw Τw 46 - 46 v_{N=N} 1300 0.6 0.6 48 - 48 Tw Wavenumber / cm⁻¹ 0071 0071 49 V_{N=N} 49 51 i -> j+k 51 Rate / ps⁻¹ Τw Rate / ps⁻¹ 5⁻¹ റ്ട 0 1 0 27% В ¹⁵N₂C5 28% Тν $v_{N=N}$ 1300 0.05 0.05 Τw i+k -> j -> i+k 1200 0.00 0.00 1200 1250 1300 1200 1250 1300 Twisting mode frequency / cm⁻¹ Twisting mode frequency / cm⁻¹ ດ່ດ 0.5 1.0 Rate / ps⁻¹

Figure 5. Relaxation pathways of the $\nu_{N=N}$ populating twisting modes of the chain, computed for (A) ¹⁴N₃C5 and (B) ¹⁵N₃C5. (See the complete set of data in Figure S5 in the SI.) Red horizontal lines show the position of $\nu_{N=N}$ for each isotope. (C,D) Individual relaxation channels populating the twisting band states for $i \rightarrow j + k$ and $i + k \rightarrow j$ processes, where *i* denotes $\nu_{N=N}$, *j*(*k*) denotes one of the twisting modes, and *k* is a low-frequency mode involved in the IVR step. The points for the same *k* values are connected. The frequencies of the *k* modes showing significant contributions are 25 (#51), 60 (#49), 81 (#48), 135 (#46), and 148 cm⁻¹ (#45).



Figure 6. All relaxation pathways of the ν_{N-C} mode for (A) ¹⁴N₃C5 and (B) ¹⁵N₃C5 (B). The majority of the pathways populate rocking modes of the chain (Ro). Red horizontal lines show the position of ν_{N-C} for each isotope. (C,D) Individual relaxation channels populating the rocking band states for $i \rightarrow j + k$ and $i + k \rightarrow j$ processes where *i* denotes ν_{N-C} , *j*(*k*) denotes one of the rocking modes, and *k* is a low-frequency mode involved in the IVR step. Points for the same *k* values are connected. The frequencies of the *k* modes showing significant contributions are 25 (#51), 60 (#49), 81 (#48), 135 (#46), and 148 cm⁻¹ (#45).

twisting modes (36.5 rate percent for ¹⁴N and 50 rate percent for ¹⁵N), NNN bending mode overtone, $\delta_{\rm NNN}$ (35% for ¹⁴N and 29% for ¹⁵N), and $\nu_{\rm N-C}$ (23% for ¹⁴N and 17% for ¹⁵N) (Figure S5 in the SI). The $\delta_{\rm NNN}$ mode frequency, ~600 cm⁻¹, is too low to populate any optical chain bands in the following relaxation process. The excitation of the $\nu_{\rm N-C}$ mode will be considered in the next section, as $\nu_{\rm N-C}$ is also a daughter mode of $\nu_{\rm N=N}$ relaxation.

The $\nu_{N=N}$ mode relaxation pathways populate multiple twisting chain states in ¹⁴N₃C5 and ¹⁵N₃C5, as shown in Figure 5A,B. Red horizontal lines show the location of the $\nu_{N=N}$ states for respective isotopes. Whereas all twisting states feature appreciable rates and the wavepacket formation seems possible, an additional requirement has to be satisfied to form a wavepacket rather than populating individual states with no specific phase relations characteristic of a wavepacket. The third-order relaxation process involves a parent mode ($\nu_{N=N'}$ mode *i*), one of the twisting modes (*j*), and a low-frequency mode (*k*). The relaxation process of mode *i* will create a wavepacket only if multiple chain states *j* become populated for the same mode k. On the contrary, if different k states are involved for different chain states *j*, then individual chain states will be excited, not a wavepacket. Five low-frequency k modes are involved in the relaxation process. Two of them, modes #49 and #51, result in the strongest rates across all twisting states (Figure 5C,D). These two decay channels are characterized by a sufficiently strong third-order interaction and involve all twisting chain states spread over a range of $>160 \text{ cm}^{-1}$ in frequency. Relaxation channels involving both low-frequency modes will generate wavepackets in the twisting bands. About 95% of all relaxation channels populate twistingband states for both ¹⁴N₃C5 and ¹⁵N₃C5 (Figure 5C,D), so the wavepacket formation is efficient. Essentially the whole twisting band is involved in the wavepacket, so the transport speed can be estimated as the mean group velocity for the band: $\langle V_{\rm gr} \rangle = \frac{a}{\pi} \int_0^{\pi/a} \frac{\partial \omega}{\partial q} \, \mathrm{d}q$, computed at 10.4 Å/ps (Figure S2 and Table S2 in the SI).

3.5. Vibrational Relaxation Pathways for ν_{N-C} . The $\nu_{\rm N-C}$ mode lifetime was computed at 0.78 ps for ¹⁴N₃C5 and 0.75 ps for ${}^{15}N_3C5$. The relaxation pathways predominantly involve the rocking states of the chain (Figure 6A,B), which account for 72.3 and 76.1 rate percent, respectively. Note that all rocking states are significantly populated, although not evenly. To check if a common relaxation process exists for each rocking mode and the same low-frequency mode, we analyzed individual third-order pathways of $\nu_{\rm N-C}$ relaxation, shown in Figure 6C,D. Five low-frequency modes (k = 45, 46, 48, 49, 51) are involved in the $i \rightarrow j + k$ and $i + k \rightarrow j$ processes, where i denotes ν_{N-C} and j is one of the rocking band states. The pathways involving k modes 45, 46, and 48 populate a single rocking state and cannot form a wavepacket. k modes 49 and 51 populate more than one rocking states and will form a wavepacket-localized chain excitation on the azido side.

The speed of such a wavepacket is expected to be extremely high at ca. 67 Å/ps, as the fast portion of the rocking band is involved (Table S2). Interestingly, the yield of the wavepacket formation with modes 51 and 49 is rather high, with 57 and 52% of all relaxation channels into rocking modes for $^{14}\mathrm{N}_3\mathrm{C5}$ and ¹⁵N₃C5, respectively. Despite the rather high predicted efficiency, such high speeds have not been clearly observed experimentally, possibly due to the following reasons: (1) A large spatial size of the wavepacket is expected as a small number of chain states is involved. A large wavepacket size will likely reduce the efficiency of its relaxation to the reporter site as its participation at the last chain site is diminished by broadening. Note, however, that the quality of the wavepacket will increase for longer chains, as more states will be covered by the strength of the involved nonlinear interaction, which is ca. 50 cm⁻¹. The rocking-state frequencies are low, which could result in their faster relaxation, although this is not confirmed experimentally. (2) It is difficult to experimentally tell apart such fast transport from a nonresonant signal appearing at $T \approx 0$ ps, especially if slower but more efficient transport pathways are present. Note that the time to pass a C15 chain for such a wavepacket is 0.35 ps, which is only two times longer than the instrument response time (Figure S6B in the SI) and is much smaller than the experimental T_{max} and even $T_{0.8}$ values (Figure 2B). The difference in the speeds determined from T_{max} and $T_{0.8}$ indicates the contributions of faster transport processes, which likely include the transport via the rocking band (Figure 2B). Note that other chain bands, such as $\nu_{\rm C-C}$ and scissoring, are found to be much less populated via the first two tiers of $\nu_{N\equiv N}$ relaxation and are not expected to participate in the energy transport initiated by

3.6. Wavepacket Formation via Direct Excitation of $\nu_{N\equiv N}$ Fermi Resonances (Mechanism A). The FR between the $\nu_{N\equiv N}$ fundamental and the combination band of $\nu_{N=N}$ and ν_{N-C} modes is strong, resulting in significant intensity borrowing. Moreover, the FRs were shown to be a major reason for a large $\nu_{N\equiv N}$ transition width, observed even in nonpolar solvents.²³ Both states of the combination state are involved in mixing with the chain states, wagging for $\nu_{N=N}$ and rocking for ν_{N-C} resulting in more than one FR. The mixing increases with the increase in chain length, and the number of FRs is expected to increase. The coupling of the $\nu_{N\equiv N}$ fundamental and the $\nu_{N=N} + \nu_{N-C}$ combination band, defined from anharmonic calculations with Gaussian 09, is ca. 30 cm⁻¹. This value is about three times larger than $\beta_{N=N/W}$ or $\beta_{N-C/Rov}$ thus providing no limitations for the mixing. Therefore, the

mixing of the $\nu_{N=N}$ and ν_{N-C} states with the chain states will determine the number of FRs for the tag. As long as the mixing with chain states occurs, the FR will be strong enough to bring IR intensity to combination bands via intensity borrowing. As a result, the wavepacket on wagging and rocking bands directly initiated by absorbing a photon will be required to satisfy the same density of chain-state conditions at $\nu_{N=N}$ and ν_{N-C} as the wavepackets following mechanism B. A similarly high transport speed is expected because only a portion of the chain bands will participate in the superposition. The key difference between mechanisms A and B is that a wavepacket via mechanism A is formed without a delay, whereas in mechanism B, the wavepacket is delayed by the lifetime of the tag. Calculations of the FRs, performed for the two isotopes (see Section S5 in the SI), did not reveal differences that could be related to the experimentally measured speeds reported here. Thus mechanism A of wavepacket initiation still requires experimental confirmation.

3.7. Classical Modeling of Ballistic Transport. Ballistic energy transport in N₃Cn-a was modeled by solving classical Newton's equations using DFT-determined harmonic force constants (Hessian). (See the details in Section S9 in the SI.) Note that harmonic approximation, unsuitable for intramolecular energy redistribution, is expected to work reasonably well for the wavepacket transport. The initial excitation at ca. 1300 cm⁻¹ was introduced by exciting a local $\nu_{\rm N=N}$ mode, the relaxation daughter of the $\nu_{N\equiv N}$ tag. Energy arrival to the reporter was monitored by summing all local energies of the carboxylic acid end-group atoms. In the absence of energy damping channels, an approximately periodic time dependence was obtained, as the excess energy is readily reflected from the chain ends (Figure 7A). The recurrency period, $t_{\rm R}$, corresponding to the energy round trip, is related to the transport speed as $V = 2L/t_{\rm R}$, where the chain length, L, was taken as $L = n \cdot l_{CC} + l_{NC}$. Here l_{CC} and l_{NC} are the CC and CN



Figure 7. COOH-group local energy versus time for (A) ¹⁴N₃C5-a, (B) ¹⁵N₃C5-a with infinite damping time, and (C) ¹⁴N₃C*n*-a with a damping time of 1.5 ps and n = 5, 10, 15. The color-matching arrows show the average arrival times, $t_{\rm D}$, calculated using eq S5 in the SI.

bond lengths, and n is the number of methylene units in the chain (n = 5, 10, 15).

A comparison of the transport speeds for ¹⁴N₃C5-a and ¹⁵N₃C5-a (Figure 7A,B) showed that the speed is smaller in ¹⁵N₃C5-a for all chain lengths (Table S5). The average speeds of 12 \pm 3 and 6 \pm 1.5 Å/ps were obtained for ¹⁴N₃C*n*-a and ¹⁵N₃C*n*-a, respectively. A damping factor, representing total dephasing of the chain states, was introduced to eliminate the energy arrival recurrencies. The transport speed was found to be somewhat affected by the value of the damping factor. For the damping factor of 1.5 ps (Figure 7C), a better match with the experimentally observed speeds was found with 13 and 10 Å/ps for ¹⁴N₃C*n*-a and ¹⁵N₃C*n*-a, respectively.

4. DISCUSSION

Figure 8 summarizes the findings for ballistic transport initiated with $\nu_{N\equiv N}$ in $^{14}N_3$ - and $^{15}N_3$ - end groups (values for $^{15}N_3$ - are



Figure 8. Mechanisms of ballistic transport initiation by the excited $\nu_{N\equiv N}$ end-group mode. The numbers indicate couplings, if in wavenumbers, lifetimes, if in picoseconds, and rate percent populating band states, if in percent. The values in parentheses computed for ¹⁵N₃C5 follow the values for ¹⁴N₃C5, unless the two values are within a few percent of each other.

shown in parentheses). Mechanism C is found to be contributing the most for both isotopes. The dominant wavepacket propagates via twisting band with the speed of ca. 10 Å/ps for both isotopes. A spatially broad wavepacket at rocking states is expected (mechanism C), propagating with an extremely high speed, exceeding 60 Å/ps. In addition, mechanisms A and B may contribute to ballistic transport via wagging band; the wavepacket is expected to be spatially broad and feature high speed of ca. 36 Å/ps (Section S3 in SI).

¹⁴N₃C5 and ¹⁵N₃C5 compounds show large similarities in the types of chain bands involved and in the group velocities expected for each band. Two hypotheses are proposed to account for the differences observed in the expriments. First, differences in the contributions of various involved wavepackets for the two isotopes determine the overall outcome faster $V_{T_{max}}$ speed for ¹⁴N₃Cn-a. Indeed, the formation of the dominant wavepacket on twisting band via mechanism C is more efficient for ¹⁵N₃Cn-a (Figure 8C). This wavepacket defines the $V_{T_{max}}$ speed in ¹⁵N₃Cn-a. Predicted at 10.4 Å/ps (Table S2 in the SI), the speed well matches the experimental value of 11.5 Å/ps in ¹⁵N₃Cn-a. The formation of such a wavepacket in ¹⁴N₃Cn-a is less efficient (Figure 8C), and faster wavepackets may affect the overall transport more significantly, resulting in faster T_{max} and $T_{0.8}$ speeds and smaller T_{max} values observed experimentally.

Alternatively, the slower transport speed in ${}^{15}N_{2}Cn$ -a may be due to a lower group velocity of the dominant wavepacket on the twisting band due to a larger involvement of higher energy states of the band. Such a statement sounds counterintuitive, as the $\nu_{N=N}$ frequency shifts down in ¹⁵N₃Cn-a. However, as a result of such a shift, the $\nu_{N=N}$ relaxation process in ${}^{14}N_3Cn$ -a occurs predominantly downhill $(i \rightarrow j + k)$, whereas there is a larger uphill contribution, $i + k \rightarrow j$ channels in $\nu_{N=N} \rightarrow Tw$ relaxation, in ¹⁵N₃Cn-a (Figure 5D). The efficiency of the uphill process linearly depends on the population of mode k. Compounds with a larger chain length feature lower frequencies of acoustic modes, which will be thermally populated to larger quantum numbers and offer increased rate contributions in $\nu_{\rm N=N} \rightarrow {\rm Tw}$ relaxation. At the same time, the twisting states involved in uphill relaxation correspond to the top of the twisting chain band and feature smaller local group velocity. Note that the downhill relaxation channels, $i \rightarrow i$ j + k, are less sensitive to the energy values of modes k, so their rates are not expected to change much for compounds with longer chains. We hypothesize that a significantly larger contribution of uphill relaxation channels in ¹⁵N₃C5 results in a smaller mean speed of the wavepacket on the twisting band. A significant difference in the $\nu_{N\equiv N}$ lifetime of ca. 0.4 ps was computed for ¹⁴N₃Cn-a (Figure 8A). However, experimentally measured lifetimes for the two isotopes did not support this prediction, showing similar lifetimes for the two isotopes (Figure S6 in the SI).

No significant mixing among $\nu_{N=N}$ and the twisting modes was found when the azido group was attached to the chain in an anti conformation, which is energetically favorable over the gauche conformation, but only by ca. 96 cm⁻¹. In the gauche conformation of the N₃ attachment, $\beta_{N=N/Tw}$ has similar values to $\beta_{N=N/W}$; both are ca. 10 cm⁻¹. Note that the anti kink at the azido-group side of the chain results in mixing of the identities of the delocalized chain states and the inability to assign them as purely wagging or twisting. The treatment of such less regular but still delocalized states will be considered elsewhere. Nevertheless, the mixing of $\nu_{N=N}$ is still small enough that (i) longer chains are required to form the wavepacket efficiently and (ii) the expected transport speed corresponds to that of the fast portion of the original wagging and twisting bands, which exceeds the experimentally observed speed by a few fold.

Chain-Initiator Design Considerations. The analysis of the transport initiation mechanisms in N_3Cn revealed that whereas there is a dominant initiation pathway for shorter chains (mechanism C on the twisting band), other mechanisms are expected to contribute more efficiently for longer chains. A higher density of chain states for longer chains is expected to result in a more efficient wavepacket formation on the wagging band via mechanisms B and A. Such a switch is expected for chain lengths exceeding $n \approx 30$ methylene units when at least two wagging state will be strongly coupled to $\nu_{N=N}$. The transport speed will change to that corresponding to a local $\frac{d\omega}{dq}$ derivative to the wagging band at the $\nu_{\rm N=N}$ frequency, which is ~36 Å/ps (Table S2). A further increase in the transport speed is expected for even longer compounds with n > 40 units, with a larger contribution of a wavepacket on rocking states with a speed $\left(\frac{d\omega}{da}\right)$ of ca. 68 Å/ps (Table S2).

Note also that it is advantageous to use only a portion of the chain band for a wavepacket, as such portions often feature almost a linear relation between the frequency and the wavevector, as is the case for the wagging and rocking bands at the positions of $\nu_{\rm N=N}$ and $\nu_{\rm N-C}$, respectively. If a linear relation between the frequency and wavevector is satisfied ($\omega \approx q + \text{constant}$), then the wavepacket will propagate without much broadening, similar to the propagation of a short laser pulse in a vacuum, $\omega = cq$, where *c* is the speed of light in a vacuum. On the contrary, a wavepacket broadening is expected with time if the whole chain band is involved in the wavepacket.²⁸

For 1D chains, chain-state localization is expected at some length, which will limit the coherence length for the wavepacket and thus the ballistic transport distance.^{29,30} Such localization will occur more readily for the states of narrow bands featuring smaller coupling among unit cells. The chain-state localization depends on intramolecular fluctuations as well as on interactions with the solvent.²² Intramolecular fluctuations include slow conformational variations, such as antigauche variations and fast thermal fluctuations. For broad alkane chain bands, such as wagging and rocking, the chain width exceeds by many fold the width of the inhomogeneous chain-site frequency distribution, which increases the length for chain-state localization. Further studies with longer compounds are required to understand the extent of the localization.

5. CONCLUSIONS

Different mechanisms of ballistic energy-transport initiation in oligomeric molecular chains are discussed and tested for transport initiation with $\nu_{\rm N\equiv N}$ excitation in ${}^{14}\rm{N}_3Cn$ -a and ${}^{15}\rm{N}_3Cn$ -a compounds. We concluded that the dominant mechanism of wavepacket formation in relatively short compounds with n = 5, 10, and 15 involves a two-step relaxation into the twisting band states (mechanism C). Whereas the wavepacket via twisting band dominates the transport, multiple wavepackets involving different optical chain bands and transport speeds are found for both ${}^{14}\rm{N}_3Cn$ -a and ${}^{15}\rm{N}_3Cn$ -a compounds. The difference in the speed for the two isotopes is linked to a larger contribution of fast wavepackets for ${}^{14}\rm{N}_3Cn$ -a.

We concluded that the density of chain states in the studied chains $(n \leq 15)$ is insufficient to induce efficient wavepackets at the wagging and rocking bands via mechanisms A and B. These mechanisms may become dominant for longer chains offering significantly faster speeds of ca. 36 Å/ps via wagging and ca. 60 Å/ps via rocking bands. The study provides tools for analyzing ballistic transport initiation mechanisms in different molecular systems, which can lead to the design of systems featuring efficient initiation and efficient through-chain transport.

The ballistic transport was initiated in this study with mid-IR photon absorption; however, if $\nu_{\rm N\equiv N}$ is excited by other means, such as thermally or as a result of electronic relaxation, its relaxation will initiate the same wavepackets in the chain as described here, rapidly transporting a significant portion of its energy to large distances along the alkane chain. Optimization of the energy injection and transport efficiencies can help in developing novel materials suitable for energy management and materials for molecular electronics.

ASSOCIATED CONTENT

Supporting Information

The Supporting Information is available free of charge at https://pubs.acs.org/doi/10.1021/acs.jpcb.1c03986.

Additional cross-peak data and details of their treatment, analysis of the FRs, dispersion curves for alkyl chains, lifetime data for $\nu_{N\equiv N}$, and vibrational relaxation pathways for ν_{N-C} (PDF)

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Notes

The authors declare no competing financial interest.

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