

# Frequency-dependent ecological interactions increase the prevalence and shape the distribution of pre-existing drug resistance

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## ABSTRACT

The evolution of resistance remains one of the primary challenges for modern medicine from infectious diseases to cancers. Many of these resistance-conferring mutations often carry a substantial fitness cost in the absence of treatment. As a result, we would expect these mutants to undergo purifying selection and be rapidly driven to extinction. Nevertheless, pre-existing resistance is frequently observed from drug-resistant malaria to targeted cancer therapies in non-small cell lung cancer (NSCLC) and melanoma. Solutions to this apparent paradox have taken several forms from spatial rescue to simple mutation supply arguments. Recently, in an evolved resistant NSCLC cell line, we found that frequency-dependent ecological interactions between ancestor and mutant ameliorate the cost of resistance in the absence of treatment. Here, we hypothesize that frequency-dependent ecological interactions in general may play a major role in the prevalence of pre-existing resistance. We combine numerical simulations with robust analytical approximations to provide a rigorous mathematical framework for studying the effects of frequency-dependent ecological interactions on the evolutionary dynamics of pre-existing resistance. First, we find that ecological interactions significantly expand the parameter regime under which we expect to observe pre-existing resistance. Even when positive ecological interactions between mutants and ancestors are rare, these clones provide the primary mode of evolved resistance because their positive interaction leads to significantly longer extinction times. Next, we find that even in the case where mutation supply is sufficient to predict pre-existing resistance, frequency-dependent ecological forces still contribute a strong evolutionary pressure that selects for increasingly positive ecological effects. Finally, we genetically engineer several of the most common clinically observed resistance mechanisms to targeted therapies in NSCLC, a treatment notorious for pre-existing resistance, and where our theory predicts positive ecological interactions to be common. We find that all three engineered mutants display a positive ecological interaction with their ancestor, as predicted. Strikingly, as with our originally evolved resistant mutant, two of the three engineered mutants have ecological interactions that fully compensate for their substantial fitness costs. As a whole, these results suggest that frequency-dependent ecological effects may provide the primary mode by which pre-existing resistance emerges.

## 1 Introduction

2 The rapid, and often inevitable, evolution of therapy resistance is the primary threat to modern medicine's successful treatment  
3 of cancer, and infectious disease (e.g. bacterial, viral, fungal, and parasitic infections)<sup>1-5</sup>. The story of resistance and treatment  
4 failure is strikingly similar across biological kingdoms. A patient is diagnosed and undergoes an initially successful treatment,  
5 only for a small resistant subclone of the original disease to relapse, resulting in treatment failure. For decades, the response to  
6 this paradigm has been the development of novel, more efficient drugs, targeting orthogonal pathways in hopes of winning  
7 the evolutionary arms race. While this response has undeniably resulted in major success stories when considering individual  
8 cancers or infections, the overall outlook for drug-resistant disease remains grim<sup>6-9</sup>.

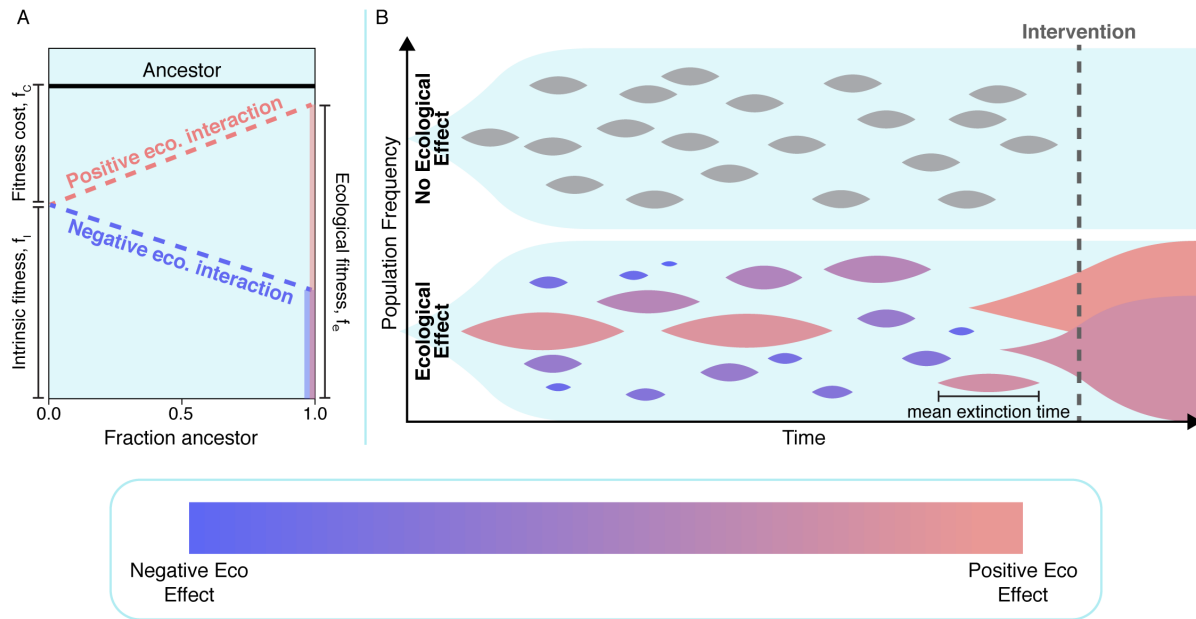
9 As a result, growing efforts have been made to study these diseases in an *evolutionary* context, whereby scientists seek  
10 to understand the ecological and evolutionary forces that inevitably result in the untreatable disease state. Understanding  
11 these evolutionary forces that lead to resistance, should allow scientists and physicians to not only design more effective  
12 drugs, but perhaps more crucially, design more effect *treatments*. For example, recent work has focused on improving  
13 and prolonging the efficacy of our already established drugs via optimal dose scheduling<sup>10-12</sup>, drug combinations<sup>13-17</sup>,  
14 understanding spatial dynamics<sup>18-20</sup>, understanding ecological interactions between competing subclones<sup>21-24</sup>, and exploiting  
15 collateral sensitivity<sup>25-29</sup>.

16 In a similar spirit, this work seeks to understand the evolutionary fates of potential resistance-conferring mutations that  
17 emerge *before* treatment has occurred. The fraction of these mutants that survive to see treatment are often the primary cause  
18 of treatment failure, referred to as "pre-existing resistance"<sup>30-33</sup>. While these resistant populations provide a large fitness  
19 advantage once treatment begins, they often carry a significant fitness disadvantage, or fitness cost ( $f_c$ ), in the absence of  
20 treatment<sup>34-38</sup>. Nevertheless, resistance-conferring mutants often persist until treatment, at which time their treatment-sensitive  
21 ancestors are preferentially killed, resulting in the competitive release and relapse of the resistant population and inevitable  
22 treatment failure. Understanding how these resistant clones – with a fitness disadvantage – persist in the disease population  
23 prior to treatment may allow us to prevent resistance from emerging.

24 This interest is derived from recent work where we measured the frequency-dependent ecological interaction between an  
25 evolved EGFR tyrosine kinase inhibitor (TKI) resistant non-small-cell lung cancer (NSCLC) population and its TKI-sensitive  
26 ancestor<sup>39</sup>. The focus of that work was on the ecological interaction under TKI treatment, and the inevitable competitive  
27 release. Strikingly, we observed an interaction between the resistant mutant and its ancestor in the absence of any treatment.  
28 The resistant population was observed to grow about twenty percent slower than the ancestor when cultured separately, however  
29 when the resistant population was co-cultured with a majority ancestor population, that difference in fitness nearly vanished.  
30 This observation, referred to as negative frequency-dependent selection (negative because the selection for the mutant increases  
31 as the mutant frequency *decreases*), is a long-studied phenomenon<sup>40-42</sup>, and has been described as the most "intuitively  
32 obvious explanation for polymorphisms in nature"<sup>43</sup>. Despite its long history and potential for potent evolutionary effects,  
33 frequency-dependent selection remains understudied in the context of drug resistance. This is especially surprising, because  
34 a resistant population typically first emerges as a single individual in a predominantly ancestor population, and as a result  
35 frequency-dependent ecological interactions have a profound potential to effect the dynamics of a resistant clone (**Fig. 1**).

36 In this work, we seek to develop a rigorous theory of pre-treatment evolution that incorporates frequency-dependent  
37 ecological interactions between the emerging resistant subclones and the ancestor from which they evolve. Using both a  
38 generalized Moran process and Wright-Fisher simulations, we show that mutants with the same intrinsic fitness (monoculture  
39 fitness) can have mean extinction times that vary by several orders of magnitude as a function of their ecological fitness (fitness  
40 when co-cultured in a predominantly ancestor environment). Next, we calculate the expected number of resistance-conferring  
41 mutants in the population as a function of the cost of resistance, as well as the population size, and rate at which resistance-  
42 conferring mutations occur. When comparing the result of this calculation both when we assume ecological interactions exist,  
43 and when they are forbidden, we identify a wide parameter space where pre-existence is only likely to occur if ecological-  
44 interactions are assumed. We then investigate the "many mutant regime" where pre-existence is likely even without ecological  
45 interactions, and demonstrate that these ecological interactions would play a prominent role in shaping the distribution of  
46 mutants, dramatically increasing the prevalence of mutants with high ecological fitness. Importantly, we show that these  
47 ecological effects drive the evolutionary outcomes even when mutants with high ecological fitness are rare. Surprisingly, despite  
48 the complexity of the model, we obtain analytical approximations for extinction rates, expected number of resistance-conferring  
49 mutants, and the distribution of observed mutants over the full range of ecological fitness. These analytical approximates both  
50 support our numerical simulations and allow us to extend our results to population sizes too large to simulate.

51 Finally, we test our theory experimentally by engineering several of the most common clinically-observed mutations to  
52 TKI-therapy in EGFR-driven NSCLC and compete these mutants against the TKI-sensitive ancestor. In all cases we observed an  
53 ecological interaction that resulted in mutant ecological fitnesses larger than their intrinsic fitness. In the case of BRAFV600E,  
54 despite harboring a fitness cost of approximately 20 percent, the ecological interaction was sufficiently large that its growth  
55 rate eclipsed the ancestor's. This is particularly striking because it suggests BRAFV600E will survive indefinitely as a small



**Figure 1. Cartoon abstraction demonstrating how frequency-dependent ecological interactions could increase the likelihood of pre-existing resistance.** (A) Cartoon visualization of a typical frequency-dependent growth experiment. The ancestor (black line) is assumed to grow at a constant rate. Two hypothetical resistant mutants are depicted. Both mutants shared the same intrinsic fitness and fitness cost, however the positive ecological mutant (red, growth increases as the fraction of ancestor cells increases) has a significantly higher ecological fitness  $f_e \approx 1$  than the negative ecological mutant (blue, growth decreases as the fraction of ancestor cells increases). As a result no mutants are present when a drug intervention is administered (vertical dashed line). (B) Top: Cartoon visualization of an evolving population with no ecological interactions. All mutants are assumed to have so non-insignificant fitness cost,  $f_c$ , and as a result go extinct. Bottom: The same evolving population, assuming ecological interactions are present. Note that an identical number of mutants emerge, however semi-rare mutants with positive ecological interactions demonstrate an increased time to extinction. As a result, when a drug intervention is administered, pre-existence is present.

56 fraction of the population, lurking until treatment results in competitive release of the untreatable resistant subclone. Taken  
57 together, these theoretical and experimental results argue that frequency-dependent ecological interactions between resistance  
58 mutants and their ancestor confer the primary mode by which resistance emerges in modern cancer therapeutics, and potentially  
59 all evolutionary diseases.

## 60 Results

### 61 Ecologically-dependent extinction time distributions with a generalized Moran process

62 We begin by considering a one-step birth-death process<sup>44–46</sup> with states  $s \in \{0, 1, \dots, N\}$ , where  $N$  is the total population size,  $s$   
63 is the mutant population, and  $N - s$  is the ancestor population. We do not consider mutation and as a result the states  $s = 0$   
64 (extinction) and  $s = N$  (fixation) are absorbing. To account for ecological interactions, the mutant's growth rate is defined to be  
65 a function of  $\frac{N-s}{N}$ , or the fraction of the population that is of the ancestral type, and assumed to be linear, see **Fig. 1, right**. In  
66 addition, for simplicity, we define the ancestor's growth rate to be constant and, without loss of generality, normalized to 1 (see  
67 Materials and Methods for full model details).

68 First, we are interested in how the distribution of extinction times differs between recently emerged mutants with identical  
69 fitness costs, but distinct ecological interactions (**Fig. 2A, left**). In particular we assume one (neutral) mutant has no ecological  
70 interaction with the ancestor, and thus  $f_c = f_e$  (**Fig. 2A, blue**), while the comparative (positive) mutant has an interaction that  
71 ameliorates the fitness cost of the mutant at extremely large ancestor fractions,  $f_e = 1$  (**Fig. 2A, red**). In the case of a mutant  
72 with a positive ecological interaction, we see that the extinction time distribution is heavily right-skewed in comparison to a  
73 neutral ecological effect. As a result, if these two mutants were equally likely to emerge in a population, we would expect  
74 to observe a mutant with a positive ecological interaction significantly more often than an equivalent mutant with a neutral  
75 ecological interaction. However, ecological interactions are not always positive. Repeating this process in comparing a neutral  
76 mutant with a mutant that has a negative ecological interaction with the ancestor reveals distinct shift to shorter extinction times  
77 as one might intuitively expect (**Fig. S1**).

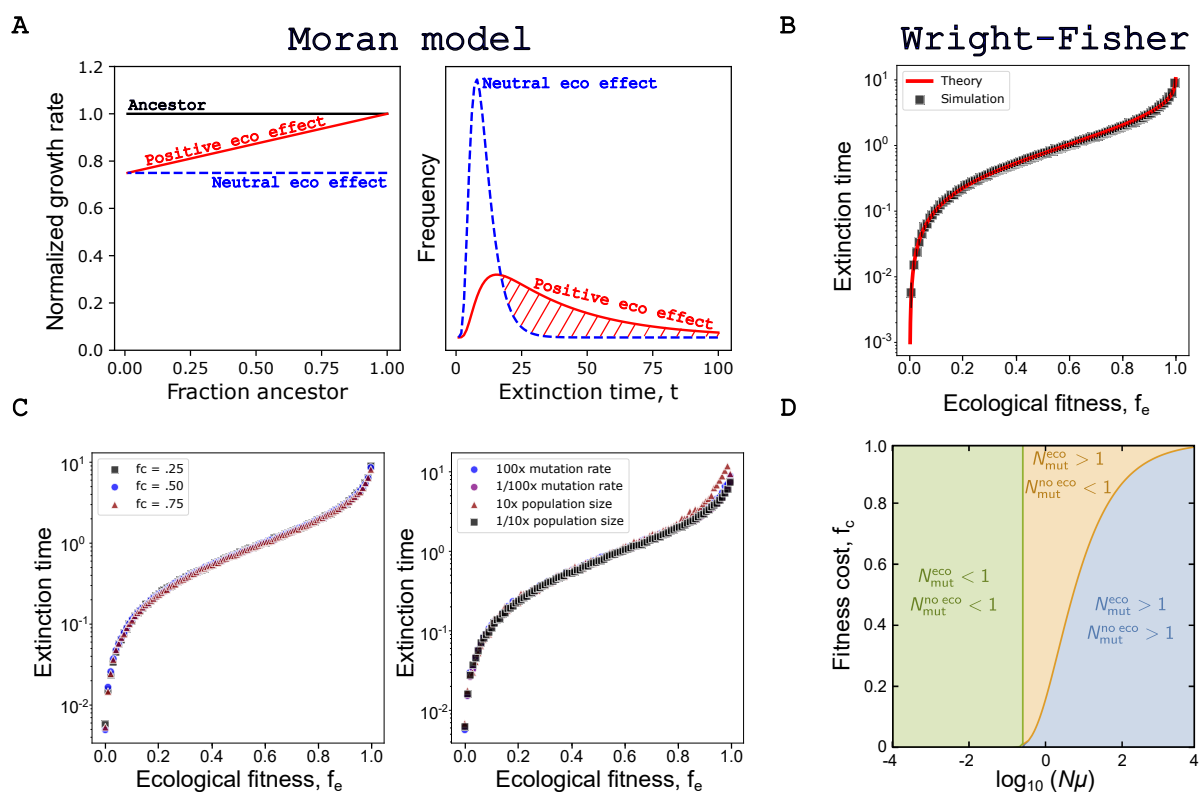
### 78 Extinction times depend on ecological interactions in a Wright-Fisher model

79 While formulating our system as a generalized Moran process allows for convenient closed-form solutions to quantities of  
80 interest such as extinction time distributions, this representation becomes computationally expensive as the population size  
81 approaches increasingly realistic values. In addition, we have completely ignored mutation, as well as more realistic conditions  
82 where many mutants are competing within an evolving population. As such, we switch to a Wright-Fisher formulation of our  
83 system<sup>47–49</sup>. In the Wright-Fisher model, populations are still constant in population size  $N$ , however each individual of the  
84 population is replaced every generation with offspring inheriting the parent's genotype with probability proportional to the  
85 parent's fitness. In addition, individuals acquire mutations with some probability  $\mu$  and we assume mutant populations are  
86 sufficiently small that we can ignore mutant-mutant interactions. Still, several of the generalizations and abstractions from the  
87 generalized Moran process remain. Namely, the ancestor's growth is defined to be constant and normalized to 1, and the mutant  
88 growth rate is assumed to vary linearly between  $f_i$  and  $f_e$  (as a result, a mutant's growth is fully characterized by these two  
89 fitness values along with the fraction of the population that is ancestor).

90 Each simulation begins with an exclusively ancestor population and with each generation cells mutate with probability  $\mu$ .  
91 Each mutant that arises has an intrinsic fitness drawn with uniform probability in  $[0, 1 - f_c]$  and a corresponding ecological  
92 fitness drawn with uniform probability in  $[0, 1]$ . Each Wright-Fisher 'generation' consists of a mutation step, followed by  
93 an offspring/selection step. For each mutant that emerges we record its intrinsic and ecological fitness values and track its  
94 evolutionary trajectory, and thus extinction time ( $\tau$ ). A mutant that emerges but does not survive the subsequent selection step  
95 is defined to survive 0 generations. Employing this model we find that the mean extinction time varies nearly five orders of  
96 magnitude between the most positive ( $\approx 10$  generations) and deleterious ( $\approx 0.001$  generations) ecological interactions (**Fig. 2B**).  
97 In order to develop a more rigorous understanding of the evolutionary dynamics, we sought an analytical approximation for the  
98 extinction time of a mutant under the same Wright-Fisher conditions. Strikingly, we find a robust approximation across the  
99 whole range of  $f_e$ :

$$\tau(f_e) \approx \frac{3 \ln(1 - f_e)}{f_e^2 - 3}. \quad (1)$$

100 Despite its simple form, this approximation agrees with simulation results with a typical error of 5% (**Fig. 2B**, full derivation  
101 and details found in the SI). Interestingly, the approximation is only a function of ecological fitness, and not mutation rate  
102 (assuming  $\mu \ll 1$ ), population size, or fitness cost. This finding is supported by our simulation results (**Fig. 2C**).



**Figure 2. Analytical approximations and simulations predict that extinction times depend on ecological interactions.** (A) Closed form extinction time distributions are calculated and visualized for a generalized Moran process ( $N=100$ ,  $f_c = 0.25$ ). The red distribution results from a mutant with a positive ecological interaction with the ancestor ( $f_e = 1.0$ ), while the blue population has no ecological interaction with the ancestor ( $f_e = 1 - f_c = 0.75$ ). (B) Wright-Fisher simulations are used to numerically calculate the mean extinction time as a function of  $f_e$  ( $N=10000$ ,  $\mu = 10^{-6}$ , 500 generations,  $f_i$  is drawn uniformly in  $[0, 1 - f_c]$ ,  $f_i$  is drawn uniformly in  $[0, 1]$ ). (C) Wright-Fisher simulations are repeated for varying values of  $f_c$ ,  $\mu$ , and  $N$  to confirm theoretical prediction that the extinction time distribution depends only on  $f_e$ . (D) Phase diagram depicting the three regimes of pre-existing resistance.

## 103 Ecological interactions can increase the probability of pre-existing resistance

104 Next we consider the model's implications for pre-existing resistance. Specifically, we are interested in quantifying the expected  
 105 number of mutants in an evolving population. While it might be tempting to quickly conclude that including ecological  
 106 interactions will necessarily increase the probability of pre-existing resistance because positive interactions will lead to longer  
 107 extinction times, it is important to note that mutants with a high intrinsic fitness are more likely to acquire a relatively deleterious  
 108 ecological fitness, than one that is beneficial. As such, a careful mathematical treatment is required. When the expected number  
 109 of mutants in a population is low ( $N_{\text{mut}} \ll 1$ ), potential resistance-conferring mutations are unlikely to be present at time of  
 110 treatment. Contrarily, when the expected number of mutants is greater than 1, we expect treatment threatening resistance to be  
 111 present when a drug is administered. We begin adapting our analytical model to calculate the mean number of mutants (see  
 112 SI for full derivation and details). To begin we consider the case where no ecological interactions are present ( $f_i$  completely  
 113 describes the growth rate of the mutant). In this case it can be shown that  $N_{\text{mut}}^{\text{no eco}}$ , the mean number of mutants ignoring  
 114 ecological interactions, is:

$$N_{\text{mut}}^{\text{no eco}} = N\mu \left( -\frac{\ln f_c}{1-f_c} - 1 \right). \quad (2)$$

115 Next, we seek to find an analytical approximation for  $N_{\text{mut}}^{\text{eco}}$ , the mean number of mutants assuming ecological interactions  
 116 exist. In the case of a sufficiently small mutation rate, we can approximate the total mutant fraction as,

$$N_{\text{mut}}^{\text{eco}} \approx N\mu \left( -\frac{\ln(1-f_{\text{max}})}{f_{\text{max}}} - 1 \right) \quad \text{for } \mu \ll 1. \quad (3)$$

117 Here,  $f_{\text{max}}$  is the maximum value that  $f_e$  can take. While we can set  $f_{\text{max}}$  arbitrarily close to 1, it can never be exactly 1 for a  
 118 well-defined normalization. Interestingly, for sufficiently small  $\mu$ , the ratio  $\frac{N_{\text{mut}}^{\text{eco}}}{N_{\text{mut}}^{\text{no eco}}}$  is constant with  $N\mu$ . While the simplicity of  
 119 the approximation is appealing, unfortunately it breaks down as  $\mu$  gets large. As a result, a more robust, though significantly  
 120 more complex, approximation was derived (see SI for full derivation):

$$N_{\text{mut}}^{\text{eco}} \approx \frac{N\mu}{f_{\text{max}}} W \left( \left( 1 - f_{\text{max}} + \mu f_c^{f_c/(f_c-1)} \right)^{-1} \right). \quad (4)$$

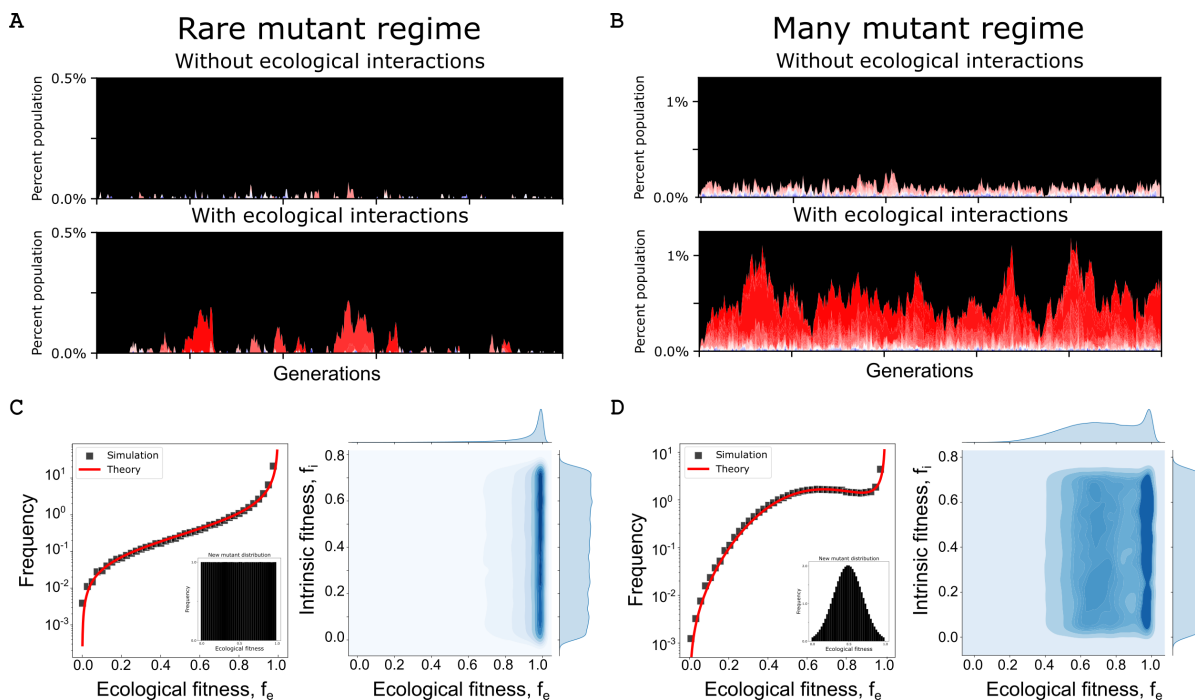
121 Here  $W(x)$  is the Lambert  $W$  function, which is the solution  $y$  of the equation  $ye^y = x$ . This approximation allows for  
 122 efficient calculation across several decades of  $\mu$  within 10% of our numerical simulations. Employing these analytical  
 123 approximations we identify three regimes of interest. The least interesting regime is the small  $N\mu$  regime (**Fig. 2D, green**).  
 124 Here the effective population size is insufficient to maintain a mutant subpopulation regardless of the strength or frequency of  
 125 ecological interactions. While this is the least mathematically interesting regime, this corresponds to extremely rare pre-existing  
 126 resistance and high likelihood of treatment success.

127 As  $N\mu$  gets larger (**Fig. 2D, yellow**) we enter a regime where ecological interactions would suggest pre-existing resistance  
 128 is likely ( $N_{\text{mut}}^{\text{eco}} > 1$ ), while ignoring ecological interactions would suggest pre-existence is still rare ( $N_{\text{mut}}^{\text{no eco}} < 1$ ). In this  
 129 regime mutants have yet to become abundant, however, mutants with strong ecological interactions persist sufficiently long to  
 130 threaten treatment efficacy. Representative simulation trajectories of this “rare mutant regime” are shown in **Fig. 3A**. Without  
 131 ecological interactions (**Fig. 3A, top panel**) the mutation rate alone is insufficient to maintain a mutant subpopulation capable  
 132 of threatening future treatment efficacy. However, with the introduction of ecological interactions (**Fig. 3A, bottom panel**),  
 133 rare positive ecological mutants climb to significant fractions of the population, and have measurably longer extinction times  
 134 that may threaten future treatments. As one might intuitively expect, the size of this regime where ecological effects drive  
 135 pre-existence is heavily dependent on the imposed fitness cost of resistant mutants. We find that the larger the fitness cost  
 136 imposed by resistance, the larger the comparative increase provided by allowing ecological effects.

## 137 Ecological interactions significantly influence the distribution of mutants

138 Next, we consider the final regime when  $N\mu$  is large (**Fig. 2D, blue**). In this regime the mutational supply is sufficiently large  
 139 to self-sustain a small, resistant subpopulation, regardless of ecological interactions (that is, both  $(N_{\text{mut}}^{\text{no eco}} > 1$  and  $N_{\text{mut}}^{\text{eco}} > 1)$ ).  
 140 Representative simulation trajectories of this “many mutant regime” are shown in **Fig. 3B**. At first glance one might assume  
 141 this regime is uninteresting. In both cases mutants are sufficiently common to threaten future treatments, albeit ecological  
 142 interactions significantly increase the steady-state fraction of resistant mutants. However, the results become more interesting  
 143 when we consider the shape of the resistant subpopulation distribution. In each trajectory plot, the color is proportional to the





**Figure 3. Positive ecological interactions make pre-existence more likely and dominate the stationary distribution of mutants.** (A) Representative Wright-Fisher trajectory in the “rare mutant regime”. Mutants exist in higher fractions and for longer periods with ecological interactions. Each mutant is colored by its ecological fitness where red represents an  $f_e$  value near 1 and blue represents an  $f_e$  value near 0. (B) Representative trajectory in the “many mutant regime”. Strong positive ecological interactions dominate the stationary distribution of mutants. (C) Left: Stationary distribution of mutant ecological fitnesses when the mutant generating function is uniform in ecological fitness. Right: joint distribution density plot between intrinsic and ecological fitness. (D) Same as C, however the mutant generating function is now Gaussian centered about  $f_e = 0.5$ .

144 mutants ecological fitness with red representing an ecological fitness near 1 and blue representing an ecological fitness near 0.  
 145 By inspection it is immediately clear that the most positive ecological mutants are over represented in the mutant population,  
 146 considering they emerge with equal probability. However, we can do better and extract this relationship explicitly from our  
 147 simulations (Fig. 2C, left). We find, similar to the impact of ecological effects on extinction times, that the frequency of a  
 148 mutant spans multiple orders of magnitude as a mutant’s ecological fitness varies from 0 to 1.

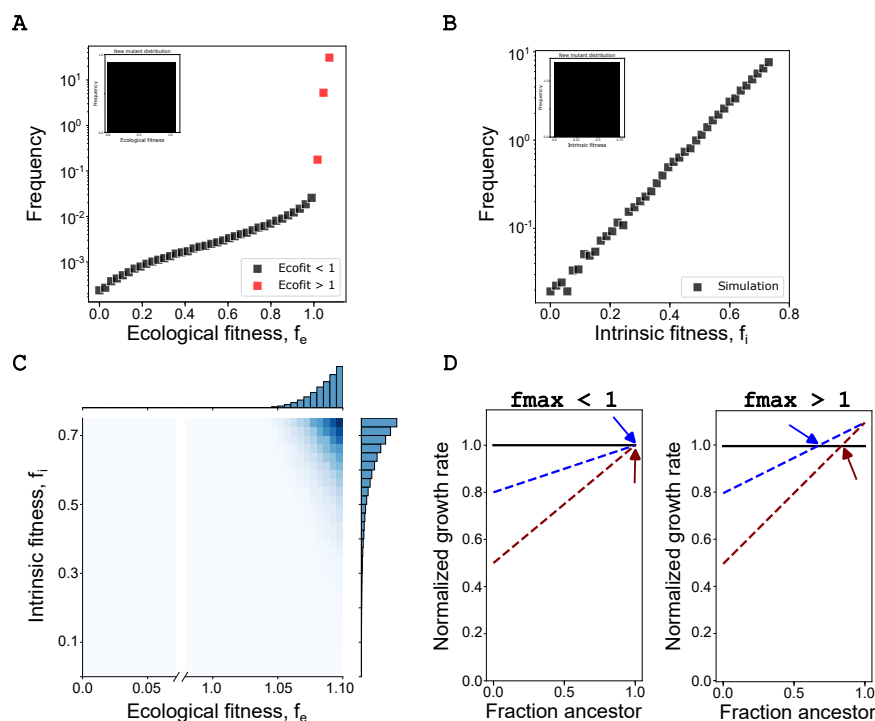
149 Extending our previous analytical work, it is straightforward to show that the stationary distribution of mutant ecological  
 150 fitnesses goes as,

$$P(f_e) \approx \frac{f_e \mu}{f_{\max}(1 - f_e)} \quad \text{for } \mu \ll 1. \quad (5)$$

151 The above approximation works remarkably well despite the simplicity of its form. From this equation we find that the  
 152 frequency of a mutant is invariant with respect to fitness cost and population size. This is shown explicitly via numerical  
 153 simulations and visualization of the joint distribution of fitness cost and ecological fitness (Fig. 2C, right).

### 154 Non-uniform ecological distributions show similar qualitative results

155 An important context to keep in mind with the work is that up to this point we have assumed emerging mutants are assigned an  
 156 ecological fitness with uniform probability in  $[0, 1]$ . This assumption was not made for simplicity, but instead out of necessity.  
 157 While evolutionary biologists have spent significant time both theorizing about, and measuring the distribution of fitness effects  
 158 (DFE), very little time has been spent quantifying either the frequency or magnitude of ecological effects (distribution of  
 159 ecological effects, DEE). As a result, it is difficult to even speculate on what the null model ought to be.



**Figure 4. Positive ecological fitnesses above 1 result in a stable fixed point between mutant and ancestor.** (A) Stationary distribution of mutant ecological fitnesses when the mutant generating function has uniform probability in  $[0, 1.10]$ . (B) Stationary distribution of mutant intrinsic fitnesses. (C) Joint distribution density plot between intrinsic and ecological fitness reveals the size of the fitness cost now has a significant impact on mutant survival. (D) Cartoon illustration of why two mutants with identical values of  $f_e$  can result in different extinction times. Colored arrows point to stable fixed points between mutant and ancestor. Importantly, only the present mutant with the stable fixed point at the smallest value of  $f_e$  will achieve stability.

160 Crucially, the analytical approximations derived herein can be simply generalized to fit any assumed, or future measured,  
 161 DEE. While we assumed a uniform distribution, a Gaussian model where the most positive and negative ecological interactions  
 162 are rare relative to more modest, or non-interacting mutants, may be more accurate. As an example, the general stationary  
 163 distribution of mutant ecological fitnesses would become,

$$P(f_e) \approx \frac{f_e \mu}{(1 - f_e)} \rho_0(f_e) \quad \text{for } \mu \ll 1. \quad (6)$$

164 Here,  $\rho_0(f_e)$  can be any theorized or measured distribution of ecological effects. As proof of principle, we numerically  
 165 simulate the distribution of mutant ecological fitnesses under an assumed Gaussian DEE, and show the above analytical  
 166 approximation still holds. The results are qualitatively similar to the uniform DEE and, strikingly, despite the rarity of mutants  
 167 with positive ecological interactions, they still manage to dominate the predicted stationary distribution of mutants (**Fig. 2D**).

#### 168 Sufficiently large positive ecological interactions result in a stable fixed point between mutant and ancestor

169 We now briefly consider the regime wherein the ecological fitness of a mutant can sample values greater than 1. Put another  
 170 way, when the mutant population emerges, it may emerge into an environment where it out-competes its ancestor. Importantly,  
 171 emerging mutants still have a nonzero fitness cost, so even the most positive ecological interactions cannot lead to a hard  
 172 selective sweep. Though our earlier analytical approximations do not apply for  $f_{\max} > 1$ , the numerical simulations are robust  
 173 in this regime. We find that the majority of stationary distribution mutants are mutants with ecological fitnesses larger than the  
 174 ancestor, or  $f_e > 1$  (**Fig. 4A**). This qualitative change in behavior above  $f_e = 1$  can be explained in evolutionary game theory  
 175 terms by a switch in the evolutionary game being played. When  $f_e < 1$ , the ancestor out-competes the mutant population at all  
 176 population frequencies. As a result, it is a question of when, not if, the mutant population will be driven to extinction. When  
 177  $f_e > 1$ , however, the mutant population out-competes the ancestor at high ancestor frequencies, while the ancestor out-competes



178 the mutant at high mutant frequencies (as a result of the mutant fitness cost). This leads to a stable fixed point at some ancestor  
179 frequency where the two populations have an equal growth rate. This is particularly worrying in the case of therapy-resistant  
180 mutants, because it suggests if such a mutant emerges and survives the initial stochasticity of drift, it coexist at a sizeable  
181 frequency in the population until treatment.

182 Next, we found that, contrary to our previous results, the fitness cost of the mutant plays an important role in determining the  
183 stationary distribution of mutants (Fig. 4B,C). Here we see that only the mutants with the largest positive ecological interactions  
184 and smallest fitness costs (intrinsic fitness =  $1 - \text{fitness cost}$ ) are represented at meaningful frequencies. This result can be  
185 explained by the qualitative shift in evolutionary game for mutants where  $f_e > 1$ . Previously, regardless of the fitness cost,  
186 any mutant with  $f_e \approx 1$  would grow at that ecological fitness, as the mutant population never became a meaningful fraction of  
187 the whole population (Fig. 4D, left). However, as hinted at in the numerical simulations,  $f_c$  and  $f_e$  combine to determine the  
188 stable fixed point between the mutant and the ancestor (Fig. 4D, right). As a result, even mutants with  $f_e < 1$  are no longer  
189 characterized by their ecological fitness, instead they are characterized by their fitness at the frequency determined by the stable  
190 fixed point.

## 191 Clinically observed lung cancer mutations confer positive ecological interactions

192 Epidermal growth factor (EGFR) tyrosine kinase inhibitors (TKIs) are the first-line treatment for patients diagnosed with  
193 advanced non-small cell lung cancer (NSCLC). While the development of targeted TKIs has importantly extended overall  
194 survival times, these drugs are rarely curative<sup>50</sup> and patients often recur with TKI-resistant tumors. As a result, EGFR-mutant  
195 NSCLC is an ideal system for studying pre-existing resistance and a location we would expect to find the strongest evidence of  
196 our predictions — namely the presence of strongly positive ecological interactions between mutants and their ancestor.

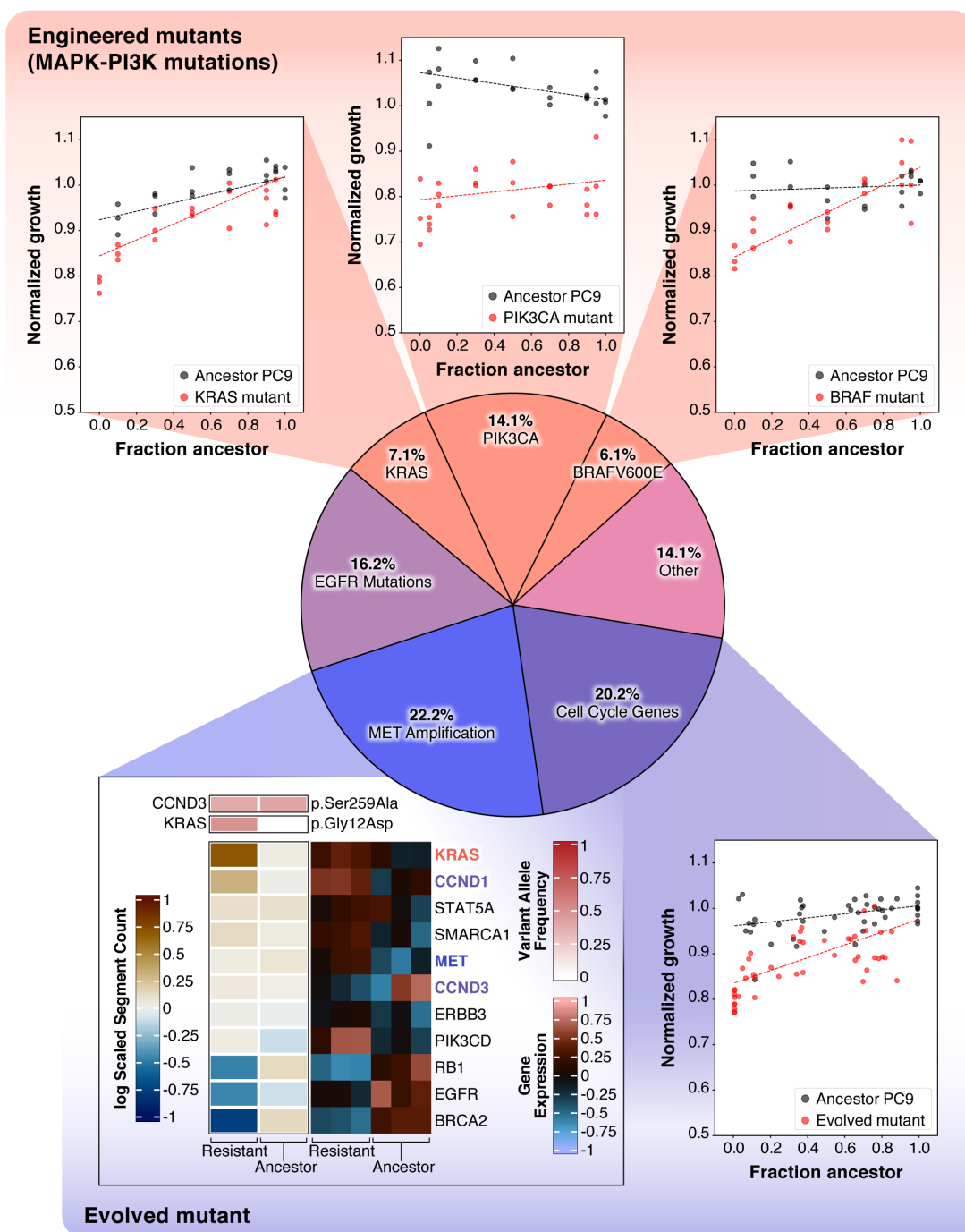
197 To test our theory we genetically engineered (see Materials and Methods) three of the most commonly clinically observed  
198 resistance mutations found in response to TKIs:<sup>51,52</sup> BRAF-V600E, KRAS-G12V, and PIK3CA-E545K. Then, using our  
199 previously described evolutionary game assay<sup>23,39</sup>, we measured the ecological interaction between each of these mutants and  
200 the ancestor PC9 cell line from which they emerged.

201 We found that each of the three engineered mutants had varying levels of positive ecological interactions with their ancestor  
202 (Fig. 5, top). The most extreme result of the three was undoubtedly the BRAFV600E mutant, in which we observed a  
203 sufficiently strong ecological interaction to out-compete the ancestor in predominantly ancestor populations ( $f_e > 1$ ). This  
204 observation suggests, at least in a laboratory environment, that if BRAFV600E emerges and survives stochastic evolutionary  
205 forces, it will stably coexist at approximately 20% of the population.

206 A similarly strong positive ecological interaction was observed between KRASG12V and the PC9 ancestor. While the  
207 ecological fitness did not eclipse the ancestor, the ecological interaction was strong enough to completely ameliorate its fitness  
208 cost of approximately 20%. Finally, the PIK3CA-E545K mutant showed the weakest ecological interaction, though still slightly  
209 positive in nature. While we already reported on the ecological interaction between the evolved mutant and its ancestor, as it  
210 was the motivator of this study<sup>39</sup>, we performed additionally sequencing analysis (WXS and RNA-seq) and identified several  
211 common clinical mutations present, distinct from the engineered mutations: MET overexpression, CCND1 amplification, and  
212 KRASG12D mutation (Fig. 5, bottom). Taken together, these experimental results match our theoretical predictions and  
213 strongly support the hypothesis that frequency-dependent ecological interactions are a primary mode by which resistance is  
214 conferred in evolutionary diseases.

## 215 Discussion

216 While much work has gone into quantifying clinically problematic resistant bacteria, cancers and viruses, we nearly always  
217 characterize these clones in monoculture - entirely outside the eco-evolutionary forces that selected for (or against) them in the  
218 first place. In this work we set out to provide the foundation for a rigorous and generalizable mathematical framework that  
219 incorporates frequency-dependent ecological interactions and can be used to study their role in pre-existing resistance. This  
220 work both compliments and builds off of recent studies from a wide range of disciplines ranging from theoretical population  
221 genetics and ecology to clinical trials across several biological kingdoms. We demonstrate that the presence of ecological  
222 interactions can significantly increase the probability of pre-existing resistance, in addition to shaping the distribution of mutants  
223 likely to be present before treatment. We derive analytical approximations of several quantities of interest including extinction  
224 time, mean mutant population numbers, and the underlying distribution of mutants each as a function of ecological fitness.  
225 Importantly, these results can easily be generalized to any theorized distribution of ecological effects, or future experimentally  
226 measured distribution. As an important example, we show that even when we assume positive ecological interactions are rare,  
227 they still end up as a plurality of the stationary mutant frequency distribution. Finally, in an model system for pre-existing  
228 resistance, we show common clinically observed mutants harbor positive, frequency-dependent ecological interactions when  
229 co-cultured with their ancestor, providing strong evidence for our theory in cancer. In addition, recent exciting work in bacteria



**Figure 5.** As predicted, common clinically observed resistance mutations in NSCLC harbor strong positive ecological interactions with their ancestor in a model system of pre-existing resistance. Pie chart: Visual representation of the known resistance mechanisms to Osimertinib, a third generation TKI and the current standard of care for EGFR-positive NSCLC. Top: Measured positive ecological interactions between engineered resistant mutants and their ancestor. From left to right — KRAS-G12V, PIK3CA-E545K, BRAF-V600F. Bottom right: Measured positive ecological interaction between evolved gefitinib-resistant NSCLC PC9 population and its ancestor. Previously reported in<sup>39</sup>. Bottom left: Fresh sequencing analysis reveals the gefitinib-resistant evolved mutant has additional clinically observed resistance mutations including: KRASG12D, MET amplification, and CCND1 amplification (cell cycle genes).

230 provides additional evidence, as frequency-dependent interactions resulted in maintenance of otherwise costly antibiotic  
231 resistant populations in *Escherichia coli*<sup>53</sup> and *Pseudomonas aeruginosa*<sup>54</sup>.

232 It is also important to address several limitations of our work. As we mentioned earlier, the distribution of ecological effects  
233 (DEE) has never been experimentally measured. As a result, assumptions regarding the distributional parameters have to made  
234 in order to calculate meaningful quantities of interest. While we did our best to combat this by developing analytical models  
235 that are agnostic to this distribution, the quantitative aspect of our results are subject to the specifics of a model. Our hope is that  
236 the analytical and numerical results herein, when combined with the promising experimental work in NSCLC, motivate future  
237 measurements of the DEE across diverse model systems. Similarly, our own experimental validation is constrained to one  
238 subsystem. Our predictions are broad and should apply to many evolving populations where pre-existence is evolved. Therefore  
239 it is important that future studies should aim to test these theories not just in other cancers, but in other organisms from  
240 HIV to drug resistant bacteria. It is possible that these principles provide the most explanatory power in cancer and bacteria  
241 where it is common to find highly dense heterogeneous populations in contrast to viruses, for example. Finally, while the model  
242 aims to generally capture major evolutionary forces that may underlie pre-existing resistance, it is still an abstraction of a much  
243 more complex clinical scenario where the immune system, spatial dynamics, and treatment adherence, to name only a few, can  
244 play major roles.

## 245 **Materials and Methods**

### 246 **Cell culture**

247 PC-9 are human adenocarcinoma cells derived from undifferentiated lung tissue were obtained from Sigma (Sigma, USA).  
248 PC-9 cells were cultured in RPMI-1640 medium supplemented with 10% heat inactivated fetal bovine serum (FBS) and 1%  
249 penicillin streptomycin solution at 37°C with humidity containing 5% CO<sub>2</sub>. Cells were split every four days to maintain  
250 optimum confluency of ≈80-90%.

### 251 **Engineering of mutant cell lines**

252 To establish PC-9 cells stably expressing target genes, HEK-293T cells were co-transfected using TransIT-Lenti transfection  
253 reagent (Mirus, USA), with 500ng psPAX2 (addgene, USA), 100ng PMD2 (addgene, USA) and 500ng of target genes. Viral  
254 particles were collected after 48hrs and used to transduce PC-9 cells. Then, to establish ancestor PC-9 cells stably expressing  
255 nuclear localized GFP, cells were transduced with pLVX-eGFP-Hygro (Vectorbuild, USA). In addition, to establish query cells  
256 expressing fluorescently labeled PC-9 cells with a gene of interest cells were co-transduced with pLVX-mCherry-Hygro or  
257 pLVX-mCherry-Puro and each of pLVX-PIK3CA-E545K-Bsd (Vectorbuild, USA). Next, 72hrs after transduction, cells were  
258 selected with 200μg/ml hygromycin, 5μg/ml puromycin and 5μg/ml blasticidin.

### 259 **Drug sensitivity assay**

260 Cells were harvested at 70-80% confluence, stained with trypan blue (Corning, USA), and counted with a TC20 Automated  
261 Cell Counter (Bio-Rad, USA). Luminescent based cell viability assays using CellTiter-Glo (CTG) reagent (Promega, USA)  
262 were performed in 96 well plate (Corning, USA). A total number of 3,000 cells were plated in 90μL of complete medium  
263 per well in three replicate per drug concentration with Multidrop reagent dispenser (Thermo Fishers, USA). After 3hrs of  
264 incubation, 10μL of gefitinib, osimertinib and erlotinib (Cayman, USA) diluted in complete RPMI-1640 medium were added  
265 to the cells. Compounds were tested in a threefold dilution in a range of 0 – 1.8μM, 0 – 3μM and 0 – 10μM for gefitinib,  
266 osimertinib and erlotinib respectively. After 72hrs of incubation, 25μL CTG reagent was add to the cells; incubated for 10  
267 minutes at room temperature and luminescence was measured.

### 268 **Game assay**

269 PC-9 mutants stably expressing nuclear localized fluorescent signal ancestor PC-9 stably expressing nuclear localized GFP  
270 were co-cultured at different initial proportion of ancestor cells at a density of 1,500 cells in 90μL of fresh medium. After 3hrs  
271 of incubation, 10μL of DMSO diluted in complete RPMI-1640 medium (final DMSO concentration of 0.1% v/v) were added  
272 to the cells in three replicates per initial proportion. Then time-lapse microscopy images were obtained for GFP and mCherry  
273 using BioSpa automated incubator (BioTek, USA) every 4 hours over the course of 96 hrs. Then, images were processed  
274 with the open-source software CellProfiler<sup>55</sup>. Images were background subtracted, converted to 8-bit, contrast enhanced, and  
275 thresholded, then raw cell numbers were extracted.

### 276 **Generalized Moran model details**

277 In this work we consider a well known generalized Moran process, a model previously used to study frequency dependent  
278 evolutionary dynamics<sup>44-46</sup>. Briefly, we consider a one-step birth-death process with states  $s \in \{0, 1, \dots, N\}$  and characterized  
279 by birth and death rates  $b_i$  and  $d_i$  with  $i \in \{1, 1, \dots, N-1\}$ . As a result this model describes a fixed population size  $N$ , with  $s$   
280 resistant mutants and  $N-s$  ancestor population. We forgo mutation rate and as a consequence the states  $s=0$  and  $s=N$  are  
281 absorbing. We consider an evolutionary game with a 2x2 payoff matrix such that:

$$\begin{array}{cc} & \begin{array}{cc} \text{R} & \text{A} \end{array} \\ \begin{array}{c} \text{R} \\ \text{A} \end{array} & \begin{pmatrix} (1-f_c) & f_e \\ 1 & 1 \end{pmatrix} \end{array}$$

282 As a result, we can write the expected payoffs in a population of  $s$  mutants and  $N-s$  ancestor individuals as:

$$P(R) = \frac{s-1}{N-1}(1-f_c) + \frac{N-s}{N-1}f_e \qquad P(A) = 1.$$

## 283 RNA-Seq

284 Paired-end reads are preprocessed using *fastp* to trim and quality filter the reads. Following the filtering, reads are aligned to  
285 GRCh38 reference genome via *STAR* aligner. Read quantification is done using *Salmon* on the extracted transcriptome locations  
286 from spliced STAR alignment. Gene-level abundance are aggregated from bootstrapped transcript abundances using R package  
287 *tximport*. The *Arriba* tool is coupled with spliced alignments for fusion-transcript detection as well. Pathway level expression  
288 activities are quantified using R package *GSEA* and *msigdbR* for the Hallmark Pathways. The R package *ComplexHeatmap* was  
289 used to generate heatmaps.

## 290 Whole exome sequencing

291 Paired-end whole-exome reads of ancestor and parental lines were preprocessed using *fastp* similar to RNA-Seq. Alignment to  
292 GATK (GATK best practices bucket) version of GRCh38 reference is done using *bwa-mem* aligner. Following the alignment,  
293 variant calling pipeline according to the GATK workflow including duplicate marking and variant calling via HaplotypeCaller  
294 was conducted. Variants passing filtering based on hard-filtering are further annotated using Variant Effect Predictor (VEP) tool.  
295 Exome alignments are further input to *CNVkit* for copy-number alterations. Using a flat-reference for bias correction log2  
296 scaled abundances are generated for ancestor and resistant strains. Copy number segments are captured using circular binary  
297 segmentation and assigned to genes mapping to the segment.

## 298 Code availability

299 Code used in this study will be made openly available on GitHub.

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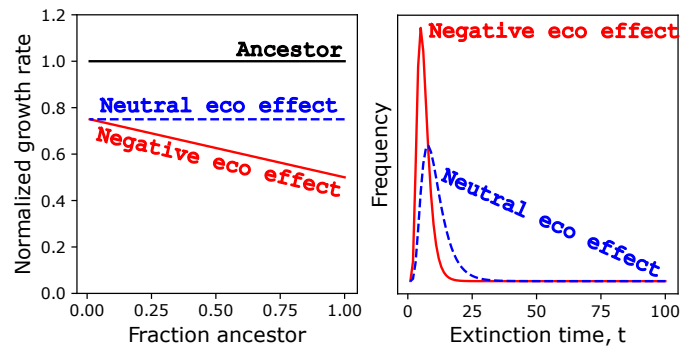
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**Figure S1. Similar qualitative trends exist when comparing neutral and negative mutants.** Closed form extinction time distributions are calculated and visualized for a generalized Moran process ( $N=100$ ,  $f_c = 0.25$ ). The red distribution results from a mutant with a negative ecological interaction with the ancestor ( $f_e = 0.5$ ), while the blue population has no ecological interaction with the ancestor ( $f_e = 1 - f_c = 0.75$ ).

## Supplemental Material: Frequency-dependent ecological interactions increase the prevalence and shape the distribution of pre-existing drug resistance

### Simulations

Here we provide additional complimentary results from our numerical simulations in the main paper.

#### Additional generalized Moran process results

Similar to the main text figure, we compare the extinction time distributions of two emerging mutants in an initially ancestor population. Here we compare a neutral mutant with a negative mutant.

While the effect is smaller than the comparison between positive and neutral mutants in the main text, we find similar qualitative trends in that extinction time distribution for neutral mutants is shifted to longer extinction times when compared to the negative mutant (**Fig. S1**).

### Analytical theory

The following sections describe the analytical theory supporting the numerical simulations in the main text. Important formulas that are used to fit the simulation results are highlighted by boxes.

#### Stationary distribution and total number of mutants

We seek to derive an approximate analytical expression for the stationary probability density of mutants  $P(f)$  in the Wright-Fisher simulations described in the main text. We assume ecological interactions are present, and that sufficient time has passed for a stationary state to be reached.  $P(f)df$  is defined as the fraction of the total population that consists of mutants with instantaneous fitnesses between  $f$  and  $f + df$ . Integrating this distribution gives the mean total number of mutants  $N_{\text{mut}}^{\text{eco}} = N \int_0^{f_{\text{max}}} df P(f)$ , where  $N$  is the fixed total population size. For the theoretical calculations we consider an upper bound on the mutant fitness  $f_{\text{max}} < 1$  to allow for a well-defined normalization (as explained in more detail below), though we can set  $f_{\text{max}}$  arbitrarily close to 1 in order to fit the numerical results.

Every generation of the model consists of a mutation step followed by selection. Let us consider first the mutation part. If  $P(f)$  is the current distribution, mutation modifies it to a new distribution,

$$P^m(f) = P(f) + \mu \rho_\alpha(f) - \mu P(f). \quad (\text{S1})$$

Here  $\mu$  is the mutation probability for a single cell in one generation, and  $\rho_\alpha(f)$  is the probability density of a new mutant having fitness  $f$ , given a total fraction of mutants  $\alpha \equiv \int_0^{f_{\text{max}}} df P(f) = N_{\text{mut}}^{\text{eco}}/N$ . The second and third terms on the right-hand side in **Eq. (S1)** are respectively the gain and loss due to new mutations.

The dependence of  $\rho_\alpha(f)$  on  $\alpha$  reflects the role of ecological interactions. In the simplest linear model, a new mutant is assigned a fitness function  $f(\alpha) = \alpha f_i + (1 - \alpha)f_e$ , where  $f_i$  (the intrinsic fitness) is randomly drawn from a uniform distribution between 0 and  $1 - f_c$ , and  $f_e$  (the ecological fitness) is randomly drawn from a uniform distribution between 0 and  $f_{\max}$ . Here  $f_c$ , where  $0 < f_c < 1$ , is the cost associated with intrinsic fitnesses, with  $1 - f_c < f_{\max}$ . For this definition of  $f(\alpha)$ , the distribution  $\rho_\alpha(f)$  is given by

$$\rho_\alpha(f) = \begin{cases} \frac{f}{\alpha(1-\alpha)f_{\max}(1-f_c)} & f < \alpha(1-f_c) \\ \frac{1}{(1-\alpha)f_{\max}} & \alpha(1-f_c) \leq f < (1-\alpha)f_{\max} \\ \frac{\alpha(1-f_c) + (1-\alpha)f_{\max} - f}{\alpha(1-\alpha)f_{\max}(1-f_c)} & f \geq (1-\alpha)f_{\max} \end{cases} \quad (\text{S2})$$

434 For  $0 < \alpha < 1$  the distribution  $\rho_\alpha(f)$  has a trapezoidal shape, rising linearly from zero for small  $f$ , then plateauing in the  
 435 middle region, before decreasing linearly to zero at  $f_{\max}$ . In the two limits  $\alpha = 0$  and  $\alpha = 1$  it reverts to a uniform distribution  
 436 between 0 and  $f_{\max}$  (for  $\alpha = 0$ ) or between 0 and  $1 - f_c$  (for  $\alpha = 1$ ).

The second part of the dynamics is the selection step, which makes a further modification of the mutant distribution, yielding

$$P^s(f) = \frac{f P^m(f)}{1 - \int_0^{f_{\max}} df P^m(f) + \int_0^{f_{\max}} df f P^m(f)}. \quad (\text{S3})$$

The above form reflects the fact that the ancestors after the mutation step, comprising a fraction  $1 - \int_0^{f_{\max}} df P^m(f)$  of the total, have fitness 1, and mutants with fitness  $f$  have a chance of surviving into the next generation proportional to  $f$ . In order for the system to be in a stationary state, the distribution  $P^s(f)$  in the next generation must end up being the same as the starting distribution  $P(f)$  in the current generation. Using **Eqs. (S1)-(S3)**, we can express the condition  $P^s(f) = P(f)$  compactly as

$$P(f) = \frac{f[(1-\mu)P(f) + \mu\rho_\alpha(f)]}{1-\beta}, \quad (\text{S4})$$

where  $\beta \equiv \int_0^{f_{\max}} df (1-f)[(1-\mu)P(f) + \mu\rho_\alpha(f)]$ . **Eq. (S4)** can be solved for  $P(f)$ ,

$$P(f) = \frac{f\mu\rho_\alpha(f)}{1-\beta-f(1-\mu)}. \quad (\text{S5})$$

Note that both  $\alpha$  and  $\beta$  on the right-hand side of **Eq. (S5)** depend implicitly on  $P(f)$ . In order for the solution to be self-consistent, we plug **Eq. (S5)** into the definitions of  $\alpha$  and  $\beta$ , which leads to a closed system of equations for these two quantities:

$$\alpha = \int_0^{f_{\max}} df \frac{f\mu\rho_\alpha(f)}{1-\beta-f(1-\mu)}, \quad \beta = \int_0^{f_{\max}} df \frac{(1-\beta)(1-f)\mu\rho_\alpha(f)}{1-\beta-f(1-\mu)}. \quad (\text{S6})$$

The equation for  $\beta$  is satisfied exactly when  $\beta = \mu$ , using the fact that  $\int_0^{f_{\max}} df \rho_\alpha(f) = 1$ . Plugging  $\beta = \mu$  into the  $\alpha$  equation, we can carry out the integral analytically, leading to the following relation:

$$\alpha = \frac{\mu}{\alpha(\alpha-1)(1-\mu)(1-f_c)f_{\max}} \left[ \alpha f_c \left( \ln[\alpha(f_c-1)+1] \right. \right. \\ \left. \left. - \ln[\alpha(f_c+f_{\max}-1)-f_{\max}+1] + (\alpha-1)f_{\max} \right) - (\alpha-1) \left( \ln[\alpha(f_c-1)+1] \right. \right. \\ \left. \left. + (f_{\max}-1) \ln[\alpha(f_c+f_{\max}-1)-f_{\max}+1] + \alpha f_{\max} \right) \right. \\ \left. + ((\alpha-1)f_{\max}+1) \ln[(\alpha-1)f_{\max}+1] \right]. \quad (\text{S7})$$

437 There is no explicit analytical solution for  $\alpha$  from the above equation, but there are ways to derive approximate solutions that  
 438 work in different limits. We consider two such limits in turn.

**Small mutant fractions ( $\mu \ll 1$ ):** When  $\mu \ll 1$ , the mean number of mutants in the population becomes small, and their fraction  $\alpha$ , given by the solution of **Eq. (S7)**, scales like  $\alpha \propto \mu$ . In this limit **Eq. (S7)** gives us  $\alpha = \mu(-f_{\max}^{-1} \ln(1 - f_{\max}) - 1) + \mathcal{O}(\mu^2)$ , so we get an approximate expression for the total mutant fraction (main text Eq. (3)):

$$N_{\text{mut}}^{\text{eco}} \approx N\mu \left( -\frac{\ln(1 - f_{\max})}{f_{\max}} - 1 \right) \quad \text{for } \mu \ll 1. \quad (\text{S8})$$

To leading order in  $\mu$ , we can approximate the stationary distribution of mutant fitnesses in **Eq. (S5)** as (main text Eq. (5)):

$$P(f) \approx \frac{f\mu}{f_{\max}(1-f)} \quad \text{for } \mu \ll 1. \quad (\text{S9})$$

439 Note that since  $\alpha \ll 1$ ,  $\rho_{\alpha}(f) \approx \rho_0(f)$ , and the distribution of instantaneous fitnesses  $f$  in **Eq. (S9)** is approximately also the  
 440 distribution of ecological fitnesses  $f_e$ . In order for **Eq. (S9)** to be normalizable, and hence its integral giving **Eq. (S8)** to be  
 441 well-defined, we need  $f_{\max}$  strictly smaller than 1. In the numerical simulations only a finite number of mutants are sampled  
 442 overall during the course of the evolutionary trajectories, and an effective value of  $f_{\max} \approx 0.995$  was found to provide good fits  
 443 between the theory and simulation results.

444 **Large mutant fractions ( $\mu \lesssim 1$ ):** We would like to extend the results above to larger values of  $\mu$  and  $\alpha$ , to cover simulation cases where the mutant fractions  $\alpha$  are on the order of 10% of the total. We note that as  $\alpha$  gets larger, the distribution of new mutant fitnesses  $\rho_{\alpha}(f)$  in **Eq. (S2)** gets increasingly suppressed at fitnesses near zero and  $f_{\max}$ . This makes the precise value of  $f_{\max}$  less important for determining  $\alpha$ , and we can approximate **Eq. (S7)** by taking the  $f_{\max} \rightarrow 1$  limit. If we then keep the expressions to leading order in  $\mu$ , assuming that  $\alpha \sim \mathcal{O}(\mu)$ , **Eq. (S7)** becomes

$$\alpha \approx \frac{\mu}{1-f_c} ((f_c - 1) \ln(\alpha) + f_c \ln f_c). \quad (\text{S10})$$

The solution to this equation has the form

$$\alpha \approx \mu W \left( \left( \mu f_c^{f_c/(f_c-1)} \right)^{-1} \right). \quad (\text{S11})$$

445 Here  $W(x)$  is the Lambert  $W$  function, which is the solution  $y$  of the equation  $ye^y = x$ . For  $x > 0$  (which is the only case that  
 446 arises in our problem) the function is single-valued (the so-called zero branch of the solution).

While **Eq. (S11)** works in the  $f_{\max} \rightarrow 1$  limit, ideally we would like an expression that works for  $f_{\max}$  close to, but not exactly 1, and for the entire range of  $\mu \lesssim 1$  including small  $\mu$ . Since we know  $N_{\text{mut}}^{\text{eco}} = N\alpha$  for  $\mu \ll 1$  and  $f_{\max} < 1$  from **Eq. (S8)**, we posit the following approximate form for  $N_{\text{mut}}^{\text{eco}}$  (main text Eq. (4)):

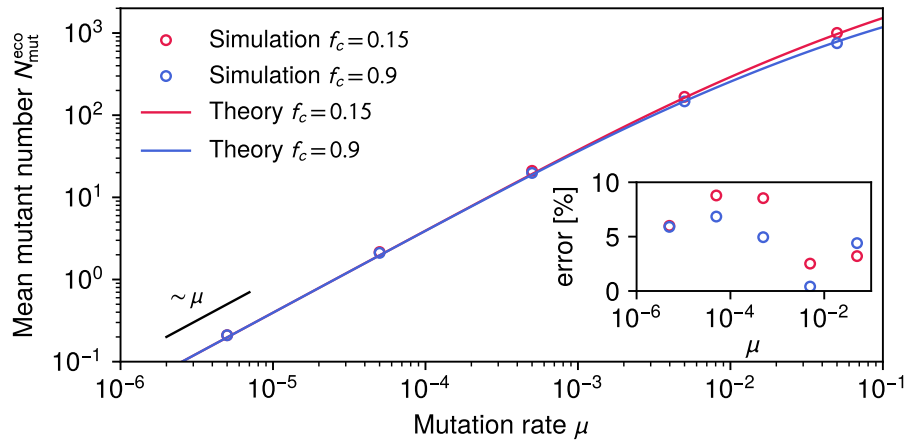
$$N_{\text{mut}}^{\text{eco}} \approx \frac{N\mu}{f_{\max}} W \left( \left( 1 - f_{\max} + \mu f_c^{f_c/(f_c-1)} \right)^{-1} \right). \quad (\text{S12})$$

447 By construction this is consistent with **Eq. (S11)** when  $f_{\max} \rightarrow 1$ . When  $1 - f_{\max}$  is small but nonzero and  $\mu \ll 1$ , we can use  
 448 the fact that  $W(x)$  diverges like  $\ln x$  for large positive  $x$  to see that **Eq. (S12)** gives  $N_{\text{mut}}^{\text{eco}} \approx -N\mu f_{\max}^{-1} \ln(1 - f_{\max})$  for  $\mu \rightarrow 0$ .  
 449 This recovers the dominant contribution in Eq. (S8) when  $1 - f_{\max}$  is small.

450 Thus in principle **Eq. (S12)** should work for a wide range of  $\mu$  and different values of  $f_c$ . **Fig. S2** depicts a comparison of  
 451 **Eq. (S12)** to simulation results, and the analytical approximation is within 10% of the numerical value across five decades of  $\mu$   
 452 and both small and large  $f_c$  (as shown by the errors shown in the inset). For small  $\mu$  the  $N_{\text{mut}}^{\text{eco}}$  curves start out independent of  $f_c$   
 453 and proportional to  $\mu$ , as expected from **Eq. (S8)**. With increasing  $\mu$ , the curves bend downwards in a way that depends on  $f_c$ ,  
 454 as the population of mutants becomes a non-negligible fraction of the total.

**Non-uniform ecological/intrinsic fitness distributions:** The derivations above can be easily extended to non-uniform distributions of the ecological and/or intrinsic fitnesses. This modifies the shape of  $\rho_{\alpha}(f)$ , depending on the specific distributions from which  $f_i$  and  $f_e$  are drawn for new mutants. In general, imagine  $f_e$  is drawn from a distribution  $\rho_0(f_e)$ , like the Gaussian example considered in the main text. In the limit  $\mu \ll 1$ , when the total mutant fraction  $\alpha$  is small, **Eq. (S9)** for the distribution becomes (main text Eq. (6)):

$$P(f_e) \approx \frac{f_e \mu}{(1 - f_e)} \rho_0(f_e) \quad \text{for } \mu \ll 1. \quad (\text{S13})$$



**Figure S2.** Comparison of the approximate analytical theory, **Eq. (S12)** (curves), and the simulation results (circles) for the mean number of mutants  $N_{\text{mut}}^{\text{eco}}$  as a function of mutation rate  $\mu$ . We set  $f_{\text{max}} = 0.995$ ,  $N = 10^4$ , and use two different values for the fitness cost,  $f_c = 0.15$  and  $0.9$  (red and blue respectively). The inset shows the absolute percent error of the analytical approximation with respect to the numerical values. The black line on the left shows the scaling  $N_{\text{mut}}^{\text{eco}} \propto \mu$  expected in the small  $\mu$  regime from **Eq. (S8)**.

455 Other results from the theory can be similarly generalized.

**No ecological interactions:** In the absence of ecological interactions, the fitness function  $f(\alpha) = f_i$  for all  $\alpha$ . If  $f_i$  is drawn from a uniform distribution between 0 and  $1 - f_c$ , the distribution  $\rho_\alpha(f)$  becomes uniform:  $\rho_\alpha(f) = 1/(1 - f_c)$ . An analogous calculation to the one above yields the mean number of mutants in this scenario (main text **Eq. (2)**):

$$\boxed{N_{\text{mut}}^{\text{no eco}} = N\mu \left( -\frac{\ln f_c}{1 - f_c} - 1 \right)}. \quad (\text{S14})$$

456 This number is a useful baseline for gauging the relative effectiveness of ecological interactions in enhancing mutant populations.

#### 457 Mean time to extinction of an individual mutant

458 The final quantity we would like to calculate theoretically is the mean number of generations that an individual mutant survives  
 459 after first arising. Note that if a mutant is generated by the mutation step, but does not survive the selection step immediately  
 460 afterwards, we say its lifetime is zero generations. To simplify the calculation, we consider the regime  $\mu \ll 1$ , where the chance  
 461 that a mutant disappears via a second mutation is negligible. And by the definition of the model, the same type of mutant cannot  
 462 be generated again from either the ancestor or other mutant populations. So in this regime the mutant persists with a randomly  
 463 fluctuating population until in one of the selection steps none of its population is chosen to survive to the next generation.

Let us focus on a single mutant type with fitness  $f$ . If there are  $\ell$  such mutants in the current generation, the probability  $W_{k\ell}$  that there will be  $k$  mutants of this type in the next generation is given by the binomial distribution characteristic of Wright-Fisher dynamics,

$$W_{k\ell} = \binom{N}{k} \left( 1 - \frac{f\ell}{N(1-\beta)} \right)^{N-k} \left( \frac{f\ell}{N(1-\beta)} \right)^k. \quad (\text{S15})$$

For  $\mu \ll 1$  we can assume that  $\beta \ll 1$ ,  $f \approx f_e$  and that  $N \gg k$  for any  $k$  that has a non-negligible probability, since the number of mutants of a single type at any given time will be a tiny fraction of the total. We can then approximate **Eq. (S15)** as

$$W_{k\ell} \approx \frac{(f_e \ell)^k}{k!} e^{-f_e \ell}, \quad (\text{S16})$$

464 which is just the limit in which the binomial distribution looks like a Poisson distribution. The probabilities  $W_{k\ell}$  can be  
 465 interpreted as components of an  $N \times N$  transition matrix  $W$ . Since the vast majority of this matrix will consist of probabilities  
 466 exponentially close to zero, we can focus on the states  $k, \ell = 0, \dots, M$  for some  $M \ll N$ . Thus we will consider  $W$  instead to be

467 an  $(M + 1) \times (M + 1)$  matrix, choosing  $M$  large enough to get a satisfactory approximation to the non-truncated system. This  
 468 reduces the problem to an  $(M + 1)$  state discrete time Markov process.

Note that  $W_{k0} = 0$ , so  $\ell = 0$  (extinction) is an absorbing state. From the theory of phase-type distributions<sup>56</sup>, the mean number of generations to extinction can be calculated using the  $M \times M$  submatrix  $S$  of the tranpose  $W^T$ , defined via  $S_{k\ell} = W_{\ell k}$  for  $k, \ell = 1, \dots, M$ . Starting from a population of 1 (after the mutation step) at generation zero, the mean time to extinction is given by

$$\tau(f_e) = \mathbf{z}^T (I - S)^{-1} \mathbf{e} - 1. \quad (\text{S17})$$

469 Here  $I$  is the  $M \times M$  identity matrix,  $\mathbf{z}$  is an  $M$ -dimensional vector with a 1 in the first element and zero elsewhere, and  $\mathbf{e}$  is  
 470 an  $M$ -dimensional vector with 1 for all its elements. The  $-1$  at the end of **Eq. (S17)** is due to the counting convention where  
 471 extinction during the first selection step is considered to be an extinction time of zero.

472 For a given choice of  $M$ , it turns out the matrix inverse in **Eq. (S17)** can be calculated analytically. Even though the resulting  
 473 expression becomes unwieldy for large  $M$ , it can always be Taylor expanded around  $f_e = 0$  to give relatively simple results.  
 474 The Taylor coefficient of order  $f_e^n$  in the expansion remains unchanged for any choice of  $M \geq n$ . Thus we can find the Taylor  
 475 expansion of  $\tau(f_e)$  in the non-truncated system up to any chosen order  $M$ , simply by Taylor expanding **Eq. (S17)**.

The first few terms of this Taylor expansion are:

$$\tau(f_e) = f_e + \frac{f_e^2}{2} + \frac{2f_e^3}{3} + \frac{f_e^4}{8} + \frac{19f_e^5}{30} + \frac{f_e^6}{144} + \frac{107f_e^7}{280} + \dots \quad (\text{S18})$$

While the lowest terms are sufficient to describe the mean extinction time of mutants with  $f_e \ll 1$ , progressively more terms are required to approximate  $\tau(f_e)$  as  $f_e$  approaches 1 from below. In fact, technically in this approximation the series  $\tau(f_e)$  diverges at  $f_e = 1$ , since we have effectively taken  $N \rightarrow \infty$  in **Eq. (S16)**. In practice this is not a problem since we only consider mutants with fitnesses up to  $f_{\max} < 1$ . Rather than working with the Taylor expansion directly, we constructed an analytical approximation designed to agree with the expansion through order  $f_e^3$ , and capture the divergence at large  $f_e$  (main text Eq. (1)):

$$\tau(f_e) \approx \frac{3 \ln(1 - f_e)}{f_e^2 - 3}. \quad (\text{S19})$$

476 Despite its simple form, this approximation agrees with the simulation results for  $\mu \ll 1$  across the whole range of  $f_e$  with a  
 477 typical error of 5%.