Hindawi Applied Bionics and Biomechanics Volume 2022, Article ID 4775595, 11 pages https://doi.org/10.1155/2022/4775595

Research Article

Biaxial Estimation of Biomechanical Constitutive Parameters of Passive Porcine Sclera Soft Tissue

Zwelihle Ndlovu,^{1,2} Dawood Desai ,² Thanyani Pandelani ,^{1,3} Harry Ngwangwa ,¹ and Fulufhelo Nemavhola ,¹

Correspondence should be addressed to Fulufhelo Nemavhola; masitfj@unisa.ac.za

Received 25 November 2021; Revised 22 January 2022; Accepted 9 February 2022; Published 28 February 2022

Academic Editor: Qiguo Rong

Copyright © 2022 Zwelihle Ndlovu et al. This is an open access article distributed under the Creative Commons Attribution License, which permits unrestricted use, distribution, and reproduction in any medium, provided the original work is properly cited.

This study assesses the modelling capabilities of four constitutive hyperelastic material models to fit the experimental data of the porcine sclera soft tissue. It further estimates the material parameters and discusses their applicability to a finite element model by examining the statistical dispersion measured through the standard deviation. Fifteen sclera tissues were harvested from porcine' slaughtered at an abattoir and were subjected to equi-biaxial testing. The results show that all the four material models yielded very good correlations at correlations above 96%. The polynomial (anisotropic) model gave the best correlation of 98%. However, the estimated material parameters varied widely from one test to another such that there would be need to normalise the test data to avoid long optimisation processes after applying the average material parameters to finite element models. However, for application of the estimated material parameters to finite element models, there would be need to consider normalising the test data to reduce the search region for the optimisation algorithms. Although the polynomial (anisotropic) model yielded the best correlation, it was found that the Choi-Vito had the least variation in the estimated material parameters, thereby making it an easier option for application of its material parameters to a finite element model and requiring minimum effort in the optimisation procedure. For the porcine sclera tissue, it was found that the anisotropy was more influenced by the fiber-related properties than the background material matrix-related properties.

1. Introduction

It is reported that majority of the vision impairment may be prevented or treated if caught early, and correct therapies are implemented. Globally, 86.1 million cases leading to the moderate and severe vision impairment were caused by undercorrected refractive error. Due to increase in aging population in many countries across the globe, vision impairment including uncorrected refractive error, glaucoma, and contract were reported to be in the rise. The rise in vision impairment is due to rising sociodemographic status and life expectancy witnessed in number of countries globally [1–4]. It is reported that 4.8 million and 21.4 million

people are blind and visually impaired in 48 countries of sub-Saharan Africa [5]. In addition, Africa has been reported to be carrying approximately 19% of the global blindness [6]. Blindness prevalence rates vary widely but the evidence suggests that approximately 1% of people in sub-Saharan Africa are blind [7]. Visual impairment is a significant health problem in the sub-Saharan Africa. The major eye conditions include cataracts, uncorrected refractive errors, glaucoma, age-related macular degeneration, corneal opacities, diabetic retinopathy, trachoma, and onchocerciasis [8, 9]. In addition, glaucoma is labelled as worldwide problem of the eye diseases where 111 million of individuals are projected to be affected by 2040 [10]. Therefore, it is vital that

¹Unisa Biomedical Engineering Research Group, Department of Mechanical Engineering, School of Engineering, College of Science Engineering and Technology, University of South Africa, Pretoria 0001, South Africa

²Department of Mechanical and Mechatronics Engineering, Faculty of Engineering and Built Environment, Tshwane University of Technology, South Africa

 $^{^3}$ Council for Scientific and Industrial and Research, Defence and Security Cluster, Brummeria, Pretoria 0001, South Africa

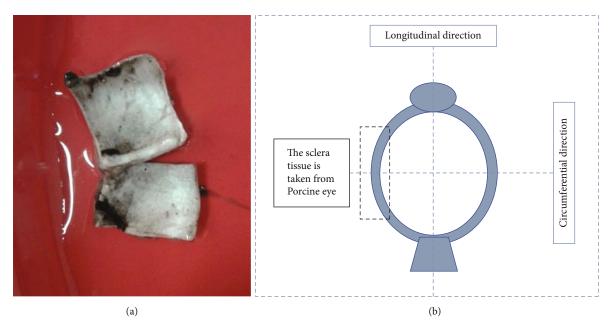


FIGURE 1: Porcine sclera tissue samples (a) cut from each eye immediately after the delivery from the abattoir to the Unisa Biomechanics Laboratories with a sketch showing how the tissue was excised from the porcine eye (b). The reference axis were defined in such a way that the longitudinal direction is from the cornea to the base while circumferential direction is 90° with the longitudinal direction.

the biomechanical properties and computational models of the eye soft tissues are developed with the view to understand the mechanisms of various diseases of the eye. Biomechanical properties of eye soft tissues are vital in improving insight into how eye diseases progress [11].

Biomechanical properties of the soft tissues have been utilised previously to study mechanical behaviour [12–14]. The progression of the diseases was also studied by developing accurate and reliable computational models [15, 16]. The detailed computational models of the eye request a thorough study of mechanical properties including the fitting of constitutive hyperelastic models. Previously, different biomechanical properties of the different ocular tissues including sclera [17-19], orbital connective tissue and fat [20, 21], cornea [22-24], and extraocular muscles [25, 26]. Sclera is normally associated with near-sightedness (myopia), and therefore, there is considerable amount of work done on the investigation of the biomechanical properties of sclera [27, 28]. In particular, the mechanical properties of the sclera are critical for the development of synthetic materials for the replacement of eye tissues. This is because globally, there is a rise of accident where organ such as eye may be lost or damaged permanently. In our previous studies, we presented the biaxial mechanical characterisation of the sheep sclera soft tissue [28]. In this study, the Fung and Choi-Vito hyperelastic constitutive models were fitted on the biaxial tensile data. Finite element modelling (FEM) has been previously utilised in studying how soft tissues behave under mechanical loading [29-35]. These constitutive parameters generated by fitting biaxial tensile data may be utilised for detailed study of diseases' progression in the eye as well as understanding pain dissemination based on the needle injection in the sclera for treatment [36, 37].

In this study, we present the biaxial biomechanical properties of the porcine sclera soft tissue. The porcine anatomy has been reported to be like that of human beings; therefore, it is believed that the biaxial mechanical data presented in this study will be useful for studying human eye diseases. Therefore, the aim of this study is to generate constitutive parameters of the porcine sclera soft tissues subjected to equi-biaxial loading. Fung, Choi-Vito, Holzapfel (2000), and polynomial (anisotropic) hyperelastic constitutive models are fitted in the equi-biaxial tensile data to estimate the constitutive material parameters. To our knowledge, there is no study that looked at utilising and comparing the Fung, Choi-Vito, Holzapfel (2000), and polynomial (anisotropic) hyperelastic constitutive models in estimating the material parameters of the porcine sclera soft tissue.

2. Methods and Materials

2.1. Sample Preparation. The sample consists of sclera (N=15) soft tissue harvested from the local abattoir with unknown ages and sexes. To preserve the mechanical properties of the sclera soft tissue, the specimen was collected within 4 to 6 hours after slaughter as discussed [38]. The detailed tissue preparation of the porcine sclera is like what we have previously presented [28]. To avoid possible deterioration of the sclera tissue including dehydration, specimen was placed in ice bag on the way to the Unisa Biomechanics Laboratory. During further processing, the unwanted ocular tissues were removed from the porcine eye using surgical blades. Two square samples of 12×12 mm (Figure 1) were cut from each eye roughly 4 to 6 mm away from the optic nerve head and corneal limbus to reduce thickness variation. Vernier caliper was then utilized to measure the thickness of

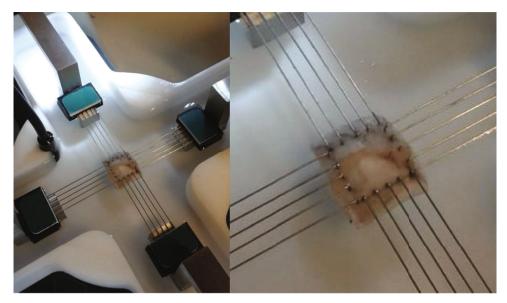


FIGURE 2: Experimental set-up of porcine sclera tissue subjected to biaxial tensile loading (Bio-Tester 5000 from Cellscale) (Waterloo, Canada). The hooks (BioRakes) were utilised in securing the sclera tissue and were punched thoroughly before they were inserted into the warm bath of isotonic solution 9.0 g/l at pH of 5.5 at a temperature of 37°C.

the sclera tissue. Randomly, the thickness of the sclera tissue was measured in four different places, and the average thickness was taken for further processing of the data. Specimens were subjected to visual inspection before individually subjected to biaxial testing equipment. Reason for visual inspection was to ensure that there was no physical damage on the tissue that may influence the mechanical data. Samples were dipped and kept in isotonic solution 9.0 g/l at pH of 5.5 for about 15 to 20 minutes before testing.

2.2. Mechanical Testing. Biaxial mechanical properties of the porcine sclera soft tissue were captured using custom-built biaxial testing device, Bio-Tester 5000 from Cellscale (Waterloo, Canada) with load capacity of 23000 mN and accuracy of 5000 μN (Figure 2). CellScale BioRakes were utilized to clamp the sclera soft tissue on all sides when equi-biaxial strain is applied. Strain rate of between 0.452 mm/s was applied during biaxial testing of each sample. To mimic the body temperature, the water bath was heated to 37°C. The temperature sensor is integrated in the custom-built biaxial device to ensure that the temperate is kept constant through testing. X and Y directions were considered as circumferential and longitudinal directions, respectively. Four (4) CellScale BioRakes were used to mount the specimens to develop mechanical properties. On both x and y directions, all fifteen (15) specimens were subjected to 25% strain using only strain-controlled mode equally in both directions.

3. Theoretical Framework

3.1. Tissue Stress-Strain Analysis. In this study, the stresses were calculated through the first Piola-Kirchoff stress T in the two directions using the equation:

$$T_{ii} = \frac{F_{ii}}{L_{i0}h_0},\tag{1}$$

where F is the load vector in directions i=1, 2, and for the current study, these indices represent longitudinal (cross-fiber-direction) and circumferential (fiber-direction) direction. The index 0 denotes the undeformed state. L represents tissue length, and h represents tissue thickness.

The finite strains were calculated by the formula:

$$\varepsilon_i = \frac{L_i - L_{i0}}{L_{i0}}. (2)$$

The stress results in Equation (1) are however noisy; therefore, they were further filtered with an 8-point moving average filter in Excel. The data were resampled and further smoothened using a quadratic function.

3.2. Constitutive Modelling. The passive response of a biological soft tissue is more complex than the response of elastic solids due to the fact that they undergo finite deformations under mechanical loads [39, 40]. Thus, the passive phases of tissues' deformations are considered using the nonlinear theory of hyperelasticity. The most useful quantity in deriving the expressions for the passive response of materials that undergo finite deformation is the strain energy function [40]. There is a huge number of variations of its implementation in the literature depending on different cases. In this study, we assume that the tracheal tissue is anisotropic and incompressible; therefore, we apply and study the material parameters from six models, namely, the Fung, Choi-Vito, Holzapfel (2000), and polynomial (anisotropic) models. In the following sections, these models are presented in terms of their strain energy functions.

3.2.1. The Fung Model. The Fung model is a hyperelastic anisotropic material model for stress-strain description of arterial wall. It is phenomenological in nature and its incompressible form is given by [41].

Table 1: The classification of the four hyperelastic anisotropic material models according to the material properties they represent. The Fung and Choi-Vito are classified as the models that model the soft tissue as layers of general material matrix, while the polynomial (anisotropic) and Holzapfel (2000) models are those that model the soft tissue as composite material with embedment of fiber structures within the layers of material matrix.

Model	Stress-like material parameter	Dimensionless material parameter	Stress-like material parameter referred to material matrix property	Stress-like material property referred to fiber property	Dimensionless material property referred to fiber property	Material parameter referred to fiber angle orientation
Polynomial (anisotropic)			$\checkmark (a_i, b_j)$	$\checkmark (c_k)$		√ (φ)
Fung	√ (c)	$\checkmark (b_i, i = 1 \cdots 6)$				
Choi-Vito	$\checkmark (b_0)$	$\checkmark (b_i, i = 1 \cdots 3)$				
Holzapfel 2000			√ (µ)	$\checkmark (c_1)$	$\checkmark (c_2)$	$\checkmark (\varphi)$

$$W = \frac{c}{2} (e^{Q} - 1),$$

$$Q = b_{1} E_{\theta\theta}^{2} + b_{2} E_{ZZ}^{2} + b_{3} E_{RR}^{2} + 2b_{4} E_{\theta\theta} E_{ZZ}$$

$$+ 2b_{5} E_{ZZ} E_{RR} + 2b_{6} E_{RR} E_{\theta\theta},$$
(3)

where $E_{ij}(i, j = \theta, Z, R)$ are the Green strain components and (θ, Z, R) are the cylindrical coordinates in the radial, circumferential, and axial reference directions, respectively. c stress-like material parameter and b_i are the nondimensional material parameters.

3.2.2. Choi-Vito Model. Choi-Vito model is hyperelastic anisotropic material model developed for canine pericardium. The model is fully phenomenological and formulated through the components of Green-Lagrange strain tensor. The model is implemented in an exponential format, and its strain-energy function is expressed as [42]

$$W = b_0 \left[\exp \left(b_1 E_{\theta\theta}^2 \right) + \exp \left(b_2 E_{ZZ}^2 \right) + \exp \left(2 b_3 E_{\theta\theta} E_{ZZ} \right) - 3 \right], \tag{4}$$

where b_i are the material parameters.

3.2.3. The Holzapfel (2000) Model. This model is hyperelastic anisotropic material model for stress-strain description of arterial layers. It is constituted by forms of the strain energy function that represent isotropy and anisotropy. Thus, its strain energy function is given by [43].

For incompressible formulation:

$$W_{f(I_1,I_4,I_6)} = \frac{\mu}{2}(I_1 - 3) + \frac{c_1}{2c_2} \sum_{i=4.6} \left(\exp^{c_2(I_i - 1)^2} - 1 \right), \quad (5)$$

where the constant μ is associated with the noncollagenous matrix of the material, which describes the isotropic part of the overall response of the tissue. The constants c_1 and c_2 are associated with the anisotropic contribution of collagen to the overall response of the tissue. The material parameters are constants and do not depend on the geometry, opening angle, or fiber angle. The model is implemented in an exponential format, and I_1 , I_4 , and I_6 are (pseudo-) invariants of C (G_0 and H_0). G_0 , H_0 are structural tensors referenced to individual family of fibers.

3.2.4. The Polynomial (Anisotropic) Model. Like its name, this model is hyperelastic anisotropic material model whose strain energy function is expressed as a polynomial series of isotropic and anisotropic strain invariants given as [44]

$$W = \sum_{i=1}^{3} a_i (I_1 - 3)^i + \sum_{j=1}^{3} b_j (I_2 - 3)^j + \sum_{k=2}^{6} c_k (I_4 - 1)^k + \sum_{m=2}^{6} e_m (I_6 - 1)^m,$$
(6)

where a_i , b_j , are stress-like material parameters referenced to isotropic (matrix) properties. c_k , and e_m are stress-like material parameters referenced to anisotropic (fiber) properties. I_1 , I_2 , I_4 , and I_6 are (pseudo-)invariants of C (\mathbf{A}_0 and \mathbf{B}_0). \mathbf{A}_0 , \mathbf{B}_0 are structural tensors referenced to individual family of fibers. \mathbf{C} is right Cauchy-Green definition tensor.

The four material models are classified further according to the type of material parameters that they represent in Table 1. From the table, the models can be grouped into two main classes: those that model the soft tissue as layers of general material matrix and those that model the soft tissue as composite material with embedment of fiber structures within the layers of material matrix. These models may also be classified into purely phenomenological or structural scenario. Material parameter defining the orientation angle of fibers (measured from axis "1") in the undeformed configuration is included in the analysis. In this analysis, both the *x* and *y* directions were plotted simultaneously including the fibre angle term.

3.3. Data Analysis. In this study, we use the constrained optimisation by linear approximation algorithm (COBYLA $(3^{rd} \text{ party: SciPy}))$ implemented in Hyperfit software for fitting the equi-biaxial tensile experimental data of Fung, Choi-Vito, Holzapfel (2000), and polynomial (anisotropic) hyperelastic constitutive models given in Equations (3)–(6). The coefficient of determination, R^2 , which measures the correlation of one variable with another, is evaluated for each model. The coefficient of determination (R^2) (also known as Nash-Sutcliffe coefficient) is defined as follows [45–47]:

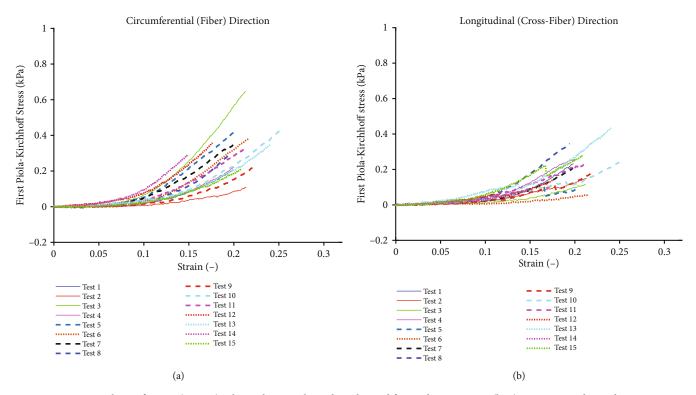


FIGURE 3: Porcine sclera soft tissue (N = 18) subjected to equi-biaxial mechanical forces showing stress (kPa) vs. strain mechanical properties up to 25% strain (a) circumferential and (b) longitudinal. Test 3 and test 4 are showing the lowest and highest tress in the circumferential direction, respectively. Additionally, test 1 is showing the highest stress, and test 15 is showing the lowest stress in the longitudinal direction, respectively.

$$R^{2} = 1 - \frac{\sum_{i=1}^{n} (y_{e} - y_{m})^{2}}{\sum_{i=1}^{n} (y_{e} - \overline{y_{e}})^{2}},$$
 (7)

where y_e is the experimental data, y_m is the model predicted data, $\overline{y_e}$ is the average value of the experimental data, the indices i, \dots, n denote the data points, and $R^2 \epsilon \langle -\infty, 1 \rangle$, where a perfect fit is defined for $R^2 = 1$.

4. Results

Stress-strain curves for the porcine sclera soft tissue subjected to equi-biaxial tensile loading are plotted in Figure 3. The stress-strain curves for porcine sclera soft tissue show that the tissue has a well-defined nonlinear behaviour as the tissue gets stretched from the toe region to 25% strain.

This study is aimed at estimating the biomechanical material parameters of a porcine sclera using four different constitutive material models, namely, Fung, Choi-Vito, Holzapfel (2000), and polynomial (anisotropic) models. All the above material models are hyperelastic anisotropic models which employ different modelling frameworks as presented in Equations (3)–(6) in Section 3.2. The material parameters for each model for all the fifteen tests are given in Tables 2–4. The tabulated results show that all the models yield very good correlations at greater than 96% with standard deviations of less than 3.2%. This implies that the model predictions were

very close to the mean stress-strain curves for all the four models in this study.

However, the polynomial (anisotropic) model yielded the best correlation at an average of 98.3% and an average standard deviation of approximately 1.73%, while the Fung model yielded the lowest average correlation of 96.4% with an average standard deviation of 3.2%. The Choi-Vito and Holzapfel models had similar average correlations of 97.2% with average standard deviations of 1.65% and 2.98%, respectively.

In terms of statistical dispersion in the estimated material parameters by the four models, the polynomial (anisotropic) model had the largest variance with the widest scatter in the material parameters over the fifteen different tests. An evaluation of the standard deviation percentage yielded deviations from 110% to 660% for the polynomial (anisotropic) model. On the other hand, the Choi-Vito model had the smallest variance in the material parameters with deviations between 31% and 91%. This result might not be surprising considering that the Choi-Vito model was originally formulated for the pericardium tissue [42, 48, 49] which, in much respect, may be similar in functionality to the sclera tissue. The implications of such deviations in terms of applying the estimated average material parameters directly to finite element (FE) models is problematic, and this has been discussed in the next section. From Figure 4, the polynomial (anisotropic) constitutive model yields the highest R^2 of 0.983 while the Fung constitutive model yields the lowest R^2 of 0.964. On the other hand,

Table 2: Estimated material parameters of porcine sclera soft tissue loaded biaxially using Fung hyperelastic constitutive model including the
coefficient of determination (R^2) of each specimen $(N = 15)$. The average constitutive $(c, b_1, b_2, b_3, b_4, b_5, b_6, and R^2)$ parameters are also included.

Test #	R^2	С	b_1	b_2	b_3	b_4	b_5	b_6
S1	0.985	1.527	1.264	1.228	-0.655	0.375	0.243	0.329
S2	0.959	1.533	0.952	1.139	-0.420	0.460	0.569	-0.027
S3	0.993	1.050	1.200	1.178	-0.118	0.533	0.379	0.628
S4	0.900	0.137	3.965	1.971	-1.625	2.864	1.851	-1.999
S5	0.971	0.500	1.924	2.824	-0.643	1.242	1.147	0.739
S6	0.907	0.791	1.293	0.801	-0.345	1.038	0.630	0.289
S7	0.915	0.822	3.911	1.877	1.002	2.527	2.473	0.068
S8	0.957	0.929	1.299	0.902	-0.388	1.071	0.563	0.513
S9	0.993	0.558	2.701	3.301	1.488	3.039	2.612	2.439
S10	0.983	0.158	4.686	3.439	-0.125	2.827	1.727	2.578
S11	0.960	0.960	1.102	0.808	-0.130	0.298	0.297	0.260
S12	0.983	1.286	1.000	0.857	-0.335	0.390	0.265	0.283
S13	0.990	1.286	1.671	0.601	-0.280	1.123	0.507	0.614
S14	0.983	1.026	0.976	1.200	-0.374	1.074	0.635	0.465
S15	0.984	0.910	1.517	0.679	-0.318	1.111	0.442	0.546
Average	0.964	0.898	1.964	1.520	-0.218	1.331	0.956	0.515
STD	0.031	0.413	1.202	0.921	0.679	0.949	0.783	1.002

Table 3: Estimated material parameters of porcine sclera soft tissue loaded biaxially using Choi-Vito hyperelastic constitutive model including the coefficient of determination (R^2) of each specimen (N=15). The average constitutive (c, b_1 , b_2 , b_3 , and R^2) parameters are also included.

Table 4: Estimated material parameters of porcine sclera soft tissue loaded biaxially using Holzapfel (2000) hyperelastic constitutive model including the coefficient of determination (R^2) of each specimen (N=15). The average constitutive (c, b_1 , b_2 , b_3 , and R^2) parameters are also included.

Test #	R^2	С	b_1	b_2	b_3	Test #	R^2	μ	k_1	k_2	φ
S1	0.979	0.004	3.180	11.421	39.018	S1	0.982	0.000	0.039	9.303	0.814
S2	0.956	0.006	-2.627	10.015	21.673	S2	0.972	0.000	0.036	5.250	2.240
S3	0.967	0.011	21.724	26.703	11.276	S3	0.984	0.000	0.098	6.017	-0.389
S4	0.985	0.017	39.952	17.770	9.632	S4	0.974	0.000	0.059	7.572	0.856
S5	0.981	0.024	23.364	27.074	17.790	S5	0.864	0.068	0.048	7.676	0.311
S6	0.935	0.011	47.858	17.579	6.936	S6	0.976	0.000	0.052	6.142	-0.362
S7	0.974	0.012	40.348	14.985	14.470	S7	0.980	0.000	0.081	6.658	0.630
S8	0.976	0.018	36.901	25.357	14.662	S8	0.983	0.000	0.077	8.141	0.854
S9	0.990	0.022	29.680	34.177	23.643	S9	0.975	0.000	0.042	5.971	0.755
S10	0.983	0.029	17.587	16.756	15.163	S10	0.978	0.000	0.078	3.696	0.649
S11	0.981	0.015	27.327	19.054	2.194	S11	0.978	0.000	0.091	4.981	0.723
S12	0.985	0.039	20.816	18.381	13.656	S12	0.980	0.000	0.116	7.329	0.457
S13	0.969	0.036	34.998	18.118	15.893	S13	0.980	0.000	0.078	7.284	0.778
S14	0.994	0.093	14.175	14.101	13.318	S14	0.982	0.013	0.083	8.418	0.549
S15	0.946	0.024	31.969	14.387	2.134	S15	0.990	0.000	0.101	3.848	0.854
Average	0.972	0.023	26.141	20.467	15.324	Average	0.972	0.005	0.074	6.767	0.654
STD	0.016	0.021	13.494	6.348	8.741	STD	0.029	0.017	0.024	2.263	0.562

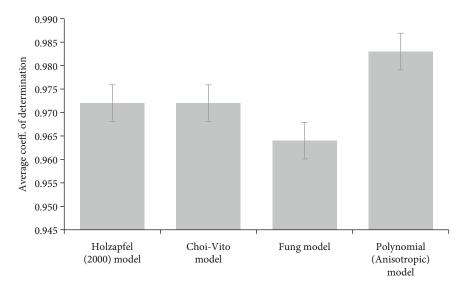


FIGURE 4: Average coefficient of determination (R^2) (with standard error) of the porcine soft tissue sclera calculated for Holzapfel (2000), Choi-Vito, Fung, and polynomial (anisotropic) hyperelastic constitutive models, with polynomial (anisotropic) constitutive model showing the highest R^2 of 0.983 and the lowest R^2 of 0.964 observed for Fung constitutive model.

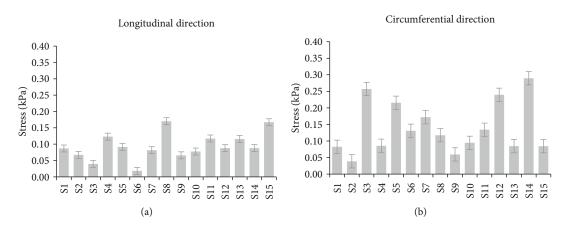


FIGURE 5: First Piola-Kirchhhoff stress (kPa) values taken at 15% engineering strain of the porcine soft tissue subjected to biaxial tension in two loading directions: (a) longitudinal and (b) circumferential.

Figure 5 shows that the porcine sclera soft tissue was found to be much stiffer in the circumferential direction with stress values taken at 15% strain.

5. Discussion

The results of correlations between model predictions and tests presented in Section 4 should never be taken at face value. It should be noted that a model is applied to a given set of experimental data from which the material parameters are estimated. Thus, each material model is optimised for each fresh set of experimental data with totally different target values, and therefore, it is likely to yield material parameters that are different from those obtained from the other tests. This is where some form of calibration may become necessary to eliminate huge variances in the model parameters from one test to another [50–53]. Dubuis et al. [54] employed a calibration technique in which the FE itself was calibrated using 3D CT scans.

Therefore, in applying the average material parameters obtained here to an FE model, one may need to consider implementing an optimisation procedure in which these average values may be used as seed values [55]. Kollmann et al. [55] applied such methods for optimisation of the parameters used in FE modelling of asphalt mixtures. For models with large numbers of material parameters such as the polynomial (anisotropic) model in this study, it might be prudent to conduct an initial sensitivity analysis to determine the most influential material parameters. Biaxial tensile testing has been utilised in understanding the mechanical properties of soft tissues. Additionally, hyperelastic constitutive models have also been presented by fitting the constitutive models of the various soft tissues including heart myocardium [56–58] and omasum [59].

Despite the highest correlation obtained for the polynomial (anisotropic) model, the direct application of its parameters to an FE model can yield huge errors due to the wide scatter of its material parameters. One may need to prescribe

Table 5: Estimated material parameters of porcine sclera soft tissue loaded biaxially using polynomial (anisotropic) hyperelastic constitutive model including the coefficient of determination (R^2) of each specimen (N = 15). The average constitutive (a_1 , a_2 , a_3 , b_1 , b_2 , b_3 , c_2 , c_3 , c_4 , c_5 , c_6 , φ , and R^2) parameters are also included.

	R^2	a_1	a_2	a_3	b_1	b_2	b_3	c_2	c_3	c_4	c_5	<i>c</i> ₆	φ
S1	0.953	0.045	0.014	0.035	-0.002	-0.003	-0.002	-0.027	-0.007	-0.018	-0.010	0.994	0.944
S2	0.976	0.023	0.048	0.039	0.000	0.001	-0.005	-0.015	0.001	0.006	0.010	0.022	0.003
S3	0.983	-0.011	0.102	-0.072	-0.220	-0.089	-0.133	-0.005	0.074	0.201	0.174	-0.259	0.268
S4	0.954	0.018	0.055	-0.051	0.035	0.031	0.021	0.011	-0.022	-0.041	-0.040	1.217	0.911
S5	0.948	0.006	0.216	-0.302	-0.095	-0.042	0.007	-0.039	0.150	0.035	0.050	-0.011	0.016
S6	0.990	0.010	-0.016	0.074	0.233	-0.158	0.186	-0.008	-0.018	0.247	0.394	-0.825	-0.083
S7	0.997	0.014	0.007	0.298	-0.118	-0.285	-0.112	-0.038	0.245	-0.217	-0.004	-0.019	0.199
S8	0.998	0.003	0.225	0.206	-0.305	0.319	-0.283	0.006	-0.096	0.195	-0.325	0.310	-0.089
S9	0.991	0.004	0.087	0.039	0.012	-0.082	0.026	-0.005	-0.006	0.024	0.016	0.015	-0.056
S10	0.993	0.015	0.093	0.006	-0.043	0.008	-0.004	0.000	-0.046	0.154	0.048	-0.147	-0.085
S11	0.998	0.008	0.201	-0.061	-0.425	0.155	0.060	-0.012	0.020	0.081	-0.155	0.180	0.216
S12	0.989	0.028	-0.011	0.075	-0.289	-0.477	-0.220	-0.004	0.003	0.465	0.198	-0.928	0.460
S13	0.989	0.028	-0.011	0.075	-0.289	-0.477	-0.220	-0.004	0.003	0.465	0.198	-0.928	0.460
S14	0.992	-0.013	0.081	-0.707	0.254	-0.952	0.325	0.031	-0.058	0.762	0.610	-4.150	0.592
S15	0.991	-0.001	0.375	-0.293	0.335	-0.371	0.014	-0.003	-0.032	-0.166	0.269	0.152	0.081
Average	0.983	0.012	0.098	-0.043	-0.061	-0.161	-0.023	-0.007	0.014	0.146	0.096	-0.292	0.256
STD	0.017	0.015	0.108	0.233	0.215	0.301	0.152	0.017	0.082	0.250	0.217	1.185	0.337

Table 6: Fitting of hyperelastic models (N = 15) showing box plot properties of the coefficient of determination (R^2) with Q1, median, and Q3 values.

	Polynomial model	Fung model	Choi-Vito model	Holzapfel (2000) model
Min	0.948	0.900	0.935	0.864
Q1	0.980	0.958	0.968	0.976
Median	0.990	0.983	0.979	0.980
Q3	0.993	0.985	0.984	0.982
Max	0.998	0.993	0.994	0.990
IQR	0.013	0.027	0.016	0.006

huge range of its parameter space within which the optimisation algorithm can search for the optimal material parameters to give accurate correlation for any given random test. Among the four material models in this study, the Choi-Vito model offers the best chance for attaining accurate correlations when directly applied to an FE model with minimal effort of optimisation. For the Choi-Vito model, only the stress-like material parameter may take more time in searching for optimal material parameter at 91% deviation from the mean value. Apart from the average value given in Table 3, the other best value from which to start the search for the stress-like material parameter for the Choi-Vito may be the gradient of the linear elastic portion of the stress-strain curve.

In terms of general material matrix anisotropy, both the Fung and Choi-Vito models do not show that the porcine sclera tissue is heavily anisotropic between the circumferential and longitudinal direction. However, the tissue seems to be different in material matrix in the radial direction from the Fung model. The values of a_i and b_j which also represent the material matrix properties in the polynomial (aniso-

tropic) model show that there is no significant anisotropy between the circumferential and longitudinal directions. On the other hand, the c_k material parameters in the polynomial (anisotropic) model and the k_i parameters in the Holzapfel (2000) model, all of which represent material parameters related with fiber properties, exhibit significant anisotropy in Tables 5 and 4. This implies that the anisotropy in the porcine sclera tissue is mainly due to different fiber properties between the circumferential and longitudinal directions and not the background material matrix properties. It is difficult to establish in this study if the fiber orientation angle had any influence on the accuracy of the correlations in the polynomial (anisotropic) and Holzapfel (2000) models. This can be better investigated through the sensitivity analysis. Table 6 shows the box plot properties of the coefficient of determination (R^2) having Q1, median, and Q3. It is clear from the table that the four models have approximately equal coefficients of determination with the Fung and Holzapfel (2000) models exhibiting the largest and lowest ranges in the R^2 values as represented by the IQR values.

6. Conclusion

The study applies four different hyperelastic material models to estimate the material parameters for the computational modelling of porcine sclera tissue. It is found that all the four material models produce very good correlations higher than 96% with the polynomial (anisotropic) model yielding the highest correlation of 98%. However, the variation of the material parameters from one test to another is a challenge as far as their direction application to FE models is concerned. For example, the polynomial (anisotropic) model has the minimum standard deviation of its material parameters from one test to another as 110%. Thus, the average material parameters obtained in this paper may result in inaccurate correlations in the FE predicted results. One way to deal with this challenge is to implement an optimisation routine which uses these material parameters as seed values. However, with such large spread in the parameter space, the search algorithm may take too long to converge especially with material models that have large numbers of estimated material parameters. Therefore, it is proposed that the test data should also be normalised or calibrated before application of the constitutive material models to reduce the variation in the estimated parameters thereby reducing the search region. In this study it is also found that the Choi-Vito model has the least variation in its material parameters. Thus, it might offer much better chance than the other models for convergence to material parameters that can yield very good correlations for the FE model. In terms of the models that are based on fiber-property formulation as identified in Table 1, the Holzapfel (2000) model offers a better option as compared to the polynomial (anisotropic) model for faster convergence as its material variation is much lower between the two models. As far as anisotropy in the porcine sclera tissue is concerned, both the polynomial (anisotropic) model and the Holzapfel (2000) model show that the fiber properties have more influence than the background material matrix. It is not clear if the angle of fiber orientation has any influence in the results. This might require more investigation.

7. Limitation

The limitation of this experimental study is that it did not segment porcine sclera per region. The thickness of porcine sclera samples used in this work was unknown. This may lead to unclear results since it was reported that some regions in the sclera exhibit anisotropy while others do not. However, it has been reported that porcine and human sclera behave in the same way despite a difference in tissue thickness. The two tissues are similar in terms of structure, histology, and collagen fiber architecture and should have similar material properties and will be useful for studying human eye diseases [60].

No imaging/microscopy was done in this study; hence, the fiber direction cannot be determined with certainty. It has previously been observed that the porcine sclera has a blood vessel that travels parallel to the ora serrata [61]. This vessel could introduce stiffening of one fiber direction and can result in different material properties compared to another fiber direction.

Further studies should be conducted to confirm human and porcine similarities with regard to material properties. Porcine sclera is easily available and can be an efficient substitute for human sclera material properties, in computational modelling.

Data Availability

All data is available in the main manuscript.

Additional Points

Correspondence and requests for materials should be addressed to F.N. Reprints and permissions information is available at http://www.nature.com/reprints.

Conflicts of Interest

The authors declare no conflict of interests.

Authors' Contributions

Fulufhelo Nemavhola, Harry M Ngwangwa, Zwelihle Ndlovu, Dawood Desai, and Thanyani Pandelani contributed to conception, design, and interpretation of the data. This first version of the manuscript was authored by Zwelihle Ndlovu. Thanyani Pandelani and Fulufhelo Nemavhola contributed to the interpretation of the constitutive models and critically revised the manuscript. Dawood Desai, Fulufhelo Nemavhola, Harry M Ngwangwa, and Thanyani Pandelani contributed to conception and design of the research. All authors gave final approval for the submission of the manuscription and agreed to be accountable for all aspects of the work.

Acknowledgments

Support from the National Research Foundation (NRF) grant number (129380) is gratefully acknowledged. UNISA CAPEX Programme supported the acquisition of biaxial testing machine in the Department of Mechanical Engineering, School of Engineering, College of Science Engineering and Technology.

References

- [1] J. D. Steinmetz, R. R. A. Bourne, P. S. Briant et al., "Causes of blindness and vision impairment in 2020 and trends over 30 years, and prevalence of avoidable blindness in relation to VISION 2020: the right to sight: an analysis for the global burden of disease study," *The Lancet Global Health*, vol. 9, no. 2, pp. e144–e160, 2021.
- [2] S. R. Flaxman, R. R. A. Bourne, S. Resnikoff et al., "Global causes of blindness and distance vision impairment 1990-2020: a systematic review and meta-analysis," *The Lancet Global Health*, vol. 5, no. 12, pp. e1221–e1234, 2017.
- [3] L. Pezzullo, J. Streatfeild, P. Simkiss, and D. Shickle, "The economic impact of sight loss and blindness in the UK adult

- population," BMC Health Services Research, vol. 18, no. 1, pp. 1–13, 2018.
- [4] P. A. Reddy, N. Congdon, G. MacKenzie et al., "Effect of providing near glasses on productivity among rural Indian tea workers with presbyopia (PROSPER): a randomised trial," *The Lancet Global Health*, vol. 6, no. 9, pp. e1019–e1027, 2018.
- [5] G. A. Stevens, R. A. White, S. R. Flaxman et al., "Global prevalence of vision impairment and blindness," *Ophthalmology*, vol. 120, no. 12, pp. 2377–2384, 2013.
- [6] K. Naidoo, "Poverty and blindness in Africa," Clinical and Experimental Optometry, vol. 90, no. 6, pp. 415–421, 2007.
- [7] S. Lewallen and P. Courtright, "Blindness in Africa: present situation and future needs," *British Journal of Ophthalmology*, vol. 85, no. 8, pp. 897–903, 2001.
- [8] R. R. Buhrmann, H. A. Quigley, Y. Barron, S. K. West, M. S. Oliva, and B. B. Mmbaga, "Prevalence of glaucoma in a rural East African population," *Investigative Ophthalmology & Visual Science*, vol. 41, no. 1, pp. 40–48, 2000.
- [9] S. Dastjerdi, B. Akgöz, and Ö. Civalek, "On the shell model for human eye in glaucoma disease," *International Journal of Engineering Science*, vol. 158, article 103414, 2021.
- [10] Y.-C. Tham, X. Li, T. Y. Wong, H. A. Quigley, T. Aung, and C. Y. Cheng, "Global prevalence of glaucoma and projections of glaucoma burden through 2040: a systematic review and meta-analysis," *Ophthalmology*, vol. 121, no. 11, pp. 2081– 2090, 2014.
- [11] M. Ferrara, G. Lugano, M. T. Sandinha, V. R. Kearns, B. Geraghty, and D. H. Steel, "Biomechanical properties of retina and choroid: a comprehensive review of techniques and translational relevance," *Eye*, vol. 35, pp. 1818–1832, 2021.
- [12] H. M. Ngwangwa and F. Nemavhola, "Evaluating computational performances of hyperelastic models on supraspinatus tendon uniaxial tensile test data," *Journal of Computational Applied Mechanics*, vol. 52, no. 1, pp. 27–43, 2021.
- [13] F. Nemavhola, "Biaxial quantification of passive porcine myocardium elastic properties by region," *Engineering Solid Mechanics*, vol. 5, no. 3, pp. 155–166, 2017.
- [14] F. Nemavhola, "Study of biaxial mechanical properties of the passive pig heart: material characterisation and categorisation of regional differences," *International Journal of Mechanical and Materials Engineering*, vol. 16, no. 1, pp. 1–14, 2021.
- [15] F. Nemavhola, "Fibrotic infarction on the LV free wall may alter the mechanics of healthy septal wall during passive filling," *Bio-medical Materials and Engineering*, vol. 28, no. 6, pp. 579–599, 2017.
- [16] F. Nemavhola, "Detailed structural assessment of healthy interventricular septum in the presence of remodeling infarct in the free wall - a finite element model," *Heliyon*, vol. 5, no. 6, article e01841, 2019.
- [17] A. Karimi, R. Razaghi, M. Navidbakhsh, T. Sera, and S. Kudo, "Mechanical properties of the human sclera under various strain rates: elastic, hyperelastic, and viscoelastic models," *Journal of Biomaterials and Tissue Engineering*, vol. 7, no. 8, pp. 686–695, 2017.
- [18] F. Ji, M. Bansal, B. Wang, Y. Hua, and I. A. Sigal, "Mechanical properties of scleral collagen fibers obtained using a new fiber-based specimen-specific model of sclera microstructure," *Investigative Ophthalmology & Visual Science*, vol. 62, no. 8, pp. 1652–1652, 2021.
- [19] D. Bronte-Ciriza, J. S. Birkenfeld, A. de la Hoz et al., "Estimation of scleral mechanical properties from air-puff optical

- coherence tomography," *Biomedical Optics Express*, vol. 12, no. 10, pp. 6341-6359, 2021.
- [20] L. Yoo, V. Gupta, C. Lee, P. Kavehpore, and J. L. Demer, "Viscoelastic properties of bovine orbital connective tissue and fat: constitutive models," *Biomechanics and Modeling in Mechanobiology*, vol. 10, no. 6, pp. 901–914, 2011.
- [21] I. Schoemaker, P. P. W. Hoefnagel, T. J. Mastenbroek et al., "Elasticity, viscosity, and deformation of orbital fat," *Investigative Ophthalmology & Visual Science*, vol. 47, no. 11, pp. 4819–4826, 2006.
- [22] M. Mahdian, A. Seifzadeh, A. Mokhtarian, and F. Doroodgar, "Characterization of the transient mechanical properties of human cornea tissue using the tensile test simulation," *Materials Today Communications*, vol. 26, article 102122, 2021.
- [23] A. Ashofteh Yazdi, J. Melchor, J. Torres et al., "Characterization of non-linear mechanical behavior of the cornea," *Scientific Reports*, vol. 10, no. 1, pp. 1–10, 2020.
- [24] H. Branislav, F. S. Lea, Ď. Stanislav, R. Jan, and P. Peter, "Glaucoma vs. biomechanical properties of cornea," *Mechanical Engineering*, vol. 69, no. 2, pp. 111–116, 2019.
- [25] J. Eckhardt, M. Sekulic-Jablanovic, S. Treves, and F. Zorzato, "Biochemical and mechanical properties of murine extraocular muscles," *Biophysical Journal*, vol. 112, no. 3, pp. 101a-102a, 2017.
- [26] X. Zhang, Y. Zhao, Z. Gao, and X. Wang, "Mechanical properties of porcine extraocular muscles in vitro," *Journal of Taiyuan University of Technology*, vol. 2, p. 02, 2017.
- [27] K. Tanaka, K. Yamamoto, and T. Katayama, "Evaluation of mechanical properties of porcine sclera," in *Recent Advances* in *Structural Integrity Analysis - Proceedings of the Interna*tional Congress (APCF/SIF-2014), L. Ye, Ed., pp. 311–315, Woodhead Publishing, Oxford, 2014.
- [28] Z. Ndlovu, F. Nemavhola, and D. Desai, "Biaxial mechanical characterization and constitutive modelling of sheep sclera soft tissue," Russian Journal of Biomechanics/Rossijski Zurnal Biomehaniki, vol. 24, no. 1, 2020.
- [29] F. Masithulela, "The effect of over-loaded right ventricle during passive filling in rat heart: a biventricular finite element model," in ASME 2015 International Mechanical Engineering Congress and Exposition, American Society of Mechanical Engineers, 2015.
- [30] F. Masithulela, "Analysis of passive filling with fibrotic myocardial infarction," in ASME International Mechanical Engineering Congress and Exposition, American Society of Mechanical Engineers, 2015.
- [31] Y. Zhang, V. Y. Wang, A. E. Morgan et al., "Finite-element based optimization of left ventricular passive stiffness in normal volunteers and patients after myocardial infarction: utility of an inverse deformation gradient calculation of regional diastolic strain," *Journal of the Mechanical Behavior of Biomedical Materials*, vol. 119, article 104431, 2021.
- [32] P. Sáez and E. Kuhl, "Computational modeling of acute myocardial infarction," Computer Methods in Biomechanics and Biomedical Engineering, vol. 19, no. 10, pp. 1107– 1115, 2016.
- [33] F. Masithulela, "Bi-ventricular finite element model of right ventricle overload in the healthy rat heart," *Bio-medical Materials and Engineering*, vol. 27, no. 5, pp. 507–525, 2016.
- [34] F. J. Masithulela, Computational biomechanics in the remodelling rat heart post myocardial infarction, 2016.

- [35] F. Nemavhola, "Mechanics of the septal wall may be affected by the presence of fibrotic infarct in the free wall at end-systole," *International Journal of Medical Engineering and Informatics*, vol. 11, no. 3, pp. 205–225, 2019.
- [36] S. A. Hans, S. Y. Bawab, and M. L. Woodhouse, "A finite element infant eye model to investigate retinal forces in shaken baby syndrome," *Graefe's Archive for Clinical and Experimental Ophthalmology*, vol. 247, no. 4, pp. 561–571, 2009.
- [37] K. D. Dwyer and K. L. Coulombe, "Cardiac mechanostructure: using mechanics and anisotropy as inspiration for developing epicardial therapies in treating myocardial infarction," *Bioactive Materials*, vol. 6, no. 7, pp. 2198–2220, 2021.
- [38] F. Nemavhola, "Pig sclera stress-strain dataset under biaxial tensile testing," *Mendeley Data*, vol. V1, 2020.
- [39] Y. Fung, "Structure and stress-strain relationship of soft tissues," *American Zoologist*, vol. 24, no. 1, pp. 13–22, 1984.
- [40] Y.-C. Fung, Mechanical properties of living tissues, vol. 547, Springer, 1993.
- [41] C. Chuong and Y. Fung, "Three-dimensional stress distribution in arteries," *Journal of Biomechanical Engineering*, vol. 105, no. 3, pp. 268–274, 1983.
- [42] H. S. Choi and R. Vito, "Two-dimensional stress-strain relationship for canine pericardium," *Journal of Biomechanical Engineering*, vol. 112, no. 2, pp. 153–159, 1990.
- [43] G. A. Holzapfel, T. C. Gasser, and R. W. Ogden, "A new constitutive framework for arterial wall mechanics and a comparative study of material models," *Journal of elasticity and the physical science of solids*, vol. 61, no. 1, pp. 1–48, 2000.
- [44] J. Bursa, P. Skacel, M. Zemanek, and D. Kreuter, "Implementation of hyperelastic models for soft tissues in FE program and identification of their parameters," in *Proceedings of the Sixth IASTED International Conference on Biomedical Engineering*, Innsbruck Austria, 2008.
- [45] L.-S. Huang and J. Chen, "Analysis of variance, coefficient of determination and F-test for local polynomial regression," *The Annals of Statistics*, vol. 36, no. 5, pp. 2085–2109, 2008.
- [46] D. C. Montgomery and G. C. Runger, *Applied statistics and probability for engineers*, John Wiley & Sons, 2010.
- [47] J. P. Barrett, "The coefficient of determination—some limitations," *The American Statistician*, vol. 28, no. 1, pp. 19-20, 1974.
- [48] Y. Feng, Y. Cao, W. Wang et al., "Computational modeling for surgical reconstruction of aortic valve by using autologous pericardium," *IEEE Access*, vol. 8, pp. 97343–97352, 2020.
- [49] S. W. Rabkin and P. Hsu, "Mathematical and mechanical modeling of stress-strain relationship of pericardium," *Ameri*can Journal of Physiology-Legacy Content, vol. 229, no. 4, pp. 896–900, 1975.
- [50] S. Zeinali-Davarani, J. Choi, and S. Baek, "On parameter estimation for biaxial mechanical behavior of arteries," *Journal of Biomechanics*, vol. 42, no. 4, pp. 524–530, 2009.
- [51] J. Huang, D. Brennan, L. Sattler, J. Alderman, B. Lane, and C. O'Mathuna, "A comparison of calibration methods based on calibration data size and robustness," *Chemometrics and Intelligent Laboratory Systems*, vol. 62, no. 1, pp. 25–35, 2002.
- [52] D. C. Taylor, V. Pawar, D. Kruzikas et al., "Methods of model calibration," *PharmacoEconomics*, vol. 28, no. 11, pp. 995– 1000, 2010
- [53] N. Mohan, P. Senthil, S. Vinodh, and N. Jayanth, "A review on composite materials and process parameters optimisation for

- the fused deposition modelling process," *Virtual and Physical Prototyping*, vol. 12, no. 1, pp. 47–59, 2017.
- [54] L. Dubuis, S. Avril, J. Debayle, and P. Badel, "Identification of the material parameters of soft tissues in the compressed leg," *Computer Methods in Biomechanics and Biomedical Engineer*ing, vol. 15, no. 1, pp. 3–11, 2012.
- [55] J. Kollmann, G. Lu, P. Liu et al., "Parameter optimisation of a 2D finite element model to investigate the microstructural fracture behaviour of asphalt mixtures," *Theoretical and Applied Fracture Mechanics*, vol. 103, article 102319, 2019.
- [56] H. Ngwangwa, F. Nemavhola, T. Pandelani et al., Determination of cross-directional and cross-wall variations of passive biaxial mechanical properties of rat myocardium, no. article 2021090244, 2021.
- [57] F. Nemavhola, H. Ngwangwa, T. Pandelani, N. Davies, and T. Franz, *Understanding regional mechanics of rat myocardia by fitting hyperelatsic models*, Research Square, 2021.
- [58] F. Nemavhola, H. Ngwangwa, N. Davies, and T. Franz, Passive biaxial tensile dataset of three main rat heart myocardia: left ventricle, mid-wall and right ventricle, no. article 2021080153(Version 1), 2021.
- [59] L. Lebea, H. Ngwangwa, T. Pandelani, and F. Nemavhola, Biomechanical behaviour and hyperelastic model parameters identification of sheep omasum, Research Square, 2021.
- [60] S. Nicoli, G. Ferrari, M. Quarta et al., "Porcine sclera as a model of human sclera for in vitro transport experiments: histology, SEM, and comparative permeability," *Molecular Vision*, vol. 15, pp. 259–266, 2009.
- [61] T. W. Olsen, S. Sanderson, X. Feng, and W. C. Hubbard, "Porcine sclera: thickness and surface area," *Investigative Ophthalmology & Visual Science*, vol. 43, no. 8, pp. 2529–2532, 2002.