

Correlation between Oncogenic Mutations and Parameter Sensitivity of the Apoptosis Pathway Model

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Abstract

One of the major breakthroughs in oncogenesis research in recent years is the discovery that, in most patients, oncogenic mutations are concentrated in a few core biological functional pathways. This discovery indicates that oncogenic mechanisms are highly related to the dynamics of biologic regulatory networks, which govern the behaviour of functional pathways. Here, we propose that oncogenic mutations found in different biological functional pathways are closely related to parameter sensitivity of the corresponding networks. To test this hypothesis, we focus on the DNA damage-induced apoptotic pathway—the most important safeguard against oncogenesis. We first built the regulatory network that governs the apoptosis pathway, and then translated the network into dynamics equations. Using sensitivity analysis of the network parameters and comparing the results with cancer gene mutation spectra, we found that parameters that significantly affect the bifurcation point correspond to high-frequency oncogenic mutations. This result shows that the position of the bifurcation point is a better measure of the functionality of a biological network than gene expression levels of certain key proteins. It further demonstrates the suitability of applying systems-level analysis to biological networks as opposed to studying genes or proteins in isolation.

Citation: Chen J, Yue H, Ouyang Q (2014) Correlation between Oncogenic Mutations and Parameter Sensitivity of the Apoptosis Pathway Model. *PLoS Comput Biol* 10(1): e1003451. doi:10.1371/journal.pcbi.1003451

Editor: Sheng Zhong, University of California, San Diego, United States of America

Received: December 8, 2012; **Accepted:** December 8, 2013; **Published:** January 23, 2014

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Funding: The National Science Foundation of China (11074009, 10721463), www.nsf.gov.cn/Portal0/default152.htm; the Ministry of Science and Technology of China (2009CB918500, 2012AA02A702), www.most.gov.cn. The funders had no role in study design, data collection and analysis, decision to publish, or preparation of the manuscript.

Competing Interests: The authors have declared that no competing interests exist.

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Introduction

Cancer is one of the most important diseases affecting human health today [1]. Although cancer is considered a genetic disease [2], with a variety of oncogenes and tumour suppressor genes identified, the specific genomic alterations vary wildly between and within cancer types. In 2008, three high-throughput cancer genomic studies reported that cancer gene mutations are concentrated in a limited number of core cellular pathways and regulatory processes [3–5]. This discovery suggests that oncogenesis is highly related to the dynamics of biologic regulatory networks, which govern the behaviour of functional pathways. Clearly, to understand the mechanisms underlying oncogenesis, we need to take a systems and dynamics approach.

A number of studies have proposed a network-based approach to investigate oncogenesis. For example, Torkamani and Schork identified functionally related gene modules targeted by somatic mutation in cancer [6]; Cerami et al. proposed an automated network analysis approach to identify candidate oncogenic processes [7]. A more recent approach by Stites et al. sought to explain mutations in Ras pathway, which are commonly found in cancer, by investigating the steady state concentrations of cellular proteins in parameters changes [8].

In this paper, we propose a new way to identify high-frequency gene mutations in cancer cells. We reason that because gene mutations may affect the activities of their corresponding proteins in a biological regulatory network, they can be considered as

perturbations of the system's dynamics. Therefore, those mutations that qualitatively affect biological network function should correspond to mutation hot spots in cancer. From a dynamics point of view, a qualitative change in a system relates to bifurcations—oncogenic mutations should therefore significantly affect certain bifurcation points.

One of the hallmarks of cancer is evasion of apoptosis; in fact p53 mutations are found in most human cancers [9]. We therefore chose the DNA damage-induced p53-centered apoptosis pathway, as an example, to evaluate our hypothesis. We evaluated the sensitivity of bifurcation points to different network parameters, and compared the results with the cancer gene mutation spectrum. We found that parameters that significantly affect the bifurcation points corresponded to high-frequency oncogenic mutations. This study investigates the mutation spectrum found in cancer cells and provides a useful tool for predicting oncogenic mutations.

Results

Network description and model building

We focused on the apoptotic pathway that responds to sustained DNA damage, induced by the chemotherapeutic compound, etoposide [10,11]. A recent study showed that while low-dose etoposide induces oscillations in p53 levels, caspase3 levels remain low, and most cells survive; in contrast, high-dose etoposide induces a monotonic increase in p53 concentration, followed by a rapid increase in caspase3 with most cells undergoing

Author Summary

Among complex genetic diseases affecting humans, cancer is a major cause of death. In 2008, a genome-wide analysis of hundreds of tumour samples showed that oncogenic mutations are concentrated in a few core functional pathways, revealing a new conceptual framework for cancer biology research, where the role of oncogenic mutations and oncogenic mechanisms are addressed from a network perspective. We therefore propose a new way of identifying high-frequency gene mutations in cancer: gene mutations may affect their corresponding proteins' activity in the biological regulatory network and can be considered as perturbations of the dynamical system. Therefore, mutations that induce qualitative changes in biological networks should correspond to high-frequency mutations in cancer. This concept can help us identify and understand the function of genes that play an important role in oncogenesis, thereby allowing targeted and effective design of gene-based therapy in cancer.

apoptosis [11]. This experiment further justifies the use of p53 in our model.

A schematic of the corresponding regulatory network, which is a modification of the p53 DNA damage response network established and analysed by Li et al. [12], is shown in Figure 1. Nuclear p53 induces *mdm2* transcription, while MDM2 antagonizes p53 by promoting multistep ubiquitination and proteasome-dependent degradation of p53 [13,14]. In unstressed cells, p53 is kept at a low concentration by its negative regulator MDM2. DNA damage reduces the binding affinity between p53 and MDM2 by inducing phosphorylation of p53 and MDM2 [15] — phosphorylated MDM2 undergoes rapid degradation [16] and p53 is subsequently activated by phosphorylation to a “response state”, triggering downstream events, such as apoptosis and cell-cycle arrest [17]. As shown in Figure 1, mono-ubiquitinated p53 is exported to the cytoplasm, while poly-ubiquitinated p53 undergoes degradation [18]. At elevated p53 levels, apoptosis can be initiated by both nuclear and cytoplasmic (or mitochondrial) p53 [19]. While nuclear p53 regulates the transcription of pro-apoptotic proteins such as Puma, Noxa, Bax and Bak [20], mitochondrial p53 exerts a direct pro-apoptotic effect by interacting with Bax and Bak to form a positive feedback loop that activates caspase3 [20–24]. In the experiments conducted by Chipuk et al. [21] and Chen et al. [11], p53 appears to regulate apoptosis through its cytoplasmic pro-death activity and not its nuclear activity.

Many previous studies of p53 dynamics have focused on the response to transient DNA damage induced by ionising radiation or UV; following cell-cycle arrest, cell proliferation resumes once the DNA damage is repaired [25,26]. In our model, we consider sustained DNA damage, which is maintained at a constant damage level until the cell initiates apoptosis [12]. In this way, we can ignore the cell-cycle arrest pathway, and instead concentrate on the apoptosis pathway.

Model simulation

We first present an overview of network dynamics in response to DNA damage at two typical doses of etoposide. As shown in Figure 2, at 1 μM etoposide (low DNA damage), the concentration of nuclear p53 (including inactivated- and activated-p53) oscillates around basal levels (blue line), while the concentration of caspase3 remains low (green line), indicating that apoptosis has not been triggered. At 100 μM etoposide (high DNA damage), nuclear p53

increases monotonically (black line), which is followed by a rapid increase in caspase3 (red line), which in turn triggers downstream apoptotic processes. These results are consistent with the experimental observations of Chen et al. [11], indicating that our model qualitatively reflects the real system.

Having created a suitable model, we next conducted bifurcation analysis to identify potential qualitative changes in the system. Using the level of DNA damage as the control parameter, two types of bifurcations were found in this analysis: two Hopf bifurcations and one saddle-node bifurcation. The transition diagrams of these bifurcations are presented in Figure 3. In Figure 3A, as the level of DNA damage increases, nuclear p53 undergoes two Hopf bifurcations. In the first bifurcation, with increasing DNA damage, the system changes from a low steady state to an oscillatory state; in the second bifurcation, with further DNA damage, the oscillatory state changes to a high steady state. This result is consistent with previously published observations [10,12,27–29]. In the case of caspase3, there exists a saddle-node bifurcation as a function of the level of DNA damage, where a stable node collides with an unstable saddle at the bifurcation point, as shown in Figure 3B. This bifurcation separates the system into two dynamic regimes: a mono-stable steady state regime and a bistable regime. In the bistable regime, one steady state corresponds to a low caspase3 concentration and the other to a high caspase3 concentration. In a wild-type cell, the caspase3 concentration remains low. Once the DNA damage level increases beyond the bifurcation point (about 26 μM etoposide in Figure 3B), the system will switch to a high caspase3 concentration that turns on the apoptosis pathway. Notice that this switch is irreversible—once the apoptosis pathway is turned on, caspase3 can maintain the high level state even when the level of DNA damage falls below the initial threshold.

Our model is based on biological facts, together with certain assumptions and simplifications. The details of our model are presented in the Supporting Information (Text S1). Notice that in our model, ac-p53 refers to phosphorylated p53.

Parameter sensitivity

In biological systems, many biological functions are controlled through dynamic bifurcations. A good example is the saddle-node bifurcation in G1/S transition of the cell cycle [30–33], where the qualitative behaviour of the system is significantly affected by changes in control parameters, which may dramatically affect the location of the critical point. Figure 3C represents such an example in the apoptosis pathway, where increasing the control parameter *kf5* (which corresponds to the rate of association of mono-ub-p53 and MDM2 in the regulatory network of Figure 1) 1.9-fold, shifts the critical point to the right. If *kf5* is increased 4.2-fold, the high caspase3 state can never be reached under medium or high drug dose. This indicates that if the parameter *kf5* is increased due to certain mutations, apoptosis will not be initiated properly, or will not initiate at all, even when the DNA is seriously damaged. The damaged cells therefore have a chance to bypass apoptosis, which may facilitate oncogenesis.

The effect of parameter changes on the location of the bifurcation point is not evenly distributed: some parameters significantly impact the bifurcation points, while others do not. We believe that genes that fall in the former category play important roles in oncogenesis.

To identify which parameters have a major impact on the location of the bifurcation point, we conducted parameter sensitivity analysis by increasing and decreasing each of the 54 parameters in our model 1.2-fold and recording the percentage change of the bifurcation points. In this way, we established a

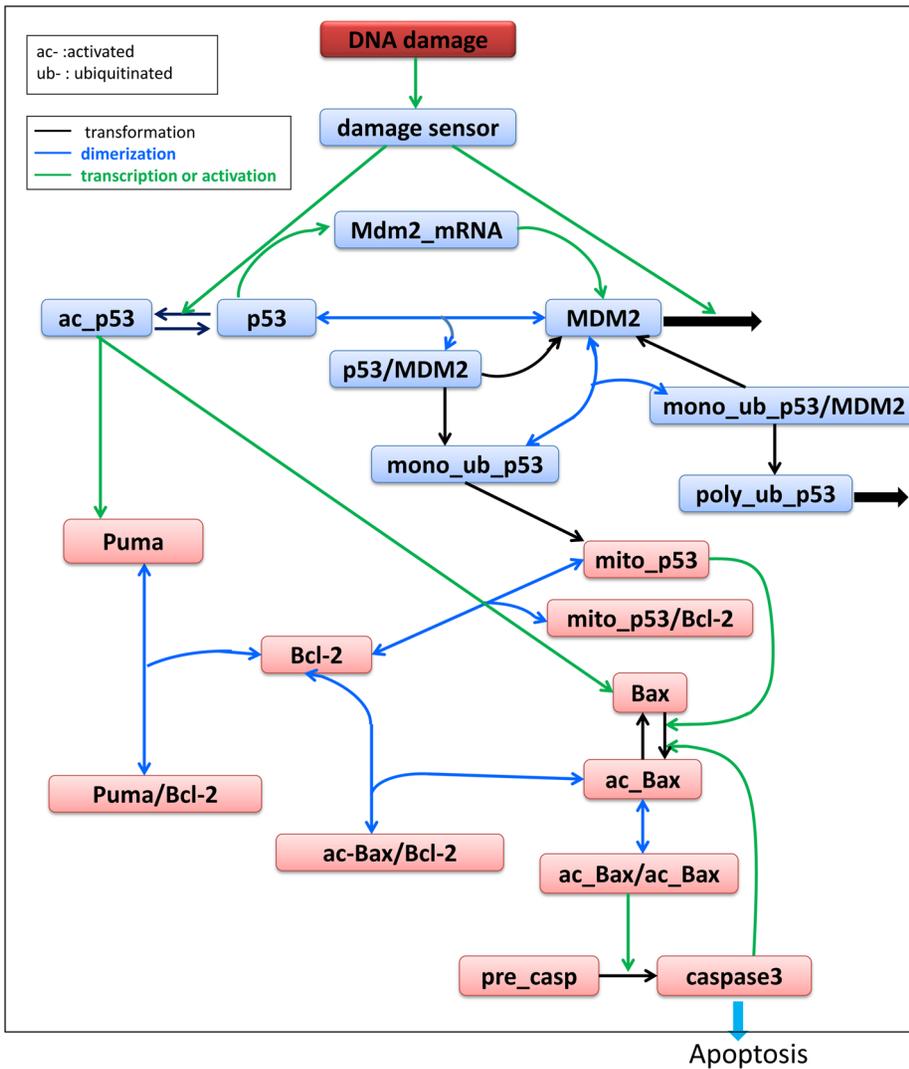


Figure 1. DNA damage-induced apoptotic pathway. Blue lines indicate dimerization; black lines indicate transformation; green lines indicate transcription or activation. “mono-ub”, mono-ubiquitinated; “poly-ub”, poly-ubiquitinated; “mito-” mitochondrial and “/” refers to a complex. The production and degradation of most components are not drawn but are included in the ODEs. Protein families with similar functions are grouped into one node/variable denoted by their representative members (e.g. Bax stands for Bax and Bak). High and low levels of caspase-3 indicate apoptosis and survival, respectively. doi:10.1371/journal.pcbi.1003451.g001

spectrum of parameter sensitivity, which allowed us to compare the result with the oncogenic mutation spectrum.

The gene mutation spectrum of cancer

High-throughput cancer genomic projects, such as the Cancer Genome Atlas (TCGA) and the Catalogue of Somatic Mutations in Cancers (COSMIC) [34], are major resources to obtain the spectrum of genetic variants in different cancer types [35]. To investigate the relationship between parameter changes and the spectrum of cancer gene mutations, we chose skin cancer mutated genes from the Catalogue of Somatic Mutations in Cancers (COSMIC) and glioblastoma multiforme mutated genes from the “CAN-genes” by Parsons et al. [4], and TCGA [5].

Based on the knowledge of biochemical reactions and gene expression [3–5], we concentrated on three types of gene mutations: somatic mutations, amplifications, and deletions. Each mutation corresponds to specific parameters in ordinary

differential equations (ODEs) in our model, the basis and details of which are given in the Supporting Information (Text S1).

The correspondence between parameter sensitivity and mutated genes

The main result of our calculation is summarized in Figure 4. Parameter sensitivities of the saddle-node bifurcation point of each parameter of the apoptosis pathway are shown in Figure 4A (see also Supporting Information Table S2); parameters that cause large or small changes in bifurcation points are marked in yellow, and green, respectively. For the apoptosis pathway about 70% of the parameters are non-influential: the bifurcation point varies very little when changing those parameters. This suggests that the apoptosis pathway is robust, a hallmark of biological networks. However, about 26% of parameters have significant effects on the critical bifurcation points, such as gc_Bax (the basal generation rate of Bax) and kex (nuclear-export rate of mono-ubiquitinated

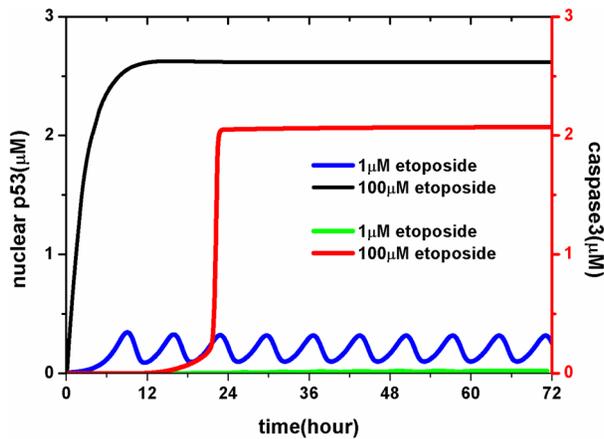


Figure 2. The typical time evolution of the level of total nuclear p53 and caspase3. Blue and black lines represent p53 concentrations at low- and high-level DNA damage, respectively; Green and red lines represent caspase-3 concentrations at low- and high-level DNA damage, respectively.
doi:10.1371/journal.pcbi.1003451.g002

p53), see Figure 4A. A small change in these parameters will induce large changes in the bifurcation points, as shown in Figure 3B. Increasing gc_Bax causes the critical bifurcation point to shift to the left. Therefore, in a biological experiment, to achieve a given rate of apoptosis, increasing the basal generation rate of Bax will require a lower dose of the DNA damaging drug compared with the unaltered basal generation rate of Bax. Similarly, increasing kex will cause the critical bifurcation point to shift to the left, so that for a given rate of apoptosis, increasing the nuclear-export rate of mono-ubiquitinated p53 will require a lower dose of the DNA damaging drug compared with the unaltered nuclear-export rate.

Our parameter sensitivity analysis of critical bifurcation points is in agreement with the literature. For example, overexpression of Bax significantly increases the rate of radiation-induced apoptosis in human breast cancer cells [36], indicating that a perturbation of the basal generation rate of Bax (in our model the corresponding parameter is gc_Bax) would significantly affect the rate of apoptosis—as is indeed predicted by our model. Furthermore, mitochondrial p53-translocation and -accumulation may be induced by a variety of apoptotic stimuli, [37,38]. In fact Marchenko et al. found that the rate of apoptosis is significantly increased after redirecting p53 from the nucleus to the mitochondria by using mitochondrial import leader peptides [37]. This means that a perturbation in the nuclear-export rate of p53 (in our model the corresponding parameter is kex) could greatly alter the rate of apoptosis. Again, we confirmed this effect in our model.

Moreover, Dewson et al. recently reported that following apoptotic signalling in cells and mitochondrial fractions, Bax homodimerises via a BH3:groove interface interaction [39], a necessary step in the apoptotic pathway. The key interaction domains that affect apoptotic function are located in the $\alpha 2$ – $\alpha 5$ regions (54–126A) of Bax; mutations in one of these key residues disrupt apoptotic function, thereby reducing the rate of cell death following treatment with etoposide [39]. According to the COSMIC database, cancer mutation hot spots do exist in the $\alpha 2$ – $\alpha 5$ helices of Bax. These loss-of-function mutations in the Bax BH3 domain decrease the dimerization rate of activated Bax (in our model the corresponding parameter is $kf10$). Our model showed that $kf10$ is indeed a sensitive parameter

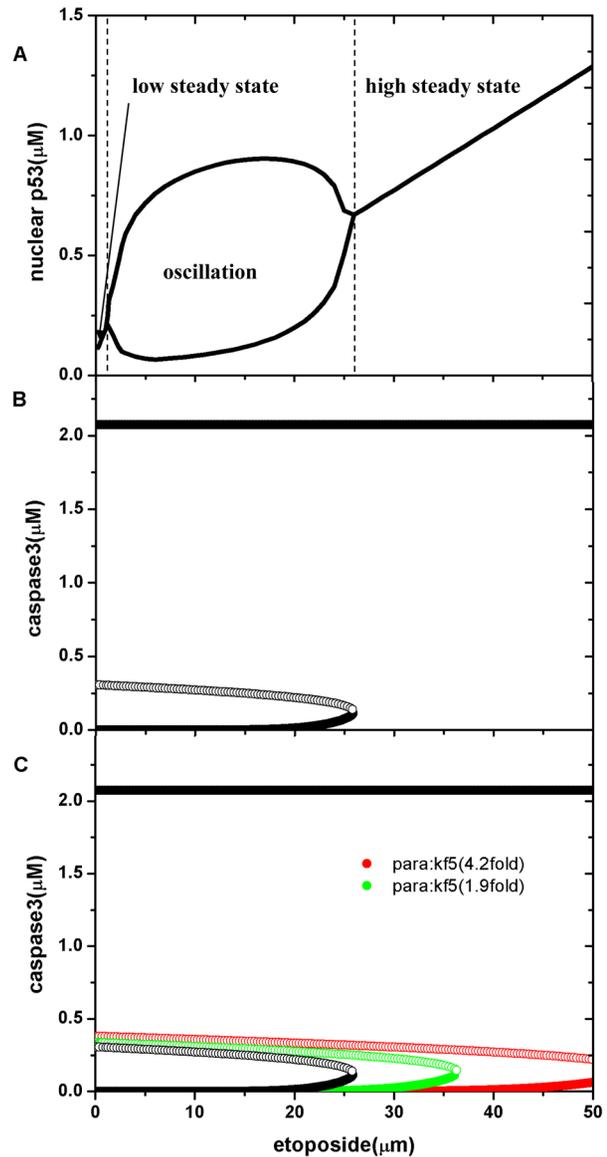


Figure 3. Bifurcation diagram for nuclear p53 and caspase3 for apoptosis. (A) The bifurcation diagram for nuclear p53 using DNA damage as the control parameter. (B) The bifurcation diagram for caspase3 using DNA damage as the control parameter (black dots). (C) Comparison of bifurcation point with an increase in the parameter $kf5$. Black, without increase; green, 1.9-fold increase; red, 4.2-fold increase.
doi:10.1371/journal.pcbi.1003451.g003

and a slight decrease in $kf10$ shifts the critical bifurcation point to the right.

We next sought to compare our results to those of Stites et al. who investigated mutations in Ras pathway by measuring the steady state concentrations of cellular proteins in parameter changes [8]. In addition to parameter sensitivity analysis of the bifurcation points, we therefore used the steady-state concentration of caspase3 as a measure of oncogenesis. To achieve this, we increased and decreased each of the 54 parameters 1.2-fold and recorded the percentage change in the steady-state concentration of caspase3. The results are presented in Figure 4B (See also Supporting Information Table S3). The parameters that cause a large or small percentage change in the steady-state concentration of caspase3 are marked in magenta and blue, respectively. Overall,

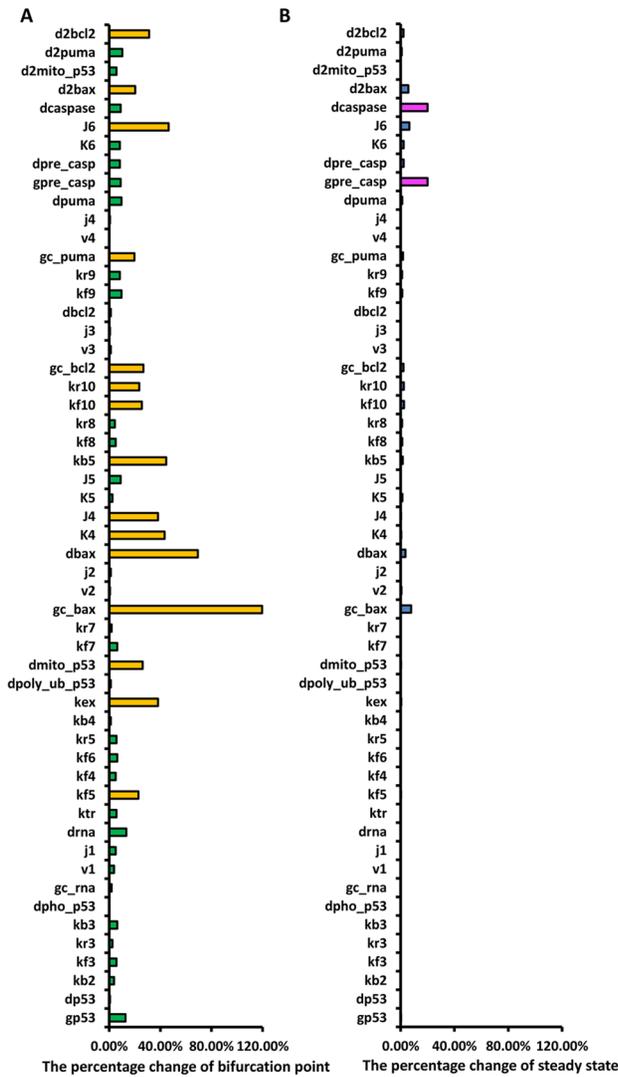


Figure 4. Parameter sensitivity analysis. (A) The change of the saddle-node bifurcation point in response to a 20% increase or decrease in each parameter of the apoptosis pathway. (B) The change in the steady-state concentration of caspase3 in response to a 20% increase or decrease in each parameter of the apoptosis pathway. doi:10.1371/journal.pcbi.1003451.g004

we found that the bifurcation point and the steady-state concentration of caspase3 are sensitive to mutually exclusive sets of parameters.

As shown in Figure 4A, the critical points of bifurcation are largely affected by 15 parameters (yellow in Figure 4A), which we then selected to compare with the skin cancer and glioblastoma multiforme gene mutation spectrum, as shown in Figure 5A. Changes in the bifurcation point (yellow bar) and in the steady-state concentration of caspase3 (blue bar) are displayed alongside mutation frequencies in skin cancer and glioblastoma multiforme. Almost all influential parameters correspond to mutation hot spots in skin cancer and glioblastoma multiforme. This result supports our hypothesis that bifurcation points are sensitive to parameters corresponding to mutations that are most likely oncogenic. Here, we note that the definition of “mutation hot spot” is not quantitative; we will discuss this issue in the last section of the paper.

For the sake of comparison, we also selected the parameters to which the bifurcation point was insensitive; the result is presented

in Figures 5B and 5C. We found that a part of the insensitive parameters correspond to very small number of mutation hot spots (Figure 5B), but the other part correspond to a large number of mutation hot spots (Figure 5C). Several factors may contribute to the inconsistency. It is well established that alteration of a single gene may not be oncogenic in itself [40]—in most cases, multiple hits are necessary [41]. We therefore suggest a synergistic effect for these parameters (Figure 5C), where two or more parameter changes, which are non-influential in isolation, may induce sensitivity in the bifurcation point when they co-occur. Indeed, we found that by decreasing kf3 (association rate of p53 and MDM2) and increasing kr3 (dissociation rate of p53/MDM2 complex) at the same time by 1.2-fold, the bifurcation point changes by about 22%. However, when changing these two parameters in isolation, the bifurcation point only changes by 5% and 2%. This may partially explain the observed inconsistency. Furthermore, one gene mutation may affect several parameters in our model, and one model parameter may involve several genes. In our analysis, the one-to-one mapping between the model parameters and the genes involved in the network is certainly an oversimplification. Fully understanding this behaviour requires detailed knowledge of the effect of mutations on the parameters, which is not available except in a few special cases.

Similarly, we investigated the effect of different parameters on the steady state concentration of caspase3 as a measure of oncogenesis. We identified two parameters (magenta in Figure 4B), which led to the largest changes in the steady-state concentration of caspase3. We also calculated changes in the critical point when changing the parameters (Figure 6). According to the results in Figures 5A and 6, and compared with the results of bifurcation points, the relationship between the protein steady-state concentration and the cancer mutation spectrum is very weak.

Discussion

Our work is based on the hypothesis that key regulators in physiological networks and oncogenesis are closely correlated and that the critical point of bifurcation is a good measure of network functionality. Therefore, mutations that cause variations in parameters that affect the bifurcation point are more likely to be oncogenic. In our apoptosis model, the location of the saddle-node bifurcation point reflects the DNA damage threshold where apoptosis is activated; when this threshold is exceeded, the system will switch from the low to the high state, which is accompanied by a rapid increase in caspase3 levels. A mutation may increase the apoptotic threshold, thereby allowing cells to evade apoptosis even at high levels of DNA damage, which may facilitate oncogenesis—a hypothesis that was confirmed by our analysis.

Distinguishing driver- from passenger-mutations is a central challenge in cancer research [42–44], and recently a network-based approach to identify cancer driver mutations has been proposed [6,7]. Similarly, our strategy may be applied to identify driver mutations by identifying parameters with the greatest impact on the bifurcation point.

Several issues need to be addressed in this analysis: First, what is the impact of the Hopf bifurcation of nuclear p53 on oncogenesis? Although a number of studies have investigated the oscillatory behaviour of p53 in response to stress [25,45–47], the functional role of these oscillations in DNA damage response remains unclear. We also conducted parameter sensitivity analysis of the Hopf bifurcation of nuclear p53 as a function of the level of DNA damage [12], and found a strong correlation between the spectrum of parameter sensitivities and the oncogenic mutation spectrum (see Figure S1). This may indicate that nuclear p53

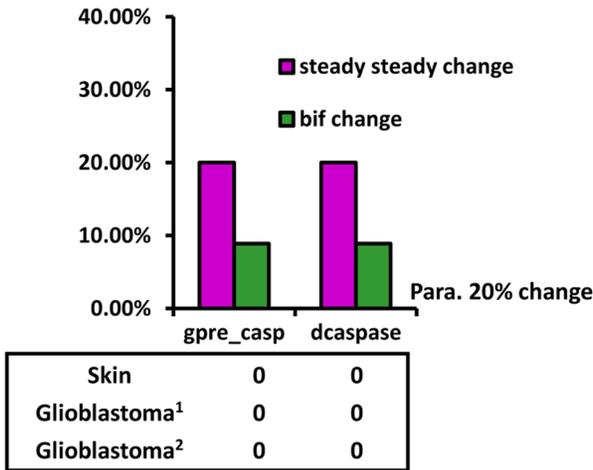


Figure 6. Comparison of parameters linked to sensitivity of caspase3 levels and gene mutations. The numbers in the frame indicate the number of occurrences in the mutation spectrum of the gene relating to the corresponding parameters. Magenta bar, change in the steady-state concentration of caspase3; Green bar, change in the critical point of bifurcation. gpre-casp, the basal generation rate of pre-caspase; dcaspase, the degradation rate of caspase3. doi:10.1371/journal.pcbi.1003451.g006

parameters, our analysis can only be qualitative. In this work, we used arbitrary thresholds to define a “mutation hot spot”, that were determined by our knowledge of the specific gene. As such, for genes involved in several regulatory pathways and with a high mutation frequency (like p53), we set a high threshold value (>10) for mutation hot spots. For genes involved in only one or two pathways, and which have very low mutation frequencies (like Puma), we believe that in spite of the low mutation frequency, they are still mutation hot spots. Because of the lack of detailed information on the impact of each mutation on the model parameters, our analysis can only achieve qualitative conclusions.

The fourth issue relates to the simplicity of our model network: although the apoptosis pathway involves both the extrinsic and intrinsic pathways [48], we used a simplified, qualitative network model to conduct our research. To prove the validity of our model, we extended the current apoptosis pathway and repeated our analysis. Compared with the original model, the extended model consisted of 10 additional nodes including Noxa, Mcl-1, Bcl-xL and the complexes that they formed. Puma, Noxa, Bcl-2, Mcl-1 and Bcl-xL are all proteins of the Bcl-2 family. Like Puma, Noxa is a pro-apoptotic protein, which is regulated by nuclear p53 at the

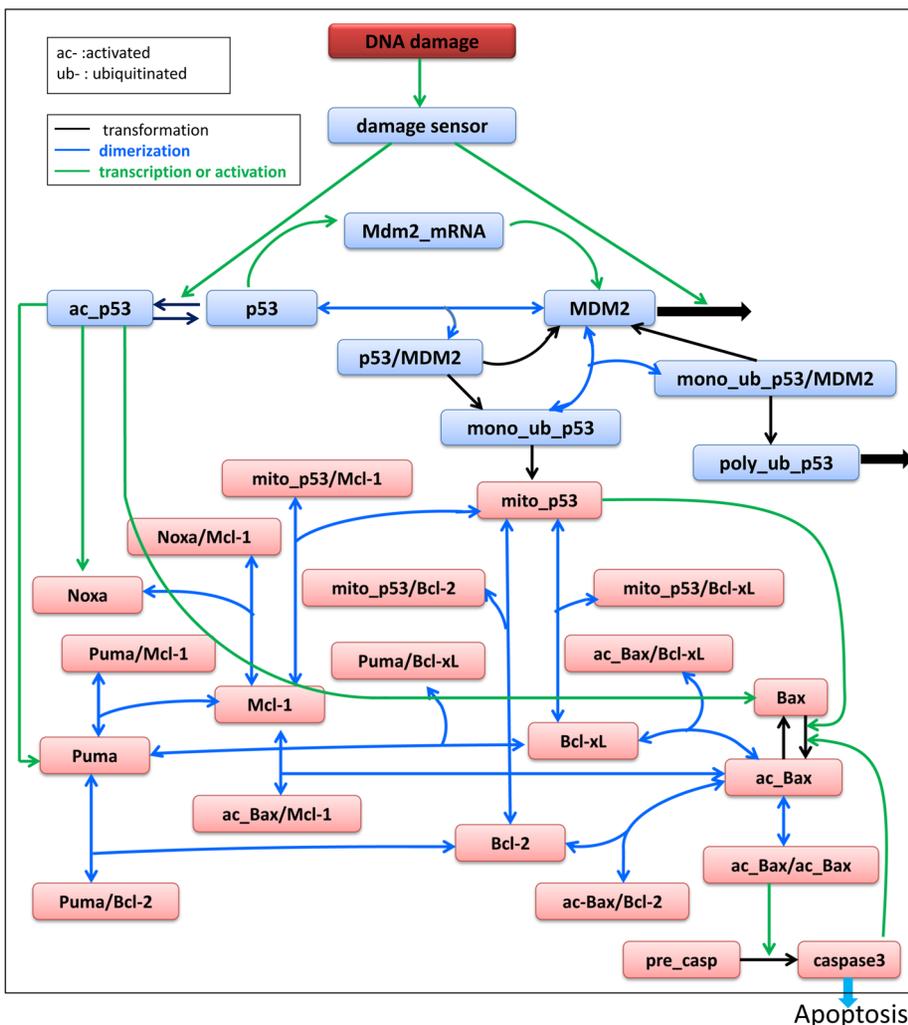


Figure 7. Extended DNA damage-induced apoptotic pathway. Blue lines indicate dimerization; black lines indicate transformation; green lines indicate transcription or activation. “mono-ub”, mono-ubiquitinated; “poly-ub”, poly-ubiquitinated; “mito-”, mitochondrial; “/” stands for complex. doi:10.1371/journal.pcbi.1003451.g007

multiforme samples. The TCGA project has catalogued somatic mutations and recurrent copy number alterations in 91 glioblastoma multiforme cases [5]. The basis and details of the correspondence of three forms of gene mutations and specific parameters in ordinary differential equations (ODEs) in our model are given in Text S1.

Supporting Information

Figure S1 Parameter sensitivity analysis and its correspondence with mutations. (A) The percentage change in the Hopf bifurcation point in response to 20% increase or decrease in each parameter. (B) The correspondence between sensitive parameters and high-frequency mutation genes. (TIF)

Figure S2 Time evolution diagram of the level of total nuclear p53 and caspase3. Blue and black lines represent p53 concentrations at low- and high-level DNA damage, respectively; Green and red lines represent caspase3 concentrations at low- and high-level DNA damage, respectively. (TIF)

Figure S3 Bifurcation diagram for caspase3 using DNA damage as the control parameter. (TIF)

Figure S4 Comparison of parameters linked to sensitivity of caspase3 levels and gene mutations. (TIF)

References

- Garcia M, Jemal A, Ward E, Center M, Hao Y, et al. (2007) Global cancer facts & figures 2007. Atlanta, GA: American Cancer Society 1.
- Vogelstein B, Kinzler KW (2004) Cancer genes and the pathways they control. *Nature medicine* 10: 789–799.
- Jones S, Zhang X, Parsons DW, Lin JC, Leary RJ, et al. (2008) Core signaling pathways in human pancreatic cancers revealed by global genomic analyses. *Science* 321: 1801–1806.
- Parsons DW, Jones S, Zhang X, Lin JC, Leary RJ, et al. (2008) An integrated genomic analysis of human glioblastoma multiforme. *Science* 321: 1807–1812.
- (2008) Comprehensive genomic characterization defines human glioblastoma genes and core pathways. *Nature* 455: 1061–1068.
- Torkamani A, Schork NJ (2009) Identification of rare cancer driver mutations by network reconstruction. *Genome research* 19: 1570–1578.
- Cerami E, Demir E, Schultz N, Taylor BS, Sander C (2010) Automated network analysis identifies core pathways in glioblastoma. *PLoS one* 5: e8918.
- Stites EC, Tramont PC, Ma Z, Ravichandran KS (2007) Network analysis of oncogenic Ras activation in cancer. *Science* 318: 463–467.
- Soussi T, Lozano G (2005) p53 mutation heterogeneity in cancer. *Biochemical and biophysical research communications* 331: 834–842.
- Lev Bar-Or R, Maya R, Segel LA, Alon U, Levine AJ, et al. (2000) Generation of oscillations by the p53-Mdm2 feedback loop: a theoretical and experimental study. *Proceedings of the National Academy of Sciences of the United States of America* 97: 11250–11255.
- Chen X, Chen J, Gan S, Guan H, Zhou Y, et al. (2013) DNA damage strength modulates a bimodal switch of p53 dynamics for cell-fate control. *BMC biology* 11: 73.
- Li Z, Ni M, Li J, Zhang Y, Ouyang Q, et al. (2010) Decision making of the p53 network: Death by integration. *Journal of theoretical biology*. doi: 10.1016/j.jtbi.2010.11.041.
- Marine JC, Francoz S, Maetens M, Wahl G, Toledo F, et al. (2006) Keeping p53 in check: essential and synergistic functions of Mdm2 and Mdm4. *Cell death and differentiation* 13: 927–934.
- Michael D, Oren M (2003) The p53-Mdm2 module and the ubiquitin system. *Seminars in cancer biology* 13: 49–58.
- Chehab NH, Malikzay A, Appel M, Halazonetis TD (2000) Chk2/hCds1 functions as a DNA damage checkpoint in G(1) by stabilizing p53. *Genes Dev* 14: 278–288.
- Stommel JM, Wahl GM (2004) Accelerated MDM2 auto-degradation induced by DNA-damage kinases is required for p53 activation. *Embo J* 23: 1547–1556.
- Vousden KH, Lane DP (2007) p53 in health and disease. *Nature reviews Molecular cell biology* 8: 275–283.
- Salmena L, Pandolfi PP (2007) Changing venues for tumour suppression: balancing destruction and localization by monoubiquitylation. *Nat Rev Cancer* 7: 409–413.
- Chipuk JE, Green DR (2006) Dissecting p53-dependent apoptosis. *Cell Death Differ* 13: 994–1002.
- Cory S, Adams JM (2002) The Bcl2 family: regulators of the cellular life-or-death switch. *Nature reviews Cancer* 2: 647–656.
- Chipuk JE, Kuwana T, Bouchier-Hayes L, Droin NM, Newmeyer DD, et al. (2004) Direct activation of Bax by p53 mediates mitochondrial membrane permeabilization and apoptosis. *Science* 303: 1010–1014.
- Slee EA, Keogh SA, Martin SJ (2000) Cleavage of BID during cytotoxic drug and UV radiation-induced apoptosis occurs downstream of the point of Bcl-2 action and is catalysed by caspase-3: a potential feedback loop for amplification of apoptosis-associated mitochondrial cytochrome c release. *Cell death and differentiation* 7: 556–565.
- Spierings D, McStay G, Saleh M, Bender C, Chipuk J, et al. (2005) Connected to death: the (unexpurgated) mitochondrial pathway of apoptosis. *Science* 310: 66–67.
- Leu JI, Dumont P, Hafey M, Murphy ME, George DL (2004) Mitochondrial p53 activates Bak and causes disruption of a Bak-Mcl1 complex. *Nature cell biology* 6: 443–450.
- Ma L, Wagner J, Rice JJ, Hu W, Levine AJ, et al. (2005) A plausible model for the digital response of p53 to DNA damage. *Proceedings of the National Academy of Sciences of the United States of America* 102: 14266–14271.
- Zhang T, Brazhnik P, Tyson JJ (2007) Exploring mechanisms of the DNA-damage response: p53 pulses and their possible relevance to apoptosis. *Cell Cycle* 6: 85–94.
- Batchelor E, Mock CS, Bhan I, Loewer A, Lahav G (2008) Recurrent initiation: a mechanism for triggering p53 pulses in response to DNA damage. *Molecular cell* 30: 277–289.
- Ramalingam S, Honkanen P, Young L, Shimura T, Austin J, et al. (2007) Quantitative assessment of the p53-Mdm2 feedback loop using protein lysate microarrays. *Cancer research* 67: 6247–6252.
- Speidel D, Helmbold H, Deppert W (2006) Dissection of transcriptional and non-transcriptional p53 activities in the response to genotoxic stress. *Oncogene* 25: 940–953.
- Haberichter T, Madge B, Christopher RA, Yoshioka N, Dhiman A, et al. (2007) A systems biology dynamical model of mammalian G1 cell cycle progression. *Mol Syst Biol* 3: 84.
- Qu Z, Weiss JN, MacLellan WR (2003) Regulation of the mammalian cell cycle: a model of the G1-to-S transition. *Am J Physiol Cell Physiol* 284: C349–364.
- Novak B, Tyson JJ, Gyorffy B, Csikasz-Nagy A (2007) Irreversible cell-cycle transitions are due to systems-level feedback. *Nat Cell Biol* 9: 724–728.

Table S1 The specific correspondence between each parameters and its gene mutations. amp, amplification; mut, mutation; del, deletion. (DOCX)

Table S2 Parameter sensitivity analysis. The effect of a 1.2-fold increase or decrease of each of the 54 parameters on the percentage change in the critical point of bifurcation. (DOCX)

Table S3 Parameter sensitivity analysis. The effect of a 1.2-fold increase or decrease of each of the 54 parameters on the percentage change in the critical point of bifurcation. (DOCX)

Text S1 Detailed description of the model and parameters used. (DOCX)

Acknowledgments

We thank Professor Jue Shi for providing the experimental data used in this article. We also thank L.J. Zhao, Z.Y. Li, B. Shao, Y.S. Cao, H.L. Wang and F.T. Li for helpful discussions.

Author Contributions

Conceived and designed the experiments: QO. Performed the experiments: JC HY. Analyzed the data: JC QO. Contributed reagents/materials/analysis tools: JC HY. Wrote the paper: JC QO. Generated the theory, developed the computational models, and wrote the manuscript: QO. Designed the software and conducted the calculations: JC HY.

33. Yao G, Lee TJ, Mori S, Nevins JR, You L (2008) A bistable Rb-E2F switch underlies the restriction point. *Nat Cell Biol* 10: 476–482.
34. Forbes SA, Bhamra G, Bamford S, Dawson E, Kok C, et al. (2008) The Catalogue of Somatic Mutations in Cancer (COSMIC). *Current protocols in human genetics*/editorial board, Jonathan L Haines [et al] Chapter 10: Unit 10.11.
35. Baudot A, Real FX, Izarzugaza JM, Valencia A (2009) From cancer genomes to cancer models: bridging the gaps. *EMBO reports* 10: 359–366.
36. Sakakura C, Sweeney EA, Shirahama T, Igarashi Y, Hakomori S, et al. (1996) Overexpression of bax sensitizes human breast cancer MCF-7 cells to radiation-induced apoptosis. *International journal of cancer Journal international du cancer* 67: 101–105.
37. Marchenko ND, Zaika A, Moll UM (2000) Death signal-induced localization of p53 protein to mitochondria. A potential role in apoptotic signaling. *The Journal of biological chemistry* 275: 16202–16212.
38. Mihara M, Erster S, Zaika A, Petrenko O, Chittenden T, et al. (2003) p53 has a direct apoptogenic role at the mitochondria. *Molecular cell* 11: 577–590.
39. Dewson G, Ma S, Frederick P, Hockings C, Tan I, et al. (2012) Bax dimerizes via a symmetric BH3:groove interface during apoptosis. *Cell death and differentiation* 19: 661–670.
40. Michor F, Iwasa Y, Nowak MA (2004) Dynamics of cancer progression. *Nature reviews Cancer* 4: 197–205.
41. Knudson AG (2001) Two genetic hits (more or less) to cancer. *Nature reviews Cancer* 1: 157–162.
42. Leary RJ, Lin JC, Cummins J, Boca S, Wood LD, et al. (2008) Integrated analysis of homozygous deletions, focal amplifications, and sequence alterations in breast and colorectal cancers. *Proceedings of the National Academy of Sciences* 105: 16224.
43. Kaminker JS, Zhang Y, Watanabe C, Zhang Z (2007) CanPredict: a computational tool for predicting cancer-associated missense mutations. *Nucleic acids research* 35: W595–W598.
44. Greenman C, Stephens P, Smith R, Dalgleish GL, Hunter C, et al. (2007) Patterns of somatic mutation in human cancer genomes. *Nature* 446: 153–158.
45. Wagner J, Ma L, Rice JJ, Hu W, Levine AJ, et al. (2005) p53-Mdm2 loop controlled by a balance of its feedback strength and effective dampening using ATM and delayed feedback. *Syst Biol (Stevenage)* 152: 109–118.
46. Ciliberto A, Novak B, Tyson JJ (2005) Steady states and oscillations in the p53/Mdm2 network. *Cell Cycle* 4: 488–493.
47. Hu W, Feng Z, Ma L, Wagner J, Rice JJ, et al. (2007) A single nucleotide polymorphism in the MDM2 gene disrupts the oscillation of p53 and MDM2 levels in cells. *Cancer Res* 67: 2757–2765.
48. Letai AG (2008) Diagnosing and exploiting cancer's addiction to blocks in apoptosis. *Nature reviews Cancer* 8: 121–132.
49. Chen L, Willis SN, Wei A, Smith BJ, Fletcher JI, et al. (2005) Differential targeting of prosurvival Bcl-2 proteins by their BH3-only ligands allows complementary apoptotic function. *Molecular cell* 17: 393–403.
50. Michor F, Iwasa Y, Nowak MA (2004) Dynamics of cancer progression. *Nature Reviews Cancer* 4: 197–205.
51. Aldridge BB, Burke JM, Lauffenburger DA, Sorger PK (2006) Physicochemical modelling of cell signalling pathways. *Nature cell biology* 8: 1195–1203.