# OEEF-Driven Intramolecular Self-Redox of Superalkali $\mathrm{Rb}_{3} \mathrm{BeB}_{6} \mathrm{Be}^{\prime} \mathrm{Rb}^{\prime}{ }_{3}$ : A High-Performance Candidate for NLO Molecular Switch 

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#### Abstract

To provide a novel intramolecular self-redox switch, a boron-based sandwich-like complex $\mathrm{Rb}_{3} \mathrm{BeB}_{6} \mathrm{Be}^{\prime} \mathrm{Rb}_{3}{ }_{3}$ is achieved by using theoretical computations. An applicable oriented external electric field (OEEF) can result in the occurrence of intramolecular self-redox (IMSR) with a long-range electron transfer from tetrahedral $\mathrm{Be}^{\prime} \mathrm{Rb}^{\prime}{ }_{3}$ to $\mathrm{Rb}{ }_{3} \mathrm{Be}$ and subsequently $\left[\mathrm{Rb}_{3} \mathrm{Be}\right]^{3+}\left[\mathrm{B}_{6}\right]^{6-}\left[\mathrm{Be}^{\prime} \mathrm{Rb}^{\prime}{ }_{3}\right]^{3+}\left(D_{3 \mathrm{~d}}\right)$ changes to $\left[\mathrm{Rb}_{3} \mathrm{Be}\right]^{2+}\left[\mathrm{B}_{6}\right]^{6-}\left[\mathrm{Be}^{\prime} \mathrm{Rb}_{3}^{\prime}\right]^{4+}\left(\mathrm{C}_{3 v}\right)$, accompanying high-performance NLO switchable effect for both static and dynamic first hyperpolarizability $\left(\beta_{0}\right)$. $\left[\mathrm{Rb}_{3} \mathrm{Be}\right]^{3+}\left[\mathrm{B}_{6}\right]^{6-}\left[\mathrm{Be}^{\prime} \mathrm{Rb}_{3}\right]^{3+}$ (off-form) owns zero of dipole moment $\left(\mu_{0}\right)$ and $\beta_{0}$, while  $\left[\mathrm{Rb}_{3} \mathrm{Be}\right]^{2+}\left[\mathrm{B}_{6}\right]^{6-}\left[\mathrm{Be}^{\prime} \mathrm{Rb}_{3}{ }_{3}\right]^{4+}$ (on-form) exhibits a $\mu_{0}$ of 3.36 D and a $\beta_{0}{ }^{\text {e }}$ of $2.18 \times 10^{5}$ au. The different dynamic first hyperpolarizabilities between $\left[\mathrm{Rb}_{3} \mathrm{Be}^{3+}\left[\mathrm{B}_{6}\right]^{6-}\left[\mathrm{Be}^{\prime} \mathrm{Rb}^{\prime}{ }_{3}\right]^{3+}\right.$ and $\left[\mathrm{Rb}_{3} \mathrm{Be}\right]^{2+}\left[\mathrm{B}_{6}\right]^{6-}\left[\mathrm{Be}^{\prime} \mathrm{Rb}_{3}^{\prime}\right]^{4+}$ are also significant. This indicates that $\mathrm{Rb}_{3} \mathrm{BeB}_{6} \mathrm{Be}^{\prime} \mathrm{Rb}_{3}^{\prime}$ is a potential candidate for an IMSR NLO switch.


## INTRODUCTION

The study of the effect of oriented external electric field (OEEF) on the chemical reaction and molecular material has been a fast-growing activity research field. ${ }^{1-3}$ For chemical reactions, it is reported that OEEF can be responsible for the electrostatic catalysis in enzymes, ${ }^{4-6}$ controlling the reactivity and selectivity of the famous Diels-Alder, proton transfer reactions, etc. ${ }^{7-9}$ Even the OEEF has been suggested to be a promising candidate for use in future smart- and greensynthetic chemistry. ${ }^{1,10}$ Under the influence of the OEEFs, unusual structures, special chemical bonds, and novel physical and chemical properties of the molecules can be found. Earlier, Li et al. ${ }^{11,12}$ have reported that the OEEF can drive the hydrogen bond in $\mathrm{H}_{3} \mathrm{~N} \cdots \mathrm{HCl}$ to change into an ionic bond. In the nano field, the OEEF can change the energy band structure of nanotube and graphene to regulate their properties. ${ }^{2}$
The design and achievement of molecular switching materials are undoubtedly one of the most important goals in molecular electronics. To date, a massive number of nonlinear optical (NLO) molecular switches ${ }^{13-29}$ have been obtained on both theoretical and experimental aspects because it is of paramount importance to the signal processing, data storage, sensing, and molecular devices. ${ }^{13}$ As we have seen, the switching processes of the reported OEEF-driven charging molecular switches ${ }^{20-27}$ and redox NLO switches ${ }^{27-29}$ mainly relate to the change of the electron number while their threedimensional molecular frameworks usually change little. So,
these redox/charging switches may be a better choice due to the requirement of a terminal device or assembly of molecules. For the charging NLO molecular switches, it was reported that an applicable OEEF can lead to long-range excess electron transfers (LEET) in $\mathrm{M}^{-}-\mathrm{Ca}^{2+} L-\mathrm{M}^{-}(\mathrm{M}=\mathrm{Li}$ or $\mathrm{Na}, L=$ $\left.\mathrm{F}_{6} \mathrm{C}_{6} \mathrm{H}_{6}\right)$ and $\mathrm{e}^{-}+\mathrm{Ca}^{2+}\left(\mathrm{Ni} @ \mathrm{~Pb}_{12}\right)^{2-} \mathrm{Ca}^{2+}+\mathrm{e}^{-}$, and consequently, both exhibit large static first hyperpolarizabilities $\left(\beta_{0}\right){ }^{20,21}$ For the redox NLO molecular switch, based on the pyridine helical complex, Xu et al. ${ }^{28}$ have explored the effect of two-electronredox process of $\mathrm{Li}_{2}$-doped single-strand pyridine helical ( $\mathrm{Li}_{2} @$ helical) on the NLO responses. In the single molecular level, we have presented that superalkali $\mathrm{Li}_{3} \mathrm{~N}_{3} \mathrm{Mg}$ can be a good candidate for an intramolecular self-redox (IMSR) NLO switch due to the change from $\mathrm{Li}_{3}{ }^{2+} \mathrm{N}_{3} \mathrm{Mg}^{+}$to $\mathrm{Li}_{3}{ }^{+} \mathrm{N}_{3} \mathrm{Mg}^{2+} .{ }^{27}$

In 2020, Wang et al. have presented that a unique boronbased sandwich cluster $\mathrm{Rb}_{6} \mathrm{Be}_{2} \mathrm{~B}_{6}$ with the $D_{3 d}$ point group is viable in the ionic complex of $\left[\mathrm{Rb}_{3} \mathrm{Be}\right]^{3+}\left[\mathrm{B}_{6}\right]^{6-}\left[\mathrm{BeRb}_{3}\right]^{3+}{ }^{30}$ To differentiate the two tetrahedral $\mathrm{BeRb}_{3}$ ligands, $\mathrm{Rb}_{6} \mathrm{Be}_{2} \mathrm{~B}_{6}$ is named $\mathrm{Rb}_{3} \mathrm{BeB}_{6} \mathrm{Be}^{\prime} \mathrm{Rb}_{3}^{\prime}$ or $\left[\mathrm{Rb}_{3} \mathrm{Be}\right]^{3+}\left[\mathrm{B}_{6}\right]^{6-}\left[\mathrm{Be}^{\prime} \mathrm{Rb}^{\prime}{ }_{3}\right]^{3+}$ in this study. Then, like the effect of OEEF on $\mathrm{M}^{-}-L \mathrm{Ca}^{2+} L-\mathrm{M}^{-}(\mathrm{M}=$

[^0]

Li or $\left.\mathrm{Na}, L=\mathrm{F}_{6} \mathrm{C}_{6} \mathrm{H}_{6}\right)$ and $\mathrm{e}^{-}+\mathrm{Ca}^{2+}\left(\mathrm{Ni} @ \mathrm{~Pb}_{12}\right)^{2-} \mathrm{Ca}^{2+}+\mathrm{e}^{-20,21}$ can an appropriate OEEF also result in the breaking of the symmetric electron clouds of $D_{3 \mathrm{~d}}\left[\mathrm{Rb}_{3} \mathrm{Be}\right]^{3+}\left[\mathrm{B}_{6}\right]^{6-}\left[\mathrm{Be}^{\prime} \mathrm{Rb}_{3}{ }_{3}\right]^{3+}$ and lead to a LEET to form an IMSR switch? Subsequently, what is the value of $\beta_{0}$ of it? In that case, the boron-based sandwich cluster $\mathrm{Rb}_{6} \mathrm{Be}_{2} \mathrm{~B}_{6}$ may be a high-performance candidate for the IMSR NLO molecular switch. We hope that this work can provide a meaningful guidance and theoretical support for the regulation and control of electric field on the chemical reaction and molecular materials.

## - COMPUTATIONAL DETAILS

In this work, all quantum chemistry calculations, including geometrical optimization, frequency calculation, were done by using Gaussian16 (version A.03) program. ${ }^{31}$ For the field-free $\mathrm{Rb}_{3} \mathrm{BeB}_{6} \mathrm{Be}^{\prime} \mathrm{Rb}^{\prime}{ }_{3}$, it is reported ${ }^{30}$ that the global minimum (GM) structure adopts a $D_{3 d}$ symmetry, and its structure was optimized at the $\mathrm{PBEO}^{32} /$ def2-qzvp ${ }^{33}$ level, which has been suggested to be reliable for the study of boron-based clusters. ${ }^{34-37}$ Then, based on this structure, the optimized geometries for each stationary point of $\mathrm{Rb}_{3} \mathrm{BeB}_{6} \mathrm{Be}^{\prime} \mathrm{Rb}^{\prime}{ }_{3}$ with different OEEFs were also calculated at the PBE0/def2-qzvp level. The natural population analysis (NPA) ${ }^{38}$ was calculated at the MP2, $\operatorname{PBE} 0$, and $\operatorname{CASSCF}(2,2)$ methods with def2-qzvp basis set. The solvent effects are included using the polarizable continuum model (PCM), and the solvents of THF and cyclohexane $\left(\mathrm{C}_{6} \mathrm{H}_{12}\right)$ are used. The quantum theory of atoms in molecules (QTAIM) analysis, ${ }^{39}$ electron localization function (ELF) diagrams, and localized-orbital locator (LOL) plots as well as the transition orbital maps were obtained with Multiwfn program package (version 3.8). ${ }^{40}$
The VIE was determined as

$$
\begin{equation*}
\mathrm{VIE}=E\left[\mathrm{Rb}_{3} \mathrm{BeB}_{6} \mathrm{Be}^{\prime} \mathrm{Rb}_{3}^{\prime}\right]^{+}-E\left[\mathrm{Rb}_{3} \mathrm{BeB}_{6} \mathrm{Be}^{\prime} \mathrm{Rb}_{3}^{\prime}\right] \tag{1}
\end{equation*}
$$

where $E\left[\mathrm{Rb}_{3} \mathrm{BeB}_{6} \mathrm{Be}^{\prime} \mathrm{Rb}_{3}{ }_{3}\right]^{+}$and $E\left[\mathrm{Rb}_{3} \mathrm{BeB}_{6} \mathrm{Be}^{\prime} \mathrm{Rb}^{\prime}{ }_{3}\right]$ are the energies of the $\left[\mathrm{Rb}_{3} \mathrm{BeB}_{6} \mathrm{Be}^{\prime} \mathrm{Rb}^{\prime}{ }_{3}\right]^{+}$cation and $\left[\mathrm{Rb}_{3} \mathrm{BeB}_{6} \mathrm{Be}^{\prime} \mathrm{Rb}_{3}^{\prime}\right]$. Both were calculated with the same geometry as that of neutral $\mathrm{Rb}_{3} \mathrm{BeB}_{6} \mathrm{Be}^{\prime} \mathrm{Rb}^{\prime}{ }_{3}$.
In general, for a nonspherically symmetric molecule in an OEEF, if the orientation dependence of OEEF effect is ignored, the magnitude order of the electron tunneling ionization rate $(\omega)$ can be roughly obtained from the following formula: ${ }^{41,42}$

$$
\begin{equation*}
\omega=4 \frac{\omega_{0}}{|F|}(2 \mathrm{VIE})^{5 / 2} \exp \left[-\frac{2(2 \mathrm{VIE})^{3 / 2}}{3|F|}\right] \tag{2}
\end{equation*}
$$

where both $F$ and VIE are measured in atomic units and $\omega_{0}=4$ $\times 10^{16} \mathrm{~s}^{-1}$.

It is known that, if the finite field (FF) approach is used to evaluate the $\beta_{0}$ value, there may occur a contamination risk from higher-order hyperpolarizabilities ${ }^{43,44}$

$$
\begin{align*}
\beta(F)= & 2 \frac{\mu(2 F)-\mu(F)}{F}=\frac{2 \boldsymbol{E}_{\mathrm{A}}(F)-\boldsymbol{E}_{\mathrm{A}}(2 F)}{F^{3}} \\
& =\beta+\frac{\delta F^{2}}{4}+\mathrm{O}\left(F^{4}\right) \tag{3}
\end{align*}
$$

However, it can be eliminated by using the Richardson extrapolation procedure. ${ }^{42,43}$ In our previous study, it has been shown that the above contamination can be ignored for several excess electron compounds. ${ }^{24-26}$ Then, a field amplitude of 10 $\times 10^{-4}$ au was used for the FF method. The optimized
structures of $\mathrm{Rb}_{6} \mathrm{Be}_{2} \mathrm{~B}_{6}$ without the presence of $F_{z}$ were considered.

For the $\beta_{0}$ value of electride Li@pyrrole, it has been suggested ${ }^{45}$ that the MP2 value is close to the expensive higher-order QCISD one. Also, for some similar electride systems, ${ }^{26,27}$ the MP2 method is reliable to investigate the $\beta_{0}$ values. M06-2X not only exhibits positive behavior for calculating electronic structures, but it is also widely utilized to calculate $\beta_{0}$ values. ${ }^{21,22,46}$ Therefore, the $\beta_{0}{ }^{e}$ values of $\mathrm{Rb}_{3} \mathrm{BeB}_{6} \mathrm{Be}^{\prime} \mathrm{Rb}_{3}{ }_{3}$ were obtained at both M06-2X/def2-qzvp and MP2/def2-qzvp levels. The electronic spectra were obtained with the time-dependent TD-PBE0/def2-qzvp level. To find which excitation path(s) makes the main contribution to the total $\beta_{0}{ }^{\mathrm{e}}, 250$ excited states are considered.

The $\beta_{0}{ }^{\mathrm{e}}$ is noted as

$$
\begin{equation*}
\beta_{0}^{\mathrm{e}}=\left(\beta_{\mathrm{x}}^{2}+\beta_{\mathrm{y}}^{2}+\beta_{\mathrm{z}}^{2}\right)^{1 / 2} \tag{4}
\end{equation*}
$$

The Bishop-Hasan-Kirtman (BHK) approach ${ }^{47}$ is applied to calculate the vibrational contribution to static first hyperpolarizability $\left(\beta_{z z z}{ }^{\mathrm{nr}}\right)$. This method is a numerical approach. The $\beta_{z z z}{ }^{n r}$ is written by the following equations

$$
\begin{align*}
& \beta_{z z z}^{\text {tot }}=\beta_{z z z}^{\mathrm{e}}+\beta_{z z z}^{\mathrm{nr}}  \tag{5}\\
& \beta_{z z z, \text { tot }}= \\
& \frac{\left[\Delta \mu_{\mathrm{i}, \mathrm{z}}\left(R_{F}, F_{\mathrm{z}, \mathrm{i}}\right)\right]+2 \Delta \mu_{\mathrm{z}}\left(R_{F w}, F w_{\mathrm{z}}\right)+\left[\Delta \mu_{\mathrm{i}, \mathrm{z}}\left(R_{F}, F_{\mathrm{z}, \mathrm{i}}\right)\right]}{\Delta F^{2}}  \tag{6}\\
& \Delta \mu_{\mathrm{z}}\left(R_{F}, F_{\mathrm{z}}\right)=\mu_{\mathrm{z}}\left(R_{F}, F_{\mathrm{z}}\right)-\mu_{\mathrm{z}}\left(R_{F w}, F w_{\mathrm{z}}\right) \tag{7}
\end{align*}
$$

where $\beta_{z z z}{ }^{\text {tot }}$ represents the total static first hyperpolarizability, the electronic and vibrational contribution to $\beta_{z z z}$ tot were, respectively, written as $\beta_{z z z}{ }^{\mathrm{e}}$ and $\beta_{z z z}{ }^{\mathrm{nr}} ; \Delta \mu_{z}\left(R_{F}, F_{z}\right)$ is the difference of dipole moments between dipole moment of test $\left(\mu_{\mathrm{z}}\left(R_{F}, F_{z}\right)\right)$ and that of work OEEF $\left(\mu_{\mathrm{z}}\left(R_{F w}, F w\right)\right)$; and $R_{\mathrm{F}}$ represents the equilibrium geometry in the presence of an OEEF.

The frequency-dependent NLO properties $(\beta(-2 \omega, \omega, \omega))$ of $\mathrm{Rb}_{3} \mathrm{BeB}_{6} \mathrm{Be}^{\prime} \mathrm{Rb}_{3}^{\prime}$ were calculated at the PBEO/def2-qzvp level. Imitating to the reported multiplicative scheme, ${ }^{13}$ the $\beta(-2 \omega, \omega, \omega)$ values at MP2 method were estimated by

$$
\begin{align*}
& \beta_{\mathrm{MP} 2}(-2 \omega ; \omega, \omega) \\
& \approx \beta_{\mathrm{MP} 2}(0 ; 0,0) \times \beta_{\mathrm{TD}-\mathrm{M} 06-2 \mathrm{X}}(-2 \omega ; \omega, \omega) \\
& \quad / \beta_{\mathrm{CP}-\mathrm{M} 06-2 \mathrm{X}}(0 ; 0,0) \tag{8}
\end{align*}
$$

The molecular structures and molecular orbitals as well as the electronic absorption spectra were plotted with GaussView program. ${ }^{48}$

## RESULTS AND DISCUSSION

Self-Redox from $\left[\mathrm{Rb}_{3} \mathrm{Be}\right]^{3+}\left[\mathrm{B}_{6}\right]^{6-}\left[\mathrm{Be}^{\prime} \mathrm{Rb}^{\prime}{ }_{3}\right]^{3+}$ to $\left[\mathrm{Rb}_{3} \mathrm{Be}\right]^{2+}\left[\mathrm{B}_{6}\right]^{6-}\left[\mathrm{Be}^{\prime} \mathrm{Rb}^{\prime}{ }_{3}\right]^{4+}$. The optimized structure with all real frequencies of $D_{3 d} \mathrm{Rb}_{3} \mathrm{BeB}_{6} \mathrm{Be}^{\prime} \mathrm{Rb}_{3}{ }_{3}$ is shown in Figure 1. According to the NPA charge analysis, the valences of both tetrahedral $\mathrm{BeRb}_{3}$ ligands are +3 . Then, the salt-like structure has been suggested to be $\left[\mathrm{Rb}_{3} \mathrm{Be}\right]^{3+}\left[\mathrm{B}_{6}\right]^{6-}\left[\mathrm{Be}^{\prime} \mathrm{Rb}^{\prime}{ }_{3}\right]^{3+} .{ }^{30}$ Our calculations can acknowledge it by using the data from NPA charges at MP2, PBE0, and $\operatorname{CASSCF}(2,2)$ methods with the def2-qzvp basis set (see Table 1). The values in Table 1 indicate that the NPA charges calculated at MP2/def2-qzvp,


Figure 1. Evolution of bond lengths of $\mathrm{Rb}_{3} \mathrm{BeB}_{6} \mathrm{Be}^{\prime} \mathrm{Rb}^{\prime}{ }_{3}$ with the increasing external electric field strength $\left(F_{z}\right)$.

Table 1. NPA Charges of $\mathrm{Q}_{\mathrm{Rb}_{3} B e}, \mathrm{Q}_{\mathrm{B}_{6}}$, and $\mathrm{Q}_{\mathrm{Be}^{\prime} \mathrm{Rb}^{\prime}{ }_{3}}$ in $\mathrm{Rb}_{3} \mathrm{BeB}_{6} \mathrm{Be}^{\prime} \mathrm{Rb}^{\prime}{ }_{3}$ with Respect to $\operatorname{OEEF}\left(F_{z}\right)$ at Different Methods

|  | $F_{\mathrm{z}}\left(\times 10^{-4} \mathrm{au}\right)$ |  |  |  |
| :---: | :---: | :---: | :---: | :---: |
|  | 0 | 50 | 55 | 65 |
| MP2/def2-qzvp |  |  |  |  |
| $Q_{\text {Rb } b_{3} \mathrm{Be}}$ | 2.756 | 2.058 | 1.932 | 1.792 |
| $Q_{B_{6}}$ | -5.513 | -5.546 | -5.559 | -5.560 |
| $\mathrm{QBe}^{\prime} \mathrm{Rb}^{\prime}{ }_{3}$ | 2.756 | 3.488 | 3.626 | 3.768 |
| PBE0/def2-qzvp |  |  |  |  |
| $Q_{\text {Rb } b_{3} \text { Be }}$ | 2.820 | 2.364 | 2.286 | 2.093 |
| $Q_{B_{6}}$ | -5.640 | -5.651 | -5.660 | -5.663 |
| $Q_{B^{\prime} \mathrm{Rb}^{\prime}{ }_{3}}$ | 2.820 | 3.287 | 3.374 | 3.570 |
| $\operatorname{CASSCF}(2,2) /$ def2-qzvp |  |  |  |  |
| $Q_{\mathrm{Rb}_{3} \mathrm{Be}}$ | 2.828 | 2.474 | 1.838 | 1.863 |
| $Q_{\mathrm{B}_{6}}$ | -5.657 | -5.674 | -5.673 | -5.691 |
| $Q_{B E S^{\prime} \mathrm{Rb}^{\prime}}$ | 2.828 | 3.202 | 3.348 | 3.637 |

PBE0/def2-qzvp, and $\operatorname{CASSCF}(2,2) /$ def2-qzvp levels are $2.756,2.820$, and 2.828 lel, respectively, for both $\left[\mathrm{Rb}_{3} \mathrm{Be}\right]$ and $\left[\mathrm{Be}^{\prime} \mathrm{Rb}^{\prime}{ }_{3}\right]$.
In the present work, considering a larger OEEF ( $F_{\mathrm{z}} \geq 65 \times$ $10^{-4} \mathrm{au}$ ) will destroy the geometrical structure of $\mathrm{Rb}_{3} \mathrm{BeB}_{6} \mathrm{Be}^{\prime} \mathrm{Rb}_{3}^{\prime}, F_{\mathrm{z}}=65 \times 10^{-4}$ au $(1 \mathrm{au}=51.422 \mathrm{~V} / \AA)$ is used as a critical value $\left(F_{c}\right)$. Then, the OEEF along with the dipole moment direction ( $F_{z}$, see Figure 1) for $\mathrm{Rb}_{3} \mathrm{BeB}_{6} \mathrm{Be}^{\prime} \mathrm{Rb}_{3}^{\prime}$ is in the range of $0-65 \times 10^{-4}$ au. To estimate the effect of OEEF on the geometrical structure, some important geometrical parameters ( $R b-R b$ length, $R_{1}, R_{2}, R_{1}{ }^{\prime}$, and $\mathrm{R}_{2}{ }^{\prime}$ ) of $\mathrm{Rb}_{3} \mathrm{BeB}_{6} \mathrm{Be}^{\prime} \mathrm{Rb}^{\prime}{ }_{3}$ were collected and are listed in Table S1. From Figure 1 and Table S1, it can be found that, as the magnitude of $F_{\mathrm{z}}$ increases, the $\mathrm{Rb}^{\prime}-\mathrm{Rb}^{\prime}$ bond length and the distance between Be ' atom and the center of $\mathrm{Rb}^{\prime}{ }_{3}$ ring ( $\mathrm{R1}^{\prime}$ ) in top tetrahedral $\mathrm{Be}^{\prime} \mathrm{Rb}_{3}^{\prime}$ slightly increase, while both $\mathrm{Rb}-\mathrm{Rb}$ bond length and R1 in bottom tetrahedral $\mathrm{Rb}_{3} \mathrm{Be}$ almost do not change. As a result, $D_{3 d} \mathrm{Rb}_{3} \mathrm{BeB}_{6} \mathrm{Be}^{\prime} \mathrm{Rb}_{3}^{\prime}$ with two identical tetrahedral ligands $\left(\mathrm{Rb}_{3} \mathrm{Be}=\mathrm{Be}^{\prime} \mathrm{Rb}^{\prime}{ }_{3}\right)$ changes into $C_{3 v} \mathrm{Rb}_{3} \mathrm{BeB}_{6} \mathrm{Be}^{\prime} \mathrm{Rb}_{3}^{\prime}$ with one slightly larger $\left(\mathrm{Be}^{\prime} \mathrm{Rb}^{\prime}{ }_{3}\right)$ and one smaller tetrahedral ligand $\left(\mathrm{Rb}_{3} \mathrm{Be}\right)$. However, there is only small ( $<0.3 \AA$ ) increases of $R b^{\prime}-R b^{\prime}$ bond length in $\mathrm{Be}^{\prime} \mathrm{Rb}^{\prime}{ }_{3}$ in the presence of $F_{\mathrm{z}}=65 \times 10^{-4}$ au as compared to $\mathrm{Rb}_{3} \mathrm{Be}$ for field-free $\mathrm{Rb}_{3} \mathrm{BeB}_{6} \mathrm{Be}^{\prime} \mathrm{Rb}^{\prime}{ }_{3}$. This behavior may be
beneficial for the molecular assembly of $\mathrm{Rb}_{3} \mathrm{BeB}_{6} \mathrm{Be}^{\prime} \mathrm{Rb}^{\prime}{ }_{3}$ in the terminal devices.

The larger the size of the tetrahedral structure has, the larger the NPA charge or the fewer the number of electrons it owns. The results in Figure 2a and Table 1 as well as Table S2 show that, at the MP2/def2-qzvp level, the NPA charge of the top tetrahedral $\mathrm{Be}^{\prime} \mathrm{Rb}_{3}^{\prime}$ increases but that of bottom tetrahedral $\mathrm{Rb}_{3} \mathrm{Be}$ decreases along with an increase in the magnitude of $F_{\mathrm{z}}$. Meanwhile, the NPA charge of the $\mathrm{B}_{6}$ ring does not change evidently. As $F_{z}=50 \times 10^{-4} \mathrm{au}$, the NPA charges of $\mathrm{Be}^{\prime} \mathrm{Rb}^{\prime}{ }_{3}$ and $\mathrm{Rb}_{3} \mathrm{Be}$ are 3.488 and 2.058 lel, respectively, and the NPA charges in each case are 3.626 and 1.932 lel, respectively, as $F_{\mathrm{z}}$ $=55 \times 10^{-4} \mathrm{au}$. For an even larger $F_{z}$ of $65 \times 10^{-4}$ au, the NPA charges are 3.768 and 1.792 lel, respectively, for $\mathrm{Be}^{\prime} \mathrm{Rb}_{3}{ }_{3}$ and $\mathrm{Rb}_{3} \mathrm{Be}$. These show that the valences of $\mathrm{Be}^{\prime} \mathrm{Rb}_{3}{ }_{3}$ and $\mathrm{Rb}_{3} \mathrm{Be}$ in $\mathrm{Rb}_{3} \mathrm{BeB}_{6} \mathrm{Be}^{\prime} \mathrm{Rb}_{3}^{\prime}$ in the presence of $F_{\mathrm{z}} \geq 50 \times 10^{-4}$ au are +4 and +2 , respectively. Similar NPA behaviors can be confirmed using both PBE0/def2-qzvp and $\operatorname{CASSCF}(2,2) /$ def2-qzvp levels (see Table 1).

Considering the solvent effect, we have calculated the NPA charges of $\mathrm{Rb}_{3} \mathrm{BeB}_{6} \mathrm{Be}^{\prime} \mathrm{Rb}_{3}^{\prime}$ with solvents of THF and cyclohexane $\left(\mathrm{C}_{6} \mathrm{H}_{12}\right)$ in the presence of $F_{z}=50 \times 10^{-4}$ au. From Table 2, at the PBE0/def2-qzvp level, the NPA charges of $\mathrm{Be}^{\prime} \mathrm{Rb}^{\prime}{ }_{3}$ and $\mathrm{Rb}_{3} \mathrm{Be}$ are, respectively, 3.836 and 1.854 lel for the solvent of THF and are 3.507 and 2.181 lel for the solvent of $\mathrm{C}_{6} \mathrm{H} 12$. At the MP2/def2-qzvp level, the NPA charges of $\mathrm{Be}^{\prime} \mathrm{Rb}_{3}{ }_{3}$ and $\mathrm{Rb}_{3} \mathrm{Be}$ are, respectively, 4.455 and 1.205 lel for the solvent of THF and are 3.390 and 2.305 lel for the solvent of $\mathrm{C}_{6} \mathrm{H}_{12}$. These results show that the influence of a solvent on the redox reaction under the OEEF is not very large. In both solvents, the valences of $\mathrm{Be}^{\prime} \mathrm{Rb}^{\prime}{ }_{3}$ and $\mathrm{Rb}_{3} \mathrm{Be}$ in $\mathrm{Rb}_{3} \mathrm{BeB}_{6} \mathrm{Be}^{\prime} \mathrm{Rb}^{\prime}{ }_{3}$ in the presence of $F_{z}=50 \times 10^{-4}$ au are still +4 and +2 , respectively.

The electron clouds of frontier molecular orbitals can provide support for this. The highest occupied molecular orbital (HOMO) and HOMO - 1 are also shown in Figure 2. For the HOMO, when the OEEF goes from 0 to 50 or $65 \times$ $10^{-4} \mathrm{au}$, the shape of its orbital is changed from a symmetric dumbbell shape of two lobes to a larger and a smaller lobe. Similar behaviors can be seen in the ELF and LOL maps (see Figure 2b,c).

So, the salt-like structure of $\mathrm{Rb}_{3} \mathrm{BeB}_{6} \mathrm{Be}^{\prime} \mathrm{Rb}^{\prime}{ }_{3}$ in the presence of $F_{z} \geq 50 \times 10^{-4}$ au is $\left[\mathrm{Rb}_{3} \mathrm{Be}\right]^{2+}\left[\mathrm{B}_{6}\right]^{6-}\left[\mathrm{Be}^{\prime} \mathrm{Rb}_{3}^{\prime}\right]^{4+}$. These results indicate that applying a critical $F_{z}$ of $50 \times 10^{-4}$ au or even a larger one in the z -axis positive direction of the field-free $\mathrm{Rb}_{3} \mathrm{BeB}_{6} \mathrm{Be}^{\prime} \mathrm{Rb}_{3}{ }_{3}$ can drive an electron to transfer from tetrahedral $\mathrm{Be}^{\prime} \mathrm{Rb}^{\prime}{ }_{3}$ to $\mathrm{Rb}_{3} \mathrm{Be}$, and then, the IMSR occurs and $\left[\mathrm{Rb}_{3} \mathrm{Be}\right]^{3+}\left[\mathrm{B}_{6}\right]^{6-}\left[\mathrm{Be}^{\prime} \mathrm{Rb}^{\prime}\right]^{3+}$ changes into $\left[\mathrm{Rb}_{3} \mathrm{Be}\right]^{2+}\left[\mathrm{B}_{6}\right]^{6-}\left[\mathrm{Be}^{\prime} \mathrm{Rb}_{3}{ }_{3}\right]^{4+}$.

Stabilities. Owing to the occurrence of $\operatorname{OEEF}(\mathrm{s})$, it deserves careful consideration of the stability of $\left[\mathrm{Rb}_{3} \mathrm{Be}\right]^{2+}\left[\mathrm{B}_{6}\right]^{6-}\left[\mathrm{Be}^{\prime} \mathrm{Rb}_{3}^{\prime}\right]^{4+}$. The results on the stability are given in Figure 3 and Table S2. From Figure 3a and Table S2, one can found that the total energy monotonically decreases with increasing the intensity of OEEF in positive directions of z -axis (from $F_{\mathrm{z}}=0$ to $65 \times 10^{-4} \mathrm{au}$ ). Therefore, the thermodynamic stability of $\mathrm{Rb}_{3} \mathrm{BeB}_{6} \mathrm{Be}^{\prime} \mathrm{Rb}_{3}{ }_{3}$ is gaining strength along with an increase in the magnitude of $F_{z}$. $\left[\mathrm{Rb}_{3} \mathrm{Be}\right]^{2+}\left[\mathrm{B}_{6}\right]^{6-}\left[\mathrm{Be}^{\prime} \mathrm{Rb}_{3}{ }_{3}\right]^{4+}$ in the presence of $F_{z} \geq 50 \times$ $10^{-4}$ au possesses a higher thermodynamic stability than that of the $\left[\mathrm{Rb}_{3} \mathrm{Be}\right]^{3+}\left[\mathrm{B}_{6}\right]^{6-}\left[\mathrm{Be}^{\prime} \mathrm{Rb}_{3}{ }_{3}\right]^{3+}$ in the presence of $F_{\mathrm{z}}<50 \times$ $10^{-4}$ au. For a molecule, the electronic stability may be characterized by its VIE values. For the gap ( $\varepsilon_{\text {gap }}$ ) between the


Figure 2. (a) Evolutions of NPA charges of $\mathrm{Rb}_{3} \mathrm{BeB}_{6} \mathrm{Be}^{\prime} \mathrm{Rb}^{\prime}{ }_{3}$ with the increasing external electric field strength $\left(F_{z}\right)$. (b) HOMOs at the isovalue of 0.02 au . (c) ELF maps and LOL maps of $\mathrm{Rb}_{3} \mathrm{BeB}_{6} \mathrm{Be}^{\prime} \mathrm{Rb}^{\prime}{ }_{3}$ in the presence of different $F_{7}$.

Table 2. NPA Charges of $Q_{\mathrm{Rb}_{3} \mathrm{Be}}, Q_{\mathrm{B}_{6}}$, and $Q_{\mathrm{Be}^{\prime} \mathrm{Rb}^{\prime}{ }_{3}}$ in $\mathrm{Rb}_{3} \mathrm{BeB}_{6} \mathrm{Be}^{\prime} \mathrm{Rb}_{3}{ }_{3}$ with Different Solvents at PBE0/def2-qzvp and MP2/def2-qzvp Levels in the Presence of $F_{z}=50 \times$ $10^{-4} \mathrm{au}$

|  | PBE0 |  |  | MP2 |  |  |  |  |  |  |  |
| :--- | ---: | ---: | ---: | ---: | ---: | :---: | :---: | :---: | :---: | :---: | :---: |
|  | THF |  |  |  |  |  |  | $\mathrm{C}_{6} \mathrm{H}_{12}$ |  | THF | $\mathrm{C}_{6} \mathrm{H}_{12}$ |
| $\mathrm{Q}_{\mathrm{Rb}_{3} \mathrm{Be}}$ | 1.854 | 2.181 |  | 1.205 | 2.305 |  |  |  |  |  |  |
| $\mathrm{Q}_{\mathrm{B}_{6}}$ | -5.690 | -5.687 |  | -5.660 | -5.694 |  |  |  |  |  |  |
| $Q_{\mathrm{Be}^{\prime} \mathrm{Rb}^{\prime}{ }_{3}}$ | 3.836 | 3.507 |  | 4.455 | 3.390 |  |  |  |  |  |  |

HOMO and LUMO (lowest unoccupied molecular orbital), a large $\varepsilon_{\text {gap }}$ value reflects high chemical stability. The results in Figure 3b,c and Table S2 show that the VIE value increases and the $\varepsilon_{\text {gap }}$ value decreases along with an increase in the magnitude of $F_{z}$. So, the electronic stability ascends, and the molecular chemical stability descends along with an increase in the magnitude of $F_{7}$. As a result, $\left[\mathrm{Rb}_{3} \mathrm{Be}\right]^{2+}\left[\mathrm{B}_{6}\right]^{6-}\left[\mathrm{Be}^{\prime} \mathrm{Rb}_{3}{ }_{3}\right]^{4+}$ in the presence of $F_{z} \geq 50 \times 10^{-4}$ au owns a higher electronic stability but lower chemical stability than that of $\left[\mathrm{Rb}_{3} \mathrm{Be}\right]^{3+}\left[\mathrm{B}_{6}\right]^{6-}\left[\mathrm{Be}^{\prime} \mathrm{Rb}_{3}{ }_{3}\right]^{3+}$ in the presence of $F_{\mathrm{z}}<50 \times$ $10^{-4}$ au.
The $\varepsilon_{\text {gap }}$ value of $\left[\mathrm{Rb}_{3} \mathrm{Be}\right]^{3+}\left[\mathrm{B}_{6}\right]^{6-}\left[\mathrm{Be}^{\prime} \mathrm{Rb}^{\prime}{ }_{3}\right]^{3+}$ in the presence of $F_{z}=50 \times 10^{-4}$ au is 1.996 eV . It is smaller than that of the reported redox switch $\mathrm{Li}_{3}{ }^{+} \mathrm{N}_{3}{ }^{3-} \mathrm{Mg}^{2+}$ in the presence of $F_{z}=72 \times 10^{-4}$ and $86 \times 10^{-4}$ au $(2.327$ and 2.314 eV$) .{ }^{27}$ However, it is much larger for $\left[\mathrm{Rb}_{3} \mathrm{Be}\right]^{3+}\left[\mathrm{B}_{6}\right]^{6-}\left[\mathrm{Be}^{\prime} \mathrm{Rb}^{\prime}{ }_{3}\right]^{3+}$ in the presence of $F_{z}=50 \times 10^{-4}$ au than for the reported $\mathrm{K}(1)^{+} \ldots$ calix[4] pyrrole $\cdots \mathrm{K}(2)^{+} \ldots 2 \mathrm{e}^{-}(1.315-1.719 \mathrm{eV})^{49}$ and $\left.\mathrm{e}^{-}+\mathrm{Ca}^{2+}\left(\mathrm{Ni} @ \mathrm{~Pb}_{12}\right)^{2-} \mathrm{Ca}^{2+}+2 \mathrm{e}^{-}(0.96-1.45 \mathrm{eV})\right)^{21}$ As a result, $\left[\mathrm{Rb}_{3} \mathrm{Be}\right]^{3+}\left[\mathrm{B}_{6}\right]^{6-}\left[\mathrm{Be}^{\prime} \mathrm{Rb}_{3}^{\prime}\right]^{3+}$ in the presence of $F_{\mathrm{z}}=50 \times 10^{-4}$ au with larger $\varepsilon_{\text {gap }}$ has larger chemical stability than the reported molecular switches of $\mathrm{e}^{-} \cdots \mathrm{K}(1)^{+} \ldots$ calix $[4]$ pyrrole $\cdots$ $\mathrm{K}(2)^{+} \ldots \mathrm{e}^{-}$and $\mathrm{e}^{-}+\mathrm{M}^{2+}\left(\mathrm{Ni} @ \mathrm{~Pb}_{12}\right)^{2-} \mathrm{M}^{2+}+\mathrm{e}^{-}(\mathrm{M}=\mathrm{Be}, \mathrm{Mg}$, and Ca). The VIEs of $\mathrm{Li}_{3}{ }^{+} \mathrm{N}_{3}{ }^{3-} \mathrm{Mg}^{2+}$ in the presence of $F_{z}=72$ $\times 10^{-4}$ and $86 \times 10^{-4} \mathrm{au}^{27} \mathrm{Li}^{-}-\mathrm{LCa}^{2+} \mathrm{L}^{2} \mathrm{Li}^{-}, \mathrm{Na}^{-}-\mathrm{LCa}^{2+} \mathrm{L}-\mathrm{Na}^{-}$ $\left(\mathrm{L}=\mathrm{F}_{6} \mathrm{C}_{6} \mathrm{H}_{6}\right),{ }^{20}$ and $\mathrm{e}^{-}+\mathrm{Ca}^{2+}\left(\mathrm{Ni} @ \mathrm{~Pb}_{12}\right)^{2-} \mathrm{Ca}^{2+}+2 \mathrm{e}^{-21}$, are
5.05, 5.05, 4.12, 4.04, and 4.48 eV . They are larger than (3.512 eV ) that of $\left[\mathrm{Rb}_{3} \mathrm{Be}\right]^{3+}\left[\mathrm{B}_{6}\right]^{6-}\left[\mathrm{Be}^{\prime} \mathrm{Rb}_{3}^{\prime}\right]^{3+}$ in the presence of $F_{\mathrm{z}}=$ $50 \times 10^{-4}$ au.

In general, it is on a time scale of approximately $10-10^{4} \mathrm{fs}^{50}$ for the occurrence of a chemical reaction. So, for a molecule under an OEEF, an order of magnitude threshold of around $10^{11} \mathrm{~s}^{-1}$ may be appropriate by taking the reciprocal of $10^{-4}$ $\mathrm{fs}^{-1}$ as the max acceptable average tunneling ionization rate $(\omega) .{ }^{35}$ Given that, the $\omega$ values listed in Figure 3 b and Table S2 indicate that except the structure in the presence of $F_{z}=55$ $\times 10^{-4} \mathrm{au}$, all the $\omega$ values of other structures are smaller than $10^{11} \mathrm{~s}^{-1}$. Therefore, except for the structure in the presence of $F_{\mathrm{z}}=55 \times 10^{-4} \mathrm{au}$, all the other structures of $\left[\mathrm{Rb}_{3} \mathrm{Be}\right]^{2+}\left[\mathrm{B}_{6}\right]^{6-}\left[\mathrm{Be}^{\prime} \mathrm{Rb}_{3}{ }_{3}\right]^{4+}$ may be stable.

Candidate for NLO Molecular Switches. Because the calculated $\beta_{0}{ }^{e}$ is sensitive to the OEEF, ${ }^{43,44}$ the optimized structures of $\left[\mathrm{Rb}_{3} \mathrm{Be}\right]^{2+}\left[\mathrm{B}_{6}\right]^{6-}\left[\mathrm{Be}^{\prime} \mathrm{Rb}_{3}{ }_{3}\right]^{4+}$ with no consideration of the presence of $F_{z}$ were used to calculate $\beta_{0}{ }^{\mathrm{e}}$. Considering the structural differentiation of $\mathrm{Rb}_{3} \mathrm{BeB}_{6} \mathrm{Be}^{\prime} \mathrm{Rb}^{\prime}{ }_{3}$, their different structures are named $\mathrm{Rb}_{3} \mathrm{BeB}_{6} \mathrm{Be}^{\prime} \mathrm{Rb}_{3}{ }_{3}(n)$, where $n$ is the significant digit of magnitude of the initial $F_{z}$. Then, field-free $\mathrm{Rb}_{3} \mathrm{BeB}_{6} \mathrm{Be}^{\prime} \mathrm{Rb}^{\prime}{ }_{3}(50)$ denotes the initial optimized structures of $\left[\mathrm{Rb}_{3} \mathrm{Be}\right]^{2+}\left[\mathrm{B}_{6}\right]^{6-}\left[\mathrm{Be}^{\prime} \mathrm{Rb}_{3}^{\prime}\right]^{4+}$ in the presence of $F_{z}$ $=50 \times 10^{-4} \mathrm{au}$.

For $\beta_{0}{ }^{\mathrm{e}}$, it is noteworthy that Figure 4 and Table S3 show a pronounced discrepancy in the redox process at the M06-2X/ def2-qzvp level. For the field-free $\mathrm{Rb}_{3} \mathrm{BeB}_{6} \mathrm{Be}^{\prime} \mathrm{Rb}^{\prime}{ }_{3}$ $\left(\left[\mathrm{Rb}_{3} \mathrm{Be}\right]^{3+}\left[\mathrm{B}_{6}\right]^{6-}\left[\mathrm{Be}^{\prime} \mathrm{Rb}_{3}^{\prime}\right]^{3+}\right)$ with the $D_{3 \mathrm{~d}}$ point group, both $\mu_{0}$ and $\beta_{0}{ }^{\mathrm{e}}$ are zero. Then, $\left[\mathrm{Rb}_{3} \mathrm{Be}\right]^{3+}\left[\mathrm{B}_{6}\right]^{6-}\left[\mathrm{Be}^{\prime} \mathrm{Rb}_{3}{ }_{3}\right]^{3+}$ is the off-form of the IMSR NLO switch. The $\beta_{0}{ }^{\mathrm{e}}$ or $\beta_{z z z}{ }^{\mathrm{e}}$ value of $\mathrm{Rb}_{3} \mathrm{BeB}_{6} \mathrm{Be}^{\prime} \mathrm{Rb}^{\prime}{ }_{3}(\mathrm{n})$ increases first and then decreases with an increase in the magnitude of $n(n=0-65)$. As $n=45$, the $\beta_{0}{ }^{\text {e }}$ or $\beta_{z z z}{ }^{e}$ value reaches its maximum $\left(1.45 \times 10^{5} \mathrm{au}\right)$ at the M06$2 \mathrm{X} / \mathrm{def} 2-\mathrm{qzvp}$ level. However, the neighboring $\mathrm{Rb}_{3} \mathrm{BeB}_{6} \mathrm{Be}^{\prime} \mathrm{Rb}^{\prime}{ }_{3}(50)$, i.e., $\left[\mathrm{Rb}_{3} \mathrm{Be}\right]^{2+}\left[\mathrm{B}_{6}\right]^{6-}\left[\mathrm{Be}^{\prime} \mathrm{Rb}^{\prime}{ }_{3}\right]^{4+}$, has been used as the on-form of the redox NLO molecular switch considering the NPA charge of tetrahedral $\mathrm{Be}^{\prime} \mathrm{Rb}^{\prime}{ }_{3}$ and $\mathrm{Rb}_{3} \mathrm{Be}$. The $\beta_{0}{ }^{\text {e }}$ values of $\mathrm{Rb}_{3} \mathrm{BeB}_{6} \mathrm{Be}^{\prime} \mathrm{Rb}^{\prime}{ }_{3}(50)$ at the M06-2X/def2-


Figure 3. Evolutions of (a) relative energy $\left(E_{\text {rel }}\right)$, (b) VIE, and (c) $\varepsilon_{\text {gap }}$ of $\mathrm{Rb}_{3} \mathrm{BeB}_{6} \mathrm{Be}^{\prime} \mathrm{Rb}^{\prime}{ }_{3}$ with increasing external electric field strength ( $F_{z}$ ). The electron tunneling ionization rates $\left(\omega, \mathrm{s}^{-1}\right)$ are within parentheses.


Figure 4. Evolutions of (a) $\beta_{0}$ and $\beta_{\text {zzz }}$ values of $\mathrm{Rb}_{3} \mathrm{BeB}_{6} \mathrm{Be}^{\prime} \mathrm{Rb}^{\prime}{ }_{3}(\mathrm{n})$ with an increase in $n(n=0-65)$ at the M06-2X/def2-qzvp level. The MP2/ def2-qzvp values are within parentheses.
qzvp and MP2/def2-qzvp levels are $1.42 \times 10^{5}$ and $2.18 \times 10^{5}$ au , respectively. Then, the $\mu_{0}(3.36 \mathrm{D})$ and $\beta_{0}{ }^{\mathrm{e}}\left(2.18 \times 10^{5} \mathrm{au}\right)$ values of $\left[\mathrm{Rb}_{3} \mathrm{Be}\right]^{2+}\left[\mathrm{B}_{6}\right]^{6-}\left[\mathrm{Be}^{\prime} \mathrm{Rb}^{\prime}{ }_{3}\right]^{4+}\left(\mathrm{Rb}_{3} \mathrm{BeB}_{6} \mathrm{Be}^{\prime} \mathrm{Rb}^{\prime}{ }_{3}(50)\right)$ at the MP2/def2-qzvp level have been used in the following discussion.
Owing to the $D_{3 \mathrm{~d}}$ symmetry, the dipole moment $\left(\mu_{0}\right)$ of $\left[\mathrm{Rb}_{3} \mathrm{Be}\right]^{3+}\left[\mathrm{B}_{6}\right]^{6-}\left[\mathrm{Be}^{\prime} \mathrm{Rb}^{\prime}{ }_{3}\right]^{3+}$ is zero. From Table 3, the $\mu_{0}$ value of the $\mathrm{C}_{3 v}\left[\mathrm{Rb}_{3} \mathrm{Be}\right]^{2+}\left[\mathrm{B}_{6}\right]^{6-}\left[\mathrm{Be}^{\prime} \mathrm{Rb}_{3}^{\prime}\right]^{4+} 3.36 \mathrm{D}$. Then, the dipole moment of $\mathrm{Rb}_{3} \mathrm{BeB}_{6} \mathrm{Be}^{\prime} \mathrm{Rb}_{3}^{\prime}$ exhibits a good performance NLO switching effect from $\left[\mathrm{Rb}_{3} \mathrm{Be}\right]^{3+}\left[\mathrm{B}_{6}\right]^{6-}\left[\mathrm{Be}^{\prime} \mathrm{Rb}_{3}{ }_{3}\right]^{3+}$ to $\left[\mathrm{Rb}_{3} \mathrm{Be}\right]^{3+}\left[\mathrm{B}_{6}\right]^{6-}\left[\mathrm{Be}^{\prime} \mathrm{Rb}_{3}^{\prime}\right]^{4+}$.

The $\beta_{0}{ }^{\text {e }}\left(2.18 \times 10^{5} \mathrm{au}\right)$ value of the on-form of $\mathrm{Rb}_{3} \mathrm{BeB}_{6} \mathrm{Be}^{\prime} \mathrm{Rb}^{\prime}{ }_{3}\left(\left[\mathrm{Rb}_{3} \mathrm{Be}\right]^{2+}\left[\mathrm{B}_{6}\right]^{6-}\left[\mathrm{Be}^{\prime} \mathrm{Rb}^{\prime}{ }_{3}\right]^{4+}=\right.$ $\left.\mathrm{Rb}_{3} \mathrm{BeB}_{6} \mathrm{Be}^{\prime} \mathrm{Rb}^{\prime}{ }_{3}(50)\right)$ is more than two times of that of the redox switch of $\mathrm{Li}_{3}{ }^{+} \mathrm{N}_{3}{ }^{3-} \mathrm{Mg}^{2+}\left(1.01 \times 10^{5} \mathrm{au}\right) .{ }^{27}$ For the reported OEEF-induced NLO molecular switches, the $\beta_{0}$ values of on-forms of Lithium@cyclo[18]carbon, ${ }^{19} \mathrm{Na}^{-}-$ $L \mathrm{Ca}^{2+} L-\mathrm{Na}^{-}\left(L=\mathrm{F}_{6} \mathrm{C}_{6} \mathrm{H}_{6}\right),,^{20} \mathrm{e}^{-}+\mathrm{Ca}^{2+}(\mathrm{Ni} @$
$\left.\mathrm{Pb}_{12}\right)^{2-} \mathrm{Ca}^{2+}+2 \mathrm{e}^{-},{ }^{21} \mathrm{Mg}\left(\mathrm{NH}_{3}\right)_{6} \mathrm{Na}_{2},{ }^{22} \mathrm{Be}_{6} \mathrm{Li}_{8}{ }^{23} \mathrm{Na}-$ $(\mathrm{HCN})_{3} \mathrm{Na},{ }^{24} \mathrm{~K}-\mathrm{F}_{6} \mathrm{C}_{6} \mathrm{H}_{6},{ }^{25} \mathrm{Na}(\mathrm{HF}){ }_{3} \mathrm{Na},{ }^{26} \mathrm{Li}_{2} @$ @helical, ${ }^{28}$ $\operatorname{Ir}\left(\mathrm{F}_{2} \mathrm{PPY}\right)_{2} \mathrm{ADC},{ }^{29}$ and $\mathrm{K}(1)^{+} \cdots$ calix $[4]$ pyrrole $\cdots \mathrm{K}(2)^{+} \ldots$ $2 \mathrm{e}^{-49}$ are $2.25 \times 10^{3}, 6.42 \times 10^{4}, 2.2 \times 10^{6}, 5.95 \times 10^{6}, 5.4$ $\times 10^{4}, 1.09 \times 10^{4}, 4.67 \times 10^{5}, 4.23 \times 10^{4}, 7.73 \times 10^{6}, 1.61 \times$ $10^{4}$, and $3.15 \times 10^{6} \mathrm{au}^{48}$ respectively. Therefore, the $\beta_{0}{ }^{e}$ value of the on-form of $\mathrm{Rb}_{3} \mathrm{BeB}_{6} \mathrm{Be}^{\prime} \mathrm{Rb}_{3}{ }_{3}$ is much larger than most of the reported OEEF-induced NLO molecular switches.

To study which excitation path is primarily contributed to $\beta_{0}{ }^{\mathrm{e}}$, for $\mathrm{Rb}_{3} \mathrm{BeB}_{6} \mathrm{Be}^{\prime} \mathrm{Rb}^{\prime}{ }_{3}$, it can be estimated by using the following simplified sum-overstate (SOS) formula: ${ }^{51}$

$$
\begin{equation*}
\beta_{0}^{\mathrm{e}} \propto\left(\Delta \mu \cdot f_{0}\right) / \Delta E^{3} \tag{9}
\end{equation*}
$$

For this formula, $\Delta E, f_{0}$, and $\Delta \mu$ denote the electronic transition energy, oscillator strength, and the difference of transition dipole moment between the ground state and the crucial excited state, respectively. In this case, the most

Table 3. Dipole Moment $\left(\mu_{0}\right), \beta_{0}$ and Its Values by Sum-Overstate Calculation ( $\beta_{0}{ }^{\text {SOS }}$ ), Difference of Dipole Moment between Ground State and Crucial Excited State $(\Delta \mu)$, Oscillator Strength $f_{0}$, and Transition Energy $(\Delta E)$ of the Crucial Excited State for $\left[\mathrm{Rb}_{3} \mathrm{Be}\right]^{3+}\left[\mathrm{B}_{6}\right]^{6-}\left[\mathrm{Be}^{\prime} \mathrm{Rb}_{3}{ }_{3}\right]^{3+}(1)$ and $\left[\mathrm{Rb}_{3} \mathrm{Be}\right]^{2+}\left[\mathrm{B}_{6}\right]^{6-}\left[\mathrm{Be}^{\prime} \mathrm{Rb}_{3}^{\prime}\right]^{4+}(2)$ at the PBE0/def2-qzvp Level

|  | $\mu_{0}$ (D) | $\mu_{z}(\mathrm{D})$ | $\beta_{0}{ }^{\text {e }}$ (au) | $\beta_{z z z}{ }^{\text {e }}$ (au) | $\beta_{0}{ }^{\text {SOS }}(\mathrm{au})$ | $\Delta \mu_{\mathrm{z}}(\mathrm{au})$ | $\Delta E(\mathrm{eV})$ | $f_{0}$ | $\lambda(\mathrm{nm})$ |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| 1 | 0.00 | 0.00 | 0.00 | 0.00 | 0.00 | 0.00 | 0.840 | 0.401 | 1477 |
|  |  |  |  |  |  | 0.00 | 1.041 | 0.326 | 1191 |
|  |  |  |  |  |  | 0.00 | 1.495 | 0.297 | 829 |
|  |  |  |  |  |  | 0.00 | 1.518 | 0.679 | 817 |
|  |  |  |  |  |  | 0.00 | 2.519 | 0.172 | 492 |
|  |  |  |  |  |  | 0.00 | 3.075 | 0.146 | 403 |
|  |  |  |  |  |  | 0.00 | 3.095 | 0.179 | 400 |
| 2 | 3.36 | $-3.36$ | $2.18 \times 10^{5}$ | $3.52 \times 10^{5}$ | $2.90 \times 10^{5}$ | 2.43 | 0.783 | 0.340 | 1584 |
|  |  |  |  |  |  | -3.59 | 1.001 | 0.278 | 1238 |
|  |  |  |  |  |  | 5.24 | 1.421 | 0.217 | 872 |
|  |  |  |  |  |  | 2.56 | 1.469 | 0.704 | 844 |
|  |  |  |  |  |  | 1.10 | 2.229 | 0.100 | 555 |
|  |  |  |  |  |  | 1.18 | 3.09 | 0.192 | 400 |



Figure 5. Electronic absorption spectrum of $\left[\mathrm{Rb}_{3} \mathrm{Be}\right]^{3+}\left[\mathrm{B}_{6}\right]^{6-}\left[\mathrm{Be}^{\prime} \mathrm{Rb}_{3}{ }_{3}\right]^{3+}(n=0)$.
important factor is the excitation energy because $\beta_{0}{ }^{e}$ is proportional to the inversion of its cube.

The results in Figures 5 and 6 show that the intense absorption bands of both $\left[\mathrm{Rb}_{3} \mathrm{Be}\right]^{3+}\left[\mathrm{B}_{6}\right]^{6-}\left[\mathrm{Be}^{\prime} \mathrm{Rb}^{\prime}{ }_{3}\right]^{3+}$ ( $\mathrm{Rb} \mathrm{b}_{3} \mathrm{BeB} \mathrm{B}_{6} \mathrm{Be}^{\prime} \mathrm{Rb}^{\prime}{ }_{3}(0)$, off-form) and $\left[\mathrm{Rb}_{3} \mathrm{Be}\right]^{2+}\left[\mathrm{B}_{6}\right]^{6-}\left[\mathrm{Be}^{\prime} \mathrm{Rb}_{3}{ }_{3}\right]^{4+}\left(\mathrm{Rb}_{3} \mathrm{BeB}_{6} \mathrm{Be}^{\prime} \mathrm{Rb}_{3}{ }_{3}(50)\right.$, on-form $)$ come from many absorption peaks. Then, $\beta_{0}{ }^{e}$ involves a contribution of many excited states. Table 3 shows that the $\Delta \mu_{\mathrm{z}}$ value is zero for $\left[\mathrm{Rb}_{3} \mathrm{Be}\right]^{3+}\left[\mathrm{B}_{6}\right]^{6-}\left[\mathrm{Be}^{\prime} \mathrm{Rb}_{3}{ }_{3}\right]^{3+}$ with the $D_{3 d}$ point group while that are not zero for $\left[\mathrm{Rb}_{3} \mathrm{Be}\right]^{2+}\left[\mathrm{B}_{6}\right]^{6-}\left[\mathrm{Be}^{\prime} \mathrm{Rb}_{3}{ }_{3}\right]^{4+}$ with $C_{3 v}$ one. Owing the zero of $\Delta \mu_{z}$, the $\beta_{0}{ }^{\text {SOS }}$ is zero for $\left[\mathrm{Rb}_{3} \mathrm{Be}\right]^{3+}\left[\mathrm{B}_{6}\right]^{6-}\left[\mathrm{Be}^{\prime} \mathrm{Rb}_{3}{ }_{3}\right]^{3+}$. In addition, from Figure 5, the wavelengths of these absorption peaks in the intense absorption band have an obvious blue shift from $\quad\left[\mathrm{Rb}_{3} \mathrm{Be}\right]^{3+}\left[\mathrm{B}_{6}\right]^{6-}\left[\mathrm{Be}^{\prime} \mathrm{Rb}^{\prime}{ }_{3}\right]^{3+} \mathrm{to}$ $\left[\mathrm{Rb}_{3} \mathrm{Be}\right]^{2+}\left[\mathrm{B}_{6}\right]^{6-}\left[\mathrm{Be}^{\prime} \mathrm{Rb}^{\prime}{ }_{3}\right]^{4+}$. For example, the maximum absorption peak ( $\lambda_{\max }$ ) in intense absorption band occurs at 817 nm for $\left[\mathrm{Rb}_{3} \mathrm{Be}\right]^{3+}\left[\mathrm{B}_{6}\right]^{6-}\left[\mathrm{Be}^{\prime} \mathrm{Rb}_{3}\right]^{3+}$ while that broad shifts
to 844 nm for $\left[\mathrm{Rb}_{3} \mathrm{Be}\right]^{2+}\left[\mathrm{B}_{6}\right]^{6-}\left[\mathrm{Be}^{\prime} \mathrm{Rb}^{\prime}{ }_{3}\right]^{4+}$. Considering these blue shifts, the $\Delta E$ value of each maximum absorption peak is smaller for $\left[\mathrm{Rb}_{3} \mathrm{Be}\right]^{2+}\left[\mathrm{B}_{6}\right]^{6-}\left[\mathrm{Be}^{\prime} \mathrm{Rb}^{\prime}{ }_{3}\right]^{4+}$ than that for $\left[\mathrm{Rb}_{3} \mathrm{Be}\right]^{3+}\left[\mathrm{B}_{6}\right]^{6-}\left[\mathrm{Be}^{\prime} \mathrm{Rb}_{3}{ }_{3}\right]^{3+}$.

By analyzing the vibrational first hyperpolarizability tensors $\left(\beta_{z z z}{ }^{\mathrm{nr}}\right)$ of a series of excess electron compounds, Luis and coworkers have shown that the impact of vibrational hyperpolarizability is also vitally important. ${ }^{46}$ Then, the $\beta_{z z z}{ }^{\text {nr }}$ values of both $\left[\mathrm{Rb}_{3} \mathrm{Be}\right]^{3+}\left[\mathrm{B}_{6}\right]^{6-}\left[\mathrm{Be}^{\prime} \mathrm{Rb}^{\prime}{ }_{3}\right]^{3+}$ and $\left[\mathrm{Rb}_{3} \mathrm{Be}\right]^{2+}\left[\mathrm{B}_{6}\right]^{6-}\left[\mathrm{Be}^{\prime} \mathrm{Rb}_{3}{ }_{3}\right]^{4+}$ were also calculated. Because the calculation of the harmonic Raman frequency is necessary to obtain the $\beta_{z z z}{ }^{\mathrm{nr}}$ value, the $\beta_{z z z}{ }^{\mathrm{nr}}$ values were obtained at the PBE0/def2-qzvp level. For the purpose of comparison, we also calculated $\beta_{z z z}{ }^{\mathrm{e}}$ at the same level. From Table 4, it is shown that $\left[\mathrm{Rb}_{3} \mathrm{Be}\right]^{2+}\left[\mathrm{B}_{6}\right]^{6-}\left[\mathrm{Be}^{\prime} \mathrm{Rb}_{3}{ }_{3}\right]^{4+}$ holds a very small ratio $\eta\left(\beta_{z z z}{ }^{\mathrm{nr}} /\right.$ $\beta_{z z z}{ }^{\mathrm{e}}$ ), which suggests that the electronic contribution plays an important role and the vibrational contribution plays a secondary role only for the NLO response of


Figure 6. Electronic absorption spectrum of $\left[\mathrm{Rb}_{3} \mathrm{Be}\right]^{2+}\left[\mathrm{B}_{6}\right]^{6-}\left[\mathrm{Be}^{\prime} \mathrm{Rb}_{3}^{\prime}\right]^{4+}(n=50)$.

Table 4. Electronic First Hyperpolarizability Tensor $\boldsymbol{\beta}_{z z z}{ }^{\mathrm{e}}$, Vibrational First Hyperpolarizability Tensor $\boldsymbol{\beta}_{\text {zzz }} \mathrm{nr}$, and Ratio $\boldsymbol{\eta}$ of $\boldsymbol{\beta}_{z z z}{ }^{\mathrm{nr}} / \boldsymbol{\beta}_{z z z}{ }^{\mathrm{e}}$ for $\left[\mathrm{Rb}_{3} \mathrm{Be}\right]^{3+}\left[\mathrm{B}_{6}\right]^{6-}\left[\mathrm{Be}^{\prime} \mathrm{Rb}_{3}^{\prime}\right]^{3+}$ and $\left[\mathrm{Rb}_{3} \mathrm{Be}\right]^{2+}\left[\mathrm{B}_{6}\right]^{6-}\left[\mathrm{Be}^{\prime} \mathrm{Rb}_{3}{ }_{3}\right]^{4+}$ at the PBE0/def2-qzvp Level

|  | $\left[\mathrm{Rb}_{3} \mathrm{Be}\right]^{3+}\left[\mathrm{B}_{6}\right]^{6-}\left[\mathrm{Be}^{\prime} \mathrm{Rb}_{3}^{\prime}\right]^{3+}$ | $\left[\mathrm{Rb}_{3} \mathrm{Be}\right]^{2+}\left[\mathrm{B}_{6}\right]^{6-}\left[\mathrm{Be}^{\prime} \mathrm{Rb}_{3}^{\prime}\right]^{4+}$ |
| :--- | :--- | :--- |
| $\beta_{z z z}{ }^{\mathrm{e}}$ | 0.000 | $6.71 \times 10^{4}$ |
| $\beta_{\text {nzz }}$ | 0.000 | $8.01 \times 10^{3}$ |
| $\eta$ | 0 | 0.12 |

$\left[\mathrm{Rb}_{3} \mathrm{Be}\right]^{2+}\left[\mathrm{B}_{6}\right]^{6-}\left[\mathrm{Be}^{\prime} \mathrm{Rb}^{\prime}{ }_{3}\right]^{4+}$. For $D_{3 \mathrm{~d}}$ $\left[\mathrm{Rb}_{3} \mathrm{Be}\right]^{3+}\left[\mathrm{B}_{6}\right]^{6-}\left[\mathrm{Be}^{\prime} \mathrm{Rb}_{3}^{\prime}\right]^{3+}$, it is zero for both $\beta_{z z z}{ }^{\mathrm{e}}$ and $\beta_{z z z}{ }^{\mathrm{nr}}$. So, there is a high-performance NLO switchable effect between $\left[\mathrm{Rb}_{3} \mathrm{Be}\right]^{2+}\left[\mathrm{B}_{6}\right]^{6-}\left[\mathrm{Be}^{\prime} \mathrm{Rb}_{3}{ }_{3}\right]^{4+}$ and $\left[\mathrm{Rb}_{3} \mathrm{Be}\right]^{3+}\left[\mathrm{B}_{6}\right]^{6-}\left[\mathrm{Be}^{\prime} \mathrm{Rb}_{3}{ }_{3}\right]^{3+}$ for both electronic and vibrational contributions.
Many experimental NLO investigations were performed by using the Z-scan method with laser pulses at wavelengths of 1064, 1340, 1560, and 1907 nm . Then, a frequency-dependent hyperpolarizability analysis has been carried out to the frequency-dependent fields ( $\lambda=\propto, 1064,1340,1560$, and 1907 nm ). Table 5 lists the TD-M06-2X and estimated MP2
$\beta_{0}(-2 \omega, \omega, \omega), \beta_{z z z}(-2 \omega, \omega, \omega)$, and $\beta_{y y y}(-2 \omega, \omega, \omega)$ values. The data in Table 5 show that it is pronounced for the differences between MP2 and the corresponding TD-M06-2X values for $\beta_{0}(-2 \omega, \omega, \omega)$ of $\left[\mathrm{Rb}_{3} \mathrm{Be}\right]^{2+}\left[\mathrm{B}_{6}\right]^{6-}\left[\mathrm{Be}^{\prime} \mathrm{Rb}_{3}{ }_{3}\right]^{4+}$. Then, the TD-M06-2X values are used for the next discussion.

Owning to the $D_{3 d}$ point group, the frequency-dependent hyperpolarizability is zero for $\left[\mathrm{Rb}_{3} \mathrm{Be}\right]^{3+}\left[\mathrm{B}_{6}\right]^{6-}\left[\mathrm{Be}^{\prime} \mathrm{Rb}_{3}{ }_{3}\right]^{3+}{ }_{0}$. The $\beta_{0}(-2 \omega, \omega, \omega)$ values range from $1.42 \times 10^{5}$ to $3.15 \times 10^{8}$ au at above wavelengths. So, the frequency-dependent hyperpolarizability of $\mathrm{Rb}_{3} \mathrm{BeB}_{6} \mathrm{Be}^{\prime} \mathrm{Rb}_{3}$ also exhibits wellperformance NLO switching effect from $\left[\mathrm{Rb}_{3} \mathrm{Be}\right]^{3+}\left[\mathrm{B}_{6}\right]^{6-}\left[\mathrm{Be}^{\prime} \mathrm{Rb}^{\prime}{ }_{3}\right]^{3+}$ (off form) to $\left[\mathrm{Rb}_{3} \mathrm{Be}\right]^{3+}\left[\mathrm{B}_{6}\right]^{6-}\left[\mathrm{Be}^{\prime} \mathrm{Rb}_{3}\right]^{4+}$ (on form). It should be stressed that the contribution to $\mathrm{BeB}_{6} \mathrm{Be}^{\prime} \mathrm{Rb}^{\prime}{ }_{3}$ exhibits a good performance NLO switching effect from $\left[\mathrm{Rb}_{3} \mathrm{Be}\right]^{3+}\left[\mathrm{B}_{6}\right]^{6-}\left[\mathrm{Be}^{\prime} \mathrm{Rb}^{\prime}\right]^{3+}$ (off form) to $\left[\mathrm{Rb}_{3} \mathrm{Be}\right]^{3+}\left[\mathrm{B}_{6}\right]^{6-}\left[\mathrm{Be}^{\prime} \mathrm{Rb}_{3}\right]^{4+}$ (on-form). It should be stressed that the contribution to $\beta_{0}(-2 \omega, \omega, \omega)$ is significantly different between $\beta_{z z z}(-2 \omega, \omega, \omega)$ and $\beta_{y y y}(-2 \omega, \omega, \omega)$ among different wavelengths of laser pulses. It is $\beta_{z z z}(-2 \omega, \omega, \omega)$ at $\lambda=\alpha$ and 1906 nm , but it is $\beta_{\mathrm{yyy}}(-2 \omega, \omega, \omega)$ at $\lambda=1460,1340$, and 1064

Table 5. TD-M06-2X and Estimated MP2 Values of Frequency-Dependent Hyperpolarizabilities $\left(\beta_{0}(-2 \omega, \omega, \omega)\right.$, $\boldsymbol{\beta}_{\text {zzz }}(-2 \omega, \omega, \omega)$, and $\beta_{y y y}(-2 \omega, \omega, \omega)$, in au) for $\left[R b_{3} B e\right]^{3+}\left[B_{6}\right]^{6-}\left[\mathrm{Be}^{\prime} \mathbf{R b}_{3}^{\prime}\right]^{3+}(1)$ and $\left[R b_{3} B e^{2+}\left[B_{6}\right]^{6-}\left[\mathrm{Be}^{\prime} \mathbf{R b}^{\prime}{ }_{3}\right]^{4+}(2)\right.$

| $\lambda(\mathrm{nm})$ |  |  |  |  |
| :---: | :---: | :---: | :---: | :---: |
| $\alpha$ | 1906 | 1460 | 1340 | 1064 |
| $\beta_{0}(-2 \omega, \omega, \omega)^{a}$ |  |  |  |  |
| 10 (0) | 0 (0) | 0 (0) | 0 (0) | 0 (0) |
| $21.42 \times 10^{5}\left(2.18 \times 10^{5}\right)$ | $1.78 \times 10^{5}\left(2.73 \times 10^{5}\right)$ | $4.87 \times 10^{6}\left(7.48 \times 10^{6}\right)$ | $3.15 \times 10^{8}\left(4.83 \times 10^{8}\right)$ | $9.67 \times 10^{5}\left(1.49 \times 10^{6}\right)$ |
| $\beta_{z z z}(-2 \omega, \omega, \omega)^{a}$ |  |  |  |  |
| 10 (0) | 0 (0) | 0 (0) | 0 (0) | 0 (0) |
| $21.61 \times 10^{5}\left(3.52 \times 10^{5}\right)$ | $1.13 \times 10^{6}\left(2.48 \times 10^{6}\right)$ | $-3.45 \times 10^{5}\left(-7.53 \times 10^{5}\right)$ | $-1.32 \times 10^{5}\left(-2.89 \times 10^{5}\right)$ | $1.71 \times 10^{4}\left(3.73 \times 10^{4}\right)$ |
| $\beta_{y y y}(-2 \omega, \omega, \omega)^{a}$ |  |  |  |  |
| 10 (0) | 0 (0) | 0 (0) | 0 (0) | 0 (0) |
| $2 \quad 5.04 \times 10^{4}\left(6.93 \times 10^{3}\right)$ | $3.32 \times 10^{5}\left(4.59 \times 10^{4}\right)$ | $3.32 \times 10^{6}\left(4.58 \times 10^{5}\right)$ | $-3.92 \times 10^{7}\left(-5.41 \times 10^{6}\right)$ | $1.13 \times 10^{6}\left(1.56 \times 10^{5}\right)$ |

[^1]nm, which provides the larger contribution to the $\beta_{0}(-2 \omega, \omega, \omega)$ value.

## - CONCLUSIONS

In summary, we have presented the results of a novel IMSR NLO switch, a boron-based sandwich-like complex $\mathrm{Rb}_{3} \mathrm{BeB}_{6} \mathrm{Be}^{\prime} \mathrm{Rb}_{3}{ }_{3}$. An OEEF of $F_{z} \geq 50 \times 10^{-4}$ au can drive an excess electron to transfer from tetrahedral $\mathrm{Be}^{\prime} \mathrm{Rb}_{3}{ }_{3}$ to $\mathrm{Rb}_{3} \mathrm{Be}$, and subsequently, the self-redox reaction occurs, and $\left[\mathrm{Rb}_{3} \mathrm{Be}\right]^{3+}\left[\mathrm{B}_{6}\right]^{6-}\left[\mathrm{Be}^{\prime} \mathrm{Rb}^{\prime}{ }_{3}\right]^{3+}\left(D_{3 d}\right)$ changes to $\left[\mathrm{Rb}_{3} \mathrm{Be}\right]^{2+}\left[\mathrm{B}_{6}\right]^{6-}\left[\mathrm{Be}^{\prime} \mathrm{Rb}^{\prime}{ }_{3}\right]^{4+}\left(\mathrm{C}_{3 v}\right)$.
$\left[\mathrm{Rb}_{3} \mathrm{Be}\right]^{3+}\left[\mathrm{B}_{6}\right]^{6-}\left[\mathrm{Be}^{\prime} \mathrm{Rb}_{3}^{\prime}\right]^{3+}$ (off-form) has zero $\mu_{0}$ and $\beta_{0}{ }^{\mathrm{e}}$ due to the $D_{3 d}$ symmetry. However, $C_{3 v}$ $\left[\mathrm{Rb}_{3} \mathrm{Be}\right]^{2+}\left[\mathrm{B}_{6}\right]^{6-}\left[\mathrm{Be}^{\prime} \mathrm{Rb}_{3}\right]^{4+}$ (on-form) exhibits high-performance NLO responses. The latter has an $\mu_{0}$ of 3.36 D and a $\beta_{0}{ }^{\text {e }}$ of $2.18 \times 10^{5} \mathrm{au}$. Both electronic and vibrational contributions exhibit good performance NLO switching effects from $[\mathrm{Rb} 3 \mathrm{Be}] 3+[\mathrm{B} 6] 6-\left[\mathrm{Be}^{\prime} \mathrm{Rb}^{\prime} 3\right] 3+$ (off form) to $[\mathrm{Rb} 3 \mathrm{Be}]-$ $3+[\mathrm{B} 6] 6-\left[\mathrm{Be}^{\prime} \mathrm{Rb}^{\prime} 3\right] 4+$ (on-form). The difference in the dynamic first hyperpolarizabilities between $\left[\mathrm{Rb}_{3} \mathrm{Be}\right]^{3+}\left[\mathrm{B}_{6}\right]^{6-}\left[\mathrm{Be}^{\prime} \mathrm{Rb}_{3}^{\prime}\right]^{3+}$ and $\left[\mathrm{Rb}_{3} \mathrm{Be}\right]^{2+}\left[\mathrm{B}_{6}\right]^{6-}\left[\mathrm{Be}^{\prime} \mathrm{Rb}^{\prime}{ }_{3}\right]^{4+}$ is also pronounced. Therefore, $\mathrm{Rb}_{3} \mathrm{BeB}_{6} \mathrm{Be}^{\prime} \mathrm{Rb}^{\prime}{ }_{3}$ may be a highperformance candidate for an IMSR NLO molecular switch because there exists significant contrast in NLO property between $\left[\mathrm{Rb}_{3} \mathrm{Be}\right]^{3+}\left[\mathrm{B}_{6}\right]^{6-}\left[\mathrm{Be}^{\prime} \mathrm{Rb}^{\prime}{ }_{3}\right]^{3+}$ and $\left[\mathrm{Rb}_{3} \mathrm{Be}\right]^{2+}\left[\mathrm{B}_{6}\right]^{6-}\left[\mathrm{Be}^{\prime} \mathrm{Rb}_{3}^{\prime}\right]^{4+}$ and the OEEF of $F_{\mathrm{z}} \geq 50 \times$ $10^{-4}$ au can trigger from the former to change into the later.

## - ASSOCIATED CONTENT

## (s) Supporting Information

The Supporting Information is available free of charge at https://pubs.acs.org/doi/10.1021/acsomega.3c04248.

Data of optimized geometries, stability analysis, and the first hyperpolarizabilities (PDF)

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## Notes

The authors declare no competing financial interest.

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[^1]:    ${ }^{a}$ The MP2 values are within parentheses.

