

# Mitochondrial-Mediated Oxidative $\text{Ca}^{2+}$ /Calmodulin-Dependent Kinase II Activation Induces Early Afterdepolarizations in Guinea Pig Cardiomyocytes: An In Silico Study

Ruilin Yang, MS; Patrick Ernst, BS; Jiajia Song, PhD; Xiaoguang M. Liu, PhD; Sabine Huke, PhD; Shuxin Wang, PhD; Jianyi Jay Zhang, MD, PhD; Lufang Zhou, PhD

**Background**—Oxidative stress-mediated  $\text{Ca}^{2+}$ /calmodulin-dependent protein kinase II (CaMKII) phosphorylation of cardiac ion channels has emerged as a critical contributor to arrhythmogenesis in cardiac pathology. However, the link between mitochondrial-derived reactive oxygen species (mdROS) and increased CaMKII activity in the context of cardiac arrhythmias has not been fully elucidated and is difficult to establish experimentally.

**Methods and Results**—We hypothesize that pathological mdROS can cause erratic action potentials through the oxidation-dependent CaMKII activation pathway. We further propose that CaMKII-dependent phosphorylation of sarcolemmal slow  $\text{Na}^+$  channels alone is sufficient to elicit early afterdepolarizations. To test the hypotheses, we expanded our well-established guinea pig cardiomyocyte excitation-contraction coupling, mitochondrial energetics, and ROS-induced-ROS-release model by incorporating oxidative CaMKII activation and CaMKII-dependent  $\text{Na}^+$  channel phosphorylation in silico. Simulations show that mdROS mediated-CaMKII activation elicits early afterdepolarizations by augmenting the late  $\text{Na}^+$  currents, which can be suppressed by blocking L-type  $\text{Ca}^{2+}$  channels or  $\text{Na}^+/\text{Ca}^{2+}$  exchangers. Interestingly, we found that oxidative CaMKII activation-induced early afterdepolarizations are sustained even after mdROS has returned to its physiological levels. Moreover, mitochondrial-targeting antioxidant treatment can suppress the early afterdepolarizations, but only if given in an appropriate time window. Incorporating concurrent mdROS-induced ryanodine receptors activation further exacerbates the proarrhythmic effect of oxidative CaMKII activation.

**Conclusions**—We conclude that oxidative CaMKII activation-dependent Na channel phosphorylation is a critical pathway in mitochondria-mediated cardiac arrhythmogenesis. (*J Am Heart Assoc.* 2018;7:e008939. DOI: 10.1161/JAHA.118.008939.)

**Key Words:** arrhythmias • computational modeling • mitochondrial dysfunction • oxidative CaMKII activation

Cardiovascular disease is a major health problem in the United States and its incidence increases steadily as the general population ages.<sup>1</sup> Despite advances in diagnosis and treatment, cardiovascular disease mortality remains high, accounting for nearly 500 000 American deaths each year.<sup>1</sup> About one half of cardiovascular disease-related deaths occur suddenly because of sudden cardiac death resulting from ventricular arrhythmias.<sup>2,3</sup> Although the incidence rate is high, the precise molecular mechanisms underlying cardiac

arrhythmogenesis are not fully understood, hindering the development of effective therapeutic strategies.

Recently, loss of mitochondrial function, which is often observed in many disease processes such as heart failure, ischemic cardiomyopathy, hypertrophic cardiomyopathy, and metabolic diseases, has emerged as a key contributor to the arrhythmogenic substrate. While the detailed mechanistic pathways remain incompletely understood, work from our laboratory and others<sup>4-7</sup> suggest that the proarrhythmic

From Key Laboratory for Mechanism Theory and Equipment Design of Ministry of Education, Tianjin University, Tianjin, China (R.Y., S.W.); Departments of Medicine (R.Y., J.S., S.H., L.Z.) and Biomedical Engineering (P.E., X.M.L., J.J.Z., L.Z.), University of Alabama at Birmingham, AL.

Accompanying Tables S1 through S28 and Figures S1 through S4 are available at <http://jaha.ahajournals.org/content/7/15/e008939/DC1/embed/inline-supplementary-material-1.pdf>

**Correspondence to:** Lufang Zhou, PhD, Division of Cardiovascular Disease, University of Alabama School of Medicine, 703 19th Street South, ZRB 306, Birmingham, AL 35294. Email: lfzhou@uab.edu

Received February 26, 2018; accepted June 7, 2018.

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## Clinical Perspective

### What Is New?

- We developed a multiscale computational model linking cardiomyocyte mitochondrial energetics to  $\text{Ca}^{2+}$ /calmodulin-dependent protein kinase II activity and  $\text{Ca}^{2+}$  handling.
- Mitochondrial-mediated oxidative  $\text{Ca}^{2+}$ /calmodulin-dependent protein kinase II activation is sufficient to elicit early afterdepolarizations solely through enhanced late  $\text{Na}^+$  current.
- Oxidative  $\text{Ca}^{2+}$ /calmodulin-dependent protein kinase II activation-elicited early afterdepolarizations are sustained even after mitochondrial-derived reactive oxygen species has returned to its physiological levels.

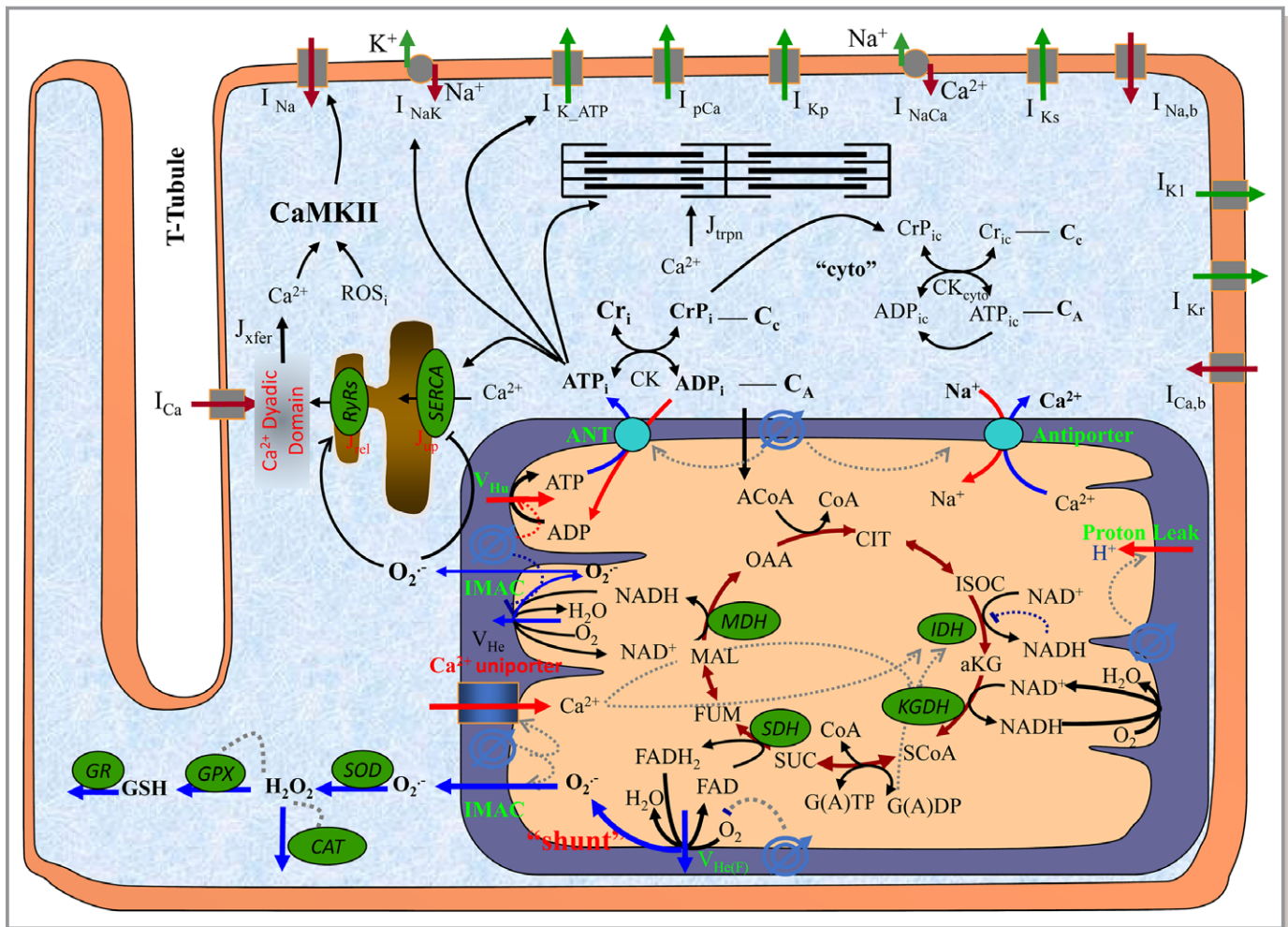
### What Are the Clinical Implications?

- It is critically important to consider mitochondria when designing novel antiarrhythmic therapies.
- It appears that there is a treatment window for antioxidants to suppress  $\text{Ca}^{2+}$ /calmodulin-dependent protein kinase II-mediated pathological effects.

effect of mitochondria dysfunction is at least partially attributed to the organellar-derived reactive oxygen species (ROS), which can influence multiple redox-sensitive ion channels/transporters underlying  $\text{Ca}^{2+}$  handling such as ryanodine receptors (RyRs)<sup>6–9</sup> and sarcoplasmic reticulum (SR)  $\text{Ca}^{2+}$  ATPase (SERCA).<sup>10,11</sup> Beside  $\text{Ca}^{2+}$  handling proteins, excessive ROS can also affect sarcolemmal voltage-gated  $\text{Na}^+$  channels,<sup>12,13</sup>  $\text{K}^+$  channels,  $\text{Na}^+/\text{Ca}^{2+}$  exchanger, and L-type  $\text{Ca}^{2+}$  channels (LCCs).<sup>11,14–18</sup> In addition to direct modulation of redox-sensitive ion channels, mitochondrial-derived ROS (mdROS) may indirectly influence  $\text{Ca}^{2+}$  handling and action potentials (APs) via redox signaling pathways such as oxidation-mediated  $\text{Ca}^{2+}$ /calmodulin-dependent kinase II (CaMKII) phosphorylation. CaMKII is a multifunctional protein kinase ubiquitously expressed in cardiomyocytes and is activated by binding to  $\text{Ca}^{2+}$ /CaM and subsequent autophosphorylation.<sup>19,20</sup> A growing body of evidence has demonstrated that CaMKII can also be activated by ROS.<sup>21–24</sup> Once activated, CaMKII can phosphorylate a wide range of key  $\text{Ca}^{2+}$  and  $\text{Na}^+$  regulatory proteins such as LCCs,<sup>25–28</sup> RyRs,<sup>29–35</sup> phospholamban,<sup>29,34,36</sup> and  $\text{Na}^+$  channels.<sup>37,38</sup> Importantly, Xie et al<sup>39</sup> showed that  $\text{H}_2\text{O}_2$  perfusion-induced oxidative CaMKII activation leads to afterdepolarizations in isolated rabbit cardiomyocytes, likely by phosphorylation of  $\text{Na}^+$  channels and LCCs. Given those advances, the detailed mechanistic pathways by which oxidation-dependent CaMKII activation creates a proarrhythmia substrate in diseased hearts remain unclear, partially because of the multidirectional interaction loops between CaMKII activation and ion

handling. As a powerful tool complementary to experimental measurement, computational modeling has been applied to elucidate how CaMKII activation may influence cardiac ion handling and electrophysiology. For instance, Onal et al<sup>40</sup> explored the CaMKII-dependent regulation of late  $\text{Na}^+$  current ( $I_{\text{Na,L}}$ ),  $\text{Ca}^{2+}$  homeostasis, and cellular excitability in atrial myocytes using a computer model. In another computational study, Dai et al<sup>41</sup> showed that CaMKII overexpression facilitates early afterdepolarization (EAD) by prolonging the deactivation of the  $I_{\text{Na,L}}$ , and combination with  $\beta$ -adrenergic activation further increases EAD risk. Modeling studies also suggested that CaMKII activation-mediated SR  $\text{Ca}^{2+}$  overload and increased cytosolic  $\text{Na}^+$  elicit post-acidosis arrhythmias in human myocytes.<sup>42</sup> To examine the role of oxidation-dependent CaMKII activation in regulating cardiac cell excitability following myocardial infarction, Christensen et al<sup>43</sup> developed a mathematical model of CaMKII activity, which, for the first time, includes both oxidative and autophosphorylation activation pathways. More recently, an integrative cardiomyocyte model has been developed by Foteinou et al<sup>44</sup> to study the mechanistic role of oxidized CaMKII in the genesis of  $\text{H}_2\text{O}_2$ -induced EADs in the heart. In a similar study, Zhang et al<sup>45</sup> developed a new Markov chain model of CaMKII  $\delta$ -isoform that involves both of the autophosphorylation and oxidation pathways to simulate CaMKII activation and its effect on APs under oxidative stress in cardiomyocytes.

Given the advances, how endogenous ROS, especially those derived from mitochondria (mdROS), affect CaMKII activity and consequently ion homeostasis and AP remains largely unexplored. Dissecting direct mdROS effects and indirect effects caused by CaMKII phosphorylation is difficult to address experimentally, as is defining the contribution of individual targets to arrhythmogenesis. As the voltage-gated  $\text{Na}^+$  currents ( $I_{\text{Na}}$ ) are a significant contributor to the initiation and duration of the cardiac AP and a well-recognized substrate of CaMKII phosphorylation, we hypothesize that mdROS-mediated oxidative CaMKII activation could elicit abnormal APs by enhancing  $I_{\text{Na}}$ . To test the hypothesis, we expanded our well-established cardiomyocyte excitation-contraction coupling, mitochondrial energetics, and ROS-induced-ROS-release (ECME-RIRR)<sup>5,46,47</sup> model by incorporating oxidative CaMKII activation and slow  $\text{Na}^+$  channel phosphorylation. Our simulations show that mdROS bursts-mediated oxidative CaMKII activation significantly augments  $I_{\text{Na,L}}$ , which alone is sufficient to cause EADs. Moreover, we show that under certain conditions the oxidative CaMKII activation-induced EADs persist even after mdROS have returned to physiological levels, an event that is likely attributed to CaMKII's property as a "memory molecule." Finally, model simulations suggest that timing is critical for antioxidant treatments to effectively eliminate mdROS-CaMKII activation-induced EADs.



**Figure 1.** Scheme of the expanded excitation-contraction coupling, mitochondrial energetics, and ROS-induced-ROS-release (RIRR) model that incorporates oxidative  $\text{Ca}^{2+}$ /calmodulin-dependent protein kinase II (CaMKII) activation. The electrophysiological module describes the major ion channels underlying the action potential (eg, fast  $\text{Na}^+$  channel and  $\text{Na}^+/\text{Ca}^{2+}$  exchanger) and processes involved in  $\text{Ca}^{2+}$  handling (eg, local  $\text{Ca}^{2+}$  control and transport of  $\text{Ca}^{2+}$  across the sarcoplasmic reticulum). The mitochondrial module accounts for major components of mitochondrial energetics such as tricarboxylic acid cycle and oxidative phosphorylation, as well as mitochondrial membrane ion channels (eg,  $\text{Ca}^{2+}$  uniporter). The RIRR module describes reactive oxygen species (ROS) production (from the electron transport chain), transport (through inner membrane anion channel [IMAC]), and scavenging (eg, by the superoxide dismutase and glutathione peroxidase enzymes).

## Methods

No human or animal subject was involved in this theoretical study. Thus, there was no institutional review board approval required. The data, analytic methods, and codes will be made available to other researchers for purposes of reproducing the results or replicating the procedure. Model equations and parameters are available within the article or Tables S1 through S28.

## Model Development

In this *in silico* study, we aimed to examine the effect of mitochondrial-derived oxidative stress on CaMKII activation to induce arrhythmias. The model was based on our recently published guinea pig cardiomyocyte ECME-RIRR model<sup>47</sup> and

incorporated several new model components including a CaMKII activity module, a Markov slow  $\text{Na}^+$  channel module, and an  $\text{Na}^+$  channel phosphorylation module. The scheme of the expanded ECME-RIRR model is shown in Figure 1, and the newly added model components are described below.

### CaMKII activity module

The CaMKII module model was built based on the Markov chain models constructed by Foteinou et al<sup>44</sup> and Zhang et al,<sup>45</sup> which comprises CaMKII activation by ROS and experimental data from Erickson et al.<sup>22</sup> For simplification, we assumed that  $\text{Ca}^{2+}$ /CaM-dependent activity, phosphorylation-dependent activity, and oxidation-dependent activity are homogeneous across the cell. With this assumption, the total activated CaMKII is defined as the sum of these activated



CaMKII (ie, binding  $\text{Ca}^{2+}$ /CaM, phosphorylated, and oxidized). The fraction of activated CaMKII can be calculated as:

$$\text{CaMKII}_{\text{active}} = \frac{[\text{CaMKII}_{\text{active}}]}{[\text{CaMKII}_{\text{total}}]} \times 100\% \quad (1)$$

where  $[\text{CaMKII}_{\text{active}}]$  is the concentration of total activated CaMKII and  $[\text{CaMKII}_{\text{total}}]$  is the concentration of total CaMKII. The complete CaMKII activation model is described in Figure S1 and Tables S4 and S25.

### The Markov slow $\text{Na}^+$ channel module

Experimental studies showed that the effect of CaMKII activation on  $\text{Na}^+$  channels is mainly on the slow component, ie, augmenting the  $I_{\text{Na,L}}$ . As our ECME-RIRR model consists only of the fast  $I_{\text{Na}}$  model, we adopted the Markov framework of the  $\text{Na}^+$  channel model developed by Grandi et al<sup>48</sup> to incorporate the  $I_{\text{Na,L}}$ :

$$I_{\text{Na,L}} = G_{\text{Na,L}} \cdot P_{\text{LO}} \cdot (V - E_{\text{Na}}) \quad (2)$$

where  $G_{\text{Na,L}}$  is the conductance of the late  $\text{Na}^+$  channels (mS/ $\mu\text{F}$ ) and  $P_{\text{LO}}$  is the open possibility of the late  $\text{Na}^+$  channels. The complete Markov slow  $\text{Na}^+$  channel model and parameters are listed in Tables S1 and S26, respectively.

### Slow $\text{Na}^+$ channel dynamic phosphorylation module

For modeling purposes, we contended that  $\text{Na}^+$  channels are either phosphorylated by activated CaMKII or not. The transition between the unphosphorylated and phosphorylated  $\text{Na}^+$  channels can be described by a 2-state Markov model (Figure S1). Specifically, the fraction of phosphorylated  $\text{Na}^+$  channels is governed by

$$\frac{d\phi_{\text{Na,CaMKII}}}{dt} = K_{\text{Phos}} \cdot (1 - \phi_{\text{Na,CaMKII}}) - K_{\text{DePhos}} \cdot \phi_{\text{Na,CaMKII}} \quad (3)$$

where  $\phi_{\text{Na,CaMKII}}$  is the fraction of phosphorylated  $\text{Na}^+$  channels,  $K_{\text{Phos}}$  is the phosphorylation rate, which is proportional to the fraction of activated CaMKII, and  $K_{\text{DePhos}}$  is a constant, which can be determined by the experimental data as described previously.<sup>48</sup> The total  $I_{\text{Na,L}}$   $I_{\text{Na,L}}^*$  is calculated by the following equations:

$$I_{\text{Na,L}}^* = (1 - \phi_{\text{Na,CaMKII}}) \cdot I_{\text{Na,L}} + \phi_{\text{Na,CaMKII}} \cdot I'_{\text{Na,L}} \quad (4)$$

$$I'_{\text{Na,L}} = G_{\text{Na,L}} \cdot P'_{\text{LO}} \cdot (V - E_{\text{Na}}) \quad (5)$$

In these equations,  $I'_{\text{Na,L}}$  represents the late  $\text{Na}^+$  current caused by CaMKII activation, and  $P'_{\text{LO}}$  is the open probability of phosphorylated late  $\text{Na}^+$  channels. The model parameters for the phosphorylated and unphosphorylated  $\text{Na}^+$  channels by activated CaMKII were refit with experimental data by Aiba et al<sup>49</sup> and are listed in Table S27.

## Simulation Protocol

The CaMKII activity and slow  $\text{Na}^+$  channel module models were integrated into the guinea pig ventricular myocytes ECME-RIRR model<sup>47</sup> after parameterization. To focus on the effect of mdROS-mediated oxidative CaMKII activation on AP and dissect the underlying ionic mechanisms, we did not consider the direct effect of mdROS on redox-sensitive ion handling proteins such as RyRs, SERCA, and  $\text{Na}^+$  channels in the present study unless otherwise specified. The formulas of other processes, such as ion channels and metabolic reactions, and model parameters were the same as those in the ECME-RIRR model<sup>47</sup> (Tables S1 through S28). The code of the new cell model was written in C<sup>++</sup> (Visual Studio, Microsoft). The nonlinear ordinary differential equations were integrated numerically with CVODE as previously described.<sup>5,50</sup>

The cardiomyocyte was stimulated at 0.25 Hz until the steady state was reached. The steady state values were then used as initial conditions for subsequent simulations. For model validation, we first simulated the effect of pacing cycle lengths (PCLs; 500, 1000, 2000, and 4000 ms) on AP duration (APD), then the ROS-induced  $I_{\text{Na,L}}$  augmentation, and finally EAD incidence rate dependence on PCL under oxidative stress. Model simulations were compared with experimental data from the literature. After model validation, we simulated the effect of mdROS on CaMKII activation,  $I_{\text{Na,L}}$ , cytosolic  $\text{Na}^+$  and  $\text{Ca}^{2+}$  handling, and AP under various conditions. The production of mdROS was modeled as a fraction, or *shunt*, of electrons from the electron transport chain into the matrix, as previously described.<sup>5,47,51,52</sup> Studies have shown that under physiological conditions, up to 2% of the electron flowing the respiratory chain are partially reduced to form the superoxide,<sup>53</sup> thus the physiological value of *shunt* was set as 2%. Pathological *shunt* was set as 10% or 14% to induce sustained mitochondrial oscillations, which is consistent with our previous computational studies.<sup>5,47,52</sup> The simulation results were postprocessed and plotted using Origin software (OriginLab).

## Results

### Model Validation

To validate the built guinea pig cardiomyocyte ECME-RIRR model that incorporates new model modules, we first simulated the effects of CaMKII phosphorylation and PCL on APD and compared the results with experimental data. Our simulations showed that increasing the PCL (from 500 to 4000 ms) caused stepwise APD elongation (Figure 2A, gray), which was further enhanced by CaMKII phosphorylation (data not shown). Those model predictions were comparable to experimental data reported by Aiba et al<sup>49</sup> (Figure 2A, black).



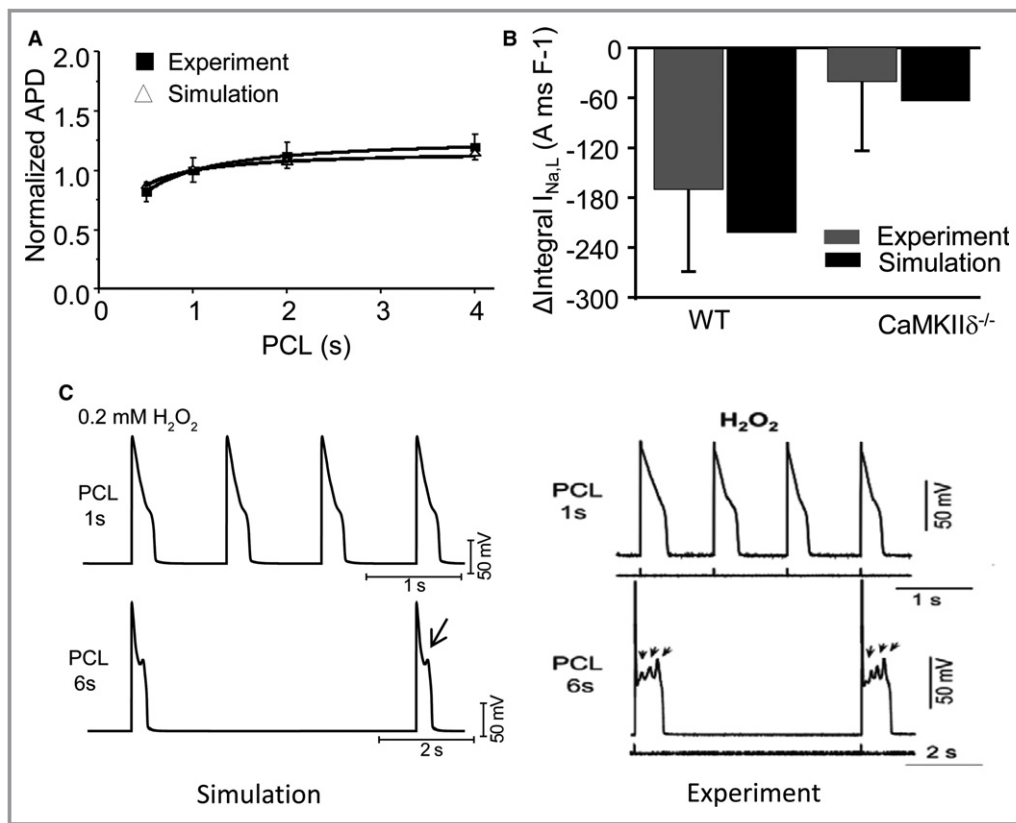
We then simulated the effect of oxidative stress on the voltage-gated  $I_{Na}$  (Figure 2B). In an experimental study, Wagner et al<sup>38</sup> showed that  $H_2O_2$  (200  $\mu$ mol/L) perfusion caused a remarkable increase ( $\approx 177$  A ms/F) in  $I_{Na,L}$  integral in wild-type mouse ventricular myocytes and this enhancement was substantially reduced in CaMKII knockout cardiomyocytes ( $\approx 48.7$  A ms/F). Our model simulations showed a similar trend: reducing CaMKII by 95% (estimated based on Western blot data in Backs et al<sup>54</sup>) notably reduced the oxidative stress–induced  $I_{Na,L}$  augmentation.

Finally, we examined the effect of ROS on APs at different PCLs. To be consistent with experimental studies by Xie et al<sup>39</sup> and Zhao et al,<sup>55</sup> the concentration of cytosolic ROS was set as 200  $\mu$ mol/L in this simulation. Our simulations showed that oxidative stress–induced EAD incidence rate is

PCL dependent: EADs could be induced readily when PCL was long (eg, 6 seconds) but hardly when PCL was relatively short (eg, 1 second) (Figure 2C). Those simulations were in agreement with previous experimental<sup>39,55</sup> (Figure 2D) and computational studies.<sup>44</sup>

### Effect of mdROS on CaMKII and Ion Handling During Mitochondrial Oscillations

After model validation, we simulated how mitochondrial-derived oxidative stress could influence CaMKII activity and ion handling in a “beating” guinea pig cardiomyocyte. As previously reported,<sup>5,46,47,52,56</sup> increasing *shunt*, the fraction of the electrons of the respiratory chain towards the generation of  $O_2^-$  from 0.02 to 0.10 triggered sustained



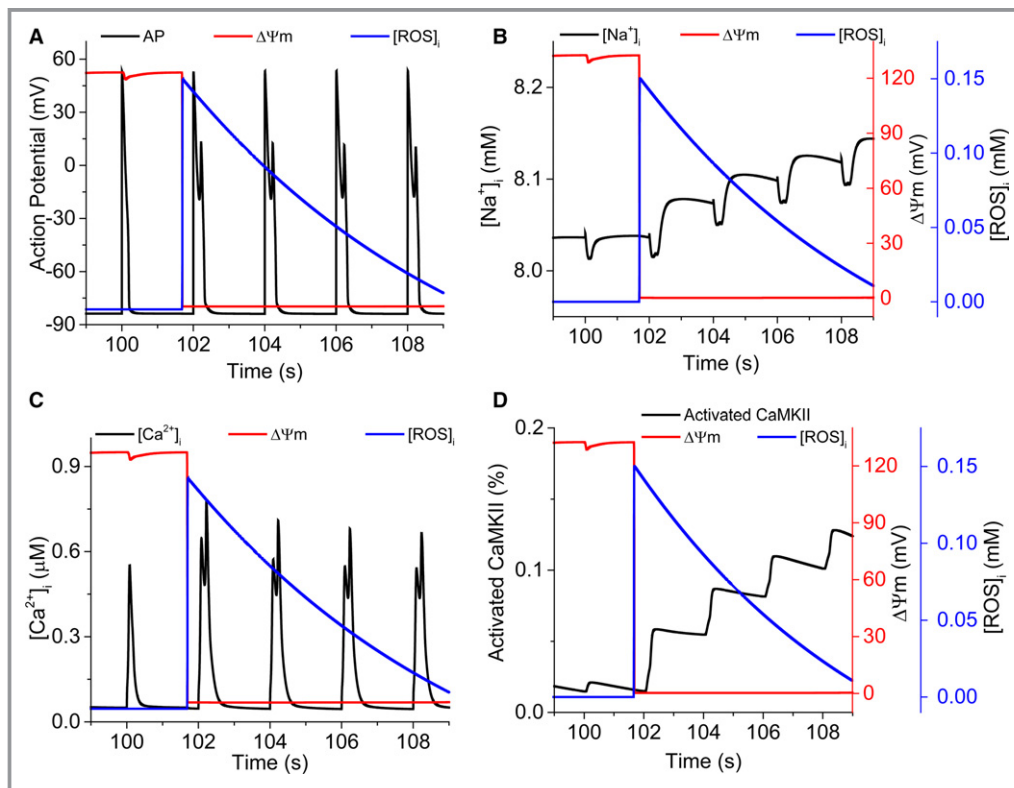
**Figure 2.** Validation of cardiomyocyte excitation-contraction coupling, mitochondrial energetics, and ROS-induced-ROS-release model that incorporates oxidative  $Ca^{2+}$ /calmodulin-dependent protein kinase II (CaMKII) activation and slow  $Na^+$  channels phosphorylation modules. A, The effect of pacing cycle length (PCL) on the duration of action potential (APD). For comparison, the APDs at different PCLs were normalized to the APD at PCL=1 second. Blank triangles are model simulations and black squares represent experimental data from Aiba et al.<sup>49</sup> B, The effects of oxidative CaMKII activation on late  $Na^+$  current ( $I_{Na,L}$ ). The integral of  $I_{Na,L}$  was calculated between 50 and 500 ms after the onset of depolarization. The CaMKII activation–induced  $I_{Na,L}$  change (ie,  $\Delta$  integral  $I_{Na,L}$ ) was obtained by subtracting the baseline  $I_{Na,L}$  integral from the CaMKII  $I_{Na,L}$  integral. Simulation was run with PCL=2 seconds. Experimental data are from Wagner et al.<sup>38</sup> C, Effect of cytosolic  $H_2O_2$  on action potential at different PCLs (1000 and 6000 seconds). Left panel shows model simulations and right panel shows experimental data from isolated rabbit ventricular myocytes (modified from Zhao et al<sup>55</sup> with permission. Copyright© 2012, The American Physiological Society). WT indicates wild-type.

mitochondrial oscillations and cyclic ROS production (Figure S2A). The results indicate that addition of new model components (eg, mdROS-mediated oxidative CaMKII activation and CaMKII-dependent  $\text{Na}^+$  channels phosphorylation) did not alter the dynamics of the existing model subsystems. Simulations also show that  $\Delta\Psi_m$  depolarization (and the associated mdROS bursting) led to sustained EADs during each oscillatory cycle (Figure 3A, for better visualization only the first depolarization was shown). Cytosolic  $\text{Na}^+$  concentration ( $[\text{Na}^+]_i$ ) climbed gradually during mitochondrial depolarization (Figure 3B). Cytosolic  $\text{Ca}^{2+}$  transient rose slightly and exhibited a large increase during the decay phase (Figure 3C). The dynamics of the fraction of activated CaMKII were similar to that of  $[\text{Na}^+]_i$  (Figure 3D).

To examine the ionic mechanisms underlying mdROS-mediated EADs, we analyzed the dynamics of major  $\text{Ca}^{2+}$  and  $\text{Na}^+$  handling currents/fluxes before and after mitochondrial depolarization, and with or without mdROS-induced oxidative CaMKII activation. In the absence of CaMKII activation, the mdROS bursts slightly elongated APD and  $\text{Ca}^{2+}$  transient, enhanced  $I_{\text{Na,L}}$ , and shifted the  $\text{Na}^+$ - $\text{Ca}^{2+}$  exchanger current ( $I_{\text{NaCa}}$ ) forward component to the right (Figure 4, red lines). The effects on L-type calcium channel current ( $I_{\text{CaL}}$ ), SR  $\text{Ca}^{2+}$  release, and SERCA  $\text{Ca}^{2+}$  uptake were

small. Addition of CaMKII activation had negligible effects on APD and cytosolic  $\text{Ca}^{2+}$  concentration ( $[\text{Ca}^{2+}]_i$ ), as well as  $I_{\text{NaCa}}$ ,  $I_{\text{CaL}}$ , and SR  $\text{Ca}^{2+}$  handling under physiological mdROS conditions (ie, polarized  $\Delta\Psi_m$ ) (Figure 4, blue lines). The  $I_{\text{Na,L}}$  integral was slightly increased, likely caused by  $[\text{Ca}^{2+}]_i$ -induced CaMKII activation. During mitochondrial depolarization, mdROS-mediated CaMKII activation did not change the peak  $I_{\text{Na}}$  but caused substantial  $I_{\text{Na,L}}$  augmentation (Figure 4C, olive line arrow #1), resulting in APD prolongation and AP reverse (Figure 4A, olive lines). The AP reverse reactivated  $I_{\text{CaL}}$  (Figure 4E, olive line), which triggered  $\text{Ca}^{2+}$ -induced  $\text{Ca}^{2+}$  release (Figure 4F, olive lines), leading to a larger  $\text{Ca}^{2+}$  elevation (Figure 4B, olive line) and a second  $I_{\text{Na,L}}$  surge (Figure 4C, olive line arrow #2). The forward mode  $I_{\text{NaCa}}$  was initially inhibited and reversed (arrow #1) and then largely amplified (arrow #2) (Figure 4C, olive line), caused by AP reverse and altered  $\text{Na}^+$  and  $\text{Ca}^{2+}$  homeostasis. It is worth mentioning that oxidative CaMKII activation alone could not induce delayed afterdepolarizations (DADs; data not shown), which is consistent with the findings of Foteinou et al.<sup>44</sup>

One unique characteristic of our ECME-RIRR model is its capability to simulate sustained mitochondrial oscillations<sup>50,56</sup> (Figure S2A), allowing examination of the dynamics of AP

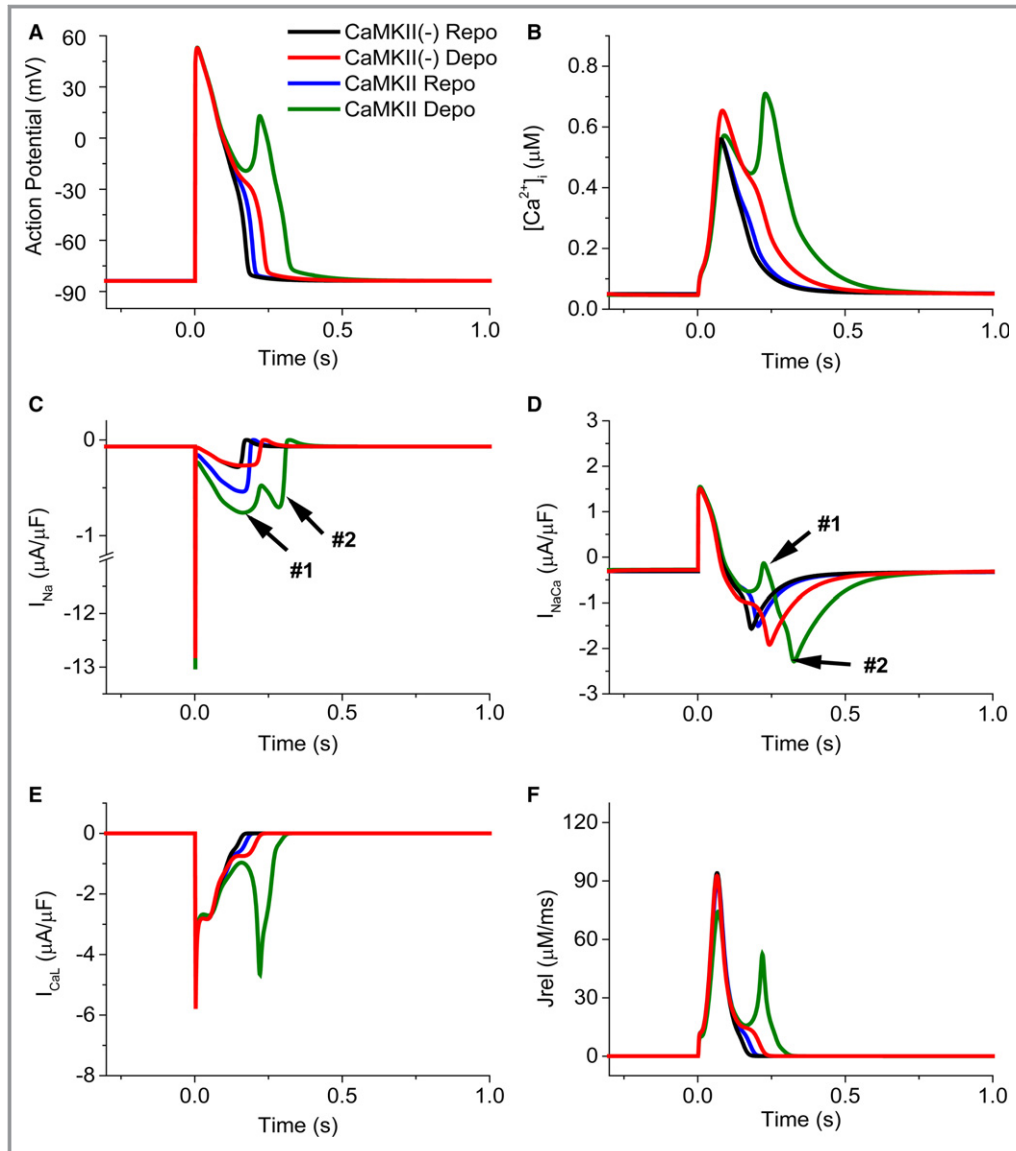


**Figure 3.** Effect of mitochondrial depolarization and mitochondrial-derived reactive oxygen species (ROS) bursts on action potential (A), cytosolic  $\text{Na}^+$  ( $[\text{Na}^+]_i$ ) (B), cytosolic  $\text{Ca}^{2+}$  concentration ( $[\text{Ca}^{2+}]_i$ ) (C), and fraction of activated  $\text{Ca}^{2+}$ /calmodulin-dependent protein kinase II (CaMKII) (D). *shunt*=0.1 and pacing cycle length=2 seconds.

upon mitochondrial repolarization.<sup>5,52</sup> As shown in Figure 5A, after  $\Delta\Psi_m$  repolarization, AP EADs surprisingly remained on the first several (eg, 7 in this simulation) beats, even though mdROS had reduced to basal levels (Figure S2A). The sustained EADs then turned to intermittent EADs and eventually became normal APs.  $[Ca^{2+}]_i$  (Figure 5B) and activation of  $I_{Na,L}$  (Figure 5C) followed the same pattern.  $[Na^+]_i$  (Figure 5D) and fraction of phosphorylated  $Na^+$  channels (Frac\_NaP) (Figure 5E) gradually decreased during the repolarization phase. However,  $[Na^+]_i$  did not completely return to the prepolarization level, causing gradual  $[Na^+]_i$

accumulation along the progression of mitochondrial oscillations (Figure S2B). In the absence of mdROS-induced oxidative CaMKII activation,  $[Na^+]_i$  remained relatively constant during mitochondrial oscillations (Figure S2C).

Importantly, with the progression of mitochondrial oscillations, the time needed for AP to return to normal morphology during  $\Delta\Psi_m$  repolarization increased. When *shunt* was further increased to 0.14, EADs (constant and intermittent) were maintained throughout the whole repolarization phase after the third depolarization (Figure S3). This behavior seemed to be attributed to the elevated CaMKII

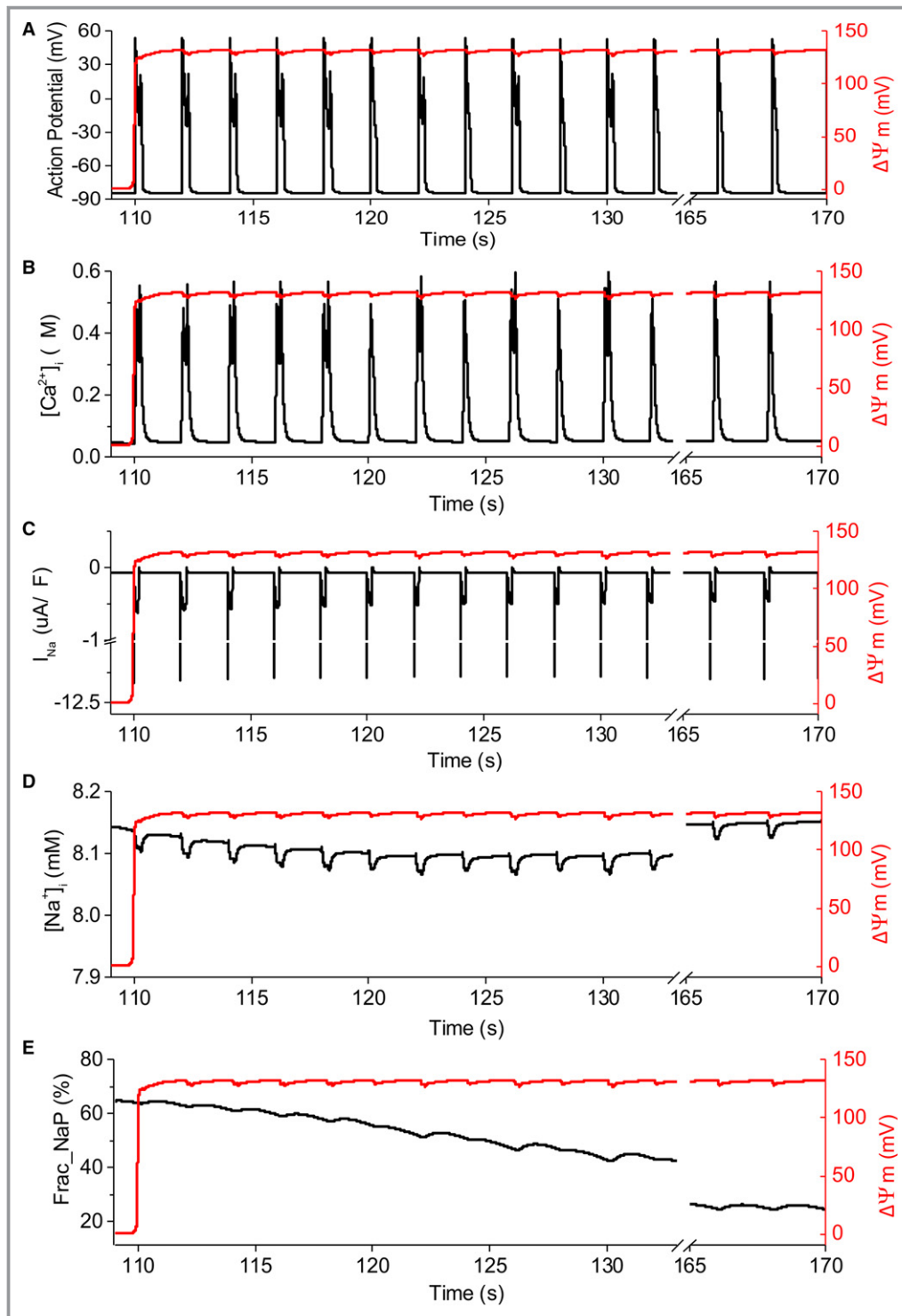


**Figure 4.** Dynamics of action potential (A), cytosolic  $Ca^{2+}$  concentration ( $[Ca^{2+}]_i$ ) (B),  $Na^+$  current ( $I_{Na}$ ) (C),  $Na^+$ - $Ca^{2+}$  exchanger current ( $I_{NaCa}$ ) (D), L-type calcium channel current ( $I_{CaL}$ ) (E), and sarcoplasmic reticulum  $Ca^{2+}$  release ( $J_{rel}$ ) (F) before (Repo) and after (Depo) mitochondrial depolarization.  $Ca^{2+}$ /calmodulin-dependent protein kinase II (CaMKII) (+) represents the new excitation-contraction coupling, mitochondrial energetics, and ROS-induced-ROS-release (ECME-RIRR) model consisting of the oxidative CaMKII activation module, whereas CaMKII (-) represents the previous ECME-RIRR model that does not incorporate the oxidative CaMKII activation module. *shunt*=0.1 and pacing cycle length=2 seconds.



activation and augmentation of  $I_{Na,L}$ . Thus, we analyzed the correlation between the number of sustained or intermittent EADs and the peak  $[Na^+]_i$  during the state transition (eg, from sustained EADs to intermittent EADs). Results show

that the numbers of sustained EADs and intermittent EADs were both closely correlated with the peak  $[Na^+]_i$ , especially under more severe stressed conditions (ie,  $shunt=0.14$ ) (Figure 6).



**Figure 5.** Dynamics of action potential (A), cytosolic  $Ca^{2+}$  concentration ( $[Ca^{2+}]_i$ ) (B),  $Na^+$  current ( $I_{Na}$ ) (C), cytosolic  $Na^+$  concentration ( $[Na^+]_i$ ) (D), and fraction of phosphorylated  $Na^+$  channels (Frac\_NaP) (E) during the first mitochondrial repolarization.  $shunt=0.1$  and pacing cycle length=2 seconds.

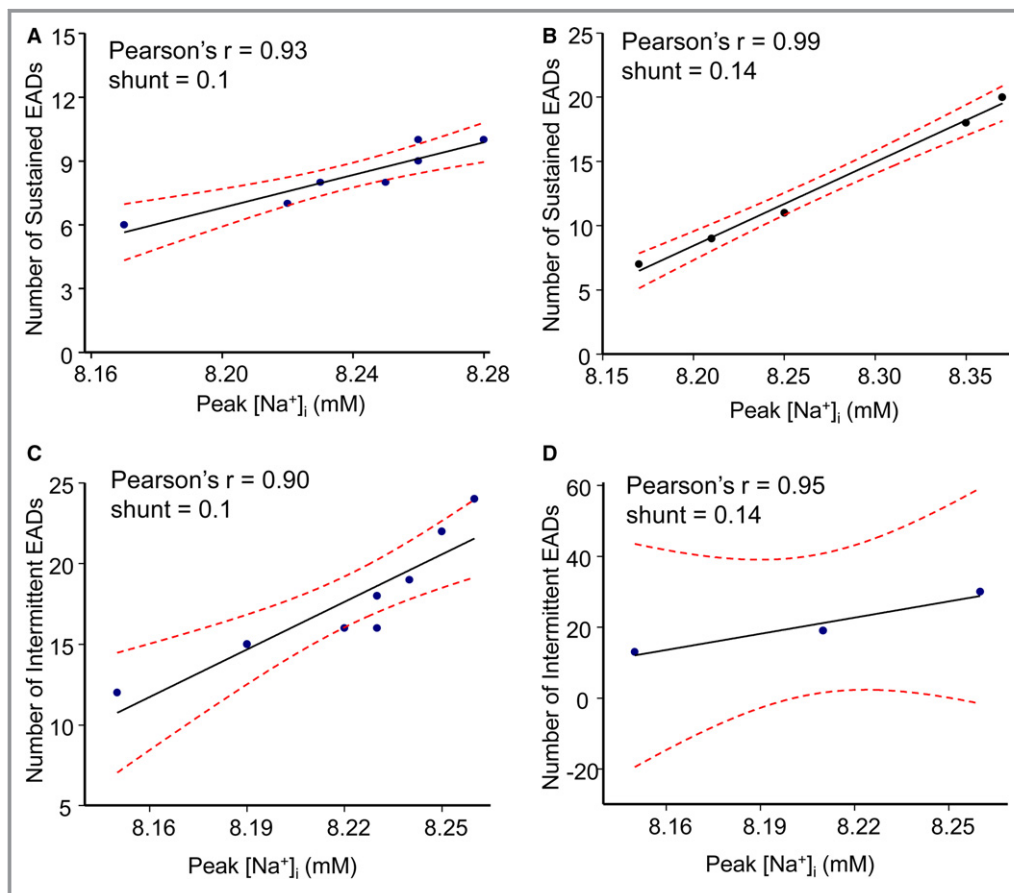
## Effect of Blocking $\text{Na}^+$ or $\text{Ca}^{2+}$ Handling Channel on mdROS-CaMKII Activation–Induced EADs

Next, we examined the effect of completely blocking individual  $\text{Na}^+$  or  $\text{Ca}^{2+}$  handling channel on mdROS-mediated oxidative CaMKII activation–induced AP abnormality during mitochondrial depolarization. Under control conditions (ie, physiological mdROS production or  $shunt=0.02$ ), blocking  $I_{\text{Na,L}}$  had no effect on AP upstroke but slightly shortened APD. The effects on  $[\text{Ca}^{2+}]_i$ ,  $[\text{Na}^+]_i$ ,  $I_{\text{NaCa}}$ ,  $I_{\text{CaL}}$ , and the peak of  $I_{\text{Na}}$  were negligible (data not shown). Under pathological mdROS production conditions (eg,  $shunt=0.14$ ), 100% elimination of  $I_{\text{Na,L}}$  abolished EADs, transient  $I_{\text{NaCa}}$  reverse, and  $I_{\text{CaL}}$  reactivation, accompanied by reduced  $[\text{Ca}^{2+}]_i$  and  $[\text{Na}^+]_i$  overload (Figure 7A, blue lines).

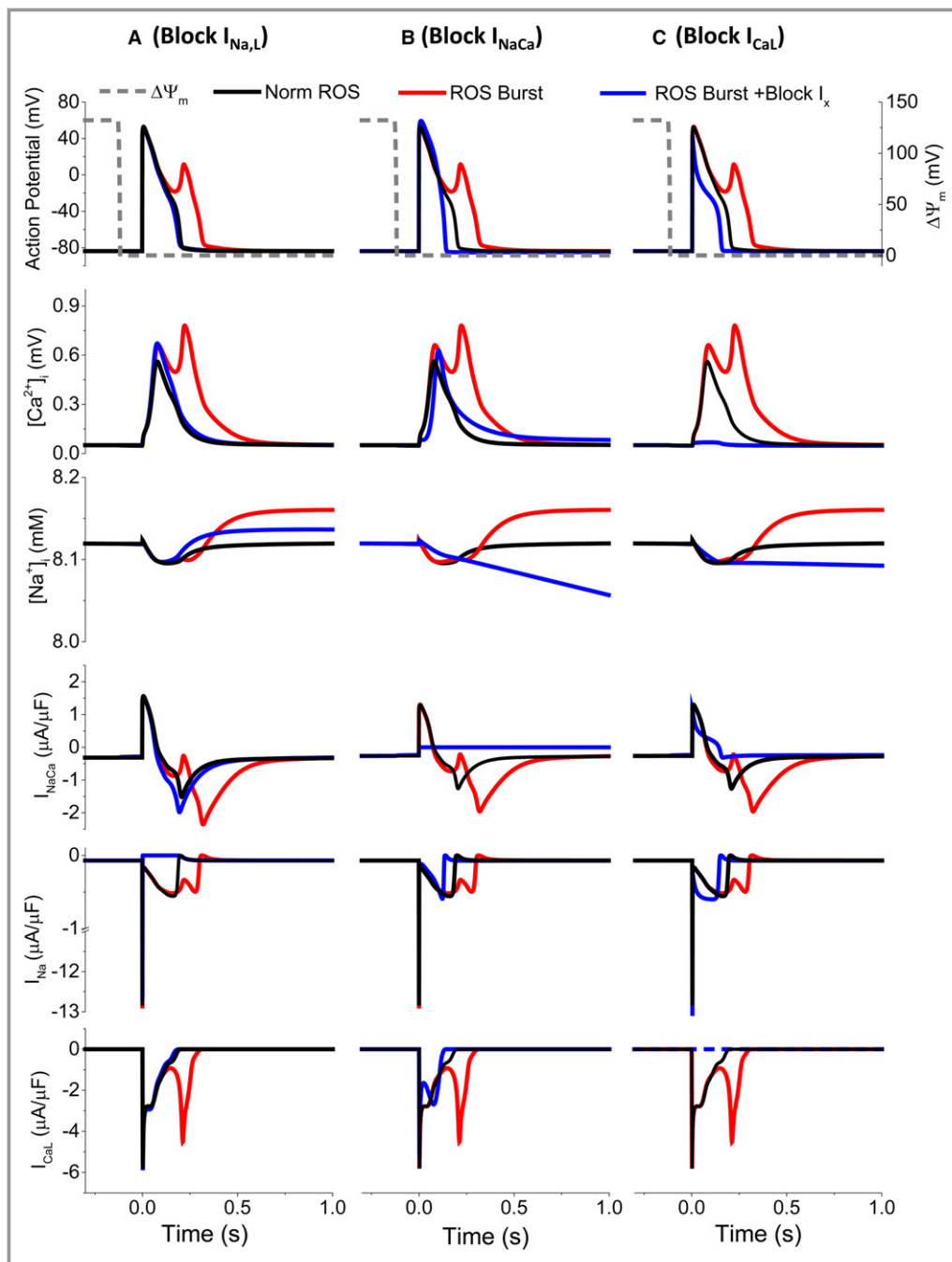
Similar to  $I_{\text{Na,L}}$  inhibition, completely blocking  $I_{\text{NaCa}}$  suppressed  $I_{\text{CaL}}$  reactivation and the subsequent  $\text{Ca}^{2+}$ -induced  $\text{Ca}^{2+}$  release, which prevented  $\text{Ca}^{2+}$  elevation and abolished the EADs (Figure 7B, blue lines).  $I_{\text{NaCa}}$  blockage also reduced

$I_{\text{Na,L}}$  enhancement and  $[\text{Na}^+]_i$  (Figure 7B), which was consistent with published data.<sup>55</sup> It is worth mentioning that although transient blockage seems beneficial, long-term  $I_{\text{NaCa}}$  inhibition may cause significant alteration of  $[\text{Ca}^{2+}]_i$  and  $[\text{Na}^+]_i$  homeostasis and eventually lead to abnormal APs (such as EADs).

Our model simulations show that blocking  $I_{\text{CaL}}$  also eliminated the oxidative CaMKII activation–induced EADs, which was consistent with previous experimental data showing that L-type  $\text{Ca}^{2+}$  channel inhibitor suppressed oxidative stress–induced EADs.<sup>39</sup> Lack of  $I_{\text{CaL}}$  activation facilitated phase 2 AP repolarization, resulting in significant APD shortening that hindered the subsequent  $\text{Ca}^{2+}$ -induced  $\text{Ca}^{2+}$  release and  $\text{Ca}^{2+}$  overload. Consequently,  $\text{Na}^+/\text{Ca}^{2+}$  exchanger inward current enhancement was suppressed (Figure 7C). The outcome of  $I_{\text{CaL}}$  blockade in the absence of mdROS bursts were shortened APD, abolished AP plateau, and diminished  $\text{Ca}^{2+}$  transients (data not shown), which agreed with previous studies.<sup>57,58</sup>



**Figure 6.** Correlation between the number of sustained early afterdepolarizations (EADs) (A and B) and intermittent EADs (C and D) and peak  $\text{Na}^+$  concentration during afterdepolarizations during mitochondrial repolarization at different  $shunts$  (0.1 for A and C and 0.14 for B and D). Black solid lines represent regression and red dash lines represent 95% confidence bands; pacing cycle length=2 seconds.



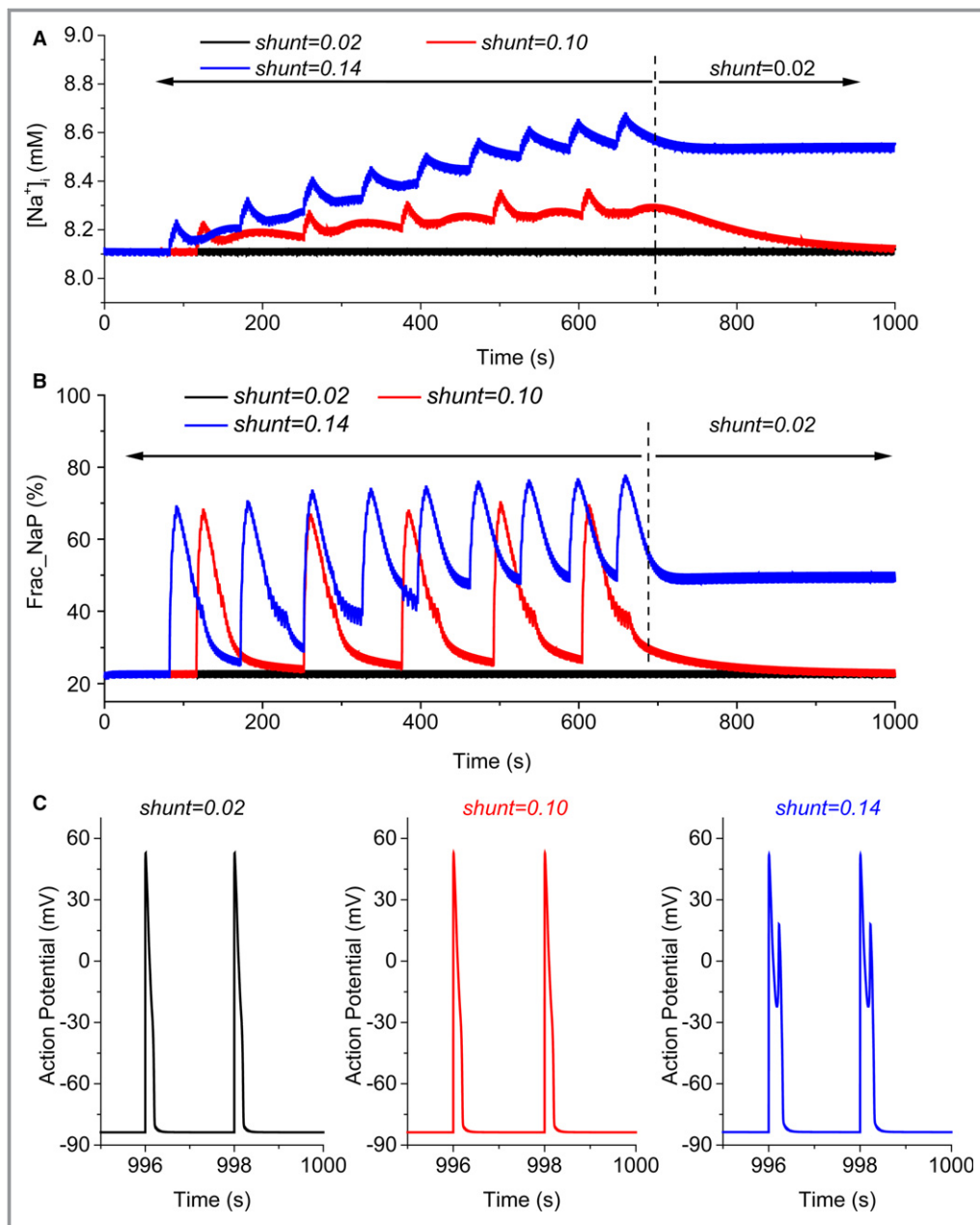
**Figure 7.** Effect of complete blockage of late  $\text{Na}^+$  current ( $I_{\text{Na,L}}$ ) (A),  $\text{Na}^+$ - $\text{Ca}^{2+}$  exchanger current ( $I_{\text{NaCa}}$ ) (B), or L-type calcium channel current ( $I_{\text{CaL}}$ ) (C) on action potential (1), cytosolic  $\text{Ca}^{2+}$  concentration ( $[\text{Ca}^{2+}]_i$ ) (2), cytosolic  $\text{Na}^+$  concentration ( $[\text{Na}^+]_i$ ) (3),  $I_{\text{NaCa}}$  (4),  $I_{\text{Na}}$  (5), and  $I_{\text{CaL}}$  (6) under normal and mitochondrial depolarization conditions.  $shunt=0.14$  and pacing cycle length=2 seconds.

### Effect of Antioxidant Treatment on mdROS-CaMKII Activation-Induced EADs

We then examined whether antioxidant treatment, such as reducing mitochondrial ROS production or increasing ROS scavenging could eliminate mdROS-CaMKII activation-induced EADs. In the simulations shown in Figure 8,  $shunt$  was initially set to the basal level (0.02) for 5 seconds, then

increased to 0.1 or 0.14, and finally reduced to 0.02 at 700 seconds. Increasing  $shunt$  caused sustained mitochondrial oscillations and correlated fluctuations of  $[\text{Na}^+]_i$  and  $\text{Frac\_NaP}$ . Interestingly, both  $[\text{Na}^+]_i$  and  $\text{Frac\_NaP}$  increased gradually with the progression of mitochondrial oscillations, with the increases more evident at higher  $shunt$  (Figure 8A and 8B). Reducing  $shunt$  from 0.1 to the basal level rendered  $[\text{Na}^+]_i$  and  $\text{Frac\_NaP}$  to their initial values and eliminated EADs

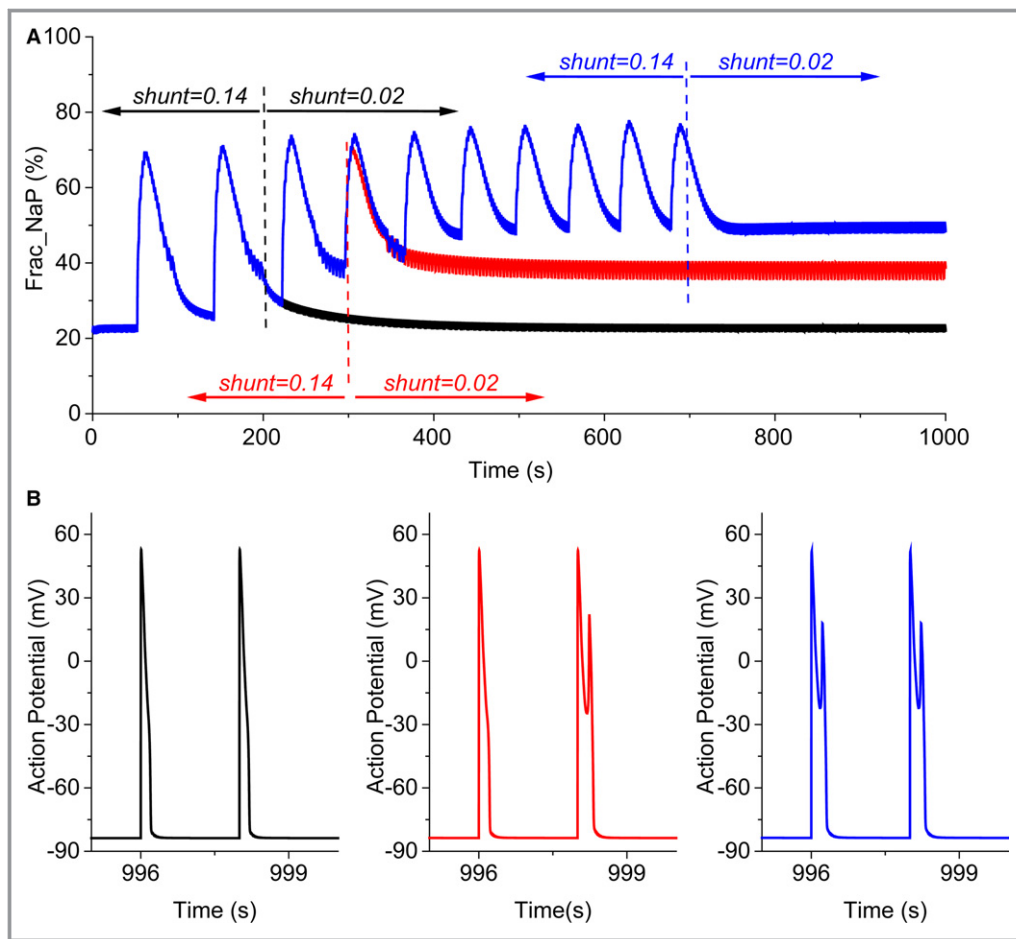




**Figure 8.** Effect of reducing *shunt* on mitochondrial-derived reactive oxygen species (mdROS)-Ca<sup>2+</sup>/calmodulin-dependent protein kinase II (CaMKII) activation-induced early afterdepolarizations (EADs). In these simulations, *shunt* was set as 0.02 (black line), 0.10 (red line), or 0.14 (blue line) during 0 to 700 seconds and 0.02 thereafter. A, Cytosolic Na<sup>+</sup> concentration ([Na<sup>+</sup>]<sub>i</sub>), (B) fraction of phosphorylated Na<sup>+</sup> channels (Frac\_NaP), and (C) action potentials of the last 2 beats. Pacing cycle length=2 seconds.

(Figure 8, red lines). However, when the preceding *shunt* was higher (ie, 0.14), reducing ROS production at 700 seconds failed to normalize the elevated [Na<sup>+</sup>]<sub>i</sub> and Frac\_NaP and suppress EADs (Figure 8, blue lines). Interestingly, we found that reducing mdROS production (*shunt*, from 0.14 to 0.02) earlier (eg, at 350 seconds) converted sustained EADs to intermittent EADs. When *shunt* reduction was induced earlier still (eg, 200 seconds), [Na<sup>+</sup>]<sub>i</sub> overload and the oxidative stress-induced EADs were eliminated (Figure 9).

Another strategy to reduce oxidative stress is to use antioxidant scavengers. In our model, this can be achieved by increasing *et\_SOD*, a parameter that represents the total amount of superoxide dismutase. Similar to reducing *shunt*, increasing *et\_SOD*, when introduced sufficiently soon after mitochondrial depolarization (eg, at 200 seconds), successfully reduced elevated [Na<sup>+</sup>]<sub>i</sub> and suppressed EADs. However, increasing ROS scavenging later (eg, 300 and 700 seconds) failed to eliminate EADs (Figure S4). Taken together, those



**Figure 9.** Effect of timing of reducing *shunt* on mitochondrial-derived reactive oxygen species- $\text{Ca}^{2+}$ /calmodulin-dependent protein kinase II (CaMKII) activation-induced early afterdepolarizations (EADs). In these simulations, *shunt* was initially set as 0.14 and then reduced to 0.02 at 200 seconds (black line), 300 seconds (red line), or 700 seconds (blue lines). A, Fraction of phosphorylated  $\text{Na}^+$  channels (Frac\_NaP). B, Action potentials of the last 2 beats. Pacing cycle length=2 seconds.

simulations imply that: (1) altered ion (eg,  $[\text{Na}^+]_i$  and  $[\text{Ca}^{2+}]_i$ ) homeostasis plays a critical role in mdROS-CaMKII activation-induced EADs, and (2) timely antioxidant treatment is critical for its antiarrhythmic effect with the sooner the better.

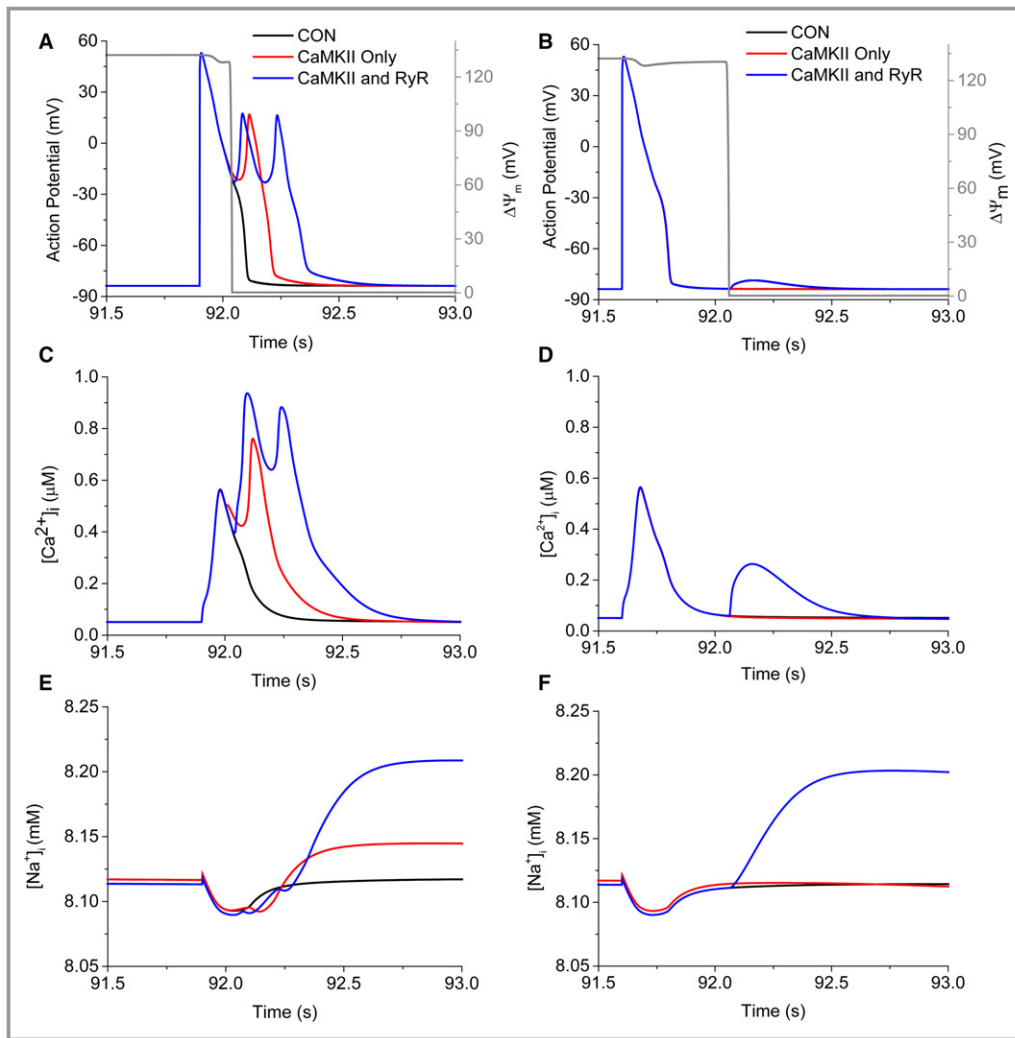
### RyRs Oxidation Effect for Inducing Arrhythmias

In a recent computational study, we showed that mdROS can induce abnormal  $\text{Ca}^{2+}$  cycling and elicit erratic APs by directly activating RyRs and inhibiting SERCA. Here, we examined whether concurrent oxidative RyRs activation would exacerbate the effect of oxidative CaMKII activation on  $\text{Ca}^{2+}$  mishandling and AP abnormality. As shown in Figure 10A, mdROS induced during phase 2 of the AP, when modeled to activate CaMKII only, caused an EAD. Adding the effect of mdROS on SR  $\text{Ca}^{2+}$  handling (eg, RyRs activation and SERCA inhibition) converted the single EAD to multiple EADs. Notably, when the mdROS burst was induced during phase 4 of the AP, concurrent oxidative RyRs and CaMKII activation elicited a

DAD, which was otherwise barely seen with oxidative CaMKII activation alone (Figure 10B). Concurrent RyRs oxidation by mdROS also exacerbated  $\text{Na}^+$  and  $\text{Ca}^{2+}$  overload during mitochondrial depolarization (Figure 10C through 10F).

### Discussion

In the present study, we expanded our recently published guinea pig cardiomyocyte ECME-RIRR model<sup>47</sup> by incorporating mdROS-induced oxidative CaMKII activation and slow  $\text{Na}^+$  channel phosphorylation. Our new model was able to replicate previous model simulations (eg, sustained mitochondrial oscillations) and experimental data (eg, rate dependence of  $\text{H}_2\text{O}_2$ -induced EADs and ROS-induced increases in intracellular  $\text{Na}^+$  and  $\text{Ca}^{2+}$ ). We then simulated how the endogenous mitochondrial-derived oxidative stress (ie, mdROS) may influence CaMKII activity and subsequently alter cardiomyocyte ion homeostasis and APs. Our main findings are: (1) mdROS-mediated oxidative CaMKII activation-induced



**Figure 10.** Concurrent mitochondrial-derived reactive oxygen species (mdROS)-mediated oxidative ryanodine receptor (RyR) activation and oxidative  $Ca^{2+}$ /calmodulin-dependent protein kinase II (CaMKII) activation on action potential (A and B), cytosolic  $Ca^{2+}$  concentration ( $[Ca^{2+}]_i$ ) (C and D), and cytosolic  $Na^+$  concentration ( $[Na^+]_i$ ) (E and F). In simulations of (A, C, and E) mdROS bursting was induced at phase 2 of the action potential and in (B, D, and F) mdROS bursting was induced at phase 4 of the action potential. Pacing cycle length=2 seconds and  $shunt=0.1$ . CON:  $shunt = 0.02$ , or no mitochondrial-derived reactive oxygen species bursting.

augmentation of  $I_{Na,L}$  alone is sufficient to elicit EADs; (2) mdROS-CaMKII activation-induced EADs can be sustained even when mdROS reduces to a physiological level; and (3) mdROS burst-induced EADs can be suppressed by antioxidant treatment only when it is given within a timely window.

It has been proposed that the proarrhythmic effect of oxidative CaMKII activation is attributed to its capability to phosphorylate multiple ion channels/transporters underlying  $Ca^{2+}$  handling and AP. However, the detailed mechanistic pathways remain incompletely understood, partially because of the difficulty in experimentally dissecting the contribution of individual ion currents. For instance, although CaMKII activation of  $I_{Na,L}$  has been implicated to be involved in

oxidative stress-induced EADs,<sup>39,44,59</sup> whether this  $I_{Na,L}$  augmentation alone can induce EADs under oxidative stress has never been examined. Therefore, in this computational study, we developed an ECME-RIRR model that considered only the direct modulatory effect of CaMKII oxidation on  $I_{Na,L}$ . Model simulations showed that oxidative CaMKII activation-induced augmentation of  $I_{Na,L}$ , which is comparable to experimental data (Figure 2B), successfully elicits EADs in a cardiomyocyte exposure to increased mdROS. Further analysis suggests that the augmented  $I_{Na,L}$  causes EADs by altering both membrane potential and intracellular ion (eg,  $Na^+$  and  $Ca^{2+}$ ) homeostasis. In particular, our simulations revealed that the mdROS-CaMKII activation-induced EADs



involve the following: (1) increased  $I_{Na,L}$  leads to APD prolongation and AP reverse; (2) the AP reverse causes a shift in  $Na^+/Ca^{2+}$  exchanger activity (reverse mode) and  $I_{CaL}$  reactivation; (3) reactivation of  $I_{CaL}$  triggers  $Ca^{2+}$ -induced  $Ca^{2+}$  release and results in a larger  $Ca^{2+}$  transient, which further augments  $I_{CaL}$  via a dynamic positive feedback mechanism; and (4) the large  $Ca^{2+}$  increase activates the forward mode  $I_{NaCa}$  and CaMKII-mediated  $I_{Na,L}$ , collectively resulting in EADs.

It is worth mentioning that while our model suggests that direct CaMKII activation of  $I_{CaL}$  is not required in mdROS-CaMKII activation-induced EADs,  $I_{CaL}$  reactivation, caused by AP reverse, plays a critical role in the EAD generation, as blocking  $I_{CaL}$  eliminates the mdROS-CaMKII activation-induced EADs. Interestingly, blocking  $I_{CaL}$  also caused APD shortening. This finding is different from that reported in our recent computational studies<sup>47</sup> focusing on mdROS-induced abnormal SR  $Ca^{2+}$  handling, in which blocking  $I_{CaL}$  suppressed EADs but did not reduce AP prolongation (as compared with normal mdROS). This suggests that the ionic mechanisms underlying oxidative CaMKII activation and oxidative RyRs activation-mediated arrhythmogenesis are different. We also found that oxidative CaMKII activation alone cannot generate DADs but concurrent oxidative RyRs and CaMKII activations can. As previous experimental studies<sup>38,39</sup> have recorded both EADs and DADs in  $H_2O_2$ -perfused isolated cardiomyocytes, it is likely that both pathways are presented in cardiomyocytes undergoing oxidative stress. In addition, our channel blocking simulations indicated that  $I_{NaCa}$  activation is also involved in the generation of oxidative CaMKII activation-induced EADs. Thus, although we showed that oxidative CaMKII activation-induced  $I_{Na,L}$  augmentation is capable of eliciting EAD, the actual arrhythmogenic effects of mdROS are clearly multifactorial and new antiarrhythmic treatments targeting both ion channels/transporters/proteins and mitochondria are essential.

Another intriguing finding from the present modeling study is that the mdROS-CaMKII activation-induced EADs may not terminate immediately upon mitochondrial repolarization, even though mdROS has been reduced to basal physiological levels. While the phenomenon of sustained EADs postmitochondrial repolarization in cardiomyocytes needs further experimental verification, it may indeed occur in cells undergoing oxidative stress such as ischemia reperfusion, as a result of the specific property of CaMKII as “a memory molecule.”<sup>60</sup> The memory refers to the autophosphorylation-mediated sustained CaMKII activation even after the dissociation of  $Ca^{2+}/CaM$  or the fall of  $Ca^{2+}$  concentration to baseline levels, which is essential for memory storage in the brain. Recently, Song et al<sup>61</sup> showed that short-term (5 minutes) ROS exposure caused persistent (more than 60 minutes) activation of  $I_{CaL}$  in isolated rat cardiomyocytes, likely via the oxidative stress-induced sustained CaMKII activation,

indicating that CaMKII may act as a redox-sensitive “memory molecule” in cardiomyocytes. Notably, our model simulations showed that the duration of persistent EADs, or the proarrhythmic “memory” of CaMKII activation, is linked to the severity of mitochondrial dysfunction: the higher the mdROS bursting, the stronger the memory. Permanent memory might form if mitochondrial malfunction lasts long enough; in this case persistent arrhythmias will occur (Figure 8). Thus, as suggested by our antioxidant treatment simulations (Figure 9 and Figure S4) the ideal antiarrhythmic treatment would require the intervention be given timely and before the permanent memory of CaMKII is formed. Our computational analysis further showed that there is a close correlation between peak  $[Na^+]_i$  and the robustness of CaMKII’s memory, or the durations of the sustained and intermittent EADs during mitochondrial repolarization, suggesting that cytosolic  $[Na^+]_i$  may be used as a risk factor of oxidative CaMKII activation-mediated arrhythmogenesis. The gradual  $[Na^+]_i$  accumulation and sustained EADs facilitated by the oxidative stress-induced CaMKII-dependent  $I_{Na,L}$  augmentation has also been reported by Wagner et al.<sup>38</sup>

In addition to antioxidant treatment, we also examined several other possible antiarrhythmic strategies such as blocking  $Na^+$  or  $Ca^{2+}$  channels. Although our simulations showed that blocking  $I_{NaCa}$ ,  $I_{CaL}$ , or  $I_{Na,L}$  all eliminated the mdROS-mediated oxidative CaMKII activation-induced EADs, their antiarrhythmic roles should be further assessed experimentally, as long-term ion channel inhibition may break ion homeostasis and induce new arrhythmogenic substrates. For instance, it has been shown that inhibition of  $Na^+/Ca^{2+}$  exchanger-mediated  $Ca^{2+}$  extrusion increases  $Ca^{2+}$  spark frequency in resting cardiac myocytes. Long-term  $I_{CaL}$  inhibition, especially by nondihydropyridine  $Ca^{2+}$  channel blockers, can cause a shortening of APD and reduce cardiac contractility and conduction. In addition, the role of  $Ca^{2+}$  channel blockers in ventricular arrhythmias is limited and less well defined.<sup>62–64</sup> Compared with  $I_{NaCa}$  and  $I_{CaL}$  inhibition, blocking the  $I_{Na,L}$  reduces depolarizing current during the plateau phase of the AP and thus may be more potent and safer. In line with this, it has been reported that a selective  $I_{Na,L}$  inhibitor, GS-458967, prevents APD prolongation without affecting AP upstroke velocity in guinea pig ventricular myocytes.<sup>65,66</sup> Ranolazine, another  $Na^+$  channel blocker, has been shown to reduce EAD and DAD occurrence in various settings where  $I_{NaL}$  is enhanced.<sup>59</sup>

## Model Limitations

As our major goal was to examine whether, and if so, mdROS-CaMKII activation-induced  $I_{NaL}$  augmentation can induce EADs, the present model only incorporates CaMKII-dependent phosphorylation of  $Na^+$  channels. However, it is well

appreciated that many other ion channels/transporters such as LCCs, RyRs, and  $K^+$  channels can be phosphorylated by CaMKII.<sup>67,68</sup> CaMKII can increase  $I_{CaL}$  and SR  $Ca^{2+}$  release, thereby exacerbating  $Ca^{2+}$  overload and increasing the risk of arrhythmogenesis. Moreover, the activity of LCCs, RyRs,  $Na^+$  channels, and  $K^+$  channels can be directly influenced by mdROS.<sup>69</sup> The effects of oxidative CaMKII activation and direct oxidation on ion channels and homeostasis as well as AP may or may not overlap. Furthermore, previous studies from our laboratory and others have shown that deregulated cytosolic ion handling perturbs mitochondrial energetics and leads to oxidative stress, which can positively feedback on CaMKII activity. Finally, recent studies suggested that CaMKII may directly phosphorylate mitochondrial ion channels such as the  $Ca^{2+}$  uniporter,<sup>23</sup> thus altering mitochondrial ion homeostasis and bioenergetics.<sup>23</sup> Those components can be added to the ECME-RIRR model in the future. That being said, lack of these mechanisms should have little impact on the present study, as our main goal was to develop a computational model to examine whether the mdROS-mediated CaMKII activation can induce EADs in cardiomyocytes and to understand the underlying ionic mechanisms.

## Conclusions

The present study provides a novel computational tool to quantitatively investigate the proarrhythmic effects of mdROS-mediated oxidative CaMKII activation in cardiomyocytes. The results indicate that CaMKII activation is sufficient to initiate downstream molecular events that promote aberrant  $Ca^{2+}$  handling and abnormal APs by sensing elevated mitochondrial-derived oxidative stress. Our simulations also underscore the importance of timely treatments in the context of oxidative CaMKII activation-induced arrhythmias.

## Acknowledgments

We thank Dr Qince Li for suggestive discussion.

## Sources of Funding

The authors acknowledge funding support from China Scholarships Council (grant No. 201506250131) and Key Technologies Research and Development Program of China (grant No. 2017YFC0110400) (to Yang) and National Institutes of Health/National Heart, Lung, and Blood Institute R01HL121206A1 (to Zhou).

## Disclosures

None.

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# **Supplemental Material**

**Table S1. Sarcolemmal membrane ionic currents**

Fast Na<sup>+</sup> current (I<sub>Na</sub>)

$I_{Na} = \bar{G}_{Na} m^3 h j (V - E_{Na})$	E1
$E_{Na} = \frac{RT}{F} \ln \frac{[Na^+]_o}{[Na^+]_i}$	E2
$\frac{dm_{Na}}{dt} = m(1-m_{Na}) - m_{Na}$	E3
$\frac{dh_{Na}}{dt} = h(1-h_{Na}) - h_{Na}$	E4
$\frac{dj_{Na}}{dt} = j(1-j_{Na}) - j_{Na}$	E5
$m = 0.32 \frac{V + 47.13}{1 - e^{-0.1(V+47.13)}}$	E6
$m = 0.08 e^{-V/11}$	E7
For $V \geq -40$ mV	
$h = 0.0$	E8
$j = 0.0$	E9
$h = 0.13 \frac{1}{1 + e^{\frac{V+10.66}{11.1}}}$	E10
$j = 0.3 \frac{e^{-2.535 \cdot 10^{-7}V}}{1 + e^{-0.1(V+32)}}$	E11
For $V < -40$ mV	
$h = 0.135 e^{\frac{80+V}{-6.8}}$	E12
$j = \frac{(-127,140 e^{0.2444 V} - 3.474 \cdot 10^{-5} e^{0.04391 V}) \cdot (V + 37.78)}{1 + e^{0.311 (V+79.23)}}$	E13



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$$h = 3.56 e^{0.079 V} + 3.1 \cdot 10^5 e^{0.35 V} \quad \text{E14}$$


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$$j = 0.1212 \frac{e^{-0.01052 V}}{1 + e^{-0.1378 (V+40.14)}} \quad \text{E15}$$


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### Markov slow Na<sup>+</sup> model ( $I_{Na,L}$ )

*Transition rate expressions (ms<sup>-1</sup>)*

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$$IC3toIC2 = \frac{P_{1a1}}{P_{2a1} \times \exp(-V/17) + 0.2 \times \exp(-V/150)} \quad \text{E16}$$


---

$$C3toC2 = IC3toIC2 \quad \text{E17}$$


---

$$LC3toLC2 = IC3toIC2 \quad \text{E18}$$


---

$$LC2toIF = \frac{P_{1a1}}{P_{2a1} \times \exp(-V/12) + 0.25 \times \exp(-V/150)} \quad \text{E19}$$


---

$$C2toC1 = IC2toIF \quad \text{E20}$$


---

$$LC2toLC1 = IC2toIF \quad \text{E21}$$


---

$$LC1toLO = \frac{P_{1a1}}{P_{2a1} \times \exp(-V/12) + 0.25 \times \exp(-V/150)} \quad \text{E22}$$


---

$$C1toO = LC1toLO \quad \text{E23}$$


---

$$IC2toIC3 = P_{1b1} \times \exp(-V/P_{2b1}) \quad \text{E24}$$


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$$C2toC3 = IC2toIC3 \quad \text{E25}$$


---

$$LC2toLC3 = IC2toIC3 \quad \text{E26}$$


---

$$IFtoIC2 = P_{1b2} \times \exp\left(-\frac{V - P_{2b2}}{P_{2b1}}\right) \quad \text{E27}$$


---

$$C1toC2 = IFtoIC2 \quad \text{E28}$$


---

$$LC1toLC2 = IFtoIC2 \quad \text{E29}$$


---

$$LOtoLC1 = P_{1b3} * \exp\left(-\frac{V - P_{2b3}}{P_{2b1}}\right) \quad \text{E30}$$


---

$$OtoC1 = LOtoLC1 \quad \text{E31}$$


---

$$IC3toC3 = P_{1a5} \times \exp\left(-\frac{V}{P_{2a5}}\right) \quad \text{E32}$$


---

$IC2toC2 = IC3toC3$	E33
$IFtoC1 = IC3toC3$	E34
$C3toIC3 = P_{1b5} + P_{2b5} \times V$	E35
$C2toIC2 = C3toIC3$	E36
$C1toIF = C3toIC3$	E37
$OtoIF = P_{1a4} \times \exp\left(\frac{V}{P_{2a4}}\right)$	E38
$IFtoO = \frac{LC1toLO \times OtoIF \times IC3toC3}{LOtoLC1 \times C3toIC3}$	E39
$IFtoIM1 = \frac{P_{1a4} \times \exp(V/P_{2a4}/P_{2a42})}{P_{1a6}}$	E40
$IM1toIF = P_{1b6} \times \exp\left(-\frac{V}{P_{2b6}}\right)$	E41
$IM1toIM2 = P_{1a7} \times \exp\left(\frac{V}{P_{2a7}}\right)$	E42
$IM2toIM1 = P_{1b7} \times \exp\left(-\frac{V}{P_{2b7}}\right)$	E43
$C3toLC3 = P_{1a8}$	E44
$C2toLC2 = C3toLC3$	E45
$C1toLC1 = C3toLC3$	E46
$OtoLO = C3toLC3$	E47
$LC3toC3 = P_{1b8}$	E48
$LC2toC2 = LC3toC3$	E49
$LC1toC1 = LC3toC3$	E50
$LOtoO = LC3toC3$	E51

*Balance equations of the late sodium channels*

$\frac{dIC3}{dt} = C3toIC3 \times C3 + IC2toIC3 \times IC2 - (IC3toIC2 + IC3toC3) \times IC3$	E52
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$$\frac{dIC2}{dt} = IC3toIC2 \times IC3 + IFtoIC2 \times IF + C2toIC2 \times C2 - (IC2toC2 + IC2toC3 + IC2toIF) \times IC2$$

E53

---


$$\frac{dIF}{dt} = IC2toIF \times C2 + IM1toIF \times IM1 + C1toIF \times C1 + OtoIF \times O - (IFtoIC2 + IFtoIM1 + IFtoC1 + FtoO) \times IF$$

E54

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$$\frac{dIM1}{dt} = IFtoIM1 \times IF + IM2toIM1 \times IM2 - (IM1toIF + IM1toIM2) \times IM1$$

E55

---


$$\frac{dIM2}{dt} = IM1toIM2 \times IM1 - IM2toIM1 \times IM2$$

E56

---


$$\frac{dC3}{dt} = IC3toC3 \times IC3 + C2toC3 \times C2 + LC3toC3 \times LC3 - (C3toIC3 + C3toC2 + C3toLC3) \times C3$$

E57

---


$$\frac{dC2}{dt} = IC2toC2 \times IC2 + C3toC2 \times C3 + LC2toC2 \times LC2 + C1toC2 \times C1 - (C2toIC2 + C2toC3 + C2toLC2 + C2toC1) \times C2$$

E58

---


$$\frac{dC1}{dt} = IFtoC1 \times IF + C2toC1 \times C2 + OtoC1 \times O + LC1toC1 \times LC1 - (C1toIF + C1toC2 + C1toO + C1toLC1) \times C1$$

E59

---


$$\frac{dO}{dt} = IFtoO \times IF + C1toO \times C1 + LOtoO \times LO - (OtoIF + OtoC1 + OtoLO) \times O$$

E60

---


$$\frac{dLC3}{dt} = C3toLC3 \times C3 + LC2toLC3 \times LC2 - (LC3toC3 + LC3toLC2) \times LC3$$

E61

---


$$\frac{dLC2}{dt} = C2toLC2 \times C2 + LC3toLC2 \times LC3 + LC1toLC2 \times LC1 - (LC2toC2 + LC2toLC3 + LC2toLC1) \times LC2$$

E62

---


$$\frac{dLC1}{dt} = C1toLC1 \times C1 + LC2toLC1 \times LC2 + LOtoLC1 \times LO - (LC1toC1 + LC1toLC2 + LC1toLO) \times LC1$$

E63

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$$\frac{dLO}{dt} = OtoLO \times O + LC1toLO \times LC1 - (LOtoO + LOtoLC1) \times LO$$

E64

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*Late sodium current*

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$$I_{Na,L} = G_{Na,L} \cdot P_{LO} \cdot (V - E_{Na})$$

E65

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Time-dependent delayed rectifier K<sup>+</sup> current (I<sub>K</sub>)

$I_K = \bar{G}_K X_1 X_K^2 (V - E_K)$	E66
$E_K = \frac{RT}{F} \ln \frac{[K^+]_o + P_{Na,K} [Na^+]_o}{[K^+]_i + P_{Na,K} [Na^+]_i}$	E67
$\bar{G}_K = 0.282 \sqrt{\frac{[K^+]_o}{5.4}}$	E68
$X_1 = \left(1 + e^{(V-40)/40}\right)^{-1}$	E69
$\frac{dX_K}{dt} = (1 - X_K) - X_K$	E70
$= 7.19 \cdot 10^{-5} \frac{V + 30}{1 - e^{0.148(V+30)}}$	E71
$= 1.31 \cdot 10^{-4} \frac{V + 30}{-1 + e^{0.0687(V+30)}}$	E72

Time-independent K<sup>+</sup> current (I<sub>K1</sub>)

$I_{K_1} = \bar{G}_{K_1} K_1 (V - E_{K_1})$	E73
$E_{K_1} = \frac{RT}{F} \ln \frac{[K^+]_o}{[K^+]_i}$	E74
$\bar{G}_{K_1} = 0.75 \sqrt{\frac{[K^+]_o}{5.4}}$	E75
$K_1 = \frac{K_1}{K_1 + K_1}$	E76
$K_1 = \frac{1.02}{1 + e^{0.2385(V - E_{K_1} - 59.215)}}$	E77
$K_1 = \frac{0.4912e^{0.08032(V - E_{K_1} + 5.476)} + e^{0.06175(V - E_{K_1} - 59.431)}}{1 + e^{0.5143(V - E_{K_1} + 4.753)}}$	E78

### Plateau K<sup>+</sup> current (I<sub>Kp</sub>)

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$$I_{K_p} = \bar{G}_{K_p} K_p (V - E_{K_p}) \quad \text{E79}$$

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$$E_{K_p} = E_{K_1} \quad \text{E80}$$

---

$$K_p = \left(1 + e^{(7.488 \text{ V})/5.98}\right)^{-1} \quad \text{E81}$$

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### Na<sup>+</sup>/Ca<sup>2+</sup> exchanger current (I<sub>NaCa</sub>)

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$$I_{NaCa} = k_{NaCa} \frac{1}{K_{m,Na}^3 + [Na^+]_o^3} \frac{1}{K_{m,Ca} + [Ca^{2+}]_o} \frac{1}{1 + k_{sat} e^{(1) \frac{VF}{RT}}} \frac{e^{\frac{VF}{RT}} [Na^+]_i^3 [Ca^{2+}]_o}{e^{(1) \frac{VF}{RT}} [Na^+]_o^3 [Ca^{2+}]_i} \quad \text{E82}$$

---

### Na<sup>+</sup>/K<sup>+</sup> pump current (I<sub>NaK</sub>)

---

$$I_{NaK} = \bar{I}_{NaK} f_{NaK} f_{NaK}^{ATP} \frac{1}{1 + \frac{K_{m,Na_i}^{1.5}}{[Na^+]_i} \frac{[K^+]_o}{[K^+]_o + K_{m,K_o}}} \quad \text{E83}$$

---

$$f_{NaK} = \frac{1}{1 + 0.1245 e^{0.1 \frac{VF}{RT}} + 0.0365 e^{\frac{VF}{RT}} \frac{e^{[Na^+]_o/67.3}}{7}} \quad \text{E84}$$

---

$$f_{NaK}^{ATP} = \frac{1}{1 + \frac{K_{NaK}^{1,ATP}}{[ATP]_i} \frac{1}{1 + \frac{[ADP]_i}{K_{NaK}^{i,ADP}}} } \quad \text{E85}$$

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### Nonspecific Ca<sup>2+</sup> activated current (I<sub>nsCa</sub>)

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$$I_{ns(Ca)} = I_{ns(Na)} + I_{ns(K)} \quad \text{E86}$$

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$$I_{\text{ns(Na)}} = \bar{I}_{\text{ns(Na)}} \left( 1 + \frac{K_{\text{m,ns(Ca)}}^3}{[\text{Ca}^{2+}]_i} \right)^{-1} \quad \text{E87}$$


---

$$\bar{I}_{\text{ns(Na)}} = P_{\text{ns(Na)}} \frac{VF^2}{RT} \frac{0.75 \left( [\text{Na}^+]_i e^{VF/RT} - [\text{Na}^+]_o \right)}{e^{VF/RT} - 1} \quad \text{E88}$$


---

$$I_{\text{ns(K)}} = \bar{I}_{\text{ns(K)}} \left( 1 + \frac{K_{\text{m,ns(Ca)}}^3}{[\text{Ca}^{2+}]_i} \right)^{-1} \quad \text{E89}$$


---

$$\bar{I}_{\text{ns(K)}} = P_{\text{ns(K)}} \frac{VF^2}{RT} \frac{0.75 \left( [\text{K}^+]_i e^{VF/RT} - [\text{K}^+]_o \right)}{e^{VF/RT} - 1} \quad \text{E90}$$


---

### Background $\text{Ca}^{2+}$ current ( $I_{\text{Ca,b}}$ )

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$$I_{\text{Ca,b}} = \bar{G}_{\text{Ca,b}} \left( V - E_{\text{Ca,N}} \right) \quad \text{E91}$$


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$$E_{\text{Ca,N}} = \frac{RT}{2F} \ln \frac{[\text{Ca}^{2+}]_o}{[\text{Ca}^{2+}]_i} \quad \text{E92}$$


---

### Background $\text{Na}^+$ current ( $I_{\text{Na,b}}$ )

---


$$I_{\text{Na,b}} = \bar{G}_{\text{Na,b}} \left( V - E_{\text{Na,N}} \right) \quad \text{E93}$$


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$$E_{\text{Na,N}} = E_{\text{Na}} \quad \text{E94}$$


---

### Sarcolemmal $\text{Ca}^{2+}$ pump current ( $I_{\text{pCa}}$ )

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$$I_{\text{pCa}} = I_{\text{pCa\_max}} F_{\text{pCa}}^{\text{ATP}} \frac{[\text{Ca}^{+2}]_i}{K_{\text{m}}^{\text{pCa}} + [\text{Ca}^{+2}]_i} \quad \text{E95}$$


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$$F_{pCa}^{ATP} = 1 + \frac{K_{m1\_pCa}^{ATP}}{[ATP]_i} \left( 1 + \frac{[ADP]_i}{K_{i\_pCa}^{ADP}} \right) + 1 + \frac{K_{m2\_pCa}^{ATP}}{[ATP]_i} \quad E96$$


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### SERCA pump ( $J_{up}$ )

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$$J_{up} = \frac{V_{maxf} f_b - V_{maxr} r_b}{1 + f_b + r_b} f_{ATP}^{SERCA} \quad E97$$


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$$f_b = \frac{[Ca^{2+}]_i^{Nfb}}{K_{fb}} \quad E98$$


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$$r_b = \frac{[Ca^{2+}]_{SR}^{Nrb}}{K_{rb}} \quad E99$$


---

$$f_{ATP}^{SERCA} = \frac{K_{m,up}^{ATP}}{[ATP]_i} \left( 1 + \frac{[ADP]_i}{K_{i,up}} \right) + 1 + \frac{[ADP]_i}{K'_{i,up}} \quad E100$$


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### L-type $Ca^{2+}$ current ( $I_{Ca}$ )

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$$I_{CaL} = 4 \frac{N_{CaRU}}{C_m} P_{Ca} \frac{VF^2}{RT} \frac{\left[ \frac{P_{(2)}([Ca^{2+}]_{dm}^{(2)} e^{2VF/RT - 0.314[Ca^{2+}]_0)} + P_{(4)}([Ca^{2+}]_{dm}^{(4)} e^{2VF/RT - 0.314[Ca^{2+}]_0)} \right]}{e^{2VF/RT} - 1} \quad E101$$


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### Sarcolemmal membrane potential

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$$\frac{dV}{dt} = -\frac{1}{C_m} \left( I_{Na} + I_{CaL} + I_{Ca,K} + I_K + I_{K1} + I_{Kp} + I_{NaCa} + I_{Na,K} + I_{nsCa} + I_{pCa} + I_{Ca,b} + I_{Na,b} + I_{K,ATP} + I_{Na,L}^* \right) \quad E102$$


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**Table S2. Ca<sup>2+</sup> handling system****40-state LCC-RyR Model**

$\alpha = 0.78133e^{(0.08(V_m-8))}$	E103
$\beta = 0.34319e^{(-0.086676(V_m-8))}$	E104
$\alpha' = a\alpha$	E105
$\beta' = \beta/b$	E106
$y_\infty = \frac{0.75}{\left(1 + e^{\frac{(V_m+25)}{5}}\right)} + 0.25$	*E107
$\tau_y = \frac{500}{\left(1 + e^{\frac{(V_m+28)}{10}}\right)} \times \frac{1}{\left(1 + e^{\frac{-(V_m+42)}{14}}\right)} + 17$	*E108
$k_b = \frac{y_\infty}{\tau_y}$	E109
$k_f = \frac{(1 - y_\infty)}{\tau_y}$	E110
$\lambda_{1,2} = \lambda_{6,7} = \alpha$	E111
$\lambda_{2,1} = \lambda_{7,6} = \beta$	E112
$\lambda_{2,3} = \lambda_{7,8} = f$	E113
$\lambda_{3,2} = \lambda_{8,7} = g$	E114
$\lambda_{1,4} = \lambda_{6,9} = \gamma_0[Ca^{2+}]_{ds}$	E115
$\lambda_{4,1} = \lambda_{9,6} = \omega$	E116
$\lambda_{4,5} = \lambda_{9,10} = \alpha'$	E117
$\lambda_{5,4} = \lambda_{10,9} = \beta'$	E118
$\lambda_{2,5} = \lambda_{7,10} = \alpha\gamma_0[Ca^{2+}]_{ds}$	E119
$\lambda_{5,2} = \lambda_{10,7} = \omega/b$	E120
$\lambda_{1,6} = \lambda_{2,7} = \lambda_{3,8} = \lambda_{4,9} = \lambda_{5,10} = k_f$	E121
$\lambda_{6,1} = \lambda_{7,2} = \lambda_{8,3} = \lambda_{9,4} = \lambda_{10,5} = k_b$	E122
$k_{1,2} = k_0[Ca^{2+}]_{ds}^2$	E123
$k_{2,1} = k_0$	E124

$k_{2,3} = k_{0,2,3}[Ca^{2+}]_{ds}^2$	E125
$k_{3,2} = k_{0,3,2}k_{0,4,3}/(k_{0,3,4}[Ca^{2+}]_{ds}^2 + k_{0,4,3})$	E126
$k_{2,4} = k_{0,2,5}[Ca^{2+}]_{ds}^2$	E127
$k_{4,2} = k_{0,5,2}k_{0,6,5}/(k_{0,5,6}[Ca^{2+}]_{ds}^2 + k_{0,6,5})$	E128
$k_{3,4} = k_{0,4,5}k_{0,3,4}[Ca^{2+}]_{ds}^2/(k_{0,3,4}[Ca^{2+}]_{ds}^2 + k_{0,4,3})$	E129
$k_{4,3} = k_{0,6,5}k_{0,5,4}[Ca^{2+}]_{ds}^2/(k_{0,5,6}[Ca^{2+}]_{ds}^2 + k_{0,6,5})$	E130
$\dot{x}_1 = -(\lambda_{1,2} + \lambda_{1,4}^{(1)} + \lambda_{1,6} + k_{1,2}^{(1)})x_1 + \lambda_{2,1}x_2 + \lambda_{4,1}x_4 + \lambda_{6,1}x_6 + k_{2,1}x_{11}$	E131
$\dot{x}_2 = \lambda_{1,2}x_1 - (\lambda_{2,1} + \lambda_{2,3} + \lambda_{2,5}^{(1)} + \lambda_{2,7} + k_{1,2}^{(1)})x_2 + \lambda_{3,2}x_3 + \lambda_{5,2}x_5 + \lambda_{7,2}x_7$ $+ k_{2,1}x_{12}$	E132
$\dot{x}_3 = \lambda_{2,3}x_2 - (\lambda_{3,2} + \lambda_{3,8} + k_{1,2}^{(2)})x_3 + \lambda_{8,3}x_8 + k_{2,1}x_{13}$	E133
$\dot{x}_4 = \lambda_{1,4}^{(1)}x_1 - (\lambda_{4,1} + \lambda_{4,5} + \lambda_{4,9} + k_{1,2}^{(2)})x_4 + \lambda_{5,4}x_5 + \lambda_{9,4}x_9 + k_{2,1}x_{14}$	E134
$\dot{x}_5 = \lambda_{2,5}^{(1)}x_2 + \lambda_{4,5}x_4 - (\lambda_{5,2} + \lambda_{5,4} + \lambda_{5,10} + k_{1,2}^{(1)})x_5 + \lambda_{10,5}x_{10} + k_{2,1}x_{15}$	E135
$\dot{x}_6 = \lambda_{1,6}x_1 + \lambda_{7,6}x_7 - (\lambda_{6,1} + \lambda_{6,7} + \lambda_{6,9}^{(1)} + k_{1,2}^{(1)})x_6 + \lambda_{9,6}x_9 + k_{2,1}x_{16}$	E136
$\dot{x}_7 = \lambda_{2,7}x_2 + \lambda_{6,7}x_6 - (\lambda_{7,2} + \lambda_{7,6} + \lambda_{7,8} + \lambda_{7,10}^{(1)} + k_{1,2}^{(1)})x_7 + \lambda_{8,7}x_8 + \lambda_{10,7}x_{10}$ $+ k_{2,1}x_{17}$	E137
$\dot{x}_8 = \lambda_{3,8}x_3 + \lambda_{7,8}x_7 - (\lambda_{8,3} + \lambda_{8,7} + k_{1,2}^{(1)})x_8 + k_{2,1}x_{18}$	E138
$\dot{x}_9 = \lambda_{4,9}x_4 + \lambda_{6,9}^{(1)}x_6 - (\lambda_{9,4} + \lambda_{9,6} + \lambda_{9,10} + k_{1,2}^{(1)})x_9 + \lambda_{10,9}x_{10} + k_{2,1}x_{19}$	E139
$\dot{x}_{10} = \lambda_{5,10}x_5 + \lambda_{9,10}x_9 + \lambda_{7,10}^{(1)}x_7 - (\lambda_{10,5} + \lambda_{10,7} + \lambda_{10,9} + k_{1,2}^{(1)})x_{10} + k_{2,1}x_{20}$	E140
$\dot{x}_{11} = k_{1,2}^{(1)}x_1 - (\lambda_{1,2} + \lambda_{1,4}^{(1)} + \lambda_{1,6} + k_{2,1} + k_{2,3}^{(1)} + k_{2,4}^{(1)})x_{11} + \lambda_{2,1}x_{12} + \lambda_{4,1}x_{14}$ $+ \lambda_{6,1}x_{16} + k_{3,2}^{(3)}x_{21} + k_{4,2}^{(1)}x_{31}$	E141
$\dot{x}_{12} = k_{1,2}^{(1)}x_2 - (\lambda_{2,1} + \lambda_{2,3} + \lambda_{2,5}^{(1)} + \lambda_{2,7} + k_{2,1} + k_{2,3}^{(1)} + k_{2,4}^{(1)})x_{12} + \lambda_{3,2}x_{13} + \lambda_{5,2}x_{15}$ $+ \lambda_{7,2}x_{17} + k_{4,2}^{(1)}x_{32} + k_{3,2}^{(3)}x_{22}$	E142
$\dot{x}_{13} = k_{1,2}^{(2)}x_3 + \lambda_{2,3}x_{12} - (\lambda_{3,2} + \lambda_{3,8} + k_{2,1} + k_{2,3}^{(2)} + k_{2,4}^{(2)})x_{13}$ $+ \lambda_{8,3}x_{18} + k_{4,2}^{(2)}x_{33} + k_{3,2}^{(4)}x_{23}$	E143
$\dot{x}_{14} = k_{1,2}^{(2)}x_4 + \lambda_{1,4}^{(1)}x_{11} - (\lambda_{4,1} + \lambda_{4,5} + \lambda_{4,9} + k_{2,1} + k_{2,3}^{(1)} + k_{2,4}^{(1)})x_{14}$ $+ \lambda_{5,4}x_{15} + \lambda_{9,4}x_{19} + k_{4,2}^{(1)}x_{34} + k_{3,2}^{(3)}x_{24}$	E144

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$$\begin{aligned}\dot{x}_{15} &= k_{1,2}^{(1)}x_5 + \lambda_{2,5}^{(1)}x_{12} + \lambda_{4,5}x_{14} \\ &\quad - \left( \lambda_{5,2} + \lambda_{5,4} + \lambda_{5,10} + k_{2,1} + k_{2,3}^{(1)} + k_{2,4}^{(1)} \right) x_{15} + \lambda_{10,5}x_{20} \\ &\quad + k_{4,2}^{(1)}x_{35} + k_{3,2}^{(3)}x_{25}\end{aligned}\tag{E145}$$


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$$\begin{aligned}\dot{x}_{16} &= k_{1,2}^{(1)}x_6 + \lambda_{1,6}x_{11} \\ &\quad - \left( \lambda_{6,1} + \lambda_{6,7} + \lambda_{6,9}^{(1)} + k_{2,1} + k_{2,3}^{(1)} + k_{2,4}^{(1)} \right) x_{16} + \lambda_{7,6}x_{17} + \lambda_{9,6}x_{19} \\ &\quad + k_{4,2}^{(1)}x_{36} + k_{3,2}^{(3)}x_{26}\end{aligned}\tag{E146}$$


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$$\begin{aligned}\dot{x}_{17} &= k_{1,2}^{(1)}x_7 + \lambda_{2,7}x_{12} + \lambda_{6,7}x_{16} \\ &\quad - \left( \lambda_{7,2} + \lambda_{7,6} + \lambda_{7,8} + \lambda_{7,10}^{(1)} + k_{2,1} + k_{2,3}^{(1)} + k_{2,4}^{(1)} \right) x_{17} + \lambda_{8,7}x_{18} \\ &\quad + \lambda_{10,7}x_{20} + k_{4,2}^{(1)}x_{37} + k_{3,2}^{(3)}x_{27}\end{aligned}\tag{E147}$$


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$$\begin{aligned}\dot{x}_{18} &= k_{1,2}^{(1)}x_8 + \lambda_{3,8}x_{13} + \lambda_{7,8}x_{17} - \left( \lambda_{8,3} + \lambda_{8,7} + k_{2,1} + k_{2,3}^{(1)} + \right. \\ &\quad \left. k_{2,4}^{(1)} \right) x_{18} + k_{4,2}^{(1)}x_{38} + k_{3,2}^{(3)}x_{28}\end{aligned}\tag{E148}$$


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$$\begin{aligned}\dot{x}_{19} &= k_{1,2}^{(1)}x_9 + \lambda_{4,9}x_{14} + \lambda_{6,9}^{(1)}x_{16} \\ &\quad - \left( \lambda_{9,4} + \lambda_{9,6} + \lambda_{9,10} + k_{2,1} + k_{2,3}^{(1)} + k_{2,4}^{(1)} \right) x_{19} + \lambda_{10,9}x_{20} \\ &\quad + k_{4,2}^{(1)}x_{39} + k_{3,2}^{(3)}x_{29}\end{aligned}\tag{E149}$$


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$$\begin{aligned}\dot{x}_{20} &= k_{1,2}^{(1)}x_{10} + \lambda_{5,10}x_{15} + \lambda_{7,10}^{(1)}x_{17} + \lambda_{9,10}x_{19} \\ &\quad - \left( \lambda_{10,5} + \lambda_{10,7} + \lambda_{10,9} + k_{2,1} + k_{2,3}^{(1)} + k_{2,4}^{(1)} \right) x_{20} + k_{4,2}^{(1)}x_{40} + k_{3,2}^{(3)}x_{30}\end{aligned}\tag{E150}$$


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$$\begin{aligned}\dot{x}_{21} &= k_{2,3}^{(1)}x_{11} - \left( \lambda_{1,2} + \lambda_{1,4}^{(3)} + \lambda_{1,6} + k_{3,2}^{(3)} + k_{3,4}^{(3)} \right) x_{21} + \lambda_{2,1}x_{22} + \lambda_{4,1}x_{24} + \lambda_{6,1}x_{26} \\ &\quad + k_{4,3}^{(1)}x_{31}\end{aligned}\tag{E151}$$


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$$\begin{aligned}\dot{x}_{22} &= k_{2,3}^{(1)}x_{12} + \lambda_{1,2}x_{21} - \left( \lambda_{2,1} + \lambda_{2,3} + \lambda_{2,5}^{(3)} + \lambda_{2,7} + k_{3,2}^{(3)} + k_{3,4}^{(3)} \right) x_{22} + \lambda_{3,2}x_{23} \\ &\quad + \lambda_{5,2}x_{25} + \lambda_{7,2}x_{27} + k_{4,3}^{(1)}x_{32}\end{aligned}\tag{E152}$$


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$$\dot{x}_{23} = k_{2,3}^{(2)}x_{13} + \lambda_{2,3}x_{22} - \left( \lambda_{3,2} + \lambda_{3,8} + k_{3,2}^{(4)} + k_{3,4}^{(4)} \right) x_{23} + \lambda_{8,3}x_{28} + k_{4,3}^{(2)}x_{33}\tag{E153}$$


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$$\begin{aligned}\dot{x}_{24} &= k_{2,3}^{(1)}x_{14} + \lambda_{1,4}^{(3)}x_{21} - \left( \lambda_{4,1} + \lambda_{4,5} + \lambda_{4,9} + k_{3,2}^{(3)} + k_{3,4}^{(3)} \right) x_{24} + \lambda_{5,4}x_{25} + \lambda_{9,4}x_{29} + \\ &\quad k_{4,3}^{(1)}x_{34}\end{aligned}\tag{E154}$$


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$$\begin{aligned}\dot{x}_{25} &= k_{2,3}^{(1)}x_{15} + \lambda_{2,5}^{(3)}x_{22} + \lambda_{4,5}x_{24} - \left( \lambda_{5,2} + \lambda_{5,4} + \lambda_{5,10} + k_{3,2}^{(3)} + \right. \\ &\quad \left. k_{3,4}^{(3)} \right) x_{25} + \lambda_{10,5}x_{30} + k_{4,3}^{(1)}x_{35}\end{aligned}\tag{E155}$$


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$$\dot{x}_{26} = k_{2,3}^{(1)}x_{16} + \lambda_{1,6}x_{21} - \left(\lambda_{6,1} + \lambda_{6,7} + \lambda_{6,9}^{(3)} + k_{3,2}^{(3)} + k_{3,4}^{(3)}\right)x_{26} + \lambda_{7,6}x_{27} + \lambda_{9,6}x_{29} + k_{4,3}^{(1)}x_{36}$$

E156

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$$\dot{x}_{27} = k_{2,3}^{(1)}x_{17} + \lambda_{2,7}x_{22} + \lambda_{6,7}x_{26} - \left(\lambda_{7,2} + \lambda_{7,6} + \lambda_{7,8} + \lambda_{7,10}^{(3)} + k_{3,2}^{(3)} + k_{3,4}^{(3)}\right)x_{27} + \lambda_{8,7}x_{28} + \lambda_{10,7}x_{30} + k_{4,3}^{(1)}x_{37}$$

E157

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$$\dot{x}_{28} = k_{2,3}^{(1)}x_{18} + \lambda_{3,8}x_{23} + \lambda_{7,8}x_{27} - \left(\lambda_{8,3} + \lambda_{8,7} + k_{3,2}^{(3)} + k_{3,4}^{(3)}\right)x_{28} + k_{4,3}^{(1)}x_{38}$$

E158

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$$\dot{x}_{29} = k_{2,3}^{(1)}x_{19} + \lambda_{4,9}x_{24} + \lambda_{6,9}^{(1)}x_{26} - \left(\lambda_{9,4} + \lambda_{9,6} + \lambda_{9,10} + k_{3,2}^{(3)} + k_{3,4}^{(3)}\right)x_{29} + \lambda_{10,9}x_{30} + k_{4,3}^{(1)}x_{39}$$

E159

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$$\dot{x}_{30} = k_{2,3}^{(1)}x_{20} + \lambda_{5,10}x_{25} + \lambda_{7,10}^{(3)}x_{27} + \lambda_{9,10}x_{29} - \left(\lambda_{10,5} + \lambda_{10,7} + \lambda_{10,9} + k_{3,2}^{(3)} + k_{3,4}^{(3)}\right)x_{30} + k_{4,3}^{(1)}x_{40}$$

E160

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$$\dot{x}_{31} = k_{2,4}^{(1)}x_{11} + k_{3,4}^{(3)}x_{21} - \left(\lambda_{1,2} + \lambda_{1,4}^{(1)} + \lambda_{1,6} + k_{4,2}^{(1)} + k_{4,3}^{(1)}\right)x_{31} + \lambda_{2,1}x_{32} + \lambda_{4,1}x_{34} + \lambda_{6,1}x_{36}$$

E161

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$$\dot{x}_{32} = k_{2,4}^{(1)}x_{12} + k_{3,4}^{(3)}x_{22} + \lambda_{1,2}x_{31} - \left(\lambda_{2,1} + \lambda_{2,3} + \lambda_{2,5}^{(1)} + \lambda_{2,7} + k_{4,2}^{(1)} + k_{4,3}^{(1)}\right)x_{32} + \lambda_{3,2}x_{33} + \lambda_{5,2}x_{35} + \lambda_{7,2}x_{37}$$

E162

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$$\dot{x}_{33} = k_{2,4}^{(2)}x_{13} + k_{3,4}^{(3)}x_{23} + \lambda_{2,3}x_{32} - \left(\lambda_{3,2} + \lambda_{3,8} + k_{4,2}^{(2)} + k_{4,3}^{(2)}\right)x_{33} + \lambda_{8,3}x_{38}$$

E163

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$$\dot{x}_{34} = k_{2,4}^{(1)}x_{14} + k_{3,4}^{(3)}x_{24} + \lambda_{1,4}^{(1)}x_{31} - \left(\lambda_{4,1} + \lambda_{4,5} + \lambda_{4,9} + k_{4,2}^{(1)} + k_{4,3}^{(1)}\right)x_{34} + \lambda_{5,4}x_{35} + \lambda_{9,4}x_{39}$$

E164

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$$\dot{x}_{35} = k_{2,4}^{(1)}x_{15} + k_{3,4}^{(3)}x_{25} + \lambda_{2,5}^{(1)}x_{32} + \lambda_{4,5}x_{34} - \left(\lambda_{5,2} + \lambda_{5,4} + \lambda_{5,10} + k_{4,2}^{(1)} + k_{4,3}^{(1)}\right)x_{35} + \lambda_{10,5}x_{40}$$

E165

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$$\dot{x}_{36} = k_{2,4}^{(1)}x_{16} + k_{3,4}^{(3)}x_{26} + \lambda_{1,6}x_{31} - \left(\lambda_{6,1} + \lambda_{6,7} + \lambda_{6,9}^{(1)} + k_{4,2}^{(1)} + k_{4,3}^{(1)}\right)x_{36} + \lambda_{7,6}x_{37} + \lambda_{9,6}x_{39}$$

E166

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$$\dot{x}_{37} = k_{2,4}^{(1)}x_{17} + k_{3,4}^{(3)}x_{27} + \lambda_{2,7}x_{32} + \lambda_{6,7}x_{36} - \left(\lambda_{7,2} + \lambda_{7,6} + \lambda_{7,8} + \lambda_{7,10}^{(1)} + k_{4,2}^{(1)} + k_{4,3}^{(1)}\right)x_{37} + \lambda_{10,7}x_{40}$$

E167

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$$\dot{x}_{38} = k_{2,4}^{(1)}x_{18} + k_{3,4}^{(3)}x_{28} + \lambda_{3,8}x_{33} + \lambda_{7,8}x_{37} - \left(\lambda_{8,3} + \lambda_{8,7} + k_{4,2}^{(1)} + k_{4,3}^{(1)}\right)x_{38}$$

E168

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$$\dot{x}_{39} = k_{2,4}^{(1)}x_{19} + k_{3,4}^{(3)}x_{29} + \lambda_{4,9}x_{34} + \lambda_{6,9}^{(1)}x_{36} - \left(\lambda_{9,4} + \lambda_{9,6} + \lambda_{9,10} + k_{4,2}^{(1)} + k_{4,3}^{(1)}\right)x_{39} + \lambda_{10,9}x_{40}$$

E169

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$$\dot{x}_{40} = k_{2,4}^{(1)}x_{20} + k_{3,4}^{(3)}x_{30} + \lambda_{5,10}x_{35} + \lambda_{7,10}^{(3)}x_{37} + \lambda_{9,10}x_{39} - (\lambda_{10,5} + \lambda_{10,7} + \lambda_{10,9} + k_{4,2}^{(1)} + k_{4,3}^{(1)})x_{40}$$
E170


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$$p_{(1)} = x_1 + x_2 + x_4 + x_5 + x_6 + x_7 + x_8 + x_9 + x_{10} + x_{11} + x_{12} + x_{14} + x_{15} + x_{16} + x_{17} + x_{18} + x_{19} + x_{20} + x_{31} + x_{32} + x_{33} + x_{34} + x_{35} + x_{36} + x_{37} + x_{38} + x_{39} + x_{40}$$
E171


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$$P_{(2)} = x_3 + x_{13} + x_{33}$$
E172


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$$P_{(3)} = x_{21} + x_{22} + x_{24} + x_{25} + x_{26} + x_{27} + x_{28} + x_{29} + x_{30}$$
E173


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$$P_{(4)} = x_{23}$$
E174


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The notation  $\lambda_{i,j}$  is used to denote the transition rate from state  $i$  to state  $j$  for the LCC. The notation  $k_{ij}$  is used to denote the transition rate from state  $i$  to state  $j$  for the RyR.  $x_i$  denotes  $i^{\text{th}}$  state,  $\dot{x}_i$  denotes the time derivative of the  $i^{\text{th}}$  state.  $P_{(n)}$  denotes the probability that a CaRU is in the  $n^{\text{th}}$  ( $n=1,2,3,4$ ) open-closed configuration. \* The equations are modified to provide better fit of  $I_{\text{CaL}}$  to experimental data <sup>3</sup>. LCC: L-type  $\text{Ca}^{2+}$  channel, RyR: ryanodine receptor, CaRU:  $\text{Ca}^{2+}$  release unit.

#### Whole-cell $\text{Ca}^{2+}$ flux through the LCCs ( $J_{\text{LCC}}$ )

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$$J_{\text{LCC}} = N_{\text{CaRU}} J_L \frac{V_m}{V_m} \frac{(p_{(2)}([Ca^{2+}]_{dm}^{(2)} e^{-V_m/0.34} [Ca^{2+}]_0) + p_{(4)}([Ca^{2+}]_{dm}^{(4)} e^{-V_m/0.34} [Ca^{2+}]_0))}{1 e^{-V_m}}$$
E175


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#### Whole-cell $\text{Ca}^{2+}$ release through the RyRs ( $J_{\text{rel}}$ )

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$$J_{\text{rel}} = N_{\text{CaRU}} r_{\text{RyR}} (p_{(3)}([Ca^{2+}]_{\text{JSR}} [Ca^{2+}]_{dm}^{(3)}) + p_{(4)}([Ca^{2+}]_{\text{JSR}} [Ca^{2+}]_{dm}^{(4)}))$$
E176


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#### The $\text{Ca}^{2+}$ flux diffused from the dyadic microdomain (dm) to the cytoplasm ( $J_{\text{xfer}}$ )

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$$J_{\text{xfer}} = N_{\text{CaRU}} r_{\text{xfer}} \sum_{i=1}^4 p_{(i)} ([Ca^{2+}]_{dm}^{(i)} - [Ca^{2+}]_i)$$
E177


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**Table S3. Sarcoplasmic Reticulum (SR) Ca<sup>2+</sup> dynamics**

SR Ca<sup>2+</sup> model equations

$J_{\text{JSR}} = 1 + \frac{K_m^{\text{CSQN}} [\text{CSQN}]_{\text{tot}}}{\left(K_m^{\text{CSQN}} + [\text{Ca}^{2+}]_{\text{JSR}}\right)^2}$	E178
$J_{\text{NSR}} = 1 + \frac{K_m^{\text{CSQN}} [\text{CSQN}]_{\text{tot}}}{\left(K_m^{\text{CSQN}} + [\text{Ca}^{2+}]_{\text{NSR}}\right)^2}$	E179
$i = 1 + \frac{K_m^{\text{CMDN}} [\text{CMDN}]_{\text{tot}}}{\left(K_m^{\text{CMDN}} + [\text{Ca}^{2+}]_i\right)^2}$	E180
$J_{\text{trpn}} = \frac{d[\text{HTRPNCa}]}{dt} + \frac{d[\text{LTRPNCa}]}{dt}$	E181
$J_{\text{tr}} = \frac{[\text{Ca}^{2+}]_{\text{NSR}} - [\text{Ca}^{2+}]_{\text{JSR}}}{\tau}$	E182
$J_{\text{up}} = \frac{V_{\text{max}f} f_b - V_{\text{max}r} r_b}{1 + f_b + r_b} f_{\text{ATP}}^{\text{SERCA}}$	E183
$f_b = \frac{[\text{Ca}^{2+}]_i^{\text{Nfb}}}{K_{fb}}$	E184
$r_b = \frac{[\text{Ca}^{2+}]_{\text{SR}}^{\text{Nrb}}}{K_{rb}}$	E185
$f_{\text{ATP}}^{\text{SERCA}} = \frac{K_{m,\text{up}}^{\text{ATP}}}{[\text{ATP}]_i} \cdot \frac{1}{1 + \frac{[\text{ADP}]_i}{K_{i,\text{up}}}} + \frac{1}{1 + \frac{[\text{ADP}]_i}{K'_{i,\text{up}}}}$	E186
$\frac{d[\text{LTRPNCa}]}{dt} = k_{\text{trpn}}^+ [\text{Ca}^{2+}]_i \left( [\text{LTRPN}]_{\text{tot}} - [\text{LTRPNCa}] \right)$	E187
$k_{\text{trpn}} = 1 - \frac{2}{3} \text{Force}_{\text{Norm}} [\text{LTRPNCa}]$	

$$\frac{d[\text{HTRPNCa}]}{dt} = k_{\text{htprn}}^+ [\text{Ca}^{2+}]_i ([\text{HTRPN}]_{\text{tot}} - [\text{HTRPNCa}]) - k_{\text{htprn}} [\text{HTRPNCa}] \quad \text{E188}$$

$$\frac{d[\text{Ca}^{2+}]_i}{dt} = J_{\text{xfer}} - J_{\text{up}} - J_{\text{trpn}} - (I_{\text{Ca,b}} - 2 I_{\text{NaCa}} + I_{\text{pCa}}) \frac{A_{\text{cap}}}{2V_{\text{myo}}F} + (V_{\text{NaCa}} - V_{\text{uni}}) \frac{V_{\text{mito}}}{V_{\text{myo}}} \quad \text{E189}$$

$$\frac{d[\text{Ca}^{2+}]_{\text{NSR}}}{dt} = \frac{V_{\text{myo}}}{V_{\text{NSR}}} (J_{\text{up}} - J_{\text{tr}}) \quad \text{E190}$$

$$\frac{d[\text{Ca}^{2+}]_{\text{JSR}}}{dt} = \frac{V_{\text{NSR}}}{V_{\text{JSR}}} J_{\text{tr}} - \frac{V_{\text{SS}}}{V_{\text{JSR}}} J_{\text{rel}} \quad \text{E191}$$

### SR Ca<sup>2+</sup> model parameters

Symbol	Value	Units	Description	Ref.
$V_{\text{NSR}}$	1.4	pL	NSR volume	4
$V_{\text{JSR}}$	0.16	pL	JSR volume	4
$K_m^{\text{CSQN}}$	0.8	mM	Ca <sup>2+</sup> half saturation constant for calsequestrin	4
$K_m^{\text{CMDN}}$	$2.38 \times 10^{-3}$	mM	Ca <sup>2+</sup> half saturation constant for calmodulin	4
$k_{\text{htprn}}^+$	20	$\text{mM}^{-1} \text{ms}^{-1}$	Ca <sup>2+</sup> on-rate for troponin high affinity sites	5
$k_{\text{htprn}}$	$3.3 \times 10^{-4}$	$\text{ms}^{-1}$	Ca <sup>2+</sup> off-rate for troponin high affinity sites	4
$k_{\text{ltrpn}}^+$	40	$\text{mM}^{-1} \text{ms}^{-1}$	Ca <sup>2+</sup> on-rate for troponin low affinity sites	5
$k_{\text{ltrpn}}$	$4 \times 10^{-2}$	$\text{ms}^{-1}$	Ca <sup>2+</sup> off-rate for troponin low affinity sites	4
$[\text{HTRPN}]_{\text{tot}}$	0.14	mM	Total troponin high-affinity sites	4
$[\text{LTRPN}]_{\text{tot}}$	0.07	mM	Total troponin low-affinity sites	4
$[\text{CMDN}]_{\text{tot}}$	$5.0 \times 10^{-2}$	mM	Total myoplasmic calmodulin concentration	4
$[\text{CSQN}]_{\text{tot}}$	5	mM	Total SR calsequestrin concentration	*
$t_r$	0.5747	ms	Time constant for transfer from NSR to JSR	4

$J_{RyR\_max}$	16.6	$ms^{-1}$	RyR flux channel constant	*
$N_{CaRU}$	300000		Number of $Ca^{2+}$ release units	*
$V_{max,f}$	$2.989 \times 10^{-4}$	$ms^{-1}$	SERCA forward rate parameter	4
$V_{max,r}$	$3.979 \times 10^{-4}$	$ms^{-1}$	SERCA reverse rate parameter	4
$K_{fb}$	$1.5 \times 10^{-4}$	mM	Forward $Ca^{2+}$ half saturation constant of SERCA	**
$K_{rb}$	3.3	mM	Reverse $Ca^{2+}$ half saturation constant of SERCA	**
$N_{fb}$	0.5		Forward cooperativity constant of SERCA	**
$N_{rb}$	0.5		Reverse cooperativity constant of SERCA	**
$K_{m,up}^{ATP}$	0.01	mM	ATP half saturation constant for SERCA	4
$K_{i,up}$	0.1	mM	ADP first inhibition constant for SERCA	4
$K'_{i,up}$	1	mM	ADP second inhibition constant for SERCA	4

\* These parameters were adjusted to achieve a ~37% of SR  $Ca^{2+}$  depletion during a normal AP cycle.

\*\*These parameters were adjusted to maintain  $[Ca^{2+}]_{NSR}$  at 0.45mM<sup>6-8</sup> while avoiding net reverse SERCA flux.

#### Effect of ROS on RyR open probability and SR $Ca^{2+}$ release

$$\begin{aligned}
 J_{rel\_ROS} &= N_{CaRU} r_{RyR} (p_{(3)\_ROS} ([Ca^{2+}]_{SR} - [Ca^{2+}]_{dm}^{(3)}) + p_{(4)\_ROS} ([Ca^{2+}]_{SR} - [Ca^{2+}]_{dm}^{(4)})) \\
 &= N_{CaRU} r_{RyR} \frac{P_{O\_ryr\_ROS}}{P_{O\_ryr}} \left( p_{(3)} ([Ca^{2+}]_{SR} - [Ca^{2+}]_{dm}^{(3)}) + p_{(4)} ([Ca^{2+}]_{SR} - [Ca^{2+}]_{dm}^{(4)}) \right)
 \end{aligned}
 \tag{E192}$$

where  $\frac{P_{Oryr\_ROS}}{P_{Oryr}}$  is the ROS-dependent scaling factor of RyR opening probability.

#### **Table S4. CaMKII Activation Module**

Transition rate expression ( $ms^{-1}$ )

$$ItoB = k_{asso} \times [CaMCA4] \tag{E193}$$



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$$AtoP = k_{asso} \times [CaMCa4] \quad E194$$

---

$$OxAtOxP = k_{asso} \times [CaMCa4] \quad E195$$

---

$$BtoI = k_{disso} \times \left(1 - \frac{K_{m,CaM}^3}{[[Ca^{2+}]_i^3 + K_{m,CaM}^3]}\right) + k_{dissoCa} \times \frac{K_{m,CaM}^3}{[Ca^{2+}]_i^3 + K_{m,CaM}^3} \quad E196$$

---

$$PtoA = k_{disso2} \times \left(1 - \frac{K_{m,CaM}^3}{[Ca^{2+}]_i^3 + K_{m,CaM}^3}\right) + k_{dissoCa2} \times \frac{K_{m,CaM}^3}{[Ca^{2+}]_i^3 + K_{m,CaM}^3} \quad E197$$

---

$$OxPtoOxA = k_{disso2} \times \left(1 - \frac{K_{m,CaM}^3}{[Ca^{2+}]_i^3 + K_{m,CaM}^3}\right) + k_{dissoCa2} \times \frac{K_{m,CaM}^3}{[Ca^{2+}]_i^3 + K_{m,CaM}^3} \quad E198$$

---

$$BtoP = k_{cat} \times \left[1 - \left(\frac{[I]}{[CaMKII_{total}]}\right)^2\right] \times \frac{[ATP]}{[ATP] + K_{m,ATP}} \quad E199$$

---

$$OxBtoOxP = k_{cat} \times \left[1 - \left(\frac{[I]}{[CaMKII_{total}]}\right)^2\right] \times \frac{[ATP]}{[ATP] + K_{m,ATP}} \quad E200$$

---

$$PtoB = k_{cat,PP1} \times \frac{1}{[P] + K_{m,PP1}} \times [PP1] \quad E201$$

---

$$OxPtoOxB = k_{cat,PP1} \times \frac{1}{[OxP] + K_{m,PP1}} \times [PP1] \quad E202$$

---

$$BtoOxB = k_{ox} \times [ROS]_i \quad E203$$

---

$$BtoOxP = k_{ox} \times [ROS]_i \quad E204$$

---

$$AtoOxA = k_{ox} \times [ROS]_i \quad E205$$

---

## CaMKII Activation Balance Equations

$\frac{d[CaM Ca]}{dt} = k_1 \times [Ca^{2+}]_i \times [CaM] + k_{-2} \times [CaM Ca2] - k_{-1} \times [CaM Ca] - k_2 \times [Ca^{2+}]_i \times [CaM Ca]$	E206
$\frac{d[CaM Ca2]}{dt} = k_2 \times [Ca^{2+}]_i \times [CaCaM] + k_{-3} \times [CaM Ca3] - k_{-2} \times [CaM Ca2] - k_3 \times [Ca^{2+}]_i \times [CaM Ca2]$	E207
$\frac{d[CaM Ca3]}{dt} = k_3 \times [Ca^{2+}]_i \times [CaCaM2] + k_{-4} \times [CaM Ca4] - k_{-3} \times [CaM Ca3] - k_4 \times [Ca^{2+}]_i \times [CaM Ca3]$	E208
$\frac{d[CaM Ca4]}{dt} = k_4 \times [Ca^{2+}]_i \times [CaCaM3] - k_{-4} \times [CaM Ca4]$	E209
$\frac{d[B]}{dt} = ItoB \times [I] + PtoB \times [P] + OxBtoB \times [OxB] - (BtoI + BtoP + BtoOxB) \times [B]$	E210
$\frac{d[P]}{dt} = BtoP \times [B] + AtoP \times [A] + OxPtoP \times [OxP] - (PtoB + PtoA + PtoOxP) \times [P]$	E211
$\frac{d[A]}{dt} = PtoA \times [P] + OxAtoA \times [OxA] - (AtoI + AtoP + AtoOxA) \times [A]$	E212
$\frac{d[OxB]}{dt} = BtoOxB \times [B] + OxPtoOxB \times [OxP] - (OxBtoB + OxBtoOxP) \times [OxB]$	E213
$\frac{d[OxA]}{dt} = AtoOxA \times [A] + OxPtoOxA \times [OxP] - (OxAtoA + OxAtoOxP) \times [OxA]$	E214
$\frac{d[OxP]}{dt} = OxBtoOxP \times [OxB] + PtoOxP \times [P] + OxAtoOxP \times [OxA] - (OxPtoOxB + OxPtoP + OxPtoOxA) \times [OxP]$	E215
$[CaM] = [CaM_{total}] - [CaM Ca] - [CaM Ca2] - [CaM Ca3] - [CaM Ca4]$	E216
$[CaMKII_{active}] = [CaMKII_{total}] - [B] - [P] - [A] - [OxA] - [OxP] - [OxB]$	E217

$$CaMKII_{active} = \frac{[CaMKII_{active}]}{[CaMKII_{total}]} \times 100\%$$

where  $CaMKII_{active}$  represents the percentage of activated CaMKII.

**Table S5. Ionic concentrations balance equations**

$$\frac{d[Ca^{2+}]_m}{dt} = (V_{uni} - V_{NaCa}) \quad E219$$

$$\frac{d[Na^+]_i}{dt} = (I_{Na} + I_{Na,L} + I_{Na,b} + I_{ns,Na} + 3I_{NaCa} + 3I_{NaK}) \frac{A_{cap}}{V_{myo}F} \quad E220$$

$$\frac{d[K^+]_i}{dt} = - (I_K + I_{K_1} + I_{Kp} + I_{ns,K} + I_{Ca,K} - 2 I_{NaK}) \frac{A_{cap}}{V_{myo}F} \quad E221$$

**Table S6. Force generation model <sup>5</sup>**

$$\frac{d[P_0]}{dt} = (k_{pn}^{trop} + f_{01}) [P_0] + k_{np}^{trop} [N_0] + g_{01}(SL) [P_1] \quad E222$$

$$\frac{d[P_2]}{dt} = (f_{23} + g_{12}(SL)) [P_2] + f_{12} [P_1] + g_{23}(SL) [P_3] \quad E224$$

$$\frac{d[P_3]}{dt} = g_{23}(SL) [P_3] + f_{23} [P_2] \quad E225$$

$$\frac{d[N_1]}{dt} = k_{pn}^{trop} [P_1] + (k_{np}^{trop} + g'_{01}(SL)) [N_1] \quad E226$$

$$\frac{d[N_0]}{dt} = \frac{d[N_1]}{dt} + \frac{d[P_0]}{dt} + \frac{d[P_1]}{dt} + \frac{d[P_2]}{dt} + \frac{d[P_3]}{dt} \quad E227$$

$f_{01} = 3 \cdot f_{XB}$	E228
$f_{12} = 10 \cdot f_{XB}$	E229
$f_{23} = 7 \cdot f_{XB}$	E230
$g_{01} = 1 \cdot g_{XB}^{\min}$	E231
$g_{12} = 2 \cdot g_{XB}^{\min}$	E232
$g_{23} = 3 \cdot g_{XB}^{\min}$	E233
$g_{01}(SL) = 1 \cdot g_{XB}^{\min}$	E234
$g_{12}(SL) = 2 \cdot g_{XB}^{\min}$	E235
$g_{23}(SL) = 3 \cdot g_{XB}^{\min}$	E236
$= 1 + \frac{2.3 - SL}{(2.3 - 1.7)^{1.6}}$	E237
$k_{np}^{\text{trop}} = k_{pn}^{\text{trop}} \frac{[\text{LTRPNCa}] N^{\text{trop}}}{K_{1/2}^{\text{trop}} [\text{LTRPN}]_{\text{tot}}}$	E238
	1
$K_{1/2}^{\text{trop}} = 1 + \frac{K_{Ca}^{\text{trop}}}{1.7 \cdot 10^{-3} - 0.8 \cdot 10^{-3} \frac{(SL - 1.7)}{0.6}}$	E239
$N^{\text{trop}} = 3.5 \cdot SL - 2.0$	E240
$K_{Ca}^{\text{trop}} = \frac{k_{\text{ltrpn}}}{k_{\text{ltrpn}}^+}$	E241
$\text{PATHS} = g_{01} g_{12} g_{23} + f_{01} g_{12} g_{23} + f_{01} f_{12} g_{23} + f_{01} f_{12} f_{23}$	E242
$PI_{\max} = \frac{f_{01} g_{12} g_{23}}{\text{PATHS}}$	E243

$$P2_{\max} = \frac{f_{01} f_{12} g_{23}}{\text{PATHS}} \quad \text{E244}$$

$$P3_{\max} = \frac{f_{01} f_{12} f_{23}}{\text{PATHS}} \quad \text{E245}$$

$$\text{Force} = \frac{P_1 + N_1 + 2 P_2 + 3 P_3}{P1_{\max} + 2 P2_{\max} + 3 P3_{\max}} \quad \text{E246}$$

$$\text{Force}_{\text{Norm}} = \frac{P_1 + N_1 + P_2 + P_3}{P1_{\max} + P2_{\max} + P3_{\max}} \quad \text{E247}$$

$$V_{\text{AM}} = V_{\text{AM}}^{\max} \frac{f_{01} [P_0] + f_{12} [P_1] + f_{23} [P_2]}{f_{01} + f_{12} + f_{23}} \cdot \frac{1}{1 + \frac{K_{M,AM}^{\text{ATP}}}{[ATP]_i}} \frac{1}{1 + \frac{[ADP]_i}{K_{i,AM}}} \quad \text{E248}$$

**Table S7. Mitochondrial membrane potential ( $\Delta\Psi_m$ )**

$$\frac{d \Psi_m}{dt} = \frac{V_{\text{He}} + V_{\text{He(F)}} - V_{\text{Hu}} - V_{\text{ANT}} - V_{\text{HLeak}} - V_{\text{NaCa}} - 2 V_{\text{uni}} - V_{\text{IMAC}}}{C_{\text{mito}}} \quad \text{E249}$$

**Table S8. Energy metabolism system**

Mitochondrial metabolites balance equations

$$\frac{d [ATP]_i}{dt} = V_{\text{ANT}} \frac{V_{\text{mito}}}{V_{\text{myo}}} - V_{\text{CK}}^{\text{mito}} - V_{\text{AM}} - \frac{1}{2} J_{\text{up}} - (I_{\text{pCa}} + I_{\text{NaK}}) \frac{A_{\text{cap}}}{V_{\text{myo}} F} \quad \text{E250}$$

$$\frac{d [ATP]_{\text{ic}}}{dt} = -V_{\text{CK}}^{\text{cyto}} - V_{\text{ATPase}}^{\text{cyto}} \quad \text{E251}$$

$\frac{d [\text{CrP}]_i}{dt} = V_{\text{CK}}^{\text{mito}} - V_{\text{tr}}^{\text{CrP}}$	E252
$\frac{d [\text{CrP}]_{\text{ic}}}{dt} = V_{\text{tr}}^{\text{CrP}} + V_{\text{CK}}^{\text{cyto}}$	E253
$\frac{d [\text{ADP}]_m}{dt} = V_{\text{ANT}} - V_{\text{ATPase}} - V_{\text{SL}}$	E254
$[\text{ATP}]_m = C_A - [\text{ADP}]_m$	E255
$\frac{d[\text{NADH}]}{dt} = - V_{\text{O}_2} + V_{\text{IDH}} + V_{\text{KGDH}} + V_{\text{MDH}}$	E256
$\frac{d[\text{ISOC}]}{dt} = V_{\text{ACO}} - V_{\text{IDH}}$	E257
$\frac{d[\text{KG}]}{dt} = V_{\text{IDH}} - V_{\text{KGDH}} + V_{\text{AAT}}$	E258
$\frac{d[\text{SCoA}]}{dt} = V_{\text{KGDH}} - V_{\text{SL}}$	E259
$\frac{d[\text{Suc}]}{dt} = V_{\text{SL}} - V_{\text{SDH}}$	E260
$\frac{d[\text{FUM}]}{dt} = V_{\text{SDH}} - V_{\text{FH}}$	E261
$\frac{d[\text{MAL}]}{dt} = V_{\text{FH}} - V_{\text{MDH}}$	E262
$\frac{d[\text{OAA}]}{dt} = V_{\text{MDH}} - V_{\text{CS}} - V_{\text{AAT}}$	E263
$[\text{CIT}] = C_{\text{Kint}} - \frac{[\text{ISOC}] + [\text{KG}] + [\text{SCoA}] + [\text{Suc}]}{+ [\text{FUM}] + [\text{MAL}] + [\text{OAA}]}$	E264

### Cytosolic metabolic reaction rate

$V_{ANT} = V_{\max ANT} \frac{0.75 \left( 1 - \frac{0.25 [ATP]_i \cdot 0.45 [ADP]_m}{0.17 [ADP]_i \cdot 0.025 [ATP]_m} e^{\frac{F}{RT} m} \right)}{1 + \frac{0.25 [ATP]_i}{0.225 [ADP]_i} e^{\frac{-h^{ANT} F}{RT} m} + 1 + \frac{0.45 [ADP]_m}{0.025 [ATP]_m}}$	E265
$V_{CK}^{cyto} = k_{CK}^{cyto} [ATP]_{ic} [Cr]_{ic} - \frac{[ADP]_{ic} [CrP]_{ic}}{K_{EQ}}$	E266
$V_{CK}^{mito} = k_{CK}^{mito} [ATP]_i [Cr]_i - \frac{[ADP]_i [CrP]_i}{K_{EQ}}$	E267
$V_{tr}^{CrP} = k_{tr}^{Cr} ([CrP]_i - [CrP]_{ic})$	E268

### Tricarboxylic acid cycle reaction rate

$V_{CS} = k_{cat}^{CS} E_T^{CS} \left( 1 + \frac{K_M^{AcCoA}}{[AcCoA]} + \frac{K_M^{OAA}}{[OAA]} + \frac{K_M^{AcCoA}}{[AcCoA]} \frac{K_M^{OAA}}{[OAA]} \right)^{-1}$	E269
$V_{ACO} = k_f^{ACO} [CIT] - \frac{[ISOC]}{K_E^{ACO}}$	E270
$f_a^{IDH} = \frac{1}{1 + \frac{[ADP]_m}{K_{ADP}^a} + 1 + \frac{[Ca^{2+}]_m}{K_{Ca}^a}}$	E271
$f_i^{IDH} = \frac{1}{1 + \frac{[NADH]}{K_{i,NADH}}}$	E272
$V_{IDH} = k_{cat}^{IDH} E_T^{IDH} \frac{1}{\left( 1 + \frac{[H^+]}{k_{h,1}} + \frac{k_{h,2}}{[H^+]} + f_i^{IDH} \frac{K_M^{NAD}}{[NAD]} + f_a^{IDH} \frac{K_M^{ISOC}}{[ISOC]} + f_a^{IDH} f_i^{IDH} \frac{K_M^{ISOC}}{[ISOC]} \frac{K_M^{NAD}}{[NAD]} \right)^{-1}}$	E273

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$$f_a^{KGDH} = \frac{1}{1 + \frac{[Mg^{2+}]}{K_D^{Mg^{2+}}} + \frac{[Ca^{2+}]_m}{K_D^{Ca^{2+}}}} \quad E274$$


---

$$V_{KGDH} = \frac{k_{cat}^{KGDH} E_T^{KGDH}}{1 + f_a^{KGDH} \frac{K_M^{KG}}{[KG]} + f_a^{KGDH} \frac{K_M^{NAD}}{[NAD]} n_{aKG}} \quad E275$$


---

$$V_{SL} = k_f^{SL} [SCoA][ADP]_m - \frac{[Suc][ATP]_m [CoA]}{K_E^{SL}} \quad E276$$


---

$$V_{SDH} = \frac{k_{cat}^{SDH} E_T^{SDH}}{1 + \frac{K_M^{Suc}}{[Suc]} + \frac{[OAA]}{K_{i,sdh}^{OAA}} + \frac{[FUM]}{K_i^{FUM}}} \quad E277$$


---

$$V_{FH} = k_f^{FH} [FUM] - \frac{[MAL]}{K_E^{FH}} \quad E278$$


---

$$f_{h,a} = \frac{1}{1 + \frac{[H^+]}{k_{h1}} + \frac{[H^+]^2}{k_{h1} k_{h2}}} + k_{offset} \quad E279$$


---

$$f_{h,i} = \frac{1}{1 + \frac{k_{h3}}{[H^+]} + \frac{k_{h3} k_{h4}}{[H^+]^2}} \quad E280$$


---

$$V_{MDH} = \frac{k_{cat}^{MDH} E_T^{MDH} f_{h,a} f_{h,i}}{1 + \frac{K_M^{MAL}}{[MAL]} + \frac{[OAA]}{K_i^{OAA}} + \frac{K_M^{NAD}}{[NAD]} + \frac{K_M^{MAL}}{[MAL]} + \frac{[OAA]}{K_i^{OAA}} + \frac{K_M^{NAD}}{[NAD]}} \quad E281$$


---

$$V_{AAT} = k_f^{AAT} [OAA][GLU] \frac{k_{ASP} K_E^{AAT}}{(k_{ASP} K_E^{AAT} + [KG] k_f^{AAT})} \quad E282$$


---

### Oxidative phosphorylation reaction rates

---


$$V_{O_2} = 0.5 \frac{r_a + r_{c1} e^{\frac{6F}{RT} \frac{B}{RT}} e^{\frac{A_{res} F}{RT}} - r_a e^{\frac{g 6F}{RT} \frac{H}{RT}} + r_{c2} e^{\frac{A_{res} F}{RT}} e^{\frac{g 6F}{RT} \frac{H}{RT}}}{1 + r_1 e^{\frac{FA_{res}}{RT}} e^{\frac{6F}{RT} \frac{B}{RT}} + r_2 + r_3 e^{\frac{FA_{res}}{RT}} e^{\frac{g 6F}{RT} \frac{H}{RT}}} \quad E283$$


---



$$V_{He} = 6 \text{ }^{res} \frac{r_a e^{\frac{A_{res} F}{RT}} (r_a + r_b) e^{\frac{g 6F}{RT}}}{1 + r_1 e^{\frac{F A_{res}}{RT}} e^{\frac{6F}{RT}} + r_2 + r_3 e^{\frac{F A_{res}}{RT}} e^{\frac{g 6F}{RT}}}$$

E284

$$A_{res} = \frac{RT}{F} \ln K_{res} \sqrt{\frac{[NADH]}{[NAD^+]}}$$

E285

$$[NAD^+] = C_{PN} - [NADH]$$

E286

$$V_{He(F)} = 4 \text{ }^{res(F)} \frac{r_a e^{\frac{A_{res(F)} F}{RT}} (r_a + r_b) e^{\frac{g 6F}{RT}}}{1 + r_1 e^{\frac{F A_{res(F)}}{RT}} e^{\frac{6F}{RT}} + r_2 + r_3 e^{\frac{F A_{res(F)}}{RT}} e^{\frac{g 6F}{RT}}}$$

E287

$$A_{res(F)} = \frac{RT}{F} \ln K_{res(F)} \sqrt{\frac{[FADH_2]}{[FAD]}}$$

E288

$$V_{ATPase} = - F1 \frac{10^2 p_a + p_{c1} e^{\frac{3F}{RT}} e^{\frac{A_{F1} F}{RT}} - p_a e^{\frac{3F}{RT}} + p_{c2} e^{\frac{A_{F1} F}{RT}} e^{\frac{3F}{RT}}}{1 + p_1 e^{\frac{F A_{F1}}{RT}} e^{\frac{3F}{RT}} + p_2 + p_3 e^{\frac{F A_{F1}}{RT}} e^{\frac{3F}{RT}}}$$

E289

$$V_{Hu} = -3 \text{ }^{F1} \frac{10^2 p_a 1 + e^{\frac{F A_{F1}}{RT}} - (p_a + p_b) e^{\frac{3F}{RT}}}{1 + p_1 e^{\frac{F A_{F1}}{RT}} e^{\frac{3F}{RT}} + p_2 + p_3 e^{\frac{F A_{F1}}{RT}} e^{\frac{3F}{RT}}}$$

E290

$$A_{F1} = \frac{RT}{F} \ln K_{F1} \frac{[ATP]_m}{[ADP]_m Pi}$$

E291

$$V_{Hleak} = g_H \quad H$$

E292

$$H = -2.303 \frac{RT}{F} pH + \quad m$$

E293

### Mitochondrial Ca<sup>2+</sup> handling rates

$$V_{uni} = V_{max}^{uni} \frac{\frac{[Ca^{2+}]_i}{K_{trans}} \left( 1 + \frac{[Ca^{2+}]_i^3}{K_{trans}} \right) \frac{2F}{RT} (\psi_m - \psi_o)}{1 + \frac{[Ca^{2+}]_i^4}{K_{trans}} + \frac{L}{1 + \frac{[Ca^{2+}]_i^{n_a}}{K_{act}}} \left( 1 - e^{-\frac{2F}{RT} (\psi_m - \psi_o)} \right)}$$

E294

$$V_{NaCa} = V_{max}^{NaCa} \frac{e^{\frac{bF(\Delta\Psi_m - \Psi^o)}{RT}} \frac{\ln \frac{[Ca^{2+}]_m}{[Ca^{2+}]_i}}{n}}{1 + \frac{K_{Na}}{[Na^+]_i} \left( 1 + \frac{K_{Ca}}{[Ca^{2+}]_m} \right)}$$

E295

### ROS-induced-ROS-release rates

$$V_{SOD\_mito} = \frac{2 \cdot k_{SOD}^1 k_{SOD}^5 \left( k_{SOD}^1 + k_{SOD}^3 \right) \left( 1 + \frac{[H_2O_2]}{K_i^{H2O2}} \right) E_{SOD}^T [O_2^-]_{p\_mito}}{k_{SOD}^5 \left( 2 \cdot k_{SOD}^1 + k_{SOD}^3 \right) \left( 1 + \frac{[H_2O_2]}{K_i^{H2O2}} \right) + [O_2^-]_{p\_mito} k_{SOD}^1 k_{SOD}^3 \left( 1 + \frac{[H_2O_2]}{K_i^{H2O2}} \right)}$$

E296

$$f([O_2^-]_{SR}) = V_{SOD\_SR}$$

$$= \frac{2 \cdot k_{SOD}^1 k_{SOD}^5 \left( k_{SOD}^1 + k_{SOD}^3 \right) \left( 1 + \frac{[H_2O_2]}{K_i^{H2O2}} \right) E_{SOD}^T [O_2^-]_{SR}}{k_{SOD}^5 \left( 2 \cdot k_{SOD}^1 + k_{SOD}^3 \right) \left( 1 + \frac{[H_2O_2]}{K_i^{H2O2}} \right) + [O_2^-]_{SR} k_{SOD}^1 k_{SOD}^3 \left( 1 + \frac{[H_2O_2]}{K_i^{H2O2}} \right)} \frac{2585.8986}{X^{1.82}}$$

E297

$$V_{CAT} = 2 k_{CAT}^1 E_{CAT}^T [H_2O_2] e^{fr [H_2O_2]}$$

E298

$$V_{GPX} = \frac{E_{GPX}^T [H_2O_2][GSH]}{1 [GSH] + 2 [H_2O_2]}$$

E299

$$V_{GR} = \frac{k_{GR}^1 E_{GR}^T}{1 + \frac{K_M^{GSSG}}{[GSSG]} + \frac{K_M^{NADPH}}{[NADPH]} + \frac{K_M^{GSSG}}{[GSSG]} \frac{K_M^{NADPH}}{[NADPH]}} \quad E300$$

$$V_{ROS}^{Tr} = j \cdot \frac{V_{IMAC}}{m} \quad m - \frac{RT}{F} \log \frac{[O_2^{\cdot-}]_{mito}}{[O_2^{\cdot-}]_{p\_mito}} \quad E301$$

$$V_{IMAC} = a + \frac{b}{1 + \frac{K_{cc}}{[O_2^{\cdot-}]_i}} G_L + \frac{G_{max}}{1 + e \left( \frac{b}{m} \right)^m} \quad E302$$

$$G_T = [GSH] + 2 \cdot [GSSG] \quad E303$$

### ROS-induced-ROS-release metabolites balance equations

$$\frac{d[O_2^{\cdot-}]_{mito}}{dt} = \text{shunt } V_{O_2} - V_{ROS}^{Tr} \quad E304$$

$$\frac{d[O_2^{\cdot-}]_{p\_mito}}{dt} = V_{ROS}^{Tr} - V_{SOD\_mito} \quad E305$$

$$\frac{d[H_2O_2]}{dt} = V_{SOD\_mito} - V_{CAT} - V_{GPX} \quad E306$$

$$\frac{d[GSH]}{dt} = V_{GR} - V_{GPX} \quad E307$$

### ROS diffusion between mitochondrion and SR

$$\frac{d[O_2^{\cdot-}]_{SR}(t)}{dt} = D_{O_2^{\cdot-}} \cdot \frac{[O_2^{\cdot-}]_{p\_mito}(t) - [O_2^{\cdot-}]_{SR}(t)}{X^2} + v_{cyto\_MSM} \cdot f([O_2^{\cdot-}]_{SR}(t)) \quad E308$$

**Table S9. General parameters**

Symbol	Value	Units	Description	Ref.
$F$	96.5	$C \cdot \text{mmol}^{-1}$	Faraday constant	
$T$	310	K	Absolute temperature	
$R$	8.31	$J \cdot \text{mol}^{-1} \cdot \text{K}^{-1}$	Universal gas constant	
$C_m$	1.0	$\mu\text{F} \cdot \text{cm}^{-2}$	Membrane capacitance	7
$A_{\text{cap}}$	$1.54 \times 10^{-4}$	$\text{cm}^2$	Capacitative cell surface area	7
$V_{\text{myo}}$	25.84	pL	Cytosolic volume	7
$V_{\text{mito}}$	15.89	pL	Mitochondrial volume	7
$V_{\text{ss}}$	$2.5 \times 10^{-7}$	pL	SS volume	**
$[\text{K}^+]_o$	5.4	mM	Extracellular $\text{K}^+$ concentration	7
$[\text{Na}^+]_o$	140.0	mM	Extracellular $\text{Na}^+$ concentration	7
$[\text{Ca}^{2+}]_o$	2.0	mM	Extracellular $\text{Ca}^{2+}$ concentration	7

\* estimated. \*\* was slightly modified to achieve ~37% of SR  $\text{Ca}^{2+}$  depletion during a normal AP cycle.

**Table S10. Sarcolemmal membrane current parameters**

Symbol	Value	Units	Description	Ref.
$\bar{G}_{\text{Na}}$	12.8	$\text{mS} \cdot \mu\text{F}^{-1}$	Maximal Na channel conductance	7
$\bar{G}_{\text{Kp}}$	$8.28 \times 10^{-3}$	$\text{mS} \cdot \mu\text{F}^{-1}$	Maximal plateau $\text{K}^+$ channel conductance	4
$P_{\text{Na,K}}$	0.0183		$\text{Na}^+$ permeability of $\text{K}^+$ channel	4
$k_{\text{NaCa}}$	9000	$\mu\text{A} \cdot \mu\text{F}^{-1}$	Scaling factor of $\text{Na}^+/\text{Ca}^+$ exchange	4
$k_{m,\text{Na}}$	87.5	mM	Na half saturation constant NCX	4
$k_{m,\text{Ca}}$	1.38	mM	Na half saturation constant NCX	4
$k_{\text{sat}}$	0.1		$\text{Na}^+/\text{Ca}^{2+}$ exchange saturation factor at negative potentials	4
$\eta$	0.35		Controls voltage dependence of NCX	4

**Table S11. Na<sup>+</sup>/K<sup>+</sup> pump parameters**

Symbol	Value	Units	Description	Ref.
$\bar{I}_{\text{NaK}}$	3.247	$\mu\text{A}\cdot\mu\text{F}^{-1}$	Maximum Na <sup>+</sup> /K <sup>+</sup> pump current	4
$K_{\text{m,Na}}$	10	mM	Na half saturation for Na <sup>+</sup> /K <sup>+</sup> pump	4
$K_{\text{m,K}}$	1.5	mM	K half saturation for Na <sup>+</sup> /K <sup>+</sup> pump	4
$K_{\text{NaK}}^{\text{I,ATP}}$	$8.0\times 10^{-3}$	mM	ATP half saturation constant for Na <sup>+</sup> /K <sup>+</sup> pump	4
$K_{\text{NaK}}^{\text{i,ADP}}$	0.1	mM	ADP inhibition constant for Na <sup>+</sup> /K <sup>+</sup> pump	4

**Table S12. Non-specific channel current parameters**

Symbol	Value	Units	Description	Ref.
$P_{\text{ns(Na)}}$	$1.75\times 10^{-7}$	$\text{cm}\cdot\text{s}^{-1}$	Non-specific channel current Na permeability	4
$K_{\text{m,ns(Ca)}}$	$1.2\times 10^{-3}$	mM	Ca <sup>2+</sup> half saturation constant for non-specific current	4
$P_{\text{ns(K)}}$	0	$\text{cm}\cdot\text{s}^{-1}$	Non-specific channel current K permeability	4

**Table S13 Background Ca<sup>2+</sup> current parameters**

Symbol	Value	Units	Description	Ref.
$\bar{G}_{\text{Ca,b}}$	$3.22\times 10^{-3}$	$\text{mS}\cdot\mu\text{F}^{-1}$	Maximum background current Ca <sup>2+</sup> conductance	4
$\bar{G}_{\text{Na,b}}$	3.5e-3	$\text{mS}\cdot\mu\text{F}^{-1}$	Maximum background current Na <sup>+</sup> conductance	*

\* The parameters were adjusted to maintain [Na<sup>+</sup>] at 8.5 mM under normal condition.

**Table S14. Sarcolemmal Ca<sup>2+</sup> current parameters**

Symbol	Value	Units	Description	Ref.
$I_{pCa\_max}$	0.575	$\mu A \cdot \mu F^{-1}$	Maximum sarcolemmal Ca <sup>2+</sup> pump current	4
$K_m^{pCa}$	$5 \times 10^{-4}$	mM	Ca <sup>2+</sup> half saturation constant for sarcolemmal Ca <sup>2+</sup> pump	4
$K_{m1\_pCa}^{ATP}$	0.012	mM	First ATP half saturation constant for sarcolemmal Ca <sup>2+</sup> pump	4
$K_{m2\_pCa}^{ATP}$	0.23	mM	Second ATP half saturation constant for sarcolemmal Ca <sup>2+</sup> pump	4
$K_{i\_pCa}^{ADP}$	1.0	mM	ADP inhibition constant for sarcolemmal Ca <sup>2+</sup> pump	4

**Table S15. Sarcoplasmic reticulum Ca<sup>2+</sup> ATPase parameters**

Symbol	Value	Units	Description	Ref.
$V_{max,f}$	$2.99 \times 10^{-4}$	$ms^{-1}$	SERCA forward rate parameter	4
$V_{max,r}$	$3.98 \times 10^{-4}$	$ms^{-1}$	SERCA reverse rate parameter	4
$K_{fb}$	$1.5 \times 10^{-4}$	mM	Forward Ca <sup>2+</sup> half saturation constant of SERCA	*
$K_{rb}$	3.3	mM	Reverse Ca <sup>2+</sup> half saturation constant of SERCA	*
$N_{fb}$	0.5		Forward cooperativity constant of SERCA	*
$N_{rb}$	0.5		Reverse cooperativity constant of SERCA	*
$K_{m,up}^{ATP}$	0.01	mM	ATP half saturation constant for SERCA	4
$K_{i,up}$	0.14	mM	ADP first inhibition constant for SERCA	4
$K'_{i,up}$	5.1	mM	ADP second inhibition constant for SERCA	4

\*These parameters were adjusted to maintain diastolic  $[Ca^{2+}]_i$  near 60 nM and  $[Ca^{2+}]_{SR}$  near 0.45 mM while avoiding net reverse SERCA flux at 1 Hz pacing.

**Table S16. L-type Ca<sup>2+</sup> current parameters**

Symbol	Value	Units	Description	Ref.
$\bar{P}_{Ca}$	$9.13 \times 10^{-13}$	$\text{cm} \cdot \text{s}^{-1}$	L-type Ca <sup>2+</sup> channel permeability to Ca <sup>2+</sup>	7
$N_{CaRU}$	300000		Number of Ca <sup>2+</sup> release units	*
f	0.85	$\text{ms}^{-1}$	Transit rate into open state	7
g	2	$\text{ms}^{-1}$	Transit rate out of open state	7
a	5.0		LCC mode transition parameter	7
b	10.0		Mode transition parameter	7
$\gamma_0$	7.5		Mode transition parameter	7
$\omega$	0.068		Mode transition parameter	*

\* These parameters are modified to provide better fit of  $I_{CaL}$  to experimental data <sup>3</sup>.

**Table S17. Ca<sup>2+</sup> release channel parameters**

Symbol	Value	Units	Description	Ref.
$k_{0,1,2}$	5265	$\text{ms}^{-1}$	RyR channel rate parameter	7
$k_{0,2,1}$	1500	$\text{ms}^{-1}$	RyR channel rate parameter	7
$k_{0,2,3}$	$2.36e^8$	$\text{ms}^{-1}$	RyR channel rate parameter	7
$k_{0,3,2}$	9.6	$\text{ms}^{-1}$	RyR channel rate parameter	7
$k_{0,4,3}$	13.65	$\text{ms}^{-1}$	RyR channel rate parameter	7
$k_{0,3,4}$	$1.42e^6$	$\text{ms}^{-1}$	RyR channel rate parameter	7
$k_{0,2,5}$	$2.36e^6$	$\text{ms}^{-1}$	RyR channel rate parameter	7
$k_{0,5,2}$	0.0013	$\text{ms}^{-1}$	RyR channel rate parameter	7
$k_{0,6,5}$	30	$\text{ms}^{-1}$	RyR channel rate parameter	7
$k_{0,5,6}$	$1.89e^7$	$\text{ms}^{-1}$	RyR channel rate parameter	7
$k_{0,4,5}$	0.07	$\text{ms}^{-1}$	RyR channel rate parameter	7
$k_{0,5,4}$	93.39	$\text{ms}^{-1}$	RyR channel rate parameter	7

**Table S18. Force generation parameters**

Symbol	Value	Units	Description	Ref.
$k_{pn}^{trop}$	0.04	$ms^{-1}$	Transition rate from tropomyosin permissive to non-permissive	5
SL	2.15	$\mu m$	Sarcomere length	5
$f_{XB}$	0.05	$ms^{-1}$	Transition rate from weak to strong cross bridge	9
$g_{XB}^{min}$	0.1	$ms^{-1}$	Minimum transition rate from strong to weak cross bridge	9
$g_{off}$	0.01	$ms^{-1}$	Minimum transition rate from strong to weak cross bridge for non-permissive tropomyosin	5
$\zeta$	0.1	$N \cdot mm^{-2}$	Conversion factor normalizing to physiological force	5
$V_{AM}^{max}$	$4.8 \times 10^{-4}$	$mM \cdot ms^{-1}$	Maximal rate of ATP hydrolysis by myofibrils (AM ATPase)	10
$K_{M,AM}^{ATP}$	0.03	mM	ATP half saturation constant of AM ATPase	10
$K_{i,AM}$	0.26	mM	ADP inhibition constant of AM ATPase	10

**Table S19. Cytoplasmic energy handling parameters**

Symbol	Value	Units	Description	Ref.
$C_T$	25	mM	Total concentration of creatine metabolites (both compartments)	11, 12
$k_{CK}^{cyto}$	$1.4 \times 10^{-4}$	$ms^{-1}$	Forward rate constant of cytoplasmic CK	13
$k_{CK}^{mito}$	$1.33 \times 10^{-6}$	$ms^{-1}$	Forward rate constant of mitochondrial CK	13
$k_{tr}^{Cr}$	$2.0 \times 10^{-3}$	$ms^{-1}$	Transfer rate constant of CrP	13
$K_{EQ}$	0.0095		Equilibrium constant of CK	9, 11



$V_{\text{ATPase}}^{\text{cyto}}$	$1.0 \times 10^{-5}$	$\text{mM} \cdot \text{ms}^{-1}$	Constitutive cytosolic ATP consumption rate	14
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**Table S20. Tricarboxylic acid cycle parameters**

Symbol	Value	Units	Description	Ref.
[AcCoA]	1.0	mM	Acetyl CoA concentration	15
$k_{\text{cat}}^{\text{CS}}$	0.5	$\text{ms}^{-1}$	Catalytic constant of CS	4
$E_{\text{T}}^{\text{CS}}$	0.4	mM	Concentration of CS	7, 15
$K_{\text{M}}^{\text{AcCoA}}$	$1.26 \times 10^{-2}$	mM	Michaelis constant for AcCoA	15
$K_{\text{M}}^{\text{OAA}}$	$6.4 \times 10^{-4}$	mM	Michaelis constant for OAA	15
$C_{\text{Kint}}$	1.0	mM	Sum of TCA cycle intermediates' concentration	15
$k_{\text{f}}^{\text{ACO}}$	$1.25 \times 10^{-2}$	$\text{ms}^{-1}$	Forward rate constant of ACO	15
$K_{\text{E}}^{\text{ACO}}$	2.22		Equilibrium constant of ACO	15
$K_{\text{ADP}}^{\text{a}}$	0.62	mM	Activation constant by ADP	4
$K_{\text{Ca}}^{\text{a}}$	0.0005	mM	Activation constant for $\text{Ca}^{2+}$	4
$K_{\text{i,NADH}}$	0.19	mM	Inhibition constant by NADH	15
$k_{\text{cat}}^{\text{IDH}}$	0.05	$\text{ms}^{-1}$	Rate constant of IDH	4
$E_{\text{T}}^{\text{IDH}}$	0.109	mM	Concentration of IDH	15
$[\text{H}^+]$	$2.5 \times 10^{-5}$	mM	Matrix proton concentration	15
$k_{\text{h,1}}$	$8.1 \times 10^{-5}$	mM	Ionization constant of IDH	15
$k_{\text{h,2}}$	$5.98 \times 10^{-5}$	mM	Ionization constant of IDH	15
$K_{\text{M}}^{\text{ISOC}}$	1.52	mM	Michaelis constant for isocitrate	15
ni	2.0		Cooperativity for isocitrate	15

$K_M^{\text{NAD}}$	0.92	mM	Michaelis constant for $\text{NAD}^+$	15
$K_D^{\text{Mg}^{2+}}$	0.031	mM	Activation constant for $\text{Mg}^{2+}$	15
$K_D^{\text{Ca}^{2+}}$	$1.27 \times 10^{-3}$	mM	Activation constant for $\text{Ca}^{2+}$	15
$E_T^{\text{KGDH}}$	0.5	mM	Concentration of KGDH	15
$k_{\text{cat}}^{\text{KGDH}}$	0.075	$\text{ms}^{-1}$	Rate constant of KGDH	4
$K_M^{\text{KG}}$	1.94	mM	Michaelis constant for $\alpha\text{KG}$	15
$K_M^{\text{NAD}}$	38.7	mM	Michaelis constant for NAD	15
$n_{\alpha\text{KG}}$	1.2		Hill coefficient of KGDH for $\alpha\text{KG}$	15
$\text{Mg}^{2+}$	0.4	mM	$\text{Mg}^{2+}$ concentration in mitochondria	15
$k_f^{\text{SL}}$	$5.0 \times 10^{-3}$	$\text{mM}^{-1} \cdot \text{ms}^{-1}$	Forward rate constant of SL	4
$K_E^{\text{SL}}$	3.12		Equilibrium constant of the SL reaction	15
[CoA]	0.02	mM	Coenzyme A concentration	15
$k_{\text{cat}}^{\text{SDH}}$	$5.0 \times 10^{-3}$	$\text{ms}^{-1}$	Rate constant of SDH	4
$E_T^{\text{SDH}}$	0.5	mM	SDH enzyme concentration	15
$K_M^{\text{Suc}}$	0.03	mM	Michaelis constant for succinate	15
$K_i^{\text{FUM}}$	1.3	mM	Inhibition constant by fumarate	15
$K_{i,\text{sdh}}^{\text{OAA}}$	0.15	mM	Inhibition constant by oxalacetate	15
$k_f^{\text{FH}}$	$3.32 \times 10^{-3}$	$\text{ms}^{-1}$	Forward rate constant for FH	4
$K_E^{\text{FH}}$	1.0		Equilibrium constant of FH	15
$k_{h1}$	$1.13 \times 10^{-5}$	mM	Ionization constant of MDH	15
$k_{h2}$	26.7	mM	Ionization constant of MDH	15
$k_{h3}$	$6.68 \times 10^{-9}$	mM	Ionization constant of MDH	15
$k_{h4}$	$5.62 \times 10^{-6}$	mM	Ionization constant of MDH	15
$k_{\text{offset}}$	$3.99 \times 10^{-2}$		pH-independent term in the pH activation factor of MDH	15
$k_{\text{cat}}^{\text{MDH}}$	0.11	$\text{ms}^{-1}$	Rate constant of MDH	4

$E_T^{MDH}$	0.15	mM	Total MDH enzyme concentration	15
$K_M^{MAL}$	1.49	mM	Michaelis constant for malate	15
$K_i^{OAA}$	$3.1 \times 10^{-3}$	mM	Inhibition constant for oxalacetate	15
$K_M^{NAD}$	0.22	mM	Michaelis constant for $NAD^+$	15
[GLU]	1	mM	Glutamate concentration	15
$k_f^{AAT}$	$6.44 \times 10^{-4}$	$ms^{-1}$	Forward rate constant of AAT	15
$K_E^{AAT}$	6.6		Equilibrium constant of AAT	15
$k_{ASP}$	$1.5 \times 10^{-6}$	$ms^{-1}$	Rate constant of aspartate consumption	4

**Table S21. Oxidative phosphorylation parameters**

Symbol	Value	Units	Description	Ref.
$r_a$	$6.39 \times 10^{-13}$	$ms^{-1}$	Sum of products of rate constants	15
$r_b$	$1.76 \times 10^{-16}$	$ms^{-1}$	Sum of products of rate constants	15
$r_{c1}$	$2.66 \times 10^{-22}$	$ms^{-1}$	Sum of products of rate constants	15
$r_{c2}$	$8.63 \times 10^{-30}$	$ms^{-1}$	Sum of products of rate constants	15
$r_1$	$2.08 \times 10^{-18}$		Sum of products of rate constants	15
$r_2$	$1.73 \times 10^{-9}$		Sum of products of rate constants	15
$r_3$	$1.06 \times 10^{-26}$		Sum of products of rate constants	15
$\rho^{res}$	$0.1 \times 10^{-3}$	mM	Concentration of electron carriers (respiratory complexes I-III-IV)	4
$K_{res}$	$1.35 \times 10^{18}$		Equilibrium constant of respiration	15
$\rho^{res(F)}$	$3.75 \times 10^{-4}$	mM	Concentration of electron carriers (respiratory complexes II-III-IV)	4
$\Delta\Psi_B$	50	mV	Phase boundary potential	15
$g$	0.85		Correction factor for voltage	15
$K_{res(F)}$	$5.77 \times 10^{13}$		Equilibrium constant of $FADH_2$ oxidation	15
[FADH2]	1.24	mM	Concentration of $FADH_2$ (reduced)	15
[FAD]	0.01	mM	Concentration of FAD (oxidized)	15

$p_a$	$1.66 \times 10^{-8}$	$\text{ms}^{-1}$	Sum of products of rate constants	15
$p_b$	$3.37 \times 10^{-10}$	$\text{ms}^{-1}$	Sum of products of rate constants	15
$p_{c1}$	$9.65 \times 10^{-17}$	$\text{ms}^{-1}$	Sum of products of rate constants	15
$p_{c2}$	$4.59 \times 10^{-17}$	$\text{ms}^{-1}$	Sum of products of rate constants	15
$p_1$	$1.35 \times 10^{-8}$		Sum of products of rate constants	15
$p_2$	$7.74 \times 10^{-7}$		Sum of products of rate constants	15
$p_3$	$6.65 \times 10^{-15}$		Sum of products of rate constants	15
$\rho^{F_1}$	0.05	mM	Concentration of $F_1F_0$ -ATPase	4
$K_{F_1}$	$1.71 \times 10^6$		Equilibrium constant of ATP hydrolysis	15
$P_i$	2.0	mM	Inorganic phosphate concentration	4
$C_A$	1.5	mM	Total sum of mito adenine nucleotides	4
$V_{\max\text{ANT}}$	0.005	$\text{mM} \cdot \text{ms}^{-1}$	Maximal rate of the ANT	4, 15
$h^{\text{ANT}}$	0.5		Fraction of $\Delta\Psi_m$	15
$g_H$	$1.0 \times 10^{-8}$	$\frac{\text{mM} \cdot \text{ms}^{-1}}{\text{mV}^{-1}}$	Ionic conductance of the inner membrane	15
$\Delta\text{pH}$	-0.6	pH units	pH gradient across the inner memb.	15
$C_{\text{PN}}$	1.0	mM	Total sum of mito pyridine nucleotides	15
$C_{\text{mito}}$	$1.81 \times 10^{-3}$	$\text{mM} \cdot \text{mV}^{-1}$	Inner membrane capacitance	15

**Table S22. Mitochondrial  $\text{Ca}^{2+}$  handling parameters**

Symbol	Value	Units	Description	Ref.
$V_{\max}^{\text{uni}}$	0.028	$\text{mM} \cdot \text{ms}^{-1}$	Vmax uniport $\text{Ca}^{2+}$ transport	4
$\Delta\Psi^\circ$	91	mV	Offset membrane potential	15
$K_{\text{act}}$	$3.8 \times 10^{-4}$	mM	Activation constant	15
$K_{\text{trans}}$	0.019	mM	$K_d$ for translocated $\text{Ca}^{2+}$	15
L	110.0		Keq for conformational transitions in uniporter	15

$n_a$	2.8		Uniporter activation cooperativity	15
$V_{max}^{NaCa}$	$1 \times 10^{-4}$	$mM \cdot ms^{-1}$	Vmax of $Na^+/Ca^{2+}$ antiporter	*
$b$	0.5		$\Delta\Psi_m$ dependence of $Na^+/Ca^{2+}$ antiporter	15
$K_{Na}$	9.4	mM	Antiporter $Na^+$ constant	15
$K_{Ca}$	$3.75 \times 10^{-4}$	mM	Antiporter $Ca^{2+}$ constant	15
$n$	3		$Na^+/Ca^{2+}$ antiporter cooperativity	15
$\delta$	$3.0 \times 10^{-4}$		Fraction of free $[Ca^{2+}]_m$	15

\*: The maximal rate of the  $Na^+/Ca^{2+}$  antiporter was adjusted to balance the mitochondrial  $Ca^{2+}$  level.

**Table S23. ROS-induced-ROS-release parameters**

Symbol	Value	Units	Description	Ref.
$af$	$1 \times 10^{-4}$		Activation factor by cytoplasmic $O_2^-$	4
$K_{cc}$	0.01	mM	Activation constant of IMAC by $O_2^-$	4
$G_L$	$3.50 \times 10^{-8}$	$mM \cdot ms^{-1} \cdot mV^{-1}$	Leak conductance for IMAC	4
$G_{max}$	$3.91 \times 10^{-6}$	$mM \cdot ms^{-1} \cdot mV^{-1}$	Integral conductance of IMAC at saturation	4
	0.07	$mV^{-1}$	Steepness factor	4
$b_m$	4	mV	Potential at half-saturation	4
$k1\_SOD$	$1.2 \times 10^3$	$mM \cdot ms^{-1}$	Second-order rate constant of conversion between native oxidized and reduced SOD	4
$k5\_SOD$	$2.5 \times 10^{-4}$	$mM^{-1} \cdot ms^{-1}$	First-order rate constant for conversion between inactive and active oxidized SOD	4
$k3\_SOD$	24	$mM^{-1} \cdot ms^{-1}$	Second-order rate constant of conversion between native reduced SOD and its inactive form	4
$etSOD$	$1.43 \times 10^{-3}$	mM	Intracellular concentration of SOD	4
$K_i^{H_2O_2}$	0.5	mM	Inhibition constant for $H_2O_2$	4
$k_{CAT}^1$	17	$mM^{-1} \cdot ms^{-1}$	Rate constant of CAT	4
$E_{CAT}^T$	0.01	mM	Intracellular CAT concentration	4
$fr$	0.05		Hydrogen peroxide inhibition factor for CAT	4
$E_{GPX}^T$	0.01	mM	Intracellular GPX concentration	4
$1$	$5 \times 10^{-3}$	$mM \cdot ms$	Constant for GPX activity	4
$2$	0.75	$mM \cdot ms$	Constant for GPX activity	4

$k_{GR}^1$	$5 \times 10^{-3}$	$ms^{-1}$	Rate constant of GR	4
$E_{GR}^T$	0.01	mM	Intracellular GR concentration	4
$K_M^{GSSG}$	0.06	mM	Michaelis constant for oxidized glutathione of GR	4
$K_M^{NADPH}$	0.015	mM	Michaelis constant for NADH for GR	4
NADPH	1	mM	Total NADH pool	4
$G_T$	1	mM	Total glutathione pool	4
<i>shunt</i>	0.02		Fraction of $O_2$ to form superoxide.	4
<i>j</i>	0.1		Fraction of IMAC conductance.	4

\*: The ROS diffusion coefficient and the distance between SR and mitochondria were adjusted to be inconsistent with previous experimental studies<sup>16,17</sup>.

**Table S24. ROS diffusion model parameters**

Symbol	Value	Units	Description	Ref.
$D_{O_2^-}$	0.295	$\mu m^2 \cdot ms^{-1}$	$O_2^-$ diffusion coefficient	*
<i>X</i>	75	nm	Distance between SR and mitochondria	*
$c_{ryr}$	0.2		ROS enhancement coefficient	**
$k_{ryr}$	19.55	$mM^{-1}$	ROS enhancement effective factor	**
$c_{SERCA}$	1.02		ROS inhibition coefficient	**
$k_{SERCA}$	43.67	$mM^{-1}$	ROS inhibition effective factor	**
$V_{cyto\_MSM}$	$2.05 \times 10^5$		Cytosolic/MSM effective volume ratio	***

\*: The ROS diffusion coefficient and the distance between SR and mitochondria were adjusted to be inconsistent with previous experimental studies<sup>16,17</sup>.

\*\* : The values of model parameter were obtained using the least-square curve fitting method, as described in the text.

\*\*\*: estimated.

**Table S25. CaMKII activation parameters**

Symbol	Value	Units	description	Ref.
$k_1$	2.5	$mM^{-1} \cdot ms^{-1}$	The kinetic rate constant	1, 18, 19
$k_{-1}, k_{-2}$	0.05	$ms^{-1}$	The kinetic rate constant	1, 18, 19
$k_2$	88.25	$mM^{-1} \cdot ms^{-1}$	The kinetic rate constant	1, 18, 19

$k_3$	12.5	$\text{mM}^{-1}\cdot\text{ms}^{-1}$	The kinetic rate constant	1, 18, 19
$k_{-3}, k_{-4}$	1.25	$\text{ms}^{-1}$	The kinetic rate constant	1, 18, 19
$k_{asso}$	2.1	$\text{mM}^{-1}\cdot\text{ms}^{-1}$	The association rate constant	1, 18, 19
$k_{disso}$	$0.7\times 10^{-4}$	$\text{ms}^{-1}$	The dissociation rate constant	1, 18, 19
$k_{dissoCa}$	$0.95\times 10^{-3}$	$\text{ms}^{-1}$	The dissociation rate constant	1, 18, 19
$k_{dissoCa2}$	$0.95\times 10^{-6}$	$\text{ms}^{-1}$	The dissociation rate constant	1, 18, 19
$k_{cat}$	$5.4\times 10^{-3}$	$\text{ms}^{-1}$	The phosphorylation rate constant	1, 18, 19
$k_{cat,PP1}$	$1.72\times 10^{-3}$	$\text{ms}^{-1}$	The dephosphorylation rate constant	1, 18, 19
$K_{m,ATP}$	$19.1\times 10^{-3}$	mM	The binding affinity for ATP	1, 18, 19
$K_{m,PP1}$	$11.0\times 10^{-3}$	mM	The binding affinity for PP1	1, 18, 19
$k_{ox}$	0.013	$\text{mM}^{-1}\cdot\text{ms}^{-1}$	The oxidation rate by ROS	1
$k_{MrsA}$	$1.0\times 10^{-4}$	$\text{ms}^{-1}$	The reduction rate by MrsA	1
$[PP1]$	$14.3\times 10^{-3}$	mM	The concentration of protein phosphatases	1
$[CaM_{total}]$	$50.0\times 10^{-3}$	mM	The concentration of total CaM	1
$[CaMKII_{total}]$	$3.15\times 10^{-6}$	mM	The concentration of total CaMKII	1

**Table S26. Markov late sodium channels parameters**

Parameter	Unphosphorylated	Phosphorylated	Ref.
P1a1	3.99	3.99	20
P2a1	0.02	0.02	
P1a4	5.76	5.76	
P2a4	107.67	1.67	
P1a5	$1.63\times 10^{-8}$	$2.5\times 10^{-8}$	
P2a5	6.21	6.21	
P1b1	0.03	0.03	
P2b1	9.35	9.35	
P1b2	0.037	0.037	
P2b2	6.66	6.66	
P1b3	$1.67\times 10^{-3}$	$1.67\times 10^{-3}$	
P2b3	17.33	17.33	
P1b5	0.013	0.013	

P2b5	$-7.2 \times 10^{-6}$	$-1.82 \times 10^{-6}$
P1a6	27.27	1.99
P1b6	$2.45 \times 10^{-6}$	$3.77 \times 10^{-6}$
P2b6	11.79	11.79
P1a7	0.0047	0.0018
P2a7	25.91	151.60
P1b7	0.03	0.03
P2b7	53.44	53.44
P1a8	$1.62 \times 10^{-6}$	$7.24 \times 10^{-6}$
P1b8	$1.54 \times 10^{-3}$	$1.54 \times 10^{-3}$
P1a42	1.21	0.10

**Table S27. Sodium channels Phosphorylation Parameters**

Symbol	Value	Units	description	Ref.
$G_{Na,Late}$	8	$mS/\mu F$	Conduction rate of late sodium channels	20
$K_{Dephos}$	$7.19 \times 10^{-4}$	$ms^{-1}$	The unphosphorylation rate of $Na^+$ channels	21
$k_{Phos\_MAX}$	1.07	$ms^{-1}$	The phosphorylation rate of $Na^+$ channels	*

\*The dephosphorylation rate was fit using the experiment data <sup>2</sup>

**Table S28. States variables initial values**

Symbol	Unit	Description	Value
V	mV	Sarcolemmal membrane potential	-84.24
$m_{Na}$		Sodium channel activation gate	0.033
$h_{Na}$		Sodium channel inactivation gate	0.98
$j_{Na}$		Sodium channel slow inactivation gate	0.99
$X_k$		Potassium channel activation gate	$1.89 \times 10^{-4}$
$[Na^+]_i$	mM	Intracellular $Na^+$ concentration	8.12



$[K^+]_i$	mM	Intracellular $K^+$ concentration	136.9
$[Ca^{2+}]_i$	mM	Intracellular $Ca^{2+}$ concentration	$5.08 \times 10^{-5}$
$[Ca^{2+}]_{JSR}$	mM	JSR $Ca^{2+}$ concentration	0.47
$[Ca^{2+}]_{NSR}$	mM	NSR $Ca^{2+}$ concentration	0.47
$[Ca^{2+}]_m$	mM	Mitochondrial free $Ca^{2+}$ concentration	$1.44 \times 10^{-4}$
$x_1$		State 1 of Calcium release	$6.9 \times 10^{-4}$
$x_2$		State 2 of Calcium release	$1.89 \times 10^{-1}$
$x_3$		State 3 of Calcium release	$7.91 \times 10^{-2}$
$x_4$		State 4 of Calcium release	$5.41 \times 10^{-6}$
$x_5$		State 5 of Calcium release	$5.15 \times 10^{-2}$
$x_6$		State 6 of Calcium release	$1.35 \times 10^{-3}$
$x_7$		State 7 of Calcium release	$3.71 \times 10^{-1}$
$x_8$		State 8 of Calcium release	$1.58 \times 10^{-1}$
$x_9$		State 9 of Calcium release	$8.17 \times 10^{-6}$
$x_{10}$		State 10 of Calcium release	$7.77 \times 10^{-2}$
$x_{11}$		State 11 of Calcium release	$6.09 \times 10^{-10}$
$x_{12}$		State 12 of Calcium release	$1.77 \times 10^{-7}$
$x_{13}$		State 13 of Calcium release	$1.26 \times 10^{-6}$
$x_{14}$		State 14 of Calcium release	$8.14 \times 10^{-11}$
$x_{15}$		State 15 of Calcium release	$7.52 \times 10^{-7}$
$x_{16}$		State 16 of Calcium release	$1.71 \times 10^{-10}$
$x_{17}$		State 17 of Calcium release	$4.67 \times 10^{-8}$
$x_{18}$		State 18 of Calcium release	$2.22 \times 10^{-8}$
$x_{19}$		State 19 of Calcium release	$1.71 \times 10^{-11}$
$x_{20}$		State 20 of Calcium release	$1.62 \times 10^{-7}$
$x_{21}$		State 21 of Calcium release	$8.74 \times 10^{-6}$
$x_{22}$		State 22 of Calcium release	$2.55 \times 10^{-3}$

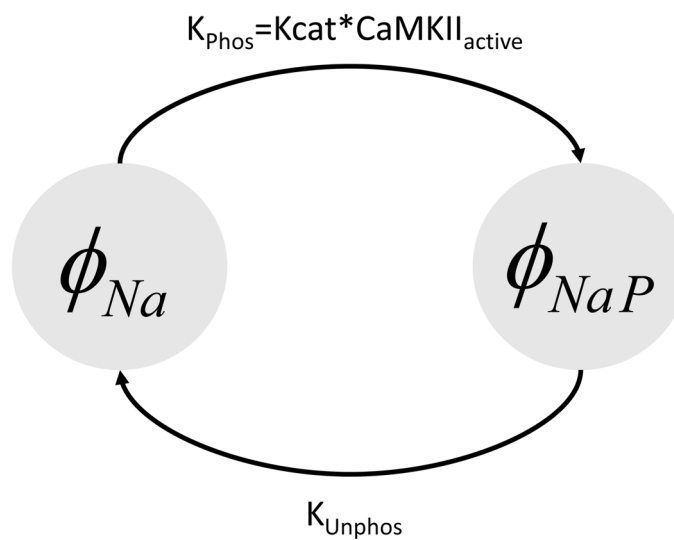
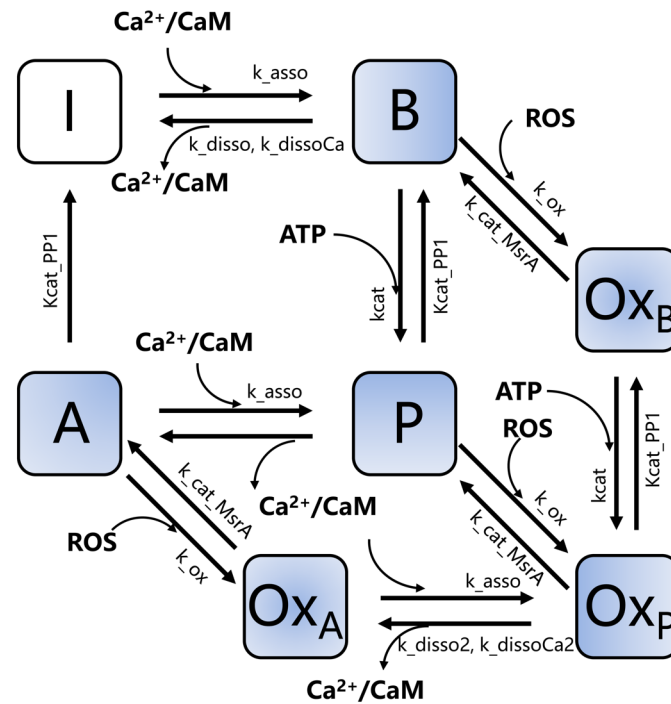
$x_{23}$		State 23 of Calcium release	$2.86 \times 10^{-3}$
$x_{24}$		State 24 of Calcium release	$1.33 \times 10^{-6}$
$x_{25}$		State 25 of Calcium release	$1.23 \times 10^{-2}$
$x_{26}$		State 26 of Calcium release	$4.84 \times 10^{-7}$
$x_{27}$		State 27 of Calcium release	$1.30 \times 10^{-4}$
$x_{28}$		State 28 of Calcium release	$9.42 \times 10^{-5}$
$x_{29}$		State 29 of Calcium release	$2.62 \times 10^{-7}$
$x_{30}$		State 30 of Calcium release	$2.48 \times 10^{-3}$
$x_{31}$		State 31 of Calcium release	$3.54 \times 10^{-5}$
$x_{32}$		State 32 of Calcium release	$9.74 \times 10^{-3}$
$x_{33}$		State 33 of Calcium release	$4.19 \times 10^{-3}$
$x_{34}$		State 34 of Calcium release	$1.16 \times 10^{-6}$
$x_{35}$		State 35 of Calcium release	$1.10 \times 10^{-2}$
$x_{36}$		State 36 of Calcium release	$4.47 \times 10^{-5}$
$x_{37}$		State 37 of Calcium release	$1.23 \times 10^{-2}$
$x_{38}$		State 38 of Calcium release	$5.23 \times 10^{-3}$
$x_{39}$		State 39 of Calcium release	$8.87 \times 10^{-7}$
$x_{40}$		State 40 of Calcium release	$8.46 \times 10^{-3}$
[LTRPNCa]	mM	Ca <sup>2+</sup> bound to low affinity troponin sites	$3.29 \times 10^{-3}$
[HTRPNCa]	mM	Ca <sup>2+</sup> bound to high affinity troponin sites	0.11
[N <sub>0</sub> ]		Non-permissive tropomyosin with 0 cross bridges	0.99
[N <sub>1</sub> ]		Non-permissive tropomyosin with 1 cross bridges	$7.91 \times 10^{-7}$
[P <sub>0</sub> ]		Permissive tropomyosin with 0 cross bridges	$9.07 \times 10^{-7}$
[P <sub>1</sub> ]		Permissive tropomyosin with 1 cross bridges	$9.88 \times 10^{-7}$
[P <sub>2</sub> ]		Permissive tropomyosin with 2 cross bridges	$1.47 \times 10^{-6}$
[P <sub>3</sub> ]		Permissive tropomyosin with 3 cross bridges	$1.28 \times 10^{-6}$
[ATP] <sub>i</sub>	mM	EC coupling linked ATP concentration	7.97

[ATP] <sub>ic</sub>	mM	Cytosolic ATP concentration not linked to EC coupling	7.95
[CrP] <sub>i</sub>	mM	Mitochondrial linked creatine phosphate concentration	15.27
[CrP] <sub>ic</sub>	mM	Cytosolic creatine phosphate concentration	15.28
[ADP] <sub>m</sub>	mM	Mitochondrial ADP concentration	0.010
[NADH]	mM	Mitochondrial NADH concentration	9.18
$\Delta\Psi_m$	mV	Inner mitochondrial membrane potential	131.3
[ISOC]	mM	Isocitrate concentration (mitochondrial)	0.55
[ $\alpha$ KG]	mM	$\alpha$ ketoglutarate concentration (mitochondrial)	$3.79 \times 10^{-5}$
[SCoA]	mM	Succinyl CoA concentration (mitochondrial)	0.18
[Suc]	mM	Succinate concentration (mitochondrial)	$1.15 \times 10^{-4}$
[FUM]	mM	Fumarate concentration (mitochondrial)	0.013
[MAL]	mM	Malate concentration (mitochondrial)	$9.67 \times 10^{-3}$
[OAA]	mM	Oxalacetate concentration (mitochondrial)	$3.35 \times 10^{-8}$
[O <sub>2</sub> <sup>-</sup> ] <sub>p_mito</sub>	mM	O <sub>2</sub> <sup>-</sup> concentration (peri_mito)	$9.45 \times 10^{-7}$
[O <sub>2</sub> <sup>-</sup> ] <sub>SR</sub>	mM	O <sub>2</sub> <sup>-</sup> concentration (peri-SR)	$1.39 \times 10^{-10}$
[O <sub>2</sub> <sup>-</sup> ] <sub>mito</sub>	mM	O <sub>2</sub> <sup>-</sup> concentration (mitochondrial)	0.29
[H <sub>2</sub> O <sub>2</sub> ]	mM	Hydrogen peroxide (cytoplasmic)	$6.70 \times 10^{-7}$
[GSH]	mM	Reduced glutathione (cytoplasmic)	0.99
[CaM <sub>Ca</sub> ]	mM	CaM with one Ca <sup>2+</sup> ion binded	$1.35 \times 10^{-4}$
[CaM <sub>Ca2</sub> ]	mM	CaM with two Ca <sup>2+</sup> ion binded	$1.29 \times 10^{-5}$
[CaM <sub>Ca3</sub> ]	mM	CaM with three Ca <sup>2+</sup> ion binded	$7.02 \times 10^{-9}$
[CaM <sub>Ca4</sub> ]	mM	CaM with four Ca <sup>2+</sup> ion binded	$7.62 \times 10^{-11}$
[B]	mM	CaMKII with Ca <sup>2+</sup> /CaM binded	$7.62 \times 10^{-11}$
[P]	mM	CaMKII with Ca <sup>2+</sup> /CaM binded and being phosphorylated	$1.05 \times 10^{-12}$
[A]	mM	CaMKII with being phosphorylated	$1.03 \times 10^{-16}$

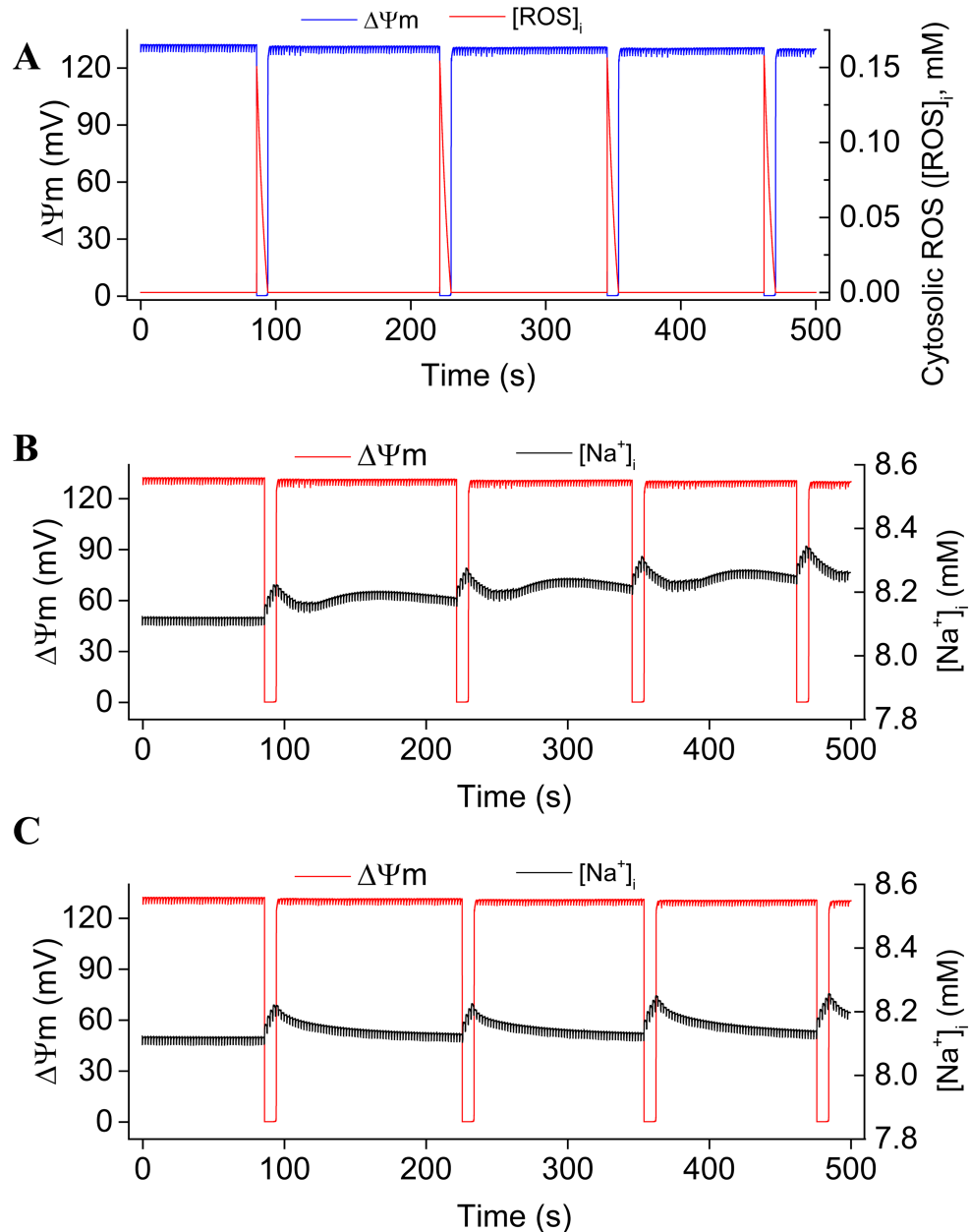
[OxB]	mM	CaMKII with Ca <sup>2+</sup> /CaM binded and being oxidated	4.04×10 <sup>-14</sup>
[OxP]	mM	CaMKII with Ca <sup>2+</sup> /CaM binded and being phosphorylated and oxidated	5.13×10 <sup>-17</sup>
[OxA]	mM	CaMKII with being phosphorylated and oxidated	1.00×10 <sup>-19</sup>
IC3		State of unphosphorylated sodium channels	5.21×10 <sup>-1</sup>
IC2		State of unphosphorylated sodium channels	2.98×10 <sup>-2</sup>
IF		State of unphosphorylated sodium channels	3.71×10 <sup>-5</sup>
IM1		State of unphosphorylated sodium channels	8.37×10 <sup>-3</sup>
IM2		State of unphosphorylated sodium channels	1.33×10 <sup>-4</sup>
C3		State of unphosphorylated sodium channels	4.16×10 <sup>-1</sup>
C2		State of unphosphorylated sodium channels	2.38×10 <sup>-2</sup>
C1		State of unphosphorylated sodium channels	2.96×10 <sup>-5</sup>
O		State of unphosphorylated sodium channels	6.78×10 <sup>-8</sup>
LC3		State of unphosphorylated sodium channels	3.92×10 <sup>-4</sup>
LC2		State of unphosphorylated sodium channels	2.24×10 <sup>-5</sup>
LC1		State of unphosphorylated sodium channels	2.79×10 <sup>-8</sup>
LO		State of unphosphorylated sodium channels	6.39×10 <sup>-11</sup>
IC3'		State of phosphorylated sodium channels	4.19×10 <sup>-1</sup>
IC2'		State of phosphorylated sodium channels	2.39×10 <sup>-2</sup>
IF'		State of phosphorylated sodium channels	2.98×10 <sup>-5</sup>
IM1'		State of phosphorylated sodium channels	7.33×10 <sup>-4</sup>
IM2'		State of phosphorylated sodium channels	7.39×10 <sup>-5</sup>
C3'		State of phosphorylated sodium channels	5.24×10 <sup>-1</sup>
C2'		State of phosphorylated sodium channels	2.99×10 <sup>-2</sup>
C1'		State of phosphorylated sodium channels	3.73×10 <sup>-5</sup>

$O'$	State of phosphorylated sodium channels	$8.54 \times 10^{-8}$
$LC3'$	State of phosphorylated sodium channels	$2.29 \times 10^{-3}$
$LC2'$	State of phosphorylated sodium channels	$1.31 \times 10^{-4}$
$LC1'$	State of phosphorylated sodium channels	$1.63 \times 10^{-7}$
$LO'$	State of phosphorylated sodium channels	$3.74 \times 10^{-10}$
$\phi_{Na}$	The fraction of unphosphorylated $Na^+$ channels	$7.81 \times 10^{-1}$
$\phi_{Na, CaMKII}$	The fraction of phosphorylated $Na^+$ channels	$2.2 \times 10^{-1}$

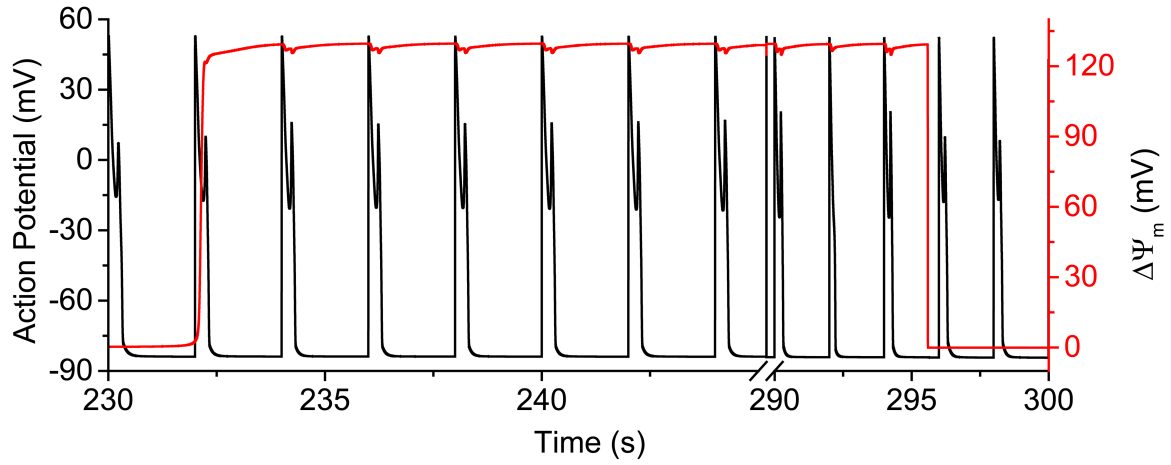
**Figure S1.** Top: The Scheme of CaMKII activation model modified from Foteinou *et al.*<sup>1</sup>. In this model, there is only one inactive state (state I). CaMKII can be activated *via* binding  $\text{Ca}^{2+}/\text{CaM}$ , autophosphorylating, and oxidizing. Bottom: The scheme of Markov model for CaMKII activation-dependent sodium channel phosphorylation. We hypothesized that the phosphorylated rate was proportional to CaMKII autophosphorylation rate and the fraction of activated CaMKII. The dephosphorylation rate was a constant which was fit using the experiment data from Wagner *et al.*<sup>2</sup>. CaMKII:  $\text{Ca}^{2+}$ /calmodulin-dependent protein kinase II; CaM: calmodulin.



**Figure S2.** (A): Increasing *shunt* from 0.02 to 0.1 caused sustained mitochondrial oscillations and cyclic reactive oxygen species (ROS) bursts in a cardiomyocyte. (B): Dynamics of cytosolic  $\text{Na}^+$  concentration ( $[\text{Na}^+]_i$ ) during mitochondrial oscillations in the presence of oxidative CaMKII oxidation. (C): Dynamics of cytosolic  $\text{Na}^+$  concentration during mitochondrial oscillations in the absence of oxidative CaMKII oxidation. CaMKII:  $\text{Ca}^{2+}$ /calmodulin-dependent protein kinase II.

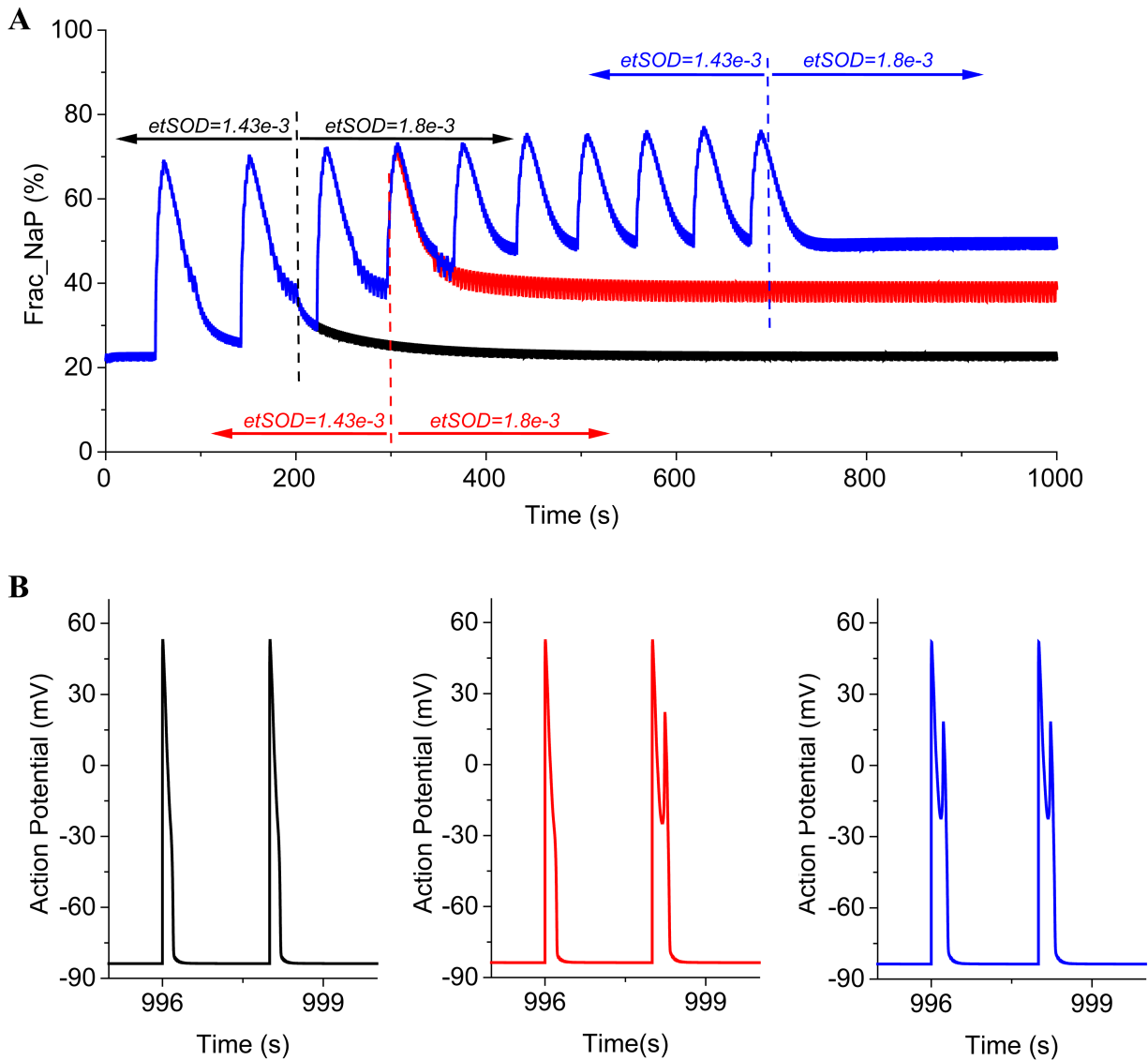


**Figure S3.** After the 3<sup>rd</sup> depolarization, the EADs sustained throughout the whole repolarization phase. *Shunt* = 0.14, PCL = 2s. EADs: early afterdepolarizations; PCL: pacing cycle length.





**Figure S4.** Effect of increasing ROS scavenging (i.e. *et\_SOD*) on mdROS-CaMKII activation-induced EADs. *et\_SOD* was increased from  $1.43 \times 10^{-3}$  mM (baseline value) to  $1.8 \times 10^{-3}$  mM at 200s (black line), 300s (red line), or 700s (blue line). (A): The fraction of phosphorylation sodium channels. (B): Action potentials of the last two beats. *shunt* = 0.14 and PCL = 2s. mdROS: mitochondrial-derived reactive oxygen species; CaMKII:  $\text{Ca}^{2+}$ /calmodulin-dependent protein kinase II; EADs: early afterdepolarizations; PCL: pacing cycle length.



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