

RESEARCH ARTICLE

Empirical mode decomposition processing to improve multifocal-visual-evoked-potential signal analysis in multiple sclerosis

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Abstract

Objective

To study the performance of multifocal-visual-evoked-potential (mfVEP) signals filtered using empirical mode decomposition (EMD) in discriminating, based on amplitude, between control and multiple sclerosis (MS) patient groups, and to reduce variability in interocular latency in control subjects.

Methods

MfVEP signals were obtained from controls, clinically definitive MS and MS-risk progression patients (radiologically isolated syndrome (RIS) and clinically isolated syndrome (CIS)). The conventional method of processing mfVEPs consists of using a 1–35 Hz bandpass frequency filter (X_{DFT}).

The EMD algorithm was used to decompose the X_{DFT} signals into several intrinsic mode functions (IMFs). This signal processing was assessed by computing the amplitudes and latencies of the X_{DFT} and IMF signals (X_{EMD}). The amplitudes from the full visual field and from ring 5 (9.8–15° eccentricity) were studied. The discrimination index was calculated between controls and patients. Interocular latency values were computed from the X_{DFT} and X_{EMD} signals in a control database to study variability.

Results

Using the amplitude of the mfVEP signals filtered with EMD (X_{EMD}) obtains higher discrimination index values than the conventional method when control, MS-risk progression (RIS and CIS) and MS subjects are studied. The lowest variability in interocular latency computations from the control patient database was obtained by comparing the X_{EMD} signals with the X_{DFT} signals. Even better results (amplitude discrimination and latency variability) were obtained in ring 5 (9.8–15° eccentricity of the visual field).

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Conclusions

Filtering mfVEP signals using the EMD algorithm will result in better identification of subjects at risk of developing MS and better accuracy in latency studies. This could be applied to assess visual cortex activity in MS diagnosis and evolution studies.

Introduction

MfVEP

The visual-evoked-potentials (VEP) test is a diagnostic tool that allows an objective assessment of the visual pathway. The conventional visual evoked potential (cVEP) measures the electrophysiological signals obtained by stimulating the full visual field using flash or checker-board stimuli. The cVEP produces an overall response in the primary visual cortex [1], but it does not provide specific topographical information about the retina and visual cortex [2].

The multifocal-visual-evoked-potentials (mfVEP) technique permits analysis of the topographical features of different sectors of the visual field represented in the visual cortex [3,4]. Several studies [5–7] have shown how the mfVEP technique overcomes most of the limitations of conventional VEPs because it allows for the simultaneous recording of local responses from many visual field sectors (up to 120).

The mfVEP technique has already been shown to be more sensitive than standard automated perimetry for the early detection of visual field defects in multiple sclerosis (MS) [8,9] and other optic neuropathies, such as glaucoma [2].

It is known that the mfVEP signal-to-noise ratio (SNR) is a significant limiting factor for further development of clinical application of mfVEPs, mainly because the amplitudes of the signal recorded are very small compared with cVEP.

In this context, various studies have attempted to improve the diagnostic capacity of the mfVEP technique either by enhancing the visual stimulus parameters [10], by altering the number of electrodes used and their localization, by adding virtual channels [11], by investigating offline signal processing methods such as principal component analysis [12], by using wavelets [13] or by applying Prony's method as a filter [14].

MfVEP analysis

Amplitude and latency are the mfVEP signal parameters most frequently used in clinical analysis. MfVEP signal amplitude can be calculated using the difference between the positive peak and the negative trough (peak-to-trough or P2T). P2T has the advantage of being a quantifiable output value (measured in volts) [13,15]. P2T amplitude decline is proportional to the risk of MS [16]. Moreover, an inverse relationship was found between retinal nerve fiber layer thickness—as measured by optical coherence topography—and P2T [15].

MfVEP latency is measured as the delayed conduction of the visual stimulus from the moment it is presented on the screen to the instant it is elicited in the visual cortex. Interocular (IO) latency is defined as the difference between the response latencies of both eyes and is measured as the subtraction between the second-highest peak implicit time [17] or as the temporal shift producing the best cross-correlation value [18].

Delays in mfVEP latency signals are usually observed after an optic neuritis (ON) episode, reflecting optic nerve fiber demyelination, whereas shortening of the latency represents

remyelination processes [19,20]. Interocular latency measurements are especially useful in the case of unilateral ON because a normal contralateral eye serves as a good control reference.

Empirical mode decomposition

Empirical mode decomposition (EMD) has been proposed [21] as an adaptive time–frequency data analysis method. This method decomposes a signal into a sum of oscillatory modes (IMF_1, IMF_2, \dots), called intrinsic mode functions (IMFs), which represent fast to slow oscillations in the signal.

The method successively obtains the highest frequencies (IMF_1, IMF_2, \dots) from a signal, so it is equivalent to a bank of filters of overlapping frequency content. In the electroencephalography (EEG) field, in reference [22] the authors demonstrated that IMF_1 represents the gamma band neuronal oscillation (>30 Hz), IMF_2 represents beta band oscillation (13–30 Hz), IMF_3 represents the alpha band oscillation (8–13 Hz), IMF_4 represents the delta band (3.5–8 Hz) oscillation, and IMF_5 and IMF_6 represent the theta band oscillation (0.5–3.5 Hz).

Typical advanced methods used to process biomedical signals include Fourier [23] and wavelet analysis. These two methods need some predefined basis functions to decompose a signal. In contrast, the EMD method does not require a prior known basis. Comparisons with Fourier and wavelet analyses show that EMD obtains much better temporal and frequency resolutions [24,25].

EMD has been applied to the study of the non-linear and non-stationary properties of time series and has been shown to be a reliable and effective method in the processing of different biomedical engineering signals: enhanced ECG to detect QRS waves [26], detection of components that might be related to phoneme representation in the brain [27], EEG artifact removal [28], and detection and classification of retinal diseases from electroretinogram signals [29]. The authors of [30] used EMD to analyze the neuronal activity of a macaque V4 visual cortex area, showing that evoked potentials can be resolved into a sum of intrinsic components; in a similar experiment, [25] showed that EMD may offer better temporal and frequency resolution in comparison with Fourier analysis. The authors of [31] used EMD to separate EEG components and detect VEPs in EEG signals.

Aim of this work

The aim of this work was to test, for the first time, application of the EMD preprocessing method to mfVEP signals to improve MS diagnosis.

For this purpose, two experiments were proposed: a) evaluation of the ability to discriminate between mfVEP signals recorded from subjects with different degrees of MS affection by using the amplitude and b) study of the variability of interocular latency in control subjects.

In the first experiment, we aimed to examine how the amplitude, quantified as P2T, of original and EMD-processed mfVEP signals could be applied to the diagnosis of MS. The difficulty of predicting which patients will develop clinically definite MS currently presents a diagnostic and therapeutic dilemma [32]. This relationship was studied in a cohort of patients with radiologically isolated syndrome (RIS), clinically isolated syndrome (CIS) and clinically definite MS.

In this field, [33] has shown that the mfVEP amplitude, quantified as SNR, performs best at discriminating MS-risk subjects when applied to the visual field (9.8–15° eccentricity, ring 5).

In the second experiment, a comparison of the variability of interocular latency values was made between the mfVEP signals filtered using the standard method and the signals processed using the EMD method.

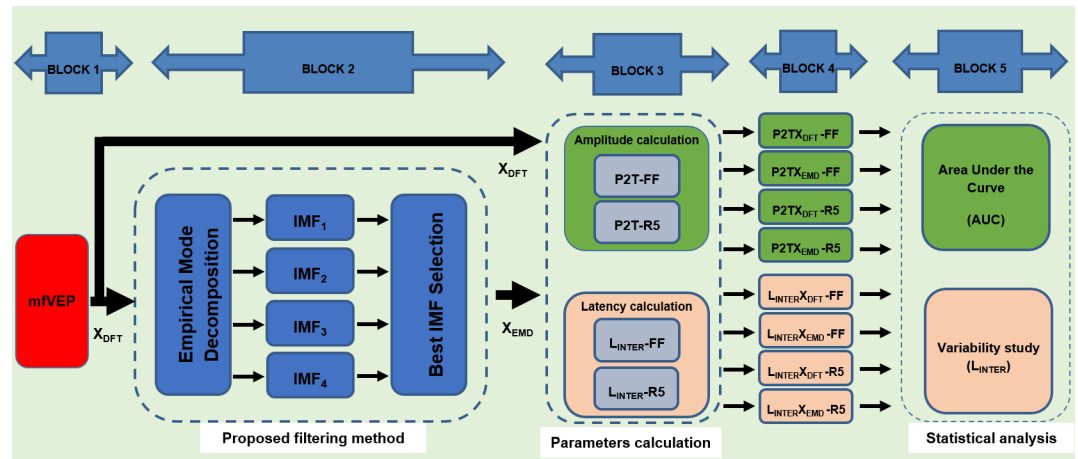


Fig 1. General diagrams of the blocks.

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Patients and methods

Fig 1 shows a general diagram of the methods used in this research. Briefly, the main blocks are as follows:

BLOCK 1. Represents the typical mfVEP signal-processing method: the mfVEPs of the study participants are recorded, the raw records are digitally filtered by frequency, and the best channel (X_{DFT}) for each sector is selected according to the SNR.

BLOCK 2. The EMD decomposition method is applied to X_{DFT} signals in the 45–150 ms interval (signal window).

BLOCK 3. In each sector, only the IMF with the highest amplitude value (quantified as P2T) is selected (X_{EMD}) and the other IMFs are discarded.

BLOCK 4. Amplitudes and latencies are computed at several locations in the visual fields (full field and ring 5) of the X_{DFT} and X_{EMD} signals.

BLOCK 5. The discrimination index between controls and patient groups is obtained for the amplitude values. The variability of interocular latency is studied only in the control group. The amplitude and latency results are compared and statistical study is performed.

Patient database

One cohort of patients with clinically definite MS (n = 28) and two other groups at different relative risks of developing MS—classified as RIS (n = 15) and CIS (n = 28)—were included in this study [34] and compared with a normal, control, age-matched subject group (n = 24) (Table 1).

Table 1. Patient demographics.

	Controls	RIS	CIS	MS
Subjects (n)	24	15	28	28
Age (years) mean ± SD	30.3±7.6	39±7.8	30.3±9.6	34.4±10.1
Male:female ratio	10:14	5:10	10:18	7:21
ON-affected eyes	0 (0%)	0 (0%)	12 (21.4%)	37 (66%)
non-ON eyes	48 (100%)	30 (100%)	44 (78.6%)	19 (34%)

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RIS subjects are defined as having white-matter anomalies of the central nervous system (CNS)—detected by magnetic resonance imaging (MRI)—that do not account for clinically apparent impairments [35].

CIS subjects are defined as having had a first clinical episode suggestive of CNS demyelination involving the optic nerve, brainstem, spinal cord or other topography not attributable to other inflammatory diseases but lacking radiological evidence of dissemination of lesions over time [36]. It is known that more than 80% of CIS patients who present lesions assessed using MRI eventually develop MS, whereas approximately 20% follow a self-limited process [37].

Clinically definite MS patients were diagnosed according to the McDonald criteria [38].

CIS and MS patients were divided into two subgroups—ON eyes and non-ON eyes—according to whether they had had prior clinical ON episodes.

This study protocol was approved by the Institutional Review Boards of Universidad de Alcalá-affiliated hospitals and adhered to the tenets of the Declaration of Helsinki. All participants provided written informed consent.

Multifocal visual evoked potentials (mfVEPs)

The typical mfVEP recording and analysis method (Fig 1, BLOCK 1) is represented in detail in Fig 2. Briefly [2,39], mfVEP recordings were obtained using VERIS software 5.9 (Electro-Diagnostic Imaging, San Mateo, USA). The stimulus was a scaled dartboard with a 44.5° diameter containing 60 sectors with 16 alternating checks each—eight white (luminance: 200 cd/m²) and eight black (luminance: <3 cd/m²)—and a Michelson contrast of approximately 99%. The sectors were cortically scaled with eccentricity to stimulate approximately equal areas of the

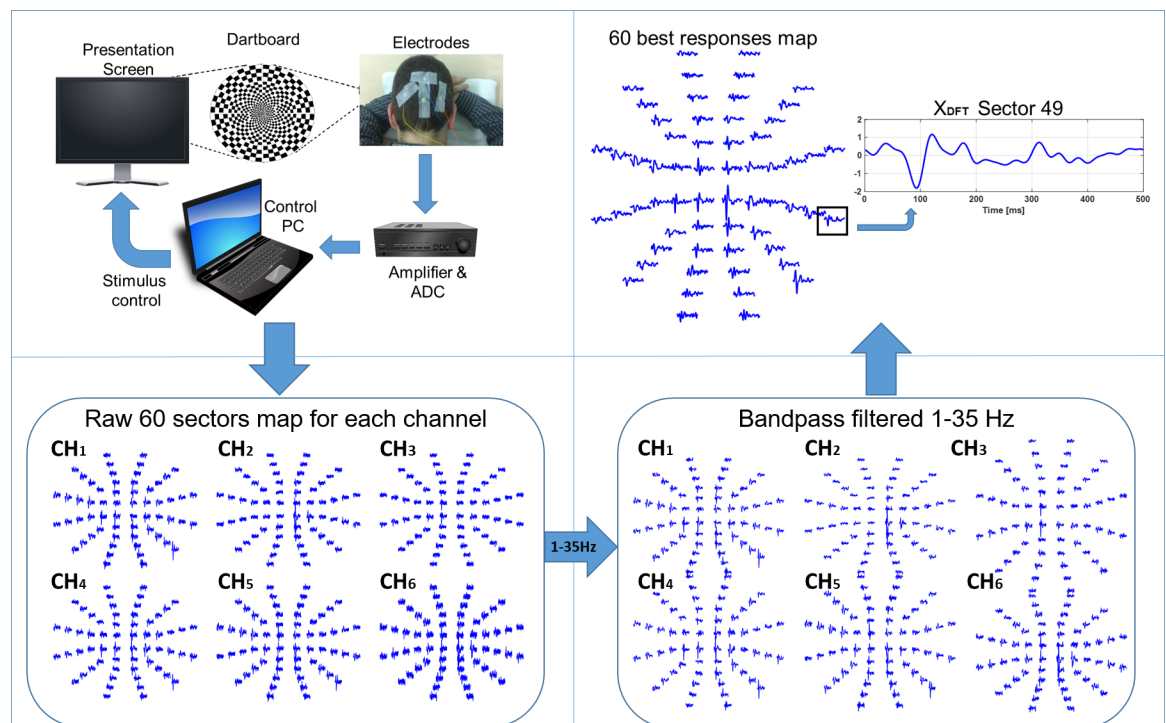


Fig 2. Typical mfVEP analysis method. Upper left: stimulus and recording process; lower left: 60-sector signal map for each of the six channels; lower right: 60-sector signal map for each of the six channels after 1–35Hz bandpass filtering; upper right: 60-sector signal map for the best channel of each sector and signal for one sector.

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visual cortex. The dartboard pattern was reversed according to a pseudorandom m-sequence at a frame rate of 75 Hz [2].

Three channels were obtained using gold cup electrodes (impedance <2 kΩ). For the mid-line channel, the electrodes were placed 4 cm above theinion (active), at theinion (reference), and on the forehead (ground). For the other two channels, the active electrodes were placed 1 cm above and 4 cm on either side of theinion. By taking the difference between pairs of channels, three additional derived channels were obtained, effectively resulting in six channels in each sector (CH₁ . . . CH₆). The length of the recording was 500 ms, and the sample frequency was 1,200 Hz. The signal was analog-amplified (gain: 10⁵, bandwidth: 3–100 Hz) and digital-bandpass-filtered (using a fast Fourier transform: 1–35 Hz).

The recording was divided into two different intervals: the signal window (45–150 ms), which contains the evoked potential response, and the noise window (325–430 ms), which essentially contains noise.

The SNR of each waveform was calculated as $SNR = \log_{10}[\text{RMS}(45\text{--}150 \text{ ms}) / \text{mean}[\text{RMS}(325\text{--}430 \text{ ms})]]$, where RMS(45–150 ms) is the root mean square (RMS) amplitude of the waveform in the signal, and mean[RMS(325–430 ms)] is the average RMS amplitude of all 60 waveforms in the noise window (40). The channel with the highest SNR (“best channel”) was selected in each sector (noted as X_{DFT}).

Empirical mode decomposition processing method

Empirical mode decomposition decomposes a non-periodic and non-stationary signal X_{DFT}(t) into a finite number of intrinsic mode functions and a residue (Eq 1).

$$X_{DFT}(t) = \sum_{j=1}^N IMF_j(t) + r_N(t) \tag{1}$$

N denotes the total number of IMFs, IMF_j(t) is the jth IMF and r_N(t) is the residue selecting N IMFs.

The IMFs must satisfy two main conditions: 1) The number of extremes and the number of zero crossings must be equal or differ by no more than one in the whole dataset; and 2) the mean value of the envelope defined by the local maximum and the envelope defined by the local minimum must be zero at any point (IMFs are nearly periodic functions with zero mean).

First, x(t) = X_{DFT}(t) (where x(t) is the input signal) and the IMFs were extracted using the four-step method below:

- a) Find all extreme points (maxima and minima) of x(t);
- b) Generate the upper and lower envelopes (UE and LE) by interpolation of the maxima and minima with a cubic spline;
- c) Compute the mean: $M(t) = \frac{UE(t)+LE(t)}{2}$; and
- d) Subtract the mean from the original signal: $c(t) = x(t) - M(t)$.

This process was iterated until the resulting signal c(t) complied with the criteria of an intrinsic mode function. At this point, IMF₁ = c(t) and the residue r(t) = x(t)-c(t) became the new input signal for step (a) (x(t) = r(t)).

The number of extreme points decreases as the number of previous loop iterations increases. This algorithm stops when r(t) contains one extreme (maxima or minima) or when four IMFs are computed. An example of an mfVEP signal decomposed into IMF₁–IMF₄ is shown in Fig 3.

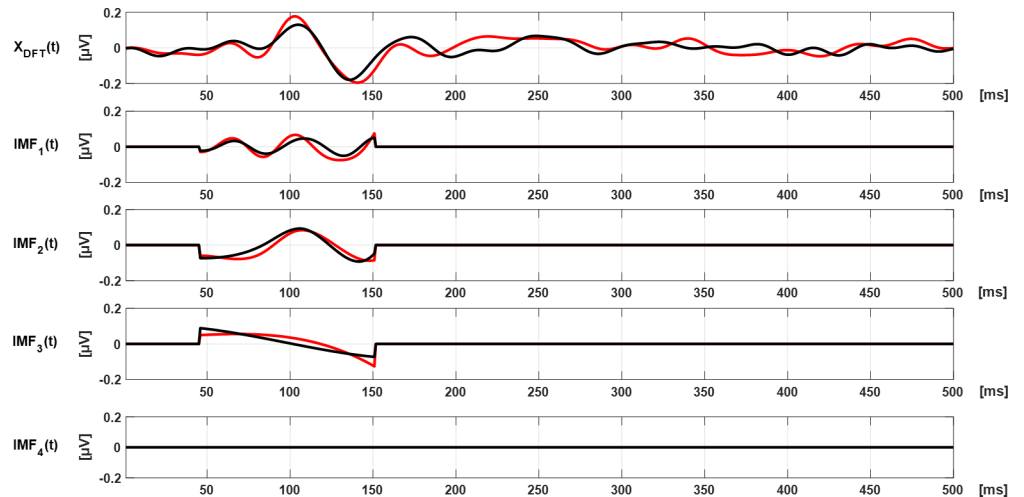


Fig 3. Original signal and IMF₁–IMF₄ from the OD (black) and OS (red) from a control subject.

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EMD-based mfVEP filtering method

The EMD method is applied to the X_{DFT} signal in the signal window interval $X_{DFT}(45-150)$ ms). The number of IMFs computed (N) is selected according to the results shown in Fig 4. This figure shows the IMFs obtained from the average of all the cases in the control database (24 subjects, 2 eyes, 60 sectors, 6 channels). The fourth IMF (IMF₄) and the residue ($r_4(t)$) are considered negligible.

Fig 4 also shows each IMF in the frequency domain. As stated in the EMD method, the first IMF is the highest frequency and, as long as the IMF number is increased, the main frequency peak is presented in a lower frequency.

EMD is similar to a frequency bank filter. Consequently, there are several filter options depending on which IMFs are selected and which IMFs are discarded. In this paper, only the IMF with the highest P2T amplitude in the signal window is selected (“winner takes all” approach, Fig 5). This IMF (noted as X_{EMD}) was considered the filtered signal using the EMD method.

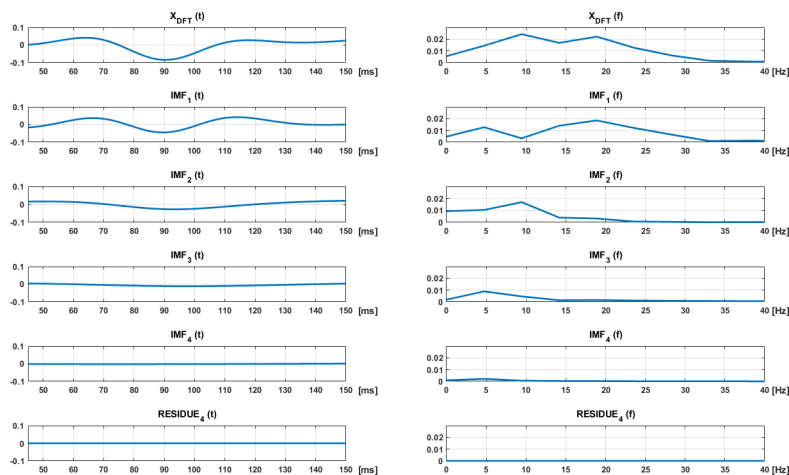


Fig 4. EMD and residues obtained when all the signals in the control database are averaged. Time (left) and frequency (right).

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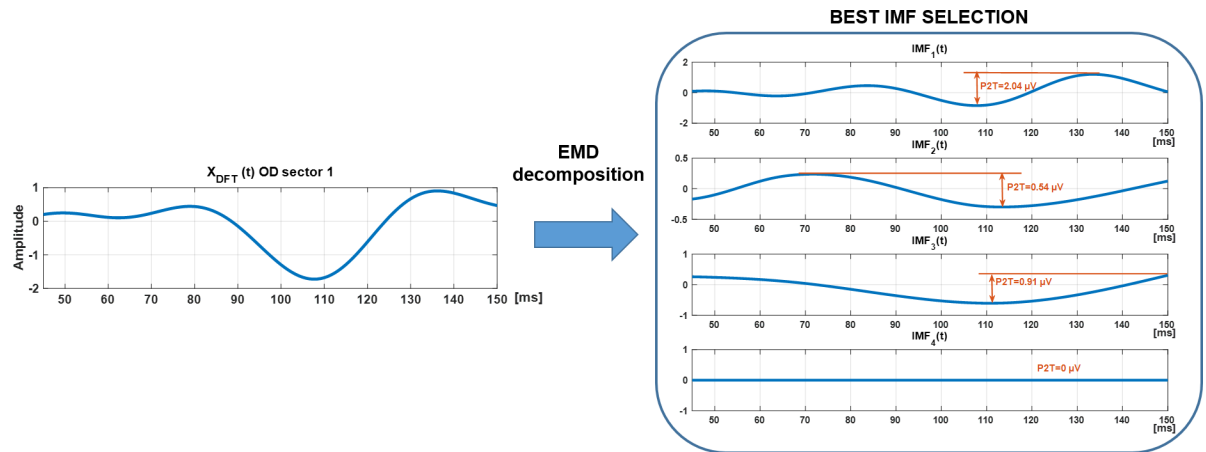


Fig 5. Example of Best IMF selection (OD, sector 1). Highest P2T values is presented in IMF1 so this one is selected as the Best IMF.

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MfVEP amplitude analysis

The amplitude (P2T) and latency parameters of the signal obtained were computed using the conventional mfVEP analysis method (X_{DFT}) and the signals were filtered using EMD (X_{EMD}). These parameters were analyzed for both the responses of all 60 recorded sectors (full visual field) and for ring 5 located at 9.8° and 15° eccentricity containing twelve sectors. Fig 6 shows the full field map of X_{DFT} and X_{EMD} signals from a control subject as an example.

MfVEP signal amplitude, quantified as P2T, is the difference between the positive peak and the negative trough in the signal window (45–150 ms). An example is detailed in Fig 5.

MfVEP latency analysis

Interocular latency is defined as the mfVEP response delay between both eye signals ($L_{INTER} = L_{OS} - L_{OD}$). Measuring the latency comprises the following steps (Fig 7).

- a. The channel selected in each sector to compute the latency must be the same for both eyes [40]. Thus, the channel that maximizes the sum of SNRs from both eyes is selected

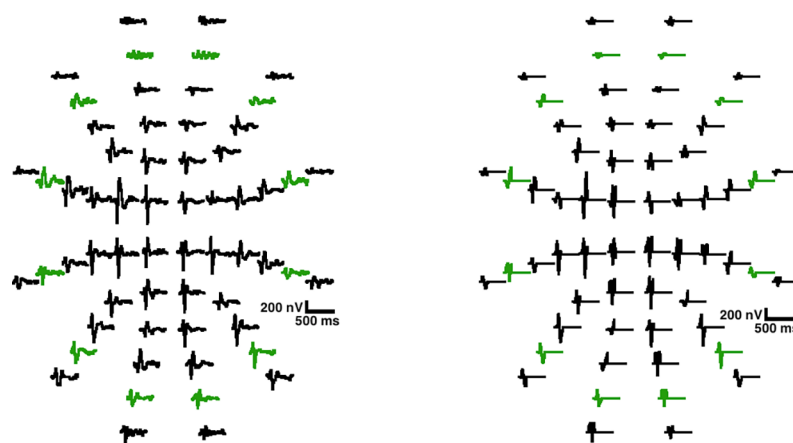


Fig 6. Example X_{DFT} and X_{EMD} . Ring 5 signals are colored in green.

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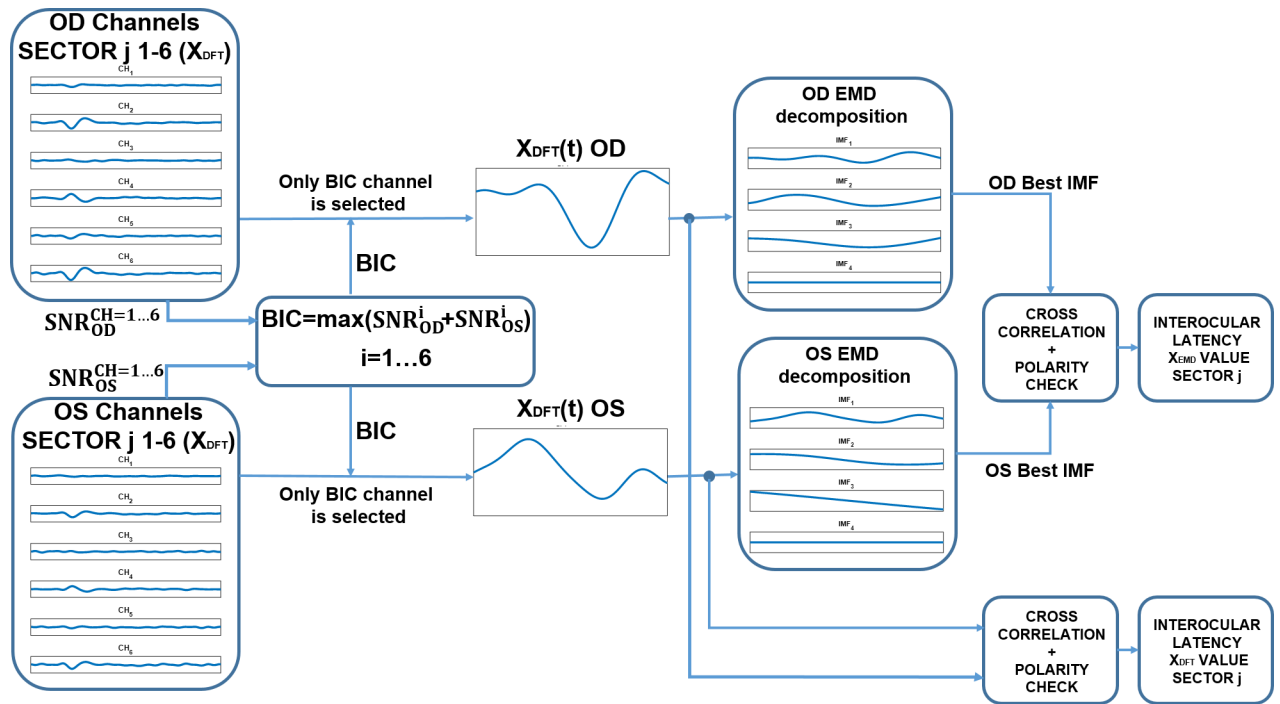


Fig 7. Interocular latency computation flow.

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(Eq 2) and is noted as best interocular channel (BIC).

$$BIC = \max(SNR_{OD}^i + SNR_{OS}^i), \quad i = 1 \dots 6 \quad (2)$$

- b. X_{DFT} signals from the BIC channel of each eye and sector are decomposed into IMFs as previously explained (Fig 1 BLOCK 2 and BLOCK 3).
- c. The normalized cross-correlations are calculated between the pair of conventional signals (X_{DFT-OD} , X_{DFT-OS}) and between the pair of IMFs (X_{EMD-OD} , X_{EMD-OS}). The estimated latency is given by the negative of the lag for which the normalized cross-correlation has the largest absolute value. This step is based on the method described by Hood [41].
- d. The correlation coefficient between the two signals (OD, OS) is computed to avoid reverse polarity. If this coefficient is negative, the signals are classified as a non-analyzable sector (NAS) and discarded. To obtain the final IO latency for the controls, the IO values of all sectors contained in each zone (full visual field or ring 5) are averaged.

Variability study (latencies)

Interocular latency should be essentially zero ($L_{INTER} \approx 0$ ms) in normal subjects [17,42].

As a statistical measure, intra- and intersubject coefficients of variability were used to compare latencies computed with X_{DFT} and X_{EMD} . The intrasubject variability coefficient (CV_{INTRA}) was computed (Eq 3) as the mean of the coefficient of variability for each subject (Eq 4). The intersubject variability (CV_{INTER}) of latency was calculated as the standard deviation from all subjects'

latency differences divided by the mean latency difference of all subjects (Eq 5).

$$CV_{INTRA} = Mean(CV_subject^{i=1...24}) \tag{3}$$

$$CV_subject^i = \frac{Standard_Deviation_{BETWEEN_ALL_SECTORS_SUBJECT_i}}{Mean_{BETWEEN_ALL_SECTORS_SUBJECT_i}} \tag{4}$$

$$CV_{INTER} = \frac{Standard_Deviation_{ALL\ THE\ SUBJECTS\ OF\ THE\ DATABASE}}{Mean_{ALL\ THE\ SUBJECTS\ OF\ THE\ DATABASE}} \tag{5}$$

Discrimination index (amplitudes)

The discrimination index quantifies the ability to discriminate between controls and patients at different risk of the disease (RIS, CIS and MS). This capacity was evaluated using receiver operating characteristic (ROC) analysis [43]. An ROC curve shows sensitivity against the false positive rate (FPR = 1-specificity) for all possible decision thresholds. The area under the ROC curve (AUC) quantifies the overlaps between P2T value distributions. An AUC value of 0.5 implies that the P2T distributions in both diagnosed groups overlap. AUC values above 0.9 indicate high diagnostic accuracy [44]. AUC values are obtained for X_{DFT} and X_{EMD} signal amplitudes in the full visual field and in the ring 5 eccentricity.

Statistical analysis

The statistical analysis and study design were based on published recommendations for ophthalmological research [45,46]. The SPSS Version 13 software application (SPSS Inc., Chicago, IL, USA) was used to perform statistical analysis.

The Kolmogorov–Smirnov test was used to determine whether the distribution was normal. A two-sample Student’s t-test was used to evaluate whether the means of two populations were significantly different. The unpaired t-test was used when the two populations were independent, and the paired t-test was used when each value in a group corresponded directly to a value in the other group. One-way ANOVA combined with Tukey’s post-hoc analysis were used to find means that were significantly different in comparisons among more than two groups.

Results

Best IMF study

IMF waveforms were obtained for the 22 controls (2 eyes, 6 channels and 60 sectors). All the computed IMFs were then averaged and represented in Fig 4. Since it is possible to check that the main components are IMF₁₋₃, it makes sense to compute only the first four IMFs and to discard the residue.

Table 2 shows the proportion of time each IMF was selected (% in controls) as the best IMF along with the spectral averaged maximum peak frequency. IMF₁ (peak frequency of 18.9 Hz) was consistently the best IMF (63.14%), and IMF₄ was never found to be the best IMF.

Table 2. Percentage of time as best IMF and maximum peak frequency.

	Original	X _{EMD} decomposed signals			
	X _{DFT}	IMF ₁	IMF ₂	IMF ₃	IMF ₄
% best IMF	—	63.14%	34.73%	2.12%	0.00%
Max peak (spectrum)	9.45 Hz	18.9 Hz	9.5 Hz	4.72 Hz	4.72 Hz

<https://doi.org/10.1371/journal.pone.0194964.t002>

Table 3. P2T measured for each study group. The values are shown as the mean ± SD.

AMPLITUDE [μV]		CONTROL	RIS	CIS		MS		Mean
				ON	non-ON	ON	non-ON	
FF	ORIGINAL X_{DFT}	0.66±0.11	0.56±0.10	0.42±0.11	0.55±0.09	0.46±0.11	0.48±0.14	0.55±0.13
	BEST IMF X_{EMD}	0.62±0.10	0.48±0.11	0.34±0.09	0.48±0.08	0.41±0.10	0.44±0.13	0.48±0.15
R5	ORIGINAL X_{DFT}	0.59±0.11	0.37±0.10	0.20±0.06	0.28±0.08	0.22±0.07	0.24±0.09	0.34±0.16
	BEST IMF X_{EMD}	0.53±0.10	0.35±0.09	0.19±0.06	0.26±0.07	0.21±0.07	0.22±0.09	0.30±0.30
Mean		0.59±0.13	0.41±0.14	0.27±0.14	0.38±0.15	0.31±0.14	0.33±0.16	—

<https://doi.org/10.1371/journal.pone.0194964.t003>

P2T value analysis

Table 3 shows the P2T values obtained after analyzing all mfVEP-aggregated responses (Full Field: FF) and the eccentric ring 5 (R5) sectors).

The means were computed using the values from all eyes in the respective group (it is not a mean of means).

A higher significant amplitude ($p < 0.05$) was obtained from the control subjects (0.59 ± 0.13) than from the patients—RIS (0.41 ± 0.14), CIS (ON = 0.27 ± 0.14 , non-ON = 0.38 ± 0.15) and MS (ON = 0.31 ± 0.14 , non-ON = 0.33 ± 0.16) groups—in the mean value of the four methods analyzed: $FF_{ORIGINAL}$, FF_{BEST_IMF} , $R5_{ORIGINAL}$ and $R5_{BEST_IMF}$.

Significantly lower values ($p < 0.05$) were obtained when the best IMF was used in the FF ($FF_{ORIGINAL} = 0.55 \pm 0.13 > FF_{BEST_IMF} = 0.48 \pm 0.15$) and R5 ($R5_{ORIGINAL} = 0.34 \pm 0.16 > R5_{BEST_IMF} = 0.30 \pm 0.30$) owing to the IMF extraction method.

P2T values were significantly lower ($p < 0.05$) in ring 5 than the full-field aggregated mfVEP responses for both original signals ($FF_{ORIGINAL} = 0.55 \pm 0.13$ vs. $R5_{ORIGINAL} = 0.34 \pm 0.16$) and the best IMF ($FF_{ORIGINAL} = 0.48 \pm 0.15$ vs. $R5_{ORIGINAL} = 0.30 \pm 0.30$).

There were no significant differences ($p > 0.05$) among the mean values for CIS-ON (0.27 ± 0.14), MS-ON (0.31 ± 0.14) and MS-non-ON (0.33 ± 0.16) obtained using the four methods analyzed.

Discrimination index

Table 4 shows the AUC values, among all study cohorts, when the X_{DFT} signal and best IMF were used. The AUC was computed between the control and the groups of patients. As a

Table 4. AUC values for RIS, CIS and MS groups.

AUC values		RIS	CIS		MS		Mean
			ON	non_ON	ON	non_ON	
FF	ORIGINAL X_{DFT}	0.66	0.91	0.84	0.94	0.86	0.84
	BEST IMF X_{EMD}	0.68	0.92	0.86	0.95	0.90	0.86
R5	ORIGINAL X_{DFT}	0.73	0.95	0.92	0.94	0.92	0.89
	BEST IMF X_{EMD}	0.76	0.98	0.94	0.97	0.95	0.92
Mean		0.71	0.89	0.89	0.95	0.91	—

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Table 5. L_{INTER} : Mean interocular latency values for control patients; NAS: Percentage of non-analyzable sectors; CV_{INTER} : Intersubject coefficient of variability; CV_{INTRA} : Intrasubject coefficient of variability; FF: Full field; R5: Ring 5.

Latency		L_{INTER} (ms)	NAS %	CV_{INTER}	CV_{INTRA}
FF	Standard X_{DFT}	-0.52	9.62	4.66	50.64
	BEST IMF X_{EMD}	-0.42	10.76	2.29	42.67
R5	Standard X_{DFT}	0.29	14.02	3.05	40.54
	BEST IMF X_{EMD}	0.24	14.77	1.9	35.74

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general rule, the AUC index increased with higher MS risk. The highest mean discrimination capacity was seen between the control and the MS-ON group ($\overline{AUC} = 0.95$). The lowest mean was seen for RIS patients ($\overline{AUC} = 0.71$), ($p < 0.05$).

If the results are compared by method, for all cases the AUC values were higher when X_{EMD} signals were used. The AUC values obtained in ring 5 were higher than the full field values for all cases. The highest mean discrimination capacity was seen in ring 5 when the X_{EMD} signals were used ($\overline{AUC} = 0.92$), ($p < 0.05$).

Interocular latencies

Table 5 shows the IO latency results obtained for the control cohort: the mean interocular value (L_{INTER}), the NAS and the inter- and intrasubject variability.

All mean L_{INTER} s are very close to 0 ms, with the value computed using IMF signals in ring 5 ($L_{INTER} = 0.24$ ms) being the closest. No significant differences were found among L_{INTER} values ($p > 0.05$) between methods and zones.

The standard method applied to the full field showed the lowest number of non-analyzable sectors (9.62%) because this case presents the highest SNR values.

X_{EMD} in ring 5 showed the lowest values regarding intersubject ($CV_{INTER} = 1.9$) and intra-subject ($CV_{INTRA} = 35.74$) variability.

For the intersubject CV, no statistical study was performed because, as it is merely a ratio between the standard deviation and the mean of the entire database, only one value was computed ((5).

Significant differences ($p < 0.05$) between zones (full field vs. ring 5) and methods (X_{DFT} vs. X_{EMD}) were found for the intrasubject coefficient of variability.

Discussion

The present study demonstrates that filtering mfVEP signals using the EMD method improves the data-analysis process when applied to diagnosis of MS. Using the amplitude of mfVEP signals (quantified as P2T) filtered with EMD obtains higher discrimination index values than using the conventional method when control, MS-risk progression (RIS and CIS) and MS subjects are studied. Moreover, the interocular latency computation method (cross-correlation [18]) obtains more reliable values if the signals were previously filtered using EMD.

The EMD method decomposes a signal into several IMFs ordered by frequency from high to low. In the mfVEP technique, since the evoked response is presented in the signal window (45–150 ms), the IMF with the highest amplitude value (P2T) in this interval is selected. We believe that the good results presented in this paper derive from the fact that the performance of EMD is similar to that of a bank filter, where each IMF is bandwidth-limited and can be

identified as one of the frequency bands of the signal. Since mfVEP components have a low voltage, they are obscured by EEG background activity, making it necessary to define a robust method to extract bands that best describe these potentials of interest (31).

The results from control subjects presented in Table 2 demonstrate that mfVEP signals can be approximated to the first four IMFs. The IMF with the highest P2T value in the signal window is selected as the best IMF. The first IMF (IMF₁) is selected as the best IMF in 63.14% of the cases and presents a peak amplitude of 18.9 Hz in the averaged spectrum. IMF₂ is selected as the best IMF in 34.73% of the cases and presents a peak amplitude of 9.5 Hz in the averaged spectrum.

The amplitude P2T values and trends agree with previous papers [16]. These authors have shown that non-ON eye amplitudes of patients with unilateral ON were significantly lower in both CIS and MS when compared with the control.

The mean results (X_{DFT} , X_{EMD} , both in ring 5 and the full field) also demonstrated this tendency: $P2T_{CONTROL} = 0.59 \pm 0.13$, $P2T_{CIS-non-ON} = 0.38 \pm 0.15$ and $P2T_{MS-non-ON} = 0.33 \pm 0.16$, $p < 0.05$. No significant differences were observed among MS-ON, MS-non-ON and CIS-ON eyes because most non-ON eyes have been shown to be subclinically affected in CIS and clinically definite MS [32].

The lowest P2T values were obtained in CIS-ON (0.27 ± 0.14 , $p < 0.05$) eyes because they had a recent ON episode and consequently the amplitudes were still low and recovering. Thus, amplitude P2T values were able to discriminate ($p < 0.05$) CIS-ON (0.27 ± 0.14) eyes from CIS-non-ON eyes (0.38 ± 0.15).

A higher discrimination index (AUC) was achieved when signals filtered with EMD were used when compared with non-EMD-filtered signals (Table 4). The higher the risk of suffering MS, the higher the discrimination index obtained: ($\overline{AUC}_{RIS} = 0.71$) < ($\overline{AUC}_{CIS-ON} = 0.89$) < ($\overline{AUC}_{MS-ON} = 0.95$).

The best mean discrimination index was obtained when using IMFs on ring 5 sectors ($\overline{AUC}_{IMF_{R5}} = 0.92$), significantly improving the SNR analysis obtained in our previous work ($\overline{AUC}_{SNR_{R5}} = 0.89$) [33]. The main difference is that in our previous work the AUC values were computed using the typical SNR parameter. The innovation in this new paper is the use of empirical mode decomposition.

Other SNR analyses [18,39] have been tested in MS-ON subjects and have previously obtained lower ROC curve AUC values (between 0.86 and 0.91) when compared with our results (MS-ON $AUC_{IMF_{R5}} = 0.97$). Those values were aggregated manually in clusters, making them somewhat unreliable. In contrast, we have used an IMF method that is fully automated, which is one reason it was possible to improve the sensitivity of the analysis.

High discrimination index values for CIS-ON ($AUC_{IMF_{R5}} = 0.98$) and CIS-non-ON ($AUC_{IMF_{R5}} = 0.94$) were obtained using IMF values from ring 5. In the case of the RIS cohort, the discrimination index was not high ($AUC_{IMF_{R5}} = 0.71$), implying that P2T may not be sufficient to discriminate RIS.

In summary, the differences in intensity were magnified when IMF values were used to compare all MS-risk groups, making this analysis potentially useful for predicting MS progression.

The second objective of this paper was to improve interocular latency measurements in control subjects by filtering mfVEP signals using EMD. The L_{INTER} latency values obtained were close to 0 ms in all cases. No significant differences were found between the values obtained using the X_{EMD} signals and the standard method.

Variability (CV_{INTER} , CV_{INTRA}) was reduced in ring 5 compared to the full field. The lowest variability values were found in X_{EMD} signals in ring 5. Significant differences were found in the intrasubject variability between the X_{EMD} and X_{DFT} signals. The lower intrasubject

variability obtained with the IMF analysis indicates that the L_{INTER} latency varies very little from sector to sector, so it would be more sensitive in detecting local visual field defects. Moreover, low intersubject variability would simplify the detection of small changes and be especially relevant when comparing subjects at MS risk with visual pathways at different stages of affection.

The average for the non-analyzable sectors obtained with the EMD analysis was 14.77% (equivalent to 8.62 sectors in a visual field of 60 sectors per eye) compared with 9.62% (equivalent to 5.77 sectors) with X_{DFT} signals. This is because when a different IMF number was selected for each eye as the best IMF, the probability of reverse polarity was increased. Rejecting records from an analysis involves a trade-off between a loss of data on the one hand and a gain in data quality on the other. In this case, we believe that a difference of an average of three sectors is not relevant.

Conclusions

MfVEP signals filtered using the EMD method improves a) the association of the P2T amplitude values with MS risk and b) the IO latency analysis by reducing variability. Even better results are obtained in ring 5 (9.8–15° eccentricity of the visual field).

The processed signals were selected in two steps: (1) the best channel as a function of the highest SNR and (2) the best IMF as a function of the highest P2T. Thus, the best information is used, thereby improving the results achieved by using IMFs.

These results suggest that mfVEPs can be used to assess visual cortex activity in MS diagnosis and longitudinal studies.

Supporting information

S1 File. Amplitude P2T values and latency interocular values. Parameters measured for each subject of the database.
(DOCX)

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References

1. Vanegas MI, Blangero A, Kelly SP. Exploiting individual primary visual cortex geometry to boost steady state visual evoked potentials. *J Neural Eng.* 2013; 10: 36003. <https://doi.org/10.1088/1741-2560/10/3/036003> PMID: 23548662

2. Hood DC. Multifocal VEP and ganglion cell damage: applications and limitations for the study of glaucoma. *Prog Retin Eye Res.* 2003; 22: 201–251. [https://doi.org/10.1016/S1350-9462\(02\)00061-7](https://doi.org/10.1016/S1350-9462(02)00061-7) PMID: 12604058
3. Baseler HA, Sutter EE, Klein SAA, Carney T. The topography of visual evoked response properties across the visual field. *Electroencephalogr Clin Neurophysiol.* 1994; 90: 65–81. [https://doi.org/10.1016/0013-4694\(94\)90114-7](https://doi.org/10.1016/0013-4694(94)90114-7) PMID: 7509275
4. Baseler H a, Sutter EE. M and P components of the VEP and their visual field distribution. *Vision Res.* 1997; 37: 675–90. PMID: 9156212
5. Grippo TM, Hood DC, Kanadani FN, Ezon I, Greenstein VC, Liebmann JM, et al. A Comparison between Multifocal and Conventional VEP Latency Changes Secondary to Glaucomatous Damage. *Investig Ophthalmology Vis Sci.* 2006; 47: 5331. <https://doi.org/10.1167/iov.06-0527> PMID: 17122121
6. Klistorner AI, Graham SL, Grigg JR, Billson FA. Multifocal topographic visual evoked potential: improving objective detection of local visual field defects. *Invest Ophthalmol Vis Sci.* 1998; 39: 937–50. PMID: 9579473
7. Yang EB, Hood DC, Rodarte C, Zhang X, Odel JG, Behrens MM. Improvement in conduction velocity after optic neuritis measured with the multifocal VEP. *Invest Ophthalmol Vis Sci.* 2007; 48: 692–698. <https://doi.org/10.1167/iov.06-0475> PMID: 17251467
8. Klistorner A, Arvind H, Nguyen T, Garrick R, Paine M, Graham S, et al. Axonal loss and myelin in early ON loss in postacute optic neuritis. *Ann Neurol.* 2008; 64: 325–331. <https://doi.org/10.1002/ana.21474> PMID: 18825673
9. Klistorner A, Garrick R, Paine M, Graham SL, Arvind H, Van Der Walt A, et al. Relationship between chronic demyelination of the optic nerve and short term axonal loss. *J Neurol Neurosurg Psychiatry.* 2012; 83: 311–314. <https://doi.org/10.1136/jnnp-2011-300928> PMID: 22193562
10. Souza GS, Schakelford HB, Moura ALA, Gomes BD, Ventura DF, Fitzgerald MEC, et al. Comparison of the reliability of multifocal visual evoked cortical potentials generated by pattern reversal and pattern pulse stimulation. *Brazilian J Med Biol Res = Rev Bras Pesqui medicas e Biol.* 2012; 45: 955–61. <https://doi.org/10.1590/S0100-879X2012007500112> PMID: 22782556
11. Mazinani B a E, Waberski TD, Weinberger AW a, Walter P, Roessler GF. Improving the quality of multifocal visual evoked potential results by calculating multiple virtual channels. *Jpn J Ophthalmol.* 2011; 55: 396–400. <https://doi.org/10.1007/s10384-011-0040-4> PMID: 21674201
12. Zhang X, Hood DC. A principal component analysis of multifocal pattern reversal VEP. *J Vis.* 2004; 4: 4–4. <https://doi.org/10.1167/4.1.4> PMID: 14995897
13. Thie J, Sriram P, Klistorner A, Graham SL. Gaussian wavelet transform and classifier to reliably estimate latency of multifocal visual evoked potentials (mfVEP). *Vision Res.* Elsevier Ltd; 2012; 52: 79–87. <https://doi.org/10.1016/j.visres.2011.11.002> PMID: 22100835
14. Fernández A, de Santiago L, Blanco R, Pérez-Rico C, Rodríguez-Ascariz JM, Barea R, et al. Filtering multifocal VEP signals using Prony's method. *Comput Biol Med.* Elsevier; 2015; 56: 13–19. <https://doi.org/10.1016/j.compbiomed.2014.10.023> PMID: 25464344
15. Klistorner A, Arvind H, Nguyen T, Garrick R, Paine M, Graham SL, et al. Multifocal VEP and OCT in optic neuritis: a topographical study of the structure-function relationship. *Doc Ophthalmol.* 2009; 118: 129–37. <https://doi.org/10.1007/s10633-008-9147-4> PMID: 18779985
16. Klistorner A, Arvind H, Nguyen T, Garrick R, Paine M, Graham SL, et al. Fellow eye changes in optic neuritis correlate with the risk of multiple sclerosis. *Mult Scler J.* 2009; 15: 928–932. <https://doi.org/10.1177/1352458509105228> PMID: 19498018
17. Klistorner A, Fraser C, Garrick R, Graham SL, Arvind H. Correlation between full-field and multifocal VEPs in optic neuritis. *Doc Ophthalmol.* 2008; 116: 19–27. <https://doi.org/10.1007/s10633-007-9072-y> PMID: 17680288
18. Grover LK, Hood DC, Ghadiali Q, Grippo TM, Wenick AS, Greenstein VC, et al. A comparison of multifocal and conventional visual evoked potential techniques in patients with optic neuritis/multiple sclerosis. *Doc Ophthalmol.* 2008; 117: 121–8. <https://doi.org/10.1007/s10633-007-9112-7> PMID: 18204943
19. Sriram P, Klistorner A, Arvind H, Graham SL. Reproducibility of multifocal VEP latency using different stimulus presentations. *Doc Ophthalmol.* 2012; 125: 43–9. <https://doi.org/10.1007/s10633-012-9334-1> PMID: 22669286
20. van der Walt A, Kolbe S, Mitchell P, Wang Y, Butzkueven H, Egan G, et al. Parallel Changes in Structural and Functional Measures of Optic Nerve Myelination after Optic Neuritis. *PLoS One.* 2015; 10: e0121084. <https://doi.org/10.1371/journal.pone.0121084> PMID: 26020925
21. Huang NE, Shen Z, Long SR, Wu MC, Shih HH, Zheng Q, et al. The empirical mode decomposition and the Hilbert spectrum for nonlinear and non-stationary time series analysis. *Proc R Soc A Math Phys Eng Sci.* 1998; 454: 903–995.

22. Tsai F-F, Fan S-Z, Lin Y-S, Huang NE, Yeh J-R. Investigating Power Density and the Degree of Nonlinearity in Intrinsic Components of Anesthesia EEG by the Hilbert-Huang Transform: An Example Using Ketamine and Alfentanil. Schmitt FG, editor. *PLoS One*. 2016; 11: e0168108. <https://doi.org/10.1371/journal.pone.0168108> PMID: 27973590
23. Combaz A, Van Hulle MM. Simultaneous Detection of P300 and Steady-State Visually Evoked Potentials for Hybrid Brain-Computer Interface. Cymbalyuk G, editor. *PLoS One*. 2015; 10: e0121481. <https://doi.org/10.1371/journal.pone.0121481> PMID: 25815815
24. Labate D, Foresta F La, Occhiuto G, Morabito FC, Lay-Ekuakille A, Vergallo P. Empirical Mode Decomposition vs. Wavelet Decomposition for the Extraction of Respiratory Signal from Single-Channel ECG: A Comparison. *IEEE Sens J*. 2013; 13: 2666–2674. <https://doi.org/10.1109/JSEN.2013.2257742>
25. Liang H, Bressler SL, Desimone R, Fries P. Empirical mode decomposition: a method for analyzing neural data. *Neurocomputing*. 2005; 65–66: 801–807. <https://doi.org/10.1016/j.neucom.2004.10.077>
26. Pal S, Mitra M. Empirical mode decomposition based ECG enhancement and QRS detection. *Comput Biol Med*. 2012; 42: 83–92. <https://doi.org/10.1016/j.compbiomed.2011.10.012> PMID: 22119222
27. Kim J, Lee S-K, Lee B. EEG classification in a single-trial basis for vowel speech perception using multivariate empirical mode decomposition. *J Neural Eng*. 2014; 11: 36010. <https://doi.org/10.1088/1741-2560/11/3/036010> PMID: 24809722
28. Urigüen JA, Garcia-Zapirain B. EEG artifact removal—state-of-the-art and guidelines. *J Neural Eng*. 2015; 12: 31001. <https://doi.org/10.1088/1741-2560/12/3/031001> PMID: 25834104
29. Bagheri A, Persano Adorno D, Rizzo P, Barraco R, Bellomonte L. Empirical mode decomposition and neural network for the classification of electroretinographic data. *Med Biol Eng Comput*. 2014; 52: 619–628. <https://doi.org/10.1007/s11517-014-1164-8> PMID: 24923413
30. Liang H, Bressler SL, Buffalo E, Desimone R, Fries P. Empirical mode decomposition of field potentials from macaque V4 in visual spatial attention. *Biol Cybern*. 2005; 92: 380–392. <https://doi.org/10.1007/s00422-005-0566-y> PMID: 15906081
31. Vergallo P, Lay-Ekuakille A, Giannoccaro NI, Trabacca A, Labate D, Morabito FC, et al. Identification of Visual Evoked Potentials in EEG detection by empirical mode decomposition. 2014 IEEE 11th International Multi-Conference on Systems, Signals & Devices (SSD14). IEEE; 2014. pp. 1–5. <https://doi.org/10.1109/SSD.2014.6808848>
32. Blanco R, Perez-Rico C, Puertas-Munoz I, Ayuso-Peralta L, Boquete L, Arevalo-Serrano J. Functional assessment of the visual pathway with multifocal visual evoked potentials, and their relationship with disability in patients with multiple sclerosis. *Mult Scler J*. 2014; 20: 183–191. <https://doi.org/10.1177/1352458513493683> PMID: 23828868
33. De Santiago L, Ortiz del Castillo M, Blanco R, Barea R, Rodríguez-Ascariz JM, Miguel-Jiménez JM, et al. A signal-to-noise-ratio-based analysis of multifocal visual-evoked potentials in multiple sclerosis risk assessment. *Clin Neurophysiol*. 2016; 127: 1574–1580. <https://doi.org/10.1016/j.clinph.2015.09.129> PMID: 26463474
34. Castillo MO Del, de Santiago L, Fernández A, Blanco R, Rodríguez-Ascariz JM, Barea R, et al. A new method for quantifying mfVEP signal intensity in multiple sclerosis. *Biomed Signal Process Control*. Elsevier Ltd; 2015; 22: 119–125. <https://doi.org/10.1016/j.bspc.2015.06.015>
35. Moore F, Okuda DT. Incidental MRI anomalies suggestive of multiple sclerosis: the radiologically isolated syndrome. *Neurology*. 2009; 73: 1714. <https://doi.org/10.1212/WNL.0b013e3181bd69a9> PMID: 19918002
36. Pérez-Rico C, Ayuso-Peralta L, Rubio-Pérez L, Roldán-Díaz I, Arévalo-Serrano J, Jiménez-Jurado D, et al. Evaluation of visual structural and functional factors that predict the development of multiple sclerosis in clinically isolated syndrome patients. *Invest Ophthalmol Vis Sci*. 2014; 55: 6127–31. <https://doi.org/10.1167/iovs.14-14807> PMID: 25190654
37. Frohman EM, Goodin DS, Calabresi P a., Corboy JR, Coyle PK, Filippi M, et al. The utility of MRI in suspected MS: Report of the Therapeutics and Technology Assessment Subcommittee of the American Academy of Neurology. *Neurology*. 2003; 61: 602–611. <https://doi.org/10.1212/01.WNL.0000082654.99838.EF> PMID: 12963748
38. Polman CH, Reingold SC, Banwell B, Clanet M, Cohen JA, Filippi M, et al. Diagnostic criteria for multiple sclerosis: 2010 Revisions to the McDonald criteria. *Ann Neurol*. 2011; 69: 292–302. <https://doi.org/10.1002/ana.22366> PMID: 21387374
39. Laron M, Cheng H, Zhang B, Schiffman JS, Tang RA, Frishman LJ. Assessing visual pathway function in multiple sclerosis patients with multifocal visual evoked potentials. *Mult Scler J*. 2009; 15: 1431–41. <https://doi.org/10.1177/1352458509350470> PMID: 19995841
40. De Santiago L, Klistorner a., Ortiz del Castillo M, Fernández A, Rodríguez-Ascariz JM, Barea R, et al. Software for analysing multifocal visual evoked potential signal latency progression. *Comput Biol Med*. Elsevier; 2015; 59: 134–141. <https://doi.org/10.1016/j.compbiomed.2015.02.004> PMID: 25732777

41. Hood DC, Zhang X, Rodarte C, Yang EB, Ohri N, Fortune B, et al. Determining abnormal interocular latencies of multifocal visual evoked potentials. *Doc Ophthalmol*. 2004; 109: 177–87. PMID: [15881264](#)
42. Hood DC, Zhang X, Greenstein VC, Kangovi S, Odel JG, Liebmann JM, et al. An interocular comparison of the multifocal VEP: a possible technique for detecting local damage to the optic nerve. *Invest Ophthalmol Vis Sci*. 2000; 41: 1580–7. PMID: [10798679](#)
43. Bamber D. The area above the ordinal dominance graph and the area below the receiver operating characteristic graph. *J Math Psychol*. 1975; 12: 387–415. [https://doi.org/10.1016/0022-2496\(75\)90001-2](https://doi.org/10.1016/0022-2496(75)90001-2)
44. Swets JA. Measuring the accuracy of diagnostic systems. *Science*. 1988; 240: 1285–93. PMID: [3287615](#)
45. Armstrong RA. Statistical guidelines for the analysis of data obtained from one or both eyes. *Ophthalmic Physiol Opt*. 2013; 33: 7–14. <https://doi.org/10.1111/opo.12009> PMID: [23252852](#)
46. Fan Q, Teo Y-Y, Saw S-M. Application of Advanced Statistics in Ophthalmology. *Investig Ophthalmology Vis Sci*. 2011; 52: 6059. <https://doi.org/10.1167/iovs.10-7108> PMID: [21807933](#)