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Study on the growth and morphology evolution of titanium oxide clusters in molten iron with molecular dynamics simulation

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Formation of nano-scale titanium oxides is a desirable result in the deoxidation process of steelmaking. However, the nucleation of nano-scale titanium oxide inclusions remains unknown up to now because of the difficulty in observing and detecting inclusions in steel melt. In this work, we studied the formation and evolution of titanium oxygen clusters in molten iron by molecular dynamics (MD) simulation using empirical atomic interaction potentials. The structures of small titanium oxygen clusters in iron are reasonable compared to the first-principles simulation results. The growth process of small clusters into larger clusters was simulated and it is found the clusters grow through the collision mechanism, with the intermediate products exhibiting chain structures. The iron environment was found to play an important role in the structural form of the titanium oxygen clusters. This study is useful to provide the details of formation and the growth mechanism of titanium oxygen clusters and to provide a valuable picture for the nucleation mechanism of titanium oxide in molten steel.

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1. Introduction

Titanium is a widely used deoxidizing element in molten steel.¹ Titanium and dissolved oxygen react to form titanium oxide during refining in the steelmaking process. The stoichiometric ratio and structure of titanium oxides depend on the ratio of titanium and oxygen concentrations in molten steel.² Titanium oxides with a certain size and structure are effective nucleation sites for sulfides,³ nitrides,⁴ and intragranular acicular ferrite.⁵ With the aim of effectively controlling the precipitation behaviour of this kind of favorable and fine titanium oxide, it is necessary to study the growth and morphology evolution of titanium oxide clusters in molten steel. However, it is difficult to observe the nucleation process of oxides directly through experimental approaches in molten steel because of the high temperature. We tried to use a MD simulation method to reproduce this process.

Regarding the nucleation process, the classical nucleation theory does not explain the existence of pre-nucleation clusters in liquid, but it was proved from CaCO_3 solution,⁶ Fe–O–Al melt,^{7–10} and Fe–O–Al–Mg melt¹¹ that the pre-nucleation clusters do exist and rearrange to form nuclei. In our previous work, Dan Zhao *et al.*¹² studied the detailed nucleation process of titanium oxides in Fe–Ti rapid solidified alloy. Through atomic probe

tomography characterization, we confirmed that the nucleation of titanium oxides includes two steps: (1) “TiO” basic units aggregated and formed $(\text{TiO})_n$ clusters; (2) O atoms were absorbed in and around the clusters and the clusters evolved into different nuclei of titanium oxides depending on the titanium and oxygen concentrations in molten steel. This is the experimental basis for the two-step nucleation of titanium oxides. Bao *et al.*¹³ proposed the possible growth pathway of titanium oxide clusters by calculating the formation energy of different $(\text{TiO})_n$ structures in a $4 \times 4 \times 4$ iron matrix using first-principles calculation. They calculated the interaction force between atoms using DFT method, but the size of the simulation systems that can be treated is limited to hundreds of atoms. Classical MD method with empirical atomic potential can treat systems of much larger size, typically up to 10^6 – 10^9 atoms, thus it provides a way to investigate the growth process of pre-nucleation clusters.

Researchers mostly focused on the study of titanium oxide nanoclusters structure^{14–16} or titanium oxide nucleation.¹⁷ The structure and growth mechanism of titanium oxide cluster before nucleation in molten iron is obscure. In this work, the melting point of iron was normalized to determine the simulated temperature. Then the evolution of titanium oxygen (Ti_xO_y , x and y represent the number of titanium and oxygen atoms) clusters were simulated in molten iron with titanium concentrations between 0.02% and 1.00%. Cluster identification and reverse tracking of the atomic trajectory were utilized to trace the evolution of the Ti_xO_y clusters in molten iron. Finally, we explored the effect of molten iron on the structure of Ti_xO_y clusters, which provides a possibility to continue to

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explore the formation of the critical nucleation of titanium oxides.

2. Method

2.1. Simulation setup

All simulations were carried out using MD simulation code LAMMPS.¹⁸ Periodic boundary condition was used and the time step for integration is 1 fs. The key factor for MD simulation is the interaction potential between atoms. To model the interaction of Ti–O system, we chose the Ti–O potential function derived from the defect oxygen in metal titanium.¹⁹ Pencer *et al.*²⁰ used this potential to accurately predict elastic constants of hcp titanium with and without interstitial oxygen solute. The Fe–O potential function came from Zhou's result.²¹ Jeon *et al.*²² employed this potential to studied the surface oxide film growth on Al–Ni–Fe alloys. Fe–Ti interaction was depicted by the potentials of EAM (embedded-atom method) format.²³

2.2. Determination of simulated temperature

The melting temperature of iron described by the potential is essential for studying the growth and evolution of Ti_xO_y clusters in the case of high temperature molten iron. The melting point was calculated according to Morris' method,²⁴ the coexisting system with solid and liquid phase was established under isothermal–isobaric (NPT) ensemble, as shown in Fig. 1(a), which consists of 23 040 iron atoms.

We changed the temperature and pressure to ensure that the system has solid–liquid coexistence under the microcanonical ensemble (NVE) after relaxed for 10 ns. The temperature of the solid–liquid coexisting system was taken as the Fe–Ti–O potential melting point (T_{pot}). The T_{pot} under different

pressures were shown in Fig. 1(b). The $T_{pot} = 2051.99$ K was obtained by linear fitting under the pressure of $P = 1$ bar.

The T_{pot} value was normalized to actual melting temperature in the simulation (T_s) using the following formula:

$$T_s = T_{pot} \times \frac{1873}{1811} \text{ K} \quad (1)$$

where 1811 K is the experimental value of pure Fe melting point,²⁵ 1873 K is the actual melting temperature, so $T_s = 2122$ K.

2.3. The potential function verified by small Ti_xO_y clusters

The titanium atoms are substituted atoms²⁶ and oxygen atoms^{27,28} are octahedral interstitial atoms in matrix iron. Different numbers of titanium and oxygen atoms were inserted into perfect bcc Fe supercell, and the geometrical structures of small $(TiO)_n$ clusters were optimized using Fe–Ti–O potential. The energetically favored structures of $(TiO)_n$ ($n \leq 3$) are shown in Fig. 2(a)–(c). These structures of small $(TiO)_n$ ($n \leq 3$) clusters are similar to those obtained using the first-principle method in our previous work.¹³

The atomic coordinates of $(TiO)_n$ clusters were extracted in Fig. 2(a)–(c), and then put in disordered molten iron for relaxation so as to verify the evolution of cluster at 2122 K. We found that the two structures $(TiO)_1$ and $(TiO)_2$ can exist stably in molten iron (shown in Fig. 2(d) and (e)). The structure $(TiO)_3$ in Fig. 2(c) converts into a stereoscopic structure at 2122 K as shown in Fig. 2(f). We calculated the bond length of Ti–O, which is from 2.01 Å to 2.19 Å. It is reasonable compared to the experiment value (1.96 Å (ref. 29)) in rutile.

The titanium and oxygen atoms in structures in Fig. 2(a)–(c) were restricted at substitutional sites and octahedral interstitial sites in iron lattice in perfect bcc Fe supercell. Whereas titanium and oxygen obtained sufficient kinetic energy from high-temperature environment, and the liquid iron in disordered state could not restrict titanium and oxygen atoms, the structure in Fig. 2(c) evolved into more stereoscopic structure in Fig. 2(f).

2.4. Calculation process and analysis method

As a result of low content of titanium and oxygen in steel, the probability of titanium and oxygen atoms collision in molten steel is low. If free titanium and oxygen atoms are inserted into iron matrix, they will form small size Ti_xO_y clusters in a limited simulation scale. Experimental results of APT by Zhao Dan *et al.*¹² showed that the ratio of Ti and O atoms is 1 : 1 in the structure of Ti_xO_y clusters in steel. In this study, we inserted some pairs of $(TiO)_1$ structure instead of free titanium and oxygen atoms in molten iron.

The concentration of titanium and oxygen can influence the titanium oxide structure. Four systems with different titanium and oxygen contents (shown in Table 1) in molten iron were simulated. The concentrations of titanium and oxygen in group (a) are 199.9 ppm and 66.1 ppm, respectively, similar with the parameters before deoxidation of titanium in actual steel-making. The titanium and oxygen concentration in other three

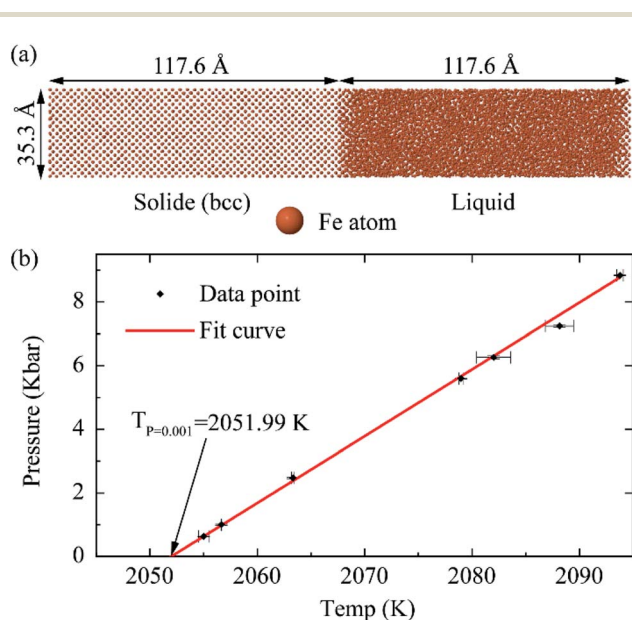


Fig. 1 The melting point was measured by solid–liquid coexistence method. (a) The establishment of the solid–liquid coexisting system on (100) crystal plane. (b) The relationship between pressure and corresponding melting point values under NVE condition.

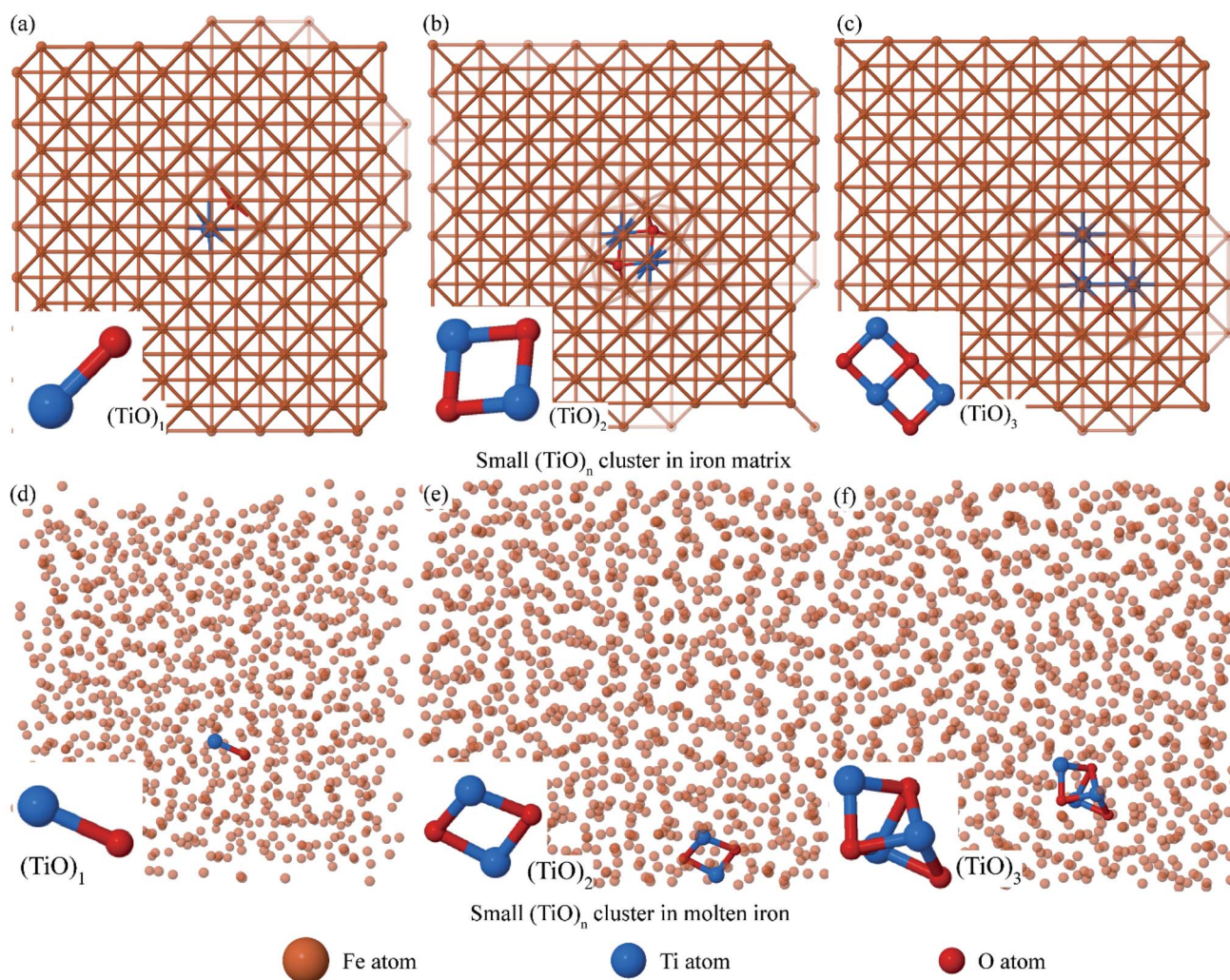


Fig. 2 Small (TiO)_n clusters were optimized in an 8 × 8 × 8 iron supercell. (a)–(c) The (TiO)_n cluster structure was established at 0 K. (d)–(f) (TiO)_n cluster structure was optimized at $T_s = 2122$ K.

groups are higher than those in actual production, but the maximum concentration is not more than 1%.

Using PACKMOL,³⁰ a package for building initial configurations in MD simulation, we constructed a 35 × 35 × 35 supercell (10.29 nm × 10.29 nm × 10.29 nm). Iron atoms and (TiO)₁ structures (shown in Fig. 2(d)) distributed randomly in the supercell (shown in Fig. 3(a)). This periodic cell was relaxed for 0.01 ns at 0 to 2500 K to obtain overheating molten iron (hysteresis phenomenon³¹). Subsequently, the cell was relaxed for 0.02 ns from 2500 to $T_s = 2122$ K. In the above two processes, the (TiO)₁ structures were fixed. Finally, the restriction on the (TiO)₁ structure was released, and the system was relaxed for 60

ns at 2122 K, the pair distribution function of molten iron at 2122 K matched with the experiment.³² All these three processes were simulated with NVT ensemble. Fig. 3 shows the simulation details.

Since many atomic clusters were involved in the evolution process and it was difficult to manually count the numbers of clusters and atoms in simulation, we developed a computer algorithm to analyse the Ti_xO_y clusters.

3. Results and discussion

3.1. The growth of Ti_xO_y cluster

As has been known that, the stable structures of Ti_xO_y clusters at high temperature is different from the cluster structures optimized at 0 K (discussed in Sec. 2.3). We inserted the molecular ion structure (TiO)₁ into molten iron and relaxed the Fe–Ti–O ternary system at 2122 K. The aggregation process of Ti_xO_y cluster in molten iron can be studied from the number of clusters and its time evolution.

Table 1 The number of atoms in four systems

	Group (a)	Group (b)	Group (c)	Group (d)
Iron number	85 730	85 550	85 250	84 750
(TiO) ₁ number	20	200	500	1000

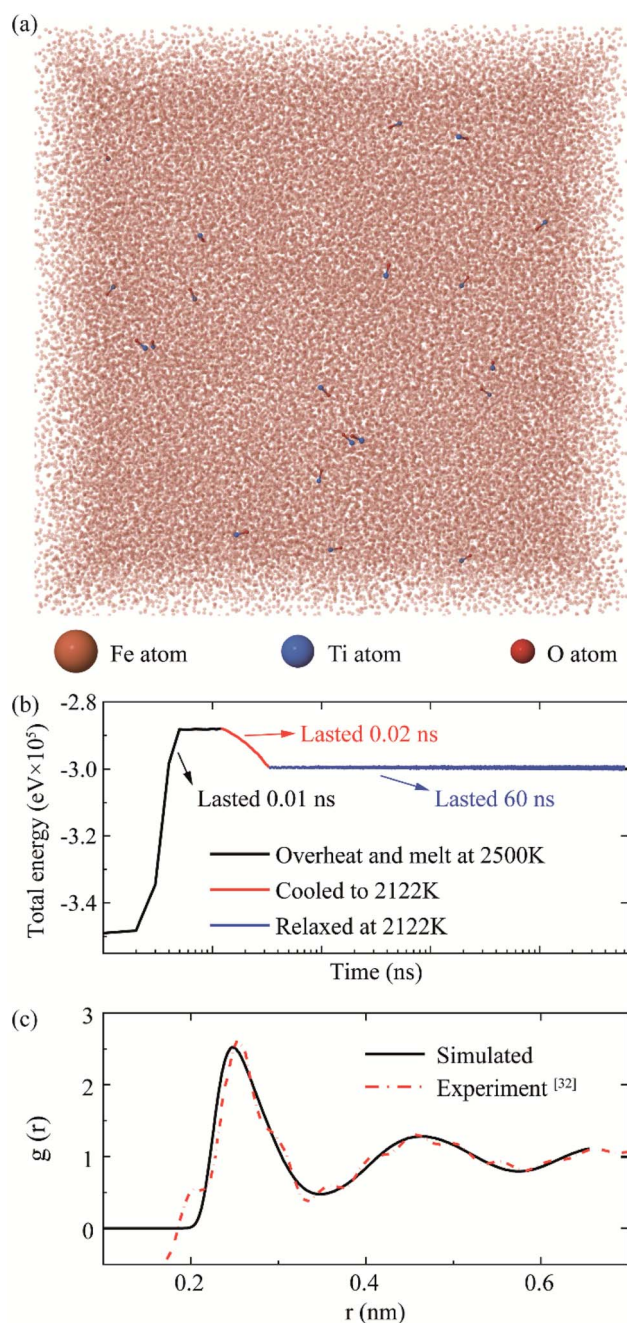


Fig. 3 The MD simulation process for $(\text{TiO})_1$ structure in iron supercell. The group (a) in Table 1 as an example. (a) The atoms configurational snapshots before calculation. (b) The relationship between system total energy and time. (c) The pair distribution function of molten iron at 2122 K.

In Fig. 4(a), in the first 1 ns, the numbers of clusters (N) decreased by 5, 141, 408 and 869 in groups (a), (b), (c) and (d), respectively. The Ti_xO_y clusters aggregated to form larger clusters, resulting in a reduction in the number of clusters. From 10 ns to 60 ns, the numbers of clusters decreased by 0.06, 0.22, 0.28 and 0.4 clusters per nanosecond. The Ti_xO_y cluster's aggregation rate was much slower in the 10–60 ns time range than that in the first 1 ns. More particularly, the higher the concentration

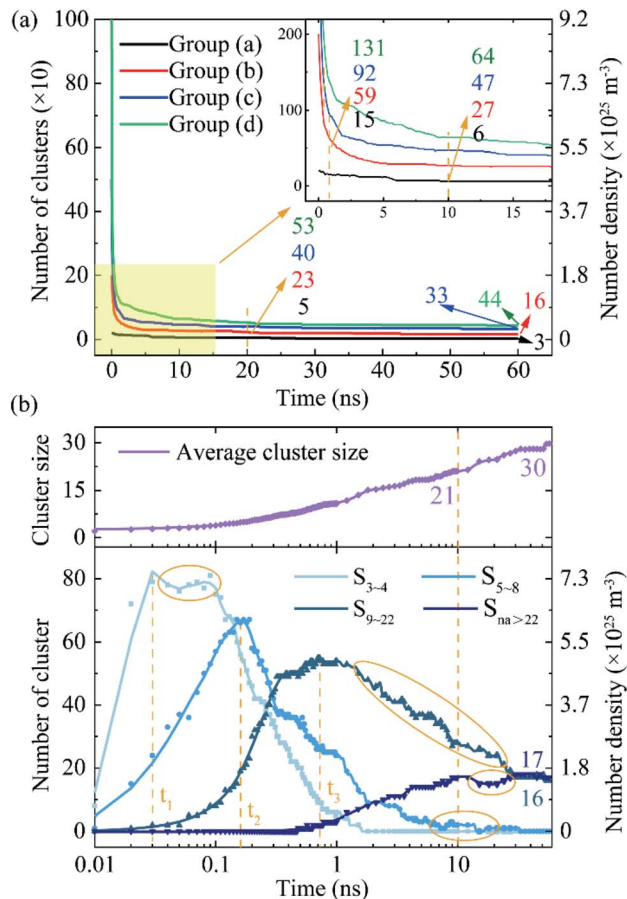


Fig. 4 The aggregation process of Ti_xO_y clusters and Ti_xO_y clusters size distribution. (a) The number of Ti_xO_y clusters vs. time. Among the four colored curves, the initial number of clusters is 20, 200, 500 and 1000, respectively (shown in Table 1). (b) Ti_xO_y clusters size distribution as a function of time. The dots represent the calculated data points while the lines represent smoothed fit to these values, t_1 (0.03 ns), t_2 (0.15 ns) and t_3 (0.7 ns) correspond to the time at the peak of cluster size.

of titanium and oxygen in molten iron, the faster the rate of cluster aggregation. Even though there coexists new clusters formation and cluster decomposition process, the above dynamic Ti_xO_y clusters in molten iron grew rapidly at the beginning period and then grew steadily.

Fig. 4(b) combines the Ti_xO_y clusters size distribution to analyse the clusters growth. We take group (c) as an example (blue curve in Fig. 4(a)). Group (c) has an appropriate number of titanium and oxygen atoms, and the cluster aggregation law is representative and applicable to other groups. The number density of clusters (n_{cluster}) was obtained as the number of clusters divided by the simulation system volume (V):

$$n_{\text{cluster}} = N/V \quad (2)$$

We tracked the evolution of the Ti_xO_y clusters, then counted the Ti_xO_y cluster size distribution at different times. The cluster with n atoms is denoted as S_n , the average cluster size ($C_{\text{avg_size}}$) in molten iron was defined as follows:

$$C_{\text{avg-size}} = S_{\text{total}}/N \quad (3)$$

where S_{total} is the number of atoms in all clusters, N is the number of clusters. The number density of clusters is obtained by $n_{\text{cluster}} = S_n/V$.

It was noteworthy that the curves show fluctuation (the yellow circle in Fig. 4(b)). As the energy fluctuates, the Ti_xO_y clusters decompose to form small-sized clusters, indicating that there were decomposition and aggregation in un-nucleated Ti_xO_y clusters. The average size of the clusters constantly increased (the purple curve in Fig. 4(b)). With the formation of new cluster and cluster decomposition, the cluster grew toward larger dimensions.

The growth process of the Ti_xO_y clusters can be restore from clusters size distribution (shown in Fig. 4(b)). The cluster size that appeared first was S_{3-4} . The number of Ti_xO_y clusters with size in range of $3 \leq n_a \leq 4$ increased with time till reaching a limiting value at time $t_1 = 0.03$ ns (see Fig. 4(b), S_{3-4} curve). With the advancing of time, the number of clusters S_{3-4} was consumed and reduced and the number of clusters S_{5-8} increased. As time process, the size distribution range became larger and larger, the number of small clusters decreased while the number of large clusters increased (see Fig. 4(b), S_{5-8} and S_{9-22} curve).

It should be mentioned that the large size Ti_xO_y clusters needed a long time to grow up. As time processed, the number density of Ti_xO_y clusters decreased which led to a decrease in the probability of cluster aggregation. It's worthwhile to further explore the growth path of Ti_xO_y clusters before nucleation. We chose one of the Ti_xO_y clusters at the end of simulation, then marked the titanium and oxygen atoms in this Ti_xO_y cluster and reverse tracked the atomic trajectory to obtain the atomic coordinates of the labeled atoms, we could ascertain the way of Ti_xO_y cluster growth. This method was implemented in the open visualization tool OVITO³³ package. The results were shown in Fig. 5.

It can be seen from Fig. 5 that there were some small Ti_xO_y clusters containing a large number of labeled titanium and oxygen atoms at 1 ns (see Fig. 5(b)① and ②). These Ti_xO_y clusters collided together in molten iron and formed bigger clusters at 10 ns. The process of collision between two clusters was shown in Fig. 5(c).

Some Ti_xO_y clusters contained a small number of labeled oxygen atoms (yellow balls in the unlabeled clusters in Fig. 5(b)③–⑤). The labeled Ti_xO_y clusters also contained a small number of unlabeled oxygen atoms (red balls in the labeled clusters Fig. 5(b)⑥ and (c)). These oxygen atoms might detach from the labeled Ti_xO_y clusters after a period of movement and merged into other Ti_xO_y clusters or into molten iron. Ti_xO_y clusters would compete with iron and other Ti_xO_y structures to absorb oxygen atoms. This phenomenon indicates that the Ti_xO_y clusters will adjust the structure due to energy fluctuations before nucleation.

Collision is the fastest way for clusters to grow up, but it is limited by the density of clusters, which affects the collision probability. The dissociation of oxygen atoms can lead to positive growth and negative growth of Ti_xO_y clusters. Zhang

*et al.*³⁴ calculated the process of nucleation of primary inclusion and found that the collision make a huge contribution to cluster growth when the cluster size is less than 10 nm.

3.2. Morphology evolution of Ti_xO_y clusters

The process of cluster aggregation and growth becomes clear according to the above discussion. The Ti_xO_y clusters were classified according to the number of titanium and oxygen atoms at $t_1 = 0.03$ ns, $t_2 = 0.15$ ns and $t_3 = 0.7$ ns in group (c) (peak position of S_{3-4} , S_{5-8} and S_{9-22} in Fig. 4, respectively). We counted the number of different types of Ti_xO_y clusters and found that Ti_xO_y clusters with a stoichiometric Ti : O ratio of 1 : 1 occupied the majority of all clusters. The proportion of $(\text{TiO})_n$ ($n \leq 11$, Ti : O = 1 : 1) clusters were listed in Table 2. The evolution process of Ti_xO_y cluster structure was explored by comparing the change of cluster proportion.

It has been found that the $(\text{TiO})_n$ ($2 \leq n \leq 6$) accounted for the majority at the peak Ti_xO_y clusters size distribution. We have extracted the atomic coordinates of the $(\text{TiO})_n$ ($2 \leq n \leq 6$) clusters in Fig. 6 to show the cluster structures.

The structures of $(\text{TiO})_2$ and $(\text{TiO})_3$ were the same as discussed in 2.3 Section. The structure of $(\text{TiO})_4$ was the first complete cubic-like structure. When $n = 5$, $(\text{TiO})_5$ and $(\text{TiO})'_5$ clusters coexisted in molten iron. The energy of the $(\text{TiO})'_5$ structure was 2.81 eV higher than that of $(\text{TiO})_5$ structure. This proved that $(\text{TiO})_5$ was more stable than $(\text{TiO})'_5$. When $n \geq 6$, the $(\text{TiO})_n$ clusters would evolve to chain-like structures (as shown in Fig. 5(b) and (c)).

Xiang *et al.*³⁵ obtained two types of $(\text{TiO})_n$ clusters using the *ab initio* calculations: cubic-like structure and ring-like structure. They found that the ring-like structures are more stable than cubic-like structures as the size of clusters increasing. The cluster structures in Fig. 6 were similar to the cubic-like structure showed in Xiang's result.³⁵ With the effect of high temperature and iron atoms, the cubic-like structure was easier to form than the ring-like structure when $n < 6$.

Fig. 7 shows the atomic coordinates after the energy minimization. Comparing the four images, the difference in the concentration of titanium and oxygen atoms affects the amount and size of the Ti_xO_y clusters. But there is not much difference in cluster structure. Where the structures of Ti_xO_y clusters are mostly chain-like as shown in Fig. 7②, ③, ⑤, ⑦ and ⑧, branched structure as shown in Fig. 7④ and ⑨, cubic-like structure as shown in Fig. 7① and ⑥. The length of the longest cluster ⑥ is about 5 nm, and the length of other clusters are about 0.5 nm to 3 nm. Demichelis³⁶ observed stable pre-nucleation clusters from early stages of calcium carbonate formation, the pre-nucleation clusters consist of chains, branches and rings, which can fold and coil like a polymer. But we did not find the folding phenomenon of chain-like or branched structures in molten iron.

3.3. Effect of molten iron on Ti_xO_y clusters structure

Many researchers studied the structural evolution process of particles, ignoring the influence of environment. But the influence of the matrix on the cluster structure cannot be

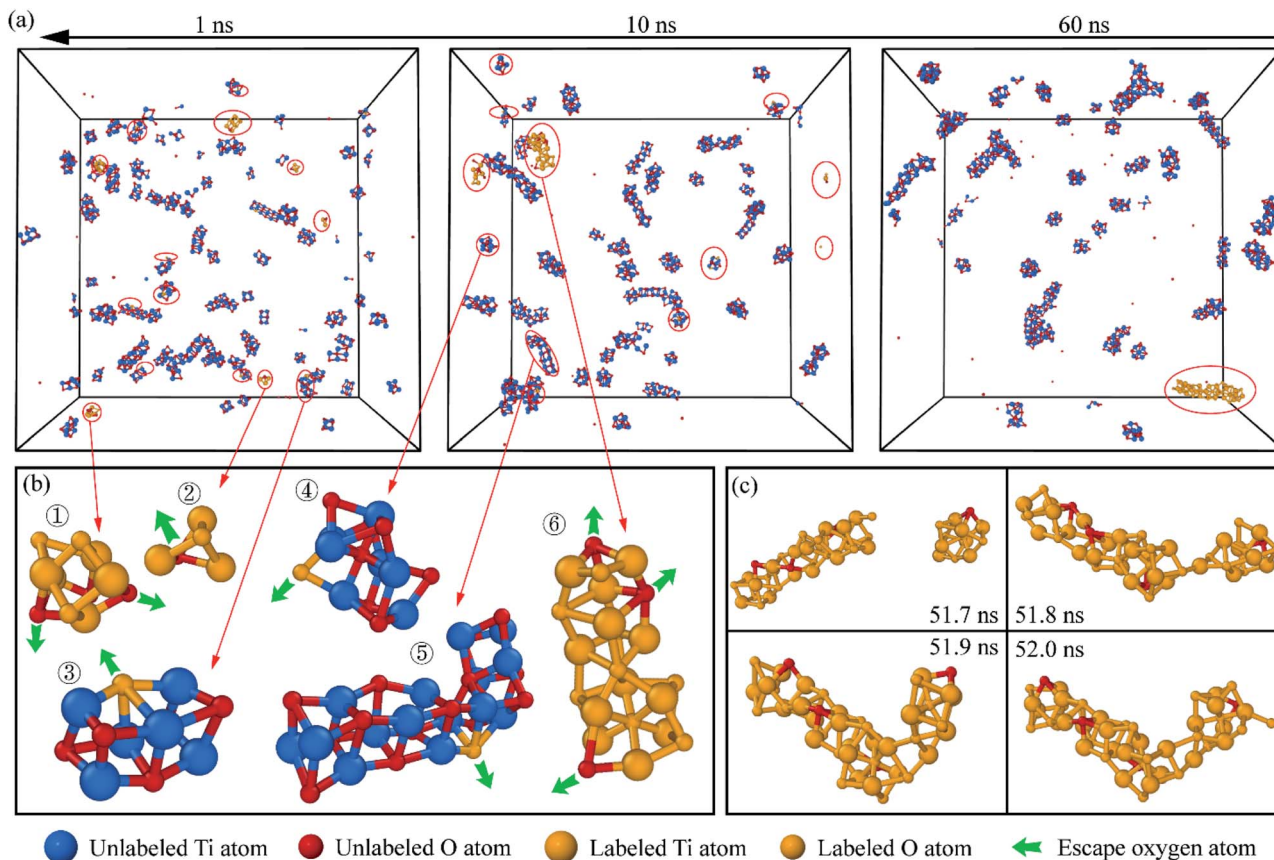


Fig. 5 Growth process of the Ti_xO_y clusters. (a) Simulation cell, iron atoms were hidden. The labeled titanium and oxygen atoms (in red circles) at 1 ns and 10 ns formed a labeled Ti_xO_y cluster (in red circle) at 60 ns. (b) Part of clusters were enlarged which contain the labeled atoms. The green arrow indicates the oxygen atom will escape from the cluster. (c) The process of collision and merging of labeled clusters. Lots of chain-like Ti_xO_y cluster structure can be found in molten iron, we discussed this phenomenon in Sections 3.2 and 3.3.

ignored. To find out the effect of molten iron on the structure of Ti_xO_y clusters, we extracted some chain-like and branched structure's (shown in Fig. 7) atomic coordinates to explore their optimal structures without iron atoms at 2122 K. We examined plenty of clusters and displayed typical structural evolutions in Fig. 8.

Table 2 The percentage of $(\text{TiO})_n$ cluster numbers at the peak of S_{3-4} , S_{5-8} and S_{9-22} on $t_1 = 0.03$ ns, $t_2 = 0.15$ ns and $t_3 = 0.7$ ns, respectively. The 'Others' represents the Ti : O does not equal to 1 : 1 in Ti_xO_y clusters

Time	t_1	t_2	t_3
$(\text{TiO})_2$ Pct	74	41	9
$(\text{TiO})_3$ Pct	18	28	12
$(\text{TiO})_4$ Pct	5	16	12
$(\text{TiO})_5$ Pct	2	8	21
$(\text{TiO})_6$ Pct	N	1	11
$(\text{TiO})_7$ Pct	N	1	8
$(\text{TiO})_8$ Pct	N	N	4
$(\text{TiO})_9$ Pct	N	1	1
$(\text{TiO})_{10}$ Pct	N	N	1
$(\text{TiO})_{11}$ Pct	N	N	4
Others Pct	1	4	17

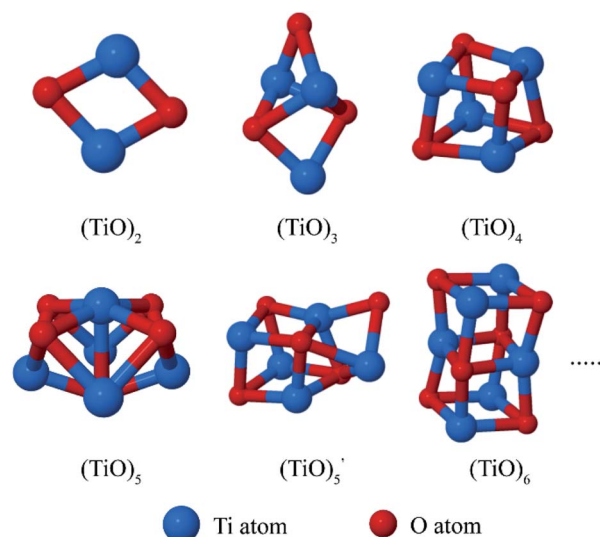


Fig. 6 The $(\text{TiO})_n$ ($2 \leq n \leq 6$) cluster structures extracted from molten iron.

The 'branch' and the 'chain' in Ti_xO_y clusters folded without iron atoms obstruction, and evolved into near-spherical or cage structures. These chain-like and branched structures can be

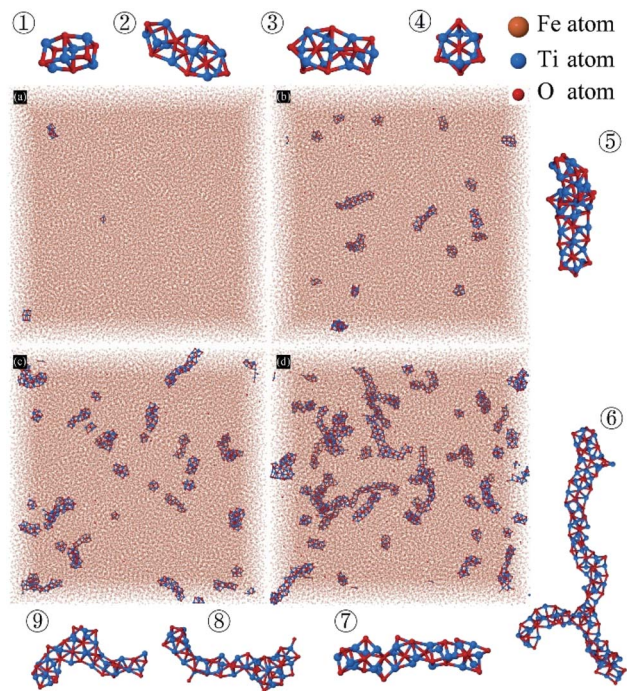


Fig. 7 Atomic coordinates snapshots in simulation box after energy minimization and typical species of TiO structures observed in simulation. (a)–(d) Correspond to systems with different concentration of Ti and O corresponding to Table 1. Illustration ①–⑨ are some typical cluster structures observed in the system.

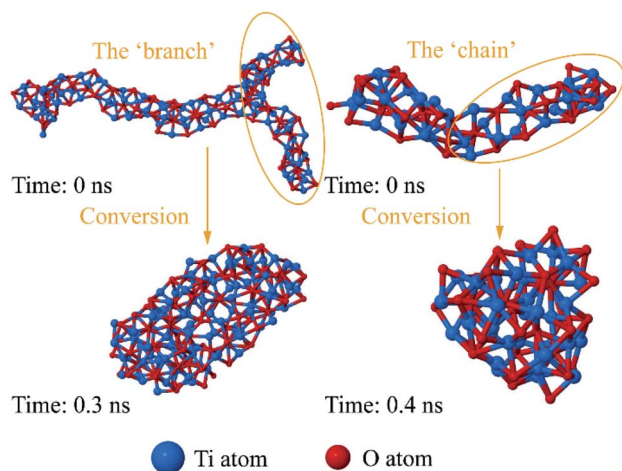


Fig. 8 The evolution of chain-like and branched clusters in the absence of iron atoms.

regarded as dynamic structure. The dynamic structures can constantly evolve but the iron atoms hindered the structures from folding and coiling. It is possible that the interactions between Fe–Ti^{37,38} and Fe–O³⁹ makes titanium and oxygen atoms difficult to move freely, which can be seen from the interfacial energy between Fe and Ti_xO_y clusters. As for how these chain-like structures grow to form critical nuclei in molten steel, the question remains to be further studied.

4. Conclusions

The formation of Ti_xO_y clusters before nucleation is clarified by MD simulations of the Fe–Ti–O system in the actual smelting process for up to 60 ns. The structure of small (TiO)_n clusters obtained by MD was compared with the results of first-principles calculation, ensuring the applicability of the atomic interaction potential. Fe–Ti–O system with titanium concentrations between 0.02% and 1.00% was simulated to prove that the concentration will affect Ti_xO_y cluster aggregation rate and size. Visual inspection, cluster identification and reverse tracking of the atomic trajectory were employed to explore the growth process and morphology evolution of Ti_xO_y cluster before nucleation. The detailed conclusions are as follow:

(1) Ti_xO_y clusters appear a size distribution variation with time, clusters of a certain size are dominant during a certain amount of time, as time process, the size of the largest number of clusters will become larger. As the energy fluctuates, a part of Ti_xO_y cluster will decompose into small clusters, but average cluster size keeps increasing.

(2) Collision is the main way for Ti_xO_y cluster to grow up in molten iron, in the meantime, oxygen atoms will detach from the Ti_xO_y cluster or merge into another Ti_xO_y cluster due to the competition between iron and titanium atoms.

(3) When the number of atoms in Ti_xO_y clusters is greater than 3 but less than 12, cluster structure with Ti to O stoichiometric ratio of 1 : 1 holds the largest proportion, which are cubic-like structure.

(4) When Ti_xO_y cluster grows, larger cluster has a dynamic chain structure. The ‘chain’ or ‘branch’ structure in Ti_xO_y cluster will fold and coil without the influence of molten iron, and evolved into near-spherical or cage structures.

Conflicts of interest

We declare that we do not have any commercial or associative interest that represents a conflict of interest in connection with this work.

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