



Article

Controllable Valley Polarization and Strain Modulation in 2D 2H-VS₂/CuInP₂Se₆ Heterostructures

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Abstract: Two-dimensional (2D) transition metal dichalcogenides endow individually addressable valleys in momentum space at the K and K' points in the first Brillouin zone due to the breaking of inversion symmetry and the effect of spin-orbit coupling. However, the application of 2H-VS₂ monolayer in valleytronics is limited due to the valence band maximum (VBM) located at the Γ point. Here, by involving the 2D ferroelectric (FE) CuInP₂Se₆ (CIPSe), the ferrovalley polarization, electronic structure, and magnetic properties of 2D 2H-VS₂/CIPSe heterostructures with different stacking patterns and FE polarizations have been investigated by using first-principles calculations. It is found that, for the energetically favorable AB-stacking pattern, the valley polarization is preserved when the FE polarization of CIPSe is upwards (CIPSe \uparrow) or downwards (CIPSe \downarrow) with the splitting energies slightly larger or smaller compared with that of the pure 2H-VS₂. It is intriguing that, for the FE CIPSe \uparrow case, the VBM is expected to pass through the Fermi energy level, which can be eventually achieved by applying biaxial strain and thus the valleytronic nature is turned off; however, for the CIPSe \downarrow situation, the heterostructure basically remains semiconducting even under biaxial strains. Therefore, with the influence of proper strains, the FE polar reversal of CIPSe can be used as a switchable on/off to regulate the valley polarization in VS₂. These results not only demonstrate that 2H-VS₂/CIPSe heterostructures are promising potential candidates in valleytronics, but also shed some light on developing practical applications of valleytronic technology.



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Keywords: valley polarization; strain modulation; 2H-VS₂/CIPSe heterostructures; first-principles calculations

1. Introduction

With the rapid development of two-dimensional (2D) materials [1–6], graphene and graphene-like single-layer materials as well as their heterostructures have aroused widespread concern because of their unique electric [7–11], magnetic [12–18], optical [19–22], and mechanical properties [23–25]. In particular, as promising materials in valleytronics where the valley state is the extreme point of energy dispersion located at K and K' in the first Brillouin zone [26,27], 2D transition metal dichalcogenides (TMDs) have recently attracted considerable attention since they are both physically intriguing and practically appealing to be used in nanoscale optoelectronic devices [28–31].

It is known that, for the monolayer Group-V TMDs, such as VX₂ (X = S, Se, Te), the coexistence of the spin-orbit coupling (SOC) effect and exchange interaction of localized *d* electrons result in spontaneous valley polarization [32]. The monolayer VS₂ has been confirmed to have an intrinsic ferromagnetic semiconducting property, which could be a

suitable candidate for constructing 2D magnetic Van der Waals (vdW) heterostructures [33]. The VS_2 monolayer exhibits magnetic characteristics with V atoms contributing magnetism ($\sim 1 \mu\text{B}$). Similar to MoS_2 , it has three stable structures (2H, 1T, and 1T'), among which the 2H structure is semiconducting and 1T and 1T' are metallic. 2H- VS_2 exhibits the spontaneous valley polarization due to the intrinsic exchange interaction between V $3d$ electrons, which is equivalent to a permanent magnetic field. Thus, the concept of the ferrovalley material has been proposed in monolayer VS_2 . The various properties of pure VS_2 have been studied since 2013 in both theory and experiment [34–36], mainly focusing on the energy band structure and the magnetic property of the material. Since 2017, VS_2 has formed heterojunctions with graphene, Mxene, CN materials, and TMDs to obtain the regulation of electronic structure and the potential applications in lithium (sodium/zinc) ion batteries [37–40].

Due to the bistable and nonvolatile characteristics of ferroelectric (FE) materials, it is desirable to combine VS_2 with a suitable FE material to improve its controllability in valleytronic structures. In this work, a newly discovered 2D Van der Waals (vdW) FE $\text{CuInP}_2\text{Se}_6$ (CIPSe) with switchable polarization directions along the out-of-plane direction is selected to construct a heterostructure with VS_2 , which has not been investigated previously. As room-temperature ferroelectrics, CIPSe possesses the atomic structure containing a sulfur framework with the octahedral voids filled by the Cu, In, and P–P triangular patterns. Bulk crystals are composed of vertically stacked, weakly interacting layers packed by vdW interactions. Owing to the site exchange between Cu and P–P pair from one layer to another, a complete unit cell consists of two adjacent monolayers to fully describe the material's symmetry.

In order to investigate whether valley and spin splitting can be modulated in 2H- VS_2 combined with a FE CIPSe layer, and how FE polarization affects the electronic structure of 2H- VS_2 , considering the small lattice mismatch of 1.18%, the 2H- VS_2 /CIPSe heterostructures are established in this work. As a result, for the energetically favorable stacking pattern (AB-stacking) and the most stable magnetic ground state (ferromagnetic phase), valley splitting energies of the combined system could be adjusted by the orientation of FE polarization in CIPSe. It is further shown that the applied biaxial strain can effectively modulate the valley polarization of the system, which suggests that 2H- VS_2 /CIPSe heterostructures are the potential candidates in valleytronics.

2. Method and Technique Details

The first-principles calculations based on the density-functional theory (DFT) have been performed on all structures by using the Vienna Ab initio simulation (VASP) package [41], implemented within the generalized gradient approximation (GGA) and Perdew–Burke–Ernzerhof (PBE) function [42] for the calculation of geometries and the electronic structures. The SOC effect was considered in all calculations. To describe the on-site Coulomb interaction, the Hubbard parameters U and J are taken as 3 eV and 1 eV for the transition metal V atom according to the previously reported value [43]. In the present simulations, the total energy and residual force were convergent to an accuracy of 10^{-4} eV and 10^{-2} eV/Å, respectively, by using a plane-wave energy cutoff of 450 eV. The Brillouin zone was represented by a Monkhorst–Pack special k -point meshes of $7 \times 7 \times 1$ for all structures. The heterostructures are composed of CIPSe unit cell and $2 \times 2 \times 1$ VS_2 supercell along the vertical direction. The in-plane lattice parameters of monolayers CIPSe and 2H- VS_2 are 6.454 and 6.378 Å, respectively, with lattice mismatch of 1.18%. A 25 Å-thick vacuum layer was added to avoid the interaction between adjacent layers. The vdW correction with zero damping DFT–D3 method of Grimme [44] was used to describe the interlayer interactions between VS_2 and CIPSe layers.

3. Results and Discussion

3.1. Electronic Structures of Pristine 2H-VS₂

Before investigating the 2H-VS₂/CIPSe heterostructures, the valley splitting and band structures of pristine 2H-VS₂ are studied firstly. The top and front views of the optimized pure 2H-VS₂ structure with its electron localization function (ELF) map are shown in Figure 1a, where the red area (valued 0.8) and blue area (values 0) represent higher and lower electron localizations, respectively. It is shown that the electrons in 2H-VS₂ are highly localized in the areas close to the S atoms. Note that there exist two configurations of VS₂, namely, 1T and 2H phases. As shown in Figure S1 of the Supplementary Materials, based on the 2H phase, the S atoms in the upper and lower layers move the same distance along the opposite direction in the plane to form the 1T phase. The spin-resolved energy band structures shown in Figure S1 indicate that 1T-VS₂ is a conductor; thus, the semiconducting 2H-VS₂ structure is mainly concentrated in the present work. Just as the calculated band structures of pristine 2H-VS₂ shown in Figure 1b, besides the semiconducting feature, the valley splitting only appears when the SOC is considered (red solid curves), since the energies at points K and K' are equivalent without considering the SOC (black dashed curves). The magnetocrystalline anisotropy energy (MAE) is defined as the energy difference between the perpendicular and parallel magnetization directions by the force theorem, namely $MAE = E[1] - E[100]$, where $E[1]$ and $E[100]$ represent the total energies of out-of-plane and in-plane spin alignments, respectively. Positive and negative MAE indicate in-plane and out-of-plane MA, respectively. The calculated MAE value is -0.158 meV/unit_cell for the pristine VS₂ monolayer, suggesting that the easy axis of magnetization is along the out-of-plane direction and the VS₂ monolayer material has obvious magnetic anisotropy. This is consistent with the results of previous reports [45,46].

Figure 1c shows the variation of the energies of the conduction band minimum (CBM) and the valence band maximum (VBM) at high symmetry points K/G in the Brillouin region according to the calculated band structures with SOC of VS₂ under biaxial strains as shown in Figure 1d. It can be seen that the VS₂ monolayer has an intrinsic valley splitting of 30 meV. Note that, for the pristine VS₂, the obtained valley splitting energies (ΔE) of the strained structures are only slightly larger (stretching) or smaller (compressing) compared with the unstrained structure. This trend of strain tuned ΔE is consistent with the results in previous study [33]. The result indicates that the valley splitting energy of VS₂ can be regulated by the strain, but the variation range is small and the effect is relatively weak. Therefore, it is necessary to seek other diversified modulation methods. For instance, constructing a heterostructure with a FE substrate is an effective way, since the FE polarization possesses bistability of polarization upward ($P\uparrow$) and polarization downward ($P\downarrow$), and, generally, the two states can be reversibly switched with the influence of an external field (such as electric field or force field). As mentioned previously, in the present work, the CIPSe is chosen as the FE substrate, and the 2H-VS₂/CIPSe heterostructures are established to further explore the physical mechanism for the control of the valley polarization of the structure by use of the FE polarization as well as the strain.

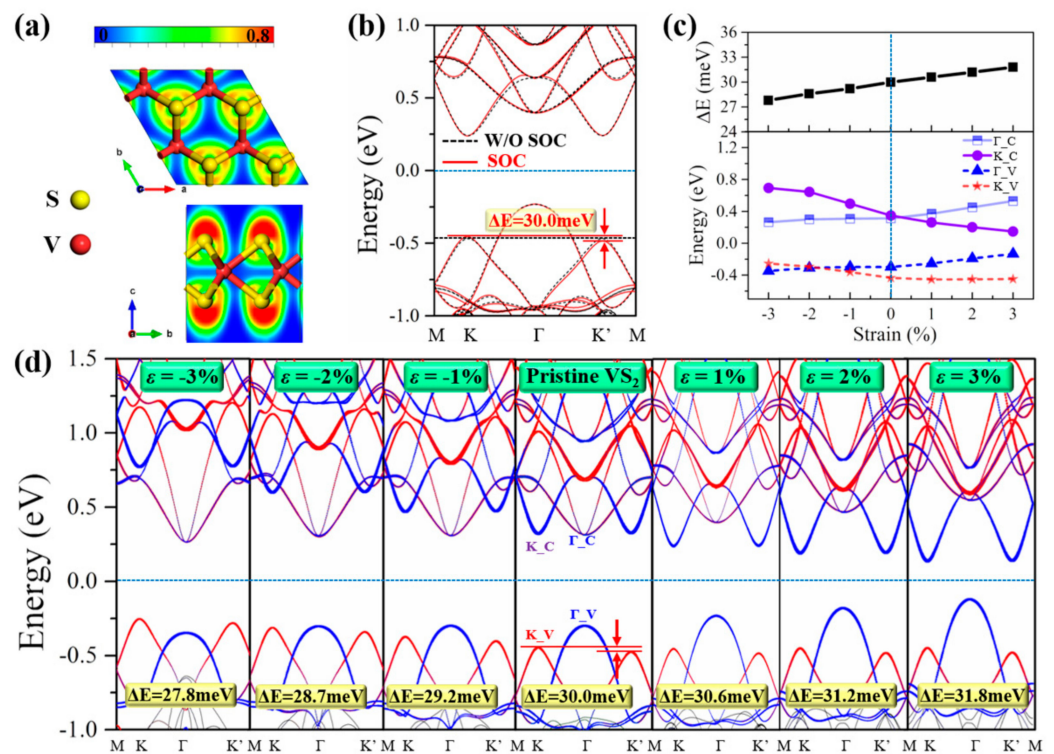


Figure 1. Valley splitting and band structures of pristine 2H-VS₂. (a) Electron Localization Function (ELF) map of pristine 2H-VS₂ with top and front views of the optimized 2H-VS₂; (b) band structures without SOC (black dashed curves) and with SOC (red solid curves) of pristine 2H-VS₂; (c) valley splitting energies (ΔE) (upper panel) and conduction/valence band energies at K and G positions (lower panel) of VS₂ under biaxial strains; (d) valley splitting and band structures with SOC of VS₂ under biaxial strains. The red and blue lines denote the contributions from $V-d_{xy} + d_{x^2-y^2}$ and $V-d_{z^2}$ orbitals, respectively. The Fermi level is set to zero.

3.2. Structural and Electronic Properties of 2H-VS₂/CIPSe Heterostructures

In the present work, according to the three cases that Cu atom in CIPSe is facing S atom (S for AA-stacking), hexagonal center (H for AB-stacking), and V atom (V for AC-stacking) in 2H-VS₂, three different stacking patterns are considered to investigate the electronic structure and magnetic properties of 2D 2H-VS₂/CIPSe heterostructures (see Figure S2 in the Supplementary Materials). The calculated total energies for each stacking pattern with respect to different polarization directions are listed in Table 1, in which both ferromagnetic (FM) and antiferromagnetic (AFM) ground states are considered. It can be seen from Table 1 that ferromagnetic 2H phases are more stable, and will be further studied in the subsequent calculations.

Table 1. Calculated total energies (eV) of 2H-VS₂/CIPSe heterostructures for each stacking pattern with respect to different polarization directions and magnetic ground states.

Polarization Direction	Magnetic Ground State	AA-Stacking (S)	AB-Stacking (H)	AC-Stacking (V)
CIPSe \uparrow	FM	-114.666 eV	-114.751 eV	-114.727 eV
CIPSe \downarrow	FM	-114.618 eV	-114.654 eV	-114.617 eV
CIPSe \uparrow	AFM	-114.193 eV	-114.287 eV	-114.256 eV
CIPSe \downarrow	AFM	-114.137 eV	-114.180 eV	-114.136 eV

The optimized atomic structures with interlayer distance and calculated band structures of 2H-VS₂/CIPSe heterostructures considering SOC with opposite directions of FE polarizations are shown in Figure 2. Compared with the intrinsic valley splitting

of the pristine VS_2 monolayer shown in Figure 1b, the valley polarization is preserved; when the FE polarization of CIPSe is pointing upwards ($2\text{H-VS}_2/\text{CIPSe}\uparrow$) or downwards ($2\text{H-VS}_2/\text{CIPSe}\downarrow$), the 2H-VS_2 layer with the splitting energies (ΔE) is slightly larger (30.7 meV) or smaller (28.7 meV) than that of the pure 2H-VS_2 (30 meV). Notably, the MAE in VS_2/CIPSe with upward (\uparrow) and downward FE polarizations (\downarrow) are 0.191 and 0.187 meV/unit_cell, respectively. The positive values indicate the easy axis of magnetization is parallel to the 2D plane. The in-plane magnetization was also found in the 2H-VTe_2 monolayer [47]. Similar to the MAE of the pristine VS_2 monolayer, the MAE in VS_2/CIPSe provides the precondition to discuss the ferrovalley. Furthermore, from the band structures shown in Figure 2b,d, for both situations of $\text{CIPSe}\uparrow$ and $\text{CIPSe}\downarrow$, the CBM of the heterostructures are mainly contributed by V d_{z^2} , d_{xy} , and $d_{x^2-y^2}$ orbitals, while the VBM is mainly contributed by Cu d orbitals. The degenerate V d_{xy} and $d_{x^2-y^2}$ orbitals in the pristine monolayer VS_2 are lifted in the $\text{CIPSe}\uparrow$ and $\text{CIPSe}\downarrow$ models, which can be attributed to the influence of interfacial interaction. In particular, the VBM in the $\text{VS}_2/\text{CIPSe}\uparrow$ case is almost passed through the Fermi energy level (Figure 2b), which is expected to be achieved by applying biaxial strain and thus the valleytronic nature can be turned off. At the same time, sufficient large valley splitting energy in VS_2/CIPSe heterostructures ensures that valley behavior can be maintained at room temperature. The magnetic behavior in the ferromagnetic VS_2 monolayer can be modulated in the VS_2/CIPSe model by reversing the direction of FE polarizations of CIPSe, achieving the magnetoelectric coupling between VS_2 and CIPSe.

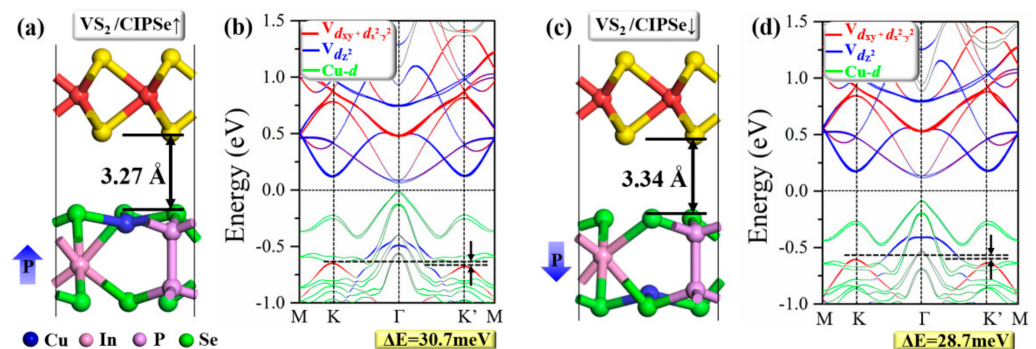


Figure 2. Atomic structures with interlayer distance and calculated band structures with SOC of (a,b) $2\text{H-VS}_2/\text{CIPSe}\uparrow$ and (c,d) $2\text{H-VS}_2/\text{CIPSe}\downarrow$ heterostructures. The arrows “ \uparrow ” and “ \downarrow ” represent ferroelectric upward and downward polarizations. The solid lines in red, blue, and green represent the contributions from $\text{V-}d_{xy} + d_{x^2-y^2}$, $\text{V-}d_{z^2}$ and $\text{Cu-}d$ orbitals, respectively. The Fermi level is set to zero.

To precisely confirm the charge transfer between the layers of $2\text{H-VS}_2/\text{CIPSe}$ heterostructures, the electrostatic potential and work functions (Φ) for pristine 2H-VS_2 and CIPSe are calculated, respectively. The work function can be defined as the minimum energy required moving an electron from the interior of a solid to the surface of the object. The smaller the energy required for an electron at the surface of the Fermi energy to escape to the vacuum energy level, the smaller the value of the work function will be. As shown in Figure 3a,b, the calculated work functions of pristine 2H-VS_2 , $\text{CIPSe}\uparrow$, and $\text{CIPSe}\downarrow$ monolayers are 5.90, 4.44, and 5.13 eV, respectively, indicating that the electrons flow from the CIPSe layer to the 2H-VS_2 layer when the 2H-VS_2 monolayer combines with the CIPSe monolayer to form a heterostructure due to the smaller work function of CIPSe. Eventually, the 2H-VS_2 layer gains negative electrons while the CIPSe layer accumulates positive charge. Since the work function of $\text{CIPSe}\uparrow$ (4.44 eV) is smaller than that of the $\text{CIPSe}\downarrow$ (5.13 eV), it is easier to lose electrons for the $\text{CIPSe}\uparrow$ case when FE polarization is upward, which is consistent with the result of Bader charge. Specifically, for the $\text{VS}_2/\text{CIPSe}\uparrow$, the charge with an amount of 0.067 electrons is transferred from CIPSe to VS_2 ; meanwhile, for the case of $\text{VS}_2/\text{CIPSe}\downarrow$, the charge transfer occurs the other way around with the value of

0.053 electrons, as demonstrated by the plane-integrated electron density difference along the vertical direction shown in Figure 3c,d. In addition, this result is also consistent with the optimized interlayer distance for each situation. As shown in Figure 2, the interlayer distance of VS₂/CIPSe_↑ (3.27 Å) is smaller than the corresponding value of VS₂/CIPSe_↓, which results in stronger electron interactions between the layers. It should be noted that the present results also indicate different strain effects that will be further analyzed in the following section.

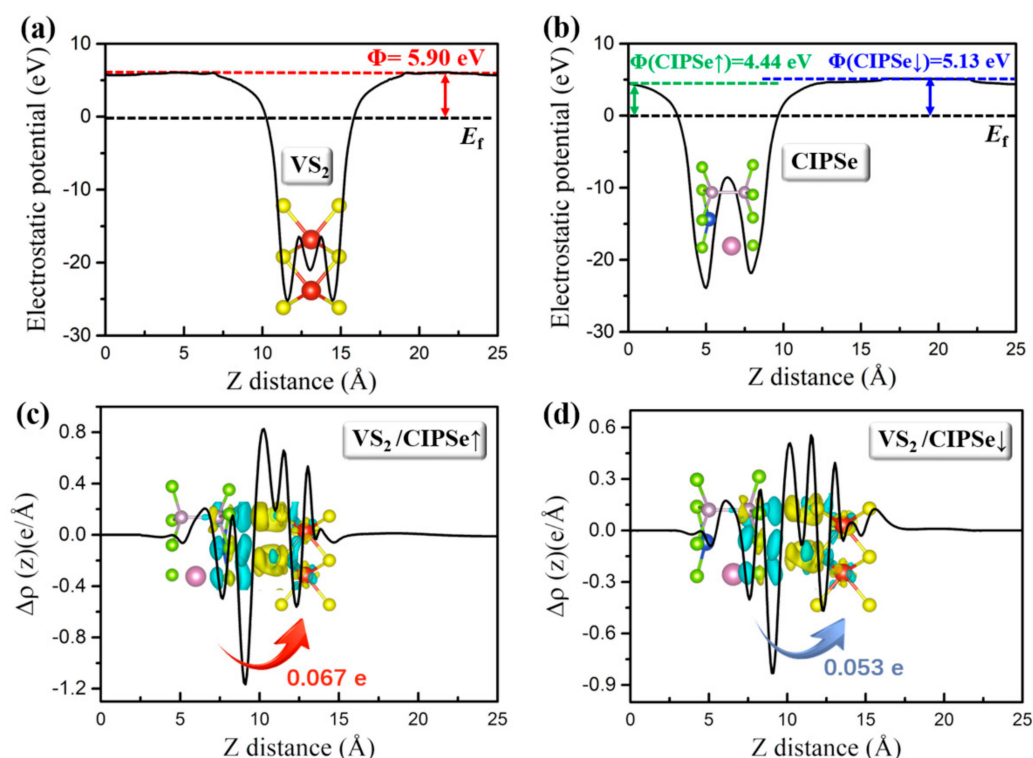


Figure 3. (a,b) Electrostatic potential and work functions (Φ) for pristine 2H-VS₂ (a) and CIPSe (b), respectively. The electrostatic potential is defined with respect to Fermi energy (E_f). Φ therefore indicates the required energy to remove an electron at Fermi level from the material to a state at rest in the vacuum nearby the surface. (c,d) The plane-integrated electron density difference along the vertical direction for the VS₂/CIPSe_↑ (c) and VS₂/CIPSe_↓ (d) heterojunctions. The insets represent the 3D isosurface of differential charge densities for the VS₂/CIPSe heterojunctions. The yellow and cyan regions represent electron accumulation and depletion, respectively, and the isosurface value is set to be 0.0002 e/Å³.

3.3. In-Plane Biaxial Strain Effect on the 2H-VS₂/CIPSe Heterostructures

It is well-known that strain engineering is an effective method to modulate the electronic and transport characteristics in 2D nanoscale electronic devices. In practical applications, strain engineering can achieve different compressive and tensile strains by bending the substrate attached to 2D materials [33,48]. Due to the mismatch of lattice constants between VS₂ and CIPSe, it is necessary to evaluate the most stable lattice constant of the heterostructure. Figure 4a shows the relationship between the total energies and the applied biaxial strains for the pure VS₂, 2H-VS₂/CIPSe_↑, and 2H-VS₂/CIPSe_↓ structures, respectively. For each system, the minimum total energy appears in the unstrained case, which is reasonable and confirms the fully relaxed structures as well.

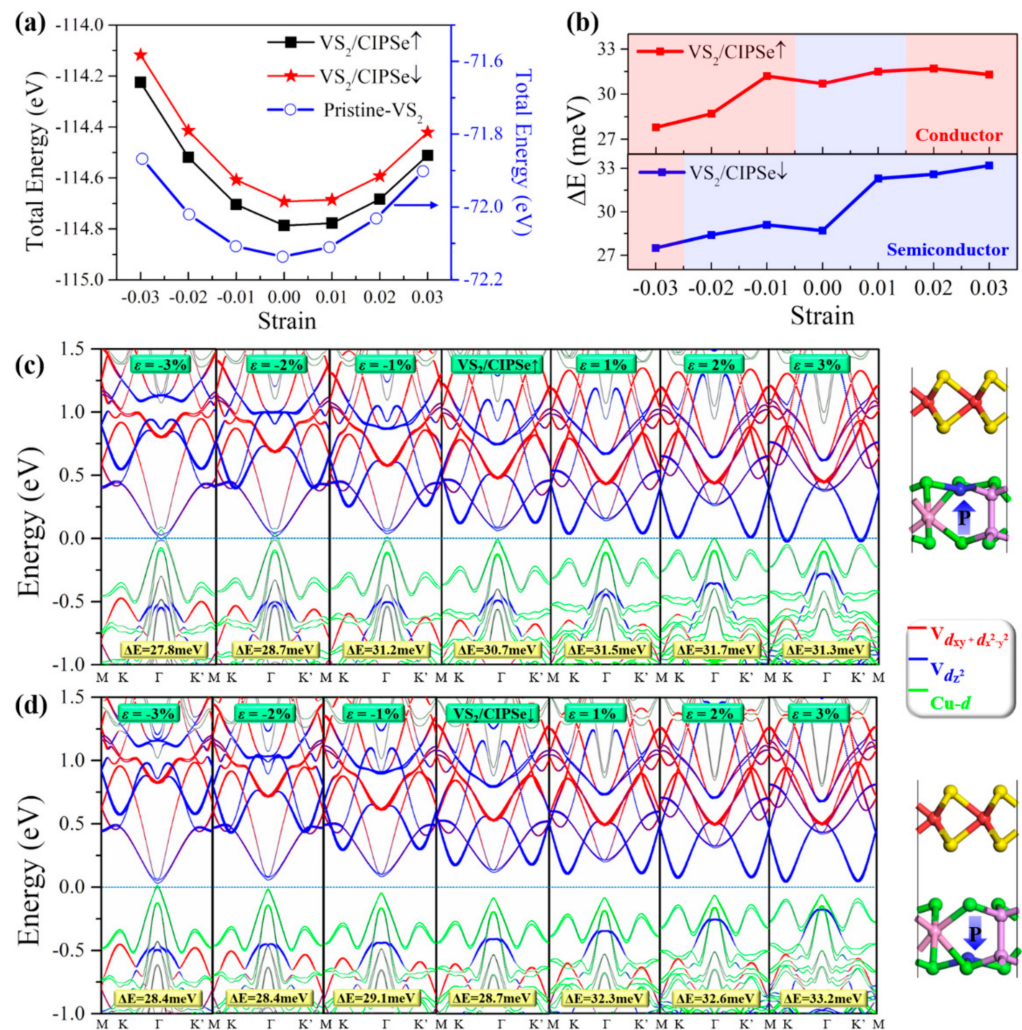


Figure 4. In-plane biaxial strain effect on valley splitting and band structures with SOC of VS₂/CIPSe heterostructures. (a) relationships between total energies and biaxial strains (black, red, and blue curves are for VS₂/CIPSe↑, VS₂/CIPSe↓ and pristine VS₂, respectively); (b) valley splitting energies (ΔE) under biaxial strains for VS₂/CIPSe↑, VS₂/CIPSe↓, red and blue area indicate conductor and semiconductor behaviors. (c,d) valley splitting and band structures with SOC of VS₂/CIPSe heterostructures under biaxial strains with upward (c) and downward (d) ferroelectric polarization. The red, blue, and green lines denote the contributions from $V-d_{xy} + d_{x^2-y^2}$, $V-d_{z^2}$ and Cu-d orbitals, respectively. The Fermi level is set to zero.

Figure 4b shows the valley splitting energies (ΔE) of the VS₂/CIPSe↑ and VS₂/CIPSe↓ with respect to the applied biaxial strains. Similar to the result shown in Figure 2c, ΔE of the strained structures are only slightly fluctuated compared with that of the unstrained structure. Nevertheless, for the VS₂/CIPSe↑ system, under the influence of biaxial strain, both stretching and compressing strains result in the transform from semiconductor to conductor. Specifically, when the heterostructure is stretched, the conducting feature mainly originates from the fact that the CBM at points K and K' cross the Fermi level; meanwhile, when the system is compressed, both the CBM and VBM at the central high-symmetry point G pass through the Fermi level, which also leads to a conducting characteristic of the heterostructure. Since the valleytronic polarization is only effective in a semiconductor, the above situation can be considered as the disappearance of valleytronic characteristics in the material. In fact, a similar situation was also reported in 2H-VSe₂/P↑ heterostructure in recent literature [49], in which the half-metallic characteristic of the system indicates that the valleytronic nature is turned off. On the other hand, the VS₂/CIPSe↓ heterostructure

remains semiconducting with the influence of most strains except for the situation of the -0.03 strain. The corresponding partial density of states (PDOS) for both spin-up and spin-down electrons under biaxial strains for AB-stacking $\text{VS}_2/\text{CIPSe}\uparrow$, pristine VS_2 , and $\text{VS}_2/\text{CIPSe}\downarrow$ heterostructures are shown in Figure S3 of the Supplementary Materials. In addition, for the intralayer FM configuration of VS_2 , the total magnetic moment of pristine VS_2 remains unchanged, as seen with the black line in Figure S3d. In contrast, the magnetic moments of VS_2/CIPSe heterostructures increase with the applied tensile strain and decline with the compressive strains. Particularly, the magnetic moment of $\text{VS}_2/\text{CIPSe}\uparrow$ is more sensitive to the external strains, compared to $\text{VS}_2/\text{CIPSe}\downarrow$ systems, due to the stronger interface interaction between VS_2 and $\text{CIPSe}\uparrow$, as the differential charge density shown in Figure 3c,d. It should be noted that, in DFT calculations, the temperature is considered as 0 K, and it is true that the valley splitting energy changes slightly, which is hard to be detected in experiments at room temperature. However, when combining the electronic structures under biaxial strains, the transition from semiconductor to metal helps to turn on/off the valley polarizations. This is intriguing and important as it demonstrates that the biaxial strain combined with the controllable FE polarizations could serve as a switch for the valleytronic nature of the material.

As detailed above, the valley splitting energy of pure 2H- VS_2 monolayer can be tuned by external strains within a quite small range from 27.8 to 31.8 meV. Therefore, a ferroelectric substrate of CIPSe monolayer is added to form heterostructures. By utilizing the different interlayer effects between 2H- VS_2 and CIPSe layers with upwards and downwards FE polarizations, respectively, a ferrovalley switch has been achieved when in-plane strains are applied simultaneously. Accordingly, we can design an ideal switchable valleytronic device based on 2H- VS_2/CIPSe heterostructures, as the schematic design plotted in Figure 5. Such a scheme for designing valleytronic switch in 2H- VS_2/CIPSe heterostructures is also expected to be applicable for other intrinsic valley TMDs combined with FE substrates.

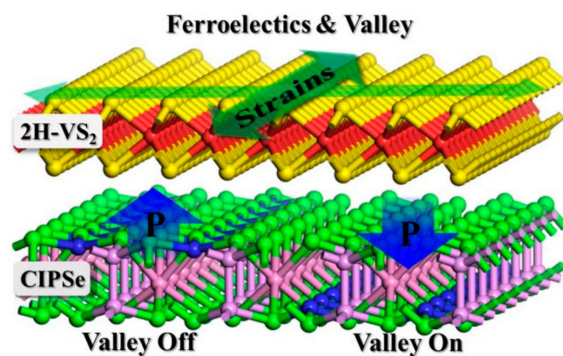


Figure 5. The schematic design for applications of the tunable ferrovalley of 2H- VS_2 monolayer under both in-plane strains and ferroelectric CIPSe substrate in 2H- VS_2/CIPSe heterostructures.

4. Conclusions

In this paper, the ferrovalley polarization, electronic structure, and magnetic properties of 2D 2H- VS_2/CIPSe heterostructures with different stacking patterns and FE polarization have been investigated by using first-principles calculations. It is shown that the valley splitting of monolayer VS_2 can be affected by the CIPSe substrate with FE polarization. In addition, the reversed orientation of FE polarization of the CIPSe substrate can modulate the magnitude of valley splitting. It is found that the biaxial strains play an important role in the modulation of valleytronic nature of the heterostructures. Although the valley splitting energies of the strained structures are only slightly fluctuated compared with that of the unstrained structure, the biaxial strain combined with the FE polarization could serve as an effective switch for the valleytronic nature of the material. The controllable valley polarization and the strain modulation mechanism revealed in the present work demonstrate that the 2H- VS_2/CIPSe heterostructures are promising candidates for the applications in 2D valleytronic devices.

Supplementary Materials: The following supporting information can be downloaded at: <https://www.mdpi.com/article/10.3390/nano12142461/s1>. 1T and 2H configurations of VS₂ and the corresponding spin-resolved energy band structures; three kinds of stacking patterns of 2H-VS₂/CIPSe heterostructures; the PDOS and total magnetic moments of the AB-stacking heterostructures and the pristine VS₂ under biaxial strains.

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Conflicts of Interest: The authors declare no conflicts.

References

1. Gupta, A.; Sakthivel, T.; Seal, S. Recent development in 2D materials beyond graphene. *Prog. Mater. Sci.* **2015**, *73*, 44–126. [[CrossRef](#)]
2. Lemme, M.C.; Akinwande, D.; Huyghebaert, C.; Stampfer, C. 2D materials for future heterogeneous electronics. *Nat. Commun.* **2022**, *13*, 1392. [[CrossRef](#)]
3. Novoselov, K.S.; Mishchenko, A.; Carvalho, A.; Castro Neto, A.H. 2D materials and van der Waals heterostructures. *Science* **2016**, *353*, aac9439. [[CrossRef](#)]
4. Mei, J.; He, T.; Bai, J.; Qi, D.; Du, A.; Liao, T.; Ayoko, G.A.; Yamauchi, Y.; Sun, L.; Sun, Z. Surface-Dependent Intermediate Adsorption Modulation on Iridium-Modified Black Phosphorus Electrocatalysts for Efficient pH-Universal Water Splitting. *Adv. Mater.* **2021**, *33*, 2104638. [[CrossRef](#)] [[PubMed](#)]
5. Tang, X.; Sun, W.; Gu, Y.; Lu, C.; Kou, L.; Chen, C. CoB₆ monolayer: A robust two-dimensional ferromagnet. *Phys. Rev. B* **2019**, *99*, 045445. [[CrossRef](#)]
6. Yang, L.-M.; Bačić, V.; Popov, I.A.; Boldyrev, A.I.; Heine, T.; Frauenheim, T.; Ganz, E. Two-Dimensional Cu₂Si Monolayer with Planar Hexacoordinate Copper and Silicon Bonding. *J. Am. Chem. Soc.* **2015**, *137*, 2757–2762. [[CrossRef](#)] [[PubMed](#)]
7. Liu, Y.; Zhang, S.; He, J.; Wang, Z.M.; Liu, Z. Recent Progress in the Fabrication, Properties, and Devices of Heterostructures Based on 2D Materials. *Nano-Micro Lett.* **2019**, *11*, 13. [[CrossRef](#)]
8. Zhu, Z.; Chen, X.; Li, W.; Qi, J. Electric field control of the semiconductor-metal transition in two dimensional CuInP₂S₆/germanene van der Waals heterostructure. *Appl. Phys. Lett.* **2019**, *114*, 223102. [[CrossRef](#)]
9. Tu, Z.; Wu, M.; Zeng, X.C. Two-Dimensional Metal-Free Organic Multiferroic Material for Design of Multifunctional Integrated Circuits. *J. Phys. Chem. Lett.* **2017**, *8*, 1973–1978. [[CrossRef](#)]
10. Tang, X.; Shang, J.; Gu, Y.; Du, A.; Kou, L. Reversible gas capture using a ferroelectric switch and 2D molecule multiferroics on the In₂Se₃ monolayer. *J. Mater. Chem. A* **2020**, *8*, 7331–7338. [[CrossRef](#)]
11. Ayadi, T.; Debbichi, L.; Badawi, M.; Said, M.; Rocca, D.; Lebègue, S. An ab initio study of the electronic properties of the ferroelectric heterostructure In₂Se₃/Bi₂Se. *Appl. Surf. Sci.* **2021**, *538*, 148066. [[CrossRef](#)]
12. Burch, K.S.; Mandrus, D.; Park, J.-G. Magnetism in two-dimensional van der Waals materials. *Nature* **2018**, *563*, 47–52. [[CrossRef](#)] [[PubMed](#)]
13. Gibertini, M.; Koperski, M.; Morpurgo, A.F.; Novoselov, K.S. Magnetic 2D materials and heterostructures. *Nat. Nanotechnol.* **2019**, *14*, 408–419. [[CrossRef](#)] [[PubMed](#)]
14. Sun, W.; Wang, W.; Li, H.; Zhang, G.; Chen, D.; Wang, J.; Cheng, Z. Controlling bimerons as skyrmion analogues by ferroelectric polarization in 2D van der Waals multiferroic heterostructures. *Nat. Commun.* **2020**, *11*, 5930. [[CrossRef](#)]
15. Huang, C.; Du, Y.; Wu, H.; Xiang, H.; Deng, K.; Kan, E. Prediction of Intrinsic Ferromagnetic Ferroelectricity in a Transition-Metal Halide Monolayer. *Phys. Rev. Lett.* **2018**, *120*, 147601. [[CrossRef](#)]
16. Xue, F.; Wang, Z.; Hou, Y.; Gu, L.; Wu, R. Control of magnetic properties of MnBi₂Te₄ using a van der Waals ferroelectric II I₂-VI₃ film and biaxial strain. *Phys. Rev. B* **2020**, *101*, 184426. [[CrossRef](#)]
17. Shang, J.; Tang, X.; Gu, Y.; Krashennnikov, A.V.; Picozzi, S.; Chen, C.; Kou, L. Robust Magnetoelectric Effect in the Decorated Graphene/In₂Se₃ Heterostructure. *ACS Appl. Mater. Interfaces* **2021**, *13*, 3033–3039. [[CrossRef](#)]
18. Cheng, H.-X.; Zhou, J.; Wang, C.; Ji, W.; Zhang, Y.-N. Nonvolatile electric field control of magnetism in bilayer CrI₃ on monolayer In₂Se₃. *Physical Rev. B* **2021**, *104*, 064443. [[CrossRef](#)]
19. Bafekry, A.; Gogova, D.; Fadlallah, M.M.; Chuong, N.V.; Ghergherehchi, M.; Faraji, M.; Feghhi, S.A.H.; Oskoeian, M. Electronic and optical properties of two-dimensional heterostructures and heterojunctions between doped-graphene and C- and N-containing materials. *Phys. Chem. Chem. Phys.* **2021**, *23*, 4865–4873. [[CrossRef](#)]
20. Xia, F.; Wang, H.; Xiao, D.; Dubey, M.; Ramasubramaniam, A. Two-dimensional material nanophotonics. *Nat. Photonics* **2014**, *8*, 899–907. [[CrossRef](#)]

21. Zhou, B.; Jiang, K.; Shang, L.; Zhang, J.; Li, Y.; Zhu, L.; Gong, S.-J.; Hu, Z.; Chu, J. Enhanced carrier separation in ferroelectric $\text{In}_2\text{Se}_3/\text{MoS}_2$ van der Waals heterostructure. *J. Mater. Chem. C* **2020**, *8*, 11160–11167. [[CrossRef](#)]
22. Wijethunge, D.; Zhang, L.; Tang, C.; Du, A. Tuning band alignment and optical properties of 2D van der Waals heterostructure via ferroelectric polarization switching. *Front. Phys.* **2020**, *15*, 63504. [[CrossRef](#)]
23. Androulidakis, C.; Zhang, K.; Robertson, M.; Tawfick, S. Tailoring the mechanical properties of 2D materials and heterostructures. *2D Mater.* **2018**, *5*, 032005. [[CrossRef](#)]
24. Liu, K.; Wu, J. Mechanical properties of two-dimensional materials and heterostructures. *J. Mater. Res.* **2016**, *31*, 832–844. [[CrossRef](#)]
25. Wei, Y.; Yang, R. Nanomechanics of graphene. *Natl. Sci. Rev.* **2019**, *6*, 324–348. [[CrossRef](#)]
26. Schaibley, J.R.; Yu, H.; Clark, G.; Rivera, P.; Ross, J.S.; Seyler, K.L.; Yao, W.; Xu, X. Valleytronics in 2D materials. *Nat. Rev. Mater.* **2016**, *1*, 16055. [[CrossRef](#)]
27. Zhu, Z.; Collaudin, A.; Fauqué, B.; Kang, W.; Behnia, K. Field-induced polarization of Dirac valleys in bismuth. *Nat. Phys.* **2012**, *8*, 89–94. [[CrossRef](#)]
28. Zhang, C.; Nie, Y.; Sanvito, S.; Du, A. First-Principles Prediction of a Room-Temperature Ferromagnetic Janus VSSe Monolayer with Piezoelectricity, Ferroelasticity, and Large Valley Polarization. *Nano Lett.* **2019**, *19*, 1366–1370. [[CrossRef](#)] [[PubMed](#)]
29. Xiao, D.; Liu, G.-B.; Feng, W.; Xu, X.; Yao, W. Coupled Spin and Valley Physics in Monolayers of MoS_2 and Other Group-VI Dichalcogenides. *Phys. Rev. Lett.* **2012**, *108*, 196802. [[CrossRef](#)]
30. Zhang, Z.; Liu, X.; Yu, J.; Hang, Y.; Li, Y.; Guo, Y.; Xu, Y.; Sun, X.; Zhou, J.; Guo, W. Tunable electronic and magnetic properties of two-dimensional materials and their one-dimensional derivatives. *WIREs Comput. Mol. Sci.* **2016**, *6*, 324–350. [[CrossRef](#)]
31. Yang, F.; Shang, J.; Kou, L.; Li, C.; Deng, Z. Computational Investigation of Orderly Doped Transition Metal Dichalcogenides: Implications for Nanoscale Optoelectronic Devices. *ACS Appl. Nano Mater.* **2022**, *5*, 3824–3831. [[CrossRef](#)]
32. Tong, W.-Y.; Tong, W.-Y.; Gong, S.-J.; Wan, X.; Duan, C.-G. Concepts of ferrovalley material and anomalous valley Hall effect. *Nat. Commun.* **2016**, *7*, 13612. [[CrossRef](#)] [[PubMed](#)]
33. Ma, X.; Yin, L.; Zou, J.; Mi, W.; Wang, X. Strain-Tailored Valley Polarization and Magnetic Anisotropy in Two-Dimensional $2\text{H-VS}_2/\text{Cr}_2\text{C}$ Heterostructures. *J. Phys. Chem. C* **2019**, *123*, 17440–17448. [[CrossRef](#)]
34. Guo, Y.; Deng, H.; Sun, X.; Li, X.; Zhao, J.; Wu, J.; Chu, W.; Zhang, S.; Pan, H.; Zheng, X.; et al. Modulation of Metal and Insulator States in 2D Ferromagnetic VS_2 by van der Waals Interaction Engineering. *Adv. Mater.* **2017**, *29*, 1700715. [[CrossRef](#)] [[PubMed](#)]
35. Jing, Y.; Zhou, Z.; Cabrera, C.R.; Chen, Z. Metallic VS_2 Monolayer: A Promising 2D Anode Material for Lithium Ion Batteries. *J. Phys. Chem. C* **2013**, *117*, 25409–25413. [[CrossRef](#)]
36. Zhao, R.; Wang, T.; Zhao, M.; Xia, C.; An, Y.; Dai, X. Modulation of the electronic properties and spin polarization of 2H VS_2 nanoribbons by tuning ribbon widths and edge decoration. *Phys. Chem. Chem. Phys.* **2019**, *21*, 18211–18218. [[CrossRef](#)] [[PubMed](#)]
37. Xiong, W.; Xia, C.; Du, J.; Wang, T.; Zhao, X.; Peng, Y.; Wei, Z.; Li, J. Electrostatic gating dependent multiple-band alignments in a high-temperature ferromagnetic $\text{Mg}(\text{OH})_2/\text{VS}_2$ heterobilayer. *Phys. Rev. B* **2017**, *95*, 245408. [[CrossRef](#)]
38. He, P.; Yan, M.; Zhang, G.; Sun, R.; Chen, L.; An, Q.; Mai, L. Layered VS_2 Nanosheet-Based Aqueous Zn Ion Battery Cathode. *Adv. Energy Mater.* **2017**, *7*, 1601920. [[CrossRef](#)]
39. Mikhaleva, N.S.; Visotin, M.A.; Kuzubov, A.A.; Popov, Z.I. VS_2 /Graphene Heterostructures as Promising Anode Material for Li-Ion Batteries. *J. Phys. Chem. C* **2017**, *121*, 24179–24184. [[CrossRef](#)]
40. Lin, H.; Jin, X.; Lou, N.; Yang, D.; Jin, R.; Huang, Y. Metallic VS_2 /blue phosphorene heterostructures as promising anode materials for high-performance lithium ion batteries: A first principles study. *Appl. Surf. Sci.* **2020**, *533*, 147478. [[CrossRef](#)]
41. Kresse, G.; Furthmüller, J. Efficient iterative schemes for ab initio total-energy calculations using a plane-wave basis set. *Phys. Rev. B* **1996**, *54*, 11169–1118642. [[CrossRef](#)] [[PubMed](#)]
42. Perdew, J.P.; Burke, K.; Ernzerhof, M. Generalized Gradient Approximation Made Simple. *Phys. Rev. Lett.* **1996**, *77*, 3865–3868. [[CrossRef](#)] [[PubMed](#)]
43. Isaacs, E.B.; Marianetti, C.A. Electronic correlations in monolayer VS_2 . *Physical Rev. B* **2016**, *94*, 03512. [[CrossRef](#)]
44. Grimme, S.; Antony, J.; Ehrlich, S.; Krieg, H. A consistent and accurate ab initio parametrization of density functional dispersion correction (DFT-D) for the 94 elements H–Pu. *J. Chem. Phys.* **2010**, *132*, 154104. [[CrossRef](#)]
45. Bian, X.; Lian, S.; Fu, B.; An, Y. Tunable spin-valley splitting and magnetic anisotropy of two-dimensional $2\text{H-VS}_2/\text{h-VN}$ heterostructure. *J. Magn. Magn. Mater.* **2022**, *546*, 168867. [[CrossRef](#)]
46. Yue, Y. First-Principles Studies of the Magnetic Anisotropy of Monolayer VS_2 . *J. Supercond. Nov. Magn.* **2017**, *30*, 1201–1206. [[CrossRef](#)]
47. Wang, C.; An, Y. Effects of strain and stacking patterns on the electronic structure, valley polarization and magnetocrystalline anisotropy of layered VTe_2 . *Appl. Surf. Sci.* **2021**, *538*, 148098. [[CrossRef](#)]
48. Shang, J.; Qiao, S.; Fang, J.; Wen, H.; Wei, Z. Strain driven band alignment transition of the ferromagnetic $\text{VS}_2/\text{C}_3\text{N}$ van der Waals heterostructure. *Chin. Phys. B* **2021**, *30*, 097507. [[CrossRef](#)]
49. Lei, C.; Xu, X.; Zhang, T.; Huang, B.; Dai, Y.; Ma, Y. Nonvolatile Controlling Valleytronics by Ferroelectricity in $2\text{H-VSe}_2/\text{Sc}_2\text{CO}_2$ van der Waals Heterostructure. *J. Phys. Chem. C* **2021**, *125*, 2802–2809. [[CrossRef](#)]