SCIENTIFIC REPORTS

natureresearch

OPEN Sub-wavelength annular-slit**assisted superoscillatory lens for longitudinally-polarized superresolution focusing**

Hyuntai Kim1* & Edward T. F. Rogers2,3

A binary metallic superoscillatory lens assisted with annular subwavelength slits is proposed, which generates a longitudinally-polarized super-resolution focal point. The annular slits are designed to selectively transmit radially-polarized light. Simulations using the fnite element method show a 0.24 λ focal spot with 21.8dB of polarization purity and only 0.342dB reduction in efciency compared to a standard superoscillatory lens.

The classical restriction on the resolution of focusing, caused by the diffractive nature of light and known as Abbe's difraction limit, has historically been a strong constraint on the resolution of various optical systems. In recent years, however, it has been shown that light can be focused well below the difraction limit in the far feld by exploiting the phenomenon of superoscillation, where light oscillates faster than its highest Fourier component in a specific local region^{1-[4](#page-6-1)}. Optical superoscillations have been realized by means of spatial light modulators, optical eigenmode methods, metasurfaces, and binary lenses⁵⁻¹⁰.

Especially important is the binary superoscillatory lens (SOL) as it is relatively easy to fabricate and has a simple structure. Various SOLs have been studied for purposes including generation of optical needles, achromatic super-resolution (SR) focusing, and far-field SR focusing $11-16$ $11-16$.

Longitudinally polarized (LP) light is generated whenever radially polarized (RP) light is focused down with high numerical aperture¹⁷⁻²¹. A true LP focus contains only polarization components in the direction of propagation, which has advantages in various applications (compared to linearly- and circularly-polarized light) due to smaller spots formed at a LP focus and radially symmetric optical forces. LP foci also improve SR focusing, thus LP-SR focusing is an essential tool in nano-applications such as particle trapping, particle acceleration, and high-resolution imaging^{[22](#page-6-8),[23](#page-6-9)}. Recently, sub-diffraction longitudinally polarized focusing using binary phase lenses and RP input has been reported $24,25$ $24,25$.

Despite these many benefts, LP foci are not widely used in practical applications, primarily because the necessary RP input is difcult to generate and align. For linearly- or circularly-polarized inputs, additional free-space optical components are required to convert the polarization state, which complicates the whole system²⁶. For waveguide inputs, such as optical fbre modes, one can prepare cylindrical vector states – which are composed of a superposition of radial, azimuthal, and hybridized degenerate modes – by means of donut shaped active fbre, or long-period-grating mode couplers^{27–[29](#page-6-14)}. In these cases, however, an additional polarizer is still required to extract the RP component. Even afer the RP input is properly prepared, the incident RP light must be carefully centered on the SOL or other focusing optic, which requires additional efort. Any misalignment of either the free-space RP generator or the focusing optic, which can easily occur due to external drifs, causes rapid degradation of modal purity which in turn degrades the LP-SR focusing efects and results in larger focal spots and/or generation of other polarization components at the focus.

It is well known that metallic subwavelength slit arrays are polarization selective: they transmit light polarized perpendicular to the slits and block the component polarized parallel to the slits. The effect can be understood by considering the movement of electrons, extraordinary optical transmission phenomena based on surface plas-mon polaritons, or from effective medium theory (EMT)^{30[,31](#page-6-16)}. One of the most widely used applications is the wire-grid polarizer, and it is also known that annular subwavelength metallic slits can transmit RP components

1Electrical and Electronic Convergence Department, Hongik University, Sejong, 30016, Republic of Korea. ²Optoelectronics Research Centre, University of Southampton, Southampton, SO17 1BJ, UK.³Institute for Life Sciences, University of Southampton, Southampton, SO17 1BJ, UK. *email: hyuntai@hongik.ac.kr

but block azimuthally polarized (AP) components. The authors have recently studied annular subwavelength slits theoretically and proposed a zone plate consisting of subwavelength rings which could selectively focus RP light³⁰.

Here, we propose a novel sub-wavelength annular slit (SAS) assisted SOL (SAS-SOL) structure which only transmits RP light and therefore generates a LP-SR focal point, while blocking other polarization components. Inspired by metallic subwavelength ring arrays, we apply an annular substructure to SOL and achieve pure RP components which are focused to a LP-SR hotspot from a single binary metallic surface. We stress here that the method we are developing is generally applicable and can be applied to any existing SOL design. In the main body of the work below, we chose an existing design [ref. [12](#page-6-17)] and modify it by adding subwavelength slits for polarization selectivity. The precise lens design is not important, as is demonstrated in subsection "Robustness and general applicability" where we simulate a range of other SOL designs from the literature and demonstrate that the SAS-SOL principle works equally well with all of them.

The most obvious light source for SAS-SOL would be mode-selected cylindrical waveguides, for example optical fibre, which generate both RP and AP components²⁶. If a free-space focusing system is preferred, then prepared RP beam would be focused correctly by the SAS-SOL. It should also be noted that having the focusing

Figure 2. (**a**) Field intensity along the radial axis at the focal plane as a function of polarization ratio. (**b**) FWHM beam size at the focal plane as a function of polarization ratio.

component fixed on the fibre facet makes alignment much simpler and improves efficiency^{[6](#page-6-18),[18](#page-6-19)}. Thus, the proposed SAS-SOL simplifes the system by polarizing the input itself, and thus makes alignment signifcantly easier. Below, we frst characterize the polarization performance of the SOL and SAS separately, and then rigorous simulations are performed to characterize and optimize the SAS-SOL to achieve high efficiency LP-SR focusing.

Results

SOL without subwavelength rings. To understand what is required of the SAS-SOL, we must frst analyze how each polarization component is focused by the SOL. Here we use the SOL design from ref. [12](#page-6-17) as the basis for our calculations. The lens has a diameter of 20 μ m, and consists of 25 transparent annular regions. The full lens specification can be found in Supplementary Information of ref. ¹². The lens which has a known focal length of 9.8 µm for 640 nm light in the immersion oil used here (see Methods). We calculate the feld intensity at the SOL focus for varying ratios of RP to AP input. The focal spot (in the *xy* plane) and cross-sectional (*xz*) view of the results are shown in Fig. [1.](#page-1-0) The mixed input has equal proportion of RP and AP input. It is worth mentioning that our finite element method (FEM) simulation results show good agreement with to the previous experiment¹², which confrms the reliability of our numerical results.

In Fig. [1](#page-1-0) we see very signifcant diferences between the cases where AP and RP light illuminate the SOL, as would be expected. Figure [1](#page-1-0) shows the AP component generates a donut-like field at the focal plane. The AP light retains its azimuthal symmetry as it is focused down, therefore all the felds at the center are cancelled due to cylindrical symmetry, and so the intensity is zero on the *z* axis. The peak of the donut-shaped field is at a radius $r=138$ nm, which has the effect of enlarging the LP-SR focusing point when using mixed illumination. The RP-illuminated focal spot is tightly confned (full width half max, FWHM=151nm) and (by symmetry) contains only LP components.

To quantify the efficiency of focusing, we calculate the total energy in the focal spot for both RP and AP by integrating the intensity in the region inside the FWHM of the RP SR focus. We then calculate the polarization extinction ratio (PER) as the ratio of the energy between RP input and AP input, and the calculated PER of the SOL without sub-slits was 5.29dB.

The field intensity at the focal plane and the beam width are both shown in Fig. [2](#page-2-0) as a function of the mode ratio. From Fig. $2(a)$, we see that when the AP component exceeds 50%, the maximum is shifted from the center axis, where the lens no longer forms a well-defned focus at the focal plane. In addition, Fig. [2\(b\)](#page-2-0) shows that the beam width increases rapidly as the portion of AP component increases. The results show that if 40% of AP component is present, beam size increases to 200nm, which is no longer sub-difraction limited. Moreover, the AP component has azimuthal ($φ$) polarization at the focal plane, which hinders the pure LP focusing. Therefore, maintaining pure RP at the SOL is essential for high quality LP-SR focusing.

SOL with subwavelength rings. To apply the annular slit arrays to our SOL, we substitute the transparent region of the SOL with subwavelength rings, which act as a wire-grid polarizer. A schematic of the RP-SOL is shown in Fig. [3.](#page-3-0) The RP-SOL will behave as a metallic layer for AP input components (and therefore block them) and will be transparent to the RP input components, (and therefore act as an SOL), overall forming an LP-SR focal point. The main design parameters of the subwavelength ring slits are: thickness of the metallic layer, the period of the slit, and the duty ratio between the metallic region and dielectric region, as depicted in Fig. [3\(a\).](#page-3-0)

To optimize the transmission and PER of the annular slits, we frst optimize the thickness, duty ratio, and slit width without considering the SOL super-structure. Each parameter has trade-ofs. In principal, the period does not affect the transmission in EMT, but high period structures ($> 0.5 \lambda$) caused the EMT approximation to fail as they cannot be considered as a single material. As the slit period increases, its polarization selectivity reduces and it permits AP light to be transmitted. There is another problem for long periods: as (in general) not all openings of SOL are exact multiples of the period, sub-wavelength annular rings positioned at the edge of the SOL opening can have uneven width compared to the other rings. Tese slits then have a phase propagation constant slightly different from that of the standard-width slits, which can disturb the transmitted field. The larger the period, the

Figure 3. (**a**) Schematic of RP SOL. (**b**) Polarization-selective behaviours of the RP-SOL.

Figure 4. (**a**) Efective refractive index calculated via EMT. (**b**) Electric feld intensity at the focal position for RP and AP input in terms of duty ratio.

Figure 5. (**a**) Electric feld intensity at the focal position for RP and AP input as a function of duty ratio. (**b**) Electric intensity distribution as a function of metal thickness for RP input.

higher the weight of the slit on this edge, which in turn leads to a decrease in the SOL efficiency. However, a short period causes makes the SAS-SOL harder to manufacture and may reduce the durability of the lens.

The duty ratio determines the effective refractive index of the annular slit arrays. A higher proportion of dielectric material reduces the loss, but also reduces the polarization selectivity (allowing more AP light through). A higher metallic proportion results in high imaginary component, therefore it efficiently blocks the AP component but also results in higher loss for RP inputs. The theoretically calculated effective indices for RP and AP input are shown in Fig. [4\(a\)](#page-3-1). The imaginary part of the index for each polarization component shows the effect of the duty

Figure 6. (**a**) Side view and (**b**) top view of the electric feld intensity when RP, mixed, and AP light illuminates the SAS-SOL.

ratio. The field intensity at the focal point for each polarization in terms of duty ratio are shown in Fig. [4\(b\)](#page-3-1). One can observe that the AP component is nearly eliminated for duty ratio < 0.4 .

In terms of thickness, as the AP response of the nano sub-slits is similar to metal, and so the transmission of the AP component decays exponentially as a function of metal thickness. For the RP response, the transmission has a peak at thickness of ~100 nm, and slowly decays because the effective medium acts as a lossy dielectric. The electric field intensity at the desired hotspot as a function of medium thickness is shown in Fig. [5](#page-3-2). The electric feld intensity decays exponentially for AP input, and the RP input shows a maximum at a thickness of around 90nm. Note that for thin metal thickness (<30nm) the incident light is not properly blocked, so the SOL fails to focus even for RP incident light.

We fnd the intensity of SR focus is optimized at a duty ratio of 0.71, period of 75nm, and metal thickness of 92 nm. The focal spots for a SAS-SOL with these optimised parameters for RP, AP and mixed inputs are shown in Fig. [6](#page-4-0). It is clear that the AP component is strongly filtered out, especially around the SR spot. The field distribution for RP input is almost identical to that for a conventional SOL lens with FWHM = 152 nm (0.24 λ_0) and 0.36 λ_{oil} , and the efficiency shows only 0.342 dB of degradation, and the PER is 21.8 dB, giving 16.5 dB of improvement.

Figure 7. Electric feld intensity distribution at the focal plane of the SAS-SOL (solid lines) and SOL without sub-slits (dashed lines) with AP input (blue lines) and RP input (red lines). The focusing medium is (a) oil and (**b**) air.

Robustness and general applicability. Having shown the design process and specifc results above, we now must demonstrate that SAS-SOLs designed in this way can feasibly be fabricated, and that the method is not limited to that particular design, but can be extended to other designs from the literature. First, we have simulated our designed structure with relatively large marginal errors of ± 10 in both duty cycle and metal thickness. We do not vary the period this is stable in most fabrication processes. The results showed the FWHM was 153.8 nm, which is only 1.18% larger than the optimized case. The PER was more than 18.83 dB, where it was 21.8 dB originally. The output intensity fluctuated within a range of 10.69% (0.49 dB). Note that when the duty ratio was smaller (i.e. smaller open slits), the PER was increased, and when the duty ratio was larger (i.e. larger slits), the output power increased. Tus we show that even allowing for 10% marginal errors in fabrication the SAS-SOL can efectively generate a pure radially-polarised superoscillatory focus.

In addition, we have applied our SAS approach to other published SOLs from ref. ^{[32](#page-6-20)}. We have chosen two designs, SOL₅ and SOL₄ in table 1 from ref.^{[32](#page-6-20)}. For SOL₅, we have used the same materials – focusing in oil and using chromium – hereinafter "oil SOL". And for SOL₄, the light was focused in air and the metal was selected as aluminium – hereinafer, "air SOL". As the conditions were same for the oil SOL as for our original design, no other optimization was required. However, as the materials were changed for the air SOL, we have optimized the duty ratio, period, and metal thickness again. The optimal parameters for the aluminium SAS-SOL focusing light in air were found to be a duty ratio of 0.22, period of 75 nm, and metal thickness of 180 nm. The electric field intensity at the SOL focal plane is shown in Fig. [7](#page-5-0) for both SOLs, where the solid lines are the results of SAS-SOL and dashed lines are the results without sub-slits (the original design of ref. ³²). The blue lines and red lines are the results when AP and RP input illuminated the lens, respectively. In the case of the oil SOL, the FWHM was 0.23 λ_0 $(0.35 \lambda_{\text{oil}})$ in both cases, the intensity loss after sub-slits was only 0.19%, and the PER is increased from 9.8dB to 23.6dB. In the case of the air SOL, the FWHM of both lenses is 0.32 λ_0 , the intensity loss after sub-slits was 7.2%, and the PER has been increased from 12.1 dB to 105.5 dB. There results show that our SAS approach is robustly applicable to various diferent SOLs.

Discussion

We have demonstrated a new SAS-SOL which generates, with a single optical component, a purely longitudinally-polarized subwavelength hotspot. Annular subwavelength slits are manufactured in the openings of conventional SOL structure, which selectively transmit RP light. Tis RP light is converted to LP by the focusing action of the SOL. Subwavelength slits were optimized using EMT theory, and numerical calculations were performed to characterize the SAS-SOL. 21.8dB of mode purity has been calculated at the SR focusing spot with only 0.342 dB degradation of efficiency compared to the SOL without subwavelength rings. We have also shown the robustness of our design to fabrication errors and demonstrated the generality of the idea to other SOLs from the literature. The SAS-SOL simplifies the generation of LP-SR hotspots by substantially reducing alignment complexity and allowing monolithic integrated components. The SAS-SOL will find wide applications in fields where nano-confnement of light is needed: including imaging, data storage and nano-manufacturing with light.

Methods

It is well known that sub-wavelength linear metallic structures transmit electric felds polarized perpendicular to the slit direction but block parallel polarization components³³. It has recently been reported that arrays of annular slits selectively transmit RP light and block AP light, and this has been applied to binary Fresnel zone plates³⁰. The efective refractive index of the metallic slit arrays for radial and azimuthal inputs calculated via EMT shows that metallic annular slit arrays respond as a 'dielectric' to RP and 'metallic' to AP inputs:

$$
n_{\text{eff,RP}} = \frac{1}{\sqrt{\frac{f}{n_1^2} + \frac{1-f}{n_2^2}}}
$$

$$
n_{\text{eff,AP}} = \sqrt{fn_1^2 + (1-f)n_2^2}
$$

where n_{eff} is the effective refractive index for each input component, *f* is the fraction of the dielectric, and n_1 and $n₂$ are the refractive index of the dielectric and metal, respectively. Our recent work also presents the effect of annular nanoslits, which works as a cylindrical symmetric polarizer 24 .

We perform FEM numerical simulations via COMSOL to analyze the characteristics of SOL for RP, AP, and combined input. Note that circular optical waveguides have second order degenerate modes with both RP and AP components²⁶. The SOL used on the simulation is the lens from ref. 12 . Chromium³⁴ has been selected as the metallic material and the lens is covered with immersion oil $(n=1.515)$, in which the focus is formed. The material parameters of aluminium were taken from ref. 35 . The expected SR focal length of the lens is 9.8 μ m.

Received: 10 October 2019; Accepted: 11 December 2019; Published online: 28 January 2020

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Acknowledgements

Tis work was supported by Korean Ministry of Science, ICT (Grant No. 2019R1F1A1063151) and Hongik University new faculty research support fund.

Author contributions

H.K. developed the concept and theory of the SAS-SOL and performed the numerical calculations. E.T.F.R. consulted on the design, verifed the theory and numerical results. Both authors discussed the results and wrote the fnal manuscript together.

Competing interests

The authors declare no competing interests.

Additional information

Correspondence and requests for materials should be addressed to H.K.

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