

Communication Cubic Octa-Carbon: Quantum-Chemical Design of Molecular Structure and Potential Way of Its Synthesis from Cubane

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Abstract: Quantum-chemical calculation of most important parameters of molecular and electronic structures of octa-carbon C₈ having cubic form (bond lengths, bond and torsion angles) using CCSD(T)/QZVP and DFT B3PW91/QZVP methods, has been carried out. NBO analysis data and HOMO/LUMO images for this compound are presented, too. Good agreement was found between the structural data obtained using the above two quantum-chemical methods and, also, with corresponding experimental data. Also, the standard thermodynamic parameters of formation of cubic C₈ considered here, and namely standard enthalpy $\Delta_f H^0$ (298K), entropy S_f⁰(298K) and Gibbs' energy $\Delta_f G^0$ (298K) of formation for this compound were calculated. By using this data, a theoretically possible variant of the synthesis of this compound by dehydrogenation of cubane C₈H₈ is considered, and the thermodynamic characteristics of each of the four stages of this process have been calculated. It is noted that each of the four stages of this process is characterized by a very high (about 500 kJ/mol) enthalpy of activation, as a result of that, for their realization within a sufficiently short time, the use of appropriate catalysts is necessary.

Keywords: octa-carbon; cubane; CCSD method; DFT method

1. Introduction

Carbon, alone, among all chemical elements is known to be the only one whose atoms' number of valence orbitals, number of valence electrons and maximum possible coordination numbers of each coincide with each other. Due to this unique circumstance, it can form long homochain structures containing many hundreds and thousands of atoms. For this element, in addition to the allotropic modifications well and long known to all science—graphite and diamond—a very significant number of other varieties are known, such as carbyne, glassy carbon, various shapes of nanotubes, nanofibers, astralenes, numerous fullerenes (containing, in a molecule, between 60 and several hundred carbon atoms) and amorphous carbon [1-10]. At the beginning of the twenty-first century another unique modification of this chemical element was obtained-graphene, the structure of which can be considered as one plane of layered graphite, separated from its bulk crystal [1,11–17]. All these modifications of carbon contain a very significant (at least several dozen) number of atoms in their structural units; nevertheless, according to the data given in [1], there is quite a lot of information in the literature on allotropic modifications of carbon containing a small (less than 10) number of atoms. One of the most interesting modifications of this type is octa-carbon C_8 , for the molecular structure of which the cubic form seems to be the most probable. This substance can serve as a very useful precursor for the organic synthesis of a number of cubane derivatives, for example, polycyclic framework compounds containing articulated cubane fragments; seems to be very promising for use in a number of branches of technology, in particular, as "building blocks" for new nanodevices,



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Copyright: © 2021 by the authors. Licensee MDPI, Basel, Switzerland. This article is an open access article distributed under the terms and conditions of the Creative Commons Attribution (CC BY) license (https:// creativecommons.org/licenses/by/ 4.0/). which, in turn, can be implemented to create digital memory systems; the possibility of using it in the creation of catalysts for various physicochemical processes is not excluded. The synthesis of such a compound, however, has not yet been experimentally carried out; though there are many works devoted to the theoretical calculation of its molecular and/or electronic structure, carried out mainly using DFT, HF, or even semiempirical methods (see, in particular, [18–32]). In this regard, the purpose of this work is to perform a quantum-chemical calculation of the molecular structure of this compound by a more rigorous ab initio quantum-chemical method, namely CCSD (T)/QZVP, as well as to theoretically consider the possibility of its synthesis based on a chemical compound that also has cubic structure, namely, cubane C_8H_8 .

2. Calculation Method

The quantum-chemical calculation of molecular structures of octa-carbon molecule having C_8 composition was carried out using the CCSD(T)/QZVP method, combining the common QZVP extended quadruple zeta split-valence basis set [33,34] and the coupled cluster method, using both single and double substitutions, including triple excitation non-iterative CCSD(T) [35–38]. The given method is one of the most accurate and reliable quantum-chemical methods for calculating the molecular structures of various chemical compounds (in particular, *p*-elements) and considers electron correlation very well. Along with this, for comparison, we also calculated the parameters of the molecular structure of C_8 using the much less time-consuming DFT method, namely DFT B3PW91/QZVP level, which, combined with QZVP and B3PW91 functionality [39,40] and according to data in [41], has minimal values of so-called "normal error" in comparison with other variants of the DFT method. Calculations were performed with the Gaussian09 program package [42]. To visualize the results of our calculations, we used the ChemCraft software, Version 1.8.

The initial structures of the C_8 molecules for carrying out quantum-chemical calculations are shown in Scheme 1:



Scheme 1. Potential molecular structures of octa-carbon: C_8 (**A**) and C_8 (**B**)—cubes, C_8 (**C**)—square antiprism, C_8 (**D**)—octagon, C_8 (**E**) and C_8 (**F**)—a combination of three rectangles with four common vertices.

The choice of these six structures was determined by the next two factors: firstly, of the valence possibilities of the carbon atom (which can bind with one, two, three, or four neighboring atoms by means of three chemical bonds, according to the exchange mechanism of chemical bond formation); secondly, by these structures' having the greatest typicality as compared with other structures of eight atoms. That is why, in particular, the hexagonal bipyramid, the dodecahedron and plane bicyclic structure containing articulated six-numbered and four-numbered rings, were not included in the number of

initial structures because, here, as well as in other permissible eight-atomic structures, each carbon atom's being bound to neighboring carbon atoms by exactly four chemical bonds is impossible to achieve. The correspondence of the found stationary points to energy minima was proved, in all cases, by calculating the second derivatives of the energies with respect to atoms' coordinates; all equilibrium structures corresponding to the minima on the potential energy surfaces have only positive frequencies.

Calculations of the structural parameters of the intermediates and transition states of the theoretically possible reaction for the production of C_8 , and namely, the reaction of the stepwise dehydrogenation of cubane C_8H_8 , were carried out using the B3PW91/QZVP method, since the use of the coupled-cluster method, CCSD(T)/QZVP, to solve this problem would require very large time and energy costs, far beyond our technical capabilities. In all cases, frequencies of normal vibrations were calculated; in the case of transient states, the first frequency was imaginary and corresponded to the motion of the atoms involved in the reaction. To confirm the correspondence of the found transition states to the studied reaction from each transition state, a descent towards the reagents and reaction products was carried out (IRC procedure in Gaussian09). Of note is that, at the second stage of the dehydrogenation process (i.e., when the second hydrogen molecule is split off), the reaction could already only proceed at those carbon atoms that are chemically bonded to those in C_8H_6 molecules deprived of hydrogen atoms. The transition state of the dehydrogenation reaction, in the formation of which hydrogen molecules would be split off from those carbon atoms that were not linked by the above-mentioned chemical bonds, was not found during the calculations.

The values of the standard thermodynamic characteristics of the carbon-containing compounds under study were calculated using the G4 method described, in detail, in [43]. All quantum-chemical calculations were carried out in the Joint Supercomputer Center of the Russian Academy of Sciences-Branch of Federal Scientific Center "Scientific Research Institute for System Analysis of the RAS" (http://www.jscc.ru, accessed on 28 October 2021).

3. Results and Discussion

According to the results of our calculations, the most stable of these six structures of octa-atomic carbon molecule mentioned above, is C_8 (A), in the form of the cube. The image of the molecular structure of this compound calculated by CCSD(T)/QZVP method is shown in Figure 1.



Figure 1. Molecular structure of theoretically possible polymorphic modification of elemental carbon C_8 according to data of quantum-chemical calculation with using CCSD(T)/QZVP method.

The geometric parameters of this molecular structure calculated with the given methods (bond lengths, bond angles and some torsion angles) are presented in Table 1. As can be seen from these data, quantitatively, the values of similar parameters are very close to each other (the difference between these two structures' bond lengths between their carbon atoms is no more than 2 pm, and, between their bond and torsion (dihedral) angles, no more than 0.4°). However, there is a very clear qualitative difference between the CCSD(T)/QZVP and DFT B3PW91/QZVP structures: in the former, the bond lengths and angles between carbon atoms are generally not the same (although some of them coincide), whereas, in the latter, they are the same (Table 1). The reasons for this qualitative difference between the results of calculations by the CCSD(T)/QZVP and DFT B3PW91/QZVP methods are most likely associated with the Jahn–Teller effect, and namely, the instability of a highly symmetric structure containing degenerate states of electrons to deformations that lower its symmetry. The point symmetry group D_{4h} was obtained during the calculation by the DFT B3PW91/QZVP method; in the course of the calculations using the CCSD(T)/QZVP method we obtained the point symmetry group C_1 , i.e., a lack of symmetry. Note, in this connection, that within the CCSD(T)/QZVP molecular structure itself the maximum difference between the lengths of carbon–carbon bonds is 0.5 pm, between the bond angles is 0.7°, and between torsion angles is 0.4°; compared with the values of these parameters themselves, these differences look very insignificant.

Table 1. Geometric parameters of the molecular structure of C_8 molecule calculated by the CCSD(T)/QZVP and DFT B3PW91/QZVP calculation methods.

Parameter	Calculated by		Parameter	Calculated by			
	QZVP	B3PW91/ QZVP		QZVP	B3PW91/ QZVP		
Carbon–Carbon Bond Lengths, pm							
(C1C4)	148.3	146.7	(C7C5)	148.0	146.7		
(C4C8)	148.0	146.7	(C5C2)	148.6	146.7		
(C8C6)	148.2	146.7	(C1C2)	148.3	146.7		
(C6C1)	148.1	146.7	(C3C4)	148.3	146.7		
(C2C3)	148.3	146.7	(C5C6)	148.5	146.7		
(C3C7)	148.5	146.7	(C7C8)	148.5	146.7		
Bond Angles, <i>deg</i>							
(C1C4C8)	90.4	90.0	(C5C6C1)	90.4	90.0		
(C4C8C6)	89.6	90.0	(C6C1C2)	89.8	90.0		
(C8C6C1)	90.3	90.0	(C6C5C7)	89.9	90.0		
(C6C1C4)	89.7	90.0	(C5C7C8)	90.2	90.0		
(C2C5C7)	89.9	90.0	(C7C8C6)	89.8	90.0		
(C5C7C3)	90.3	90.0	(C8C6C5)	90.1	90.0		
(C1C2C3)	90.2	90.0	(C7C8C4)	89.8	90.0		
(C2C3C4)	89.8	90.0	(C8C4C3)	90.4	90.0		
(C3C4C1)	90.2	90.0	(C4C3C7)	89.7	90.0		
(C6C1C4)	89.7	90.0	(C3C7C8)	90.1	90.0		
(C1C2C5)	90.3	90.0	(C7C8C4)	89.8	90.0		
(C2C5C6)	89.9	90.0	(C8C4C3)	90.4	90.0		
Selected Torsion (Dihedral) Angles, deg							
(C1C4C8C6)	-0.2	0.0	(C1C2C7C8)	0.0	0.0		
(C1C4C3C2)	0.4	0.0	(C4C6C5C3)	0.2	0.0		
(C1C2C5C6)	0.0	0.0	(C1C2C3C7)	-90.1	-90.0		
(C2C3C7C5)	-0.2	0.0	(C2C5C6C8)	90.3	90.0		
(C5C6C8C7)	-0.4	0.0	(C5C6C8C4)	-90.2	-90.0		
(C3C4C8C7)	0.2	0.0	(C7C8C4C1)	-90.0	-90.0		

The images of the highest occupied (HOMO) and lowest vacant (LUMO) molecular orbitals obtained using the above quantum chemical methods are presented in Figure 2. As can be seen therein, the forms of the given MOs obtained by these different methods are very similar to each other, wherein, however, the energies of these MOs are very different from each other. Most likely this difference is associated with a well-known feature of the DFT methods, and namely—due to some approximations that simplify the calculation of the electron correlation—the underestimation, in particular, of the difference in the



HOMO-LUMO energies. That is why the data of the coupled-cluster method (CCSD), in the given case, should be considered much more reliable.

Figure 2. The images of the highest occupied (HOMO) and lowest vacant (LUMO) molecular orbitals obtained by CCSD(T)/QZVP (**left**) and DFT B3PW91/QZVP (**right**).

NBO analysis data of the C₈ structures within each of these methods are presented in Table 2. As follows from these data, in the case of using the CCSD(T)/QZVP method, a weakly pronounced polarization of carbon atoms occurs, some of which carry an insignificant (about 0.01 electron charge unit (\bar{e})) positive charge, and some of which carry the same slight negative charge. This feature, as was noted above, is also most likely a result of the Jahn–Teller effect. In the DFT B3PW91/QZVP calculations, the charges on each of the eight carbon atoms, with an accuracy of four significant digits after the decimal, are zero (Table 2).

Table 2. NBO analysis data for the cubic octa-carbon C_8 calculated by the CCSD(T)/QZVP and DFT B3PW91/QZVP methods.

Calculation	Effective Charge on Carbon Atoms, in Units of Electron Charge (ē)							
Method	C1	C2	C3	C4	C5	C6	C7	C8
CCSD(T)/ QZVP	-0.0104	+0.0099	-0.0098	+0.0102	-0.0097	+0.0102	+0.0099	-0.0103
B3PW91/ QZVP	0.0000	0.0000	0.0000	0.0000	0.0000	0.0000	0.0000	0.0000

According to our calculations of the standard thermodynamic parameters of the isobaric process (the standard enthalpy of formation $\Delta_f H^0(298K)$), the standard entropy of formation S_f^0 (298K), and the standard Gibbs energy of formation $\Delta_f G^0(298K)$) by the G4 method for the C₈ molecule, their values are 1871.6 kJ/mol, 348.7 J/mol·K and 1767.6 kJ/mol, respectively. As it can be seen from these data, $\Delta_f H^0(298K)$ and $\Delta_f G^0(298K)$ values are positive (and very significant in modulus), and cannot be obtained for the most stable modification of elemental carbon, graphite, according to the classical canons of thermodynamics. In this connection, it seems advisable to consider the possibility of obtaining cubic octa-carbon in some other way, and one of the most promising methods is the stepwise dehydrogenation of the saturated polycyclic hydrocarbon, cubane C₈H₈, which was first obtained more than 50 years ago [44,45] and, by its own the spatial structure, is the compound closest to octa-carbon, according to the general scheme shown in Figure 3.



Figure 3. Scheme of the probable dehydrogenation reaction of cubane C_8H_8 with the formation of cubic octa-carbon C_8 (a) and the energetic profile of this reaction (b) (TS1, TS2, TS3, TS4 are various transient states).

In accordance with calculation by the DFT B3PW91/QZVP method, the carboncarbon bond lengths in the cubane molecule are 156.1 pm, the carbon-hydrogen bonds are 108.7 pm, the bond angles are 90.0° and 125.2°, for CCC and CCH, respectively. These values are in very good agreement with the experimental values of these parameters found in [46,47] (157.1 pm, 108.2 pm, 90.0° and 125.0° , respectively). The noted good agreement allows us to assert that, using this method, it is possible to adequately describe the specificity of the dehydrogenation reaction of C_8H_8 to C_8 , including the molecular structures of intermediates and transient states TSn (so-called "activated complexes"). The indicated molecular structures are shown in Figure 4, some of their geometric parameters and negative frequency characteristic of the transient states TSn are presented in Table 3 and in Supplementary Materials. As can be seen, the formation of any of the four TSn transient states is accompanied by a rather pronounced deformation of the cubic structure of the initial C_8H_8 ; at the same time, interestingly, in the series TS1–TS2–TS3–TS4, the carbon-carbon bond lengths, as compared to those in cubane, first decrease, then increase, then decrease again and increase again; a similar situation takes place for the carbonhydrogen bond lengths. The interatomic distances (H1H2), on the contrary, in the same row decrease monotonically (Table 3). In connection with this deformation, the change in

the bond angles formed by carbon atoms located in the adjacent vertices of the hexahedron (distorted cube) also looks quite natural, one part of which becomes greater than 90° , while the other part is less than 90° , although the deviation in the values of both these and of other angles from 90° is, as a rule, not more than 5° .



Figure 4. The images of molecular structures of cubane C_8H_8 (**a**), intermediates C_8H_6 (**c**), C_8H_4 (**e**), C_8H_2 (**g**) and transient states TS1 (**b**), TS2 (**d**), TS3 (**f**), TS4 (**h**) of reactions of its dehydrogenation.

Table 3. Enthalpy of activation ($\Delta H^{\#}$, kJ/mol), Gibbs's energy of activation ($\Delta G^{\#}$, kJ/mol), entropy of activation ($\Delta S^{\#}$, J/mol·K) under standard conditions, standard enthalpy of reaction (ΔH_{r} , kJ), the standard Gibbs's energy of the reaction (ΔG_{r} , kJ), the standard entropy of the reaction (ΔS_{r} , J/K), some geometric parameters and negative frequency characteristic of the transient states TSn (n = 1–4, see Figures 3 and 4) of the dehydrogenation process cubane calculated by the DFT B3PW91/QZVP method.

Transition Stage (TSn)	TS1	TS2	TS3	TS4
$\Delta H^{\#}$	534.4	506.9	478.2	448.2
$\Delta G^{\#}$	527.5	504.5	476.3	446.5
$\Delta S^{\#}$	23.0	8.0	6.5	5.9
$\Delta H_{ m r}$	314.8	337.3	326.2	347.3
$\Delta G_{\mathbf{r}}$	271.4	298.6	287.8	314.5
ΔS_{r}	145.6	129.6	128.8	110.1
r(H1H2), pm	90.9	90.4	85.2	84.3
r(C1H1), pm	140.2	134.3	144.4	137.6
r(C1H2), pm	125.5	124.4	132.8	134.5
r(C2H2), pm	197.2	209.4	218.9	219.2
r(C1C2), pm	155.0	160.7	157.7	154.4
∠H1C1H2, deg	39.6	40.7	35.5	36.1
\angle H2C1C2, deg	88.7	93.7	97.4	98.5
v_1 , cm ⁻¹	-1569	-1258	-1144	-1022

The decomposition reaction of cubane, according to the $C_8H_8 \rightarrow C_8 + 4H_2$ general scheme in both the solid and the gas phase, proceeds with an increase in the total volume of the reaction system (due to the formation of gaseous hydrogen), and therefore, according to the classical canons of thermodynamics, should be accompanied by an increase in the entropy of the reaction system. On the other hand, this reaction is endothermic (according to our calculation, its standard enthalpy is 1325.6 kJ, its standard entropy is 514.1 J/K, and its standard Gibbs's energy is 1172.4 kJ), so its implementation is provided by the entropy factor. Using the classical Gibbs—Helmholtz equation for the isobaric process $\Delta_r G^0(T) = \Delta_r H^0(298 \text{ K}) - T\Delta_r S^0(298 \text{ K})$ (where $\Delta_r H^0(298 \text{ K})$ and $\Delta_r S^0(298 \text{ K})$ are the changes in enthalpy and entropy as a result of a chemical process referred to standard conditions, *T* is the process temperature in K, $\Delta_r G^0(T)$ is the dependence of the Gibbs's free energy on the temperature *T*), it is easy to find that this reaction can proceed at a temperature $T \ge 2578.5 \text{ K}$. A similar situation is observed for individual stages of this reaction with the sequential formation of compounds C_8H_6 , C_8H_4 , C_8H_2 and C_8 (see Figure 3).

As can be seen from the data presented in Figure 3b and Table 3, each of the four successive stages of the cubane dehydrogenation reaction is characterized by high values of activation enthalpies and, at the same time, rather low values of activation entropies, as a result of which the energy barriers for the formation of transient states are very significant, wherein the realization of each of these stages is due to the entropy factor, so that all of them can be realized only at sufficiently high temperatures (more than 2000 K). However, even at such high temperatures, the rates of these reactions are likely to be insufficient for their practical implementation within a sufficiently short time, and if so, then in order to increase them, it will be necessary to search for appropriate catalysts for these very reactions.

4. Conclusions

As it can be seen from the above, both the used independent quantum-chemical calculation methods—CCSD(T)/QZVP and DFT B3PW91/QZVP—unequivocally indicate the existence of cubic octa-carbon as the most stable of all possible carbon modifications having a C₈ composition, wherein the quantitative parameters of the molecular structure (bond lengths, bond and torsion (dihedral) angles) of this carbon modification, calculated using these methods, turn out to be very close to each other, though, qualitatively, they

are different; according to the data of the first of these methods, as similar parameters are different (though insignificantly), but, according to the second, they are the same (Table 1). Taking into account the fact that, in reality, all carbon atoms in the cubic structure of C_8 should most likely be equivalent to each other, we can expect that the real structure of cubic octa-carbon C_8 should be some kind of intermediate variant between the structures obtained as a result of our quantum-chemical calculations using the above independent methods. The assessment of the thermodynamic characteristics of the reaction carried out in this article (from the use of which, in principle, cubic octa-carbon can be obtained, namely, the dehydrogenation of cubane C_8H_8) indicates the reality of such a reaction, albeit under rather harsh conditions (i.e., at a high temperature) and with the obligatory use of a catalyst to ensure its flow at a sufficiently high rate. The goal, now, is to confirm all this experimentally.

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References

- 1. Kharisov, B.I.; Kharissova, O.V. Carbon Allotropes: Metal-Complex Chemistry, Properties and Applications; Springer Nature AG: Cham, Switzerland, 2019; ISBN 978-3-030-03504-4. [CrossRef]
- 2. Belenkov, E.A.; Mavrinsky, V.V. Crystal structure of a perfect carbyne. Crystallogr. Rep. 2008, 53, 83–87. [CrossRef]
- 3. Pan, B.; Xiao, J.; Li, J.; Liu, P.; Wang, C.; Yang, G. Carbyne with finite length: The one-dimensional sp carbon. *Sci. Adv.* 2015, *1*, e1500857. [CrossRef]
- 4. Shi, L.; Rohringer, P.; Suenaga, K.; Niimi, K.S.Y.; Kotakoski, J.; Meyer, J.; Peterlik, H.; Wanko, M.; Jahangirov, S.; Rubio, A.; et al. Confined linear carbon chains as a route to bulk carbyne. *Nat. Mater.* **2016**, *15*, 634–639. [CrossRef]
- Schueller, O.J.A.; Brittain, S.T.; Whitesides, G.M. Fabrication of glassy carbon microstructures by pyrolysis of microfabricated polymeric precursors. *Adv. Mater.* 1997, 9, 477–480. [CrossRef]
- 6. Jorio, A.; Dresselhaus, M.S.; Dresselhaus, G.; Gogotsi, Y. Carbon Nanotubes: Advanced Topics in the Synthesis, Structure, Properties and Applications, 1st ed; Springer: Berlin, Germany, 2008; ISBN 978-3-540-72864-1. [CrossRef]
- Tibbetts, G.; Lake, M.; Strong, K.; Rice, B. A review of the fabrication and properties of vapor-grown carbon nanofiber/polymer composites. *Compos. Sci. Technol.* 2007, 67, 1709–1718. [CrossRef]
- Khamatgalimov, A.; Kovalenko, V. Substructural Approach for Assessing the Stability of Higher Fullerenes. *Int. J. Mol. Sci.* 2021, 22, 3760. [CrossRef]
- 9. McCulloch, D.G.; McKenzie, D.R.; Goringe, C.M. Ab initio simulations of the structure of amorphous carbon. *Phys. Rev.* 2000, *B61*, 2349. [CrossRef]
- 10. Robertson, J. Diamond-like amorphous carbon. Mater. Sci. Eng. R Rep. 2002, 37, 129–281. [CrossRef]
- 11. Katsnelson, M.; Novoselov, K. Graphene: New bridge between condensed matter physics and quantum electrodynamics. *Solid State Commun.* **2007**, *143*, 3–13. [CrossRef]
- 12. Geim, A.K.; Novoselov, K. The rise of graphene. Nat. Mater. 2007, 6, 183–191. [CrossRef] [PubMed]
- 13. Ghuge, A.D.; Shirode, A.R.; Kadam, V.J. Graphene: A comprehensive review. Curr. Drug Targets 2017, 18, 724–733. [CrossRef]

- 14. Wu, J.; Pisula, W.; Mullen, K. Graphenes as potential material for electronics. Chem. Rev. 2007, 107, 718–747. [CrossRef]
- 15. Yu, X.; Cheng, H.; Zhang, M.; Zhao, Y.; Qu, L.; Shi, G. Graphene-based smart materials. *Nature Rev. Mater.* 2017, 2, 17046. [CrossRef]
- 16. Novoselov, K.S. Technology: Rapid progress in producing graphene. Nature 2014, 505, 291. [CrossRef]
- 17. Van den Brink, J. Graphene: From strength to strength. Nat. Nanotechnol. 2007, 2, 199–201. [CrossRef] [PubMed]
- 18. Krishnan, R.; Binkley, J.S. Structure, stability, and fragmentation of small carbon clusters. J. Chem. Phys. 1987, 87, 2191–2197.
- 19. Martin, J.M.L.; Francois, J.P.; Gijbels, R. Ab initio study of the infrared spectra of linear C_n clusters (n = 6–9). *J. Chem. Phys.* **1990**, 93, 8850–8861. [CrossRef]
- Martin, J.M.L.; Francois, J.P.; Gijbels, R. A critical comparison of MINDO/3, MNDO, AM1, and PM3 for a model problem: Carbon clusters C₂-C₁₀. An ad hoc reparametrization of MNDO well suited for the accurate prediction of their spectroscopic constants. *J. Comput. Chem.* **1991**, *12*, 52–70. [CrossRef]
- 21. Parasuk, V.; Almlöf, J. The electronic and molecular structure of carbon clusters: C₈ and C₁₀. *Theor. Chim. Acta* **1992**, *83*, 227–237. [CrossRef]
- Hutter, J.; Luethi, H.P.; Diederich, F. Structures and vibrational frequencies of the carbon molecules C₂-C₁₈ calculated by density functional theory. J. Am. Chem. Soc. 1994, 116, 750–756. [CrossRef]
- 23. Tseng, S.; Shen, M.; Yu, C. A MNDO study of carbon clusters with specifically fitted parameters. *Theor. Chim. Acta* 1995, 92, 269–280. [CrossRef]
- 24. Martin, J.M.L.; El-Yazal, J.; Francois, J.-P. Structure and vibrational spectra of carbon clusters Cn (n = 2–10, 12, 14, 16, 18) using density functional theory including exact exchange. *Chem. Phys. Lett.* **1995**, 242, 570–579. [CrossRef]
- 25. Martin, J.M.L.; Taylor, P.R. Structure and Vibrations of Small Carbon Clusters from Coupled-Cluster Calculations. *J. Phys. Chem.* **1996**, *100*, 6047–6056. [CrossRef]
- 26. Wang, S.L.; Rittby, C.M.L.; Graham, W.R.M. Detection of cyclic carbon clusters. II. Isotopic study of the 12(*eu*) mode of cyclic C8 in solid Ar. *J. Chem. Phys.* **1997**, *107*, 7025–7033. [CrossRef]
- 27. Nyrönen, T.H.; Reijo Suontamo, R. An MO study of neutral C high-symmetry clusters. *Chem. Phys. Lett.* **1997**, 280, 227–232. [CrossRef]
- 28. Jones, R.O. Density functional study of carbon clusters C_{2n} ($2 \le n \le 16$). I. Structure and bonding in the neutral clusters. *J. Chem. Phys.* **1999**, *110*, 5189–5200. [CrossRef]
- 29. Sharapa, D.; Hirsch, A.; Meyer, B.; Clark, T. Cubic C8: An Observable Allotrope of Carbon? *ChemPhysChem* 2015, 16, 2165–2171. [CrossRef]
- 30. Varandas, A.J.C. Even numbered carbon clusters: Cost-effective wavefunction-based method for calculation and automated location of most structural isomers. *Eur. Phys. J. D* 2018, 72, 134. [CrossRef]
- 31. Rocha, C.M.R.; Li, J.; Varandas, A.J.C. Difficulties and Virtues in Assessing the Potential Energy Surfaces of Carbon Clusters via DMBE Theory: Stationary Points of C κ (κ = 2–10) at the Focal Point. *J. Phys. Chem. A* **2019**, *123*, 3121–3130. [CrossRef]
- 32. Chaglayan, B.; Huran, A.W.; Amor, N.B.; Brumas, V.; Evangelisti, S.; Leininger, T. Spherical aromaticity and electron delocalization in C₈ and B₄N₄ cubic systems. *Theor. Chem. Acc.* **2019**, *138*, 5. [CrossRef]
- 33. Schaefer, A.; Horn, H.; Ahlrichs, R. Fully optimized contracted Gaussian basis sets for atoms Li to Kr. J. Chem. Phys. 1992, 97, 2571–2577. [CrossRef]
- 34. Weigend, F.; Ahlrichs, R. Balanced basis sets of split valence, triple zeta valence and quadruple zeta valence quality for H to Rn: Design and assessment of accuracy. *Phys. Chem. Chem. Phys.* **2005**, *7*, 3297–3305. [CrossRef] [PubMed]
- 35. Pople, A.; Krishnan, R.; Schlegel, H.B.; Binkley, J.S. Electron Correlation Theories and Their Application to the Study of Simple Reaction Potential Surfaces. *Int. J. Quantum Chem.* **1978**, *14*, 545–560. [CrossRef]
- 36. Bartlett, R.J.; Purvis, G.D., III. Many-body perturbation-theory, coupled-pair many-electron theory, and importance of quadruple excitations for correlation problem. *Int. J. Quantum Chem.* **1978**, *14*, 561–581. [CrossRef]
- Purvis, G.D., III; Bartlett, R.J. A full coupled-cluster singles and doubles model—The inclusion of disconnected triples. J. Chem. Phys. 1982, 76, 1910–1918. [CrossRef]
- Pople, J.A.; Head-Gordon, M.; Krishnan, R. Quadratic configuration interaction—A general technique for determining electron correlation energies. J. Chem. Phys. 1987, 87, 5968–5975. [CrossRef]
- 39. Becke, A.D. Density-functional exchange-energy approximation with correct asymptotic behavior. *Phys. Revs. A* **1988**, *38*, 3098–3100. [CrossRef] [PubMed]
- 40. Perdew, J.P.; Burke, K.; Wang, Y. Generalized gradient approximation for the exchange-correlation hole of a many-electron system. *Phys. Revs. B* **1996**, *54*, 16533–16539. [CrossRef]
- Medvedev, M.G.; Bushmarinov, I.S.; Sun, J.; Perdew, J.P.; Lyssenko, K.A. Density functional theory is straying from the path toward the exact functional. *Science* 2017, 355, 49–52. [CrossRef]
- 42. Frisch, M.J.; Trucks, G.W.; Schlegel, H.B.; Scuseria, G.E.; Robb, M.A.; Cheeseman, J.R.; Scalmani, G.; Barone, V.; Mennucci, B.; Petersson, G.A.; et al. *Gaussian 09, Revision A.01*; Gaussian Inc.: Wallingford, UK, 2009.
- 43. Ochterski, J.W. Thermochemistry in Gaussian; Gaussian Inc.: Wallingford, UK, 2000.
- 44. Eaton, P.E. Cubanes: Starting materials for the chemistry of the 1990s and the new century. *Angew. Chem. Int. Ed.* **1992**, *31*, 1421–1436. [CrossRef]

- 45. Biegasiewicz, K.F.; Griffiths, J.R.; Savage, G.P.; Tsanaktsidis, J.; Priefer, R. Cubane: 50 Years Later. *Chem. Rev.* 2015, 115, 6719–6745. [CrossRef] [PubMed]
- 46. Hedberg, L.; Hedberg, K.; Eaton, P.E.; Nodari, N.; Robiette, A.G. Bond lengths and quadratic force field for cubane. *J. Am. Chem. Soc.* **1991**, *113*, 1514–1517. [CrossRef]
- 47. Schubert, W.; Yoshimine, M.; Pacansky, J. Ab initio self-consistent field calculations on the structure of cubane, cubene, and the cubyl radical. *J. Phys. Chem.* **1981**, *85*, 1340–1342. [CrossRef]