



Exploration of the Structural, Electronic and Tunable Magnetic Properties of Cu₄M (M = Sc-Ni) Clusters

Dong Die ^{1,*}, Ben-Xia Zheng ¹, Xiao-Yu Kuang ^{2,*}, Zheng-Quan Zhao ¹, Jian-Jun Guo ¹ and Quan Du ¹

- ¹ School of Science, Xihua University, Chengdu 610039, China; xhu_zbx@163.com (B.-X.Z.); dd_cpl@163.com (Z.-Q.Z.); jmst_gjj@163.com (J.-J.G.); duquanlm@163.com (Q.D.)
- ² Institute of Atomic and Molecular Physics, Sichuan University, Chengdu 610065, China
- Correspondence: science_dd@163.com (D.D.); kuangxiaoyu@scu.edu.cn (X.-Y.K.); Tel.: +86-028-8772-5802 (D.D.)

Received: 23 July 2017; Accepted: 8 August 2017; Published: 15 August 2017

Abstract: The structural, electronic and magnetic properties of Cu₄M (M = Sc-Ni) clusters have been studied by using density functional theory, together with an unbiased CALYPSO structure searching method. Geometry optimizations indicate that M atoms in the ground state Cu₄M clusters favor the most highly coordinated position. The geometry of Cu₄M clusters is similar to that of the Cu₅ cluster. The infrared spectra, Raman spectra and photoelectron spectra are predicted and can be used to identify the ground state in the future. The relative stability and chemical activity are investigated by means of the averaged binding energy, dissociation energy and energy level gap. It is found that the dopant atoms except for Cr and Mn can enhance the stability of the host cluster. The chemical activity of all Cu₄M clusters is lower than that of Cu₅ cluster whose energy level gap is in agreement with available experimental finding. The magnetism calculations show that the total magnetic moment of Cu₄M cluster mainly come from M atom and vary from 1 to 5 μ_B by substituting a Cu atom in Cu₅ cluster with different transition-metal atoms.

Keywords: geometrical structure; electronic property; magnetic moment; Cu₄M (M = Sc-Ni) cluster

1. Introduction

The binary alloy clusters have been investigated widely during the past several decades [1–34]. Experimental and theoretical research has manifested that the introduction of a dopant atom into a small cluster can considerably change the nature of the host cluster. Copper clusters doped with an impurity atom have been actively pursued to tailor the desired structural, electronic, magnetic and optical properties for potential applications in solid state chemistry, materials science, nanotechnology and microelectronics [35–47]. For example, the bimetallic Cu_nPd_m ($m + n \le 6$) clusters are more stable than the monometallic particles with the same size [35]. The presence of Cr dopant obviously enhances the stability of $Cu_n Cr$ (n = 9-16) in comparison to that of pure counterparts [36]. The bond stiffness of the copper cluster are decreased after doping with Pd atoms. The most stable Cu₇Sc, $Cu_{15}Sc$ and $Cu_{16}Sc$ clusters could be regarded as a σ -aromatic species, a superatom and the germ of a crystallization process, respectively [37–39]. The Ti- and V-doping dramatically improves the adsorption of copper clusters on NO molecules, but it does not affect the O₂ adsorption probability significantly [40]. The Cu-Fe icosahedral nano-clusters exhibit larger magnetic moments than the Fe thin films and bulk systems [41]. The Cu_n Se clusters are the perfect candidate for renewable energy sources in the photocatalysis field [42]. Recently, the Cu_2 , Cu_6 and Cu_{12} clusters doped with various atoms have received particular interest owing to their unique physical and chemical properties [48-50]. It was shown that, among all Cu_2X (X = Sc-Zn) clusters, the Cu_2Ti is found to have the highest ability of the dissociation absorption of H_2 moleculaes [48]. The Cu₆Co cluster is the best catalyst



for the water–gas–shift reaction (CO + $H_2O\rightarrow C_2O + H_2$, $\Delta H_{25^\circ C} = -41$ kJ/mol) [49]. The doping of single 3*d* transition metal atoms would overcome the problem of stabilization at the noble Cu₁₂ icosahedra [50]. As far as we know, however, there is relatively few systematic work concerning the doped Cu₄ clusters. On the other hand, it is well known that the bimetallic clusters often have intriguing properties, which should be very different from those of the bulk materials or atoms, in virtue of the so-called surface and size effects. Therefore, in this paper, the structural, electronic, and magnetic properties of small Cu₄M (M = Sc-Ni) clusters are studied systematically by means of density functional theory (DFT). It is hoped that this work could provide valuable information to realize the influence of dopant atom and would be of help to chemists, especially those designing new nanomaterials.

2. Computational Methods

Geometry optimizations and vibrational frequency computations were performed by using B3LYP, (Becke A. D., Kingston, ON, Canada) hybrid exchange–correlation functional in conjunction with an effective core potential LanL2DZ basis sets, as implemented in the GAUSSIAN09 program package (Frisch, M. J. et al., Wallingford, KY, USA) [51–55]. The default convergence thresholds are used in all computations. One hundred and twenty initial configurations of each Cu₄M cluster were generated by the CALYPSO soft (Ma Y.M., Changchun, Jilin, China) [56]. A local version of particle swarm optimization algorithm is employed to utilize a fine exploration of potential energy surface. Similar structures can be distinguished by the bond characterization matrix. Due to the spin polarization, every initial configuration was optimized at various possible spin states. All low-energy isomers obtained at B3LYP/LanL2DZ level were also calculated at the BLYP/6-311+G(d) level. The accuracy of the computational method has been checked by calculations on Cu₂, Ti₂, V₂, Cr₂, Fe₂ and Ni₂ dimers. The calculated results summarized in Table 1 are in good agreement with available experimental findings.

Dimer Functional/Basis Set		R (Å) D_e (eV)		$f(cm^{-1})$		VIP (eV)		EA (eV)		
		Calc. Expt.	Calc.	Expt.	Calc	. Expt.	Calc.	Expt.	Calc.	Expt.
Cu ₂	B3LYP/LanL2DZ	2.26 2.22 ^a	2.02	2.01 ^a	256	264 ^a	7.99	7.90 ^a	0.63	0.83 ^a
	Blyp/6-311+G(d)	2.27	2.01		244		8.20		0.83	
Ti ₂	B3LYP/LanL2DZ	1.91 1.94 ^b	1.42	1.54 ± 0.19 ^b						
V_2	B3LYP/LanL2DZ	1.75 1.77 ^c	1.94	$2.47\pm0.22^{\text{ c}}$			6.39	6.35 ^c		
Cr ₂	B3LYP/LanL2DZ						6.22	6.4 ± 0.2 ^d		
Fe ₂	B3LYP/LanL2DZ	2.15 2.02 ^e	1.28	1.30 ^e			6.24	6.30 ^e		
Ni ₂	B3LYP/LanL2DZ	2.38 2.20 ^f	1.59	2.06 ^f						

Table 1. The geometries and electronic properties of Cu₂, Ti₂, V₂, Cr₂ and Fe₂ dimers.

^a Ref. [57], ^b Ref. [58], ^c Ref. [59], ^d Ref. [60], ^e Ref. [61], ^f Ref. [62].

3. Results and Discussion

3.1. Geometrical Structures and Vibrational Spectra

In order to examine the effects of M (M = Sc-Ni) atoms on copper clusters, structural searches of the Cu₅ cluster were carried out firstly using the abovementioned functional and basis sets. The ground state and low-lying structures of Cu₅ and Cu₄M clusters are plotted in Figure 1. These structures are denoted by IA, IB, IC, etc. Their energy difference (ΔE) compared to each of the ground state and spin multiplicity (SM) are listed in Table 2. Some physical parameters of the lowest energy Cu₅ and Cu₄M clusters are collected in Table 3.



Figure 1. The ground state and low-lying isomers of Cu_4M (M = Sc-Cu) clusters.

Table 2. The l	lower energy i	isomer (LI), ΔE aı	nd spin multiplicity	y (SM) of Cu ₅ a	and Cu ₄ M (M	= Sc-Ni)
clusters at the	e B3LYP/LanL	2DZ and Blyp/6-	311+G(d) levels.			

Clusters		B3LYP/LanL2DZ			Blyp/6-311+G(d)			
Clusters =	LI	ΔE (eV)	SM	LI	ΔE (eV)	SM		
	IA	0	2	IA	0	2		
Cu ₅	IB	0.54	2	IB	0.44	2		
	IC	0.88	2	IC	0.91	2		
	ID	0	2	IE	0	2		
Cu ₄ Sc	IE	0.07	2	IF	0.07	2		
	IF	0.21	2	IJ	Blyp/6-311+G(d) ΔE (eV) SM 0 2 0.44 2 0.91 2 0 2 0.07 2 0.09 2 0 3 0.15 3 0.28 4 0.28 4 0.28 4 0.49 4 0.28 4 0.43 5 0.36 5 0.43 5 0 6 0.23 6 0.26 6 0 5 0.18 5 0.33 5 0 4 0.16 4 0.31 4 0 3 0.10 3 0.112 3	2		
	IE	0	3	IE	0	3		
Cu ₄ Ti	ID	0.15	3	ID	0.15	3		
	IH	0.22	3	IL	0.28	3		
	ID	0	4	ID	0	4		
Cu_4V	IG	0.36	4	IE	0.28	4		
	IL	0.36 4 IE 0.43 4 IK 0 5 ID 0.13 7 IC	0.49	4				
	ID	0	5	ID	0	5		
Cu ₄ Cr	IG	0.13	7	IG	0.36	5		
	II	0.24	7	IJ	0.43	5		
	ID	0	6	ID	0	6		
Cu ₄ Mn	IG	0.16	6	IG	0.23	6		
	IH	0.24	6	IH	0.26	6		
	ID	0	5	ID	0	5		
Cu ₄ Fe	IG	0.11	5	IG	0.18	5		
	II	0.25	5	IJ	0.33	5		
	IE	0	4	IE	0	4		
Cu ₄ Co	ID	0.01	4	IG	0.16	4		
	IG	0.18	2	II	0.31	4		
	ID	0	3	ID	0	3		
Cu ₄ Ni	IG	0.09	3	IG	0.10	3		
	II	0.31	3	IL	0.12	3		

Clusters	μ (D)	<i>a_{xx}</i> (a.u.)	<i>a_{yy}</i> (a.u.)	<i>a_{zz}</i> (a.u.)	ā (a.u.)	ZPE (J/mol)	$R_{\overline{V}}$ (Å)
Cu ₅	0.01	282.6	199.3	105.0	195.6	7265.7	
Cu ₄ Sc	2.22	314.1	223.6	182.7	240.1	7020.5	2.72
Cu ₄ Ti	1.54	128.1	206.6	304.1	212.9	7204.7	2.61
Cu_4V	1.07	299.2	200.6	118.6	206.1	7383.0	2.58
Cu ₄ Cr	0.83	299.3	196.2	115.6	203.7	7077.0	2.60
Cu ₄ Mn	0.56	116.0	286.7	217.2	206.6	7148.5	2.55
Cu ₄ Fe	0.37	110.7	283.8	206.7	200.4	7319.2	2.51
Cu ₄ Co	0.27	108.1	202.5	283.1	197.9	7315.1	2.48
Cu ₄ Ni	0.08	283.2	201.9	106.4	197.2	7532.0	2.44

Table 3. The dipole moment (μ), polarizability (a_{xx} , a_{yy} , a_{zz} , \overline{a}) and zero-point energy (ZPE) of the most stable Cu₂ and Cu_nM (M = Sc-Ni) clusters and average coordination bond length ($R_{\overline{V}}$) for M atoms.

The results of two theoretical levels show that the ground state structure of Cu₅ clusters is an isosceles trapezium. This is consistent with previous reports [57]. The most stable structure of Cu_4Sc cluster is planar ID isomer for B3LYP/LanL2DZ level and three-dimensional (3D) IE isomer for BLYP/6-311+G(d) level. The former at BLYP/6-311+G(d) level is unstable and almost degenerate with the latter, which is very close to the planar configuration. The latter at B3LYP/LanL2DZ level is 0.07 eV higher in energy than the former. The IF isomer of Cu₄Sc cluster is obtained by distorting the geometry starting from C_{2v} to C_s symmetry. The lowest energy structure of Cu_4Ti cluster is 3D IE isomer. The Cu–Ti–Cu bond angle is about 158°. Its triplet spin state is lower in energy than other spin state. It is worth mentioning that there is a T_d configuration for Au₄Ti cluster [63], but this configuration for Cu_4Ti cluster turns into an IF isomer. In the case of Cu_4M (M = V-Fe and Ni) clusters, all of the ground state structures exhibit a planar structure similar to the most stable Cu₅ cluster. Other planar and 3D isomers are found as the low-lying isomers. The optimized results for Cu₄Cr cluster reveal that the quintet spin state is more stable than the triplet and septet spin states. In addition, the 3D IE configuration becomes a planar ID structure after geometric optimization and the IF structure does not exist for Cu₄M (M = V-Fe and Ni) clusters. The most stable structure of Cu₄Co cluster resembles the ground state of Cu₄Ti cluster. The Cu–Co–Cu bond angle is 168°. The ID isomer for Cu₄Co cluster is obtained only at the B3LYP/LanL2DZ level. The other 3D isomers of Cu₄Co cluster, such as trigonal bipyramid and tetragonal pyramid, etc., are less stable than the ground state. From the optimized results, it is obvious that the M (M = Sc-Ni) atoms in the lowest energy Cu_4M clusters tend to occupy the most highly coordinated position. This phenomenon is in accordance with the principle of maximum overlap in molecular orbital theory. Next, we will discuss the results based on the B3LYP/LanL2DZ level.

The comparison of calculated spectra and experimental spectra is an effective method to determine the structures of small isolated metal clusters. As a result, the vibrational and Raman spectra of the ground state Cu₅ and Cu₄M (M = Sc-Ni) clusters are computed and displayed in Figure 2. The two types of spectra belong to absorption and scattering spectra, respectively. The fundamental frequencies of the vibrational spectra and Raman spectra for all isomers are in the range of 30–260 and 40–240 cm⁻¹. For the same vibrational frequency, if a weak peak occurs in the vibrational spectrum, then a strong peak will exist in the Raman spectrum. The most intense peak in all vibrational spectra of Cu₄M is related to the Cu-M-Cu antisymmetric stretching vibration. The substitution of Sc, Ti and V atoms for Cu atom has a great influence on the spectra of the host cluster. The vibrational spectra of Cu₄Co and Cu₅ clusters look very similar, whereas the distance between the second peak and the third peak of the latter is 8.4 cm⁻¹ greater than that of the former. These spectra can indeed be used as the fingerprint signals to identify their geometrical structures.



Figure 2. Vibrational (black) and Raman (red) spectra of the ground state Cu₄M (M = Sc-Cu) clusters.

3.2. Electronic Properties

Binding energy is an important parameter to reflect the relative thermal stability of clusters. Some properties of materials can be estimated by using the data of binding energy. The atomic averaged binding energies (E_b) of the Cu₄M and Cu₅ clusters are calculated by the following formula:

$$E_b(Cu_4M) = [4E(Cu) + E(M) - E(Cu_4M)]/5,$$
(1)

$$E_b(Cu_5) = [5E(Cu) - E(Cu_5)]/5,$$
(2)

where $E(Cu_4M)$, E(Cu), E(M) and $E(Cu_5)$ denote the energy of Cu_4M cluster, a Cu atom, a dopant atom and Cu_5 cluster. The calculated E_b for the most stable Cu_4M and Cu_5 clusters is shown in Figure 3a. The E_b of Cu_4M clusters is bigger for M = Sc, Ti, V, Fe, Co and Ni and smaller for M = Crand Mn than that of Cu_5 cluster. That is to say, apart from Cr and Mn atoms, the replacement of a Cu atom by single M (M = Sc, Ti, V, Fe, Co and Ni) atom increases the stability of the host clusters. At the same time, the thermal stability of clusters can also be analyzed by the minimum dissociation energy, which involves the dissociation channels below:

$$Cu_5 \to Cu_m + Cu_{5-m},\tag{3}$$

$$Cu_4M \to Cu_m + Cu_{4-m}M,$$
 (4)

where *m* is less than or equal to 4. The corresponding dissociation energy (DE) is calculated as follows:

$$DE_m(Cu_5) = E(Cu_{5-m}) + E(Cu_m) - E(Cu_5),$$
(5)

$$DE_m(Cu_4M) = E(Cu_{4-m}M) + E(Cu_m) - E(Cu_4M),$$
(6)

where *E* denotes the energy of the corresponding cluster or atom. The DEs of the lowest energy Cu₅ and Cu₄M clusters for the distinct dissociation channels have been given in Table 4. The minimum DEs of Cu₅ and Cu₄M have been shown as a function of dopant atoms in Figure 3b. This is also in line with the above analysis based on averaged binding energy. In order to understand E_b and DE further, the overlap of orbital radius (ΔR) is calculated using the following formula:

$$\Delta R = R_{Cu} + R_M - R_{\overline{V}},\tag{7}$$

where R_{Cu} , R_M and $R_{\overline{V}}$ are the radius of Cu and M atoms and the average coordination bond length of the M atom in the Cu₄M cluster. The calculated ΔR is displayed in Figure 3c. The overlap of the orbital radius of Fe atom and Cu atoms is slightly smaller than the one we expect. Overall, the ΔR , DE and E_b basically maintain a consistent change. This means that the binding energy is closely related to the overlap of the electron cloud.

The energy gap (E_g) between the highest occupied molecular orbital (HOMO) and lowest unoccupied molecular orbital (LUMO) is a fairly important quantity that reflects chemical activity of small clusters. The cluster with a large energy gap usually has high chemical stability. For the ground state Cu_5 and Cu_4M (M = Sc-Ni) clusters, the HOMO-LUMO energy gaps are calculated and shown in Figure 4. The Cu₅ cluster with C_{2v} symmetry has an energy gap of 1.34 eV. The energy gap of neutral Cu_5 cluster can be estimated experimentally by photoelectron spectrum (PES) spectra of the corresponding anionic cluster. The experimental PES spectra of Cu_5^- was reported by Cha et al. [64] and is shown in Figure 5. The energy difference between the first and second peaks in PES spectra of anionic clusters is an approximate measure of the HOMO-LUMO gap of the corresponding neutral clusters. The energy gap of Cu₅ clusters has been measured and is 1.30 eV. The measured value is in agreement with our calculated result. The energy gaps of Cu_4M clusters whose LUMO and HOMO diagram are shown in Figure 6 are bigger than that of Cu_5 clusters. The substitution of Cuatom with M (M = Sc-Ni) atom improves the chemical stability of the host cluster. The Cu_4Ti and Cu₄Mn clusters have a large energy gap relative to the neighbouring clusters. The large energy gaps can be interpreted by an eight electron rule for Cu_4Ti and a half-filled *d* orbital for Cu_4Mn . The two clusters presumably are less reactive and should be useful as a building block for constructing the cluster-assembled materials.

Dissociation Channels		DE (eV)						
	m = 1	m = 2	<i>m</i> = 3	m = 4				
$Cu_5 = Cu_m + Cu_{5-m}$	1.84	2.03						
$Cu_4Sc = Cu_m + Cu_{4-m}Sc$	2.23	2.20	3.10	2.36				
$Cu_4Ti = Cu_m + Cu_{4-m}Ti$	2.20	2.09	2.92	2.41				
$Cu_4V = Cu_m + Cu_{4-m}V$	2.12	2.10	2.81	2.07				
$Cu_4Cr = Cu_m + Cu_{4-m}Cr$	1.86	2.03	2.17	1.45				
$Cu_4Mn = Cu_m + Cu_{4-m}Mn$	2.18	1.73	2.78	1.55				
$Cu_4Fe = Cu_m + Cu_{4-m}Fe$	2.02	2.11	2.47	2.32				
$Cu_4Co = Cu_m + Cu_{4-m}Co$	1.89	2.08	2.28	1.93				
$Cu_4Ni = Cu_m + Cu_{4-m}Ni$	1.94	2.11	2.34	2.00				

Table 4. The dissociation energy (DE) of Cu_5 and Cu_4M (M = Sc-Ni) clusters for the distinct dissociation channels.



Figure 3. The atomic averaged binding energy (**a**), the minimum DE (**b**) and the overlap of orbital radius for the ground-state Cu_4M (M = Sc-Cu) clusters (**c**).



Figure 4. The HOMO-LUMO energy gaps of the ground state Cu_4M (M = Sc-Cu) clusters.



Figure 5. The experimental PES spectrum of Cu₅⁻ cluster, which is cited from Ref. [64].



Figure 6. The LUMO (**first row**) and HOMO (**second row**) molecular orbitals of the ground state Cu₄M (M = Sc-Ni) clusters.

The vertical ionization potential (VIP) and electron affinity (EA) can reflect the ability of the cluster to lose electrons and capture electrons and are defined as follows:

$$VIP = E(\text{cluster}^+) - E(\text{cluster})$$

$$EA = E(\text{cluster}) - E(\text{cluster}^-)$$
(8)

where $E(\text{cluster}^+)$ and $E(\text{cluster}^-)$ are the single point energies of the cationic and anionic clusters in the corresponding neutral geometry. For the most stable Cu₅ and Cu₄M clusters, the calculated first VIP, EA and the available experimental data are given in Table 5. The calculated VIP and EA of Cu₅ are in agreement with the experimental findings [65,66]. Thereby, the reliability of the current calculation method is again demonstrated. In all clusters, the VIP of Cu₄Ti is the largest and the EA of Cu₄Mn is the smallest. This may be attributed to the fact that the Cu₄Ti with eight valence electrons is not easy to lose electrons and the half-filled 3*d* orbitals of Mn atoms in Cu₄Mn are not readily accessible to electrons. The photoelectron spectroscopy (PES) of clusters can be obtained by VIP and HOMO. The simulated PES of the lowest energy Cu₅ and Cu₄M clusters are obtained by adding the occupied orbital energy relative to the HOMO to the VIP and fitting them with a broadening factor of 0.1 eV, as plotted in Figure 7. An intense band at 5.5–12 eV are apparent in the PES of all clusters. The doping atoms significantly change the PES of the host cluster, especially in the range of 6–8 eV. It should be pointed out that the Cu₄Co and Cu₅ clusters have similar vibrational spectra but different PES, which can be employed to identify their geometrical structures.

Table 5. VIP and EA of the ground state Cu_4M (M = Sc-Ni) and Cu_5 clusters, and the charge (Q) and local magnetic moment (M) of 3*d*, 4*s*, 4*p*, and 5*p* states for the M atom in the ground state Cu_4M clusters.

Clusters	VIP (eV)	EA (eV)	M-3 <i>d</i>		M-4 <i>s</i>		M-4 <i>p</i>		M-5 <i>p</i>	
ciusteis			Q (e)	$\mathbf{M}\left(\mu _{B}\right)$						
Cu ₅	6.24 (6.30)	1.70 (1.82)								
Cu ₄ Sc	5.89	1.08	1.65	0.96	0.63	0.09	0.04	0	0.21	0.02
Cu ₄ Ti	6.55	1.23	2.70	2.08	0.60	0.04	0.56	0.02	0.30	0
Cu_4V	6.20	1.41	3.73	3.27	0.59	0.01	0.55	0.01	0	0
Cu ₄ Cr	6.17	1.61	4.92	4.66	0.55	0.03	0.43	0	0	0
Cu_4Mn	6.29	0.95	5.35	4.61	0.89	0.21	0.77	0.11	0	0
Cu ₄ Fe	6.28	1.10	6.66	3.30	0.86	0.20	0.64	0.12	0	0
Cu ₄ Co	6.45	1.63	7.8	2.13	0.81	0.17	0.57	0.11	0	0
Cu ₄ Ni	6.52	1.57	8.95	0.99	0.78	0.14	0.22	0.08	0.31	0.03



Figure 7. Simulated PES of the ground state Cu₄M (M = Sc-Cu) clusters.

3.3. Magnetic Properties

The DFT provides a powerful tool for the study of the magnetic properties of metal clusters. The total magnetic moment of cluster chiefly comprises the orbital and spin magnetic moments of electron. The orbital magnetic moment of an electron is much smaller than its spin magnetic moment and, hence, the magnetic moments of clusters are mainly from spin magnetic moments. The total magnetic moment of the ground state Cu_5 and Cu_4M (M = Sc-Ni) clusters has been calculated and is shown in Figure 8. The magnetic moment of Cu₄Mn (5 μ _B) is the largest in all doped clusters. The magnetic moment of other Cu₄M clusters is 1, 2, 3, 4, 4, 3 and 2 μ_B for M = Sc, Ti, V, Cr, Fe, Co and Ni, respectively. Interestingly, the magnetic moment of Cu_4M clusters is equal to that of free M atoms, except for M = Cr. This exception can be attributed to the opened 4s shell of Cr atom, while other atoms have a closed 4s shell. The substitution of a Cu atom by a single M (M = Ti-Ni) atom can enhance the magnetism of the host clusters. The various magnetic moments hint that the Cu₄M clusters have potential utility in new nanomaterials with tunable magnetic moments. As an effort to explain the magnetism, Figure 9 displays the spin density of states (SDOS) for the global minimum structures of Cu₄M clusters. All of the ground state clusters have a strong band between -4 and -2 eV, which consists chiefly of the valence s and d orbitals of the constituent atoms. It is clear from this figure that the magnetic moment of Cu_4M (M = Sc-Cr) clusters is generated by the electrons near the HOMO. The magnetic moment of Cu_4M (M = Mn-Ni) largely derives from the energy level far away from HOMO. This implies that the Cu₄Mn, Cu₄Fe, Cu₄Co and Cu₄Ni clusters may be a hard magnetic nanomaterial.



Figure 8. Total magnetic moment of the ground state Cu_4M (M = Sc-Cu) clusters and local magnetic moment on the dopant atoms.



Figure 9. The SDOS of ground state Cu_4M (M = Sc-Ni) clusters. A broadening factor δ = 0.1 eV is used. Spin up (positive) and spin down (negative) densities are given in each case. The blue part is the density difference (spin up minus spin down). The dashed line indicates the location of the HOMO level.

To explore the magnetic properties further, we have executed the natural bond orbital analysis [67] for the most stable Cu₄M (M = Sc-Ni) clusters. The local magnetic moments on M atom is 1.06, 2.14, 3.29, 4.69, 4.93, 3.62, 2.41 and 1.24 μ_B for M = Sc, Ti, V, Cr, Mn, Fe, Co and Ni atoms, as shown in Figure 8. The total magnetic moment of Cu₄M clusters is mainly localized on the M atom. The magnetic moment yielded by the copper atom is small in the total magnetic moment. Furthermore, Cu atoms in Cu₄M (M = Sc-Cr) clusters exhibit an antiferromagetic alignment with respect to the M atom's magnetic moment. Compared with the free atom, the magnetic moment of the M atom in the copper cluster increases for M = Sc, Ti and V atoms and reduces for M = Cr, Mn, Fe, Co and Ni atoms, as displayed in Figure 10. This may be because the number of electrons in the 3*d* shell of dopant atom is less than 5 from Sc to V atoms and is greater than or equal to 5 (\geq 5) from Cr to Ni atoms.



Figure 10. The magnetic moment of the free M atom as the reference point, the change of magnetic moments of the M atom in Cu_4M (M = Sc-Ni) clusters.

The charge and local magnetic moment on 3*d*, 4*s*, 4*p* and 5*p* shells of M atoms in Cu₄M (M = Sc-Cr) clusters are listed in Table 5. It can be seen from Table 5 that the magnetic moment of M atom mainly comes from its 3*d* shell. The 4*s*, 4*p* and 5*p* shells bring a small amount of magnetic moments. In contrast to the isolated atoms, the charge on the 3*d* shell of M atoms except Cr increases 0.35–0.95 e. The charge on 4*s* shell of all dopant atoms decreases by 0.47–1.41 e. In addition, the 4*p* and 5*p* shells of M atoms in Cu₄M cluster are also found to have a number of charges. The distribution of shell charge shows that some electrons of the M atom are transferred from 4*s* shell to 3*d*, 4*p* and 5*p* shells. At the same time, an interatomic charge transfer takes place in the Cu₄M clusters. According to our calculations, 0.1–0.47 e transfer from Sc, V and Cr to Cu atoms; however, 0.01–0.26 e transfer from Cu to Ti, Mn, Fe, Co and Ni atoms. The charge transfer suggests that the M atom in Cu₄M clusters has an orbital hybridization among *s*, *p* and *d* shells. If ΔM and ΔC denote the changes of magnetic moments and charge of 3*d* shells of M atoms, we find that the $|\Delta M|$ increases with the $|\Delta C|$ increasing, as displayed in Figure 11. It can be deduced from this figure that the charge transfer should be the primary reason for the change of the magnetic moment of M atoms in Cu₄M clusters.



Figure 11. The change of magnetic moment (ΔM) and the charge transfer (ΔC) of 3*d* orbital of M atom in Cu₄M (M = Sc-Ni) clusters.

4. Conclusions

The structural, electronic and magnetic properties of Cu_4M (M = Sc-Ni) clusters have been investigated by the CALYPSO structure searching method and density functional theory. The structural searches reveal that M atoms in the most stable Cu_4M clusters favor the most highly coordinated position. The structure of Cu_4M clusters resembles that of Cu_5 cluster. The infrared spectra, Raman spectra and PES are given to identify the ground state. Research of electronic properties shows that the M atoms in Cu_4M (M = Sc-V and Fe-Ni) clusters can improve the stability of the host cluster. The energy gap of all Cu_4M clusters is bigger than that of Cu_5 cluster. The magnetism analyses indicate that the 3*d* transition-metal atom in the Cu_4M cluster carries most of the total magnetic moment. The change of magnetic moment is closely related to the charge transfer.

Acknowledgments: This project was supported by the National Natural Science Foundation of China (11574220) and by the Education Department of Sichuan Province (Grant No. 172481).

Author Contributions: D.D., X.-Y.K. and Z.-Q.Z conceived and designed technology roadmap; B.-X.Z, D.D., J.-J.G. and Q.D. performed the computations; D.D. wrote the paper; B.-X.Z plotted Figures; All authors analyzed the data and revised the paper.

Conflicts of Interest: The authors declare no conflict of interest.

References

- Xing, X.D.; Wang, J.J.; Kuang, X.Y.; Xia, X.X.; Lu, C.; Maroulis, G. Probing the low-energy structures of aluminum-magnesium alloy clusters: A detailed study. *Phys. Chem. Chem. Phys.* 2016, *18*, 26177–26183. [CrossRef] [PubMed]
- Kuang, X.J.; Wang, X.Q.; Liu, G.B. A density functional study on the Au_nAg (n = 1–12) alloy clusters. *J. Alloys Compd.* 2013, 570, 46–56. [CrossRef]
- 3. Zhang, C.; Chen, C.; Dong, H.; Shen, J.R.; Zhao, H.; Dau, J. A synthetic Mn₄Ca-cluster mimicking the Oxygen-evolving center of photosynthesis. *Science* **2015**, *348*, 690–693. [CrossRef] [PubMed]
- 4. Hussain, R.; Hussain, A.I.; Chatha, S.A.S.; Mansha, A.; Ayub, K. Density functional theory study of geometric and electronic properties of full range of bimetallic Ag_nY_m (n + m = 10) clusters. *J. Alloys Compd.* **2017**, 705, 232–246. [CrossRef]
- 5. Eric, C.T.; Stefan, V. Catalysis by clusters with precise numbers of atoms. Nat. Nanotechnol. 2015, 10, 577–588.
- 6. Pakiari, A.H.; Jamshidi, Z. Nature and strength of M-S bonds (M = Au, Ag and Cu) in binary alloy gold clusters. *J. Phys. Chem. A* 2010, *114*, 9212–9221. [CrossRef] [PubMed]
- Tahzeeb, M.; Ashok, B. Nanoscale alloying: A study in free Cu-Ag bimetallic clusters. J. Alloys Compd. 2013, 559, 24–33.
- Brito, B.G.A.; Hai, G.Q.; Rabelo, J.N.T.; Candido, L. A quantum Monte Carlo study on electron correlation in all-metal aromatic clusters MAl₄⁻ (M = Li, Na, K, Rb, Cu, Ag and Au). *Phys. Chem. Chem. Phys.* 2014, 16, 8639–8645. [CrossRef] [PubMed]

- Chen, L.; Gao, Y.; Xu, H.; Wang, Z.; Li, Z.; Zhang, R.Q. The mechanism of N-Ag bonding determined tunability of surface-enhanced Raman scattering of pyridine on MAg (M = Cu, Ag, Au) diatomic clusters. *Phys. Chem. Chem. Phys.* 2014, *16*, 20665–20671. [CrossRef] [PubMed]
- 10. Li, W.; Chen, F. Effect of multiple exciton generation on ultraviolet—Visible absorption of Ag-Cu clusters: Ab initio study. *J. Alloys Compd.* **2014**, 607, 238–244. [CrossRef]
- Neukermans, S.; Janssens, E.; Tanaka, H.; Silverans, R.E.; Lievens, P. Element- and Size-Dependent Electron Delocalization in Au_nX⁺ Clusters (X = Sc, Ti, V, Cr, Mn, Fe, Co, Ni). *Phys. Rev. Lett.* 2003, *90*, 033401. [CrossRef] [PubMed]
- Yan, W.; Tang, Z.; Wang, L.; Wang, Q.; Yang, H.; Chen, S. PdAu alloyed clusters supported by carbon nanosheets as efficient electrocatalysts for Oxygen reduction. *Int. J. Hydrogen Energy* 2017, 42, 218–227. [CrossRef]
- 13. Martins, M. Bimetallic PdM (M = Fe, Ag, Au) alloy nanoparticles assembled on reduced graphene oxide as catalysts for direct borohydride fuel cells. *J. Alloys Compd.* **2017**, *718*, 204–214. [CrossRef]
- 14. Kaul, I.; Ghosh, P. First principles investigations of small bimetallic PdGa clusters as catalysts for hydrogen dissociation. *Chem. Phys.* **2017**, *487*, 87–96. [CrossRef]
- 15. Li, G.F.; Zhou, Z.Q.; Chen, X.M.; Wang, J.J. Bimetallic Pb_nCu_n (*n* = 2–14) clusters were investigated by density functional theory. *Comput. Theor. Chem.* **2017**, *1106*, 21–27. [CrossRef]
- 16. Wu, X.; Sun, Y.; Wei, Z.; Chen, T.J. Influence of noble metal dopants (M = Ag, Au, Pd or Pt) on the stable structures of bimetallic Co-M clusters. *J. Alloys Compd.* **2017**, *701*, 447–455. [CrossRef]
- 17. Lee, K.E.; Shivhare, A.; Hu, Y.F.; Scott, R.W.J. Supported bimetallic AuPd clusters using activated Au₂₅ clusters. *Catal. Today* **2017**, *280*, 259–265. [CrossRef]
- 18. Landry, A.M.; Iglesia, E. Displacement-reduction routes to PtPd clusters and mechanistic inferences for the synthesis of other bimetallic compositions. *J. Catal.* **2016**, *344*, 389–400. [CrossRef]
- 19. Chattaraj, D.; Bhattacharya, S.; Dash, S.; Majumder, C. Atomic, electronic, and magnetic properties of bimetallic ZrCo clusters: A first-principles study. *J. Appl. Phys.* **2016**, *120*, 094301. [CrossRef]
- 20. Landry, A.M.; Iglesia, E. Synthesis of bimetallic AuPt clusters with clean surfaces via sequential displacement-reduction processes. *Chem. Mater.* **2016**, *28*, 5872–5886. [CrossRef]
- Oh, E.; Delehanty, J.B.; Field, L.D.; Makinen, A.J.; Goswami, R.; Huston, A.L.; Medintz, I.L. Synthesis and characterization of pegylated luminescent gold nanoclusters doped with silver and other metals. *Chem. Mater.* 2016, 28, 8676–8688. [CrossRef]
- Li, W.L.; Liu, C.; Abroshan, H.; Ge, Q.J.; Yang, X.J.; Xu, H.Y.; Li, G. Catalytic CO Oxidation using bimetallic M_xAu_{25-x} clusters: A combined experimental and computational study on doping effects. *J. Phys. Chem. C* 2016, 120, 10261–10267. [CrossRef]
- Sels, A.; Salassa, G.; Pollitt, S.; Guglieri, C.; Rupprechter, G.; Barrabes, N.; Burgi, T. Structural investigation of the ligand exchange reaction with rigid dithiol on doped (Pt, Pd) Au₂₅ Clusters. *J. Phys. Chem. C* 2017, 121, 10919–10926. [CrossRef]
- 24. Elisa, M.S.H.; Juan, M.M.C.; Pedro, G.A.L. Global minimum structures, stability and electronic properties of small Ni_xSn_y ($x + y \le 5$) bimetallic clusters; A DFT study. *Eur. Phys. J. D* **2016**, *70*, 208.
- Carretta, S.; Amoretti, G.; Santini, P.; Mougel, V.; Mazzanti, M.; Gambarelli, S.; Colineau, E.; Caciuffo, R. Magnetic properties and chiral states of a trimetallic uranium complex. *J. Phys. Condens. Matter* 2013, 25, 486001. [CrossRef] [PubMed]
- 26. Chiesa, A.; Carretta, S.; Santini, P.; Amoretti, G.; Pavarini, E. Many-body ab initio study of antiferromagnetic {Cr₇M} molecular rings. *Phys. Rev. B* **2016**, *94*, 224422. [CrossRef]
- 27. Adams, R.D.; Zhang, Q.; Yang, X.Z. Two-dimensional bimetallic carbonyl cluster complexes with new properties and reactivities. *J. Am. Chem. Soc.* **2011**, *133*, 15950–15953. [CrossRef] [PubMed]
- Cuadrado, R.; Chantrell, R.W. Electronic and magnetic properties of bimetallic L1(0) cuboctahedral clusters by means of fully relativistic density-functional-based calculations. *Phys. Rev. B* 2012, *86*, 224415. [CrossRef]
- 29. Yang, Y.; Cheng, D.J. Role of Composition and geometric relaxation in CO₂ binding to Cu-Ni bimetallic clusters. *J. Phys. Chem. C* 2014, *118*, 250–258. [CrossRef]
- 30. Mondal, K.; Banerjee, A.; Ghanty, T.K. Structural and chemical properties of subnanometer-sized bimetallic Au₁₉Pt cluster. *J. Phys. Chem. C* 2014, *118*, 11935–11945. [CrossRef]

- Chen, L.; Gao, Y.; Cheng, Y.K.; Su, Y.B.; Wang, Z.G.; Li, Z.Q.; Zhang, R.Q. Strong core@shell dependence in surface-enhanced raman scattering of pyridine on sTable 13-atom silver-caged bimetallic clusters. *J. Phys. Chem. C* 2015, 119, 17429–17437. [CrossRef]
- Pellarin, M.; Issa, I.; Langlois, C.; Lebeault, M.A.; Ramade, J.; Lerme, J.; Broyer, M.; Cottancin, E. Plasmon spectroscopy and chemical structure of small bimetallic Cu_(1-x)Ag_x clusters. *J. Phys. Chem. C* 2015, 119, 5002–5012. [CrossRef]
- 33. Li, H.F.; Wang, H.Q. Probing the stability of neutral and anionic transition-metal-doped golden cage nanoclusters: M@Au₁₆ (M = Sc, Ti, V). *Phys. Chem. Chem. Phys.* **2014**, *16*, 244–254. [CrossRef] [PubMed]
- 34. Lu, C.; Kuang, X.Y.; Lu, Z.W.; Mao, A.J.; Ma, Y.M. Determination of structures, stabilities, and electronic properties for bimetallic cesium-doped gold clusters: A density functional theory study. *J. Phys. Chem. A* **2011**, *115*, 9273–9281.
- 35. Irena, E.; Moshe, S. DFT study of small bimetallic palladium-copper clusters. *Chem. Phys. Lett.* **2005**, 401, 232–240.
- 36. Pham, H.T.; Cuong, N.T.; Tam, N.M.; Tung, N.T. A systematic investigation on CrCu_n clusters with *n* = 9–16: Noble gas and tunable magnetic property. *J. Phys. Chem. A* **2016**, *120*, 7335–7343. [CrossRef] [PubMed]
- 37. Holtzl, T.; Janssens, E.; Veldeman, N.; Veszpremi, T.; Lievens, P.; Nguyen, M.T. The Cu₇Sc cluster is a stable s-aromatic seven-membered ring. *ChemPhysChem* **2008**, *9*, 833–838. [CrossRef] [PubMed]
- Holtzl, T.; Veldeman, N.; De, H.J.; Veszpremi, T.; Lievens, P.; Nguyen, M.T. Growth mechanism and chemical bonding in scandium-doped copper clusters: Experimental and theoretical study in concert. *Chem. Eur. J.* 2009, 15, 3970–3982. [CrossRef] [PubMed]
- Veldeman, N.; Holtzl, T.; Neukermans, S.; Veszpremi, T.; Nguyen, M.T.; Lievens, P. Experimental observation and computational identification of Sc@Cu₁₆⁺ a stable dopant-encapsulated copper cage. *Phys. Rev. A* 2007, 76, 011201. [CrossRef]
- 40. Hirabayashi, S.; Ichihashi, M. Reactions of Ti- and V-doped Cu cluster cations with nitric oxide and oxygen: Size dependence and preferential NO adsorption. *J. Phys. Chem. A* **2016**, *120*, 1637–1643. [CrossRef] [PubMed]
- 41. Cutrano, C.S.; Lekka, C.E. Structural, magnetic and electronic properties of Cu-Fe nanoclusters by density functional theory calculations. *J. Alloys Compd.* **2017**, 707, 114–119. [CrossRef]
- 42. Li, C.G.; Zhang, J.; Yuan, Y.Q.; Tang, Y.N.; Ren, B.Z.; Chen, W.G. Geometries, stabilities and electronic properties of copper and selenium doped copper clusters: Density functional theory study. *Physica E* **2017**, *86*, 303–310. [CrossRef]
- 43. Jiang, Z.Y.; Lee, K.H.; Li, S.T.; Chu, S.Y. Structures and charge distributions of cationic and neutral $Cu_{n-1}Ag$ clusters (n = 2-8). *Phys. Rev. B* **2006**, *73*, 235423. [CrossRef]
- 44. Han, S.L.; Xue, X.L.; Nie, X.C.; Zhai, H.; Wang, F.; Sun, Q.; Jia, Y.; Li, S.F.; Guo, Z.X. First-principles calculations on the role of Ni-doping in Cu_n clusters: From geometric and electronic structures to chemical activities towards CO₂. *Phys. Lett. A* **2010**, *374*, 4324–4330. [CrossRef]
- 45. Kahnouji, H.; Najafvandzadeh, H.; Hashemifar, S.J.; Alaei, M.; Akbarzadeh, H. Density-functional study of the pure and palladium doped small copper and silver clusters. *Chem. Phys. Lett.* **2015**, *630*, 101–105. [CrossRef]
- Ricardo-Chavez, J.L.; Pastor, G.M. First principles calculations on Ni impurities in Cu clusters. J. Magn. Magn. Mater. 2005, 294, 122–126. [CrossRef]
- 47. Li, C.G.; Shen, Z.G.; Hu, Y.F.; Tang, Y.N.; Chen, W.G.; Ren, B.Z. Insights into the structures and electronic properties of Cu_{n+1}^{μ} and Cu_nS^{μ} (n = 1-12; $\mu = 0 \pm 1$) clusters. *Sci. Rep.* **2017**, *7*, 1345. [CrossRef] [PubMed]
- 48. Li, J.; Liu, Y.Q.; Zhang, J.J.; Liang, X.G.; Duan, H.M. Density functional theory study of the adsorption of hydrogen atoms on Cu₂X (X = 3*d*) clusters. *Chem. Phys. Lett.* **2016**, *651*, 137–143. [CrossRef]
- 49. Cao, Z.; Guo, L.; Liu, N. A theoretical study of the water—Gas-shift reaction on Cu₆TM (TM = Co, Ni, Cu, Rh, Pd, Ag, Ir, Pt, Au) Clusters. *J. Clust. Sci.* **2016**, 27, 523–535. [CrossRef]
- 50. Sargolzaei, M.; Lotfizadeh, N. Spin and orbital magnetism of a single 3*d* transition-metal atom doped into icosahedral coinage-metal clusters X₁₂ (X = Cu, Ag, Au). *Phys. Rev. B* **2011**, *83*, 155404. [CrossRef]
- 51. Frisch, M.J.; Trucks, G.W.; Schlegel, H.B.; Scuseria, G.E.; Robb, M.A.; Cheeseman, J.R.; Montgomery, J.A., Jr.; Vreven, T.; Kudin, K.N.; Burant, J.C.; et al. *Gaussian 09 Revision A. 02*; Gaussian, Inc.: Wallingford, CT, USA, 2009.

- 52. Lee, C.; Yang, W.; Parr, R.G. Development of the Colle-Salvetti correlation-energy formula into a functional of the electron density. *Phys. Rev. B* **1988**, *37*, 785–789. [CrossRef]
- 53. Becke, A.D. A new mixing of Hartree-Fock and local density-functional theories. *J. Chem. Phys.* **1993**, *98*, 1372–1377. [CrossRef]
- 54. Wadt, W.R.; Hay, P.J. Ab initio effective core potentials for molecular calculations. Potentials for main group elements Na to Bi. *J. Chem. Phys.* **1985**, *82*, 284–298. [CrossRef]
- 55. Hay, P.J.; Wadt, W.R. Ab initio effective core potentials for molecular calculations. Potentials for K to Au including the outermost core orbitals. *J. Chem. Phys.* **1985**, *82*, 299–311. [CrossRef]
- 56. Wang, Y.; Lv, J.; Zhu, L.; Ma, Y. Crystal structure prediction via particle-swarm optimization. *Phys. Rev. B* **2010**, *82*, 094116. [CrossRef]
- 57. Guzmán-Ramírez, G.; Aguilera-Granja, F.; Robles, J. DFT and GEGA genetic algorithm optimized structures of clusters. *Eur. Phys. J. D* 2010, *57*, 49–60. [CrossRef]
- Wang, S.Y.; Yu, J.Z.; Mizuseki, H.; Sun, Q.; Wang, C.Y.; Kawazoe, Y. Energetics and local spin magnetic moment of single 3, 4*d* impurities encapsulated in an icosahedral Au₁₂ cage. *Phys. Rev. B* 2004, 70, 165413. [CrossRef]
- 59. Wu, X.; Ray, A.K. A density functional study of small neutral and cationic vanadium clusters V_n and V_n^+ (n = 2-9). *J. Chem. Phys.* **1999**, *110*, 2437. [CrossRef]
- 60. Simard, B.; Lebeaultdorget, M.A.; Marijnissen, A.; Meulen, J.J.T. Photoionization spectroscopy of dichromium and dimolybdenum: Ionization potentials and bond energies. *J. Chem. Phys.* **1998**, *108*, 9668–9674. [CrossRef]
- 61. Ma, Q.M.; Xie, Z.; Wang, J.; Liu, Y.; Li, Y.C. Structures, binding energies and magnetic moments of small iron clusters: A study based on all-electron DFT. *Solid State Commun.* **2007**, *142*, 114. [CrossRef]
- 62. Morse, M.D. Clusters of transition-metal atoms. Chem. Rev. 1988, 86, 1049–1109. [CrossRef]
- 63. Gagliardi, L. When does gold behave as a halogen? Predicted uranium tetraauride and other MAu₄ tetrahedral species, (M = Ti, Zr, Hf, Th). *J. Am. Chem. Soc.* **2003**, *125*, 7504. [CrossRef] [PubMed]
- 64. Cha, C.; Ganteför, G.; Eberhardt, W. Photoelectron spectroscopy of Cu_n⁻ clusters: Comparison with jellium model predictions. *J. Chem. Phys.* **1993**, *99*, 6308–6312. [CrossRef]
- 65. Ingolfsson, O.; Busolt, U.; Sugawara, K. Energy-resolved collision-induced dissociation of Cu_n^+ (n = 2-9): Stability and fragmentation pathways. *J. Chem. Phys.* **2000**, *112*, 4613–4620. [CrossRef]
- Rienstra-Kiracofe, J.C.; Tschumper, G.S.; Schaefer, H.F.; Nandi, S.; Ellison, G.B. Atomic and molecular electron affinities: Photoelectron experiments and theoretical computations. *Chem. Rev.* 2002, 102, 231–282. [CrossRef] [PubMed]
- 67. Reed, A.E.; Curtiss, L.A.; Weinhold, F. Intermolecular Interactions from a Natural Bond Orbital, Donor-Acceptor Viewpoint. *Chem. Rev.* **1988**, *88*, 899–926. [CrossRef]



© 2017 by the authors. Licensee MDPI, Basel, Switzerland. This article is an open access article distributed under the terms and conditions of the Creative Commons Attribution (CC BY) license (http://creativecommons.org/licenses/by/4.0/).