

Neuronal heterogeneity of normalization strength in a circuit model

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Abstract

The size of a neuron's receptive field increases along the visual hierarchy. Neurons in higher-order visual areas integrate information through a canonical computation called normalization, where neurons respond sublinearly to multiple stimuli in the receptive field. Neurons in the visual cortex exhibit highly heterogeneous degrees of normalization. Recent population recordings from visual cortex find that the interactions between neurons, measured by spike count correlations, depend on their normalization strengths. However, the circuit mechanism underlying the heterogeneity of normalization is unclear. In this work, we study normalization in a spiking neuron network model of visual cortex. The model produces a range of neuronal heterogeneity of normalization strength and the heterogeneity is highly correlated with the inhibitory current each neuron receives. Our model reproduces the dependence of spike count correlations on normalization as observed in experimental data, which is explained by the covariance with the inhibitory current. We find that neurons with stronger normalization are more sensitive to contrast differences in images and encode information more efficiently. In addition, networks with more heterogeneity in normalization encode more information about visual stimuli. Together, our model provides a mechanistic explanation of heterogeneous normalization strengths in the visual cortex, and sheds new light on the computational benefits of neuronal heterogeneity.

Introduction

Understanding how the brain integrates and extracts information from multiple stimuli has long been a central focus in neuroscience. In visual cortex, neurons in the primary visual area respond to local features of stimuli, such as orientation and moving direction, while neurons in the higher-order visual areas have broader receptive fields and extract global features of visual stimuli. The responses of visual neurons to multiple stimuli have been well characterized by a phenomenon known as normalization, where neurons respond sublinearly.

34 Normalization has been observed across brain regions (Heeger, 1992; Louie et al., 2011; Ohshiro et al., 2011),
35 sensory modalities (Olsen et al., 2010; Rabinowitz et al., 2011) and species (Barbera et al., 2022; MacEvoy
36 et al., 2009; Ni et al., 2012), and has been regarded as a canonical computation in nervous system (Carandini
37 and Heeger, 2012). Normalization has also been thought to be the fundamental mechanism through which
38 selective attention acts to enhance neuronal responses to attended stimulus (Reynolds and Heeger, 2009).

39 It has long been demonstrated that the strength of normalization is variable across neurons (Lee and Maunsell,
40 2009; Ni et al., 2012; Ruff et al., 2016). Some neurons are suppressed by the addition of a non-preferred
41 stimulus, while some neurons show additive responses to multiple stimuli. Recent population recordings from
42 multiple visual cortical areas of macaque monkeys reveal that the interactions between neurons, measured by
43 spike count correlations, depend on their normalization strengths (Ruff et al., 2016; Verhoef and Maunsell,
44 2017). Spike count correlations are shaped by network connectivity and dynamical state, and impose strong
45 constraints on circuit models (Hennequin et al., 2018; Huang et al., 2019; Huang, 2021; Ocker et al., 2017). In
46 addition, spike count correlations constrain the amount of information encoded by a neuronal population (Kohn
47 et al., 2016) and can reflect perceptual inference (Bányai and Orbán, 2019). Therefore, an understanding of the
48 network mechanisms underlying the relationship between normalization strength and neuronal correlations is
49 likely to provide insights into the neural population code of the integration of multiple stimuli.

50 Despite the success of the phenomenological models of divisive normalization at reproducing the firing rates
51 of neurons under different stimulus conditions, the neurophysiological basis of normalization remains unclear.
52 Recently, mechanistic circuit models have been developed to account for the sublinear response properties or
53 reproduce the divisive scaling of responses (Heeger and Mackey, 2019; Heeger and Zemlianova, 2020; Lindsay
54 et al., 2019; Rubin et al., 2015). However, they focus on modeling the trial-averaged neuronal responses in
55 homogeneous neural populations and do not consider the trial-to-trial correlations between neurons and the
56 heterogeneity of normalization strength. Recent statistical models of normalization suggest that the strength of
57 normalization impacts the spiking variability of individual neurons and the correlations between neurons, how-
58 ever, they do not take into account network interactions that shape both normalization and neural correlations
59 (Coen-Cagli and Solomon, 2019; Weiss et al., 2023).

60 In this work, we study normalization in a two-layer network of spiking neurons, modeling the primary visual
61 cortex (V1) and a higher-order visual area (V4 or MT). The network produces internally generated spiking vari-
62 ability due to a balance of strong excitation and inhibition (Huang et al., 2019; Van Vreeswijk and Sompolinsky,
63 1996). The neurons in our model exhibit a range of normalization strengths in response to multiple stimuli. Our
64 model reproduces the dependence of spike count correlations on normalization strength as observed in experi-
65 mental data (Ruff et al., 2016). Interestingly, we identify the inhibitory current to be the major determinant of
66 normalization strength and its relationship with spike count correlations. Further, we demonstrate that neurons
67 with stronger normalization are more sensitive to contrast differences of visual stimuli and encode information
68 more efficiently. Networks with more heterogeneity in normalization encode higher information about visual
69 stimuli, demonstrating the computational benefits of neuronal heterogeneity.

70 **Results**

71 We use a two-layer spiking neuron network model, with the feedforward layer modeling V1 neurons and the re-
72 current layer modeling V4 or MT area (Figure 1A). Two Gabor images of orthogonal orientations are presented
73 to the network. The V1 neurons are modeled as linear-nonlinear-Poisson neurons with Gabor receptive fields

74 oriented at their preferred orientation, determined from a superimposed pinwheel orientation map (Kaschube
75 et al., 2010). There are two populations of V1 neurons, $V1_1$ and $V1_2$, each of which has a non-overlapping
76 receptive field centering on each Gabor image, respectively.

77 The V4/MT layer is a recurrent network of excitatory and inhibitory neurons, each modeled as an exponential
78 integrate-and-fire neuron. Neurons from the V4/MT layer receive inputs from both V1 populations and respond
79 to both images (Figure 1B). There are two types of connections in both feedforward projections from V1 to
80 V4/MT and recurrent projections within the V4/MT layer (Figure 1A), following anatomical findings from
81 visual cortex (Angelucci et al., 2002; Bosking et al., 1997; Malach et al., 1993; Mariño et al., 2005). The
82 majority of connections are local, of which the connection probability decays with distance. We choose the
83 spatial scales of excitatory and inhibitory projections to be the same, consistent with anatomy (Mariño et al.,
84 2005). A small portion of connections are long-range, meaning that their connection probability does not
85 depend on distance, but they connect between similarly tuned excitatory neurons. The spatially dependent
86 connections allow the V4/MT neurons to retain location information of the two images, while the tuning specific
87 long-range connections increase the tuning selectivity and the size of receptive fields of V4/MT neurons.

88 The V4/MT network admits a stable and asynchronous solution with homogeneous V1 inputs, similar to the
89 classic balanced network model (Renart et al., 2010; Van Vreeswijk and Sompolinsky, 1996) (Supp Fig S1).
90 The balance between strong excitation and inhibition generates Poisson-like spiking variability in individual
91 neurons. The distribution of firing rates is lognormal due to the expansive transfer function of neurons with
92 large input fluctuations (Roxin et al., 2011). With orientation-tuned inputs from V1, the V4/MT model neurons
93 capture several features of neuronal responses in visual cortex, as shown in our previous work (Huang et al.,
94 2022). The tuning curves are heterogeneous with various widths and magnitudes (Ringach et al., 2002). The
95 spike count correlations are higher between similarly tuned neurons (Cohen and Maunsell, 2009; Gu et al.,
96 2011), and depend on stimulus orientation (Hennequin et al., 2018; Lin et al., 2015; Ponce-Alvarez et al.,
97 2013).

98 **Broad distribution of normalization strengths in the model and data**

99 We analyze the network responses to two Gabor images with orthogonal orientations, which are known to evoke
100 the normalization mechanism in the visual cortex (Busse et al., 2009; Ni et al., 2012; Ruff et al., 2016; Verhoef
101 and Maunsell, 2017). Neurons' responses to two stimuli presented together tend to be much less than the linear
102 sum of the responses to each stimulus when presented individually. This phenomenon has been observed across
103 the visual hierarchy in macaque monkeys (Ruff et al., 2016) as well as in the primary visual cortex in cat (Busse
104 et al., 2009) and tree shrew (MacEvoy et al., 2009).

105 When presented with one image, neurons that prefer the orientation of the image are activated across the V4/MT
106 network, resulting in local patches of active regions following the pinwheel map of orientation preference
107 (Figure 1B1, B2). Neurons in the same spatial location of the presented image respond with higher rates since
108 they receive more local feedforward inputs. When both images are presented together, there is no clear spatial
109 structure of population activation pattern of firing rates (Figure 1 B3).

110 We define normalization index of each neuron as the sum of the neuron's firing rates in response to each image
111 presented individually, divided by its firing rate when both images are presented together (Eq. 14), following
112 the definition from our previous experimental work (Ruff et al., 2016). A normalization index of one means
113 that the neuron's response to multiple stimuli is a linear summation and a normalization index larger than one

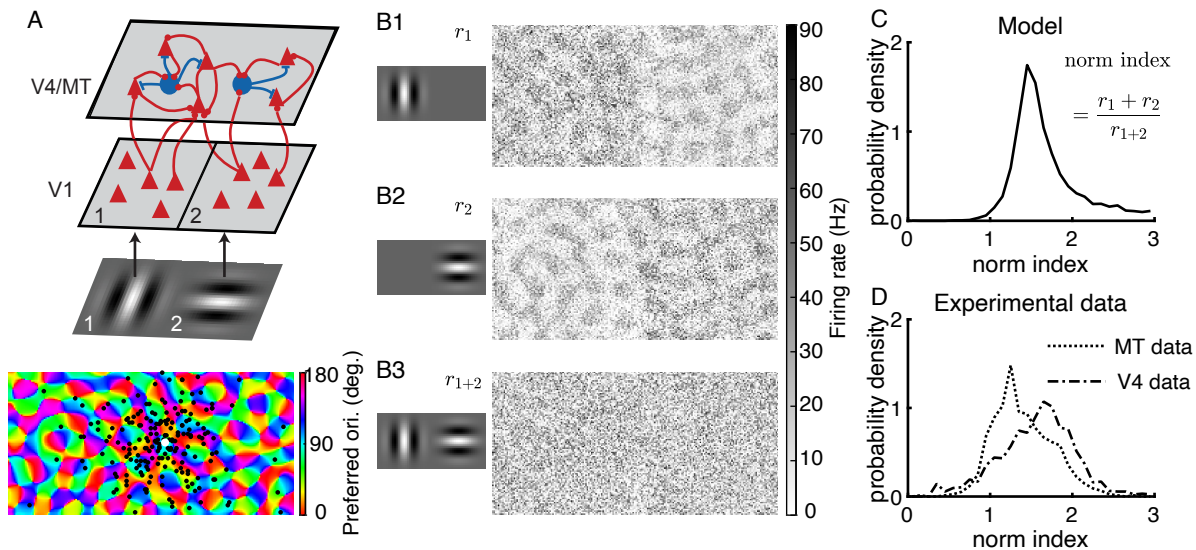


Figure 1: Model schematic, activation patterns, and distributions of normalization indices.

(A) Model schematic. V4/MT area is modeled as a spatially ordered spiking neuron network of excitatory and inhibitory neurons. V1 neurons are modeled as linear-nonlinear-Poisson neurons with Gabor receptive fields. The two sub-populations of V1 neurons, V1₁ and V1₂, have non-overlapping receptive fields, each centering on one Gabor image. The preferred orientations of both V4/MT and V1 neurons are assigned according to pinwheel orientation maps (bottom panel). Bottom: Locations of postsynaptic excitatory neurons (black dots) of one example presynaptic excitatory neuron (white dot) in the V4/MT layer. The majority of the connections are local in space and a small portion of the connections are between similarly tuned excitatory neurons across the whole network (see Methods). (B) Firing rate patterns of the model V4/MT neurons when one Gabor image is presented at location 1 (B1) or location 2 (B2), or when both images of orthogonal orientations are presented together (B3). (C) The model V4/MT neurons exhibit a wide range of normalization indices. The normalization index is defined as the sum of the neuron's firing rates in response to each image presented individually (B1, B2), divided by its firing rate when both images are presented together (B3). (D) The normalization indices of neurons recorded from macaque V4 and MT areas (data from Ruff et al. (2016)).

114 means a sublinear summation. A larger normalization index means stronger normalization.

115 Our model V4/MT neurons exhibit a wide range of normalization indices with the majority being between one
116 and two (Figure 1C). The normalization indices of our model neurons span a similar range as those of neurons
117 recorded from macaque V4 and MT areas (Figure 1D; Ruff et al. (2016)). The normalization index of a neuron
118 is independent from its tuning preference in both our model and data (Figure S2). The wide distribution of
119 normalization indices is a robust phenomenon in networks with strong recurrent connections (Figure S3). Even
120 in random networks with no spatial or tuning dependent connections, there is a spread of normalization indices
121 due to random connections when two input populations project to the whole network (Figure S3A,B magenta).
122 The distribution widens when the two input populations project to distinct sets of target neurons (Figure S3B
123 cyan). In our model, the two images of orthogonal orientations activate different sets of V4/MT neurons, which
124 is similar to the case with small overlap of input projections in the random networks (Figure S3B). In contrast,
125 networks with weak recurrent connections produce narrow distributions of normalization strengths (Figure S4).
126 Being able to reproduce the range of neuronal heterogeneity of normalization in our model, we next examine
127 how neurons with different normalization strengths interact with each other.

128 **Spike count correlations between neurons depend on their similarity of normalization strength**

129 The neuronal heterogeneity of normalization strength in our model is shaped by network connectivity and
130 neuronal transfer functions. Both factors are known to determine the interactions between neurons (Huang
131 et al., 2019; Ocker et al., 2017). Next we examine how correlations between neurons depend on neurons'
132 normalization indices. We use spike count correlations to measure the interactions between neurons, which is
133 commonly used to measure the trial-to-trial co-fluctuations of neuronal responses in experiments (Cohen and
134 Kohn (2011); see Methods).

135 We find that spike count correlations between neurons depend on their normalization indices in the model in a
136 way that is qualitatively consistent with the neuronal correlations measured in visual cortex (Figure 2). First,
137 neurons with similar normalization indices have higher spike count correlations than those with different nor-
138 malization indices (diagonal vs. off-diagonal elements in Figure 2A1, B1 and C1). For neuron pairs of the same
139 average normalization indices, their spike count correlations decrease as the difference between their normal-
140 ization indices becomes larger (Figure 2A2, B2 and C2). Second, for neuron pairs with similar normalization
141 indices (diagonal elements in Figure 2A1, B1 and C1), their spike count correlations first decrease with their
142 average normalization indices and can increase at large normalization indices in the model and the V4 data
143 (Figure 2A3, B3 and C3). The same pattern of spike count correlations is also observed in neurons recorded
144 from Macaque V1 area (Supp Fig S5). The model also produces the same relationship between spike count cor-
145 relation and normalization strengths using superimposed Gabor images in addition to two separately presented
146 images (Supp Fig S6). The close match of the dependence of correlations on normalization indices in our
147 model with that in data suggests common circuit mechanisms that determine the heterogeneity of normaliza-
148 tion. In contrast, the dependence of neuronal correlations on normalization index is very weak in networks with
149 weak recurrent connections, emphasizing the importance of recurrent connections in determining the strength
150 of normalization (Figure S4).

151 A potential explanation for the observed dependence of correlations on the similarity of normalization indices
152 is that neurons with similar normalization indices may have more similar tuning preferences than those with
153 different normalization indices. Several previous experimental studies have consistently demonstrated that

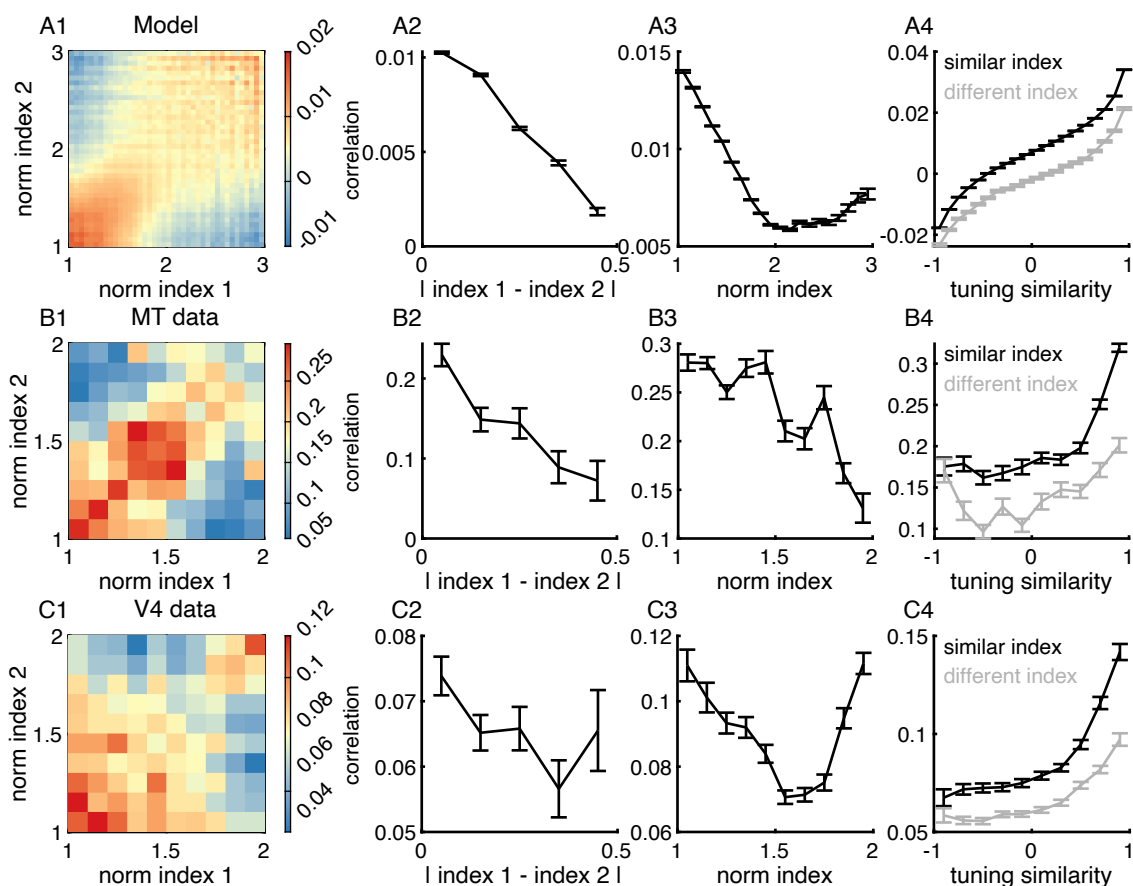


Figure 2: Neurons with similar normalization indices have higher spike count correlations than those with different normalization indices.

(A) Spike count correlations between a pair of model MT/V4 neurons depend on their normalization indices. (A1) Spike count correlations between a pair of neurons as a function of the normalization indices of the pair. (A2) For neuron pairs of the same average normalization indices (equal to 1.5), their spike count correlations decrease with the difference in their normalization indices. (A3) For neuron pairs of similar normalization indices (difference < 0.5), their spike count correlations decrease with their average normalization indices. (A4) Across all levels of tuning similarity, the spike count correlations between neurons with similar normalization indices are consistently larger than those of neurons with distinct normalization indices. (B) Same as (A) for neuronal data recorded from the MT area (28 sessions). (C) Same as (A) for neuronal data recorded from the V4 area (21 sessions). Error bars represent the SEM. Data in panels B and C are from Ruff et al. (2016).

154 neurons with similar tuning preferences tend to have higher spike count correlations (Cohen and Maunsell,
155 2009; Gu et al., 2011; Hennequin et al., 2018; Lin et al., 2015). Therefore, tuning similarity between neurons
156 is a potential confound that underlies the dependence of correlations on normalization indices. However, this is
157 not the case in our model and in data. First, we find no significant correlation between the tuning preference and
158 the normalization index of a neuron in both model and data (Supp Fig S2). Second, we compare the spike count
159 correlations of neuron pairs with either similar or different normalization indices across different magnitudes of
160 tuning similarity, measured as the correlation between the tuning curves of two neurons (Eq. 16). We observe
161 that across all levels of tuning similarity, the spike count correlations between model neurons with similar
162 normalization indices are consistently larger than those of model neurons with distinct normalization indices
163 (Figure 2, A4). We re-analyzed our experimental data and found consistent patterns in neural recordings from
164 all three visual areas, MT (Figure 2 B4), V4 (Figure 2 C4) and V1 (Supp Fig S5).

165 **Recurrent inhibition best explains the heterogeneity of normalization**

166 Having demonstrated that our model successfully reproduces the distribution of normalization strength and the
167 dependence of spike count correlations on normalization indices observed in visual cortex, we next examine
168 the circuit mechanisms in our model that underlie the neuronal heterogeneity of normalization. We decompose
169 the total current each V4/MT neuron receives into three components: feedforward excitation from V1 neurons,
170 recurrent excitation from other V4/MT excitatory neurons and recurrent inhibition from other V4/MT inhibitory
171 neurons. We find that the normalization index of each V4/MT neuron is strongly and negatively correlated
172 with the normalization index of the inhibitory current, defined in the same way as the normalization index of
173 firing rate (Eq. 15; Figure 3C). This means that neurons with stronger normalization receives relatively more
174 inhibition when both images are presented compared to neurons with weaker normalization. In contrast, the
175 correlations between the normalization indices of the firing rates and those of the feedforward and recurrent
176 excitatory currents, respectively, are much weaker (Figure 3A,B). In particular, the weak correlation between
177 normalization and feedforward excitation indicates that the normalization strength of each neuron in the model
178 is mainly determined by recurrent connections. In addition, there is also strong correlation between the firing
179 rate normalization indices and the average inhibitory current a neuron receives when two images are presented,
180 and only weak correlations with the excitatory currents (Supp Fig S7A). The correlation between normalization
181 and the number of excitatory or inhibitory input connections is also weak (Supp Fig S7B).

182 To investigate if the inhibitory currents also contribute to the dependence of spike count correlations on normal-
183 ization indices (Figure 2A), we compute the covariance between the excitatory and inhibitory currents a pair
184 of neurons receive. Let $Total_i$ be the total current neuron i receives ($i = 1, 2$), then $Total_i = E_i + I_i$, where
185 E_i and I_i are the excitatory and inhibitory current, respectively, that neuron i receives. Here we combine both
186 feedforward and recurrent excitation in the excitatory current, E , since the following covariance analysis yields
187 similar patterns for both current types. The covariance between the total currents of neuron 1 and neuron 2 can
188 then be decomposed into four components

$$\text{Cov}(Total_1, Total_2) = \text{Cov}(E_1, E_2) + \text{Cov}(E_1, I_2) + \text{Cov}(I_1, E_2) + \text{Cov}(I_1, I_2). \quad (1)$$

189 Previous theoretical analysis has shown that in balanced network models both the excitatory and inhibitory
190 inputs to a pair of neurons ($\text{Cov}(E_1, E_2)$ and $\text{Cov}(I_1, I_2)$, respectively) are correlated which are cancelled
191 by the large negative correlation between the excitatory and inhibitory inputs ($\text{Cov}(E_1, I_2)$ and $\text{Cov}(I_1, E_2)$)
192 (Renart et al., 2010). In this way, the total current covariance remains small and neurons in the balanced
193 networks are asynchronous.

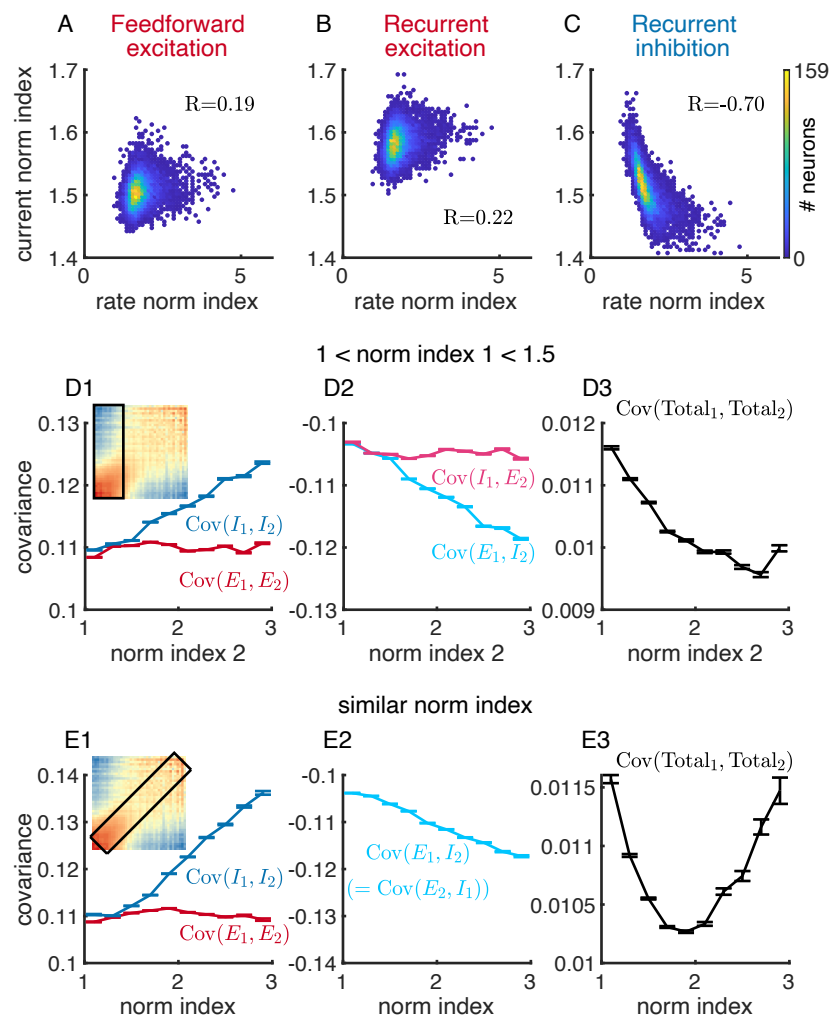


Figure 3: Recurrent inhibition best explains the heterogeneity of normalization.

(A) The relationship between the normalization indices of neurons' firing rates and those of the feedforward excitatory currents neurons receive in the model. (B-C) Similar to (A), but for recurrent excitatory current (B) and recurrent inhibitory current (C). The normalization index of recurrent inhibitory current is strongly correlated with the firing rate normalization index. (D) When restricting the normalization index of neuron 1 in a pair to be between 1 and 1.5, while allowing the normalization index of the neuron 2 to vary, only the covariance components with the inhibitory currents depend on the normalization index of neuron 2 ($Cov(I_1, I_2)$ in D1 and $Cov(E_1, I_2)$ in D2). Here the excitatory current includes both feedforward and recurrent excitation. The covariance between total currents to the pair of neurons, $Cov(Total_1, Total_2)$, decreases with the normalization index of neuron 2 (D3), consistent with the changes in spike count correlations (D1 inset). Inset in D1: Spike count correlations between a pair of neurons as a function of their normalization indices, same as in Figure 2A1. Black box indicates the range of normalization indices of neuron pairs analyzed in panels D1-3. (E) Similar to (D), but for neuron pairs with similar normalization indices (difference < 0.6), indicated by the black box in E1 inset. Note that $Cov(I_1, E_2)$ is the same as $Cov(E_1, I_2)$ in panel E2, as both normalization indices of neuron 1 and neuron 2 vary together.

194 We find that only the covariance components with the inhibitory currents depend on normalization indices
195 in our model. We focus our analysis on two cases. First, we restrict the normalization index of neuron 1
196 in a pair to be between 1 and 1.5, while allowing the normalization index of the neuron 2 to vary (Figure
197 3D1 inset, black box region). As the normalization index of neuron 2 becomes larger and thus more distinct
198 from neuron 1, the inhibitory current of neuron 2 becomes more correlated with the inhibitory current of
199 neuron 1 ($\text{Cov}(I_1, I_2)$ in Figure 3D1) and more negatively correlated with the excitatory current of neuron 1
200 ($\text{Cov}(E_1, I_2)$ in Figure 3D2). In contrast, the covariance components with the excitatory current of neuron 2
201 is independent of its normalization index ($\text{Cov}(E_1, E_2)$ in Figure 3D1 and $\text{Cov}(I_1, E_2)$ in Figure 3D2). The
202 covariance, $\text{Cov}(E_1, I_2)$, becomes more negative than the increase in $\text{Cov}(I_1, I_2)$, resulting in a reduction in
203 the total current covariance, $\text{Cov}(\text{Total}_1, \text{Total}_2)$, as the normalization index of neuron 2 increases (Figure
204 3D3). This is consistent with the changes in spike count correlations (Figure 2A and replicated as the inset of
205 Figure 3D1).

206 Second, we conduct the same analysis of current covariance components for neuron pairs with similar normal-
207 ization indices (Figure 3E1, inset, black box region). We observe a similar pattern: the covariance components
208 with the inhibitory currents, $\text{Cov}(I_1, I_2)$, $\text{Cov}(E_1, I_2)$ and $\text{Cov}(I_1, E_2)$, increase in magnitude with normal-
209 ization index, while the covariance between excitatory currents, $\text{Cov}(E_1, E_2)$, is independent of normalization
210 index (Figure 3E1, E2). Note that $\text{Cov}(I_1, E_2)$ is the same as $\text{Cov}(E_1, I_2)$ in this case as both normalization
211 indices of neuron 1 and neuron 2 vary together. The total current covariance decreases initially as the normal-
212 ization indices of both neurons increase, and turns to increase when normalization is strong due to the large
213 increase in the covariance between inhibitory currents, $\text{Cov}(I_1, I_2)$ (Figure 3E3), consistent with the changes
214 in spike count correlations (Figure 2A1,A3).

215 In sum, we find that neurons with stronger normalization receives more recurrent inhibition from the network.
216 Their inhibitory currents tend to be more correlated with the input currents of other neurons, which allows for
217 better cancellation of current correlations and leads to lower spike count correlations with other neurons.

218 **Neurons with stronger normalization are more sensitive to contrast differences of images**

219 Our results so far have focused on the population response properties of V4/MT neurons to two images of
220 equal contrast. We next examine the dependence of V4/MT neuron responses on the contrast of each image.
221 We observe that neurons exhibit diverse response tuning to different contrast combinations of the two images
222 (Figure 4, A1-A4). We group neurons by their normalization indices (Eq. 14) and their response selectivity to
223 the two images (Eq. 17). Because of symmetry, here we only present results of neurons that prefer stimulus
224 1. Therefore, neurons with strong selectivity respond more strongly to stimulus 1, while neurons with weak
225 selectivity respond similarly to both images.

226 The firing rates of neurons with weak normalization and weak selectivity increase linearly as the contrast of
227 either one of the images increases (Figure 4A1). Thus they respond maximally when both images have high
228 contrast. On the contrary, neurons with strong normalization and weak selectivity are largely suppressed when
229 both images have high contrast, and respond maximally when there is only one image present (Figure 4A2).
230 Neurons with strong selectivity preferentially respond when their preferred image has high contrast (contrast
231 1), as expected (Figure 4A3-A4). However, neurons with strong normalization are much more suppressed
232 by increasing the contrast of their non-preferred image (contrast 2), and respond maximally when only their
233 preferred image is present (Figure 4A4). Together, neurons with heterogeneous normalization strength and

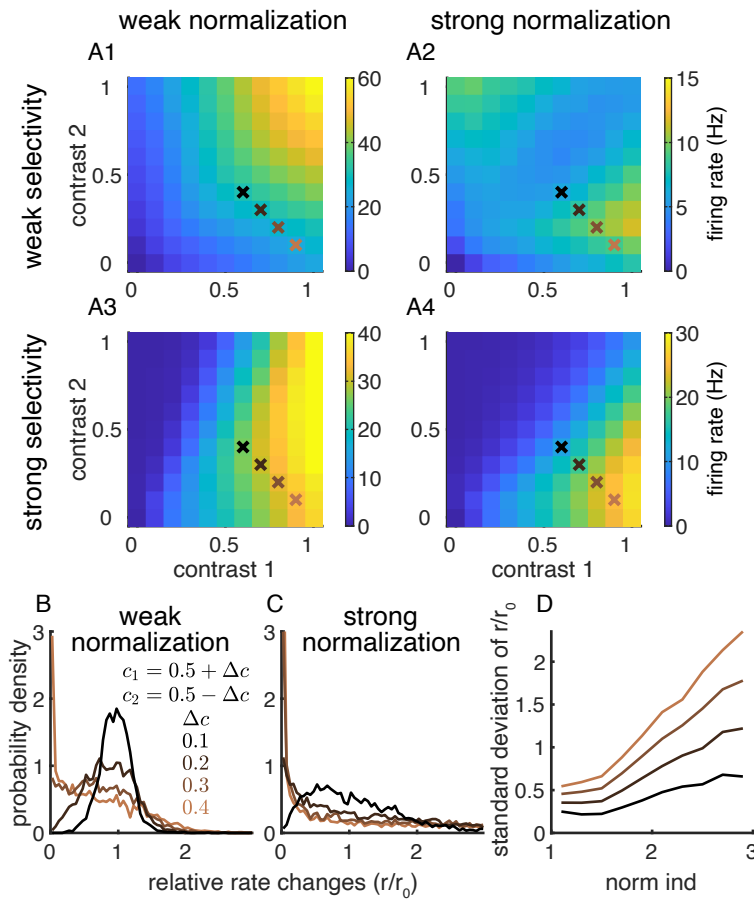


Figure 4: Neurons with stronger normalization are more sensitive to contrast differences of images.

(A) Neurons exhibit diverse response tuning to different contrast combinations of two Gabor images with orthogonal orientations. (A1) The firing rates of neurons with weak normalization and weak selectivity. (A2) The firing rates of neurons with strong normalization and weak selectivity. (A3) The firing rates of neurons with weak normalization and strong selectivity. (A4) The firing rates of neurons with strong normalization and strong selectivity. Neurons that prefer stimulus 1 were selected for the results in A1-4. Crosses indicate the contrast combinations analyzed in B-D with the same color labels. (B-C) As contrast difference between the two images increases, the distribution of relative rate changes (r/r_0) of neurons becomes broader. The relative rate changes are neurons' firing rates to images of a given contrast difference, Δc , divided by their firing rates to images of equal contrast (i.e. $\Delta c = 0$). Neurons with strong normalization (C) have a much broader distribution of relative rate changes compared to neurons with weak normalization (B). (D) The standard deviation of rate changes increases with normalization index.

234 selectivity preferentially respond to different contrast combinations of the two images.

235 We notice in the contrast dependence of responses that neurons with strong normalization are mostly active
236 when the contrast difference between the two images is large (Figure 4A, lower right corners). To quantify
237 this, we consider conditions where the average contrast of the two images is 0.5 and we gradually increase
238 the difference between the contrasts of the two images. Specifically, we choose contrast 1 as $c_1 = 0.5 + \Delta c$
239 and contrast 2 as $c_2 = 0.5 - \Delta c$, where $2\Delta c$ is the contrast difference between the images (crosses in Figure
240 4A1-A4). We quantify the relative change in firing rate, r/r_0 , by normalizing the firing rate of each neuron with
241 its rate (r_0) when both images have equal contrasts, i.e. $\Delta c = 0$. As Δc increases, the distribution of relative
242 rate changes of neurons becomes broader, suggesting that some neurons become more active ($r/r_0 > 1$) while
243 other neurons become more suppressed ($r/r_0 < 1$) (Figure 4B,C). Here neurons of both stimulus preferences
244 are included. For the same contrast difference, Δc , neurons with stronger normalization have a much broader
245 distribution of relative rate changes compared to neurons with weaker normalization, suggesting that they are
246 more sensitive to contrast difference (Figure 4B,C). Indeed, the standard deviation of the distributions of relative
247 rate changes increases with the normalization index for each Δc (Figure 4D). This indicates that neurons with
248 strong normalization exhibit much larger changes in their firing rates when there is a contrast difference in the
249 two images.

250 **Neurons with stronger normalization encode information more efficiently**

251 Normalization has been hypothesized to be computational advantageous because it adapts neurons' dynamical
252 range of responses and can increase neurons' sensitivity to changes in stimulus. To quantify the computa-
253 tional benefits of normalization in our model, we measure the linear Fisher information of stimulus parameters
254 from the activity of neurons with different normalization indices. The linear Fisher information measures the
255 accuracy of estimating a stimulus parameter, such as contrast or orientation, from neuron population activity
256 using an optimal linear decoder (Beck et al., 2011; Kohn et al., 2016; Seriès et al., 2004). The linear Fisher
257 information of a stimulus parameter, s , is defined as

$$I_F(s) = \mathbf{f}'(s)^T \Sigma^{-1}(s) \mathbf{f}'(s), \quad (2)$$

258 where \mathbf{f} is the tuning curve function of the neuron population with respect to s , $'$ denotes differentiation with
259 respect to s , and Σ is the covariance matrix of the population responses. Higher Fisher information means
260 lower threshold in detecting changes in the stimulus parameter s . We focused our analysis on the information
261 of the contrast and orientation of one image while keeping the other image at the same contrast and of an
262 orthogonal orientation. The linear Fisher information were measured from the spike counts of the V4/MT
263 excitatory neurons using a bias-corrected estimation (Kanitscheider et al. (2015); see Methods).

264 We find that neurons with stronger normalization encode more information per spike compared to neurons
265 with weaker normalization (Figure 5). We grouped neurons based on their normalization indices and randomly
266 sampled a various number of neurons within each group. We then divided the Fisher information of the sampled
267 neurons by the their trial-averaged total number of spikes (See Methods). The Fisher information of contrast
268 per spike is non-monotonic for neurons with weak normalization with a maximum at around 12 spikes and
269 reduces to zero as the total number of spikes increases (Figure 5A1,A3). The variance of the Fisher information
270 per spike across samples also peaks at around 10 spikes and largely shrinks when the total number of spikes
271 is above 100. Neurons with stronger normalization encode more information per spike when the total number
272 of spikes is below 100 (Figure 5A2). This is consistent with our observation in the previous section that the

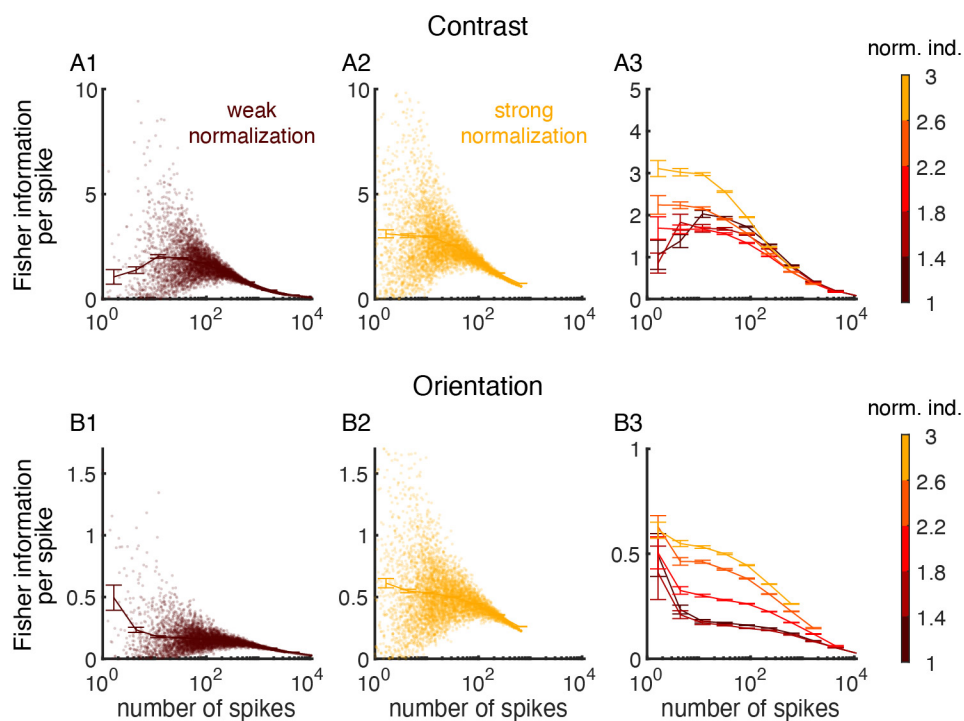


Figure 5: Neurons with stronger normalization encode information more efficiently.

(A) The linear Fisher information (Eq. 2, see Methods) of the contrast of one of the two images per spike from neurons with different normalization indices. Various numbers of neurons were randomly sampled from the model V4/MT excitatory neurons whose normalization indices were within the specified range indicated by the color bar. The linear Fisher information of the sampled group of neurons was divided by the number of spikes from the sampled group of neurons during the time window used for calculating the Fisher information. (A1) The linear Fisher information per spike as a function of the total number of spikes from the sampled neurons. Neurons with normalization indices from 1 to 1.4 were sampled. Each dot is a different sampling of a group of neurons. The solid curves is the average for each bin of the number of spikes and the error bar is standard error. (A2) Same as A1 except that neurons with normalization indices from 2.6 to 3 were sampled. (A3) The average Fisher information per spike as a function of the total number of spikes from the sampled neurons, for neurons of different ranges of normalization indices. Neurons with stronger normalization (lighter color) encode more information per spike than neurons with weak normalization (darker color). (B1-3) Same as A1-3 for the linear Fisher information of the orientation of one of the two images.

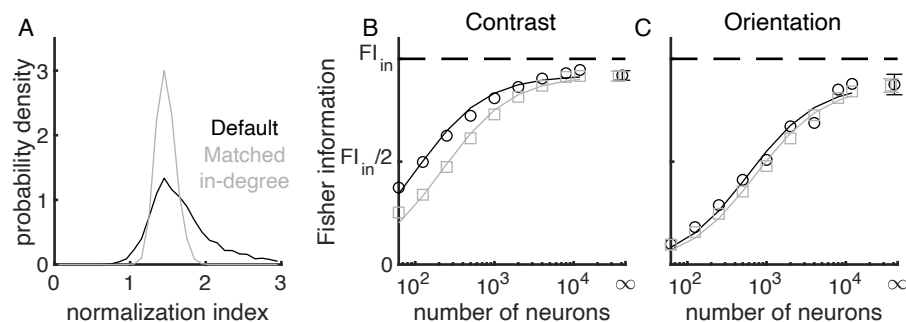


Figure 6: Heterogeneous normalization enhances the information of image contrast but not orientation.

(A) The distribution of normalization indices is narrower in the network with matched in-degrees (grey) than that in the default network (black). In the network with matched in-degrees, the number of presynaptic neurons that project to each V4/MT neuron is fixed to be the same for each type of inputs (recurrent excitation, recurrent inhibition and feedforward excitation). The default network is the same as described in Figure 1 and analyzed in previous figures. (B) The linear Fisher information of the contrast of one image as a function of the number of excitatory neurons sampled from the model V4/MT network. Open circles are the numerical estimation of the linear Fisher information (Eq. 18). The asymptotic values of the linear Fisher information at limit of large number of sampled neurons (dots at $N = \infty$) are estimated by fitting Eq. 19, and solid curves are the fits (see Methods). Error bars are the 95% confidence intervals. Dashed line is the total amount of linear Fisher information from V1 neurons. The total input information is the same for both networks. (C) Same as B for the linear Fisher information of the orientation of one image.

273 firing rates of neurons with strong normalization are sensitive to contrast changes in the images (Figure 4).
 274 The efficiency of information encoding of neurons with different normalization indices converges and decays
 275 to zero when the total number of spikes is large (Figure 5A3). The Fisher information of orientation shows
 276 similar trend as the information of contrast, except that the Fisher information per spike for orientation tends to
 277 decrease monotonically for neurons with weak normalization (Figure 5B).

278 Heterogeneous normalization enhances the information of image contrast but not orientation

279 Lastly, we compare the information content in networks with different amount of heterogeneity in normaliza-
 280 tion. We have shown that the normalization index of a model neuron is strongly correlated with the inhibitory
 281 current it receives (Figure 3A-C). To reduce the heterogeneity in normalization, we constructed a control net-
 282 work with the same number of input connections (i.e. in-degree) to each V4/MT neuron, including both local
 283 and long-range connections, so that neurons receive roughly the same magnitude of currents. All the other
 284 parameters, such as the connection weights and the spatial spreads of connections were kept the same as the
 285 default network. Matching the in-degrees in a homogeneous network without spatial or tuning dependent con-
 286 nections leads to similar firing rates in neurons from the same cell type population (excitatory or inhibitory)
 287 (Brunel, 2000). Matching the in-degrees in our spatial network also largely reduces the spread of normalization
 288 indices (Figure 6A). The remaining heterogeneity in normalization is partly due to the tuning selectivity of
 289 neurons and the spatial arrangement of the pinwheel orientation map.

290 As the number of sampled V4/MT neurons increases, the Fisher information of the sampled neurons increases

291 and approaches the upper bound of the total input information from V1 neurons (Figure 6B,C). The information
292 of image contrast is higher in the default network than that in the network with matched in-degrees, which has
293 less heterogeneity in normalization (Figure 6B). The information difference between the two networks reduces
294 as the number of sampled neurons increases and the information curves from both networks saturate to a
295 similar level close to the upper bound of input information. This again demonstrates the efficiency of neural
296 coding in networks with heterogeneity, that is, networks with more heterogeneity of normalization encode more
297 information of contrast with a smaller number of neurons.

298 Interestingly, the information of orientation is very similar in both networks with different amounts of nor-
299 malization heterogeneity across various number of sampled neurons, with the information from the default
300 network being slightly higher (Figure 6C). This suggests that heterogeneous normalization is more beneficial
301 for encoding contrast than orientation in our network.

302 Discussion

303 Normalization mechanism has often been used to describe neurons' sublinear responses to multiple stimuli in
304 visual cortex (Britten and Heuer, 1999; Heeger, 1992; Ni et al., 2012; Rust et al., 2006; Verhoef and Maunsell,
305 2017)). However, neurons exhibit diverse response patterns in their integration of multiple stimuli; some neu-
306 rons show facilitated responses to two stimuli, while some neurons are strongly suppressed by an addition of a
307 non-preferred stimulus (Barbera et al., 2022; Guan et al., 2020; Ni et al., 2012; Ruff et al., 2016). The mech-
308 anism underlying the neuronal heterogeneity of normalization and its contribution to neural coding is not well
309 studied. In this work, we analyzed response properties of a recurrent network of excitatory and inhibitory spik-
310 ing neurons modeling the visual cortex. Our model neurons exhibit a range of normalization strengths that is
311 consistent with experimental data (Ruff et al., 2016). We find that a neuron's normalization strength is strongly
312 correlated with the relative magnitude of inhibitory current it receives. In addition, our model reproduces the
313 relationship between normalization strength and the spike count correlations between pairs of neurons observed
314 in experimental data, which can be explained by the covariance with inhibitory current. Further, we demonstrate
315 that model neurons with different normalization strengths and selectivity respond to different combinations of
316 the stimulus contrasts. Model neurons with stronger normalization are more sensitive to the contrast difference
317 of images and encode more stimulus information per spike. Lastly, we show that neuronal heterogeneity can
318 be beneficial for coding, as networks with more heterogeneity encode more information of image contrast.

319 We find that strong recurrent coupling among the excitatory and inhibitory neurons and distinct sources of
320 feedforward inputs are important for generating a wide range of heterogeneity of normalization strength. In
321 networks with weak recurrent coupling, the distribution of normalization indices is narrow and the spike count
322 correlations between neurons only weakly depend on their normalization strengths (Supp Fig S4). This suggests
323 that strong recurrent connections amplify the heterogeneity in neuron responses to multiple inputs. In networks
324 with strong recurrent coupling and disordered connections (i.e. no spatial or tuning dependence of connections),
325 neurons exhibit a range of normalization strengths when the network receives two sources of feedforward inputs
326 (Supp Fig S3). The distribution of normalization strengths broadens as the two sources of inputs target more
327 distinct populations of neurons. The range of normalization strengths is similar to that of the detailed circuit
328 model of visual cortex where the two images of orthogonal orientations activate largely non-overlapped groups
329 of neurons in the V4/MT network (Figure 1). Our results are consistent with a recent finding where models
330 with strong recurrent coupling explains the large distribution of rate changes in monkey visual cortex induced

331 by optogenetic stimulation (Sanzeni et al., 2023).

332 The balanced network model (Van Vreeswijk and Sompolinsky, 1996) has been successful at explaining the
333 genesis of neuronal variability and the close relationship of excitation and inhibition observed in experiments
334 in cortex (Haider et al., 2006; Okun and Lampl, 2008; Xue et al., 2014). However, balanced networks produce
335 a linear relationship between input and output rate, which has been considered as a limitation for complex com-
336 putation (van Vreeswijk and Sompolinsky, 1998). Recent theoretical work suggests that nonlinear computation
337 can be achieved in balanced networks when some neurons are silenced by excess inhibition, creating a local
338 imbalance in currents (Baker et al., 2020). They show that a network can produce sub-linear summation, if
339 individual stimulus silences a group of neurons when presented alone (Baker et al., 2020). Our finding is dif-
340 ferent from this work in that we analyzed neurons with positive rates in all three stimulus conditions (stimulus
341 1 alone, stimulus 2 alone or both). In other words, neurons in our model do not need to be silenced in one
342 stimulus condition to show sublinear summation. Consistent with the previous work, our results demonstrate
343 that individual neurons can exhibit diverse and nonlinear response functions to multiple stimuli, even though
344 the population averaged rate remains mostly linear (Figure 4A1-4).

345 Even though the normalization phenomena has been widely observed in visual cortex, as well as in other brain
346 regions, the source of normalization has been under debate. It was initially hypothesized that the divisive form
347 of normalization can be implemented by shunting inhibition (Carandini et al., 1997). However, it has been
348 shown that shunting inhibition alone results in a subtractive, not divisive, modulation of firing rates (Chance
349 et al., 2002). Instead, divisive gain modulation can be achieved by modulating both excitatory and inhibitory
350 inputs in a balanced manner (Chance et al., 2002). Later experimental findings suggest that it is the excitation,
351 rather than inhibition, that underlies the sublinear responses of neurons since both excitation and inhibition are
352 suppressed with an addition of non-preferred stimulus (Sato et al., 2016). Recent experiments suggest that a
353 feedforward mechanism is sufficient to account for the sublinear responses of neurons in primary visual cortex
354 without invoking a recurrent mechanism (Barbera et al., 2022; Priebe and Ferster, 2006), though mechanisms
355 for higher-order visual areas are not studied. In our model, we find that the normalization strength of a neuron is
356 highly anti-correlated with the inhibitory current it receives, and is only weakly correlated with the feedforward
357 and recurrent excitatory currents (Figure 3A-C). Moreover, the covariance with the inhibitory current also ex-
358 plains the relationship between spike count correlation and normalization. Neurons with stronger normalization
359 receive relatively more inhibitory currents, which cancel out more correlation in their currents, making those
360 neurons less correlated with other neurons. Our results are consistent with previous theoretical work which sug-
361 gests that the population firing rate patterns in cortical circuits are primarily determined by inhibitory currents
362 (Mongillo et al., 2018). Together, our results emphasize the role of inhibition in determining the normalization
363 strength and neuronal correlations.

364 Numerous experimental work has demonstrated that the neural mechanisms of normalization and selective
365 attention are closely related (Carandini and Heeger, 2012; Ni et al., 2012; Reynolds and Heeger, 2009; Reynolds
366 et al., 1999; Treue and Maunsell, 1996). In particular, the neuronal heterogeneity of attentional modulation in
367 firing rates is highly correlated with the neuronal heterogeneity of normalization, meaning that neurons that
368 demonstrate stronger normalization are also more modulated by attention (Lee and Maunsell, 2009; Ni et al.,
369 2012). In addition, the spike count correlations among neurons with stronger normalization are also more
370 modulated by attention (Verhoef and Maunsell, 2017). Both experimental and modeling work suggests that
371 inhibitory neurons are more targeted by attention than excitatory neurons, which could stabilize population
372 dynamics and reduce neural correlations (Huang et al., 2019; Kanashiro et al., 2017; Mitchell et al., 2007;

373 Thiele et al., 2016). Our finding of the strong correlation between normalization strength and inhibitory current
374 (Figure 3C) suggests that inhibition may be the unifying mechanism that relates the neuronal heterogeneity of
375 normalization and attentional modulation. Future extension of our model is needed to explore the interplay
376 between normalization and attention mechanisms in enhancing the neural representation of attended stimuli.

377 Several network models have been proposed to explain the normalization mechanism (Heeger and Zemlianova,
378 2020; Rubin et al., 2015; Somers et al., 1998). One of them, the stabilized supralinear network (SSN) model
379 (Hennequin et al., 2018; Rubin et al., 2015), is closely related to our model. The SSN model also has strong
380 recurrent excitation which is stabilized by inhibitory feedback and the recurrent connections depend on tuning
381 similarity. The SSN model reproduces the sublinear summation of neuronal responses to two stimuli and the
382 quenching of neuronal variability by stimulus contrast. The key differences between our model and the SSN
383 model are that our model consists of spiking neurons instead of rate units and that the population rate of our
384 model do not show strong saturation as input strength increases. Nevertheless, both our model and the SSN
385 model may share common mechanisms for generating heterogeneous normalization strength. For comparison,
386 we implemented the two-dimensional version of the SSN model with probabilistic connections to introduce
387 heterogeneity (Supp Fig S8; Rubin et al. (2015)). We found that the normalization index of a neuron strongly
388 depended on the neuron's preferred orientation in the SSN model, which was not observed in our experimental
389 data and the spiking network model (compare Supp Fig S8B with Supp Fig S2). There was a similar relationship
390 between spike count correlations and normalization indices in the SSN model, however, the relationship was
391 absent after we matched for the distribution of tuning preferences across normalization indices (Supp Fig S8C).

392 Past work has proposed several computational benefits of normalization (summarized in review Carandini and
393 Heeger (2012)). For example, by adapting neurons' response range based on background input, neurons can
394 remain sensitive to small changes in stimulus. This is most evident for retinal neurons which need to respond to
395 light intensities over a range of several orders of magnitude (Rieke and Rudd, 2009). In visual cortex, it has been
396 shown that divisive normalization can reduce the statistical redundancy present in natural images (Schwartz and
397 Simoncelli, 2001). Divisive normalization can also implement marginalization in the framework of probabilistic
398 population code (Beck et al., 2011). Complementary to these works, our results reveal additional benefits of
399 normalization, that is, neurons with stronger normalization encode more stimulus information per spike (Figure
400 5).

401 In addition, we demonstrate that the neuronal heterogeneity of normalization contributes to coding. Past works
402 have shown that cellular heterogeneity, such as in spiking threshold or excitability, can increase network re-
403 sponsiveness (Di Volo and Destexhe, 2021), improve network resilience to changes in modulatory inputs (Hutt
404 et al., 2023) and enhance the mutual information between stimulus and neural responses (Kastner et al., 2015;
405 Sharpee, 2017). Heterogeneity in neuronal time scales can also improve learning in tasks with rich intrinsic
406 temporal structure (Perez-Nieves et al., 2021). Our work is different from these works in that our model neu-
407 rons are homogeneous in terms of their cellular properties, and the heterogeneity in their response properties
408 is generated by network interactions. The heterogeneous normalization strength allows the neural population
409 to encode different contrast combinations of the two images (Figure 4). In networks with less heterogeneity
410 of normalization, more neurons are needed to encode the same amount of information (Figure 6B). Therefore,
411 neuronal heterogeneity in normalization improves the efficiency of information coding. Interestingly, we find
412 that heterogeneity has a larger impact on the information of image contrast than on the information of orien-
413 tation. Future work is needed to investigate how neuronal heterogeneity impacts population representational
414 geometry of multiple stimulus features in circuit models.

415 **Methods**

416 **Spiking neuron network model of visual cortex**

417 The model consists of two layers of spiking neurons, modeling the primary visual cortex (V1) and a higher-
 418 order visual area (V4 or MT), respectively (Figure 1A). Neurons from the two layers are arranged on a uniform
 419 grid covering a rectangle of size $\Gamma = [0, 2] \times [0, 1]$. There are 5,000 excitatory neurons in the V1 layer, 20,000
 420 excitatory neurons and 5,000 inhibitory neurons in the V4/MT layer.

421 **V1 model neurons** V1 neurons are modeled as linear-nonlinear Poisson spiking neurons, following previous
 422 models (Huang et al., 2022; Kanitscheider et al., 2015). V1 neurons are divided into two populations, V1₁ and
 423 V1₂, each of which has a non-overlapping receptive field centering on each Gabor image, respectively. Neurons
 424 located at the left half of the rectangle Γ ($[0, 1] \times [0, 1]$) have receptive fields centered at and with the same size
 425 as image 1, while those located at the right half of the rectangle ($[1, 2] \times [0, 1]$) have receptive fields centered
 426 at and with the same size as image 2. The receptive field of a neuron from population k ($k = 1, 2$) is modeled
 427 as a Gabor filter:

$$F_i^{(k)}(x, y) = \exp\left(-\frac{1}{2\sigma^2} \left((x - x_k)^2 + (y - y_k)^2\right)\right) \cos\left(\frac{2\pi}{\lambda} \left((x - x_k) \cos \theta_i + (y - y_k) \sin \theta_i\right)\right), \quad (3)$$

428 where the subscript i denotes the neuron's index, $\sigma = 0.2$ is the standard deviation of the Gaussian envelope,
 429 $\lambda = 0.6$ represents the wavelength of the sinusoidal factor, x and y are the coordinates of the neuron, (x_k, y_k) is
 430 the center of the receptive field ($(x_1, y_1) = (0.5, 0.5)$ for V1₁ neurons and $(x_2, y_2) = (1.5, 0.5)$ for V1₂ neurons)
 431 and θ_i is the preferred orientation of neuron i . The preferred orientation of each neuron was assigned according
 432 to a pinwheel orientation map generated with the method from Kaschube et al. (2010) (Supp Materials Eq. 20).
 433 The preferred orientation at (x, y) is $\theta_i(x, y) = \text{angle}(z(x, y))/(2\pi)$ and

$$z(x, y) = \sum_{j=0}^{n-1} \exp\left(i \frac{2\pi}{\Lambda} (l_j (\cos(j\pi/n)x + \sin(j\pi/n)y) + \phi_j)\right), n = 30$$

434 where $\Lambda = 0.125$ is the average column spacing, $l_j = \pm 1$ is a random binary vector and the phase ϕ_j is
 435 uniformly distributed in $[0, 2\pi]$.

436 Spike trains of V1 neurons are generated as inhomogeneous Poisson process with instantaneous rate

$$r_i(t) = \left[\iint F_i^{(k)}(x, y) \cdot \tilde{m}_k(x, y, t) dx dy \right]_+, \quad (4)$$

437 where $\tilde{m}_k(x, y, t)$ is the pixel value of image k ($k = 1, 2$) defined below (Eq. 6) and $[x]_+ = \begin{cases} x, & x \geq 0 \\ 0, & x < 0 \end{cases}$
 438 denotes half rectification. In the presence of image k , the average of rate of V1 _{k} neurons was 10 Hz. In the
 439 absence of image k , V1 _{k} neurons had a spontaneous rate of 5 Hz.

440 Two Gabor images of orthogonal orientations are presented to the V1 neurons, either individually or simulta-
 441 neously. Each image has 25×25 pixels and is defined as

$$m_k(x, y) = c_k \exp\left(-\frac{1}{2\sigma^2} \left((x - x_k)^2 + (y - y_k)^2\right)\right) \cos\left(\frac{2\pi}{\lambda} \left((x - x_k) \cos \theta_k + (y - y_k) \sin \theta_k\right)\right) \quad (5)$$

442 where c_k is the contrast of image k , and σ and λ are the same as the Gabor filters of the V1 neurons (Eq. 3).
 443 Each pixel is corrupted by independent additive noise as

$$\tilde{m}_k(x, y, t) = m_k(x, y) + \xi_k(x, y, t), \quad k = 1, 2, \quad (6)$$

444 where $\xi_k(x, y, t)$ is modeled as Ornstein-Uhlenbeck process

$$\tau_n d\xi_k = -\xi_k dt + \sigma_n dW \quad (7)$$

445 with $\tau_n = 40$ ms, $\sigma_n = 3.5$ and dW being a Wiener process.

446 **V4/MT model neurons** V4/MT layer is a recurrently coupled network of excitatory ($\alpha = e$) and inhibitory
 447 neurons. The neuronal and synaptic parameters are the same as in our previous model (Huang et al., 2019).
 448 The preferred orientation of each neuron was assigned with a separately generated orientation map using the
 449 same method as that of V1 neurons. Each neuron is modeled as an exponential integrate-and-fire (EIF) neuron
 450 whose membrane potential is described by:

$$C_m \frac{dV_j^\alpha}{dt} = -g_L(V_j^\alpha - E_L) + g_L \Delta_T e^{(V_j^\alpha - V_T)/\Delta_T} + I_j^\alpha(t). \quad (8)$$

451 A spike is generated each time $V_j^\alpha(t)$ exceeds a threshold, V_{th} . Then the neuron's membrane potential is held
 452 for a refractory period, τ_{ref} , after which it is reset to a fixed value V_{re} . Neuron parameters for excitatory neurons
 453 are $\tau_m = C_m/g_L = 15$ ms, $E_L = -60$ mV, $V_T = -50$ mV, $V_{th} = -10$ mV, $\Delta_T = 2$ mV, $V_{re} = -65$ mV and
 454 $\tau_{ref} = 1.5$ ms. Inhibitory neurons are the same except $\tau_m = 10$ ms, $\Delta_T = 0.5$ mV and $\tau_{ref} = 0.5$ ms. The total
 455 current to the j^{th} neuron is:

$$\frac{I_j^\alpha(t)}{C_m} = \sum_{k=1}^{N_F} \frac{J_{jk}^{\alpha F}}{\sqrt{N}} \sum_n \eta_F(t - t_n^{F,k}) + \sum_{\beta=e,i} \sum_{k=1}^{N_\beta} \frac{J_{jk}^{\alpha\beta}}{\sqrt{N}} \sum_n \eta_\beta(t - t_n^{\beta,k}) \quad (9)$$

456 where $N = N_e + N_i$ is the total number of the network population. The postsynaptic current is given by

$$\eta_\beta(t) = \frac{1}{\tau_{\beta d} - \tau_{\beta r}} \begin{cases} e^{-t/\tau_{\beta d}} - e^{-t/\tau_{\beta r}}, & t \geq 0 \\ 0, & t < 0 \end{cases} \quad (10)$$

457 where $\tau_{er} = 1$ ms, $\tau_{ed} = 5$ ms for excitatory synapses and $\tau_{ir} = 1$ ms, $\tau_{id} = 8$ ms for inhibitory synapses. The
 458 feedforward synapses from V1 neurons to V4/MT neurons have a fast and a slow component.

$$\eta_F(t) = p_f \eta_e(t) + p_s \eta_s(t) \quad (11)$$

459 with $p_f = 0.2$, $p_s = 0.8$. $\eta_s(t)$ has the same form as equation 10 with a rise time constant $\tau_r^s = 2$ ms and a decay
 460 time constant $\tau_d^s = 100$ ms.

461 **Network connections** There are two types of feedforward and recurrent excitatory connections projecting
 462 to the excitatory V4/MT neurons. 85% of connections are generated according to connection probability that
 463 depends only on the physical distance between neurons (Eq. 12). The remaining 15% of excitatory connections
 464 are randomly chosen from similarly tuned neurons and do not depend on space. The probability of inhibitory

465 projections and the projections to the inhibitory neurons only depends on distance (Eq. 12) and not on tuning
466 similarity.

467 The distance-dependent connections are sampled according to probability function, $p_{\alpha\beta}(\mathbf{x}_1, \mathbf{x}_2)$, between a
468 neuron from population β at location $\mathbf{x}_1 = (x_1, y_1)$ to a neuron from population α at location $\mathbf{x}_2 = (x_2, y_2)$,
469 $\alpha, \beta = \{e, i\}$.

$$p_{\alpha\beta}(\mathbf{x}_1, \mathbf{x}_2) = \bar{p}_{\alpha\beta} g(x_1 - x_2, y_1 - y_2; \sigma_\beta). \quad (12)$$

470 Here $\bar{p}_{\alpha\beta}$ is the mean connection probability and

$$g(x, y; \sigma) = \frac{1}{2\pi\sigma^2} \left(\sum_{k=-\infty}^{\infty} e^{-(x+2k)^2/(2\sigma^2)} \right) \left(\sum_{k=-\infty}^{\infty} e^{-(y+k)^2/(2\sigma^2)} \right), \quad (13)$$

471 is a wrapped Gaussian distribution periodic on the domain Γ . The excitatory and inhibitory recurrent connection
472 widths of the V4/MT layer were $\sigma_e = \sigma_i = 0.2$ and the feedforward connection width from the V1 layer to the
473 V4/MT layer was $\sigma_{\text{ffwd}} = 0.1$. A presynaptic neuron was allowed to make more than one synaptic connection
474 to a single postsynaptic neuron.

475 The long-range excitatory connections are sampled between similarly tuned neurons, i.e. $\cos(\theta_i - \theta_j) \geq 0.6$,
476 where θ_i and θ_j are the preferred orientations of neuron i and j .

477 The recurrent synaptic weights within the V4/MT layer were $J_{ee} = 80\text{mV}$, $J_{ei} = -240\text{mV}$, $J_{ie} = 40\text{mV}$
478 and $J_{ii} = -300\text{mV}$. Note that each synaptic weight was scaled by $1/\sqrt{N}$ (Eq. 9). The mean connection
479 probabilities were $\bar{p}_{ee} = 0.01$, $\bar{p}_{ei} = 0.04$, $\bar{p}_{ie} = 0.03$ and $\bar{p}_{ii} = 0.04$. The out-degrees were $K_{ee}^{\text{out}} = 200$,
480 $K_{ei}^{\text{out}} = 800$, $K_{ie}^{\text{out}} = 150$ and $K_{ii}^{\text{out}} = 200$. The feedforward connection strengths from V1 layer to V4/MT
481 layer were $J_{eF} = 160\text{mV}$ and $J_{iF} = 140\text{mV}$, with probabilities $\bar{p}_{eF} = 0.05$ and $\bar{p}_{iF} = 0.05$ (out-degrees
482 $K_{eF}^{\text{out}} = 1000$ and $K_{iF}^{\text{out}} = 250$).

483 **Network with matched in-degrees** In the network with matched-in-degrees (Figure 6), the number of presy-
484 naptic neurons (in-degrees) that project to each V4/MT neuron was matched to be the same across each popula-
485 tion for each type of connections (V4/MT excitatory, V4/MT inhibitory, or V1 excitatory), while the out-degrees
486 were allowed to vary. All other parameters including synaptic weights and connection probabilities were the
487 same as the default network.

488 **Simulation** All simulations were performed on the CNBC Cluster in the University of Pittsburgh. All simula-
489 tions were written in a combination of C and Matlab (Matlab R 2021b, Mathworks). The differential equations
490 of the neuron model were solved using forward Euler method with time step 0.05 ms.

491 Datasets and analysis

492 Neuronal activity was collected from four adult male rhesus monkeys (*Macaca mulatta*; monkeys BR, JD, ST,
493 SY) as they were passively fixating at superimposed orthogonal drifting gratings at a range of contrasts (details
494 are described in Ruff et al. (2016)). All animal procedures were approved by the Institutional Animal Care and
495 Use Committees of the University of Pittsburgh and Carnegie Mellon University.

496 MT data was collected with 24-channel V-Probes and 24-channel linear microarrays in area MT of two monkeys
497 (Figure 2B). There were a total of 2,133 visual stimulus trials for 769 units and 10,600 pairs from 28 recording

498 sessions. V4 data was collected with a pair of 6×8 microelectrode arrays implanted in area V4 of two monkeys
499 (Figure 2C). In one monkey, both arrays were in V4 in the right hemisphere. In the other monkey, arrays were
500 implanted bilaterally in area V4. There were a total of 2,160 visual stimulus trials for 1,276 units and 39,719
501 pairs from 21 recording sessions. V1 data was collected with a 10×10 microelectrode array implanted in area
502 V1 of two monkeys (Figure S5). There were a total of 1,467 visual stimulus trials for 2,124 units and 97,169
503 pairs from 23 recording sessions.

504 In our analysis, we included units if their response to 0% contrast stimuli was significantly different from the
505 average response to stimuli with at least 50% contrast (t -test, $P < 0.01$). Pairs of units that came from the
506 same electrode were excluded for correlation analysis. For each unit recorded in each stimulus condition, spike
507 counts were calculated from 30 to 230 ms for V1 units and from 50 to 250 ms for V4 and MT units after stimulus
508 onset, to allow for latency in response. Each stimulus was presented for 200 ms. We quantified spike count
509 correlations as the Pearson's correlation coefficient between spike count responses to repeated presentations of
510 the same stimulus. This measure is extremely sensitive to outliers, so we did not analyze trials for which the
511 response of either unit was more than three standard deviations away from its mean (following the convention
512 of Kohn and Smith (2005)).

513 To compute the normalization index of recorded units, we included the mean spike counts in response to
514 stimulus conditions where the contrast of one stimulus was 50% and the other was 0%, and where the contrast
515 of both stimuli were 50%. The normalization index was computed using Equation 14 for each combination
516 of orthogonal drifting gratings and then averaged across all combinations within a session. To compute the
517 selectivity of recorded units, we included the mean spike counts in response to stimulus conditions where the
518 contrast of one stimulus was 50% and the other was 0%. Tuning similarity was quantified as the Pearson's
519 correlation coefficient between mean spike count responses to each stimulus direction presented alone, with
520 50% contrast and the contrast of the other direction equal to 0%. The spike count correlation of a pair of units
521 in one session was averaged across the stimulus conditions used to compute the normalization index. In Figure
522 2B, 2C, and S5, the spike count correlation was averaged across unit pairs from all recording sessions.

523 **Statistical methods**

524 **Normalization index** The normalization index of a neuron is defined as the sum of a neuron's firing rate to
525 each one of the two stimuli when presented alone divided by its firing rate when both stimuli are presented
526 together (Ruff et al., 2016):

$$\text{norm index} = (\text{FR}_{\text{stim1}} + \text{FR}_{\text{stim2}}) / \text{FR}_{\text{both}}. \quad (14)$$

527 A normalization larger than 1 indicates sublinear summation.

528 The current normalization index is defined similarly:

$$\text{current norm index} = (I_{\text{stim1}} + I_{\text{stim2}}) / I_{\text{both}}, \quad (15)$$

529 where I is the average recurrent excitatory, recurrent inhibitory or feedforward excitatory current a neuron
530 receives.

531 **Spike count correlation and current covariance** We computed the spike count correlation of V4/MT model
532 neurons when both images of orthogonal orientations were presented together. Spike counts were computed

533 using a sliding window of 200 ms with 50 ms step size and the Pearson correlation coefficients were computed
 534 between pairs of neurons. In Figure 2A, there were 10 simulations and each simulation was 20 seconds long.
 535 The first 1 second of each simulation was excluded from the correlation analysis to avoid transient effects.
 536 Neurons whose average firing rates were within one standard deviation from the mean population rates in all of
 537 the three stimulus conditions (image 1 alone, image 2 alone, or both images presented together) were included.
 538 In total, 8663 excitatory V4/MT neurons were sampled to compute spike count correlations.

539 To compute current covariance (Figure 3D,E), each type of synaptic currents (feedforward excitation, recurrent
 540 excitation and recurrent inhibition) to each neuron were recorded every 10 ms. The excitatory current combines
 541 both feedforward and recurrent excitation. In total, 4163 neurons were sampled to compute current covariance.
 542 The simulation was 20 seconds long.

543 **Tuning similarity** Tuning similarity between a pair of neurons is defined as the Pearson correlation between
 544 their tuning curves of orientation:

$$\text{tuning similarity} = \text{corr}, (f_i(\theta), f_j(\theta)) \quad (16)$$

545 where f_i and f_j are neuron i and neuron j 's tuning curves, respectively. Tuning curves were computed using
 546 one image.

547 **Selectivity** Selectivity measures how selective a neuron is to stimulus 1 compared to stimulus 2.

$$\text{selectivity} = \frac{\text{FR}_{\text{stim1}} - \text{FR}_{\text{stim2}}}{\text{FR}_{\text{stim1}} + \text{FR}_{\text{stim2}}}. \quad (17)$$

548 Selectivity takes a value between -1 and 1 . The larger the absolute value of selectivity is, the more selective the
 549 neuron is to its preferred stimulus. A selectivity equaling 0 means there is no preference of the neuron between
 550 the two stimuli.

551 **Linear Fisher information** To compute the linear Fisher information, stimulus 2 was presented during 200
 552 ms intervals (ON) interleaved with 300 ms OFF intervals, during which the spike trains of V1₂ neurons were
 553 independent Poisson process with rate 5 Hz. Meanwhile stimulus 1 was present throughout a simulation.
 554 Spike counts of V4/MT excitatory neurons during the ON intervals were used to compute the linear Fisher
 555 information. Each simulation was 20 seconds long. The first spike count in each simulation was excluded. The
 556 connectivity matrices were fixed for all simulations and the initial state of each neuron's membrane potential
 557 was randomized in each simulation.

558 For the linear Fisher information of contrast, the contrast of stimulus 2 during ON intervals was randomly
 559 chosen from $c_1 = c + \delta c/2$ and $c_2 = c - \delta c/2$, where $c = 0.5$ and $\delta c = 0.01$. For the linear Fisher information
 560 of orientation, the orientation of stimulus 2 during ON intervals was randomly chosen from $\theta_1 = \theta + \delta\theta/2$ and
 561 $\theta_2 = \theta - \delta\theta/2$, where $\theta = 0.5\pi$ rad and $\delta\theta = 0.02$ rad. The linear Fisher information of V4/MT neurons was
 562 computed using a bias-corrected estimate (Kanitscheider et al. (2015))

$$\hat{I}_{bc} = \frac{(\mathbf{f}_2 - \mathbf{f}_1)^\top}{\delta x} \left(\frac{Q_1 + Q_2}{2} \right)^{-1} \frac{(\mathbf{f}_2 - \mathbf{f}_1)}{\delta x} \frac{2N_{\text{tr}} - N - 3}{2N_{\text{tr}} - 2} - \frac{2N}{N_{\text{tr}}\delta x^2}, \quad (18)$$

563 where $\delta x = \delta c$ or $\delta \theta$, \mathbf{f}_i and Q_i are the empirical mean and covariance, respectively, for c_i or θ_i . N_{tr} is the
564 number of trials for each c_i or θ_i .

565 We used the fitting algorithm proposed by Kafashan et al. (2021) to estimate the asymptotic value of the linear
566 Fisher information, I_∞ , at the limit of $N \rightarrow \infty$, where N is the number of sampled neurons (Figure 6B,C).
567 Briefly, the theory of information-limiting correlations (Moreno-Bote et al. (2014)) shows that the linear Fisher
568 information, I_N , in a population of N neurons can be decomposed into a limiting component, I_∞ , and a
569 nonlimiting component $I_0(N)$,

$$I_N = \frac{1}{\frac{1}{I_0} + \frac{1}{I_\infty}}, \quad (19)$$

570 where we assume that the nonlimiting component increases linearly with N , i.e., $I_0 = aN$. Hence, Equation
571 19 can be rewritten as

$$1/I_N = (1/a)(1/N) + 1/I_\infty, \quad (20)$$

572 which shows that $1/I_N$ scales linearly with $1/N$ with $1/I_\infty$ as the intercept. Hence, we do a linear fit of $1/I_N$
573 versus $1/N$, with N varying from 8 to 12000 and estimate $1/I_\infty$.

The linear Fisher information from V1 neurons can be estimated analytically as ((Kanitscheider et al., 2015),

$$I_F^{\text{in}}(s) = \frac{\partial f^\top}{\partial s} \Sigma^{-1}(s) \frac{\partial f}{\partial s},$$

where $s = c$ or θ , with

$$\frac{\partial f}{\partial s} = T F_i \cdot \frac{\partial m(c, \theta)}{\partial s},$$

$$\Sigma_{ij}(s) = F_i \cdot F_j \text{Var}(\xi^T) + \delta_{ij} T F_i \cdot m(c, \theta),$$

574 where $\xi^T(t) = \int_t^{t+T} \xi(u) du$, T is the time window for spike counts, and δ_{ij} is a Kronecker delta, which is
575 1 if $i = j$, and 0 otherwise. We can calculate the variance of the integrated noise over time window T as
576 $\text{Var}(\xi^T) = \sigma_n^2 [T - \tau_n(1 - \exp(-T/\tau_n))]$.

577 In Figure 5, a number of neurons were randomly sampled from the model V4/MT excitatory neurons whose
578 normalization indices were within a specified range. The number of sampled neurons, N , was logarithmically
579 spaced between 1 and 8103. For $N < 545$ neurons, the number of samplings for each N decreased from 200 to
580 14 proportionally with $\log(N)$, rounded to the nearest integer. For $N \geq 545$ neurons, there were 5 samplings
581 for each N . The linear Fisher information of the sampled group of neurons was divided by the average number
582 of spikes from the sampled group of neurons during the time window used for calculating the Fisher information
583 ($T = 200$ ms). In Figure 6B,C, the number of neurons were $N = 8, 16, 31, 62, 125, 250, 500, 1000, 2000,$
584 $4000, 8000, 12000$. There were 20 samples of neurons for each N . Neurons with firing rates less than 1 Hz
585 were excluded. There were 304,000 spike counts in total for c_1 and c_2 , or θ_1 and θ_2 conditions.

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590 **Author Contributions**

591 D.S. and C.H. conceived the project; D.S. performed the simulations and analysis, in consultation with C.H.
592 and M.C.; D.R. and M.C. provided the experimental data; C.H. supervised the project; all authors contributed
593 to writing the manuscript.

594 **Data and Software Availability**

595 Computer code for all simulations and data analysis will be available online upon publication.

596 **Declaration of Interests**

597 The authors declare no competing interests.

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759 **Supplementary Information**

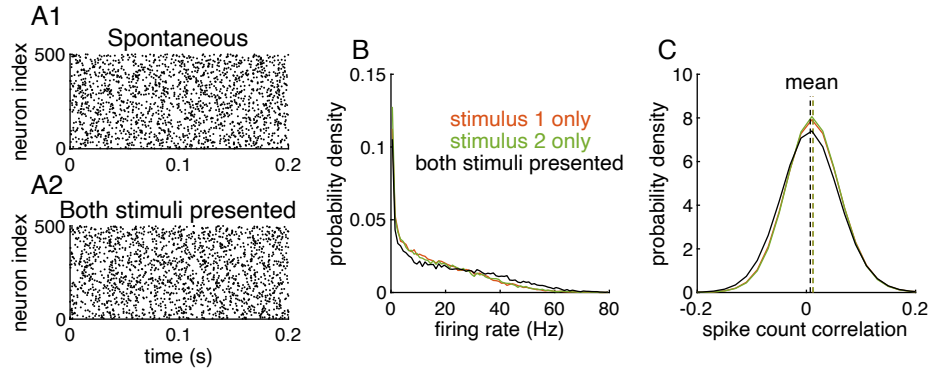


Figure S1: Related to Figure 1. The V4/MT network activity is stable and asynchronous in both spontaneous and evoked states.

(A1) Spike raster of V4/MT neurons when both $V1_1$ and $V1_2$ neurons have homogeneous rates of 10 Hz. 500 neurons were randomly sampled from the V4/MT population. (A2) Spike raster of V4/MT neurons when two images are simultaneously presented. (B) The firing rate distributions of V4/MT neurons when only stimulus 1 (red), only stimulus 2 (green) or both stimuli are presented (black). (C) The distributions of spike count correlations of V4/MT neuron pairs from the three stimulus conditions. Dashed lines indicate the average spike count correlations (0.012 when only stimulus 1 is presented, 0.012 when only stimulus 2 is presented, 0.007 when both stimuli are presented).

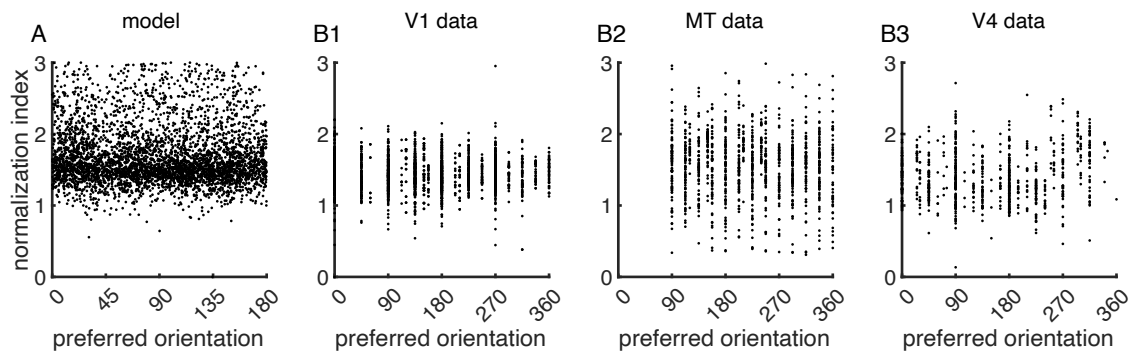


Figure S2: **Related to Figure 2. The normalization index of a neuron is independent from its tuning preference in both the model and data.**

(A) The normalization index and the tuning preference of model V4/MT neurons are statistically independent. We use permutation test to assess the statistical significance of the null hypothesis that the normalization index and tuning preference are independent. First, we calculate the mutual information between the normalization index and tuning preference of V4/MT neurons. Then, we shuffle the normalization index of neurons 2000 times and recalculate the mutual information for each permutation. Lastly, we compute the p-value as the proportion of permutations with higher mutual information than that of the original observation. There is no significant dependence between the normalization index and the tuning preference of model V4/MT neurons ($p = 0.31$). (B) The normalization index and the tuning preference of experimentally recorded neurons are statistically independent in V1 area (B1, $p > 0.05$ for all 23 recording sessions), MT area (B2, $p > 0.05$ for 21 out of 28 recording sessions), and V4 area (B3, $p > 0.05$ for 14 out of 21 recording sessions).

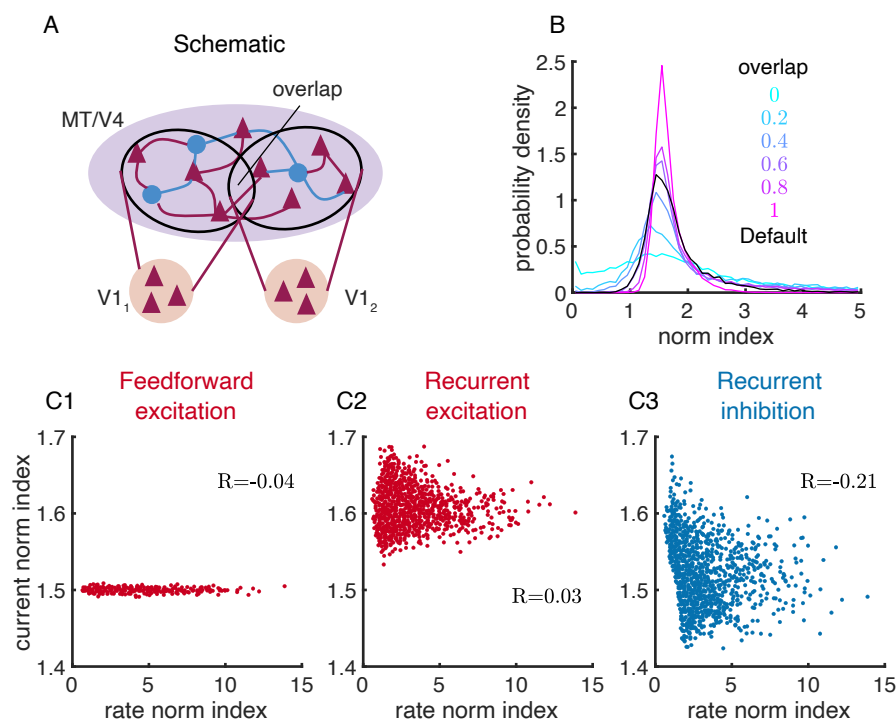


Figure S3: Related to Figures 1 and 3. Neurons exhibit a range of normalization strength in networks with strong recurrent coupling and disordered connections.

(A) The schematic of the disordered network. The excitatory and inhibitory connections within V4/MT layer are random and with the same connection probability as those of the default model with spatial structure. The two V1 populations project randomly to the excitatory and inhibitory neurons in the V4/MT layer with the same connection probabilities as those in the default model. A fraction, α , of neurons in the V4/MT layer can receive input from both V1 populations, which represents the overlap of the feedforward projections from V1₁ and V1₂. The spike trains of V1 neurons are independent Poisson processes with fixed rates. In Stimulus 1 alone condition, V1₁ neurons have firing rate of 10Hz and V1₂ neurons have rate 5Hz. In Stimulus 2 alone condition, V1₁ neurons have firing rate of 5Hz and V1₂ neurons have rate of 10Hz. When both stimuli are presented, both V1₁ and V1₂ neurons fire at 10 Hz. (B) The distribution of normalization indexes is broader in networks with smaller overlap, α . The distribution of normalization indexes from the default network (black; same as that in Figure 1C) is similar to that of the random network model with $\alpha = 0.6$. The normalization index of neurons in the random network model is calculated in the same way as in the default model, i.e. $\text{norm index} = (\text{FR}_{\text{stim1}} + \text{FR}_{\text{stim2}}) / \text{FR}_{\text{both}}$. (C) Relationship between current and rate normalization indexes in a random network model with $\alpha = 0.6$. Only the normalization index of recurrent inhibitory current has a strong correlation with that of the firing rate. The range of the normalization index of feedforward excitatory current is very small in the random network model, since there is no spatial or tuning dependent connections.

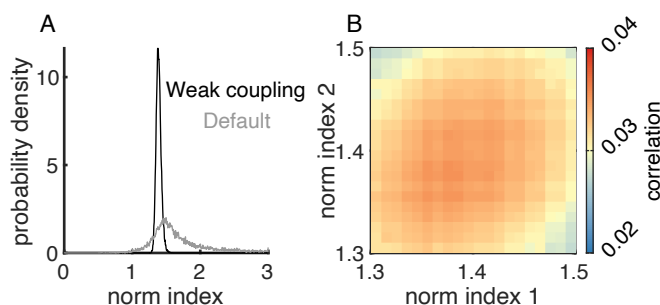


Figure S4: Related to Figures 1 and 2. Networks with weak recurrent coupling produce homogeneous normalization strength and weak dependence of spike count correlations on normalization.

(A) The distribution of normalization indexes is much narrower in a network with weak recurrent coupling (black) compared to that in the default network (gray). The gray curve is the same as in Figure 1C but with different scale of the y-axis. (B) The dependence of spike count correlations on normalization index was weaker in the network with weak recurrent coupling. The range of spike count correlations between pairs of model V4/MT neurons was 0.008 in the network with weak recurrent coupling, compared to a range of 0.02 in the default network (Figure 2A1). In the network with weak recurrent coupling, the strengths of all recurrent connections were decreased to 10% of those in the default network. Independent white noise currents with mean 0 and standard deviation 6.8 mV/ms were applied to every excitatory and inhibitory V4/MT neuron such that the neurons' f-I curve was the same as that in the default network. The strengths of feedforward projections were scaled down by a factor of 2.9 to keep the mean firing rate of V4/MT neurons the same as that in the default network. The default network was the same as that used in Figures 1 and 2.

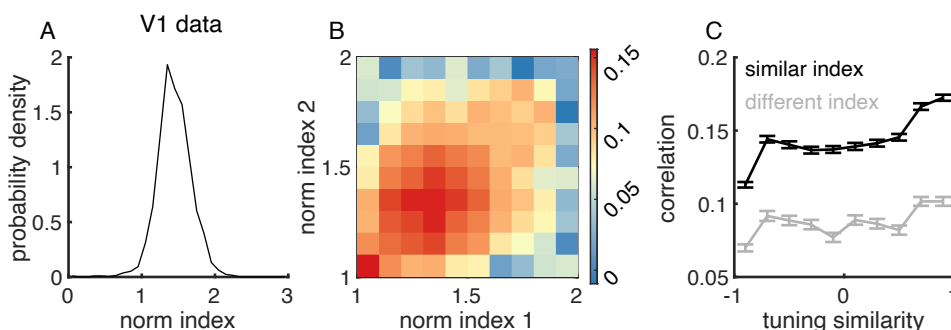


Figure S5: Related to Figure 1 and 2. Heterogeneity of normalization index and normalization-related modulation of spike count correlations are also observed in experimental data recorded from V1 area.

(A) The recorded V1 neurons exhibit a similar range of normalization indexes as V4 and MT neurons (Figure 1D). (B) Spike count correlations between recorded V1 neurons depend on their normalization indexes. Same format as Figure 2A1,B1,C1). (C) Across all levels of tuning similarity, the spike count correlations between recorded V1 neurons with similar normalization indexes are consistently larger than those of neurons with distinct normalization indexes. Same format as Figure 2A4,B4,C4). Data from Ruff et al., 2016.

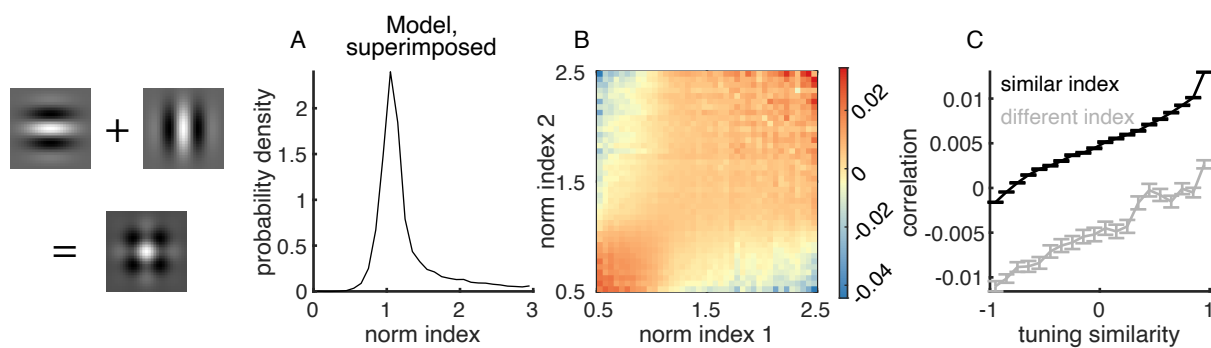


Figure S6: Related to Figures 1 and 2. Heterogeneity in normalization index and normalization-related modulation of spike count correlations in the model in response to two superimposed Gabor images.

(A) Distribution of normalization indexes (Eq. 14 where FR_{both} was the firing rate when two superimposed Gabor images were presented). (B) Spike count correlations as a function of the normalization indexes of the two neurons in the pair. (C) Neurons with similar normalization indexes have higher noise correlations than those with different normalization indexes. This relationship is consistent across neuron pairs with various tuning similarities. Model results with superimposed Gabor images are qualitatively the same as those with two separate Gabor images (Figures 1C, 2A1,A4).

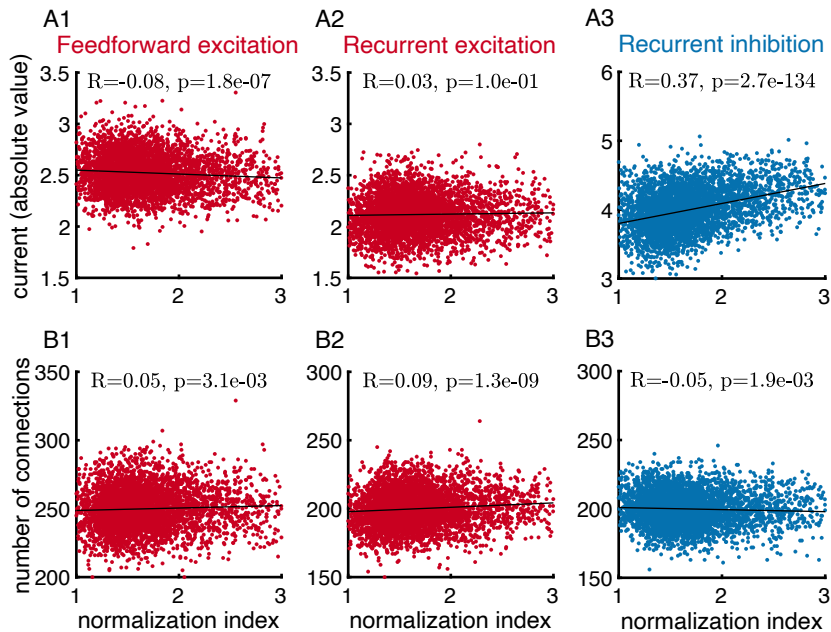


Figure S7: **Related to Figure 3. The normalization index of neurons is strongly correlated with the magnitude of the mean recurrent inhibitory current.**

(A) There is a strong correlation between the firing rate normalization indexes and the average inhibitory current a neuron receives when two images are presented (A3), and only weak correlations with the feedforward (A1) and recurrent (A2) excitatory currents. (B) The correlation between normalization and the number of excitatory or inhibitory input connections is weak.

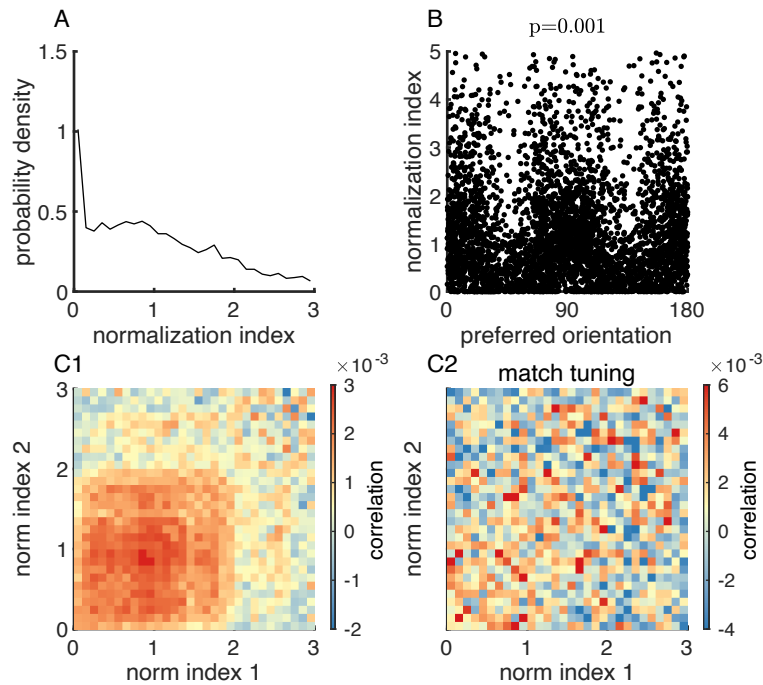


Figure S8: The normalization index of a neuron strongly depends on the neuron’s preferred orientation in the stabilized supralinear network (SSN) model.

The SSN model is a large-scale, probabilistically connected, 2D model of a visual area. E/I units are arranged on a grid of 75×75 . Preferred orientations are assigned according to a superposed orientation map. Parameters of the model are the same as those used in Figure 6 of Rubin et al., 2015. Additionally, we apply globally correlated additive noise to each unit, ξ_i , where ξ_i satisfies $\tau_n d\xi_i = -\xi_i dt + \sigma_n (\sqrt{c} dW_0 + \sqrt{1-c} dW_i)$, with dW_0 and dW_i being Wiener process, $\tau_n = 40$ ms, $\sigma_n = 3.5$, and correlation $c = 0.2$. **(A)** The normalization index of model neurons is broadly distributed in the SSN model. **(B)** The normalization index and the tuning preference of model SSN neurons are statistically dependent ($p = 0.001$). **(C1)** Spike count correlations between a pair of neurons as a function of the normalization indexes of the pair. **(C2)** The dependence of spike count correlation on normalization indexes is absent after matching for the distribution of tuning preferences of neurons across normalization indexes **(C2)**.