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Establishment of a robust single axis of cell polarity by coupling multiple positive feedback loops

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Establishment of cell polarity—or symmetry breaking—relies on local accumulation of polarity regulators. Although simple positive feedback is sufficient to drive symmetry breaking, it is highly sensitive to stochastic fluctuations typical for living cells. Here, by integrating mathematical modelling with quantitative experimental validations, we show that in the yeast *Saccharomyces cerevisiae* a combination of actin- and guanine nucleotide dissociation inhibitor-dependent recycling of the central polarity regulator Cdc42 is needed to establish robust cell polarity at a single site during yeast budding. The guanine nucleotide dissociation inhibitor pathway consistently generates a single-polarization site, but requires Cdc42 to cycle rapidly between its active and inactive form, and is therefore sensitive to perturbations of the GTPase cycle. Conversely, actin-mediated recycling of Cdc42 induces robust symmetry breaking but cannot restrict polarization to a single site. Our results demonstrate how cells optimize symmetry breaking through coupling between multiple feedback loops.

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he Rho-type GTPase Cdc42 is a central regulator of cell polarity in animal and fungal cells^{1,2}. At the G1-S transition in the cell cycle of Saccharomyces cerevisiae, Cdc42 becomes concentrated in a cortical cap that defines the future bud site^{3,4}. Cdc42 binds to various effectors that control essential morphogenetic processes, such as polarized membrane transport⁵, assembly of a septin ring⁶ and fusion of exocytic vesicles with the plasma membrane^{7,8}. To fulfill its functions, Cdc42 must constantly cycle between GTP-bound/active and GDP-bound/inactive states. In budding yeast activation of Cdc42 is controlled by a single guanine nucleotide exchange factor (GEF), Cdc24 and Cdc42 hydrolytic activity is promoted by four GTPase-activating proteins (GAPs), Bem2, Bem3, Rga1 and Rga2 (ref. 7). In addition, Cdc42 is extracted from membranes by a single Rho-guanine nucleotide dissociation inhibitor (GDI), Rdi1 (refs 9,10).

Concentration of Cdc42 at the polarization site in yeast cells can occur via feedback amplification of stochastic fluctuations^{11,12} and either requires focused, actin-mediated transport of vesicle-bound Cdc42 (refs 13,14) or Bem1-mediated recruitment of soluble Cdc42 (refs 14–17). Both pathways drive polarization through constant recycling of Cdc42 (refs 14,17).

Polarized transport of Cdc42-bearing vesicles has been shown to underlie spontaneous polarization of constitutively active and membrane-restricted Cdc42 via a simple positive feedback mechanism¹³. In addition, polarization of wild-type Cdc42 depends on actin-based secretion, particularly in the absence of Bem1 (ref. 14) or Rdi1 (ref. 17). However, although a role for membrane transport in polarity establishment has been widely established^{18,19}, its relevance for polarization of wild-type yeast cells is still controversial^{11,16,20–22}. A negative role for actin in cell polarization has even been proposed based on endocytosis of polarity regulators^{20,23} or dilution of Cdc42 in the cap region^{24,25}. Although such mechanisms provide explanations for travelling waves²³ or oscillating polarization patches²⁴, they cannot account for the positive role of actin during the actual process of symmetry breaking—both in the presence and absence of Bem1-driven feedback^{13,14}.

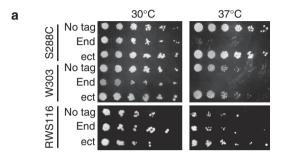
A second polarization mechanism has been proposed to rely on activation of Cdc42 through a Bem1-Cdc24-Cla4 complex 15,16,26,27 and on extraction of Cdc42 from membranes by Rdi1 (ref. 17). The available experimental evidence has been combined in a Turing-type model of yeast polarization 18. However, many details of the proposed reactions remain under debate 12,21,29. Moreover, the precise relationship between actinand GDI-dependent mechanisms during establishment of polarization in wild-type cells is unclear.

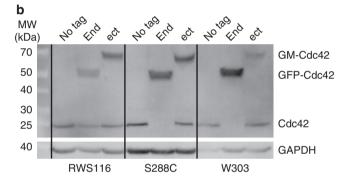
Here, we built a stochastic model for yeast polarity establishment through actin- and GDI-mediated recycling of Cdc42. We established assumptions and parameter values for this model through genetic analyses, *in vitro* reconstitution and live cell imaging. Predictions from the model were tested and validated experimentally. We demonstrate that the establishment of a stable and unique polarization axis requires coordination of two pathways. Actin-mediated recycling of Cdc42 is very robust, but does not reliably result in formation of a single-polarization site. In contrast, GDI-dependent recycling is sensitive to changes in the GTPase cycle of Cdc42 but faithfully generates a unique polarization site. Our results suggest that correct polarity establishment is achieved through coupling of multiple feedback loops.

Results

Validation of strains. To build a mechanistic model for yeast polarity establishment we sought to firmly establish the connections between all involved regulators and pathways. Spontaneous cell polarization has been proposed to occur via amplification of stochastic fluctuations through simple positive feedback in the presence of low concentrations of reacting molecules^{30,31} but this model has been recently challenged²⁴. In an attempt to resolve this issue we varied expression levels of GFP-Cdc42 in control and LatB-treated cells with an inducible GAL promoter³⁰. We indeed found that Cdc42 expression level had no effect on polarization efficiency (Supplementary Fig. S1a).

When we tagged the genomic copy of Cdc42 in haploid cells of S288C and W303 backgrounds we confirmed²⁴ that expression of





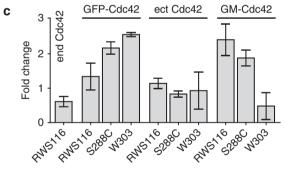


Figure 1 | Effects of GFP-tagging of Cdc42 on cell growth and polarization. (a) Growth of the standard lab strains S288C and W303 and the arrest-strain RWS116 at different temperatures. Shown are the respective control strains (no tag) and strains where Cdc42 has been tagged at its endogenous locus (end) or as additional copy integrated in the ectopic LEU2 locus (ect). (b) Western blot of different Cdc42 fusion proteins in the strains used in (a). Cdc42 was detected with a polyclonal serum against Cdc42. A monoclonal antibody against the constitutively expressed glyceraldehyde-2-phosphate dehydrogenase (GAPDH) was used as loading control. Identity of visualized bands is indicated on the right. (c) Quantification of Cdc42 expression levels showing fold change compared with expression of the endogenous copy in the respective strain background. Bars correspond to mean ± s.d. from three independent experiments. Labels correspond to untagged Cdc42 in strains expressing GFP-Cdc42 at the endogenous locus (end Cdc42) or the LEU2 locus (ect Cdc42), to GFP tagged Cdc42 at the endogenous locus (GFP-Cdc42) and GFP-myc tagged Cdc42 at the LEU2 locus (GM-Cdc42). Strain backgrounds are indicated on x axis.

GFP-Cdc42 as the only source of Cdc42 leads to impaired growth of yeast cells at high temperatures (Fig. 1a). We also tagged Cdc42 in the strain RWS116, which could be arrested in the cell cycle through depletion of the G1 cyclins¹⁴. The resulting strain retained a duplicated version of the untagged Cdc42 expressed to half the level of the GFP-Cdc42 fusion (Fig. 1b,c). This strain as well as strains expressing GFP-myc-Cdc42 from ectopic chromosomal loci (Fig. 1b,c, Supplementary Fig. S1b) exhibited no temperature sensitivity (Fig. 1a). Tagging also did not affect growth and polarization kinetics, either in the presence or absence of actin-dependent transport (Supplementary Fig. S1c-f).

Parallel Cdc42 recycling pathways in polarity establishment. Overexpressed Cdc42 might be buffered by its GDI, which is generally found in a 1:1 complex with its substrates in the cytosol³². Actin and Rdi1 have been proposed to act in parallel during polarity maintenance¹⁷. To systematically investigate the connection between Rdi1- and actin-mediated recycling of Cdc42, we analysed genetic interactions of Cdc42 and its regulators with synthetic genetic arrays³³. Genetic lesions in all examined components had a negative impact on processes linked to actin functions (Fig. 2a, Supplementary Table S1). In contrast, few physical interactions of Cdc42 regulators with actin-associated

proteins have been reported (Fig. 2a, Supplementary Table S2). These results indicate that, in addition to the role of Cdc42 in formation and polarization of actin structures, Cdc42 signalling and actin-mediated transport processes also act in parallel during essential cellular processes.

Rdi1 exhibited interactions with several components involved in endocytic recycling (Fig. 2a, Supplementary Table S1), consistent with a role in actin-independent recycling of Cdc42 during polarity establishment. To test this, we studied synchronized yeast cells expressing GFP-Cdc42 fusions (Supplementary Fig. S1b-d), and monitored Cdc42 cap formation¹⁴. As expected from a defect in extraction of membrane-bound Cdc42, \(\Delta rdi1 \) cells accumulated Cdc42 on membranes (Fig. 2b). Nevertheless, polarization kinetics were unaffected in \(\Delta rdi1 \) cells and in cells expressing Cdc42 R66E, a mutant unable to interact with the GDI³⁴ (Fig. 2b). However, depolymerization of actin with latrunculin B (LatB), which has moderate effects on control cells¹⁴ (Fig. 2c), blocked polarization in $\Delta rdi1$ and Cdc42^{R66E}-expressing cells (Fig. 2c). A similar synergistic effect was observed when exocytosis was blocked using a temperature-sensitive allele of MYO2 (myo2-16, Fig. 2d). Reduction of endocytosis by deletion of the ESCRTIII component VPS27 (ref. 35) resulted in less efficient polarization of $\Delta rdi1$ cells (Fig. 2e). Colocalization of GFP-Cdc42 and FM4-64-stained endocytic membranes in Δvps27 cells revealed Cdc42

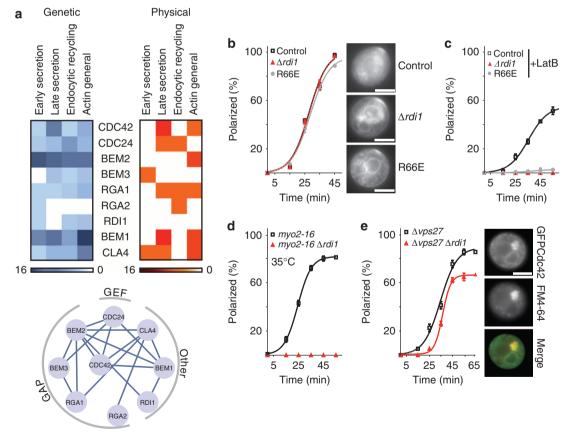


Figure 2 | Polarity establishment through GDI- and actin-mediated recycling of Cdc42. (a) Heat plots of genetic (blue) and physical (red) interactions between Cdc42 regulators and proteins involved in actin-related processes. Colour code: number of interactions. Genetic interactions among Cdc42 regulators are indicated in the lower panel. (**b-e**) Effects of genetic and pharmacological perturbations on polarization kinetics of Cdc42. Data points represent means of three experiments with n = 50 cells each. Error bars indicate mean ± s.d. Continuous lines are sigmoidal fits. Individual plots depict the effects of: (**b**) inhibiting extraction of Cdc42 from the plasma membrane in Δ*rdi*1 cells and cells expressing Cdc42^{R66E}, a mutant that cannot interact with the GDI; (**c**) disruption of actin polymerization (by LatB) in control, Δ*rdi*1 and cdc42^{R66E} cells; (**d**) inactivation of the temperature-sensitive myo2-16 allele in control and Δ*rdi*1 cells, and (**e**) deletion of *VPS2*7 in control and Δ*rdi*1 cells. Colocalization of Cdc42 and the membrane dye FM4-64 in aberrant endosomal compartments of Δ*vps2*7 cells is demonstrated in panel **e**. Scale bar, 4 μm.

accumulation in aberrant endocytic compartments, confirming passage of Cdc42 through the endocytic system (Fig. 2e).

Our results confirm that Rdi1- and actin-based cycling of Cdc42 contribute to polarity establishment via distinct and parallel mechanisms. We therefore proceeded to design a particle-based mathematical model of Cdc42 polarization to study the interplay between the two pathways.

A stochastic model for polarity establishment. To build an experimentally tractable model, we considered the two recycling pathways for Cdc42 separately. Recent studies have stressed the importance of considering individual vesicle carriers instead of simple protein flux^{21,25}. However, many mechanistic details of actin-based membrane recycling are unknown, rendering detailed models highly speculative. Importantly, the proposed dilution effect of vesicle delivery on the Cdc42 cap²¹ is not supported by our experiments, as Cdc42 cap intensities are significantly higher in control cells compared with cells, in which actin-mediated transport processes are disrupted (Fig. 3a). A recent study has also shown the feasibility of polarity establishment if Cdc42 exhibits non-uniform diffusion³⁶. We therefore opted to simulate actin-mediated recycling of Cdc42 using a coarse-grained approach (Fig. 3b, Supplementary Methods and Supplementary Tables S8, 9). We assumed that membrane-bound Cdc42 molecules are delivered to the plasma membrane from internal membranes along actin cables. Sites of enhanced cable nucleation are generated at a rate that depends on the amount of active Cdc42 at the respective nucleation site. Endocytosis was modelled with a constant extraction rate.

For Rdi1-mediated recycling (Fig. 3c) we assumed a well-mixed pool of Cdc42 in the cytosol and diffusion of Cdc42 in the plasma membrane with $D = 0.036 \, \mu \text{m}^2 \, \text{s}^{-1}$ (ref. 37). Nucleotide

exchange can occur spontaneously or catalysed by the GEF Cdc24 via a bounded positive feedback loop involving the Cdc42 effector Bem1 (refs 14,15). Such bounded feedback is essential to achieve realistic cap shapes (Fig. 4) and corresponds to depletion of limiting components involved in Cdc42 recruitment. GTP hydrolysis is modelled with a constant rate depending on GAP activity.

It has been shown that GDIs preferentially extract GDP-bound Rho GTPases^{38,39}. To firmly establish this important aspect in our model, we performed *in-vitro* extraction experiments with purified Cdc42 and RhoGDI³⁹. We found that the GDI indeed extracted GDP-bound Cdc42 around 10 times faster than GTP-Cdc42 (Fig. 3d). In the presence of catalytic amounts of GAP domain, GTP-Cdc42 was extracted at nearly the same rate as GDP-Cdc42 (Fig. 3d), indicating that GTP hydrolysis is ratelimiting for GDI-mediated Cdc42 extraction. This was supported by the extremely slow extraction of Cdc42 bound to non-hydrolyzable GTP analogue (GMPPNP, Fig. 3d). In living yeast cells, we confirmed previous reports^{14,17} that constitutively active Cdc42 (Cdc42^{G12V}) is restricted to membranes and the slow actin-mediated recycling pathway (Fig. 3e, Supplementary Table S9). Hence, we incorporated selective extraction of GDP-Cdc42 by the GDI into our model.

Recruitment from the Rdi1-GDP-Cdc42 pool to the membrane was assumed to occur at a background rate and via a second positive feedback loop that enhances attachment of cytosolic Cdc42 to sites of high Cdc42 activity. This feedback represents the previously proposed competition between Rab and Rho GEFs and the respective GDIs⁴⁰⁻⁴². To observe whether such competition indeed occurs for Rho GTPases, we investigated the effect of GEF activity on the interaction between GDI and mammalian Rac1, which is similar in mechanism and kinetics to GDI-Cdc42 interaction³⁹. Exposure to the GEF domain of Dock180 (DHR2C)

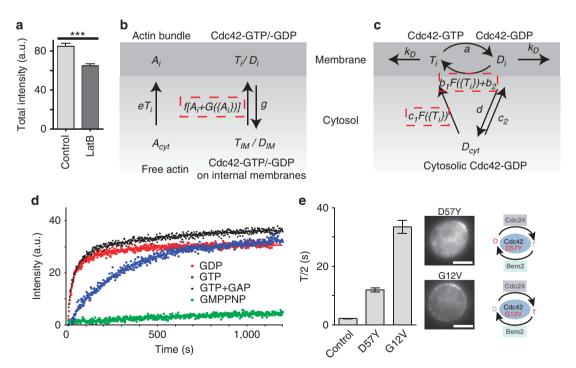


Figure 3 | **Building a mathematical model of the combined pathways.** (a) Comparison of total intensities of GFPCdc42 caps in controls and LatB-treated cells. Bars indicate means \pm s.e.m. n> 80. ***t-test, P<0.0001. (**b,c**) Schematic depiction of model reactions for actin- (**b**) and GDI-mediated (**c**) recycling pathways. See Supplementary Methods and Supplementary Tables S1,S2 for details of reactions and parameters. Non-linear feedback reactions are indicated by dashed boxes. (**d**) Extractability of Cdc42 from hexadecanoylaminofluorescein (HAF)-labelled liposomes loaded with the indicated methylanthraniloyl-modified (Mant-) nucleotides. (**e**) Halftimes (FRAP T/2) for localization of inactive Cdc42^{D57Y} (n=16) and constitutively active Cdc42^{G12V} (n=16). Bars indicate mean \pm s.e.m. The schematics illustrate changes in the Cdc42 GTPase cycle. Scale bar, 4 μm.

and a non-hydrolyzable GTP analogue was sufficient to dissociate soluble GDI–Rac1 complexes, allowing free GMPPNP-bound Rac1 to bind to liposomes (Supplementary Fig. S2a). Conversely, nucleotide exchange by the GEF was strongly reduced in the presence of GDI (Supplementary Fig. S2b), consistent with competition for binding to the switch II region of the GTPase⁴⁰. These results cannot be directly transferred to living yeast cells. However, we found that the dominant-negative mutant Cdc42^{D57Y}, which sequesters its GEF^{43,44}, could no longer be extracted by the GDI and was instead slowly recycled via actin-mediated transport^{14,17} (Fig. 3e). Our results are consistent with competition between GEF and GDI for binding of Cdc42-GDP. We therefore implemented interference of GEF activity with Cdc42–GDI interaction by increasing the rate of Cdc42 membrane association in regions of high Cdc42 activity (equivalent to high GEF concentrations).

GDI-mediated polarization is of considerable theoretical interest^{28,30,45}. Our results indicate that GDI-mediated recycling of Cdc42 depends on the latter's catalytic cycle, and both GAP and GEF need to be regulated to allow rapid shuttling between membrane and cytosol. In a previous model, positive feedback in Cdc42 activation was based on non-linear recruitment of Cdc24 to Cdc42-GTP^{28,46}. The model predicts slower turnover of Cdc24 if Cdc42 activity is increased. However, we found that the level of GEF expression or actin or Cdc42 activity had no influence on Cdc24 turnover at the polarized site (Supplementary Fig. S3b), indicating that feedback must be implemented in a different manner. Our model assumes linear recruitment of the GEF to

Cdc42-GTP, but instead incorporates two GEF-mediated, and experimentally supported, positive feedback loops for activation and physical recruitment of Cdc42 (dashed boxes in Fig. 3c), respectively. A short comparison of features and limitations in various models for yeast cell polarity is shown in Supplementary Table S10. A detailed review on this subject has also been published recently⁴⁷.

Determination of quantitative model parameters. Having established a general structure for the two Cdc42 recycling pathways we set out to determine realistic values for the parameters involved in their operation. We aimed to base all model reactions (Supplementary Table S8) and parameters (Supplementary Table S9) on experimental evidence. Several parameter values and data concerning the distribution of Cdc42 between cell compartments were taken from the literature (Supplementary Methods). The remaining values were fitted to quantitatively reproduce characteristics of control cells and of the individual recycling pathways observed in LatB-treated or Δrdi1 cells (Figs 4,5). In all conditions our model was able to recapitulate polarization profiles of Cdc42 with realistic background levels and values for cap width and cap height (Fig. 4). In addition, the polarization response was robust to considerable variations in the individual parameter values (Supplementary Fig. S4).

The mobility of Cdc42 is a major element in any dynamic polarization model. We performed fluorescence recovery after photobleaching (FRAP) experiments to monitor Cdc42 recycling.

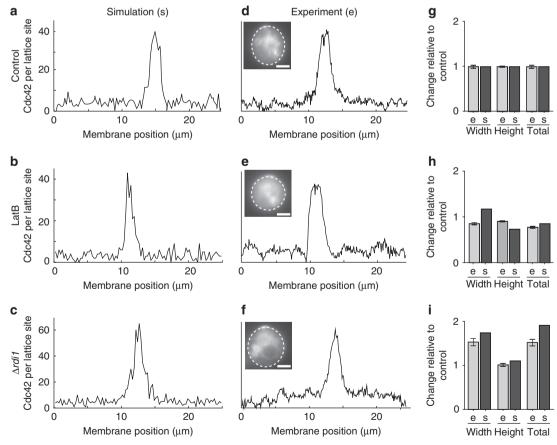


Figure 4 | Fitting cap shape parameters. (a-f) Examples of simulated (a-c) and experimentally determined (d,e) cap profiles in control cells (a,d), LatB-treated cells (b,e) and $\Delta rdil$ cells (c,f). Dashed lines in images indicate fields of view used for line scans. Scale bar, 4 μm. (g-i) Comparisons of cap size (width), average cap intensity (height) and total cap intensity (total, = width × height) in experiments (e) and simulations (s) for control (g), LatB-treated (h) and $\Delta rdil$ cells (i). Bars represent means ± s.e.m. of measurements normalized to values for control cells (n > 80 for control and LatB cells, and n = 35 for $\Delta rdil$ cells). Note that total intensity values for control and LatB cells correspond to the values used in Fig. 3a.

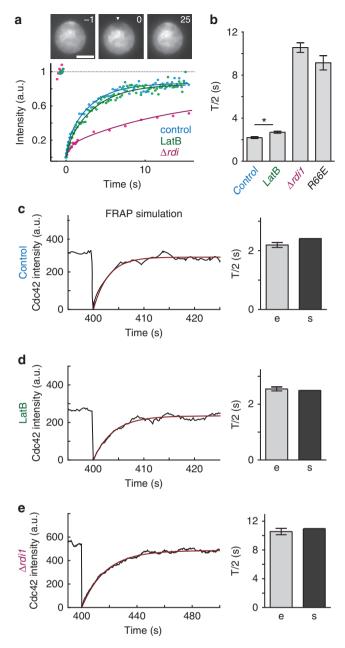


Figure 5 | Fitting Cdc42 turnover parameters. (**a**,**b**) Representative FRAP curves (**a**) and FRAP T/2 values (**b**) for GFPCdc42 in controls (n=56), $\Delta rdi1$ cells (n=20), cells expressing GFPCdc42^{R66E} (n=11) and cells treated with LatB (n=24). The arrowhead in (**a**) indicates the position targeted for FRAP. Bars in (**b**) represent means \pm s.e.m. *: t-test, P < 0.05. Time is indicated in s. Scale bar, $4 \, \mu m$. (**c-e**) Simulated (black) FRAP curves and exponential fits (red), and comparison of T/2 values for simulated (**s**) and experimental (**e**, identical to bars in (**b**)) recovery. Actual and simulated FRAP data are shown for control (**c**), LatB-treated (**d**) and $\Delta rdi1$ (**e**) cells.

In agreement with previous measurements^{14,17}, recovery of Cdc42 fluorescence in control cells occurred with an average *T*/2 of 2.2 s, and was independent of Cdc42 expression level (Fig. 5a,b, Supplementary Fig. S3a). Disruption of actin structures with LatB led to a slightly increased *T*/2 of 2.5 s (Fig. 5a,b, Supplementary Fig. S3a). This slower recovery was proposed to result from greater accumulation of Cdc42 in caps²¹. However, Cdc42 cap intensities in LatB-treated cells were significantly

reduced (Fig. 3a), supporting a positive role for actin in Cdc42 polarization. Perturbation of Cdc42–Rdi1 interactions by deletion of *RDI1* or the use of the Cdc42^{R66E} mutant drastically slowed recovery to a *T*/2 of 10 s (Fig. 5b), confirming previous work on polarity maintenance¹⁷. Our results confirm that Rdi1- and actin-dependent Cdc42 recycling act in parallel during polarity establishment and show that the pathways act on different time scales. All values for Cdc42 mobility could be accurately reproduced in our model (Fig. 5c–e, Supplementary Table S3).

Validating the model. Our model was able to reproduce characteristics of Cdc42 mobility and distribution under various experimental conditions. Next, we searched for model predictions that we could validate experimentally. One critical aspect of the model is the fact that GDI-mediated extraction is restricted to GDP-Cdc42, predicting loss of polarization in LatB-treated cells at very low rates of hydrolysis (Fig. 6a). The hydrolysis rate in control cells, estimated by fitting values for cap height/width and FRAP times, was $2.74\,\mathrm{s}^{-1}$ (grey dashed line Fig. 6a). To check the model-based prediction we reduced GTP hydrolysis on Cdc42 by deleting BEM2, the GAP with the largest number of genetic interactions with actin (Fig. 2a). Cdc42 in $\Delta bem2$ cells was able to polarize efficiently, albeit with slightly reduced speed (Fig. 6b). However, when actin was disrupted most $\Delta bem2$ cells could no longer polarize (Fig. 6b). Similar results were obtained when monitoring Cdc24 or Bem1 (Supplementary Fig. S3d). In our simulations polarization occurred over a wide range of hydrolysis values, with the control rate being close to the maximum permissible before polarization breaks down (Fig. 6a). To study the impact of changes in hydrolysis rates on a more quantifiable parameter, we tested the effect of deleting BEM2 on Cdc42 mobility. The model predicted a gradual increase in T/2 upon reduction of the GTP hydrolysis rate (Fig. 6c). This slowdown was expected to be more pronounced in LatB-treated cells. In agreement with this prediction, in $\Delta bem2$ cells and the slow-acting mutant Cdc42^{G60A} (ref. 48), FRAP halftimes increased to 6.7 and 6.8 s, respectively, (Fig. 6d, Supplementary Table S3). In our model this recovery rate corresponds to a roughly 16-fold decrease in the rate of GTP hydrolysis to (grey dashed lines in Fig. 6c). At this hydrolysis rate, Cdc42 in LatB-treated cells is predicted to recycle with a T/2 of 8.7 s—a value close to the measured 9.6 s for LatB-treated Δbem2 cells (Supplementary Table S3). Hence, our results indicate that the contribution of actin to Cdc42 recycling is increased in $\Delta bem2$, likely due to reduced extraction of active Cdc42 by its GDI.

The mechanism of formation of multiple polarization sites. In all our simulations, the GDI pathway alone was never able to generate multiple stable polarization site. However, yeast cells are capable of simultaneously polarizing at two or more sites, for example, after deletion of BEM2 (ref. 49), deletion or overexpression of BEM1 (refs 14,16) or overexpression of constitutively active Cdc42 (ref. 13). Interestingly, we noticed that $2.3 \pm 0.5\%$ ($n = 4 \times 100$ cells) of $\Delta rdi1$ cells formed two stable polarization sites (Fig. 7a, Supplementary Table S4), a value that could be reproduced in our model after fitting the actinmediated pathway (Fig. 7b,c, grey dashed line at $a = 2.74 \,\mathrm{s}^{-1}$). Varying parameters in the model generated two testable predictions. First, increased Cdc42 activation should strongly increase the percentage of $\Delta rdi1$ cells that form multiple polarization sites (Fig. 7c, blue curve). Second, even cells with a functional GDI should form multiple caps if rates of GTP hydrolysis are reduced sufficiently (Fig. 7c, black curve). Rdi1-mediated recycling of Cdc42 alone was unable to generate multiple stable caps in our simulations. The formation of multiple caps at lower hydrolysis

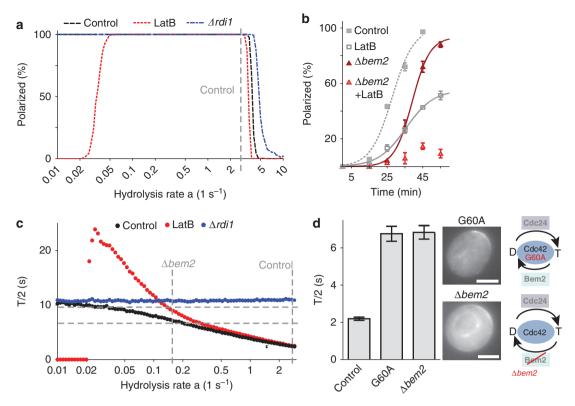


Figure 6 | Effects of GTP hydrolysis on polarization efficiency and Cdc42 dynamics. (a) Predicted dependence of polarization efficiencies in control, LatB-treated and $\Delta rdi1$ cells on the rate of GTP hydrolysis. The hydrolysis rate for control cells ($a = 2.74 \, \text{s}^{-1}$) was estimated by fitting model parameters (Figs 4,5), and is indicated by the vertical dashed grey line. (b) Polarization efficiency of Cdc42 in control and $\Delta bem2$ cells in the presence or absence of LatB. Data points represent means of three experiments with 50 cells each. Error bars indicate s.d. The lines are sigmoidal fits. (c) Plot of simulated Cdc42 FRAP T/2 (mean values from 400 runs/data point) against rate of GTP hydrolysis. Fitted and estimated hydrolysis rates in control and $\Delta bem2$ cells are indicated as vertical dashed grey lines. T/2 values measured in $\Delta bem2$ cells without (6.8 s; n = 20) and with LatB (9.6 s, n = 12) are indicated as horizontal dashed grey lines. (d) FRAP T/2 and localization of Cdc42 in $\Delta bem2$ cells and in cells expressing Cdc42^{G60A} (n = 11), a mutant with a lower GTPase activity. Bars represent means \pm s.e.m. Schematics illustrate changes in the Cdc42 GTPase cycle. Scale bar, 4 μm.

rates can be explained by the reduction or loss of the ability of GDI-mediated recycling to restrict cap formation to a singlepolarization site and the enhanced nucleation of actin at higher levels of Cdc42-GTP. To increase Cdc42 activity in $\Delta rdi1$ cells, we exploited the known cell cycle-dependent activation of Cdc42 after the G1/S transition 49,50 . We released $\Delta rdi1$ cells from G1 arrest in the presence of LatB to prevent immediate polarization and washed the drug out at different times to allow polarization with varying initial Cdc42 activity (Supplementary Fig. S5a). As predicted, the number of cells with two polarization sites increased from 2.3-13% and 23% with increasing duration of drug treatment and hence increasing level of Cdc42 activity (Fig. 7d, Supplementary Table S4). Next, we used $\Delta bem2$ cells to increase Cdc42 activity in the presence of Rdi1. We found that similar to a previous report⁴⁹, 8.7% of cells formed two buds (Fig. 7e), and this was independent of the GFP tag, strain background or Cdc42 expression level (Supplementary Fig. S5, Supplementary Table S4). We further increased Cdc42 activity by overexpressing Cdc24 (Supplementary Fig. S5d) or expressing a Cdc42 mutant with high intrinsic GDP release rate (Cdc42F28L (ref. 51)). Neither treatment induced formation of double buds in control cells (Fig. 7e, Supplementary S5c). However, in $\Delta bem2$ strains the number of cells forming multiple polarization sites increased significantly (Fig. 7e, Supplementary S5c). Our results indicate that actin-mediated recycling of Cdc42 is prone to creating multiple polarization sites, and that this effect is sensitive to the level of Cdc42 activity.

Moreover, our results show that perturbation of GDI-mediated polarization can induce formation of multiple buds in otherwise wild-type cells.

Although formation of two polarization sites in a small percentage of cells in a population might, at first sight, seem tolerable, even slight effects on cell division could translate into a strong evolutionary disadvantage. Indeed, we found that the formation of multiple buds directly correlated with an increased number of mis-segregated nuclei (Fig. 8a) and this effect was dependent on increased activity of Cdc42 (Fig. 8b). On average, more than 20% of cells with double buds also exhibited defects in nuclear segregation (Figs 8b,7e). Formation of multiple buds therefore likely has direct impact on cell survival.

Discussion

We have shown that yeast cells can establish polarity by localizing the central polarity regulator Cdc42 through a combination of two recycling pathways with distinct mechanistic features. GDI-dependent recycling of Cdc42 is fast and coupled to the GTPase cycle of Cdc42. Symmetry breaking in this pathway occurs via a combination of positive feedback loops for activation and recruitment of Cdc42, is characterized by efficient formation of a unique polarization axis, but is sensitive to perturbations in the GTPase cycle of Cdc42. In contrast, actin-mediated recycling of Cdc42 is slower and depends solely on Cdc42 activity¹³. The use of actin cables for delivery of Cdc42 to the plasma membrane

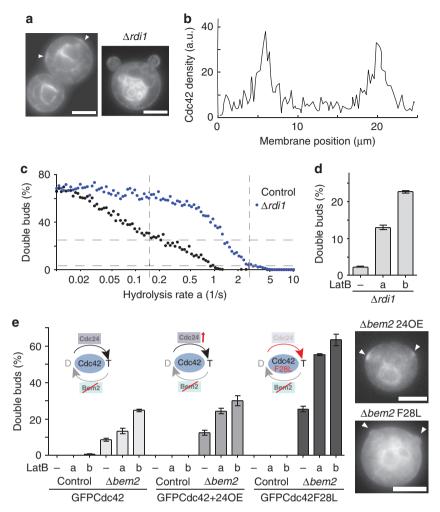


Figure 7 | Formation of multiple polarization sites. (a) Examples of simultaneous formation of two Cdc42 caps (arrows) and buds in $\Delta rdi1$ cells. Scale bar, 4 μm. (b) Intensity profile illustrating formation of two caps in a simulated $\Delta rdi1$ cell. (c) Predicted effects of varying the rate of GTP hydrolysis on formation of multiple polarization sites in simulations of control and $\Delta rdi1$ cells. Fitted and estimated hydrolysis rates in control and $\Delta bem2$ cells are indicated as vertical dashed grey lines. Percentage of double buds observed in $\Delta bem2$ cells after washing LatB out (25%, n = 300) and in $\Delta rdi1$ cells (2.3%, n = 400) are indicated as horizontal dashed grey lines. See also Supplementary Table S7. (d) Effect of washout of LatB on the percentage of $\Delta rdi1$ cells with two buds. Cells were treated with LatB for 20 min (a) or 40 min (b) before washout of the drug or without treatment (–). See Supplementary Methods for experimental details. (e) Effect of Cdc42 activity level on the formation of double buds in control and $\Delta bem2$ cells. Cells expressing GFPCdc42, GFPCdc42 and Cdc24RFP or GFPCdc42 F28L (a mutant with fast intrinsic GDP exchange) were treated with LatB as in (d). Examples of double cap formation in $\Delta bem2$ cells expressing either GFPCdc42 or GFPCdc42 F28L are shown on the right. Bars represent means ± s.e.m. for three experiments with 100 cells each. Schematics illustrate changes in the Cdc42 GTPase cycle. Scale bar, 4 μm.

leads to formation of very stable polarization sites. However, this stability comes with a significant risk of stochastically generating multiple stable polarization sites—an effect that becomes especially prominent if Cdc42 activity is increased. By combining the two recycling pathways, yeast cells ensure reliable establishment of a unique polarity axis.

To quantitatively analyse the interplay between Cdc42 recycling pathways, we built a particle-based mechanistic model for polarity establishment and performed extensive stochastic simulations. We kept the model complexity at a level that was appropriately supported by experimental evidence. We used measurements from a variety of quantitative *in vivo* and *in vitro* experiments to validate and constrain assumptions and parameters. This integrated approach allowed us to make detailed predictions concerning polarization efficiency, protein localization kinetics and number of polarization sites, which were confirmed with remarkable accuracy by our experimental data.

Two key features in our model should be emphasized. First, we found that polarity establishment in yeast did not sensitively depend on the quantity of Cdc42 in the cell. This was also observed in our simulations, where a 10-fold increase in Cdc42 concentration failed to prevent polarization (N(Cdc42) = 3,000–30,000 yield 100% polarization). These findings contradict a recent study, in which stochastic polarization of Cdc42 was proposed to depend critically on low expression levels 30 . Instead, we find that polarization depends on the level of Cdc42 activity. Second, because of separate positive feedback in Cdc42 activation (Cdc42 $^{\rm GTP}$ –GEF–Bem1–Cla4 interactions) and Cdc42 recruitment (GEF–GDI competition), our model does not depend on non-linear recruitment of the GEF, which was required for polarization in a previous model 28 and was not supported by our experiments.

Our results indicate that yeast cells did not simply evolve two redundant polarization pathways to safeguard an essential process against random error. Instead they combine positive features of

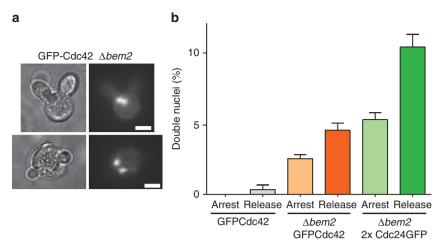


Figure 8 | Multiple polarization sites and DNA segregation (a) Examples of $\Delta bem2$ cells displaying two nuclei and two buds. Scale bar, $4 \mu m$. (b) Percentage of cells with two nuclei in controls and in $\Delta bem2$ cells expressing GFPCdc42 or two copies of Cdc24GFP. Bars represent means \pm s.e.m. for three experiments with 100 cells each.

both pathways to simultaneously achieve reliability and spatial precision in cell polarization. Such an optimized interplay of pathways requires precise selection of parameter values. Indeed, our results suggest that the GTPase cycle of Cdc42 has a central role in coordinating pathways underlying polarity establishment. In particular, the Cdc42 hydrolysis rate is restricted to a rather narrow range between roughly 1 and 3 s. Faster rates lead to a loss of polarization due to insufficient amounts of active Cdc42 in the cell (Fig. 6a), although slower hydrolysis leads to formation of multiple buds (Fig. 7c). The latter effect is a result of a reduced recycling speed and hence smaller contribution for the GDI pathway (Fig. 6c) and a simultaneous failure of the actin pathway to focus polarization to a single site if Cdc42 activity is increased (Fig. 7c). GDI recycling therefore needs to be faster than the actin pathway to ensure polarization at a single site and in our simulations Cdc42 in control cells seems to indeed hydrolyse GTP with nearly maximal possible speed. At the other extreme, if the GDI pathway is deleted, cells become very prone to form multiple caps (Fig. 7c).

Our results provide a mechanistic link between the fast GTPase cycle and GDI-mediated membrane recycling of Rho GTPases. Similar interactions have also been reported for small GTPases of the Rab family⁵². The mechanisms we identified for localization of Cdc42 might therefore also be applicable for other processes of spatial cellular organization.

Our proposed model was capable of reproducing all our experimental results and made several accurate and quantitative predictions. However, there are still many open questions concerning the biophysical and biochemical basis for cell polarization. For example, it has recently been demonstrated that lipid composition at the polarized site, in particular negatively charged phospholipids, influence the association of Cdc42 with the plasma membrane and hence impact on cell polarity^{53,54}. Furthermore, although we assumed cell cycle-dependent activation of Cdc24 and inactivation of Bem2 in the LatB washout experiments (Fig. 7, Supplementary Fig. S5), the detailed biochemistry of these regulatory processes is not fully understood and they were not included in the mathematical model. Finally, we did not consider potential regulation of GDI-Cdc42 interaction or GDI-membrane interaction by phosphorylation⁵⁵. All these additional aspects provide ample scope for future improvements in both modelling and mechanistic understanding of cell polarization. As nicely summarized in a recent review, the

value of a mathematical model should be judged 'not by how complex and detailed it is, but by what could be learned from it'⁴⁷. Our current model consequently incorporates the minimum degree of complexity compatible with generation of meaningful forecasts, and was able to reflect and predict basic properties of cellular organization that will hopefully help to rationalize a variety of different biological processes.

Methods

Cell culture and plasmids. All strains are derived from RWS116, in which only one G1 cyclin, CLN2, is expressed under the control of a methionine repressible promoter. Unless otherwise stated, cells were grown at RT in SC-Met medium containing 2% glucose. Cells were arrested in G1 by addition of 3 mM methionine for 4 h and released again by washing twice and resuspension in methionine-free medium. To verify strain growth, three-fold serial dilutions of an equal amount of logarithmically growing cells were spotted as triplicate onto Sc-Met plates and incubated at indicated temperatures for 2 days. Standard genomic manipulation procedures⁵⁶ were used for GFP integrations or gene deletions. Site-directed mutagenesis was performed as described⁵⁷. Strains, plasmids and primers are listed in Supplementary Tables S8–S10, respectively.

Immunoblot analyses. Total protein extracts of 1.4×10^7 cells were boiled in SDS-sample buffer and analysed by SDS-PAGE, transferred to nitrocellulose membrane and probed with a polyclonal Cdc42 serum (1:500; sc-6793; Santa Cruz Biotechnology) or with a monoclonal glyceraldehyde-3-phosphate dehydrogenase antibody (1:1500; ab 125247, Abcam). Immunoblots were visualized using a Fuji-Las3000 imager. Quantification of bands was performed in ImageJ.

Interaction screen. We used the following set of query proteins: Cdc42, Cdc24, Bem2, Bem3, Rga1 and Rga2, Rdi1, Bem1 and Cla4. Physical and genetic interaction partners were collected from public databases (BioGRID⁵⁸, MPACT⁵⁹). Physical interactions included data from affinity purification, co-crystallization, FRET, PCA, protein–peptide interaction, reconstituted complexes and two-hybrid. Genetic interactions represented synthetic growth defects, haploinsufficiencies and synthetic lethality. We only considered negative interactions from synthetic genetic array screens. Interaction partners involved in actin-related processes were grouped in four categories: actin general (actin patches or cables), early secretion (ER-to-Golgi transport), late secretion (Golgi-to-plasma membrane transport) and endocytic recycling. All identified interactions are listed in Supplementary Tables \$1,\$2. For each query the number of interactions with members of each category were extracted. The number of unique interactions in each functional group served as a measure of the overall strength of interaction with that group and was colour-coded in a heat map (see Fig. 1a).

Microscopy and imaging. Coverslips were coated with ConA (2 mg ml^{-1} , Sigma). Raw images were used for all quantifications and analyses. Polarization and washout experiments were performed on a Zeiss Axio Imager.A1 upright microscope with 1.4 NA \times 100 objective, an X-Cite120 light source (Lumen Dynamics)

and an iXON DU-897 EMCCD camera (Andor) coupled to a $\times 2$ magnification ring. Images were acquired with Metamorph 7.0 software.

Images for FRAP experiments were acquired on a custom-built setup from Till Photonics based on an iMic stand with Olympus 1.45 NA $\,\times\,100$ objective and iXON DU-897 EMCCD camera. Four hundred eighty-eight nanometre (Coherent) and 561 nm (Cobolt) lasers were directed through an AOTF and coupled into the iMic. A galvanometer allowed switching between FRAP and epifluorescence modes. Two additional galvanometers were used to adjust laser incidence angles or FRAP positions. For FRAP, caps were selected 10–20 min after release from G1 arrest. Acquisition was controlled by the Live Acquisition software.

Drug treatments and staining

Actin disruption. Cells were released in medium containing 400 μ M LatB. In washout experiments, LatB was added for 20 or 40 min, and then removed by washing twice. Polarization was monitored after 40–60 min. FM4-64 staining: cells were incubated in 0.32 μ M FM4-64 for 2 min and washed once.

DAPI-staining. One millilitre cells were released for 2–25 h, fixed with 3% formaldehyde for 2 h, washed twice and resuspended in 30 μ l PBS + 0.1% Triton. Fixed cells were then incubated with 0.1 μ g ml $^{-1}$ DAPI for 10 min and washed twice with PBS.

FRAP analysis. To quantify fluorescence recovery MATLAB (MathWorks, 2010a) routines were implemented. Intensities in the bleached region were corrected for background fluorescence and total cellular fluorescence. The recovery curve was fitted with a double exponential function $y_{\rm fit}(t) = a(1-b(\exp(-tc)) - d(\exp(-te))$. The fast component corresponded to diffusion of soluble Cdc42 in the cytosal and the slower component ro recovery of membrane-bound Cdc42 pool via a combination of GDI- and actin-mediated mechanisms. The halftime for the slower component, $t^2_{1/2} = -\log(0.5)/e$ was used for further comparison. Time stamps were automatically extracted from the metadata. Data points were only used if reliable fits could be generated (residual sum of squares >0.95). Means and s.e.m. were calculated from >10 independent experiments (Supplementary Table S3).

Calculation of cap width and height. For measurements of cap width and height, GFP-Cdc42 caps were identified from medial cross-sections and a region $R^{\rm cap}$ was drawn around the perimeter of the cap. A background region $R^{\rm bg}$ was selected inside the same cell. Background signal I^0 from the camera chip was calculated from a region distant from any cell. Cap height H was calculated as $H = (I(R^{\rm cap}) - I^0)/(I(R^{\rm bg}) - I^0)$. Cap width W corresponded to the size of the cap area $R^{\rm cap}$. Total intensitiy $I^{\rm tot}$ was calculated as $I^{\rm tot} = H^*W$.

Protein purification. His₆-tagged Cdc42 was purified from baculovirus-infected Sf21 insect cells. All purification steps were performed at 4 °C. Stirred 1l cultures of Sf21 cells were infected for 48 h by Kinnakeet Biotechnology (Midlothian, VA). Cell pellets were resuspended in 40 ml hypotonic buffer (20 mM sodium borate pH 10.2, 5 mM MgCl₂, 200 μ M PMSF, 1 μ g ml $^{-1}$ aprotinin and leupeptin) and disrupted by Dounce homogenization.

Membrane-containing components of the lysate were spun down at 1,50,000 g in a Ti70 rotor (Beckman Coulter) for 20 min and resuspended in 50 ml TBSM (50 mM Tris pH 7.5, 150 mM NaCl, 5 mM MgCl₂). The procedure was repeated twice and the final pellet was resuspended in TBSM + 1% Triton-X100. The lysate was further homogenized and agitated for 30 min on a rotisserie, resulting in solubilization of geranylgeranylated Cdc42. The remaining insoluble fraction was pelleted in a tabletop centrifuge at 9,000 g for 20 min at 4 °C and discarded. The supernatant containing detergent-solubilized, isoprenylated His₆-tagged Cdc42 was incubated for 30 min with chelating Sepharose beads (Qiagen) charged with Ni²⁺. Beads were then washed with 400 ml high salt buffer (50 mM Tris pH 7.5, 700 mM NaCl, 5 mM MgCl₂, 0.1% CHAPS, 20 mM imidazole) and protein was eluted with 10 ml elution buffer (50 mM Tris pH 7.5, 150 mM NaCl, 5 mM MgCl₂, 0.1% CHAPS, 500 mM imidazole). The fractions containing Cdc42 were pooled and concentrated to 2 ml. His₆-tagged prenylated Rac1 was purified in the same manner as Cdc42.

N-terminal GST fusions to human RhoGDI and to the GAP domain of Cdc42-GAP (human, residues 234-462) as well as N-terminally $\rm His_6$ -tagged DHR2C domain of human Dock180 were purified from E. coli cells. Cells were grown at 37 °C to OD 0.8. Protein expression was induced by 1 mM IPTG for 3 h before pelleting at 6,000 g for 10 min. Cell pellets were homogenized in TBSM and lysed by sonication. Extracts were spun at 20,000 g for 30 min. Supernatants with GST-tagged proteins were incubated with glutathione beads and equilibrated with TEDA buffer (20 mM Tris pH 8.0, 1 mM EDTA, 1 mM DTT, 1 mM sodium azide) for 30 min at 4 °C. Beads were washed with several column volumes of TEDA-containing 500 mM NaCl and protein was eluted with 10 mM glutathione in TBSM. His₆-tagged DHR2 domain was purified on Sepharose beads charged with Ni²+ as described above. All proteins were concentrated in 10 MWC Amicon Ultra concentrators.

Liposome binding assays. Liposomes were prepared by extrusion using Avanti mini-extruders (1 or $8 \mu m$ membranes) followed by centrifugation at 16,000 g for 10μ min and resuspension in TBSM. Lipids were purchased from Avanti Polar Lipids. The standard lipid composition in molar percentages was 35% PE, 25% PS, 5% PI and 35% cholesterol (Nu Chek Preps).

For Cdc42–liposome association assays a Varian Cary Eclipse fluorimeter was used in the counting mode. Excitation and emission wavelengths were 365 and 440 nm, respectively. Samples were stirred continuously at 25 °C in TBSM. To prepare HAF (hexadecanoylaminofluorescein)-labelled lipids for FRET assays, 1.25 nmol of HAF (Molecular Probes) was vortexed with 50 μ l of lipids (1 mg ml $^{-1}$). To monitor release of Cdc42 from liposomes, Cdc42 was preloaded with methylanthraniloyl-modified (Mant) nucleotide and incubated with 30 μ l of HAF-containing liposomes at RT for 5 min. The mixture was added to the cuvette, bringing the final Cdc42 concentration to 40 nM. At the indicated time points, 50 nM RhoGDI and 10 nM Cdc42-GAP were added, and fluorescence was recorded for 20 min. Traces monitored the changes in Mant fluorescence due to changes in FRET between Mant-nucleotide-bound Cdc42 and liposomes containing HAF.

Statistics and data analysis. Curve fitting for polarization curves was done with Prism 4 (GraphPad Software, La Jolla) using a sigmoidal dose-response equation $y = \text{bottom} + (\text{top-bottom})/(1 + 10^{(\text{LogEC50-X})^{*}}\text{Hill Slope})$). Unpaired two-tailed t-tests were performed to validate significance of differences.

References

- Etienne-Manneville, S. Cdc42--the centre of polarity. J. Cell. Sci. 117, 1291–1300 (2004).
- 2. Munro, S. Lipid rafts: elusive or illusive? Cell 115, 377-388 (2003).
- Richman, T. J., Sawyer, M. M. & Johnson, D. I. Saccharomyces cerevisiae Cdc42p localizes to cellular membranes and clusters at sites of polarized growth. *Eukaryot. Cell* 1, 458–468 (2002).
- Ziman, M. & Johnson, D. I. Genetic evidence for a functional interaction between Saccharomyces cerevisiae CDC24 and CDC42. Yeast 10, 463–474 (1994).
- Pruyne, D., Gao, L., Bi, E. & Bretscher, A. Stable and dynamic axes of polarity use distinct formin isoforms in budding yeast. *Mol. Biol. Cell* 15, 4971–4989 (2004).
- Barral, Y., Mermall, V., Mooseker, M. S. & Snyder, M. Compartmentalization of the cell cortex by septins is required for maintenance of cell polarity in yeast. *Mol. Cell* 5, 841–851 (2000).
- 7. Park, H. O. & Bi, E. Central roles of small GTPases in the development of cell polarity in yeast and beyond. *Microbiol. Mol. Biol. Rev.* **71**, 48–96 (2007).
- Wedlich-Soldner, R. & Li, R. Closing the loops: new insights into the role and regulation of actin during cell polarization. Exp. Cell Res. 301, 8–15 (2004).
- Koch, G. et al. Association of the Rho family small GTP-binding proteins with Rho GDP dissociation inhibitor (Rho GDI) in Saccharomyces cerevisiae. Oncogene 15, 417–422 (1997).
- 10. Tiedje, C., Sakwa, I., Just, U. & Hofken, T. The Rho GDI Rdi1 regulates Rho GTPases by distinct mechanisms. *Mol. Biol. Cell* **19**, 2885–2896 (2008).
- 11. Johnson, J. M., Jin, M. & Lew, D. J. Symmetry breaking and the establishment of cell polarity in budding yeast. *Curr. Opin. Genet. Dev.* 21, 740–746 (2011).
- Slaughter, B. D., Smith, S. E. & Li, R. Symmetry breaking in the life cycle of the budding yeast. Cold Spring Harbor Pers. Biol. 1, a003384 (2009).
- Wedlich-Soldner, R., Altschuler, S., Wu, L. & Li, R. Spontaneous cell polarization through actomyosin-based delivery of the Cdc42 GTPase. *Science* 299, 1231–1235 (2003).
- Wedlich-Soldner, R., Wai, S. C., Schmidt, T. & Li, R. Robust cell polarity is a dynamic state established by coupling transport and GTPase signaling. J. Cell Biol. 166, 889–900 (2004).
- Irazoqui, J. E., Gladfelter, A. S. & Lew, D. J. Scaffold-mediated symmetry breaking by Cdc42p. Nat. Cell. Biol. 5, 1062–1070 (2003).
- Kozubowski, L. et al. Symmetry-breaking polarization driven by a Cdc42p GEF-PAK complex. Curr. Biol. 18, 1719–1726 (2008).
- Slaughter, B. D., Das, A., Schwartz, J. W., Rubinstein, B. & Li, R. Dual modes of cdc42 recycling fine-tune polarized morphogenesis. *Dev. Cell* 17, 823–835 (2009).
- Harris, K. P. & Tepass, U. Cdc42 and vesicle trafficking in polarized cells. Traffic 11, 1272–1279 (2010).
- Osmani, N., Peglion, F., Chavrier, P. & Etienne-Manneville, S. Cdc42 localization and cell polarity depend on membrane traffic. *J. Cell Biol.* 191, 1261–1269 (2010).
- Irazoqui, J. E., Howell, A. S., Theesfeld, C. L. & Lew, D. J. Opposing roles for actin in Cdc42p polarization. Mol. Biol. Cell 16, 1296–1304 (2005).
- Savage, N. S., Layton, A. T. & Lew, D. J. Mechanistic mathematical model of polarity in yeast. Mol. Biol. Cell 23, 1998–2013 (2012).
- Yamamoto, T. et al. Initial polarized bud growth by endocytic recycling in the absence of actin cable-dependent vesicle transport in yeast. Mol. Biol. Cell 21, 1237–1252 (2010).

- Ozbudak, E. M., Becskei, A. & van Oudenaarden, A. A system of counteracting feedback loops regulates Cdc42p activity during spontaneous cell polarization. *Dev. Cell* 9, 565–571 (2005).
- Howell, A. S. et al. Negative feedback enhances robustness in the yeast polarity establishment circuit. Cell 149, 322–333 (2012).
- Layton, A. T. et al. Modeling vesicle traffic reveals unexpected consequences for Cdc42p-mediated polarity establishment. Curr. Biol. 21, 184–194 (2011).
- Bose, I. et al. Assembly of scaffold-mediated complexes containing Cdc42p, the exchange factor Cdc24p, and the effector Cla4p required for cell cycle-regulated phosphorylation of Cdc24p. J. Biol. Chem. 276, 7176–7186 (2001).
- Butty, A. C. et al. A positive feedback loop stabilizes the guanine-nucleotide exchange factor Cdc24 at sites of polarization. EMBO J. 21, 1565–1576 (2002).
- Goryachev, A. B. & Pokhilko, A. V. Dynamics of Cdc42 network embodies a Turing-type mechanism of yeast cell polarity. FEBS Lett. 582, 1437–1443 (2008).
- Suzuki, R., Toshima, J. Y. & Toshima, J. Regulation of clathrin coat assembly by Eps15 homology domain-mediated interactions during endocytosis. *Mol. Biol. Cell* 23, 687–700 (2012).
- Altschuler, S. J., Angenent, S. B., Wang, Y. & Wu, L. F. On the spontaneous emergence of cell polarity. *Nature* 454, 886–889 (2008).
- Jilkine, A., Angenent, S. B., Wu, L. F. & Altschuler, S. J. A density-dependent switch drives stochastic clustering and polarization of signaling molecules. *PLoS Comput. Biol.* 7, e1002271 (2011).
- Boulter, E. et al. Regulation of Rho GTPase crosstalk, degradation and activity by RhoGDI1. Nat. Cell Biol. 12, 477–483 (2010).
- 33. Costanzo, M. et al. The genetic landscape of a cell. Science 327, 425-431 (2010).
- Gibson, R. M. & Wilson-Delfosse, A. L. RhoGDI-binding-defective mutant of Cdc42Hs targets to membranes and activates filopodia formation but does not cycle with the cytosol of mammalian cells. *Biochem. J.* 359, 285–294 (2001).
- Katzmann, D. J., Stefan, C. J., Babst, M. & Emr, S. D. Vps27 recruits ESCRT machinery to endosomes during MVB sorting. J. Cell Biol. 162, 413–423 (2003).
- Slaughter, B. D. et al. Non-uniform membrane diffusion enables steady-state cell polarization via vesicular trafficking. Nat. Commun. 4, 1380 (2013).
- Marco, E., Wedlich-Soldner, R., Li, R., Altschuler, S. J. & Wu, L. F. Endocytosis
 optimizes the dynamic localization of membrane proteins that regulate cortical
 polarity. *Cell* 129, 411–422 (2007).
- Pelham, H. R. & Munro, S. Sorting of membrane proteins in the secretory pathway. Cell 75, 603–605 (1993).
- Johnson, J. L., Erickson, J. W. & Cerione, R. A. New insights into how the Rho guanine nucleotide dissociation inhibitor regulates the interaction of Cdc42 with membranes. J. Biol. Chem. 284, 23860–23871 (2009).
- Schoebel, S., Oesterlin, L. K., Blankenfeldt, W., Goody, R. S. & Itzen, A. RabGDI displacement by DrrA from Legionella is a consequence of its guanine nucleotide exchange activity. *Mol. Cell* 36, 1060–1072 (2009).
- 41. Ugolev, Y., Berdichevsky, Y., Weinbaum, C. & Pick, E. Dissociation of Rac1(GDP).RhoGDI complexes by the cooperative action of anionic liposomes containing phosphatidylinositol 3,4,5-trisphosphate, Rac guanine nucleotide exchange factor, and GTP. J. Biol. Chem. 283, 22257–22271 (2008).
- Dransart, E., Olofsson, B. & Cherfils, J. RhoGDIs revisited: novel roles in Rho regulation. *Traffic* 6, 957–966 (2005).
- Stowers, L., Yelon, D., Berg, L. J. & Chant, J. Regulation of the polarization of T cells toward antigen-presenting cells by Ras-related GTPase CDC42. Proc. Natl Acad. Sci. USA 92, 5027–5031 (1995).
- 44. Jung, V. et al. Two types of RAS mutants that dominantly interfere with activators of RAS. Mol. Cell Biol. 14, 3707–3718 (1994).
- Onsum, M. D. & Rao, C. V. Calling heads from tails: the role of mathematical modeling in understanding cell polarization. Curr. Opin. Cell Biol. 21, 74–81 (2009).
- Howell, A. S. et al. Singularity in polarization: rewiring yeast cells to make two buds. Cell 139, 731–743 (2009).

- Mogilner, A., Allard, J. & Wollman, R. Cell polarity: quantitative modeling as a tool in cell biology. Science 336, 175–179 (2012).
- Caviston, J. P., Tcheperegine, S. E. & Bi, E. Singularity in budding: a role for the evolutionarily conserved small GTPase Cdc42p. *Proc. Natl Acad. Sci. USA* 99, 12185–12190 (2002).
- 49. Knaus, M. et al. Phosphorylation of Bem2p and Bem3p may contribute to local activation of Cdc42p at bud emergence. EMBO J. 26, 4501–4513 (2007).
- Nern, A. & Arkowitz, R. A. Nucleocytoplasmic shuttling of the Cdc42p exchange factor Cdc24p. J. Cell Biol. 148, 1115–1122 (2000).
- Lin, Q., Fuji, R. N., Yang, W. & Cerione, R. A. RhoGDI is required for Cdc42-mediated cellular transformation. *Curr. Biol.* 13, 1469–1479 (2003).
- Wu, Y. W. et al. Membrane targeting mechanism of Rab GTPases elucidated by semisynthetic protein probes. Nat. Chem. Biol. 6, 534–540 (2010).
- Das, A. et al. Flippase-mediated phospholipid asymmetry promotes fast Cdc42 recycling in dynamic maintenance of cell polarity. Nat. Cell Biol. 14, 304–310 (2012)
- Fairn, G. D., Hermansson, M., Somerharju, P. & Grinstein, S. Phosphatidylserine is polarized and required for proper Cdc42 localization and for development of cell polarity. *Nat. Cell Biol.* 13, 1424–1430 (2011).
- DerMardirossian, C. & Bokoch, G. M. GDIs: central regulatory molecules in Rho GTPase activation. Trends Cell Biol. 15, 356–363 (2005).
- Janke, C. et al. A versatile toolbox for PCR-based tagging of yeast genes: new fluorescent proteins, more markers and promoter substitution cassettes. Yeast 21, 947–962 (2004).
- Sambrook, J.a.R., D. W. Molecular Cloning A Laboratory Manual 3rd Edn (Cold Spring Harbor Laboratory Press, Cold Spring Harbor, New York, 2001).
- Breitkreutz, B. J. et al. The BioGRID Interaction Database: 2008 update. Nucleic Acids Res. 36, D637–D640 (2008).
- Mewes, H. W. et al. MIPS: curated databases and comprehensive secondary data resources in 2010. Nucleic Acids Res. 39, D220–D224 (2011).

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Author contributions

T.F., B.K., E.F. and R.W.-S. conceived the study, analysed the data and wrote the manuscript. T.F., G.P. and G.B. performed experiments. B.K. and E.F. built mathematical models and performed simulations. J.J. performed protein purifications and liposome assays with help from R.A.C. M.C. and C.B. provided SGA data and expertise.

Additional information

Supplementary Information accompanies this paper at http://www.nature.com/naturecommunications

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