

INSPIRE: interpretable, flexible and spatially-aware integration of multiple spatial transcriptomics datasets from diverse sources

Jia Zhao¹, Xiangyu Zhang¹, Gefei Wang¹, Yingxin Lin¹, Tianyu Liu^{1,2}, Rui B. Chang^{3,4}, Hongyu Zhao^{1,2*}

¹Department of Biostatistics, School of Public Health, Yale University, New Haven, CT, USA

²Interdepartmental Program in Computational Biology and Bioinformatics, Yale University, New Haven, CT, USA

³Department of Neuroscience, School of Medicine, Yale University, New Haven, CT, USA

⁴Department of Cellular and Molecular Physiology, School of Medicine, Yale University, New Haven, CT, USA

Abstract

1 Recent advances in spatial transcriptomics technologies have led to a growing number of diverse
2 datasets, offering unprecedented opportunities to explore tissue organizations and functions
3 within spatial contexts. However, it remains a significant challenge to effectively integrate and
4 interpret these data, often originating from different samples, technologies, and developmental
5 stages. In this paper, we present INSPIRE, a deep learning method for integrative analyses
6 of multiple spatial transcriptomics datasets to address this challenge. With designs of graph
7 neural networks and an adversarial learning mechanism, INSPIRE enables spatially informed
8 and adaptable integration of data from varying sources. By incorporating non-negative matrix
9 factorization, INSPIRE uncovers interpretable spatial factors with corresponding gene programs,
10 revealing tissue architectures, cell type distributions and biological processes. We demonstrate
11 the capabilities of INSPIRE by applying it to human cortex slices from different samples,

*Correspondence: hongyu.zhao@yale.edu.

12 mouse brain slices with complementary views, mouse hippocampus and embryo slices generated
13 through different technologies, and spatiotemporal organogenesis atlases containing half a
14 million spatial spots. INSPIRE shows superior performance in identifying detailed biological
15 signals, effectively borrowing information across distinct profiling technologies, and elucidating
16 dynamical changes during embryonic development. Furthermore, we utilize INSPIRE to build
17 3D models of tissues and whole organisms from multiple slices, demonstrating its power and
18 versatility.

19 **Introduction**

20 Spatial transcriptomic (ST) technologies enable spatially resolved transcriptomic studies by
21 profiling gene expressions with spatial information in intact tissues [1, 2]. Recently, various ST
22 technologies have been developed with complementary strengths [3, 4]. For example, widely
23 used next-generation sequencing-based methods, such as 10x Visium [5], Slide-seq [6, 7] and
24 Stereo-seq [8], allow for transcriptome-wide gene expression profiling. While technologies based
25 on in situ hybridization (e.g., seqFISH [9, 10] and MERFISH [11]) and in situ sequencing (e.g.,
26 STARmap [12, 13]) require panel designs for target genes with prior knowledge, they offer single-
27 cell and subcellular resolution that is essential in characterizing cellular communications. These
28 diverse ST approaches provide great opportunities for deciphering complex tissue architecture
29 [14, 15], understanding how cells interact with each other [16, 17], and identifying spatial
30 developmental trajectories in tissues [18, 19].

31 Non-negative matrix factorization (NMF) has proven an appealing approach for analyzing
32 transcriptomic count matrices [20, 21, 22]. For instance, in the context of single-cell RNA-
33 sequencing (scRNA-seq) data analyses, NMF-based methods have the ability to decompose
34 gene expression in individual cells into a set of interpretable gene programs associated with
35 cell-type identities and cellular activities [23, 24]. These methods offer valuable insights, such
36 as unraveling cell states that arise in various perturbations [25, 26]. Most recently, two NMF-
37 based dimension reduction methods, SpiceMix [27] and NSFH [28], were proposed for analyzing
38 complex ST data by capturing spatial dependence of cells. Owing to the decomposition nature
39 of NMFs [29], SpiceMix and NSFH are powerful in deciphering signals within ST data by
40 decomposing them into a collection of interpretable spatial factors, each encoding a unique
41 spatial pattern [27, 28]. These methods excel at uncovering spatial organization of cell identities,

42 identifying spatially variable features, and revealing important biological processes. However,
43 these methods are designed only for interpreting a single ST dataset. The development of
44 interpretable and spatially-aware analytical methods that can effectively integrate multiple
45 diverse ST datasets is in great need and remains a challenge.

46 With advancements in ST technologies, numerous ST studies utilizing different technologies
47 have been conducted, each often generating multiple slices [3, 4]. For instance, ST profiles have
48 been characterized in multiple sagittal and coronal sections from mouse brains [30, 31, 32],
49 and in multiple parallel slices along the left-right axis from a late-stage mouse embryo [8].
50 Multiple ST slices have also been created from mouse embryos at varying developmental
51 time points [8, 33]. Effectively interpreting these diverse ST datasets, both within and across
52 studies, is crucial for establishing a comprehensive understanding of tissue architectures and
53 their developmental dynamics. However, unwanted variations across samples, batches, ST
54 technologies and developmental time points can introduce confounding factors that hinder the
55 discovery of biologically meaningful spatial signals [34, 35]. Consequently, while methods like
56 SpiceMix and NSFH can unveil meaningful spatial factors in a single ST dataset, they face
57 difficulties in distinguishing shared biological signals among datasets from the heterogeneous
58 unwanted variation when applied to multiple ST datasets. This task can become even more
59 challenging if certain datasets contain unique biologically meaningful spatial factors that need
60 to be accurately identified and separated from the unwanted variation [36]. Therefore, there
61 remains a need for computational methods that are specifically designed for joint analyses of
62 multiple diverse ST datasets.

63 Here, we develop INSPIRE, a deep learning-based method that unifies NMF and adversarial
64 learning [37] to achieve interpretable, flexible and spatially-aware integration of ST datasets.
65 INSPIRE leverages graph neural networks [38, 39] to perform spatially informed analyses of ST
66 slices, by accounting for local microenvironments of cells or spatial spots. For joint analyses of
67 multiple datasets, INSPIRE incorporates a tailored adversarial learning mechanism to adaptively
68 distinguish complex unwanted variations across multiple batches, samples, technical platforms
69 and developmental stages from intrinsic biological variations, even when certain datasets present
70 unique biological signals. Hence, INSPIRE can reliably eliminate heterogeneous unwanted
71 variations in its analyses. By seamlessly integrating this adversarial learning mechanism with
72 NMF, INSPIRE enables a harmonized NMF for multiple diverse ST datasets. It allows for

73 the discovery of spatial factors among multiple datasets without confounded by unwanted
74 variations, deciphering detailed spatial organizations in diverse datasets. For these spatial
75 factors, INSPIRE also explicitly models their gene signatures, enabling the interpretation of
76 their biological meanings and the identification of gene programs associated with them.

77 Through the application of INSPIRE to various ST datasets, including human cortex slices
78 from different samples, mouse brain slices prepared at different orientations and resolutions, as
79 well as a collection of whole mouse embryo slices, we demonstrate that INSPIRE can flexibly
80 integrate diverse ST datasets from multiple samples, created by different ST technologies
81 and at varying developmental time points. In these diverse integrative analyses, INSPIRE
82 shows its power to decipher fine-grained spatial architecture with biological meanings, elucidate
83 spatial cell-population distributions, and uncover biological processes organized in complex
84 tissues. Through these applications, we show that INSPIRE is a versatile analytical approach
85 that allows for various downstream analyses. For instance, it enables pathway enrichment
86 analysis, identification of spatially variable genes, detection of spatial trajectories, imputation
87 of spatial gene expressions as well as 3D reconstruction of tissue structures using multiple
88 parallel slices along an axis. Of note, INSPIRE is also scalable to handle large-scale datasets.
89 As a demonstration, we applied INSPIRE to spatiotemporal atlases of mouse organogenesis,
90 comprising half a million high-resolution spatial spots. INSPIRE effectively modeled these
91 atlases, deciphering dynamical changes during mouse embryonic development. INSPIRE is
92 publicly available as a Python package (<https://github.com/jiazhao97/INSPIRE>), offering
93 an efficient and reliable tool for ST data analyses.

94 **Results**

95 **Method overview.**

96 INSPIRE takes gene expression count matrices and spatial coordinates from multiple ST slices
97 as inputs. It effectively integrates information across slices in a shared latent space. In this space,
98 meaningful biological variations from the input slices are preserved, while complex unwanted
99 variations are eliminated (Fig. 1a and panel a1). Utilizing this shared latent space, INSPIRE
100 achieves an integrated NMF on gene expressions across slices, decomposing biological signals in
101 different slices into consistent and interpretable spatial factors with associated gene programs

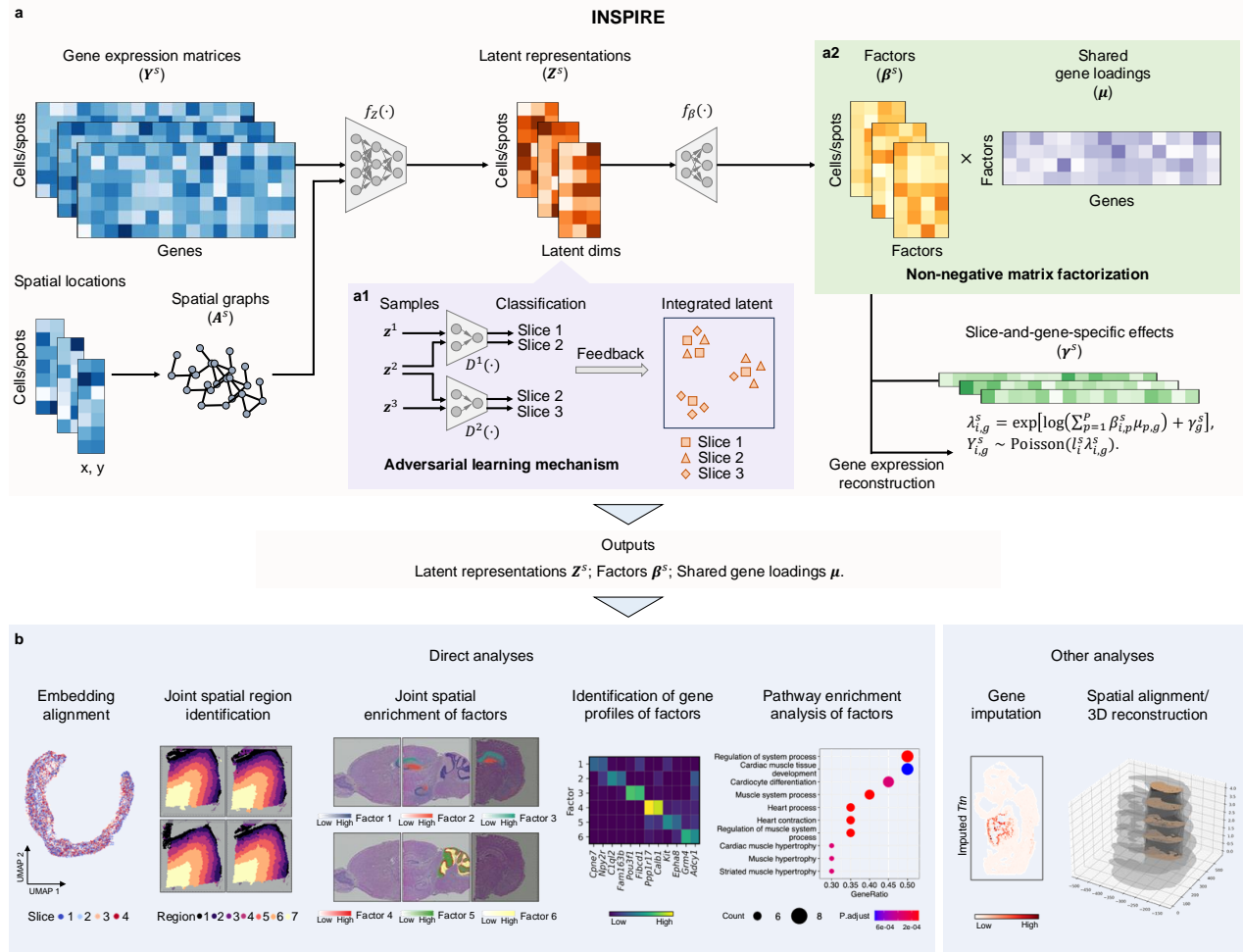


Figure 1: Overview of INSPIRE. **a.** INSPIRE is a unified deep learning method that incorporates adversarial learning and non-negative matrix factorization (NMF) for interpretable integrations of ST datasets. Raw gene expressions and spatial locations from multiple slices are taken as the inputs. **(a1).** INSPIRE embeds the biological variations from ST slices into a shared latent space. By incorporating a tailored adversarial learning mechanism, INSPIRE effectively eliminates unwanted variations in this latent space, providing harmonized representations of cells or spatial spots among slices. **(a2).** The latent space enables INSPIRE to achieve an integrated NMF for multiple slices, further decomposing biological signals into a set of consistent and interpretable factors among slices. Unconfounded by unwanted variations, these spatial factors reveal detailed spatial organizations in multiple ST slices. The gene signatures of these spatial factors are explicitly characterized by the shared gene loading matrix, elucidating their biological meanings. After training, INSPIRE simultaneously outputs integrated latent representations, interpretable spatial factors, and corresponding gene loadings. **b.** INSPIRE's outputs enable multiple downstream analyses, including spatial trajectory inference, identification of fine-grained spatial regions and tissue structures, detection of spatially variable genes, and pathway enrichment analysis for deciphering biological processes in tissues. INSPIRE can also be applied to tasks including gene imputation and 3D reconstruction of tissues with multiple parallel 2D slices.

102 (Fig. 1a and panel a2). The non-negative spatial factors of cells or spatial spots are inferred
103 from their latent representations, where unwanted variations are largely eliminated. Hence,
104 these spatial factors are free from complex unwanted variations, enabling unified discoveries of
105 fine-grained spatial patterns among slices. The gene signatures associated with these spatial
106 factors are captured through shared non-negative gene loadings among slices, enhancing the
107 interpretability of multi-slice integrative analyses.

108 INSPIRE seamlessly incorporates the above designs in a unified deep-learning framework
109 (Fig. 1a). Specifically, it uses a spatially-informed encoder, $f_Z(\cdot)$, to map cells or spatial spots
110 from ST slices $s = 1, 2, \dots, S$ into the shared latent space. This encoder is a graph neural
111 network [38, 39] that takes gene expressions and spatial neighborhood graphs of ST slices as
112 inputs. For any cell or spatial spot i from slice s , the encoder is designed to output its latent
113 representation \mathbf{z}_i^s , unaffected by unwanted variations. INSPIRE achieves this by incorporating
114 a tailored adversarial learning mechanism [34, 37] (Fig. 1a, panel a1). To align $\{\mathbf{z}_i^s\}_i$ from
115 slice s with $\{\mathbf{z}_i^{s+1}\}_i$ from slice $s + 1$, an auxiliary discriminator network, $D^s(\cdot)$, is deployed in
116 the latent space to detect where poor mixing between $\{\mathbf{z}_i^s\}_i$ and $\{\mathbf{z}_i^{s+1}\}_i$ occurs. Its feedback
117 then guides encoder $f_Z(\cdot)$ to improve the alignment. The discriminator can adaptively preserve
118 slice-specific signals by only guiding $f_Z(\cdot)$ to integrate shared biological variations between
119 slices. By introducing $S - 1$ discriminators, including $D^s(\cdot)$, $s = 1, 2, \dots, S - 1$, INSPIRE
120 effectively harmonizes all S slices in the shared latent space.

121 Next, INSPIRE adopts an integrated NMF across slices to further decompose the biological
122 signals in the shared latent space into a set of interpretable spatial patterns with gene programs
123 (Fig. 1a, panel a2). This provides characterizations of tissue structures at a finer-grained
124 level and with enhanced interpretability. The integrated NMF includes non-negative spatial
125 factor matrices $\{\beta^s\}_s$ for the multiple slices, and a shared non-negative gene loading matrix, μ ,
126 among slices. For any cell i in slice s , β_i^s presents the set of non-negative weights across the
127 hidden spatial factors it contains. The sum of the non-negative weights of spatial factors for any
128 given cell equals to one. The contributions of different genes to diverse hidden spatial factors
129 are explicitly encoded by the non-negative weights in μ , revealing gene programs associated
130 each detailed spatial pattern. Two unique designs in INSPIRE enable its integrated NMF
131 across slices. First, INSPIRE uses a decoder network, $f_\beta(\cdot)$, to generate spatial factors $\{\beta_i^s\}_{s,i}$
132 directly from integrated representations $\{\mathbf{z}_i^s\}_{s,i}$ in the latent space. This ensures that $\{\beta_i^s\}_{s,i}$

133 only decompose meaningful biological signals among slices, as the unwanted variations are
134 removed in $\{\mathbf{z}_i^s\}_{s,i}$. Second, INSPIRE introduces additional slice s -and-gene g -specific effects
135 γ_g^s to help explicitly model confounding signals. Therefore, $\{\beta_i^s\}_{s,i}$ and $\boldsymbol{\mu}$ can efficiently fit the
136 biological signals, decomposing these key signals into a set of detailed spatial factors with their
137 associated gene modules that are consistent among slices.

138 INSPIRE formulates the learning of encoder network $f_Z(\cdot)$, decoder network $f_\beta(\cdot)$, and gene
139 loading matrix $\boldsymbol{\mu}$ into a unified optimization problem. After training, INSPIRE simultaneously
140 outputs integrated latent representations $\{\mathbf{Z}^s\}_s$, spatial factors $\{\beta^s\}_s$, and interpretable gene
141 loadings $\boldsymbol{\mu}$. The outputs enable comprehensive characterizations of tissue structures through
142 various downstream analyses (Fig. 1b). These include the identification of spatial trajectories
143 and major spatial regions using $\{\mathbf{Z}^s\}_s$; the discovery of detailed tissue architectures, spatial
144 distributions of cell types, and the organization of biological processes using $\{\beta^s\}_s$; and the
145 detection of spatial variable genes, the identification of gene modules, along with pathway
146 enrichment analysis using $\boldsymbol{\mu}$. Details are included in the Methods section.

147 **INSPIRE offers superior accuracy and interpretability for the inte-** 148 **grative analysis of multiple ST datasets.**

149 In this section, we first demonstrate that by integrating adversarial learning with NMF for joint
150 modeling of multiple ST slices, INSPIRE can achieve superior accuracy in capturing biological
151 signals across slices. This advantage allows INSPIRE to produce improved results for the
152 identification of spatial regions, which is critical in ST data analysis. Additionally, we highlight
153 that INSPIRE can model gene programs that characterize detailed spatial organization patterns
154 in tissues, enhancing the interpretability of multi-slice integrative analysis.

155 We applied INSPIRE to a human dorsolateral prefrontal cortex (DLPFC) dataset run on the
156 Visium platform [40]. This dataset contains four DLPFC tissue slices, indexed 151673-151676,
157 from a neurotypical adult donor. Researchers have manually annotated six DLPFC layers
158 (L1-L6) and white matter (WM) for each slice based on cytoarchitecture and gene markers [40].

159 We first focused on analyzing the spot representations obtained in INSPIRE's latent space.
160 In this space, information across slices was effectively integrated, while different cortical layers
161 were still well separated (Fig. 2a). Importantly, the spot representations revealed a clear
162 trajectory from L1 to L6 and WM that is shared among slices. The identified trajectory aligns

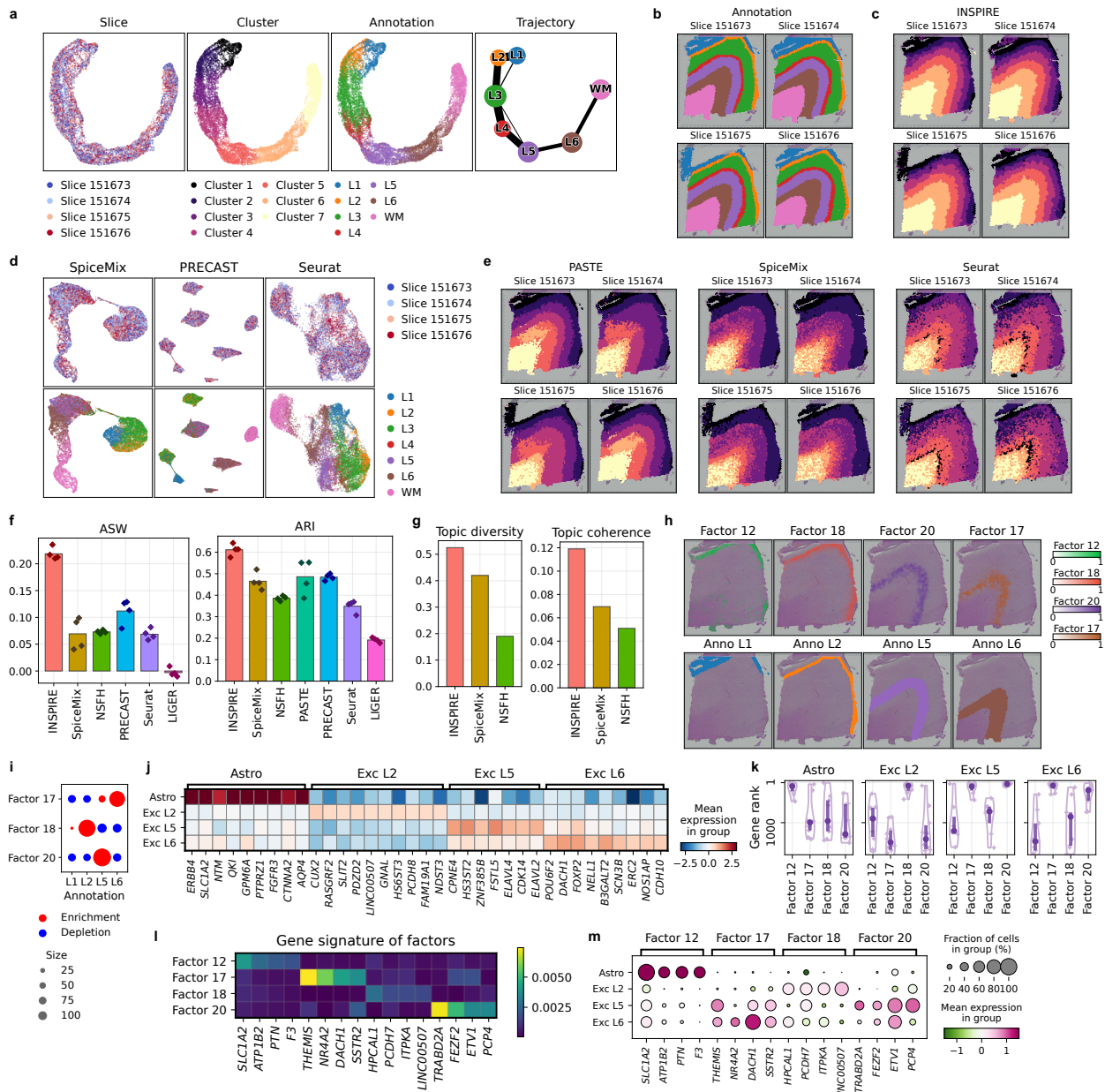


Figure 2: Benchmarking of INSPIRE and state-of-the-art methods based on the human DLPFC dataset. **a.** UMAP plots of spot representations from INSPIRE, colored by slice indices, INSPIRE’s assigned spatial domain labels, and manual annotations. The PAGA algorithm was applied to the spot representations for spatial trajectory inference. **b.** Manual annotations on slices. **c, e.** Spatial domain identification results from INSPIRE (**c**), PASTE, SpiceMix, and Seurat (**e**). **d.** UMAP plots of spot representations from SpiceMix, PRECAST and Seurat, colored by slice indices and manual annotations. **f.** ASW and ARI scores of the benchmarked methods. **g.** Factor diversity and factor coherence scores of the benchmarked methods. **h.** Spatial distributions of factors 12, 18, 20 and 17 identified by INSPIRE on slice 151673. **i.** Enrichment or depletion of different spatial factors in cortical layers. **j, k.** We identified marker genes for four cell types using a scRNA-seq atlas (**j**), and visualized the rank distribution of them in different spatial factors (**k**). **l.** Spatial factor-specific genes identified by INSPIRE. **m.** Expression levels of the factor-specific genes among cell types.

163 with corticogenesis, during which cortical neurons are born in a successive order from outer to
164 inner layers [41], showing INSPIRE’s ability to distill meaningful biological variation among
165 slices. The effective preservation of biological signals in the latent space enables INSPIRE to
166 reliably identify spatial regions in tissues. Using spot representations, INSPIRE effectively
167 recovered the layer structures among all DLPFC slices (Fig. 2c). This result shows a consistent
168 pattern compared to manual annotation, indicating INSPIRE’s high reliability in spatial domain
169 identification (Fig. 2b, c).

170 For a quantitative evaluation of INSPIRE’s spot representation and spatial domain identifi-
171 cation, we used the manual annotations as ground truth and adopted three metrics: average
172 silhouette width (ASW), adjusted rand index (ARI), and normalized mutual information (NMI).
173 ASW measures the conservation of different annotated layers in spot representations, while
174 ARI and NMI assess the accuracy of spatial domain identification by comparing it to the
175 manual annotations. Higher scores on these metrics indicate better performance. To benchmark
176 INSPIRE against existing tools, we compared it to representative state-of-the-art methods
177 applicable for producing spot representations or identifying spatial domains in this analysis,
178 including Seurat [42], LIGER [22], SpiceMix [27], NSFH [28], PRECAST [35], and PASTE [43].
179 INSPIRE achieved superior performance compared to all the other methods, reflected by the
180 highest scores for all three metrics (Fig. 2f and Supplementary Fig. 2). In contrast, scRNA-seq
181 data integration methods Seurat and LIGER showed less satisfactory results across all three
182 scores due to their lack of consideration for spatial information (Fig. 2e, f and Supplementary
183 Fig. 3). Two spatially-informed data integration methods, PASTE and PRECAST, had better
184 performance compared to Seurat and LIGER, illustrating the importance of spatial coordinate
185 modeling. However, PASTE could not provide spot representations across slices, and its spatial
186 domain identification results were inconsistent across slices (Fig. 2e). PRECAST incorrectly
187 mixed spots from layers L4 and L5, and showed limited ability to preserve the continuous
188 trajectory among cortical layers (Fig. 2d). SpiceMix and NSFH are two spatially-aware
189 NMF-based methods for ST data analysis, designed to handle one ST slice at a time. We
190 manually concatenated the four slices to form one ST slice to apply these methods. Both
191 methods successfully uncovered the spatial trajectory among layers, indicating their ability
192 to capture biological signals (Fig. 2d and Supplementary Fig. 1). However, compared to
193 INSPIRE, they both showed less satisfactory performance across all three metrics, suggesting

194 their limited ability to leverage information across slices for achieving improved results (Fig.
195 **2f**, Supplementary Figs. 2 and 3).

196 So far, we have demonstrated the superior performance of INSPIRE in learning spot
197 representations. We note that the gained accuracy in the latent space is contributed by the
198 NMF component in INSPIRE. For illustration, we manually removed the NMF component
199 from INSPIRE, and denoted this version as “INSPIRE (w/o NMF)”. Compared to INSPIRE
200 (w/o NMF), INSPIRE’s spot representation consistently showed higher scores for all three
201 metrics ASW, ARI, and NMI (Supplementary Fig. 4). This demonstrates the effectiveness of
202 INSPIRE’s integration of the shared latent space with the NMF model.

203 Next, we focused on analyzing the spatial factors and the associated gene loading in the
204 NMF across slices from INSPIRE. To quantitatively evaluate the quality of spatial factors, we
205 employed two metrics: factor diversity and factor coherence [44]. Factor diversity measures the
206 percentage of unique genes associated with each factor, with a higher diversity score indicating
207 more varied factors. Factor coherence evaluates the interpretability of factors by assessing
208 the co-expression of genes associated with the same factor across spots. A higher coherence
209 score indicates better interpretability of spatial factors. Using these two metrics, we compared
210 the performance of INSPIRE to NMF-based methods SpiceMix and NSFH. As shown by the
211 highest scores for both metrics, INSPIRE achieved superior factor quality compared to other
212 methods (Fig. **2g**).

213 Besides quantitative evaluation, we also visualized INSPIRE’s spatial factors to illustrate
214 their ability to decipher detailed spatial organization patterns among slices. For instance,
215 three factors (factors 18, 20, and 17) showed clear enrichment in cortical layers L2, L5, and
216 L6, respectively (Fig. **2h, i**). By exploring their gene loadings from INSPIRE, we found their
217 correspondence to excitatory neuronal subtypes specific to L2, L5, and L6, respectively. To be
218 specific, we identified marker genes for these neuronal subtypes using an external scRNA-seq
219 atlas (Fig. **2j**). These marker genes showed top rankings in the gene loadings of these factors
220 (Fig. **2k**; the Methods section), confirming the biological meanings of the factors. Additionally,
221 with the interpretable gene loadings, INSPIRE is able to unveil variable genes that are associated
222 with the spatial factors, offering the biological insights. For example, genes specific to the
223 three factors were identified (Fig. **2l**; the Methods section) and their reliability was validated
224 (Fig. **2m**). Unlike INSPIRE, which uncovered neuronal subtypes in detailed cortical layers,

225 SpiceMix only captured broad layer structures with its factors (Supplementary Figs. 5 and
226 6). For example, its factor 14 described a mixture of multiple layers, including L4, L5, and
227 L6. Consistent with its relatively low factor quality scores, NSFH's factors did not present
228 clear spatial structures in the tissue (Supplementary Fig. 7). Notably, beyond cortical layers,
229 INSPIRE also depicted other detailed spatial structures. For instance, INSPIRE revealed
230 the spatial distribution of astrocytes, with the gene signature of factor 12 characterizing the
231 gene expression profile of astrocytes (Fig. 2j-m). This demonstrated that INSPIRE identified
232 the spatial organization in the tissue that is not covered by manual layer annotation, further
233 highlighting INSPIRE's ability to decipher fine-grained and interpretable spatial structures
234 using spatial factors and gene loadings.

235 **Precise stitching of multiple sagittal and coronal mouse brain slices** 236 **with partially shared spatial structures.**

237 In this section, we evaluate INSPIRE's performance in a more challenging scenario compared to
238 our previous benchmarking study: integrating multiple slices from different samples, where the
239 spatial structures only partially overlap. This situation presents a unique challenge in learning
240 spot representations and spatial factors, as it requires methods to adaptively identify and align
241 shared biological variations among the slices, while preserving signals unique to each slice and
242 accounting for batch effects.

243 To explore the complex architecture of the brain, 10x Genomics created Visum slices in
244 both sagittal and coronal planes. Due to the size restriction on the captured area, the sagittal
245 plane was further dissected into two sections, each profiled in an individual ST slice. In total,
246 there are three ST brain slices: the sagittal anterior [30], sagittal posterior [31], and coronal
247 slices [32]. Brain structures captured in these ST slices are only partially shared. For instance,
248 while all the three slices contain the isocortex, the main olfactory bulb is unique to the sagittal
249 anterior slice, and the cerebellum is unique to the sagittal posterior slice. We used INSPIRE to
250 jointly model the three slices, merging data collected from distinct views of the brain.

251 When applied to this task, INSPIRE effectively depicted the mouse brain architecture.
252 After INSPIRE's integration, the representations of spatial spots were correctly aligned across
253 the three slices in the latent space (Fig. 3b). By clustering the spot representations, INSPIRE
254 was able to partition the mouse brain into 36 distinct and well-organized spatial regions (Fig.

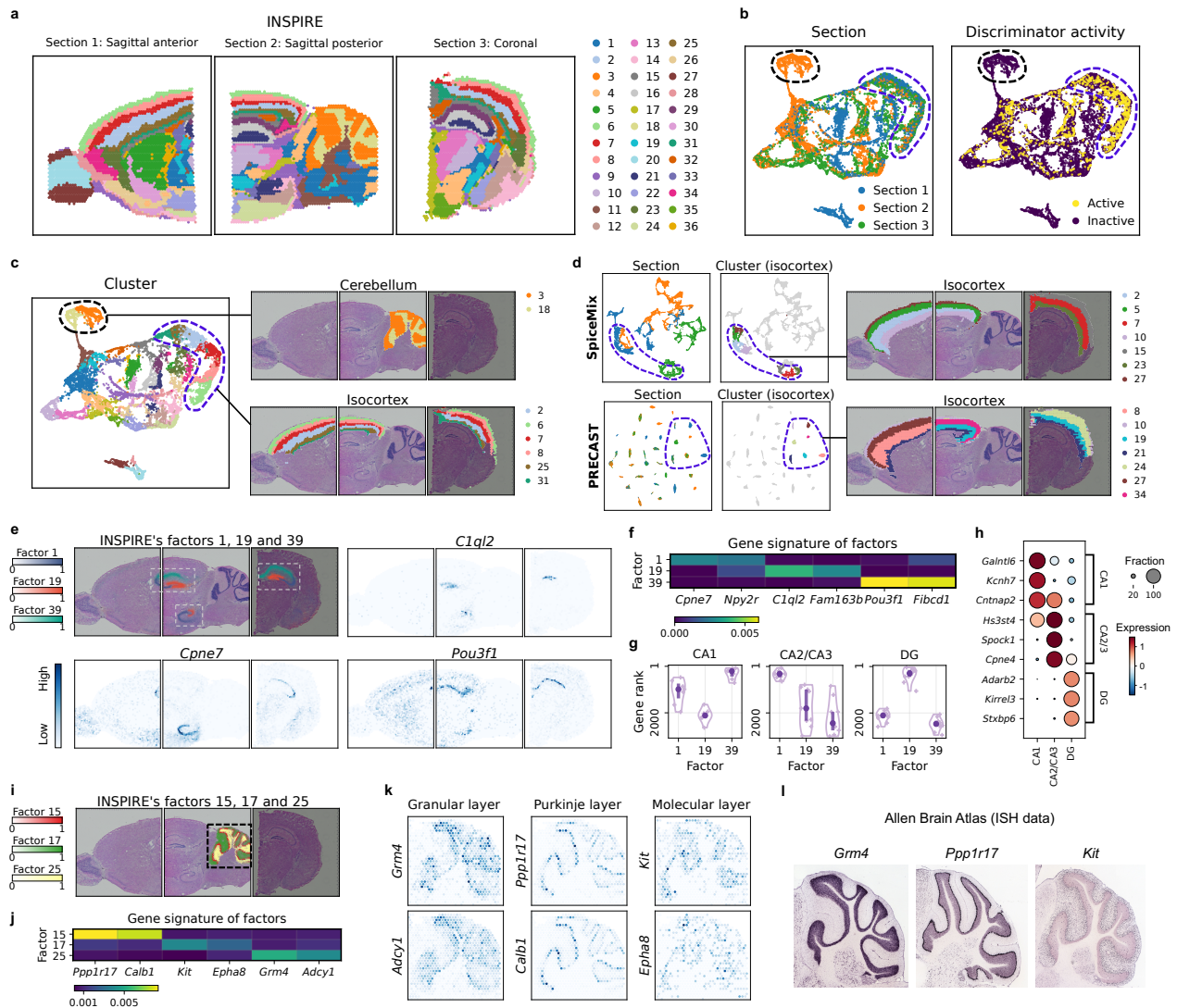


Figure 3: Analysis of multiple mouse brain ST slices with only partially shared spatial tissue organizations. INSPIRE integrated sagittal anterior, sagittal posterior and coronal sections of mouse brains. **a**. Spatial clusters visualized on the three ST slices. **b**. UMAP plots of spot representations from INSPIRE, colored by slice indices and discriminator activities. INSPIRE's discriminators were active on the spots describing the shared spatial structures across slice, while they were inactive on spots related to the slice-unique structures. Thereby, they adaptively guided INSPIRE to align shared variations among slices, while preserving slice-unique signals. **c**. Spatial regions 3 and 18 from INSPIRE characterized the cerebellum. Spatial regions 2, 6, 7, 8, 25 and 31 characterized layers in the isocortex. **d**. UMAP plots of spot representations from SpiceMix and PRECAST, and visualizations of their spatial clusters in the isocortex. **e, f**. Spatial distributions of factors 1, 19 and 39 identified by INSPIRE (**e**). Based on the learned gene signatures (**f**), INSPIRE identified spatially variable genes associated with the three factors respectively (**e**). **g, h**. We identified marker genes of CA1, CA2/3 and DG using a scRNA-seq atlas (**h**), and visualized the rank distribution of them in gene loadings of the three factors (**g**). **i, j**. Spatial distributions (**i**) and gene signatures (**j**) of factors 5, 17 and 25 respectively. **k**. Top spatially variable genes associated with each of the three factors identified by INSPIRE. **l**. ISH images of genes *Grm4*, *Ppp1r17* and *Kit* from Allen Brain Atlas.

255 **3a**). Among these clusters, six layer-structured spatial domains with labels 2, 6, 7, 8, 25,
256 and 31 together formed the isocortex region shared across the three brain slices (Fig. **3b, c**).
257 Importantly, INSPIRE also successfully preserved slice-unique tissue structures such as the
258 cerebellum, characterized by spatial regions 3 and 18 in the sagittal posterior slice, and the
259 main olfactory bulb, characterized by spatial regions 20 and 27 in the sagittal anterior slice
260 (Fig. **3b, c**). In contrast, SpiceMix, NSFH, and PRECAST, which performed relatively well
261 in the human DLPFC-based benchmarking study, produced results that were confounded by
262 strong batch effects and intrinsic differences among the slices (Fig. **3d** and Supplementary
263 Fig. 12), highlighting their limited applicability in creating a comprehensive tissue ST atlas
264 through the integration of slices with partial overlap. For instance, none of these methods
265 successfully described the shared cortical layers among the multiple mouse brain slices (Fig.
266 **3d**, Supplementary Figs. 9, 10, and 11).

267 In this example, we also confirmed that INSPIRE's designed discriminators (the Methods
268 section) indeed adaptively distinguished between shared biological signals among slices and
269 slice-unique signals, facilitating INSPIRE's adaptive data integration. In the latent space,
270 discriminators were active for spot populations shared among slices, such as spots in the
271 isocortex (Fig. **3b, c**), encouraging their alignment across slices. Conversely, discriminators
272 were found inactive for slice-specific spot populations, such as spots in the cerebellum (Fig. **3b,**
273 **c**), helping preserve their identities.

274 Next, we investigated the spatial factors inferred by INSPIRE. Each of them provided a
275 unique and detailed description of the spatial organization in the brain (Supplementary Fig.
276 13). For instance, the spatial distributions of different hippocampal neuron types in the brain,
277 which are concentrated mainly in the curve-shaped CA1, CA2/CA3, and DG subregions of
278 the hippocampus, were depicted by spatial factors 1, 19, and 39. This observation aligns well
279 with the reference from the Allen Reference Atlas – Mouse Brain [45] (Fig. **3e**, Supplementary
280 Figs. 16, 17). The gene loadings for spatial factors 1, 19, and 39 also corresponded with marker
281 genes for these hippocampal neuron types identified in an external scRNA-seq atlas [46] (Fig.
282 **3h**). Using these factors, we were able to identify specific regional markers, such as *C1ql2* and
283 *Fam163b* for CA1; *Cpne7* and *Npy2r* for CA2/CA3; and *Pou3f1* and *Fibcd1* for DG (Fig. **3e,**
284 **f**). Furthermore, we showed that INSPIRE excels at capturing detailed spatial organization
285 unique to individual sections by spatial factors. One example is that, non-negative weights

286 (proportions) of spatial factors 15, 17, and 25 on spots revealed spatial distributions of neurons
287 specific to the molecular layer, the Purkinje layer, and the granular layer in the cerebellum,
288 respectively. Using the associated gene signatures, spatially variable genes specific to each of
289 these fine-grained layers were identified, such as *Grm4*, *Adcy1* for the granular layer; *Ppp1r17*,
290 *Calb1* for the Purkinje layer; and *Kit*, *Epha8* for the molecular layer (Fig. 3j, k). The spatial
291 specificity of these genes was confirmed by in situ hybridization (ISH) data from the Allen
292 Brain Atlas (Fig. 3l), providing additional support for the high quality and interpretability of
293 INSPIRE’s results.

294 Unlike INSPIRE, both SpiceMix and NSFH produced results that were less satisfactory
295 due to the confounding of their inferred spatial factors by strong batch effects across sections
296 (Supplementary Figs. 14 and 15). Additionally, NSFH showed limited capability in characteriz-
297 ing detailed spatial structures, as evidenced by the lack of clear spatial patterns in its learned
298 factors (Supplementary Fig. 15). This challenging task demonstrates the superior performance
299 and broad applicability of INSPIRE for integrating ST slices with batch effects and a very low
300 degree of spatial overlap, outperforming all other tools.

301 **INSPIRE integrates ST data from different ST technologies, facilitat-** 302 **ing multiple downstream analyses.**

303 Different ST technologies and platforms produce data with varying spatial resolutions and
304 sequencing depths [3, 4]. In this section, we demonstrate INSPIRE’s performance in integrating
305 data from different ST technologies, leveraging the strengths of each technology to enhance
306 biological insights.

307 We first collected mouse brain ST datasets from Slide-seq V2 [7] and MERFISH [47]. The
308 Slide-seq V2 dataset contains expression measurements of over 20,000 genes, with a near-cellular
309 spatial resolution of 10 μm , where each barcoded bead typically captures one to two cells. In
310 contrast, the MERFISH dataset measures gene expression levels in individual cells but covers
311 only 1,122 genes. Before integration, we applied the standard Scanpy workflow [48] to each of
312 these datasets. The Slide-seq V2 data failed to recover known layer structure in the isocortex
313 (Fig. 4a). Conversely, the MERFISH data successfully revealed this structure, indicating its
314 higher data quality for annotating spatial regions (Supplementary Fig. 18). Aligning these
315 two datasets helps to combine the better spatial organization characterization from MERFISH

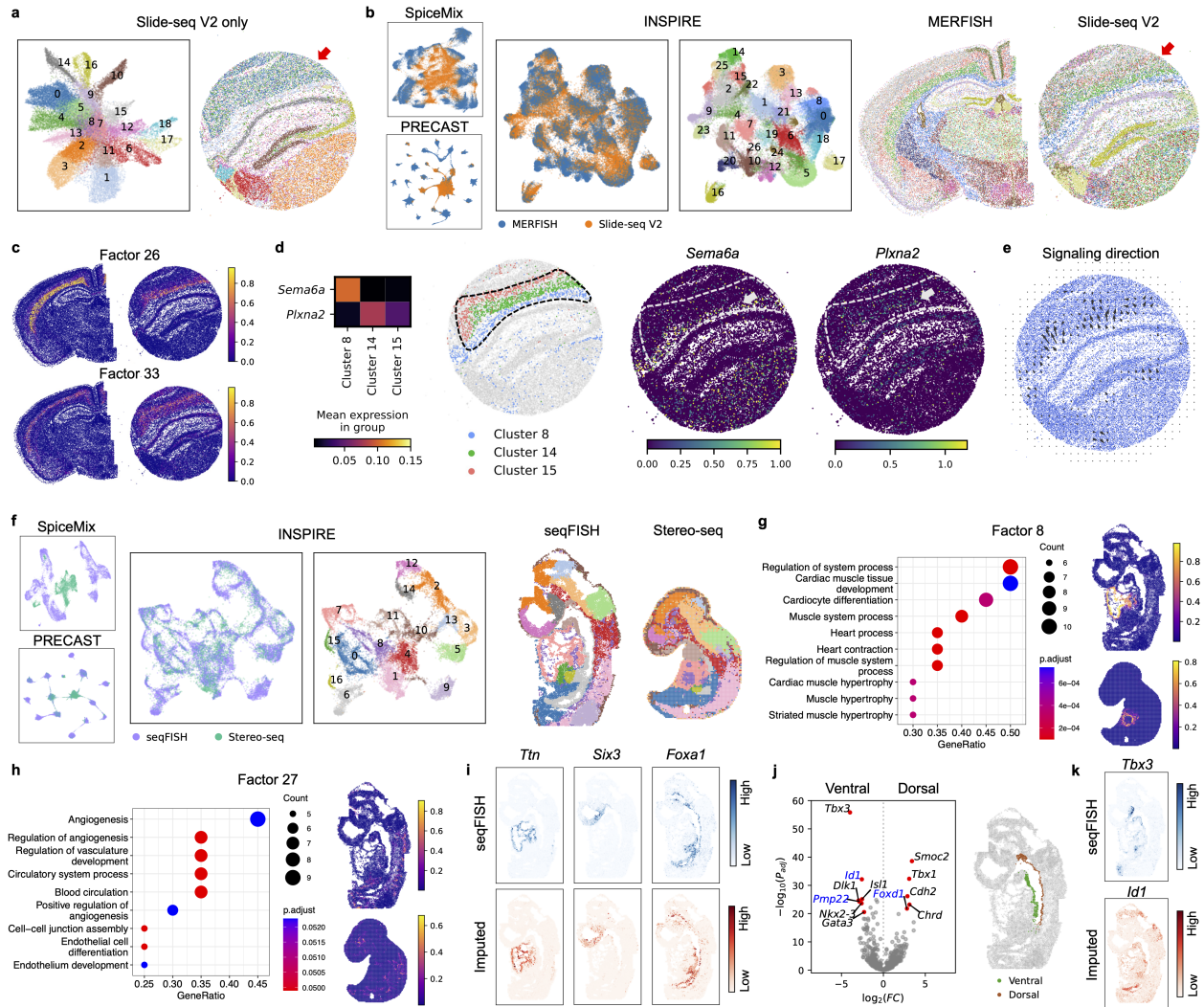


Figure 4: Integrative analyses of data from different ST technologies to enhance biological insights. **a.** Spatial domain identification from the analysis of Slide-seq V2 data alone. **b.** Cell representations aligned between the MERFISH and Slide-seq V2 datasets using SpliceMix, PRECAST, INSPIRE, and spatial domain identification result from INSPIRE. **c.** Spatial distributions of INSPIRE's factors 26 and 33. **d.** Expressions of genes *Sema6a*, *Plxna2* among INSPIRE's identified spatial regions 8, 14 and 15. **e.** Signaling direction from ligand *Sema6a* to receptor *Plxna2* across INSPIRE's annotated regions inferred by the COMMOT method. **f.** Cell representations aligned between the seqFISH and Stereo-seq embryo datasets using SpliceMix, PRECAST, INSPIRE, and spatial domain identification result from INSPIRE. **g, h.** Significant gene ontology terms and spatial distributions of INSPIRE's factors 8 (**g**) and 27 (**h**). **i.** We manually held out genes from the seqFISH dataset and imputed their expressions from the Stereo-seq dataset to show INSPIRE's gene imputation capability. We visualized the expressions of *Ttn*, *Six3* and *Foxa1* measured by seqFISH (top panel), and compared them with the imputed expression levels (bottom panel). **j.** Differentially expressed gene analysis between the ventral and dorsal sides of the developing gut tube in the seqFISH dataset. Top differentially expressed genes with imputed expression levels from INSPIRE are annotated in blue, and top differentially expressed genes with expression levels quantified by seqFISH are annotated in black. **k.** *Tbx3* expression levels measured by seqFISH, and *Id1* expression levels imputed by INSPIRE.

316 with the transcriptome-wide measurement from Slide-seq V2. However, prior to integration,
317 the two datasets showed strong discrepancies, making their integration a challenging task
318 (Supplementary Fig. 19).

319 Despite the challenge, INSPIRE effectively eliminated confounding technical noises in its
320 cell representations, enabling the identification of spatial regions consistent across the two
321 datasets (Fig. 4b). For example, it identified three different hippocampal regions (clusters 9,
322 16, and 23), and three broad cortical layers (clusters 2, 14 and 15). INSPIRE's spatial factors
323 revealed additional spatial structures at a finer granularity. Specifically, spatial factors 11, 15,
324 26, 27, 29, and 33 delineated six highly detailed cortical layers in both datasets, unaffected
325 by the strong technical effects (Fig. 4c and Supplementary Fig. 23). A notable achievement
326 was INSPIRE's ability to call out the hidden cortical layer structure within the Slide-seq V2
327 data by leveraging information from the MERFISH data (Fig. 4a-c). To demonstrate how this
328 facilitates downstream biological analyses, we utilized the COMMOT method [16] to screen
329 for cell-cell communications among INSPIRE's identified cortical layers and nearby regions in
330 the Slide-seq V2 data. Such analysis revealed interactions that were undetectable using the
331 MERFISH data alone, due to its limited number of profiled genes. For example, MERFISH did
332 not capture gene *Plxna2*. However, the integrative analysis enabled COMMOT to identify a
333 signaling direction from ligand *Sema6a* to receptor *Plxna2* cross INSPIRE's annotated regions
334 (Fig. 4d, e). Among them, *Sema6a* was enriched in fiber tracts (cluster 8), while *Plxna2*
335 was highly expressed in the inner cortical layer (cluster 14) with decreasing expression in the
336 adjacent cortical layer (cluster 15). This *Sema6a*-*Plxna2* interaction suggests potential cell
337 migration and neuronal connectivity around the inner cortical layer area of the brain [49].

338 As a comparison, other methods including SpiceMix, NSFH and PRECAST performed
339 less satisfactorily in this challenging task. Their results including representation of cells,
340 identification of spatial domains and/or spatial factors were still severely confounded by the
341 unwanted technical effects (Fig. 4b, Supplementary Figs. 20, 21, 22 and 25). Additionally,
342 SpiceMix's factors did not show clear spatial distributions in any dataset, lacking the ability to
343 uncover spatial organization patterns in this analysis (Supplementary Fig. 24).

344 Next, we collected two mouse whole-embryo slices generated by seqFISH [33] and Stereo-seq
345 [8] respectively, and applied INSPIRE to jointly analyze them. Similar to previous cross-
346 technology data example, these datasets exhibited clear discrepancies due to strong technical

347 effects prior to integration (Supplementary Fig. 26). Nevertheless, INSPIRE successfully aligned
348 cell embeddings between the two datasets after data integration (Fig. 4f). This alignment
349 facilitated the detection of 16 well-organized and biologically meaningful spatial domains
350 consistent between the two mouse embryos (Fig. 5f). For instance, cluster 1 corresponded to
351 developing hearts, while cluster 2 described the midbrains in both embryo datasets. Additionally,
352 INSPIRE's spatial factors allowed for more detailed spatial characterization of the embryos
353 (Supplementary Fig. 30). For example, spatial factors 6 and 8 accurately delineated subregions
354 within the embryonic hearts, including the atria and ventricles (Fig. 4g and Supplementary
355 Fig. 33). Spatial factor 27 was ubiquitously distributed in both embryos. Through gene
356 ontology (GO) analysis of genes related to factor 27, we found it depicted meaningful biological
357 processes such as angiogenesis, vasculature development, and circulatory system processes in
358 both datasets (Fig. 4h).

359 Through this example, we show that INSPIRE's effective data integrative analysis (Sup-
360 plementary Fig. 34) enables accurate information transfer across datasets, facilitating deeper
361 biological understanding. To validate this, we manually held out six genes from the seqFISH
362 dataset, which includes only 351 genes in total. These held-out genes included cardiomyocyte
363 markers *Ttn* and *Popdc2* [50, 51], brain markers *Six3* and *Lhx2* [52, 53], and gut endoderm
364 markers *Foxa1* and *Cldn4* [54, 55]. Using INSPIRE, we imputed spatially-resolved expression
365 levels of these genes from the Stereo-seq dataset. The imputed gene expressions showed consis-
366 tent patterns with the measured expression levels, highlighting INSPIRE's effective integrative
367 analysis even with a limited number of genes (Fig. 4i and Supplementary Fig. 35). After
368 validating INSPIRE's gene imputation capability, we extended this approach to impute all
369 genes from the Stereo-seq dataset for cells in the seqFISH dataset, increasing the number of
370 genes in the seqFISH dataset from 351 to over 20,000. This comprehensive gene imputation
371 enabled a detailed exploration of gene expression differences between the dorsal and ventral
372 parts of the developing gut tube, which were clearly separated only in the seqFISH dataset
373 (Fig. 4j). Based on *t*-test results, the top differentially expressed genes on the dorsal side
374 include *Smoc2*, *Tbx1*, *Cdh2*, *Chrd*, and *Foxd1*, while the top genes enriched on the ventral side
375 include *Tbx3*, *Id1*, *Isl1*, *Dlk1*, *Pmp22*, *Nkx2-3*, and *Gata3* (Fig. 4j). Dorsal-ventral patterning
376 of the gut tube is essential for the separation of the dorsal esophagus and the ventral trachea in
377 mouse embryos [56, 57]. Consistent with a previous study of mouse embryo [58], genes known

378 to be upregulated in the esophagus, such as *Foxd1*, were detected to be highly expressed on the
379 dorsal side of the gut tube. Similarly, genes upregulated in the trachea, including *Tbx3*, *Id1*,
380 and *Isl1*, were identified as enriched on the ventral side. This supports the reliability of our
381 analysis of dorsal-ventral differential gene expressions. Notably, among the identified genes,
382 the expression levels of *Id1*, *Pmp22*, and *Foxd1* were imputed using INSPIRE (Fig. 4j, k),
383 underscoring INSPIRE's ability to facilitate biological discoveries.

384 To compare the performance of INSPIRE to other methods, we also applied SpiceMix,
385 NSFH, and PRECAST to this cross-technology data analysis. However, consistent with the
386 results from previous cross-technology data example, all these methods had difficulties to
387 account for strong unwanted discrepancies between datasets caused by technical effects, leading
388 to less satisfactory integrative analyses (Fig. 4f, Supplementary Figs. 27, 28, 29, 31 and
389 32). The comparison between INSPIRE and these methods further demonstrated the superior
390 performance and wide applicability of the INSPIRE method.

391 **INSPIRE creates a comprehensive mouse organogenesis atlas, en-** 392 **abling spatiotemporal analysis of embryonic development.**

393 Understanding how a complex organism develops over time and space is a fundamental
394 problem in developmental biology. Recently, mouse whole-embryo slices were collected at
395 eight developmental stages, spanning from embryonic day 9.5 (E9.5) to day 16.5 (E16.5) [8].
396 To investigate the spatiotemporal dynamics of organogenesis, we applied INSPIRE to jointly
397 analyze this collection of ST slices across different developmental time points.

398 These eight ST slices were profiled using high-resolution technology Stereo-seq, with each
399 slice containing numerous spatial spots measuring 25 μm in diameter. For example, the ST
400 slices sampled at E14.5, E15.5, and E16.5 each included over 100,000 spatial spots. In total,
401 the eight whole-embryo slices encompass more than half a million spatial spots. Analyzing this
402 spatiotemporal dataset presents new challenges for computational methods: it requires not
403 only precise alignment of eight complex slices across various developmental stages, but also
404 demands high efficiency and scalability to manage over half a millions spatial spots.

405 INSPIRE is scalable to handle this challenging task, and completed the analysis in 80
406 minutes. It successfully aligned the eight ST slices in its latent space, accommodating the
407 extreme large number of spatial spots and varying embryo sizes (Fig. 5a). This alignment

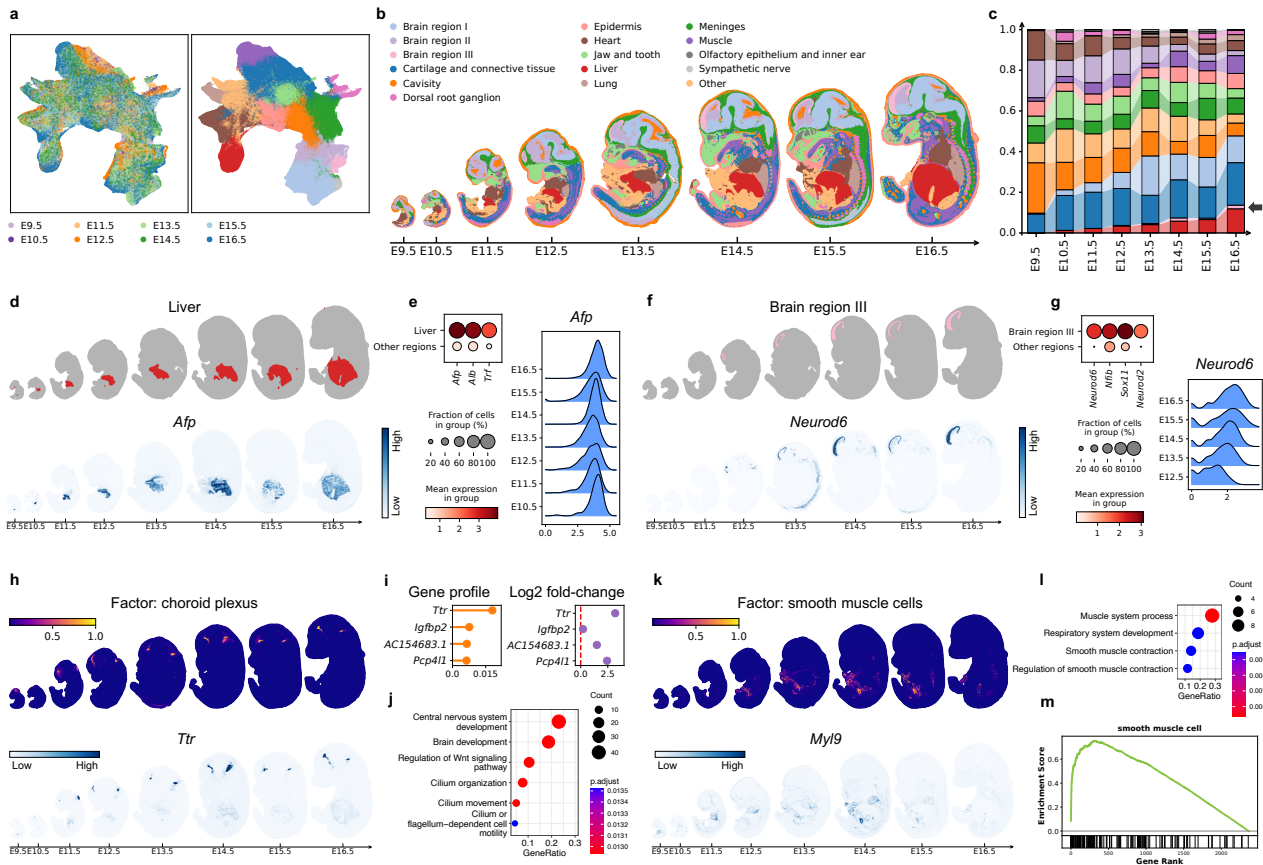


Figure 5: Construction of the spatiotemporal mouse organogenesis atlas by integrating whole-embryo ST slices across various developmental stages. **a.** UMAP plots of spot representations, colored by slice indices and spatial domain labels assigned by INSPIRE. **b.** Visualization of the identified spatial domains across slices. **c.** For each developmental stage, we visualized the proportions of the embryo occupied by different spatial regions. **d, e.** Visualization of the liver region (**d**) and the expression patterns of liver marker genes (**e**). **f, g.** Visualization of a brain region (**f**) and the expression pattern of its differentially expressed genes (**g**). **h, i.** Spatial distribution of the factor representing the choroid plexus (**h**) and its gene signature (**i**). The gene profile indicates the expression levels of genes for this factor. The log₂-fold change measures the difference between gene expressions in this factor and other factors. **j.** GO analysis for the genes specific to the factor in **h**. **k.** Spatial distribution of the factor related to smooth muscle cells and the spatial expression pattern of a smooth muscle cell marker gene. **l.** GO analysis for the genes specific to the factor in **k**. **m.** Gene set enrichment analysis comparing genes related to the factor in **k** with the marker gene set for smooth muscle cells.

408 enabled INSPIRE to identify biologically meaningful spatial regions that consistently localized
 409 across all eight embryonic stages. These regions corresponded to major organs or tissues, such
 410 as heart, liver, lung, and brain (Fig. 5b). Their spatial locations aligned with the known
 411 anatomical structure of the mouse embryo [59]. The identities of these regions were further
 412 validated by analyzing the expression levels of specific marker genes, such as *My17* for heart,

413 *Afp* for liver, *Sftpc* for lung [8], and *Six3*, *Lhx2*, *Otx2*, and *Pou3f1* for brain [52, 60], across all
414 developmental time points (Fig. 5b, d, and Supplementary Fig. 36).

415 Using the well-annotated spatial regions identified by INSPIRE, we visualized the changes
416 in proportions of spatial spots covered by the corresponding organs or tissues within embryos
417 across developmental stages, providing insights into embryo developmental dynamics (Fig. 5c).
418 The liver, initially occupying a very small area at the earliest stage E9.5, rapidly increased its
419 proportion within the embryo as development progressed (Fig. 5c, d, e). In contrast, the heart
420 was already well-structured at early stages E9.5 and E10.5, with its size remaining relatively
421 stable in subsequent stages (Supplementary Figs. 36 and 37), consistent with its role as the
422 first functional organ to form in the embryo [61]. Importantly, this analysis also highlighted
423 organs or tissues that were barely formed at earlier stages but became well developed in later
424 embryonic stages. For example, the shape of the lung became clear after stage E12.5, aligning
425 with the observed increase in the expression of the lung marker gene after E12.5 (Supplementary
426 Figs. 36 and 38). This finding is consistent with the fact that although lung buds begin to form
427 during the early embryonic stages from E9.5 to E12.5, the process of branching morphogenesis
428 occurs after E12.5 [62]. Similarly, INSPIRE identified a brain region characterized by the
429 specific expression of genes *Neurod6* and *Neurod2*, which only became clearly localized in the
430 forebrain after stage E12.5 (Fig. 5c, f, g). The expressions of these two genes suggest active
431 neuronal differentiation and development in the forebrain during these stages. These results
432 demonstrate INSPIRE's capability to deepen the understanding of developmental dynamics
433 through its effective integrative data analysis.

434 Using NMF modeling, INSPIRE enabled cross-developmental stage comparisons that went
435 beyond the resolution of major organs or tissues. Instead of concentrating solely on broader
436 structures, it identified intricate tissue architectures and cell type distributions through its
437 spatial factors, allowing for detailed comparisons among embryos at various stages. For instance,
438 two distinct spatial factors emerged in the forebrain region by stage E11.5, gradually forming a
439 layered structure that became clearly visible by stage E14.5 (Supplementary Fig. 39). Similarly,
440 three spatial factors captured the evolving structure of the embryonic mouth and jaw, with their
441 spatial organization becoming increasingly complex by stages E12.5 and E13.5 (Supplementary
442 Fig. 40). Furthermore, analyzing the spatial distributions of INSPIRE's spatial factors alongside
443 their gene signatures offered more in-depth biological insights into the developmental dynamics.

444 As an example, we identified a factor annotated as the choroid plexus based on its spatial
445 location in the embryo at E16.5 (Fig. 5h). GO analysis of its gene profile, as reported by
446 INSPIRE, confirmed its involvement in central nervous system and brain development. It also
447 linked this factor to biological processes like cilium organization and movement, providing
448 insights into its specific functions (Fig. 5i, j). This factor, along with its associated genes *Ttr*
449 and *Pcp4l1*, exhibited clear spatial localization after stage E11.5, illustrating its developmental
450 trajectory over time. Another example is the identification of a factor with detailed spatial
451 concentrations within the embryos, specifically surrounding many tiny tube-like structures (Fig.
452 5k). Gene set enrichment analysis revealed its correspondence with smooth muscle cells (Fig.
453 5l, m), showing alignment between its specific gene programs and a set of smooth muscle cell
454 marker genes such as *Acta2* and *Myl9* [63]. Given that this spatial factor also colocalized with
455 the expression of *Nkx2-3* (Supplementary Fig. 41), we inferred that it described the nuanced
456 distributions of gastrointestinal smooth muscle cells [64]. Spatial visualizations indicated that
457 gastrointestinal smooth muscle cells and tracts became clearly presented after stage E12.5,
458 uncovering their spatiotemporal dynamics. To summarize, the above results highlight the power
459 of INSPIRE to facilitate the study of embryonic development by effectively identifying nuanced
460 differences with biological meanings across developmental stages using spatial factors and the
461 associated gene profiles.

462 **INSPIRE enables precise 3D reconstruction of tissues and whole** 463 **organisms.**

464 Recently, there has been a growing number of ST datasets composed of multiple parallel 2D
465 slices (x-y-axis) along the z-axis within tissues. Each slice captures a 2D spatial transcrip-
466 tomic landscape, and when these slices are spatially aligned and jointly analyzed, they offer
467 valuable opportunities to construct a comprehensive 3D view of spatial structures and cell
468 type distributions within tissues or organs, deepening our understanding of complex biological
469 systems. Here, we demonstrate INSPIRE's capability to reliably register adjacent 2D ST slices,
470 enabling accurate 3D reconstruction of tissues. For a comprehensive illustration, we applied
471 INSPIRE for two different scenarios, utilizing slices that vary in scale from tissue regions to
472 whole organisms.

473 In the first scenario, we highlighted INSPIRE's enhanced performance in slice registration

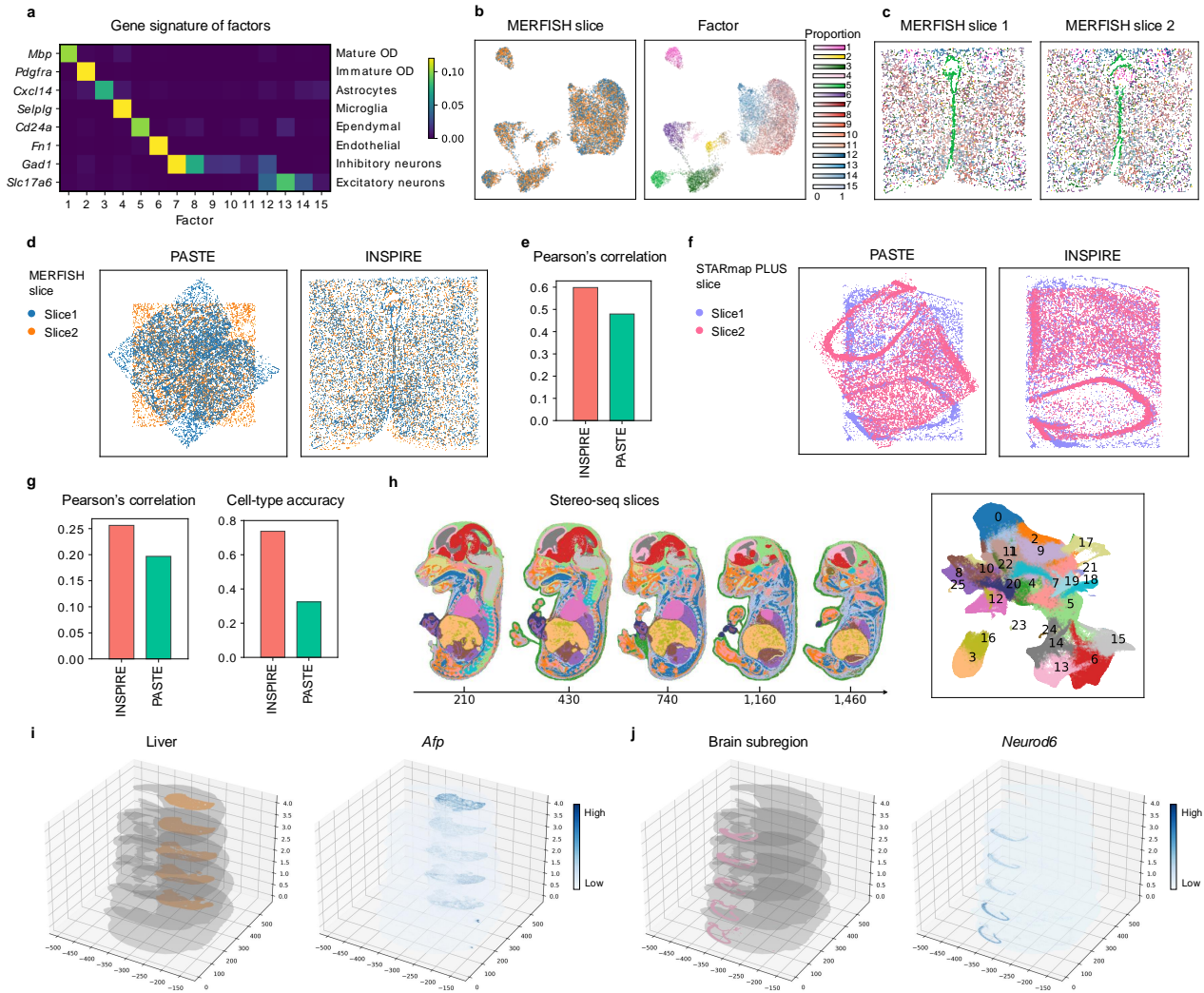


Figure 6: 3D reconstruction of tissues and whole organisms by INSPIRE. We utilized INSPIRE to spatially align two MERFISH slices from the mouse hypothalamic preoptic region (**a - e**), two STARmap PLUS slices from the mouse hippocampus region (**f, g**), and five whole-embryo slices produced by Stereo-seq (**h - j**). **a**. Gene signatures of spatial factors, with each row indicating a marker gene specific to a cell type. **b**. UMAP plots of cell representations from INSPIRE, colored by MERFISH slice indices and the inferred factor proportions among cells. **c**. The MERFISH slices colored by the proportions of factors. **d**. The MERFISH slices after PASTE alignment and INSPIRE alignment, respectively. **e**. Pearson correlation scores of INSPIRE and PASTE evaluated using the MERFISH dataset. **f**. The STARmap PLUS slices after PASTE alignment and INSPIRE alignment, respectively. **g**. Pearson correlation and cell-type accuracy scores of INSPIRE and PASTE evaluated using the STARmap PLUS dataset. **h**. Visualization of the Stereo-seq whole-embryo slices and UMAP plot of spot representations, colored by the identified spatial domains across slices. **i**. Visualization of liver structure and distribution of *Afp* expression on the reconstructed 3D model of the embryo. **j**. Visualization of the 3D structure of a brain subregion and the distribution of *Neurod6* expression on the reconstructed 3D embryo.

474 by using two sets of mouse brain region slices. Specifically, we first tested INSPIRE on a
475 dataset comprising two adjacent MERFISH slices from the mouse hypothalamic preoptic region
476 [65]. The application of INSPIRE revealed spatial factors that corresponded distinctly to
477 different cell types or subtypes within the hypothalamic preoptic region, aiding in accurate
478 cell-type identification in the brain (Fig. 6a, b). Moreover, the two slices displayed consistent
479 spatial factor distributions both in the UMAP plot and in spatial locations, providing valuable
480 information for establishing spatial correspondence between slices (Fig. 6b, c). Utilizing
481 this integration result, we identified mutual nearest neighbor (MNN) cells between the two
482 slices within the integrated embedding, serving as anchor pairs for guiding the registration
483 process. These anchors enabled the calculation of the optimal rigid transformation, effectively
484 aligning one slice with the other and achieving precise registration (Fig. 6d and Supplementary
485 Fig. 42). However, PASTE, a state-of-the-art method for spatial registration, could not
486 align these two slices as INSPIRE did. To quantitatively compare INSPIRE and PASTE, we
487 utilized the Pearson correlation metric, which measures the similarity of gene expression levels
488 between spatially proximal spots from the two slices after spatial registration, with a higher
489 score indicating better performance. As shown in Fig. 6e, INSPIRE demonstrated superior
490 registration performance compared to PASTE. We also compared INSPIRE and PASTE on
491 another dataset, consisting of two STARmap PLUS slices from the mouse hippocampus region
492 [13]. Consistent with the previous results, INSPIRE achieved precise registration between the
493 two slices, while PASTE did not (Fig. 6f, Supplementary Figs. 43 and 44). For the quantitative
494 evaluation, in addition to the Pearson correlation metric, we evaluated cell-type accuracy score
495 as the original dataset provided cell type annotations. The cell-type accuracy score measures
496 the similarity of cell type annotation between spatially proximal spots from the two slices
497 after spatial registration, with a higher score indicating better spatial alignment performance.
498 INSPIRE achieved higher scores for both metrics compared to PASTE (Fig. 6g), highlighting
499 its superior performance in the slice registration task.

500 In the second scenario, we tested INSPIRE's ability to register multiple slices at the whole-
501 organism level. We applied INSPIRE to a Stereo-seq dataset consisting of five adjacent 2D
502 slices taken along the left-right axis of a mouse embryo at developmental stage E16.5. Spatial
503 registration and integrative analysis of these slices are crucial for constructing a comprehensive
504 3D model of the mouse embryo. In this application, INSPIRE effectively and efficiently

505 integrated 567,381 spatial spots across multiple slices (Supplementary Fig. 45). Its consistent
506 identification of tissues across the slices, such as heart, liver and brain, further showed the
507 reliability of the integration result (Fig. 6h). Guided by MNN cells from each pair of adjacent
508 slices, INSPIRE sequentially aligned all adjacent slices using rigid transformation. The resulting
509 3D model of mouse embryo successfully reconstructed major organs such as liver and heart,
510 and characterized 3D expression pattern of their marker genes (Fig. 6i and Supplementary Fig.
511 46). INSPIRE was also able to reconstruct detailed spatial structures such as tissue subregions
512 for accelerating comprehensive understandings of tissue 3D organizations. For instance, it
513 described the 3D structures of subregions in the forehead which vary along the left-right axis
514 (Fig. 6j and Supplementary Fig. 47).

515 To summarize, the results from these two scenarios illustrate that INSPIRE could be applied
516 to build 3D architectures of tissues or even the whole organisms with high reliability. This
517 capability of INSPIRE makes it a powerful tool for conducting 3D analyses in a wide range of
518 biological systems, enhancing our understanding beyond traditional 2D analyses.

519 Discussion.

520 In this paper, we have presented INSPIRE, an effective and versatile tool powered by advanced
521 deep learning technologies for integrating and interpreting multiple ST slices from diverse
522 sources. The results demonstrate that INSPIRE effectively addresses the challenges posed by the
523 heterogeneity in ST data, such as variations in samples, technologies, and developmental stages.
524 By combining an adversarial learning mechanism and NMF, INSPIRE not only integrated these
525 diverse datasets, but also deciphered fine-grained spatial tissue architectures through spatial
526 factors and interpreted their biological meanings based on their associated gene signatures.

527 Although several computational methods have also been developed and have greatly facil-
528 itated transcriptomics data analysis, direct application of them did not sufficiently address
529 challenges in ST data integrative analysis, as shown in our examples. Methods including Seurat
530 and LIGER, designed to remove batch effects among scRNA-seq datasets, lack the ability to
531 model spatial dependencies among spots or cells in ST data. PASTE and PRECAST, although
532 capable of performing spatially-informed analysis for multiple ST tissue slices, have shown less
533 satisfactory results in managing heterogeneous unwanted variation across ST datasets. PASTE
534 is primarily designed for joint analysis of ST slices from biological replicate samples, whereas

535 PRECAST relies on Gaussian mixture model shared among slices to correct for unwanted
536 variations, which can be less powerful when dealing with strong slice-specific effects. Methods
537 SpiceMix and NSFH use spatially-informed NMF to extract spatial signals from tissue slices,
538 successfully revealing fine-grained spatial organizations with biological interpretations. However,
539 they are limited to handling one slice at a time and are not designed for integrative analysis
540 of ST data. In contrast, INSPIRE addresses all these challenges and offers advantages over
541 existing methods in ST data integrative analysis by the innovations on its model.

542 The first major advantage of INSPIRE is its utilization of a tailored adversarial learning
543 mechanism. The adversarial learning mechanism adaptively detects unwanted variations among
544 datasets, even when certain slices present their unique biological signals, providing accurate
545 guidance for neural networks to distill meaningful biological variations across slices in the
546 shared latent space. Meanwhile, the nonlinearity of neural networks offers great flexibility for
547 INSPIRE to adjust for heterogeneous unwanted effects originating from diverse sources.

548 Second, the seamless integration of the adversarial learning mechanism with NMF in
549 INSPIRE can decipher biological signals across multiple slices into detailed and interpretable
550 spatial factors, unconfounded by unwanted variations. The capability to learn NMF consistently
551 among slices is particularly essential to reveal fine-grained spatial structural patterns in multi-
552 slice integrative analysis. Meanwhile, downstream analyses, including GO analysis and GSEA,
553 provide interpretation of biological meanings of spatial factors, leading to the discovery of
554 spatial cell type distributions and biological processes. Additionally, as shown in the DLPFC
555 example, the learning of spatial factors aids in eliminating redundant signals that are not
556 related to the inferred gene programs, thus enhancing the discovery of biologically meaningful
557 spot representations in the latent space and facilitating improved result in analyses including
558 spatial trajectory inference and spatial domain identification.

559 Lastly, INSPIRE incorporates GNNs to perform spatially informed analyses. The GNNs
560 take into account the microenvironments of cells or spatial spots within the tissue, enhancing
561 the ability of INSPIRE to understand tissue organizations. Furthermore, with the utilization
562 of lightweight GNNs that allow for mini-batch optimization, INSPIRE is scalable to analyze
563 large-scale ST datasets, as demonstrated by the construction of mouse organogenesis atlas and
564 the 3D reconstruction of mouse embryo tasks, each encompassing over half a million spots.

565 Through a comprehensive benchmarking study, INSPIRE has shown superior performance

566 in integrating information across multiple tissue slices, significantly enhancing the characteriza-
567 tion of spatial architecture compared to existing methods. We also demonstrated INSPIRE's
568 effectiveness and wide applicability in a range of challenging applications, including stitching
569 together tissue slices with only partially overlapping structures, integrating data from different
570 ST technologies, aligning slices collected at a series of embryonic developmental stages, and
571 reconstructing 3D tissue models. Each of these applications highlighted a distinct advantage
572 of INSPIRE: constructing a comprehensive atlas by merging data from different tissue views,
573 enabling downstream analyses that leverage the strengths of distinct ST technologies, ad-
574 vancing the study of developmental dynamics, and deepening our understanding of 3D tissue
575 organization.

576 One potential limitation of INSPIRE, despite its numerous strengths, is its dependence on
577 shared genes across datasets for data integration and interpretation. This reliance might result
578 in the exclusion of important gene signals that are unique to specific datasets. Extending this
579 method to incorporate and align non-shared genes among ST datasets could further enhance
580 biological analyses.

581 The interpretable and scalable integration of diverse ST datasets across different experimental
582 designs is invaluable in advancing biological discoveries. As the field of spatial transcriptomics
583 continues to grow rapidly, the need for comprehensive integrative analysis of ST datasets will
584 only increase. We expect that INSPIRE, with its exceptional performance, interpretability, and
585 versatility, will be a powerful addition to the modern life scientist's ST analysis toolkit.

586 Methods

587 The model of INSPIRE.

588 INSPIRE offers interpretable and spatially-informed integration of ST data from multiple tissue
589 slices. Let $s = 1, 2, \dots, S$ be the index of ST slices. For slice s , we observe gene expression count
590 matrix $\mathbf{Y}^s = [y_{i,g}^s] \in \mathbb{R}^{N_s \times G}$ and 2D spatial coordinates of cells or spatial spots $\mathbf{P}^s \in \mathbb{R}^{N_s \times 2}$,
591 where $i = 1, 2, \dots, N_s$ is the index for cells or spatial spots, and $g = 1, 2, \dots, G$ is the index
592 for genes. Using all the information as input, INSPIRE learns to decipher spatial structures
593 across all the S slices and infers the associated gene programs.

594 To integrate both gene expressions and spatial locations across all ST slices, INSPIRE
595 encodes the gene expression information of all cells or spatial spots into a shared latent space \mathcal{Z} ,
596 using a neural network that accounts for spatial dependencies among cells or spots. Specifically,
597 INSPIRE builds a 2D neighborhood graph for each slice using the spatial location matrix. We
598 denote the neighborhood graph for slice s as $\mathbf{A}^s = [a_{i,j}] \in \{0, 1\}^{N_s \times N_s}$, where $a_{i,j} = 1$ if cells
599 or spots i and j are spatial neighbors, and $a_{i,j} = 0$ otherwise. Using both gene expressions
600 $\{\mathbf{Y}^s\}_{s=1,2,\dots,S}$ and spatial graphs $\{\mathbf{A}^s\}_{s=1,2,\dots,S}$, the latent representations of cells or spatial
601 spots are generated by:

$$602 \quad x_{i,g}^s = \log \left(\frac{y_{i,g}^s}{\sum_{g=1}^G y_{i,g}^s} M + 1 \right), \quad (1)$$

$$603 \quad \mathbf{Z}^s = f_Z(\mathbf{X}^s, \mathbf{A}^s), \quad (2)$$

604 where we perform log-normalization on count matrices $\{\mathbf{Y}^s\}_{s=1,2,\dots,S}$ for algorithm stability.
605 In the data normalization, we set $M = 10^4$ for sequencing-based ST data, and set $M = 10^3$
606 for imaging-based ST data. The log-normalized data $\mathbf{X}^s = [x_{i,g}^s] \in \mathbb{R}^{N_s \times G}$ are then encoded
607 to latent representations $\mathbf{Z}^s \in \mathbb{R}^{N_s \times P}$ through a graph neural network $f_Z(\cdot)$ with parameters
608 shared among all slices, where P is the dimensionality of the shared latent space. For slice s ,
609 the latent representation \mathbf{Z}^s embeds information from both gene expressions \mathbf{Y}^s and spatial
610 neighbors encoded in graph \mathbf{A}^s , describing spatially-informed biological variations in slice s .
611 Importantly, in addition to capturing spatially-aware biological signals in each slice, the shared
612 latent space is designed for achieving the integration across all input slices. For harmonizing
613 latent representations $\mathbf{Z}^1, \mathbf{Z}^2, \dots, \mathbf{Z}^S$ from different ST slices, INSPIRE adopts a tailored
614 adversarial mechanism in latent space \mathcal{Z} . Let $\mathbf{z}_i^s \in \mathbb{R}^P$ be the latent representation of cell

615 or spot i in slice s . An auxiliary discriminator network, $D^s(\cdot) : \mathcal{Z} \rightarrow (0, 1)$, is deployed
616 to identify where the poor mixing between representations $\{\mathbf{z}_i^s\}_{i=1,2,\dots,N_s}$ from slice s and
617 $\{\mathbf{z}_i^{s+1}\}_{i=1,2,\dots,N_{s+1}}$ from slice $s + 1$ occurs. Encoder network $f_Z(\cdot)$ is trained to compete against
618 discriminator $D^s(\cdot)$, aiming to mix $\{\mathbf{z}_i^s\}_{i=1,2,\dots,N_s}$ from slice s and $\{\mathbf{z}_i^{s+1}\}_{i=1,2,\dots,N_{s+1}}$ from slice
619 $s + 1$. Through this competition, discriminator $D^s(\cdot)$ provides feedback to improve encoder
620 $f_Z(\cdot)$ until representations $\{\mathbf{z}_i^s\}_{i=1,2,\dots,N_s}$ and $\{\mathbf{z}_i^{s+1}\}_{i=1,2,\dots,N_{s+1}}$ from slices s and $s + 1$ are well
621 integrated. INSPIRE introduces $S - 1$ discriminators $\{D^s(\cdot)\}_{i=1,2,\dots,S-1}$ for aligning all the S
622 tissue slices. Guided by the $S - 1$ discriminators, encoder $f_Z(\cdot)$ learns to generate integrated
623 representations of cells or spatial spots across all S tissue slices.

624 Based on the shared latent space, INSPIRE then achieves a harmonized non-negative matrix
625 factorization (NMF) for gene expressions across all input slices, that are not confounded by
626 complex unwanted variations. The hidden spatial factors identified by this integrated NMF
627 across slices provide a unified characterization of fine-grained tissue structures across all slices.
628 Meanwhile, the gene loading matrix describes gene modules associated with each spatial factor,
629 interpreting the biological meanings of the detailed spatial organization patterns discovered by
630 the spatial factors. We assume there are K hidden spatial factors in input slices. Each spatial
631 factor characterizes a fine-grained spatial structure in the tissue. Let $\boldsymbol{\beta}_i^s = [\beta_{i,1}^s, \beta_{i,2}^s, \dots, \beta_{i,K}^s]$
632 denote the set of non-negative weights among the K hidden spatial factors for cell or spot
633 i in slice s , with $\beta_{i,k}^s \geq 0$ and $\sum_{k=1}^K \beta_{i,k}^s = 1$. INSPIRE generates $\boldsymbol{\beta}_i^s$ from integrated latent
634 representation \mathbf{z}_i^s of cells or spots across slices:

$$635 \quad \boldsymbol{\beta}_i^s = f_{\beta}(\mathbf{z}_i^s), \quad (3)$$

636 where network $f_{\beta}(\cdot)$ contains a simple linear layer, followed by a softmax function. Notably, in
637 the shared latent space, representations $\{\mathbf{Z}^s\}_{s=1,2,\dots,S}$ are spatially-aware and free of unwanted
638 variations. Hence, generated from \mathbf{Z}^s , the obtained $\boldsymbol{\beta}^s = [\beta_{i,k}^s] \in \mathbb{R}^{N_s \times K}$ for different slices
639 are also spatially-informed and well integrated across ST slices. The integrated $\{\boldsymbol{\beta}^s\}_{s=1,2,\dots,S}$
640 together with shared gene loading matrix $\boldsymbol{\mu} = [\mu_{k,g}] \in \mathbb{R}^{K \times G}$ across slices form a harmonized
641 NMF model for all input slices. In the model, $\{\boldsymbol{\beta}^s \boldsymbol{\mu}\}_{s=1,2,\dots,S}$ focus on capturing shared
642 biological signal in all slices and further decomposing it into a set of K interpretable spatial
643 factors. To account for confounding factors including batch effects and technical effects
644 across ST slices, INSPIRE also introduces slice- and gene-specific effects $\gamma_g^s \in \mathbb{R}$ to the
645 integrated NMF model. Combining non-negative weights for spatial factors in cells or spots

646 $\{\beta^s\}_{s=1,2,\dots,S}$, non-negative gene loadings μ shared across slices, and slice- and gene-specific
 647 effects $\{\gamma^s\}_{s=1,2,\dots,S}$, $\gamma^s = [\gamma_g^s, \gamma_2^s, \dots, \gamma_G^s] \in \mathbb{R}^G$ for modeling unwanted variations, INSPIRE
 648 reconstructs the observed gene expression counts using the following integrated NMF-based
 649 model across all ST slices:

$$650 \quad y_{i,g}^s \sim \text{Poisson}(l_i^s u_{i,g}^s), \quad (4)$$

$$651 \quad u_{i,g}^s = \exp \left[\log \left(\sum_{k=1}^K \beta_{i,k}^s \mu_{k,g} \right) + \gamma_g^s \right], \quad (5)$$

652 where l_i^s is the observed total transcript count in cell or spot i from slice s , gene loadings
 653 satisfy $\mu_{k,g} \geq 0$ and $\sum_{g=1}^G \mu_{k,g} = 1$. For gene loadings μ and slice- and gene-specific effects
 654 $\{\gamma^s\}_{s=1,2,\dots,S}$, INSPIRE models them as learnable parameters. After training, INSPIRE's
 655 learned $\mu_k = [\mu_{k,1}, \mu_{k,2}, \dots, \mu_{k,G}] \in \mathbb{R}^G$ reveals the gene signature corresponding to hidden
 656 spatial factor k , where a high value of $\mu_{k,g}$ indicates a greater impact of gene g on spatial factor
 657 k . Through learning and analyzing gene loadings μ , INSPIRE is able to find gene programs that
 658 are associated with different hidden spatial factors. Meanwhile, in the integrated NMF across
 659 slices, non-negative weights $\{\beta_{\cdot,k}^s\}_{s=1,2,\dots,S}$, $\beta_{\cdot,k}^s = \{\beta_{i,k}^s\}_{i=1,2,\dots,N_s}$ with spatial coordinates of
 660 cells or spots describe a spatial enrichment pattern of spatial factor k across all the S ST
 661 slices. Using $\{\beta^s\}_{s=1,2,\dots,S}$, INSPIRE is capable of depicting fine-grained spatial organization
 662 structures across all ST slices, without being confounded by unwanted variations.

663 INSPIRE is a unified method that incorporates the adversarial learning mechanism for data
 664 integration with the NMF model for jointly depicting interpretable spatial structures in multiple
 665 tissue slices. We propose to train INSPIRE under the following optimization framework:

$$666 \quad \min_{\{f_Z, f_\beta, \mu, \gamma\}} \max_{\{D^1, D^2, \dots, D^{S-1}\}} \sum_{s=1}^{S-1} \mathcal{L}_{\text{Integration}}^s + \mathcal{L}_{\text{NMF}} + \lambda_{\text{AE}} \mathcal{R}_{\text{AE}} + \lambda_{\text{Geometry}} \mathcal{R}_{\text{Geometry}}, \quad (6)$$

$$668 \quad \mathcal{L}_{\text{Integration}}^s = \mathcal{L}_{\text{Integration}}^s(f_Z, D^s),$$

$$669 \quad \mathcal{L}_{\text{NMF}} = \mathcal{L}_{\text{NMF}}(f_Z, f_\beta, \mu, \gamma),$$

$$670 \quad \mathcal{R}_{\text{AE}} = \mathcal{R}_{\text{AE}}(f_Z),$$

$$671 \quad \mathcal{R}_{\text{Geometry}} = \mathcal{R}_{\text{Geometry}}(f_Z),$$

672 where $\mathcal{L}_{\text{Integration}}^s$ is the objective function of adversarial learning for integrating data from slice
 673 s and slice $s + 1$; \mathcal{L}_{NMF} is the objective function of the joint NMF for reconstructing gene
 674 expression counts across all ST slices; \mathcal{R}_{AE} and $\mathcal{R}_{\text{Geometry}}$ are regularizers to encourage the

675 preservation of biological signals across slices in the shared latent space; λ_{AE} and $\lambda_{\text{Geometry}}$ are
 676 coefficients for the two regularizers respectively, and are set to $\lambda_{\text{AE}} = 1.0$ and $\lambda_{\text{Geometry}} = 0.02$.
 677 We explain each component in optimization problem (6) in details in the next sections. The
 678 parameters in INSPIRE include: parameters in network $f_Z(\cdot)$ that encodes latent representations
 679 $\{\mathbf{Z}^s\}_{s=1,2,\dots,S}$; parameters in network $f_\beta(\cdot)$ that generates spatial factors for cells or spots among
 680 slices $\{\beta^s\}_{s=1,2,\dots,S}$; gene loading matrix μ shared across slices; parameters in $S-1$ discriminators
 681 $\{D^s(\cdot)\}_{s=1,2,\dots,S-1}$ that assist data integration across slices; as well as slice- and gene-specific
 682 effects $\gamma = \{\gamma^s\}_{s=1,2,\dots,S}$ that account for unwanted variations. After training, INSPIRE
 683 simultaneously outputs latent representations $\{\mathbf{Z}^s\}_{s=1,2,\dots,S}$, spatial factors $\{\beta^s\}_{s=1,2,\dots,S}$ and
 684 gene loadings μ . The latent representations of cells or spatial spots are utilized for identifying
 685 major spatial domains in tissues and detecting spatial trajectories. Detailed spatial factors
 686 $\{\beta^s\}_{s=1,2,\dots,S}$ are used for the discovery of fine-grained tissue sub-regions and spatial distributions
 687 of cell types, providing a characterization of spatial patterns in tissues at a higher resolution.
 688 Gene loading matrix μ characterizes gene signatures associated with the detailed spatial
 689 structures discovered by spatial factors. It deciphers the biological meaning of spatial factors
 690 through factor-specific gene program detection and pathway enrichment analysis.

691 **Adversarial learning mechanism for data integration across slices.**

692 The adversarial training between the discriminators and the encoder is formulated as a
 693 min-max optimization problem, $\min_{\{f_Z\}} \max_{\{D^1, D^2, \dots, D^{S-1}\}} \sum_{s=1}^{S-1} \mathcal{L}_{\text{Integration}}^s(f_Z, D^s)$, contained
 694 in (6), where

$$695 \quad \mathcal{L}_{\text{Integration}}^s = \frac{1}{N_s} \sum_{i=1}^{N_s} \log D^s(\mathbf{z}_i^s) + \frac{1}{N_{s+1}} \sum_{i=1}^{N_{s+1}} \log(1 - D^s(\mathbf{z}_i^{s+1})).$$

696 The latent representations are obtained using Eqs. (1) and (2). Given latent codes $\{\mathbf{z}_i^s\}_{i=1,2,\dots,N_s}$
 697 and $\{\mathbf{z}_i^{s+1}\}_{i=1,2,\dots,N_{s+1}}$ generated by $f_Z(\cdot)$, discriminator $D^s(\cdot) : \mathcal{Z} \rightarrow (0, 1)$ is trained to
 698 distinguish between $\{\mathbf{z}_i^s\}_{i=1,2,\dots,N_s}$ from slice s and $\{\mathbf{z}_i^{s+1}\}_{i=1,2,\dots,N_{s+1}}$ from slice $s+1$. Here,
 699 $D^s(\cdot)$ is trained to output a high score (close to one) for representations in slice s , while it
 700 learns to assign a low score (close to zero) for representations in slice $s+1$. This is achieved by
 701 maximizing $\mathcal{L}_{\text{Integration}}^s$ with respect to $D^s(\cdot)$. Given discriminators $\{D^s(\cdot)\}_{s=1,2,\dots,S-1}$, encoder
 702 $f_Z(\cdot)$ is trained to mix latent representations across all slices, such that any discriminator
 703 cannot distinguish latent codes between slices. This is achieved by minimizing $\sum_{s=1}^{S-1} \mathcal{L}_{\text{Integration}}^s$
 704 with respect to $f_Z(\cdot)$. Through the competition between encoder $f_Z(\cdot)$ and discriminators
 705 $\{D^s(\cdot)\}_{s=1,2,\dots,S-1}$, the discriminators will guide the improvement of the encoder until the

706 encoder generates integrated latent representations for cells or spatial spots across all the S
707 slices.

708 With the above design, Discriminator $D^s(\cdot)$ will guide $f_Z(\cdot)$ to mix $\{\mathbf{z}_i^s\}_{i=1,2,\dots,N_s}$ from slice
709 s with $\{\mathbf{z}_i^{s+1}\}_{i=1,2,\dots,N_{s+1}}$ from slice $s+1$. However, a slice-specific cell or spot population
710 should not be mixed with cells or spots from another slice. To preserve slice-specific cell
711 populations from being incorrectly mixed with other cells, we follow our previous work [34]
712 to adopt a thresholding for discriminator scores. Consider a cell population that is unique
713 in slice s . Discriminator $D^s(\cdot)$ can easily recognize cells in this population as cells from
714 slice s , and assign extremely high scores to them. By similar reasoning, $D^s(\cdot)$ will assign
715 extremely low scores to slice $s+1$ -unique cell populations. Therefore, as slice-unique cell
716 populations are prone to be assigned with extreme discriminator scores, we set boundaries
717 for discriminator scores to make discriminators inactive on them. Specifically, the outputs
718 of standard discriminators are transformed into $(0, 1)$ through the sigmoid function. For any
719 applicable latent code \mathbf{z} , $D^s(\mathbf{z}) = \text{sigmoid}(d^s(\mathbf{z})) = 1/(1 + \exp(-d^s(\mathbf{z})))$, where $d^s(\mathbf{z}) \in \mathbb{R}$ is the
720 logit value of discriminator score $D^s(\mathbf{z})$. We bound discriminator score $D^s(\mathbf{z})$ by thresholding
721 its logit $d^s(\mathbf{z})$ to a reasonable range $[-m, m]$, where m is set to 50.0:

$$722 \quad \tilde{D}^s(\mathbf{z}) = \text{sigmoid}(\text{clamp}(d^s(\mathbf{z}))),$$

723 where $\text{clamp}(\cdot) = \max(\min(\cdot, m), -m)$, $m > 0$. By clamping $d^s(\mathbf{z})$, $\tilde{D}^s(\mathbf{z})$ becomes a constant
724 when $d^s(\mathbf{z}) < -m$ or $d^s(\mathbf{z}) > m$, providing zero gradients for updating parameters in encoder
725 network $f_Z(\cdot)$. With this design, the slice-unique cell populations with extreme $d^s(\mathbf{z})$ scores
726 will be left in the inactive region of discriminators. Consequently, discriminators will not
727 force encoder $f_Z(\cdot)$ to mix slice-unique cell populations with other cells, avoiding incorrect
728 integration. Meanwhile, $\tilde{D}^s(\mathbf{z})$ remains the same as $D^s(\mathbf{z})$ when $\tilde{D}^s(\mathbf{z}) \in [-m, m]$, effectively
729 guiding encoder $f_Z(\cdot)$ to align cells that are likely to belong to the shared cell populations among
730 slices for data integration. For clarity, we still use the notation $D^s(\cdot)$ to denote discriminator
731 $\tilde{D}^s(\cdot)$ with the score thresholding design hereinafter.

732 **Joint NMF for reconstructing gene expressions in multiple ST slices.**

733 The major objective function in optimization problem (6) of INSPIRE, \mathcal{L}_{NMF} , corresponds
734 to the reconstruction of gene expression counts in all S input slices through a joint NMF model.
735 INSPIRE uses encoder $f_Z(\cdot)$ to generate integrated data $\{\mathbf{Z}^s\}_{s=1,2,\dots,S}$ across slices, guided by
736 discriminators $\{D^s(\cdot)\}_{s=1,2,\dots,S-1}$. By Eq. (3), it then leverages network $f_\beta(\cdot)$ to decompose the

737 signal captured in $\{\mathbf{Z}^s\}_{s=1,2,\dots,S}$ into a set of K interpretable spatial factors $\{\boldsymbol{\beta}\}_{s=1,2,\dots,S}$ that
 738 characterize spatial structures of tissues at a fine-grained level. Combining the obtained spatial
 739 factors with additional parameters, including gene loadings $\boldsymbol{\mu}$ as well as slice- and gene-specific
 740 effects $\boldsymbol{\gamma}$, INSPIRE reconstructs the gene expression counts from all inputs slices through
 741 an integrated NMF-based model described by Eqs. (4) and (5). Based on this model, the
 742 corresponding objective function is given by

$$743 \quad \mathcal{L}_{\text{NMF}} = - \sum_{s=1}^S \frac{1}{N_s} \sum_{i=1}^{N_s} \sum_{g=1}^G [y_{i,g}^s \log(l_i^s u_{i,g}^s) - l_i^s u_{i,g}^s].$$

744 By minimizing \mathcal{L}_{NMF} with respect to $f_Z(\cdot)$, $f_\beta(\cdot)$, $\boldsymbol{\mu}$ and $\boldsymbol{\gamma}$, INSPIRE deciphers interpretable
 745 hidden spatial factors that are unified across slices with $\{\boldsymbol{\beta}^s \boldsymbol{\mu}\}$. Here, $\{\boldsymbol{\beta}^s\}_{s=1,2,\dots,S}$ characterizes
 746 detailed spatial organizations in tissues, while $\boldsymbol{\mu}$ describes gene signatures associated with the
 747 tissue organization patterns identified by spatial factors for interpretability.

748 **Regularization for encouraging the preservation of biological variations across**
 749 **slices.**

750 INSPIRE uses two regularizers, \mathcal{R}_{AE} and $\mathcal{R}_{\text{Geometry}}$, to help preserve biological signals across
 751 slices in the shared latent space. We design regularizer \mathcal{R}_{AE} as

$$752 \quad \mathcal{R}_{\text{AE}} = \sum_{s=1}^S \frac{1}{N_s} \sum_{i=1}^{N_s} \|\mathbf{x}_i^s - f_X^s(\mathbf{z}_i^s, s)\|_2,$$

753 where slice-specific neural network $f_X^s(\cdot, s)$ is introduced to reconstruct log-normalized gene
 754 expressions in cells or spots \mathbf{x}_i^s based on latent codes \mathbf{z}_i^s and slice label s . Encoder $f_Z(\cdot)$
 755 and network $f_X^s(\cdot, s)$ together form an auto-encoder structure between log-normalized data
 756 $\{\mathbf{X}^s\}_{s=1,2,\dots,S}$ and latent codes $\{\mathbf{Z}^s\}_{s=1,2,\dots,S}$. In regularizer \mathcal{R}_{AE} , slice-specific network $f_X^s(\cdot, s)$
 757 is designed to recover gene expressions from the latent space while accounting for slice-
 758 specific effects using slice labels. Therefore, encoder $f_Z(\cdot)$ is encouraged to distill all biological
 759 information into the latent space without slice-specific effects. To preserve a good geometric
 760 structure in the latent space for revealing biological signals, e.g., continued developmental
 761 trajectories of cells, we propose regularizer $\mathcal{R}_{\text{Geometry}}$:

$$762 \quad \mathcal{R}_{\text{Geometry}} = \sum_{s=1}^S \frac{1}{N_s} \sum_{i=1}^{N_s} \|\mathbf{c}_{x,i}^s - \mathbf{c}_{z,i}^s\|_2^2,$$

$$763 \quad c_{x,i,j}^s = 1 - \frac{\langle \mathbf{x}_i^s, \mathbf{x}_j^s \rangle}{\|\mathbf{x}_i^s\|_2 \|\mathbf{x}_j^s\|_2},$$

$$764 \quad c_{z,i,j}^s = 1 - \frac{\langle \mathbf{z}_i^s, \mathbf{z}_j^s \rangle}{\|\mathbf{z}_i^s\|_2 \|\mathbf{z}_j^s\|_2},$$

765 where for cells or spots i and j from slice s , $c_{x,i,j}^s$ is the cosine similarity between their log-
766 normalized gene expressions \mathbf{x}_i^s and \mathbf{x}_j^s , $c_{z,i,j}^s$ is the cosine similarity between their latent
767 representations \mathbf{z}_i^s and \mathbf{z}_j^s ; $\mathbf{c}_x^s = [c_{x,i,j}^s] \in \mathbb{R}^{N_s \times N_s}$ and $\mathbf{c}_z^s = [c_{z,i,j}^s] \in \mathbb{R}^{N_s \times N_s}$ are corresponding
768 cosine similarity matrices; $\mathbf{c}_{x,i}^s$ and $\mathbf{c}_{z,i}^s$ are the i -th rows of \mathbf{c}_x^s and \mathbf{c}_z^s respectively. In regularizer
769 $\mathcal{R}_{\text{Geometry}}$, cells or spots with high similarities in gene expressions are encouraged to be close in
770 the latent space, while cells or spots with dissimilar gene expressions are encouraged to remain
771 distinct in the latent space. Hence, by using $\mathcal{R}_{\text{Geometry}}$, INSPIRE encourages $f_Z(\cdot)$ to preserve
772 biological meaningful structures in the shared latent space.

773 **Selection of informative genes.**

774 When all input ST slices provide the whole transcriptome profiling, INSPIRE selects the
775 informative genes and uses them as features. Following the Scanpy pipeline [48], INSPIRE
776 selects the top M highly variable genes for each slice. It then takes the intersection of these
777 highly variable genes across all ST slices to ensure that the features of cells or spatial spots are
778 shared across all slices. By default, we set $M = 6,000$. If the number of selected features is
779 less than 2,000 with $M = 6,000$, a larger value of M can be adopted. When some ST slices to
780 be analyzed are based on ST technologies that measure the expressions of a limited number of
781 genes, such as MERFISH, INSPIRE uses all the shared genes across the input slices for the
782 integrative analysis.

783 **Network structures.**

784 Encoder $f_Z(\cdot)$ contains a graph neural network (GNN) layer and a dense layer. The GNN
785 layer takes log-normalized gene expressions \mathbf{x}_i^s and spatial graph \mathbf{A}^s as input. It outputs
786 512-dimensional hidden vectors. Then the dense layer in $f_Z(\cdot)$ maps the 512-dimensional hidden
787 vectors to the P -dimensional latent representations \mathbf{z}_i^s of cells or spatial spots. We set $P = 32$
788 throughout all analyses. Inspired by previous works [15, 66, 67], INSPIRE provides two options
789 for the GNN layer: the graph attention layer and the lightweight graph-convolutional layer.

790 The graph attention layer is formulated as:

$$\begin{aligned}
 791 \quad \mathbf{h}_i^s &= \sigma \left(\sum_{j \in \mathcal{N}_i} \alpha_{i,j} \mathbf{W} \mathbf{x}_j^s \right), \\
 792 \quad \alpha_{i,j} &= \frac{\exp(e_{i,j}^s)}{\sum_{j' \in \mathcal{N}_i} \exp(e_{i,j'}^s)}, \\
 793 \quad e_{i,j}^s &= \text{sigmoid}(\mathbf{v}_1^T \mathbf{W} \mathbf{x}_i^s + \mathbf{v}_2^T \mathbf{W} \mathbf{x}_j^s),
 \end{aligned}$$

794 where \mathbf{h}_i^s represents the output of the graph attention layer; $\mathcal{N}_i = \{j | a_{i,j}^s = 1\}$ represents the
 795 neighbor set of cell or spot i encoded in spatial graph \mathbf{A}^s ; \mathbf{W} , \mathbf{v}_1 and \mathbf{v}_2 are parameters in the
 796 graph attention layer; $\sigma(\cdot)$ is the activation function. Based on the graph attention mechanism,
 797 parameters \mathbf{v}_1 and \mathbf{v}_2 are used to learn edge weights $\alpha_{i,j}^s$ between neighboring cells or spots,
 798 helping to adaptively borrow information from neighboring cells or spots. INSPIRE adopts
 799 the graph attention layer in $f_Z(\cdot)$ when handling the integration task for ST datasets with
 800 moderate numbers of cells or spatial spots. To integrate large atlas-scale ST datasets which
 801 contain hundreds of thousands or even millions of cells or spots, INSPIRE uses the lightweight
 802 graph-convolutional layer in $f_Z(\cdot)$, which is formulated as:

$$\begin{aligned}
 803 \quad \mathbf{H}^s &= \sigma(\mathbf{W} \tilde{\mathbf{X}}^s), \\
 804 \quad \tilde{\mathbf{X}}^s &= \text{concat}(\mathbf{X}^s, \tilde{\mathbf{A}}^s \mathbf{X}^s, (\tilde{\mathbf{A}}^s)^2 \mathbf{X}^s, \dots, (\tilde{\mathbf{A}}^s)^L \mathbf{X}^s),
 \end{aligned}$$

805 where \mathbf{H}^s represents the output of the lightweight graph-convolutional layer; \mathbf{W} denotes the
 806 parameters; $\tilde{\mathbf{A}}^s = (\tilde{\mathbf{D}}^s)^{-1/2} \mathbf{A}^s (\tilde{\mathbf{D}}^s)^{-1/2}$, $\tilde{\mathbf{D}}^s$ is the diagonal degree matrix of \mathbf{A}^s ; and L is the
 807 number of steps in the concatenation. We set $L = 1$ by default. The graph attention layer
 808 has the advantage of providing an inference of the edge importance between neighborhood
 809 cells or spots for adaptively aggregating information in microenvironments of cells or spots. By
 810 preparing $\tilde{\mathbf{X}}^s$ as a preprocessing step, the lightweight graph-convolutional layer enables an
 811 efficient training with mini-batch samples from $\tilde{\mathbf{X}}^s$, serving as a scalable approach to account
 812 for spatial dependencies in datasets with large numbers of cells or spots.

813 For network $f_\beta(\cdot)$ which produces K -dimensional spatial factors β_i^s from latent codes \mathbf{z}_i^s of
 814 cells or spatial spots, INSPIRE adopts a one-layer dense network with the softmax activation.
 815 The choice of K depends on the scale of the tissues to be analyzed. For example, INSPIRE set
 816 $K = 20$ for analyzing the cortex region of the brain, while it adopts $K = 40$ for analyzing the
 817 whole-brain slices.

818 For discriminators $\{D^s(\cdot)\}_{s=1,2,\dots,S-1}$ that guide encoder $f_Z(\cdot)$ to achieve the data integration,
819 INSPIRE uses two-layer dense networks. $D^s(\cdot)$ works as a binary classifier to distinguish between
820 $\{\mathbf{z}^s\}_{i=1,2,\dots,N_s}$ from slice s and $\{\mathbf{z}^{s+1}\}_{i=1,2,\dots,N_{s+1}}$ from slice s . Then, encoder $f_Z(\cdot)$ competes
821 against $D^s(\cdot)$ to integrate $\{\mathbf{z}^s\}_{i=1,2,\dots,N_s}$ with $\{\mathbf{z}^{s+1}\}_{i=1,2,\dots,N_{s+1}}$. Here, $D^s(\cdot)$ takes latent codes
822 \mathbf{z} of cells or spots from slices s or $s+1$ as input. It first uses a dense layer with an activation
823 function to map \mathbf{z} to a 512-dimensional hidden state. It then uses another dense layer to
824 produce a score belonging to $(0, 1)$ from the 512-dimensional hidden state.

825 INSPIRE introduces slice-specific network $f_X^s(\cdot, s)$ in its regularizer \mathcal{R}_{AE} to help preserve
826 biological variations across slices in the shared latent space. $f_X^s(\cdot, s)$ takes latent representations
827 \mathbf{z}_i^s and slice label s as inputs. It adopts a graph attention layer or a lightweight graph-
828 convolutional layer, followed by a dense layer, to recover log-normalized gene expressions \mathbf{x}_i^s
829 while accounting for slice-specific effects and spatial dependencies among cells or spatial spots.
830 The dimensionality of the hidden state in $f_X^s(\cdot, s)$ is set to be 512.

831 **Model training details.**

832 INSPIRE employs Adamax, which is a variant of the Adam algorithm [68], for stochastic
833 optimization during model training. By default, the number of optimization steps in INSPIRE
834 is set to 10,000 with learning rate $\text{lr} = 0.0005$, coefficients for computing running averages
835 $\beta_1 = 0.9$, $\beta_2 = 0.999$ and weight decay parameter $\lambda = 0.0001$. We conducted all experiments
836 on a single graphics processing unit. The computation times for all experiments are detailed in
837 Supplementary Table 1.

838 **Evaluation metrics.**

839 We evaluated spot or cell representations using ASW and assessed spatial domain identification
840 results, inferred from these representations, with ARI and NMI metrics. The quality of spatial
841 factors was measured by factor diversity and factor coherence.

842 *ASW.* ASW calculates the silhouette width of cells or spatial spots with respect to spatial
843 region annotation labels. A higher score indicates that cells or spots within the same spatial
844 region are closely grouped, while those from different spatial regions are well separated.

845 *ARI.* ARI measures the alignment between spatial domain identification result and expert
846 manual annotation. A lower score suggests that the two sets of labels for cells or spots are

847 independent, while a higher score indicates that the labels are identical, except for a possible
848 permutation.

849 *NMI*. NMI calculates the normalized mutual information between spatial domain identi-
850 fication result and expert manual annotation. A low NMI value indicates minimal shared
851 information between the label sets, while a high value suggests a strong correlation between
852 them.

853 *Factor diversity*. Topic diversity is defined as the percentage of unique genes among the
854 top 10 genes across all factors. A higher score reflects greater diversity among factors, while a
855 lower score indicates more redundancy.

856 *Factor coherence*. Topic coherence measures the interpretability of factors by calculating the
857 average pointwise mutual information of top genes associated with each factor, then averaging
858 these values across all factors. Specifically,

$$\begin{aligned} \text{Factor coherence} &= \frac{1}{K} \sum_{k=1}^K \frac{1}{45} \sum_{i=1}^{10} \sum_{j=i+1}^{10} m(g_i^{(k)}, g_j^{(k)}), \\ m(g_i, g_j) &= -\frac{\log \frac{P(g_i, g_j)}{P(g_i)P(g_j)}}{\log P(g_i, g_j)}, \end{aligned}$$

861 where $\{g_1^{(k)}, g_2^{(k)}, \dots, g_{10}^{(k)}\}$ denotes the top 10 genes associated with factor k , $m(\cdot, \cdot)$ is the
862 normalized pointwise mutual information, $P(g_i, g_j)$ is the probability of genes g_i and g_j co-
863 expressing in a spot or cell, and $P(g_i)$ is the marginal probability of gene g_i .

864 **Rankings of genes within a spatial factor.**

865 The gene loading associated with spatial factor k is represented as $\boldsymbol{\mu}_{k,\cdot} = [\mu_{k,1}, \mu_{k,2}, \dots, \mu_{k,G}]$,
866 where $\boldsymbol{\mu}$ is the gene loading matrix derived from integrated NMF across all input slices, and G
867 is the total number of genes analyzed. The non-negative values in $\boldsymbol{\mu}_{k,\cdot}$ indicate the relative
868 expression levels among genes within a factor, with a higher $\mu_{k,g}$ corresponding to greater
869 enrichment of gene g expression in factor k . Therefore, for each spatial factor k , we can rank
870 genes according to the non-negative values in $\boldsymbol{\mu}_{k,\cdot}$. The gene with the highest value is ranked
871 first, and the gene with the lowest value is ranked last.

872 Identification of genes specific to a spatial factor.

873 To identify highly expressed genes specific to spatial factor k , we first select the top G_0 ranked
874 genes based on the gene loading associated with spatial factor k , with G_0 set to 50 by default.
875 For each selected gene g , we then calculate the fold change between its estimated weight on
876 spatial factor k and all other spatial factors. A gene g is considered highly expressed and
877 specific to spatial factor k , if $\mu_{k,g}/\mu_{k',g} > 1$ for any $k' \neq k$.

878 Number of spatial factors.

879 In the human DLPFC example, we demonstrated that the NMF component in INSPIRE
880 enhances the accuracy of spot representations in the latent space. Additionally, we investigated
881 how varying the number of spatial factors in INSPIRE affects the quality of these spot
882 representations. The results indicate that the quality remained stable across different numbers
883 of spatial factors, with a slight improvement in accuracy as the number of spatial factors
884 increased (Supplementary Fig. 48 and Supplementary Note 1).

885 Next, we examined the relationship between the number of spatial factors and both the
886 quality of the spatial factors and the model fitting accuracy using the human DLPFC and
887 mouse brain data. The results suggest that increasing the number of spatial factors improves
888 model fit to the ST datasets but also reduces the diversity of the spatial factors. These examples
889 illustrate that the optimal number of spatial factors depends on the scale of the ST slices.
890 Specifically, for the human DLPFC slices, representing only a subregion of the brain, the factor
891 diversity score dropped below 50% when the number of spatial factors exceeded 20. In contrast,
892 for the mouse brain data, which includes multiple complementary views of the brain, the factor
893 diversity score remained above 50% even with 40 spatial factors (Supplementary Figs. 49, 50,
894 and Supplementary Note 2). Based on empirical observations, we recommend using number of
895 spatial factors $K = 20$ for analyzing a subregion of an organ, $K = 40$ for a complex organ, and
896 $K = 60$ for a whole organism. Alternatively, the INSPIRE model can be run with different
897 values of spatial factor number K , and we recommend selecting the largest K such that factor
898 diversity exceeds a specified threshold. By default, we suggest a threshold of 50%.

899 **Data availability.**

900 All data used in this work are publicly available through online sources.

- 901 • Human dorsolateral prefrontal cortex dataset profiled by Visium platform [40] (<https://research.libd.org/spatialLIBD/>).
- 902
- 903 • Mouse brain sagittal anterior, sagittal posterior, and coronal sections profiled by Visium
- 904 [30, 31, 32] (<https://www.10xgenomics.com/datasets>).
- 905 • Mouse brain slice profiled by Slide-seq V2 [7] (https://singlecell.broadinstitute.org/single_cell).
- 906
- 907 • Mouse brain slice profiled by MERFISH [47] (<https://doi.brainimaginglibrary.org/doi/10.35077/act-bag>).
- 908
- 909 • Mouse whole-embryo slice profiled by seqFISH [33] (<https://crukci.shinyapps.io/SpatialMouseAtlas/>).
- 910
- 911 • Mouse whole-embryo datasets across different developmental time points profiled by
- 912 Stereo-seq [8] (<https://db.cngb.org/stomics/mosta/>).
- 913 • Mouse hypothalamic preoptic region slices profiled by MERFISH [65] (<https://doi.org/10.5061/dryad.8t8s248>).
- 914
- 915 • Mouse hippocampus region slices profiled by SRARmap PLUS [13] (<https://doi.org/10.5281/zenodo.7458952>).
- 916

917 **Code availability.**

918 The INSPIRE software is available at <https://github.com/jiazhao97/INSPIRE>.

919 **Acknowledgements**

920 This work was supported in part by NIH grants R01 GM134005, U24 HG 012108, and P50
921 CA196530 to H.Z.; NCCIH grant R01 AT012041, the Allen Discovery Center program, a Paul
922 G. Allen Frontiers Group advised program of the Paul G. Allen Family Foundation to R.B.C.

923 References

- 924 [1] Ståhl, P. L. *et al.* Visualization and analysis of gene expression in tissue sections by spatial
925 transcriptomics. *Science* **353**, 78–82 (2016).
- 926 [2] Burgess, D. J. Spatial transcriptomics coming of age. *Nature Reviews Genetics* **20**, 317–317
927 (2019).
- 928 [3] Moses, L. & Pachter, L. Museum of spatial transcriptomics. *Nature Methods* **19**, 534–546
929 (2022).
- 930 [4] Tian, L., Chen, F. & Macosko, E. Z. The expanding vistas of spatial transcriptomics.
931 *Nature Biotechnology* **41**, 773–782 (2023).
- 932 [5] Larsson, L., Frisé, J. & Lundeberg, J. Spatially resolved transcriptomics adds a new
933 dimension to genomics. *Nature methods* **18**, 15–18 (2021).
- 934 [6] Rodriques, S. G. *et al.* Slide-seq: A scalable technology for measuring genome-wide
935 expression at high spatial resolution. *Science* **363**, 1463–1467 (2019).
- 936 [7] Stickels, R. R. *et al.* Highly sensitive spatial transcriptomics at near-cellular resolution
937 with Slide-seq2. *Nature biotechnology* **39**, 313–319 (2021).
- 938 [8] Chen, A. *et al.* Spatiotemporal transcriptomic atlas of mouse organogenesis using DNA
939 nanoball-patterned arrays. *Cell* **185**, 1777–1792 (2022).
- 940 [9] Lubeck, E., Coskun, A. F., Zhiyentayev, T., Ahmad, M. & Cai, L. Single-cell in situ RNA
941 profiling by sequential hybridization. *Nature methods* **11**, 360–361 (2014).
- 942 [10] Eng, C.-H. L. *et al.* Transcriptome-scale super-resolved imaging in tissues by RNA
943 seqFISH+. *Nature* **568**, 235–239 (2019).
- 944 [11] Chen, K. H., Boettiger, A. N., Moffitt, J. R., Wang, S. & Zhuang, X. Spatially resolved,
945 highly multiplexed RNA profiling in single cells. *Science* **348**, aaa6090 (2015).
- 946 [12] Wang, X. *et al.* Three-dimensional intact-tissue sequencing of single-cell transcriptional
947 states. *Science* **361**, eaat5691 (2018).

- 948 [13] Zeng, H. *et al.* Integrative in situ mapping of single-cell transcriptional states and tissue
949 histopathology in a mouse model of Alzheimer’s disease. *Nature Neuroscience* **26**, 430–446
950 (2023).
- 951 [14] Moncada, R. *et al.* Integrating microarray-based spatial transcriptomics and single-
952 cell RNA-seq reveals tissue architecture in pancreatic ductal adenocarcinomas. *Nature*
953 *Biotechnology* **38**, 333–342 (2020).
- 954 [15] Wang, G. *et al.* Construction of a 3D whole organism spatial atlas by joint modelling
955 of multiple slices with deep neural networks. *Nature Machine Intelligence* **5**, 1200–1213
956 (2023).
- 957 [16] Cang, Z. *et al.* Screening cell-cell communication in spatial transcriptomics via collective
958 optimal transport. *Nature methods* **20**, 218–228 (2023).
- 959 [17] Wan, X. *et al.* Integrating spatial and single-cell transcriptomics data using deep generative
960 models with SpatialScope. *Nature Communications* **14**, 7848 (2023).
- 961 [18] Qiu, X. *et al.* Mapping transcriptomic vector fields of single cells. *Cell* **185**, 690–711
962 (2022).
- 963 [19] Shang, L. & Zhou, X. Spatially aware dimension reduction for spatial transcriptomics.
964 *Nature communications* **13**, 7203 (2022).
- 965 [20] Brunet, J.-P., Tamayo, P., Golub, T. R. & Mesirov, J. P. Metagenes and molecular pattern
966 discovery using matrix factorization. *Proceedings of the national academy of sciences* **101**,
967 4164–4169 (2004).
- 968 [21] Duren, Z. *et al.* Integrative analysis of single-cell genomics data by coupled nonnegative
969 matrix factorizations. *Proceedings of the National Academy of Sciences* **115**, 7723–7728
970 (2018).
- 971 [22] Welch, J. D. *et al.* Single-cell multi-omic integration compares and contrasts features of
972 brain cell identity. *Cell* **177**, 1873–1887 (2019).
- 973 [23] Stein-O’Brien, G. L. *et al.* Enter the matrix: factorization uncovers knowledge from omics.
974 *Trends in Genetics* **34**, 790–805 (2018).

- 975 [24] Kotliar, D. *et al.* Identifying gene expression programs of cell-type identity and cellular
976 activity with single-cell RNA-Seq. *Elife* **8**, e43803 (2019).
- 977 [25] Puram, S. V. *et al.* Single-cell transcriptomic analysis of primary and metastatic tumor
978 ecosystems in head and neck cancer. *Cell* **171**, 1611–1624 (2017).
- 979 [26] Chung, W. *et al.* Single-cell RNA-seq enables comprehensive tumour and immune cell
980 profiling in primary breast cancer. *Nature communications* **8**, 15081 (2017).
- 981 [27] Chidester, B., Zhou, T., Alam, S. & Ma, J. SPICEMIX enables integrative single-cell
982 spatial modeling of cell identity. *Nature genetics* **55**, 78–88 (2023).
- 983 [28] Townes, F. W. & Engelhardt, B. E. Nonnegative spatial factorization applied to spatial
984 genomics. *Nature methods* **20**, 229–238 (2023).
- 985 [29] Lee, D. D. & Seung, H. S. Learning the parts of objects by non-negative matrix factorization.
986 *nature* **401**, 788–791 (1999).
- 987 [30] Mouse brain sagittal anterior section by Visium from 10X Genomics.
988 [https://www.10xgenomics.com/datasets/mouse-brain-serial-section-2-sagittal-anterior-1-](https://www.10xgenomics.com/datasets/mouse-brain-serial-section-2-sagittal-anterior-1-standard-1-0-0)
989 [standard-1-0-0.](https://www.10xgenomics.com/datasets/mouse-brain-serial-section-2-sagittal-anterior-1-standard-1-0-0)
- 990 [31] Mouse brain sagittal posterior section by Visium from 10X Genomics.
991 [https://www.10xgenomics.com/datasets/mouse-brain-serial-section-2-sagittal-posterior-](https://www.10xgenomics.com/datasets/mouse-brain-serial-section-2-sagittal-posterior-1-standard-1-0-0)
992 [1-standard-1-0-0.](https://www.10xgenomics.com/datasets/mouse-brain-serial-section-2-sagittal-posterior-1-standard-1-0-0)
- 993 [32] Mouse brain coronal section by Visium from 10X Genomics.
994 [https://www.10xgenomics.com/datasets/mouse-brain-section-coronal-1-standard-1-](https://www.10xgenomics.com/datasets/mouse-brain-section-coronal-1-standard-1-1-0)
995 [1-0.](https://www.10xgenomics.com/datasets/mouse-brain-section-coronal-1-standard-1-1-0)
- 996 [33] Lohoff, T. *et al.* Integration of spatial and single-cell transcriptomic data elucidates mouse
997 organogenesis. *Nature biotechnology* **40**, 74–85 (2022).
- 998 [34] Zhao, J. *et al.* Adversarial domain translation networks for integrating large-scale atlas-level
999 single-cell datasets. *Nature computational science* **2**, 317–330 (2022).
- 1000 [35] Liu, W. *et al.* Probabilistic embedding, clustering, and alignment for integrating spatial
1001 transcriptomics data with PRECAST. *Nature communications* **14**, 296 (2023).

- 1002 [36] Luecken, M. D. *et al.* Benchmarking atlas-level data integration in single-cell genomics.
1003 *Nature methods* **19**, 41–50 (2022).
- 1004 [37] Goodfellow, I. *et al.* Generative Adversarial Nets. In *Advances in Neural Information*
1005 *Processing Systems*, 2672–2680 (2014).
- 1006 [38] Veličković, P. *et al.* Graph attention networks. In *International Conference on Learning*
1007 *Representations* (2018).
- 1008 [39] Kipf, T. N. & Welling, M. Semi-Supervised Classification with Graph Convolutional
1009 Networks. In *International Conference on Learning Representations* (2017).
- 1010 [40] Maynard, K. R. *et al.* Transcriptome-scale spatial gene expression in the human dorsolateral
1011 prefrontal cortex. *Nature Neuroscience* **24**, 425–436 (2021).
- 1012 [41] Gilmore, E. C. & Herrup, K. Cortical development: layers of complexity. *Current Biology*
1013 **7**, R231–R234 (1997).
- 1014 [42] Hao, Y. *et al.* Integrated analysis of multimodal single-cell data. *Cell* **184**, 3573–3587
1015 (2021).
- 1016 [43] Zeira, R., Land, M., Strzalkowski, A. & Raphael, B. J. Alignment and integration of
1017 spatial transcriptomics data. *Nature Methods* **19**, 567–575 (2022).
- 1018 [44] Dieng, A. B., Ruiz, F. J. & Blei, D. M. Topic modeling in embedding spaces. *Transactions*
1019 *of the Association for Computational Linguistics* **8**, 439–453 (2020).
- 1020 [45] Oh, S. W. *et al.* A mesoscale connectome of the mouse brain. *Nature* **508**, 207–214 (2014).
- 1021 [46] Kleshchevnikov, V. *et al.* Cell2location maps fine-grained cell types in spatial transcrip-
1022 tomics. *Nature Biotechnology* **40**, 661–671 (2022).
- 1023 [47] Zhang, M. *et al.* Molecularly defined and spatially resolved cell atlas of the whole mouse
1024 brain. *Nature* **624**, 343–354 (2023).
- 1025 [48] Wolf, F. A., Angerer, P. & Theis, F. J. SCANPY: large-scale single-cell gene expression
1026 data analysis. *Genome biology* **19**, 1–5 (2018).

- 1027 [49] Renaud, J. *et al.* Plexin-A2 and its ligand, Sema6A, control nucleus-centrosome coupling
1028 in migrating granule cells. *Nature neuroscience* **11**, 440–449 (2008).
- 1029 [50] Weinert, S., Bergmann, N., Luo, X., Erdmann, B. & Gotthardt, M. M line-deficient titin
1030 causes cardiac lethality through impaired maturation of the sarcomere. *The Journal of*
1031 *cell biology* **173**, 559–570 (2006).
- 1032 [51] Breher, S. S. *et al.* Popeye domain containing gene 2 (Popdc2) is a myocyte-specific
1033 differentiation marker during chick heart development. *Developmental dynamics: an*
1034 *official publication of the American Association of Anatomists* **229**, 695–702 (2004).
- 1035 [52] Lagutin, O. V. *et al.* Six3 repression of Wnt signaling in the anterior neuroectoderm is
1036 essential for vertebrate forebrain development. *Genes & development* **17**, 368–379 (2003).
- 1037 [53] Porter, F. D. *et al.* Lhx2, a LIM homeobox gene, is required for eye, forebrain, and
1038 definitive erythrocyte development. *Development* **124**, 2935–2944 (1997).
- 1039 [54] Sasaki, H. & Hogan, B. L. Differential expression of multiple fork head related genes
1040 during gastrulation and axial pattern formation in the mouse embryo. *Development* **118**,
1041 47–59 (1993).
- 1042 [55] Collins, M. M., Baumholtz, A. I. & Ryan, A. K. Claudin family members exhibit unique
1043 temporal and spatial expression boundaries in the chick embryo. *Tissue Barriers* **1**, e24517
1044 (2013).
- 1045 [56] Kuwahara, A. *et al.* Delineating the early transcriptional specification of the mammalian
1046 trachea and esophagus. *Elife* **9**, e55526 (2020).
- 1047 [57] Que, J. *et al.* Multiple dose-dependent roles for Sox2 in the patterning and differentiation
1048 of anterior foregut endoderm. *Development* **134**, 2521–2531 (2007).
- 1049 [58] Kim, E. *et al.* Isl1 regulation of Nkx2. 1 in the early foregut epithelium is required for
1050 trachea-esophageal separation and lung lobation. *Developmental cell* **51**, 675–683 (2019).
- 1051 [59] Richardson, L. *et al.* EMAGE mouse embryo spatial gene expression database: 2014
1052 update. *Nucleic acids research* **42**, D835–D844 (2014).

- 1053 [60] Simeone, A., Acampora, D., Gulisano, M., Stornaiuolo, A. & Boncinelli, E. Nested
1054 expression domains of four homeobox genes in developing rostral brain. *Nature* **358**,
1055 687–690 (1992).
- 1056 [61] Savolainen, S. M., Foley, J. F. & Elmore, S. A. Histology atlas of the developing mouse
1057 heart with emphasis on e11.5 to e18.5. *Toxicologic pathology* **37**, 395–414 (2009).
- 1058 [62] Atala, A., Lanza, R., Mikos, T. & Nerem, R. *Principles of regenerative medicine* (Academic
1059 press, 2018).
- 1060 [63] Schaum, N. *et al.* Single-cell transcriptomics of 20 mouse organs creates a Tabula Muris:
1061 The Tabula Muris Consortium. *Nature* **562**, 367 (2018).
- 1062 [64] Qiu, C. *et al.* A single-cell time-lapse of mouse prenatal development from gastrula to birth.
1063 *Nature* **626**, 1084–1093 (2024). URL <https://doi.org/10.1038/s41586-024-07069-w>.
- 1064 [65] Moffitt, J. R. *et al.* Molecular, spatial, and functional single-cell profiling of the hypotha-
1065 lamic preoptic region. *Science* **362**, eaau5324 (2018).
- 1066 [66] Dong, K. & Zhang, S. Deciphering spatial domains from spatially resolved transcriptomics
1067 with an adaptive graph attention auto-encoder. *Nature Communications* **13**, 1739 (2022).
- 1068 [67] Xia, C.-R., Cao, Z.-J., Tu, X.-M. & Gao, G. Spatial-linked alignment tool (SLAT) for
1069 aligning heterogenous slices. *Nature Communications* **14**, 7236 (2023).
- 1070 [68] Kingma, D. P. & Ba, J. Adam: A method for stochastic optimization. In *International*
1071 *Conference on Learning Representations* (2015).