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# Probing the structure and electronic properties of beryllium doped boron clusters: A planar $\text{BeB}_{16}^-$ cluster motif for metallo-borophene

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Beryllium-doped boron clusters display essential similarities to borophene (boron sheet) with a molecular structure characterized by remarkable properties, such as anisotropy, metallicity and high conductivity. Here we have determined low-energy structures of  $\text{BeB}_n^{0/-}$  ( $n = 10\text{--}20$ ) clusters by utilizing CALYPSO searching program and DFT optimization. The results indicated that most ground states of clusters prefer plane or quasi-plane structures by doped Be atom. A novel unexpected fascinating planar  $\text{BeB}_{16}^-$  cluster with  $C_{2v}$  symmetry is uncovered which possesses robust relative stability. Furthermore, planar  $\text{BeB}_{16}^-$  offers a possibility to construct metallo-borophene nano-materials. Molecular orbital and chemical bonding analysis reveal the peculiarities of  $\text{BeB}_{16}^-$  cluster brings forth the aromaticity and the strong interaction of B-B  $\sigma$ -bonds in boron network.

Molecular geometric configuration and attributes of pure<sup>1–3</sup> and doped boron clusters<sup>4–9</sup> have drawn much attention in recent years. The use of boron clusters as subunits in novel bioactive architectures with potential use as drugs is of primary importance<sup>10</sup>. From a Materials Science perspective the emergence of graphene<sup>11</sup> and synthetic two-dimensional structures as silicene<sup>12,13</sup>, germanene<sup>14</sup>, stanene<sup>15</sup>, antimonene<sup>16</sup>, bismuthene<sup>17,18</sup> and tellurene<sup>19</sup> have opened new pathways for modern research<sup>20–22</sup>. Relying on experimental and theoretical work, Hersam's group<sup>23</sup> have confirmed and established the synthesis of 2D boron polymorphs (borophene) characterized by anisotropy and metallicity, and paved the way to investigations leading to the discovery of novel materials. Recently, it was reported that magnesium diboride ( $\text{MgB}_2$ ), which consists of graphene-like honeycomb networks of sandwiched boron, shows superconductivity<sup>24</sup>. It should be noted that beryllium has the same valence electrons number with magnesium. Be-doped boron clusters appear to have significant potential candidate as layered 2D materials<sup>25–28</sup>. This certainly gives reason for more systematic investigations.

Boron is the lightest metalloid chemical element, the lowest-Z element<sup>23</sup> with a trivalent outer shell<sup>29,30</sup>. Consequently, boron does not form closed-shell electronic structures via conventional covalent bonds<sup>31–33</sup>, but favors delocalized chemical bonds with electron pairs shared among three (or more) atoms instead. Recently, systematic investigations of pure boron clusters in term of the anisotropy and polymorphism have brought forth new significant findings leading to the design of new borides. A selection of characteristic architectures of pure boron clusters includes: tank tread<sup>34</sup>, wankel motor<sup>35–39</sup>, wheel-like<sup>40</sup>, boron nanotubes<sup>41</sup>,  $B_{12}$  icosahedra<sup>42</sup>, buckyballs<sup>43</sup>, fullerene<sup>44</sup>,  $B_{36}$  with hexagonal holes (HHs)<sup>45</sup>, naphthalene<sup>46</sup>, borospherene<sup>47</sup> and more. Co and Rh doped  $B_{12}^-$  clusters featured half-sandwich structure has been reported by Wang and co-workers<sup>48</sup>. There followed the Co-centered boron molecular drums structure for the  $\text{CoB}_{16}^-$  cluster<sup>49</sup>. Additional work by the same group includes the Mn-centered tubular boron cluster for  $\text{MnB}_{16}^-$ , a drum and quasi-planar structure for  $\text{RhB}_{18}^-$  and the planar  $\text{CoB}_{18}^-$ <sup>50–52</sup>. Very recently, Cui and co-workers reported tubular structures for  $\text{LiB}_{20}$  and  $\text{LiB}_{20}^-$ <sup>53</sup>. These

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impressive findings reveal that single metal atom doping leads to new opportunities for the use of boron clusters as geometrical ligands.

Several theoretical investigations of boron clusters with doping transition-element serve as the object of discovering new materials recently<sup>54,55</sup>. The alkaline-earth metal-doped boron clusters and Be-doped ones in particular have been systematically studied<sup>56–58</sup>. Nevertheless, more systematic work is needed to systematize and deepen our understanding of Be-doped boron clusters. To fill the existing lacunae and bring forth new insights on medium-sized Be-doped boron clusters, we have thoroughly investigated  $\text{BeB}_n^{0/-}$  clusters.

## Results and Discussion

**Geometric configurations and photoelectron spectra.** The determined low-energy  $\text{BeB}_n^{0/-}$  ( $n = 10–20$ ) are shown in Figs 1 and 2. We labeled each isomer using  $nt/t^-$  ( $t = a, b, c$ ), therein  $nt$  stands for the neutral clusters and  $nt^-$  stands for the anionic clusters. The lowest-energy structures  $\text{BeB}_n^{0/-}$  ( $n = 10, 12, 13, 14, 15, 16$ ) and  $\text{BeB}_{11}^-$  are quasi-planar structures. The lowest-energy structure  $\text{BeB}_{11}$  shows a half-sandwich structure consisting of one half-sandwich structure composed by eleven boron atoms and one Be atom in the center. The lowest-energy structures  $\text{BeB}_{17}^{0/-}$  like a trapezoid and its center portion appear on the convex. The lowest-energy structure of  $\text{BeB}_{18}$  and  $\text{BeB}_{20}^-$  are 3D cage-like structure. The lowest-energy structure  $\text{BeB}_{18}^-$  with a parallelogram located in the center displays a planar structure. The ground-state structures  $\text{BeB}_{19}^{0/-}$  and  $\text{BeB}_{20}$  can be viewed as plate-like structures (in Figs S4 and S5 of Supplementary Information). The lowest-energy structures of  $\text{BeB}_n^{0/-}$  clusters are generally evolutionary from the quasi-planar to 3D cage-like or plate-like structures. For plane and quasi-planar structures, the coordinate number of Be atom is interesting. The  $\text{BeB}_n^{0/-}$  ( $n = 10, 12, 14, 16$ ) and  $\text{BeB}_{18}^-$  feature heptacoordinate and the  $\text{BeB}_{11}^-$  and  $\text{BeB}_n^{0/-}$  ( $n = 13, 15$ ) possess octacoordinate, while the  $\text{BeB}_{17}^{0/-}$  are quasi-planar hexacoordinate structures due to the attribute of Be atom<sup>59,60</sup>. This evident structures evolution pattern contributes to form plane clusters of  $\text{BeB}_n^{0/-}$ , which are potential two-dimensional material. The metastable of  $nb/b^-$  ( $n = 10–13$ ) clusters display half-sandwich architectural feature, while when the cluster sizes increase  $n \geq 14$ , the clusters are varies cage-like, quasi-planar and plate-like structures. The  $nc/c^-$  ( $n = 10–18$ ) clusters display half-sandwich, plane, cage-like structures, different from the larger size isomers ( $n \geq 19$ ) are double-ring and plate-like structures.

To get a deep understand to differences between different metal-doped clusters, we provide a comparison for doped boron clusters. The transition-metal doped boron clusters,  $\text{NbB}_{10}^-$  and  $\text{TaB}_{10}^-$ , are wheels structures with high coordination number<sup>4</sup>, while  $\text{BeB}_{10}^{0/-}$  clusters are quasi-planar structures with one B-Be unit inside. For doped  $\text{B}_{12}$  clusters, the prior works report that half-sandwich structures  $\text{VB}_{10}^-$ ,  $\text{CoB}_{12}^-$  and  $\text{RhB}_{12}^-$  clusters<sup>4,48</sup> are different with  $\text{BeB}_{12}^{0/-}$  clusters, which are standard quasi-planar structures featuring a triangle in the center. Compare with drum-like  $\text{CoB}_{16}^-$  cluster<sup>49</sup> and tubular-like  $\text{MnB}_{16}^-$  cluster<sup>50</sup>, the ground state  $\text{BeB}_{16}^{0/-}$  display quasi-plane structures. It is worth noting that adjacent alkali element Lithium doped into  $\text{B}_{20}$  display highly symmetrical tubular  $\text{LiB}_{20}^{0/-}$  clusters<sup>53</sup>. We report  $\text{BeB}_{20}$  and  $\text{BeB}_{20}^-$  are plate-like and 3D cage-like structures, respectively. The reason for the structural differences of same-sized clusters may be doped-metals have different valence electron and atomic radius<sup>61</sup>.

Photoelectron spectra (PES) analysis, obtained via a TD-DFT approach, is of absolute importance for the assessment of the nature of the determined lowest-energy structures. We simulated the PES of  $\text{BeB}_n^-$  clusters and the results are displayed in Fig. 3. Our group also simulated the PES of some other cluster system using the method<sup>62,63</sup>. The PES pattern of the  $\text{BeB}_{10}^-$  possesses five peaks located at 3.26, 3.75, 4.18, 4.75 and 5.77 eV. The PES of  $\text{BeB}_{11}^-$  possesses four clear peaks at 3.45, 4.21, 4.59, and 5.01 eV, with B and C peaks forming a broad bond. For  $\text{BeB}_{12}^-$ , we observe three major peaks at 2.90, 4.21 and 4.50 eV, wherein the double-peak feature (A and B) is prominent and broad. The  $\text{BeB}_{13}^-$  PES contains five major peaks at 3.16, 3.49, 4.32, 4.75 and 5.22 eV. The relevant broad bond is found at triple-peak feature consisted of peaks B, C and D. Five peaks are observed for  $\text{BeB}_{14}^-$  at 3.33, 3.86, 4.16, 4.63 and 5.45 eV. The peaks A, B and C constitute a relatively wide bond. For  $\text{BeB}_{15}^-$  there are five major peaks at 3.46, 4.28, 4.64, 5.06 and 5.82 eV, whereas the  $\text{BeB}_{16}^-$  spectrum has only two sparse peaks at 4.08 and 5.25 eV. The well-structure spectrum of  $\text{BeB}_{17}^-$  shows five peaks at 3.90, 4.32, 4.79, 5.13 and 5.49 eV, suggesting a greater span triple-peak feature (B, C and D). A crowded spectrum pattern  $\text{BeB}_{18}^-$  has five peaks observed at 3.59, 3.98, 4.21, 5.13 and 5.57 eV, with two broad bonds. There are five peaks in the spectrum of  $\text{BeB}_{19}^-$  at 3.63, 4.73, 5.13, 5.51 and 5.82 eV, therein an unfitted bond is located at the range between 4.5 to 6.0 eV. The spectrum of  $\text{BeB}_{20}^-$  possesses five peaks at 2.59, 3.36, 4.43, 4.85 and 5.79 eV.

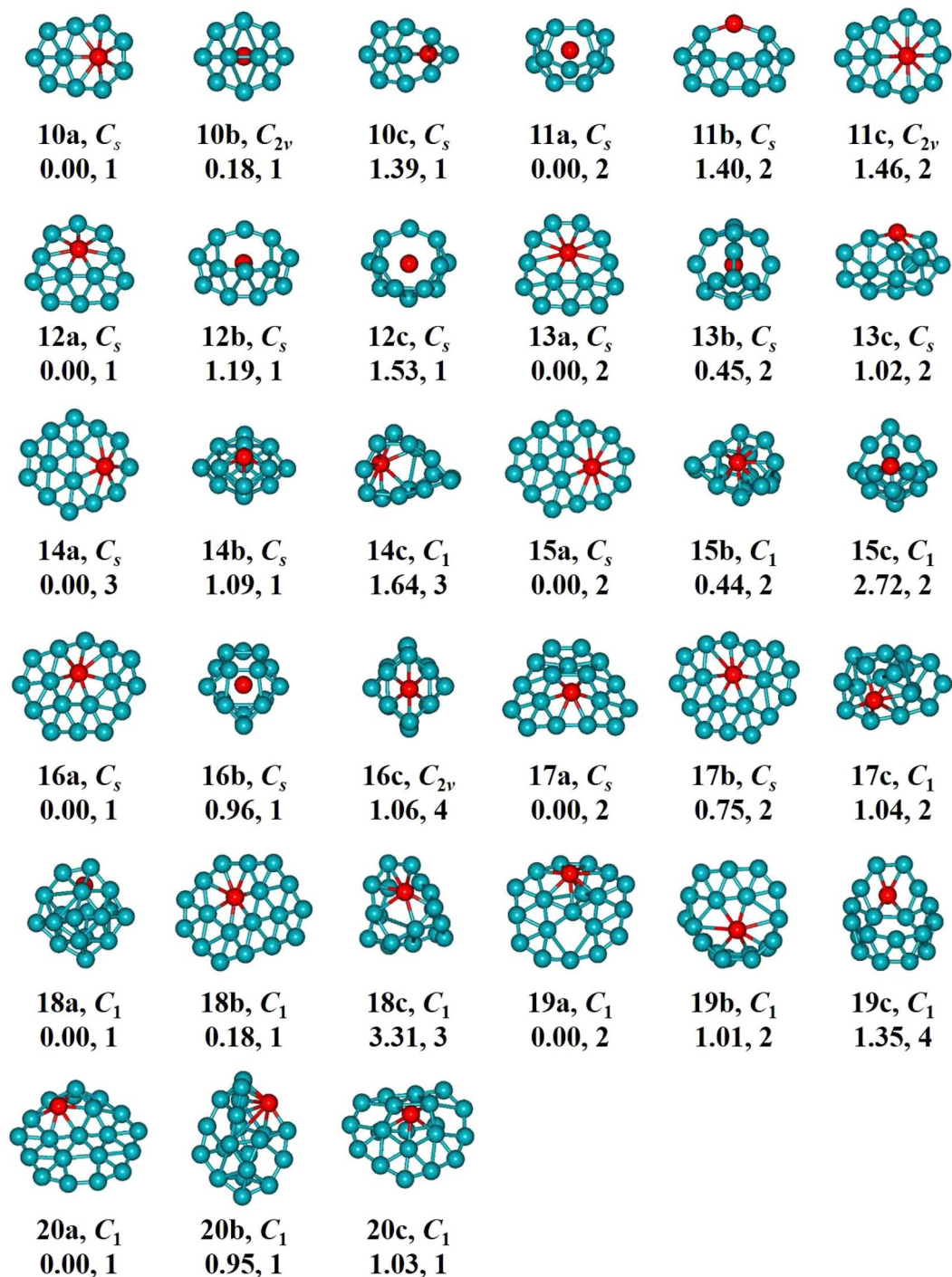
**Relative stabilities.** We characterize the inherent stability of the  $\text{BeB}_n^{0/-}$  ( $n = 10–20$ ) clusters by computing the  $E_b$  (eV), according to the following formula:

$$E_b(\text{BeB}_n) = [nE(\text{B}) + E(\text{Be}) - E(\text{BeB}_n)]/(n + 1) \quad (1)$$

$$E_b(\text{BeB}_n^-) = [(n - 1)E(\text{B}) + E(\text{B}^-) + E(\text{Be}) - E(\text{BeB}_n^-)]/(n + 1) \quad (2)$$

The average binding energy ( $E_b$ ) of a cluster is clearly a measure of its thermodynamic stability. An increase in  $E_b$  means a higher stability. The value of neutral  $\text{BeB}_n$  clusters less than the value of their anionic counterparts in Fig. S1(a), indicating that the anionic clusters feature higher thermodynamically. The trend of the curves for both neutral and anionic are gradually upward indicated that the high thermodynamic stability with the cluster size increases. The second vital physical quantity we take into account here is the  $\Delta^2 E$ . The relevant formulae are

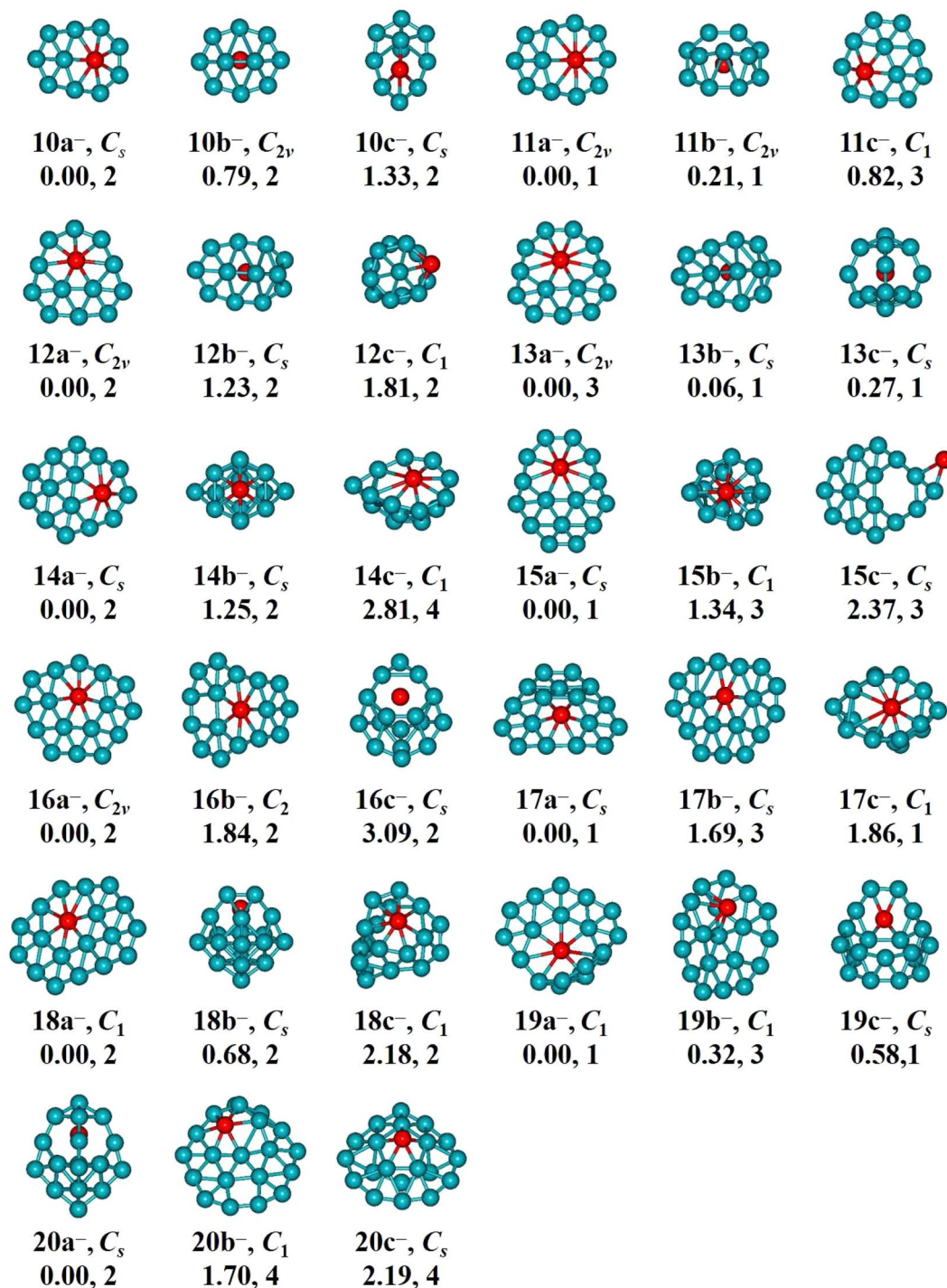
$$\Delta^2 E(\text{BeB}_n) = E(\text{BeB}_{n-1}) + E(\text{BeB}_{n+1}) - 2E(\text{BeB}_n) \quad (3)$$



**Figure 1.** Low-lying geometrical structures of  $BeB_n$  ( $n = 10-20$ ) clusters. “a” stands for the lowest-energy structures. “b” and “c” stand for the metastable state structures.

$$\Delta^2 E(BeB_n^-) = E(BeB_{n-1}^-) + E(BeB_{n+1}^-) - 2E(BeB_n^-) \quad (4)$$

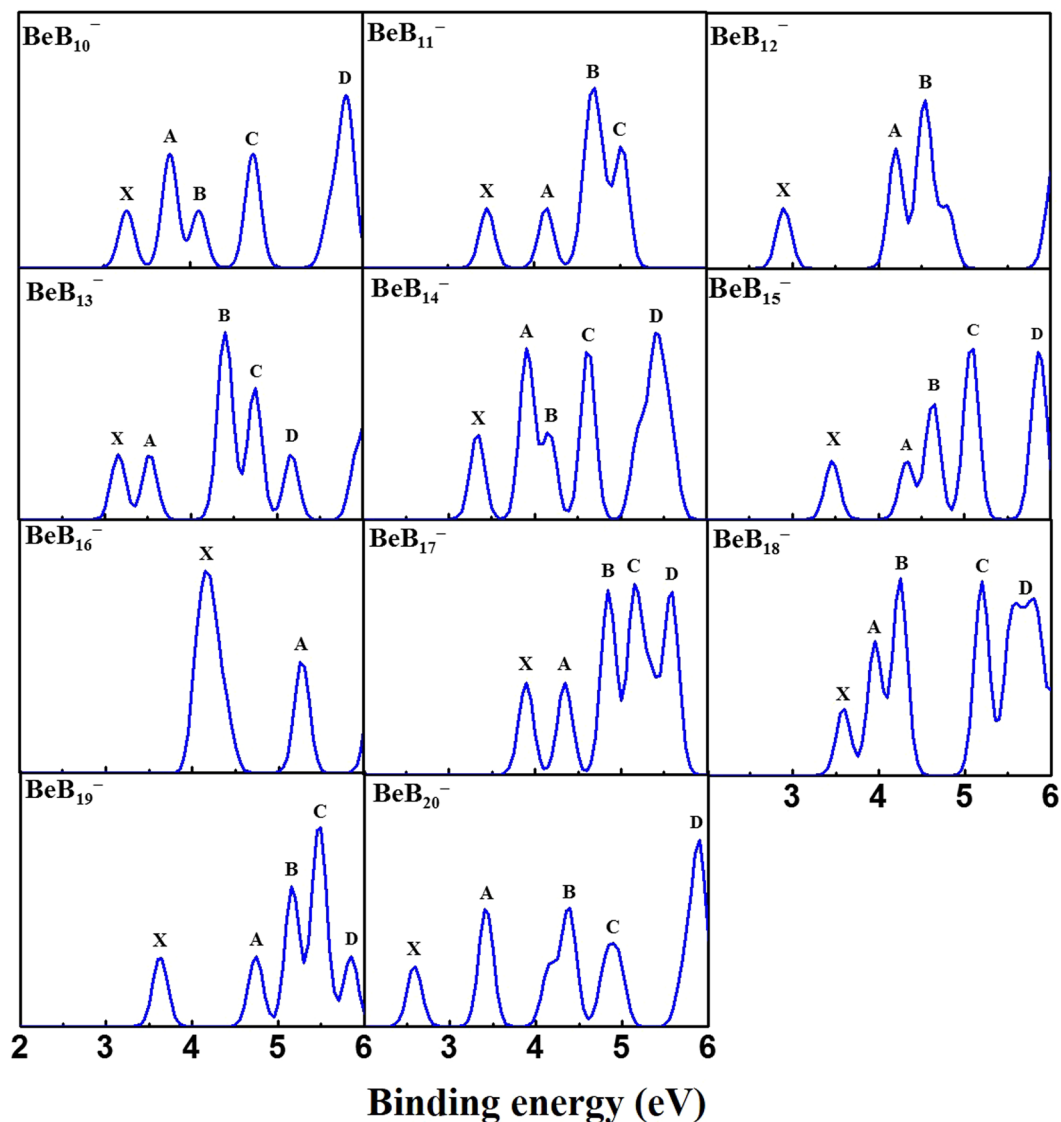
As inferred from Fig. S1(b), both of the neutral and anionic curves show odd-even alternation. The evident peak values generated at  $n = \text{even}$  number, suggest that clusters with the even boron atoms feature higher stability than which with odd boron atoms. Finally, we discuss the HOMO-LUMO energy gap ( $E_{gap}$ ) which provides a valuable index of the stability of clusters. Large values indicate strong chemical stability. We summarize the  $E_{gap}$  values of the lowest-energy  $BeB_n^{0/-}$  clusters in Table 1, and the line chart is displayed in Fig. S1(c). From the latter we can clearly see some apparent local maxima:  $BeB_{11}$  and  $BeB_{16}^-$ , which means that they feature higher stability



**Figure 2.** Low-lying geometrical structures of BeB<sub>n</sub><sup>-</sup> ( $n=10-20$ ) clusters. “a” stands for the lowest-energy structures. “b” and “c” stand for the metastable state structures.

than the others. Consequently, based on the above analyses, we can reach a definitive conclusion that the BeB<sub>16</sub><sup>-</sup> can be seen as a “magic” cluster.

**Chemical banding.** To deeply perceive the bonding nature of BeB<sub>16</sub><sup>-</sup> (C<sub>2v</sub> symmetry), we display eleven MO figures for BeB<sub>16</sub><sup>-</sup>, including one LUMO, one HOMO and nine HOMO- $n$  ( $n=1-9$ ) in Fig. 4 by analyzing the chemical bonding. The LUMO, HOMO, HOMO-2, HOMO-5 and HOMO-9 dominated primarily by  $\pi_p$  and  $\pi_p^*$  orbitals are a direct interaction  $2p$  orbitals of B atoms. The HOMO- $n$  ( $n=1, 4, 8$ ) feature  $\sigma_p$  and  $\sigma_p^*$  orbitals. The HOMO- $n$  ( $n=3, 6, 7$ ) features  $\sigma_p$ ,  $\sigma_p^*$ ,  $\sigma_{sp}$  and  $\sigma_{sp}^*$  orbitals. AdNDP analysis distributes 51 valence electrons into different regions as reflected by the occupation numbers (ONs) in Fig. 5. We divide it into three sets. The first set consists of twelve  $2c-2e$  (1.79–1.93 |e|) localized  $\sigma$ -bonds. The second set consists of nine delocalized  $\sigma$ -bonds,



**Figure 3.** The simulated PES of  $\text{BeB}_n^-$  ( $n = 10\text{--}20$ ) clusters.

$\text{BeB}_n$					$\text{BeB}_n^-$			
$n$	Sta.	Sym.	$E_b$	$E_{gap}$	Sta.	Sym.	$E_b$	$E_{gap}$
10	$^1A'$	$C_s$	4.69	2.93	$^2A''$	$C_s$	5.06	2.81
11	$^2A'$	$C_s$	4.73	3.30	$^1A_1$	$C_{2v}$	5.08	2.36
12	$^1A'$	$C_s$	4.87	2.94	$^2A_2$	$C_{2v}$	5.17	1.66
13	$^2A''$	$C_s$	4.84	1.74	$^3B_2$	$C_{2v}$	5.14	2.17
14	$^3A''$	$C_s$	4.90	2.47	$^2A''$	$C_s$	5.23	2.14
15	$^2A''$	$C_s$	4.93	1.85	$^1A'$	$C_s$	5.20	1.89
16	$^1A'$	$C_s$	4.99	1.77	$^2B_2$	$C_{2v}$	5.29	2.93
17	$^2A'$	$C_s$	5.03	2.17	$^1A'$	$C_s$	5.30	2.03
18	$^1A$	$C_1$	5.08	2.60	$^2A$	$C_1$	5.32	1.89
19	$^2A$	$C_1$	5.18	1.97	$^1A$	$C_1$	5.25	2.39
20	$^1A$	$C_1$	5.10	2.67	$^2A'$	$C_s$	5.31	2.09

**Table 1.** The calculated electronic states, symmetries, average binding energies ( $E_b$ , in eV) and energy gaps ( $E_{gap}$ , in eV) of  $\text{BeB}_n^{0/-}$  clusters in the size range of  $n = 10\text{--}20$ .

which are five  $3c\text{-}2e$  (1.79–1.86 |e|), two  $4c\text{-}2e$  (1.72 |e|), and two  $4c\text{-}2e$  (1.79 |e|). The five delocalized  $\pi$ -bonds in last set involving two  $4c\text{-}2e$  (1.81 |e|), two  $4c\text{-}2e$  (1.83 |e|) and one  $17c\text{-}2e$  (2.00 |e|). It is worth nothing that the ON of the  $17c\text{-}2e$   $\pi$ -bonds maintain ON of 2.00 |e|. All values of the ONs listed above ranging from 1.72–2.00 |e|

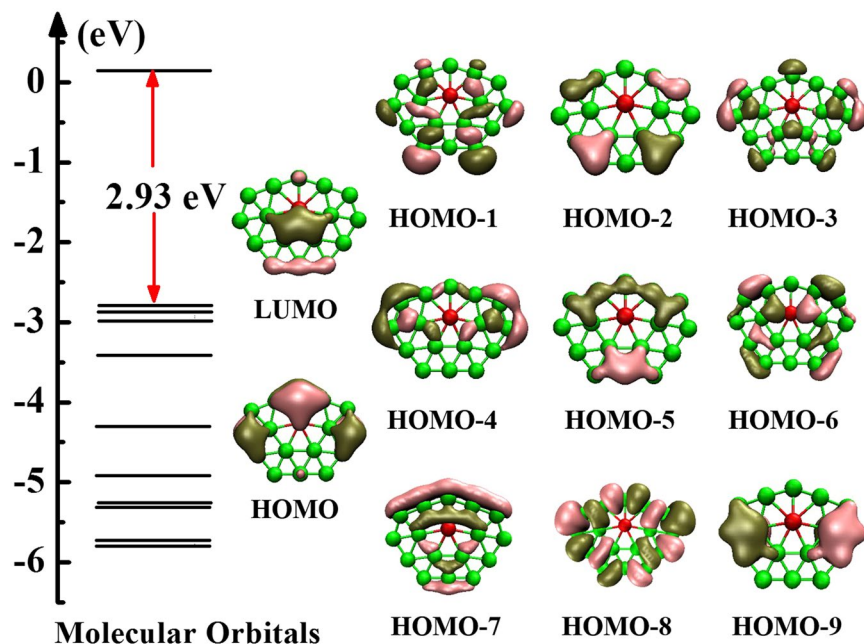


Figure 4. Molecular orbitals for  $\text{BeB}_{16}^-$  cluster corresponding to different energy level.

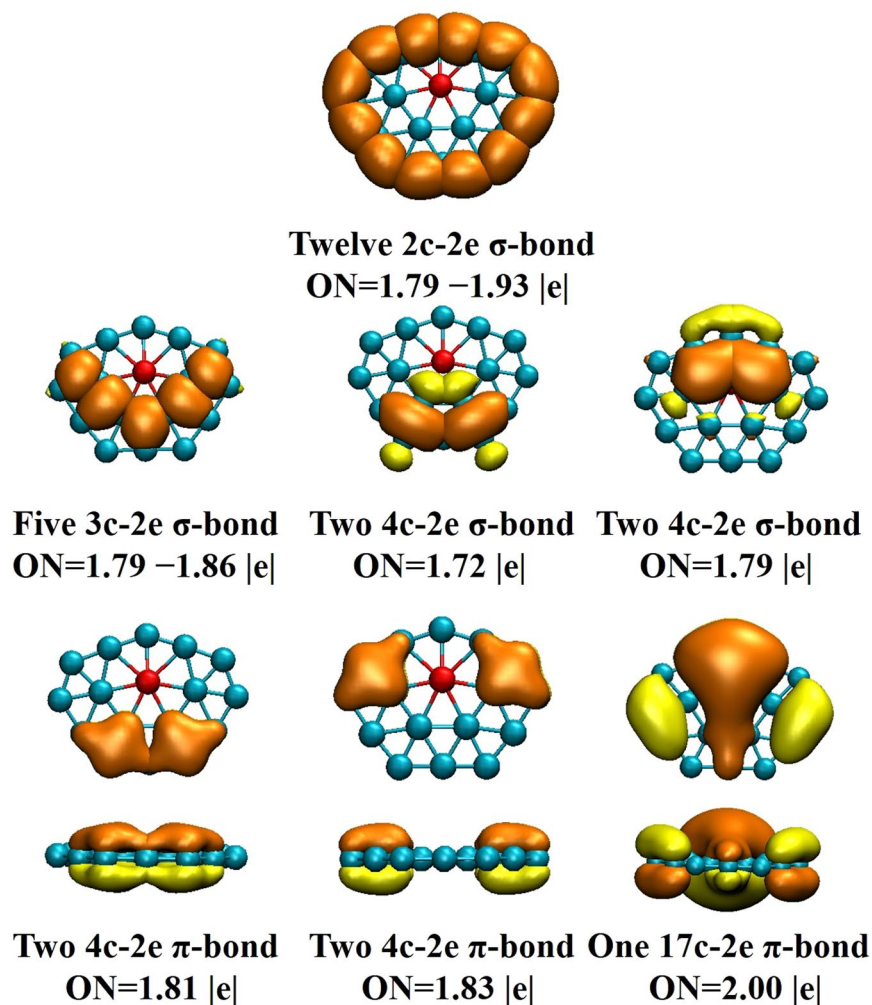


Figure 5. AdNDP analysis of  $\text{BeB}_{16}^-$  cluster.

are approaching the ideal value 2.00 |e|, which means that the results we calculate is fairly credible. Furthermore, the ten  $\pi$  electrons conform to the  $4n + 2$  rule ( $n = 2$ ), indicating the  $\text{BeB}_{16}^-$  cluster possesses  $\pi$ -aromaticity, which result to the robust relative stability for  $\text{BeB}_{16}^-$  cluster.

The Wiberg bond index of  $\text{BeB}_{16}^-$ , showed in Fig. S2(a), indicate that the bond orders values of B-B (0.13–0.35) greater than the Be-B (0.06–0.11). For Fig. S2(b), the B-B bond lengths (1.54–1.80 Å) are shorter than Be-B bond lengths (1.85–2.03 Å). The results of bond orders and bond lengths show that the peripheral B-B bonds are stronger than the inner Be-B bonds. We have also performed the NPA (natural charge of atom) calculations of  $\text{BeB}_n^{0/-}$  in Fig. S3 indicate that electron transfer from Be atom to boron fragment. The NPA data of  $\text{BeB}_n^{0/-}$  ( $n = 10$ –20) clusters are summarized in Table S1. From what has been discussed, we come to the conclusion that the B-B  $\sigma$ -bonds and the aromaticity decide the high stability of  $\text{BeB}_{16}^-$  cluster. It is worth noting that due to planar structure and chemical bonding characteristics of  $\text{BeB}_{16}^-$  cluster, also inspired by fascinating prospect of two-dimensional monolayer metallo-borophene<sup>4</sup>, we successfully build a schematic of possibility of metallo-borophene (not optimized) based on  $\text{BeB}_{16}^-$  unit cluster presented in Fig. S6 of Supplementary Information, which indicated the  $\text{BeB}_{16}^-$  cluster is a potential motif for metallo-borophene.

## Conclusions

In summary, the ground-state  $\text{BeB}_n^{0/-}$  ( $n = 10$ –20) structure obey the evolution rule: quasi-planar to 3D cage-like or plate-like structures, which the doped Be atom contributed to the plane or quasi-plane structures. We hope that the simulated PES can provide valuable guidance for future research on  $\text{BeB}_n$  clusters and borophene. Based on the relative stability analysis, the  $\text{BeB}_{16}^-$  cluster characterized by enhanced stability is clearly a “magic” cluster. Chemical bonding analysis indicated that  $\text{BeB}_{16}^-$  cluster adapt  $\pi$ -aromaticity and the strong interaction of B-B  $\sigma$ -bonds which is deemed as the dominant reasons for the inherent stability of  $\text{BeB}_{16}^-$  cluster. The planar  $\text{BeB}_{16}^-$  cluster may serve as a motif for the design of a new boron-based functional material to complement the metallo-borophene effort for synthetic 2D materials development. Our present findings on Be-doped boron clusters should provide valuable information for further explorations of novel cluster architectures.

## Computational Methods

We used the CALYPSO code to search the  $\text{BeB}_n^{0/-}$  ( $n = 10$ –20) clusters. The global explorations of Be-doped boron cluster system was implemented by utilizing particle swarm optimization (PSO) algorithm<sup>64–66</sup>. The effectiveness of this structural prediction method, has been successfully tested on the identification of ground-state structures of various systems<sup>67–69</sup>. To ensure high efficiency in structure predicting, we proceeded to 50 generations for each size, where each generation contains 30 structures. PSO algorithm produces sixty percent of the structures and the rest is generated randomly. The top fifty low-lying isomers were reoptimized with PBE0<sup>70</sup> functional and 6–311 + G(d)<sup>71</sup>, as performed via Gaussian 09 package<sup>72</sup>. The PES of Be-doped boron clusters was simulated utilizing TD-DFT method<sup>73</sup>. We then analyzed chemical bonding of  $\text{BeB}_{16}^-$  cluster relying on the NBO and AdNDP methods<sup>74</sup> at the PBE0/6-311 + G(d) level to display valuable insights into the nature of the bonding by using Multiwfn<sup>75</sup>. The bond orders, bond lengths and NPA are also computed by using the same basis set and method.

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## Author Contributions

X.Y.K. and C.L. conceived the idea. D.L.K., W.G.S. and C.L. performed the calculations. D.L.K., W.G.S., H.X.S., B.L.C., X.X.X. and G.M. wrote the manuscript. All authors reviewed the manuscript.

## Additional Information

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