

1 Predictive performance of international COVID-19 2 mortality forecasting models

3 Joseph Friedman*, Patrick Liu*, Christopher E. Troeger, Austin Carter, Robert C. Reiner JR, Ryan M.
4 Barber, James Collins, Stephen S. Lim, David M. Pigott, Theo Vos, Simon I. Hay[†], Christopher J.L.
5 Murray[†], Emmanuela Gakidou^{†**}

6

7 *These authors contributed equally to the analysis and are listed in alphabetical order.

8 [†]These authors jointly supervised the work.

9 **Correspondence to: Emmanuela Gakidou (gakidou@uw.edu).

10

11 Abstract

12 Forecasts and alternative scenarios of COVID-19 mortality have been critical inputs into a range of
13 policies and decision-makers need information about predictive performance. We identified n=386
14 public COVID-19 forecasting models and included n=8 that were global in scope and provided public,
15 date-versioned forecasts. For each, we examined the median absolute percent error (MAPE) compared
16 to subsequently observed mortality trends, stratified by weeks of extrapolation, world region, and
17 month of model estimation. Models were also assessed for ability to predict the timing of peak daily
18 mortality. The MAPE among models released in July rose from 1.8% at one week of extrapolation to
19 24.6% at twelve weeks. The MAPE at six weeks were the highest in Sub-Saharan Africa (34.8%), and the
20 lowest in high-income countries (6.3%). At the global level, several models had about 10% MAPE at six
21 weeks, showing surprisingly good performance despite the complexities of modelling human
22 behavioural responses and government interventions. The framework and publicly available codebase
23 presented here (<https://github.com/pyliu47/covidcompare>) can be routinely used to compare
24 predictions and evaluate predictive performance in an ongoing fashion.

25 [†]Correspondence to: Emmanuela Gakidou (gakidou@uw.edu).

26 *These authors contributed equally to the analysis and are listed in alphabetical order.

27 Introduction

28 Forecasts and alternative scenarios of COVID-19 have been critical inputs into a range of important
29 decisions by healthcare providers, local and national government agencies and international
30 organizations and actors¹⁻⁴. For example, hospitals need to prepare for potential surges in the demand
31 for hospital beds, ICU beds and ventilators¹. National critical response agencies such as the US Federal
32 Emergency Management Agency have scarce resources including ventilators that can be moved to
33 locations in need with sufficient notice^{5,6}. Longer range forecasts are important for decisions such as the
34 potential to open schools, universities and workplaces, and under what circumstances⁷. Much longer-
35 range forecasts—six months to a year—are important for a wide range of policy choices, where efforts
36 to reduce disease transmission must be balanced against economic outcomes such as unemployment
37 and poverty⁸. Furthermore, vaccine and new therapeutic trialists need to select locations that will have
38 sufficient transmission to test new products in the time frame when phase three clinical trials are ready
39 to be launched. Nevertheless, hundreds of forecasting models have been published and/or publicly
40 released, and it is often not immediately clear which models have had the best performance, or are
41 most appropriate for predicting a given aspect of the pandemic.

42 Existing COVID-19 forecasting models differ substantially in methodology, assumptions, range of
43 predictions, and quantities estimated. Furthermore, mortality forecasts for the same location have often
44 differed substantially, in many cases by more than an order of magnitude, even within a six-week
45 forecasting window. The challenge for decision-makers seeking input from models to guide decisions,
46 which can impact many thousands of lives, is therefore not the availability of forecasts, but guidance on
47 which forecasts are likely to be most accurate. Out-of-sample predictive validation—checking how well
48 past versions of forecasting models predict subsequently observed trends—provides insight into future
49 model performance⁹. Although some comparisons have been conducted for models describing the
50 epidemic in the United States¹⁰⁻¹³, to our knowledge similar analyses have not been undertaken for
51 models covering multiple countries, despite the growing global impact of COVID-19.

52 This paper introduces a publicly available dataset and evaluation framework
53 (<https://github.com/pyliu47/covidcompare>) for assessing the predictive validity of COVID-19 mortality
54 forecasts. The framework and associated open-access software can be routinely used to track model
55 performance. This will, overtime, serve as a reference for decision-makers on historical model
56 performance, and provide insight into which models should be considered for critical decisions in the
57 future.

58 Results

59 Eight models which fit all inclusion criteria were evaluated (Table 1). These included those modelled by:
60 DELPHI-MIT (Delphi)^{14,15}, Youyang Gu (YYG)¹⁰, the Los Alamos National Laboratory (LANL)¹⁶, Imperial
61 College London (Imperial)¹⁷, the SIKJ-Alpha model from the USC Data Science Lab (SIKJAlpha)¹⁸, and three
62 models produced by the Institute for Health Metrics and Evaluation (IHME)¹⁹ (see methods section for
63 more details). Results are presented in the main text for two main predictive tasks: 1) predicting the
64 magnitude of mortality, and 2) predicting the timing of peak mortality (see methods). Magnitude results
65 are presented in the main text for models that continued to produce forecasts at the time of publication
66 of this article, while peak timing results are presented for models released early enough to capture the
67 first peak in most locations. Results for all historical models are shown in the appendix. Magnitude of

68 mortality results in the main text are presented according to two main analytical approaches. In the
69 “most current” approach, used to select data shown in Figure 3, the most recent 4-week period allowing
70 for the calculation of errors is selected for each extrapolation length. In the “month stratified” approach,
71 used to select data for Figures 4 and 5, models from July were used to calculate errors at each length of
72 extrapolation, with all months shown in the appendix. In each case errors were assessed from one to
73 twelve weeks of forecasting (see methods and Figure 2 for more details).

74 The evaluation framework developed here for assessing how well models predicted the total number of
75 cumulative deaths is shown in Figure 1 for an example country—the United States—and similar figures
76 for all locations included in the study can be found in the appendix. Figure 1, and similar figures in the
77 appendix, also highlight the direction of error for each model in each location. When looking across
78 iterations of forecasts, a wide range of variation can be observed for nearly all of the models.
79 Nevertheless, in many locations, models largely reached consensus regarding trajectories in the summer
80 of 2020. Models diverged again when predicting trajectories for Fall 2020 and Winter 2021, as some
81 models predicted upticks related to seasonality, while others projected continued slow declines in
82 mortality.

83 Figure 2 highlights the most recent errors for each length of extrapolation. For all models, the most
84 recent 1-week errors, reflecting forecasts created in October, ranged from 1% to 2%. The 12-week
85 median absolute percent errors (MAPE), reflecting models produced in July and August, ranged from
86 22.4% for the SIK-J Alpha model, to 79.9% for the Imperial model. At the global level pooling across
87 models, the most recent 6-week MAPE value was 7.2%.

88 Systematic assessments of bias for all models produced in July are shown in Figure 4, and Supplemental
89 Figure 2. The Delphi and LANL models from July underestimated mortality, with median percent errors
90 of -5.6% and -8.3% at 6 weeks respectively, while Imperial tended to overestimate (+47.7%), and the
91 remaining models were relatively unbiased.

92 Overall model performance for models produced in July is shown for cumulative deaths by week in
93 Figure 5. As one might expect, MAPE tends to increase by the number of weeks of extrapolation. Across
94 models released in July the MAPE rose from 1.8% at one week to 24.6% at twelve weeks. Decreases in
95 predictive ability with greater periods of extrapolation were similarly noted for errors in weekly deaths
96 (Supplemental Figure 3). At the global level, MAPE at six weeks was less than 15% for LANL (10.6%),
97 IHME-MS-SEIR (10.6%), SIKJalpha (12.3%) and Delphi (13.6%). The Imperial model had larger errors,
98 about 5-fold higher than other models by six weeks. This appears to be largely driven by the
99 aforementioned tendency to overestimate mortality. At twelve weeks, MAPE values were lowest for the
100 IHME-MS-SEIR (23.7%) model, while the Imperial model had the most elevated MAPE (98.8%). Predictive
101 performance between models was generally similar for median absolute errors (MAEs) (see
102 supplemental figure 4). Global MAE values at 12 weeks, among models released in July varied from 204
103 for the IHME-MS-SEIR model to 1,264 for the Imperial model.

104 Figure 5 also shows that model performance varies substantially by region. The lowest errors across
105 models were observed among high-income countries with a 6-week MAPE values of 6.3%. In contrast,
106 the largest errors were seen in sub-Saharan Africa, with a 6-week MAPE of 34.8%, and Latin America and
107 the Caribbean, with a MAPE of 22.4%. Individual model performance and availability also varied by
108 region.

109 The evaluation framework for exploring the ability of models to predict the timing of peak mortality
110 accurately—a matter of paramount importance for health service planning—is shown in Figure 6 for an
111 example location, Massachusetts. Similar figures for all locations are shown in the appendix. Median
112 absolute errors (MAE) for peak timing also rose with increased forecasting weeks, from 13 days at one
113 week to 30 days at eight weeks (Figure 7). The MAE at eight weeks ranged from 27 days for the IHME
114 Curve Fit and SIKJ-Alpha models to 54 days for the LANL model, with an overall error across models of 30
115 days (Figure 7). Models were generally biased towards predicting peak mortality too early
116 (Supplemental Figure 5).

117 Discussion

118 Eight COVID-19 models were identified that covered more than five countries, were regularly updated,
119 publicly released and provide archived results for past forecasts. Taken together at twelve weeks, the
120 models released in July had a median average percent error of 24.6% percent. Errors tend to increase
121 with longer forecasts, rising from 1.8% at one week to 24.6% at 12 weeks. At twelve weeks of
122 extrapolation, the best predictive performance among models considered at the global level was
123 observed for the IHME-MS-SEIR models, with a MAPE of 23.7%, although the best performing model
124 varied by region. The projections provided by Imperial had considerably higher error (98.8%) and the
125 SIKJalpha and Delphi models had intermediate performance for the same period. In the most current
126 models, the 6-week MAPE across models was 7.2%.

127 Although models largely converged in their predictions for the summer of 2020 period, forecasts began
128 to diverge again among predictions for Fall 2020 and Winter 2021. These later divergences are likely due
129 to differences in model assumptions related to the effects of seasonality. Although the top performing
130 models are currently performing in a highly comparable fashion, the updated results presented in this
131 framework in an ongoing fashion may highlight major predictive performance differences as the validity
132 of these assumptions are born out in the coming months.

133 A forecast of the trajectory of the COVID-19 epidemic for a given location depends on three sets of
134 factors: 1) attributes of the virus itself, and characteristics of the location, such as population density
135 and the use of public transport; 2) individual behavioural responses to the pandemic such as avoiding
136 contact with others or wearing a mask; and 3) the actions of governments, such as the imposition of a
137 range of social distancing mandates. Given the complexity of forecasting human and governmental
138 behaviours, especially in the context of a new pandemic, performance of most of the models evaluated
139 here was encouraging. Nevertheless, errors were observed to grow with greater extrapolation time,
140 indicating that governments and planners should recognize the wide uncertainty that comes with longer
141 range forecasts, and strategize accordingly. Hospital administrators may want to hedge on the higher
142 end of the forecast range, while government policymakers may elect to use the mean forecast,
143 depending on their risk tolerance.

144 We also observed substantial differences in average model predictive performance between regions,
145 which can likely be explained by several factors. Data quality has been shown to vary substantially
146 between countries, and many models were initially calibrated on data from early epidemics in China,
147 Europe, and the United States. Furthermore, different regions are at different stages of their epidemic
148 at any given time. For many of the countries in Sub-Saharan Africa for example, the challenge is
149 predicting if, and when, large outbreaks will occur. It is therefore easier for a model to demonstrate

150 large magnitude errors when it predicts a completely different epidemic trajectory. Contrastingly, in
151 some of the more established epidemics, it is easier to predict the nature of more stabilized, ongoing
152 transmission dynamics.

153 We also note that the vast majority of COVID-19 forecasting models did not provide sufficient
154 information to be included in this framework, given that publicly available and date-version forecasts
155 were not made available. We would encourage all research groups forecasting COVID-19 mortality to
156 consider providing historical versions of their models in a public platform for all locations, to facilitate
157 ongoing model comparisons. This will improve reproducibility, the speed of development for modelling
158 science, and the ability of policy makers to discriminate between a burgeoning number of models²⁰.
159 Many of the models featured in this analysis were generally unbiased, or tended to underestimate
160 future mortality, while other models, such as the Imperial model, as well as many other published
161 models that did not meet our inclusion criteria, tend to substantially overestimate transmission, even
162 within the first four weeks of a forecast. This tendency towards over-estimation among SEIR and other
163 transmission-based models is easy to understand given the potential for the rapid doubling of
164 transmission. Nevertheless, sustained exponential growth in transmission is not often observed, likely
165 due to the behavioural responses of individuals and governments; both react to worsening
166 circumstances in their communities, modifying behaviours and imposing mandates to restrict activities.
167 This endogenous behavioural response is commonly included in economic analyses, however, it has not
168 been routinely featured in transmission dynamics modelling of COVID-19. More explicit modelling of the
169 endogenous response of individuals and governments may improve future model performance for a
170 range of models.

171 Modelling groups are increasingly providing both reference forecasts, describing likely future trends,
172 and alternative scenarios describing the potential effects of policy choices, such as school openings,
173 timing of mandate re-imposition, or planning for hospital surges. For these scenarios, the error in the
174 reference forecast—which we describe in this manuscript—is actually less important than the error in
175 the effect implied by the difference between the reference forecast and policy scenario. Unfortunately,
176 evaluating the accuracy of these counterfactual scenarios is an extremely difficult task. The validity of
177 such claims depends on the supporting evidence for the assumptions about a policy's impact on
178 transmission. The best option for decision-makers is likely to examine the impact of these policies as
179 portrayed by a range of modelling groups, especially those that have historically had reasonable
180 predictive performance in their reference forecasts.

181 Given that a number of very different models demonstrated recent six-week errors for cumulative
182 deaths below 10%, it would likely be worthwhile to construct an ensemble of these models and evaluate
183 the performance the ensemble compared to each component. Although from a logistical standpoint,
184 creating an ensemble of the forecasts would be relatively straightforward, it would be more challenging
185 to integrate such a model pool with scenarios assessing policy options, given that the models have
186 highly different underlying structures. Nevertheless, the inclusion of the models shown here, and future
187 models meeting criteria into an ensemble framework, is an important area for future research.

188 This analysis of the performance of publicly released COVID-19 forecasting models has limitations. First,
189 we have focused only on forecasts of deaths, as they are available for all models included here. Hospital
190 resource use is also of critical importance, however, and deserves future consideration. Nevertheless,
191 this will be complicated by the heterogeneity in hospital data reporting; many jurisdictions report

192 hospital census counts, others report hospital admissions, and still others do not release hospital data
193 on a regular basis. Without a standardized source for these data, assessment of performance can only
194 be undertaken in an *ad hoc* way. Second, many performance metrics exist which could have been
195 computed for this analysis. We have focused on reporting median absolute percent error, as the metric
196 is frequently used, quite stable, and provides an easily interpreted number that can be communicated to
197 a wide audience. Relative error is an exacting standard, however. For example, a forecast of three
198 deaths in a location that observed only one may represent a 200% error, yet it would be of little policy
199 or planning significance. Conversely, focusing on absolute error would create an assessment dominated
200 by a limited number of locations with large epidemics. Future assessment could consider different
201 metrics that may offer new insights, although the relative rank of performance by model is likely to be
202 similar.

203 When taking an inclusive approach to including forecasts from various modelling groups, including
204 estimates from a wide range of time periods and geographies, extra care must be taken to ensure
205 comparability between models. We use various techniques to construct fair companions, such as
206 stratifying by region, month of estimation, and weeks of forecasting, and masking summary statistics
207 representing a small number of values. Nevertheless, other researchers may prefer distinct methods of
208 maximizing comparability over a complex and patchy estimate space. Furthermore, the domains
209 assessed here —magnitude of total mortality and peak timing—are not an exhaustive list of all possible
210 dimensions of model performance. By providing an open-access framework to compile forecasts and
211 calculate errors, other researchers can build on the results presented here to provide additional
212 analyses.

213 COVID-19 mortality forecasts have been used in myriad ways by policymakers as they make difficult
214 decisions about resource management under unprecedented circumstances. Examples include
215 prospectively managing or moving resources between regions such as hospital beds, ICU beds,
216 ventilators, masks and other personal-protective equipment, as well as decisions about social distancing
217 measures, stay-at-home orders, and closing schools, universities and workplaces^{1,7}. It is therefore of
218 paramount importance that decision-makers can quickly assess how robust each modelling groups
219 predictions have been historically. Furthermore, we believe a similar approach could be adopted in
220 future pandemics, and for modelling other infectious diseases such as influenza.

221 Ultimately, policymakers would benefit from considering a multitude of forecasting models as they
222 consider resource planning decisions related to the response to the ongoing COVID-19 pandemic. This
223 study provides a publicly available framework and codebase, which will be updated in an ongoing
224 fashion, to continue to monitor model predictions in a timely manner, and contextualize them with prior
225 predictive performance. It is our hope that this spurs conversation and cooperation amongst
226 researchers, which might lead to more accurate predictions, and ultimately aid in the collective
227 response to COVID-19. As the pandemic continues worldwide and resurges in Europe and North America
228 become more evident, regularly updating models, and continually assessing their predictive validity, will
229 be important in order to provide stakeholders with the best tools for COVID-19 decision-making.

230

231 **Methods**

232 **Systematic Review**

233 A total of 386 published and unpublished COVID-19 forecasting models were reviewed (see appendix).
234 Models were excluded from consideration if they did not 1) produce estimates for at least five different
235 countries, 2) did not extrapolate at least four weeks out from the time of estimation, 3) did not estimate
236 mortality, 4) did not provide downloadable, publicly available results, or 5) did not provide date-
237 versioned sets of previously estimated forecasts, which are required to calculate subsequent out-of-
238 sample predictive validity. Eight models which fit all inclusion criteria were evaluated (Table 1). These
239 included those modelled by: DELPHI-MIT (Delphi)^{14,15}, Youyang Gu (YYG)¹⁰, the Los Alamos National
240 Laboratory (LANL)¹⁶, Imperial College London (Imperial)¹⁷, the SIKJ-Alpha model from the USC Data
241 Science Lab (SIKJalpha)¹⁸, and three models produced by the Institute for Health Metrics and Evaluation
242 (IHME)¹⁹. Beginning March 25th, IHME initially produced COVID forecasts using a statistical curve fit
243 model (IHME-CF), which was used through April 29th for publicly released forecasts¹. On May 4th, IHME
244 switched to using a hybrid model, drawing on a statistical curve fit first stage, followed a second-stage
245 epidemiological model with susceptible, exposed, infectious, recovered compartments (SEIR)²¹. This
246 model—referred to herein as the IHME-CF SEIR model—was used through May 26th. On May 29th, the
247 curve fit stage was replaced by a spline fit to the relationship between log cumulative deaths and log
248 cumulative cases, while the second stage SEIR model remained the same²². This model, referred to as
249 the IHME-MS SEIR model, is the basis for recently published work on US State level scenarios of COVID-
250 19 projections in the fall and winter of 2020/2021²³ and was still in use at the time of this publication.
251 The three IHME models rely upon fundamentally different assumptions and core methodologies, and
252 therefore are considered separately. They were also released during different windows of the pandemic,
253 and are therefore compared to models released during similar time periods.

254 In some cases, numerous scenarios were produced by modelling groups, to describe the potential
255 effects of interventions, or future trajectories under different assumptions. In each case the baseline or
256 status quo scenario was selected to evaluate model performance as that represents the modelers' best
257 estimate about the most probable course of the pandemic. Table 1 summarizes information about each
258 model assumptions, methodologies, input data, modelled outputs, and forecasting range.

259 **Model Comparison Framework**

260 In order to conduct a systematic comparison of the out-of-sample predictive validity of international
261 COVID-19 forecasting models, a number of issues must be addressed. Looking across models, a high
262 degree of heterogeneity can be observed in numerous dimensions, including sources of input data,
263 frequency of public releases of model estimates, geographies included in the results, and how far into
264 the future predictions are made available for. Differences in each of these areas must be taken into
265 account, in order to provide a fair and relevant comparison.

266 Input data: A number of sources of input data—describing observed epidemiological trends in COVID-
267 19—exist, and they often do not agree for a given country and time point^{24–26}. We chose to use mortality
268 data collected by the Johns Hopkins University Coronavirus Resource Center as the in-sample data
269 against which forecasts were validated at the national level, and data from the New York Times for
270 state-level data for the United States^{25,26}. We chose to mainly rely on the Hopkins data as 1) it was the
271 most common input data source used in the different models considered, 2) it covered all countries for

272 which modelling groups produced forecasts, 3) although some quality issues were noted, and managed
273 in our analysis, largely quality was deemed acceptable, and 4) data were made publicly available on a
274 GitHub page and updated daily, which facilitates the maintenance of a timely comparison framework.
275 Locations were excluded from the evaluation (including Ecuador and Peru) where models used
276 alternative data sources, such as excess mortality, in settings with known marked under-registration of
277 COVID-19 deaths and cases^{27,28}. We adjusted for differences in model input data using intercept shifts,
278 whereby all models were shifted to perfectly match the in-sample data for the date in which the model
279 was released (see supplemental methods).

280 Frequency of public releases of model estimates: Most forecasting models are updated regularly, but at
281 different intervals, and on different days. Specific days of the week have been associated with a greater
282 number of reported daily deaths. Therefore, previous model comparison efforts in the United States—
283 such as those conducted by the US Centers for Disease Control and Prevention—have required modelers
284 to produce estimates using input data cut-offs from a specific day of the week²⁹. For the sake of
285 including all publicly available modelled estimates, we took a more inclusive approach, considering each
286 publicly released iteration of each model. To minimize the effect of day-to-day fluctuations in death
287 reporting, we focus on errors in cumulative and weekly total mortality, which are less sensitive to daily
288 variation.

289 Geographies and time periods included in the results: Each model produces estimates for a different set
290 of national and subnational locations, and extrapolates a variable amount of time from the present.
291 Each model was also first released on a different date, and therefore reflects a different window of the
292 pandemic. Here, we also took an inclusive but stratified approach, and included estimates from all
293 possible locations and time periods. To increase comparability, summary error statistics were stratified
294 by super-region used in the Global Burden of Disease Study³⁰, weeks of extrapolation, and month of
295 estimation, and we masked summaries reflecting a small number of locations or time points. Models
296 were included in the global predictive validity results only when they were present for all regions.
297 Estimates were included at the national level for all countries, except the United States, where they
298 were also included at the admin-1 (state) level, as they were available for most models. In order to be
299 considered for inclusion, models were required to forecast at least four weeks into the future.

300 Outcomes: Finally, each model also includes different estimated quantities, including daily and
301 cumulative mortality, number of observed or true underlying cases, and various dimensions of hospital
302 resource utilization. The focus of this analysis is on mortality, as it was the most widely reported
303 outcome, and it also has a high degree of societal, epidemiological and public health importance. We did
304 not focus on forecasts of confirmed cases for several reasons. Certain models we wished to include did
305 not provide an estimate of confirmed cases to subsequently assess predictive performance. Mortality,
306 on the other hand, was available for all models. Furthermore, confirmed cases also depend on testing
307 rates, which vary widely over time and across locations. Modelling confirmed cases, therefore,
308 represents different and perhaps larger challenges. Of course, death numbers also have limitations, but
309 they are generally more reliable than case numbers, at least in the early stages of the pandemic, and in
310 locations with limited capacity to test.

311 **Comparison of Cumulative Mortality Forecasts**

312 The total magnitude of COVID-19 deaths is a key measure for monitoring the progression of the
313 pandemic. It represents the most commonly produced outcome of COVID-19 forecasting models, and

314 perhaps the most widely debated measure of performance. The main quantity that is considered is
315 errors in total cumulative deaths—as opposed to other metrics such as weekly or daily deaths—as it has
316 been most commonly discussed measure, to-date, in academic and popular press critiques of COVID-19
317 forecasting models. Nevertheless, alternate measures are presented in the appendix. Errors were
318 assessed for systematic upward or downward bias, and errors for weekly, rather than cumulative
319 deaths, were also assessed. In calculating summary statistics, percent errors were used to control for the
320 large differences in the scale of the epidemic between locations. Medians, rather than means, are
321 calculated due to a small number of large magnitude outliers present in a few time-series. Errors from
322 all models were pooled to calculate overall summary statistics, in order to comment on overarching
323 trends by geography and time.

324 Results are presented using two analytical strategies in the main text. Both strategies are highlighted in
325 Figure 2. The “most current” approach is used to select the data shown in Figure 3. The “month
326 stratified” approach is used for Figures 3 and 4. In the “most current” approach, the most recent 4
327 weeks of model dates are used for each extrapolation length. Therefore, for 1-week errors, models from
328 October were used, whereas for 12-week errors, models from July and August were used. This allows for
329 the assessment of the most recent evidence possible for each set of errors displayed. 4-week periods
330 are used to ensure that the results are not unduly biased by featuring only a small number of runs for
331 each model.

332 In the “month stratified” approach, models from July are used in all cases. This strategy allows for more
333 reliable assessment of certain aspects of predictive validity, as the same models are being compared
334 over time and geographies. For example, the month stratified approach may provide a more comparable
335 assessment of how errors grow with increased length of extrapolation. Models are shown for July in the
336 main text—the most recent month allowing for assessment of errors at twelve weeks of forecasting—
337 and errors stratified for all months are shown in the appendix.

338 **Comparison of Peak Daily Mortality Forecasts**

339 Each model was also assessed on how well it predicted the timing of peak daily deaths—an additional
340 aspect of COVID-19 epidemiology with acute relevance for resource planning. Peak timing may be better
341 predicted by different models than those best at forecasting the magnitude of mortality, and therefore
342 deserves separate consideration as an outcome of predictive performance. In order to assess peak
343 timing predictive performance, the observed peak of daily deaths in each location was estimated first—
344 a task complicated by the highly volatile nature of reported daily deaths values. Each timeseries of daily
345 deaths was smoothed, and the date of the peak observed in each location, as well as the predicted peak
346 for each iteration of each forecasting model was calculated (see supplemental methods). A LOESS
347 smoother was used, as it was found to be the most robust to daily fluctuations. Results shown here
348 reflect only those locations for which the peak of the epidemic had passed at the time of publication,
349 and for which at least one set of model results was available seven days or more ahead of the peak date.
350 Predictive validity statistics were stratified by the number of weeks in advance of the observed peak that
351 the model was released, as well as the month in which the model was released. Results shown in the
352 main text were pooled across months, as there was little evidence of dramatic differences over time
353 (see appendix). There was insufficient geographic variation to stratify results by regional groupings,
354 although that remains an important topic for further study, which will become feasible as the pandemic
355 peaks in a greater number of countries globally.

356 **Data and Code Availability**

357 All data and versioned code required to reproduce this analysis its included visualizations are publicly
358 available at (<https://github.com/pyliu47/covidcompare>).

359 **References**

360 1 Team IC-19 health service utilization forecasting, Murray CJ. Forecasting COVID-19 impact on
361 hospital bed-days, ICU-days, ventilator-days and deaths by US state in the next 4 months.
362 *medRxiv* 2020; : 2020.03.27.20043752.

363 2 Lu FS, Nguyen AT, Link NB, Lipsitch M, Santillana M. Estimating the Early Outbreak
364 Cumulative Incidence of COVID-19 in the United States: Three Complementary Approaches.
365 *medRxiv* 2020; : 2020.04.18.20070821.

366 3 Weinberger D, Cohen T, Crawford F, *et al.* Estimating the early death toll of COVID-19 in the
367 United States. *medRxiv* 2020; : 2020.04.15.20066431.

368 4 Epidemic Model Guided Machine Learning for COVID-19 Forecasts in the United States |
369 medRxiv. <https://www.medrxiv.org/content/10.1101/2020.05.24.20111989v1> (accessed
370 June 23, 2020).

371 5 Critical Supply Shortages — The Need for Ventilators and Personal Protective Equipment
372 during the Covid-19 Pandemic | NEJM. *New England Journal of Medicine*
373 <http://www.nejm.org/doi/full/10.1056/NEJMp2006141> (accessed July 26, 2020).

374 6 FEMA Administrator March 27, 2020, letter to Emergency Managers Requesting Action on
375 Critical Steps | FEMA.gov. [https://www.fema.gov/news-release/2020/03/27/fema-](https://www.fema.gov/news-release/2020/03/27/fema-administrator-march-27-2020-letter-emergency-managers-requesting-action)
376 [administrator-march-27-2020-letter-emergency-managers-requesting-action](https://www.fema.gov/news-release/2020/03/27/fema-administrator-march-27-2020-letter-emergency-managers-requesting-action) (accessed July
377 26, 2020).

378 7 Viner RM, Russell SJ, Croker H, *et al.* School closure and management practices during
379 coronavirus outbreaks including COVID-19: a rapid systematic review. *The Lancet Child &*
380 *Adolescent Health* 2020; **4**: 397–404.

381 8 Atkeson A. What Will Be the Economic Impact of COVID-19 in the US? Rough Estimates of
382 Disease Scenarios. National Bureau of Economic Research, 2020 DOI:10.3386/w26867.

383 9 Tashman LJ. Out-of-sample tests of forecasting accuracy: an analysis and review.
384 *International Journal of Forecasting* 2000; **16**: 437–450.

385 10Gu Y. COVID-19 Projections Using Machine Learning. <https://covid19-projections.com/>
386 (accessed June 23, 2020).

387 11Reich Lab COVID-19 Forecast Hub. <https://reichlab.io/covid19-forecast-hub/> (accessed June
388 23, 2020).

- 389 12 Project Score Data: COVID-19 Forecasts - Zoltar.
390 https://zoltardata.com/project/44/score_data (accessed June 23, 2020).
- 391 13 UCLAML Combating COVID-19. <http://covid19.uclaml.org/compare> (accessed June 23, 2020).
- 392 14 MIT DELPHI Epidemiological Case Predictions COVIDAnalytics.
393 <https://www.covidanalytics.io/projections> (accessed June 23, 2020).
- 394 15 Li ML, Bouardi HT, Lami OS, Trikalinos TA, Trichakis NK, Bertsimas D. Forecasting COVID-19
395 and Analyzing the Effect of Government Interventions. *medRxiv* 2020; :
396 2020.06.23.20138693.
- 397 16 Los Alamos National Laboratory COVID-19 Confirmed and Forecasted Case Data.
398 <https://covid-19.bsvgateway.org/> (accessed June 23, 2020).
- 399 17 Imperial College COVID-19 LMIC Reports. <https://mrc-ide.github.io/global-lmic-reports/>
400 (accessed June 23, 2020).
- 401 18 Srivastava A, Xu T, Prasanna VK. Fast and Accurate Forecasting of COVID-19 Deaths Using the
402 SIKJ α Model. *arXiv:200705180 [physics, q-bio]* 2020; published online July 12.
403 <http://arxiv.org/abs/2007.05180> (accessed Aug 23, 2020).
- 404 19 COVID-19 estimation updates. Institute for Health Metrics and Evaluation. 2020; published
405 online March 24. <http://www.healthdata.org/covid/updates> (accessed June 23, 2020).
- 406 20 Rivers C, George D. How to Forecast Outbreaks and Pandemics. 2020; published online July
407 5. [https://www.foreignaffairs.com/articles/united-states/2020-06-29/how-forecast-](https://www.foreignaffairs.com/articles/united-states/2020-06-29/how-forecast-outbreaks-and-pandemics)
408 [outbreaks-and-pandemics](https://www.foreignaffairs.com/articles/united-states/2020-06-29/how-forecast-outbreaks-and-pandemics) (accessed July 8, 2020).
- 409 21 IHME COVID-19 Estimation Update: May 4th, 2020.
410 [http://www.healthdata.org/sites/default/files/files/Projects/COVID/Estimation_update_050](http://www.healthdata.org/sites/default/files/files/Projects/COVID/Estimation_update_050420.pdf)
411 [420.pdf](http://www.healthdata.org/sites/default/files/files/Projects/COVID/Estimation_update_050420.pdf) (accessed July 6, 2020).
- 412 22 IHME COVID-19 Estimation Update: May 29th, 2020.
413 [http://www.healthdata.org/sites/default/files/files/Projects/COVID/Estimation_update_05.3](http://www.healthdata.org/sites/default/files/files/Projects/COVID/Estimation_update_05.30.2020.pdf)
414 [0.2020.pdf](http://www.healthdata.org/sites/default/files/files/Projects/COVID/Estimation_update_05.30.2020.pdf) (accessed July 6, 2020).
- 415 23 Reiner RC, Barber RM, Collins JK, *et al.* Modeling COVID-19 scenarios for the United States.
416 *Nature Medicine* 2020; : 1–12.
- 417 24 Coronavirus Pandemic (COVID-19) - Statistics and Research - Our World in Data.
418 <https://ourworldindata.org/coronavirus> (accessed June 28, 2020).
- 419 25 [nytimes/covid-19-data](https://github.com/nytimes/covid-19-data). The New York Times, 2020 [https://github.com/nytimes/covid-19-](https://github.com/nytimes/covid-19-data)
420 [data](https://github.com/nytimes/covid-19-data) (accessed June 28, 2020).

421 26 COVID-19 Map. Johns Hopkins Coronavirus Resource Center.
422 <https://coronavirus.jhu.edu/map.html> (accessed June 23, 2020).

423 27 Covid-19 data - Tracking covid-19 excess deaths across countries | Graphic detail | The
424 Economist. [https://www.economist.com/graphic-detail/2020/07/15/tracking-covid-19-](https://www.economist.com/graphic-detail/2020/07/15/tracking-covid-19-excess-deaths-across-countries)
425 [excess-deaths-across-countries](https://www.economist.com/graphic-detail/2020/07/15/tracking-covid-19-excess-deaths-across-countries) (accessed July 26, 2020).

426 28 A greater tragedy than we know: Excess mortality rates suggest that COVID-19 death toll is
427 vastly underestimated in LAC. UNDP.
428 [https://www.latinamerica.undp.org/content/rblac/en/home/presscenter/director-s-graph-](https://www.latinamerica.undp.org/content/rblac/en/home/presscenter/director-s-graph-for-thought/a-greater-tragedy-than-we-know--excess-mortality-rates-suggest-t.html)
429 [for-thought/a-greater-tragedy-than-we-know--excess-mortality-rates-suggest-t.html](https://www.latinamerica.undp.org/content/rblac/en/home/presscenter/director-s-graph-for-thought/a-greater-tragedy-than-we-know--excess-mortality-rates-suggest-t.html)
430 (accessed July 20, 2020).

431 29 CDC. Coronavirus Disease 2019 (COVID-19). Centers for Disease Control and Prevention.
432 2020; published online Feb 11. [http://www.cdc.gov/coronavirus/2019-ncov/covid-](http://www.cdc.gov/coronavirus/2019-ncov/covid-data/forecasting-us.html)
433 [data/forecasting-us.html](http://www.cdc.gov/coronavirus/2019-ncov/covid-data/forecasting-us.html) (accessed June 23, 2020).

434 30 Dicker D, Nguyen G, Abate D, *et al.* Global, regional, and national age-sex-specific mortality
435 and life expectancy, 1950–2017: a systematic analysis for the Global Burden of Disease Study
436 2017. *The Lancet* 2018; **392**: 1684–735.

437

438 **Acknowledgements**

439 This work was primarily supported by the Bill & Melinda Gates Foundation. J.F. received support from
440 the UCLA Medical Scientist Training program (NIH NIGMS training grant GM008042).

441

442 **Competing Interests**

443 The authors declare they have no competing interests as defined by Nature Research that might be
444 perceived to influence the results and/or discussion reported in this manuscript.

445

446 **Author Contributions**

447 JF, PL, TV, SIH, CJLM, and EG conceptualized and designed the study, with substantial input from RR, RB,
448 JC, SL, and DP. JF and PL acquired the data, and JF, PL, CT, and AC wrote the analytical code to conduct
449 the analysis. JF, PL, and CJLM drafted the first draft of the article and all authors meaningfully revised.
450 SIH, CJLM, and EG supervised the work.

451

452 **Tables and Figures**

Model	Data Access	Model Type	Mortality Input Data	Model Outputs	Geographies	Range	Model Structure and Assumptions
IHME - CurveFit	http://www.healthdata.org/covid/data-downloads	Statistical Curve Fit	JHU+ local and national governments	Hospital and ICU Admissions, Ventilator, Hospital Beds Utilization; Confirmed Daily and Cumulative Cases; Daily and Cumulative Mortality	34 Countries*	Aug 4 ^{th**}	Statistical curve fit model aimed at predicting peak of hospital resource use as a function of social distancing.
IHME - CF SEIR	http://www.healthdata.org/covid/data-downloads	Curve Fit + SEIR	JHU+ local and national governments	Hospital and ICU Admissions, Ventilator, Hospital Beds Utilization; Confirmed Daily and Cumulative Cases; Daily and Cumulative Mortality	52 Countries*	Aug 4 ^{th**}	Hybrid curve fit (next 8 days) and SEIR model (after 8 days) with additional parameters including mobility, testing, temperature, and population density.
IHME - MS SEIR	http://www.healthdata.org/covid/data-downloads	Mortality Spline + SEIR	JHU+ local and national governments	Hospital and ICU Admissions, Ventilator, Hospital Beds Utilization; Confirmed Daily and Cumulative Cases; Daily and Cumulative Mortality	163 Countries*	Feb 1st	Covariate-adjusted (population, testing, mandates, flu/pneumonia seasonality, mask use, etc.) SEIR model based on daily deaths estimates harmonized with testing, hospitalization via a random knot spline.
Youyang Gu	https://github.com/youyanggu/covid19-projections	SEIR	JHU	Daily and Cumulative Mortality; Daily, Active, and Cumulative Cases	73 Countries*	Nov 1 ^{st**}	SEIR model with three R0 values corresponding to: 1) Pre-mitigation 2) Post mitigation 3) Post reopening. Performs grid search to optimize parameter selection.
MIT - DELPHI	https://github.com/COVIDAnalytics/DELPHI	SEIR	JHU	Cumulative Mortality; Active Cases, Cumulative Detected Cases, Active Hospitalized Cases; Cumulative Hospitalized Cases	159 Countries*	Jan 15th	Standard SEIR model adjusted for effective meta-analysis driven parameters of contact rate, under-detection, hospitalization, and societal-governmental response measures (4 phased non-linear parametric model).
Imperial-LMIC	https://github.com/mrc-ide/global-lmic-reports	SEIR	Euro-CDC	Daily and Cumulative Cases; Daily and Cumulative Mortality; ICU incidence, ICU Demand, Hospital Incidence, Hospital Demand	176 Countries	Jan 22nd	Modeled using SQUIRE, an age standardized SEIR model with parameters for healthcare capacity and disease severity. Incorporates mobility dependent R0 based on Google mobility data. Baseline scenario assumes current levels of mobility and interventions persist.
LANL -GR	https://covid-19.bsvgateway.org/	Dynamic Growth	JHU	Confirmed Daily and Cumulative Cases; Daily and Cumulative Mortality	153 Countries*	Dec 15th	Estimates cases driven by a dynamic growth parameter, adjusted based on trends in observed cases. Mortality driven by estimated CFR, assumed to be consistent over the forecast period.
USC SIKJalpha	https://github.com/scc-usc/ReCOVER-COVID-19	SIKJalpha	JHU	Confirmed Daily and Cumulative Cases; Daily and Cumulative Mortality	177 Countries*	Feb 10th	Application of SIKJalpha epidemiological model which models temporally varying infection rates and human mobility. Models CFR as a function of cases with different infection times.

Table 1. Models Included in the Study

All eight models included in the study are shown. The full list of models assessed for inclusion is shown in the supplemental review file. Range indicates the last date upon which forecasts are available in the most current version of each model.

*Includes state-level estimates for the United States.

**No longer actively producing forecasts at the time of publication.

United States

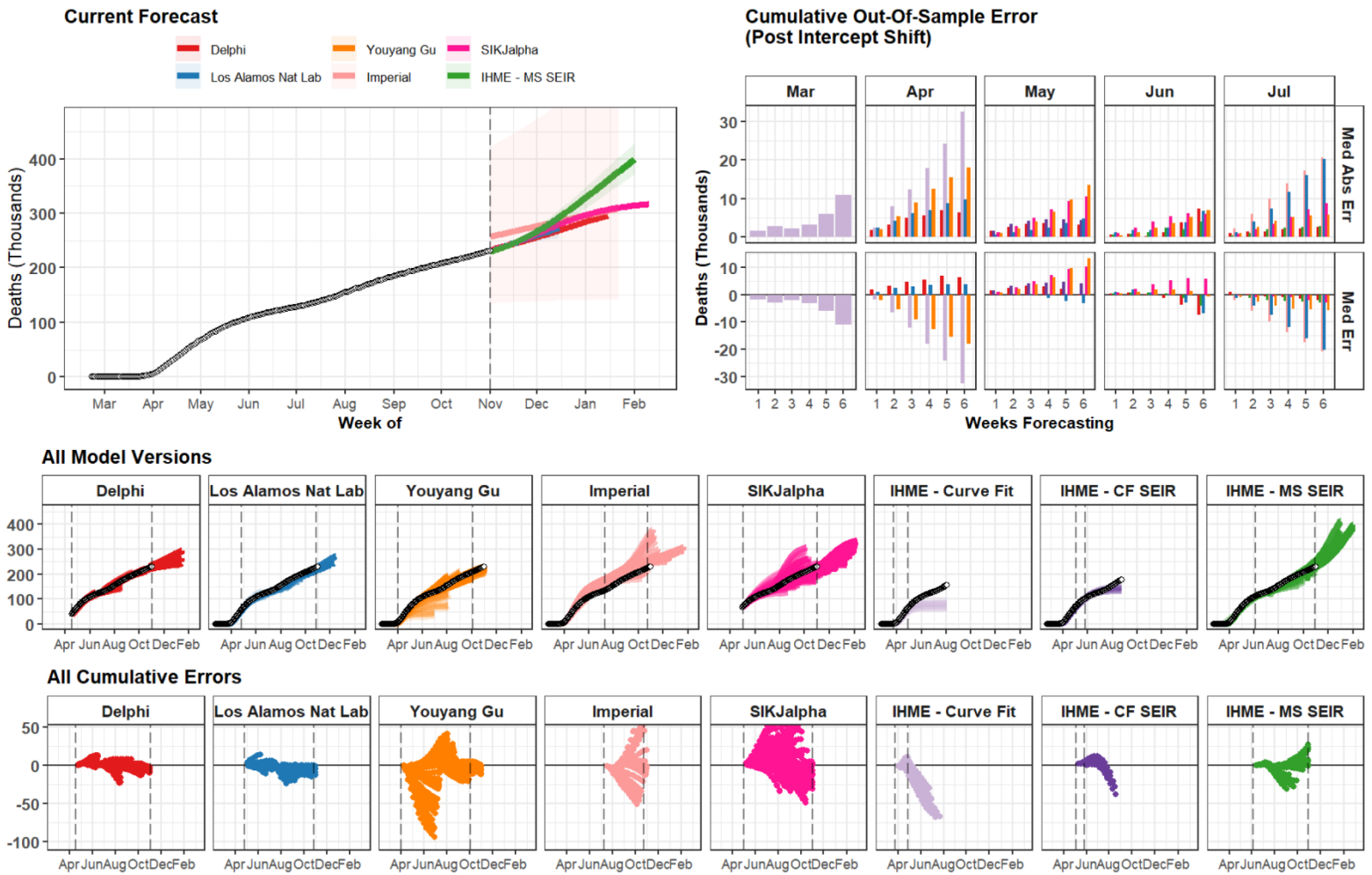
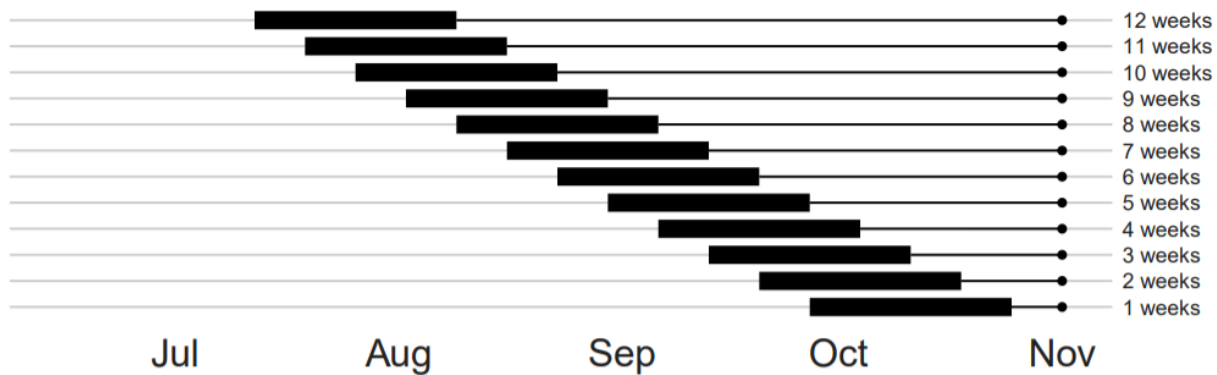


Figure 1. Cumulative Mortality Forecasts and Prediction Errors by Model – Example for United States

The most recent version of each model is shown on the top left. The middle row shows all iterations of each model as separate lines, with the intensity of color indicating model date (darker models are more recent). The vertical dashed lines indicate the first and last model release date for each model. The bottom row shows all errors calculated at weekly intervals. The top right panel summarizes all observed errors, using median error and median absolute error, by weeks of forecasting, and month of model estimation. Errors incorporate an intercept shift to account for differences in each model's input data. This figure represents an example for the United States of country-specific plots made for all locations examined in this study. Graphs for all geographies can be found in the supplement. Note that while certain model uses different input data source than the other modelling groups causing apparently discordant past trends in the top left panel. We plot raw estimates on the top left panel, however we implement an intercept shift to account for this issue in the calculation of errors.

456

"Most Current" Analytical Approach



"Month Stratified" Analytical Approach

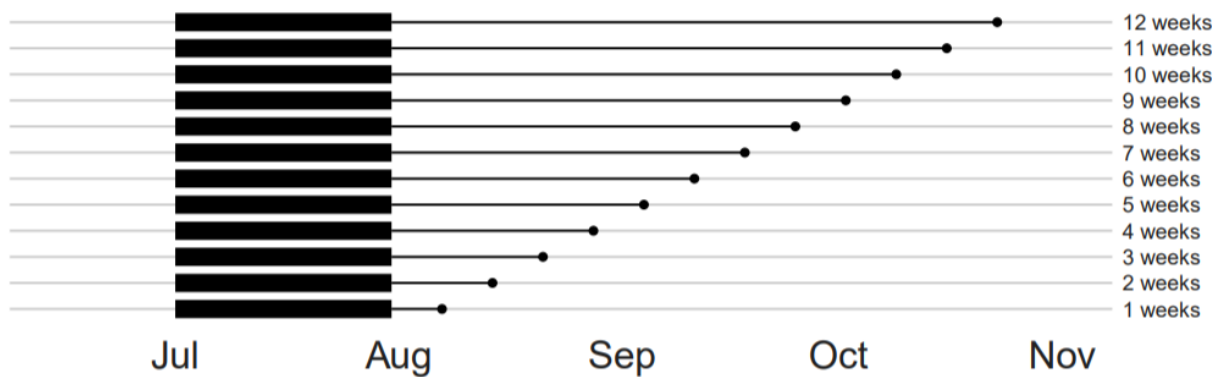


Figure 2. Illustration of Analytical Framework

This figure highlights the analytical framework presented in the main text. Part A highlights the “most current” approach, which is used to select the data shown in Figure 3. Part B highlights the “month stratified” approach used for Figures 4 and 5. The Y axis shows the number of weeks of extrapolation for each scenario, while the x axis shows a range of model date—the date on which a model was released. The thick band in each plot highlights the 4-week window of model dates used for each extrapolation week value. The thin line shows the period for which each set of models is extrapolating before errors are calculated. In the top panel, the most recent four weeks of model dates are used for each extrapolation length. Therefore, for 1-week errors models from October were used, whereas for 12-week errors, models from July and August were used. In the bottom panel, models from July are used in all cases. The analytic strategy highlighted in the top panel provides the most recent evidence possible for each extrapolation length. The strategy in the bottom allows for more reliable assessment of how errors grow with increased extrapolation time.

It is made available under a [CC-BY 4.0 International license](https://creativecommons.org/licenses/by/4.0/).

457

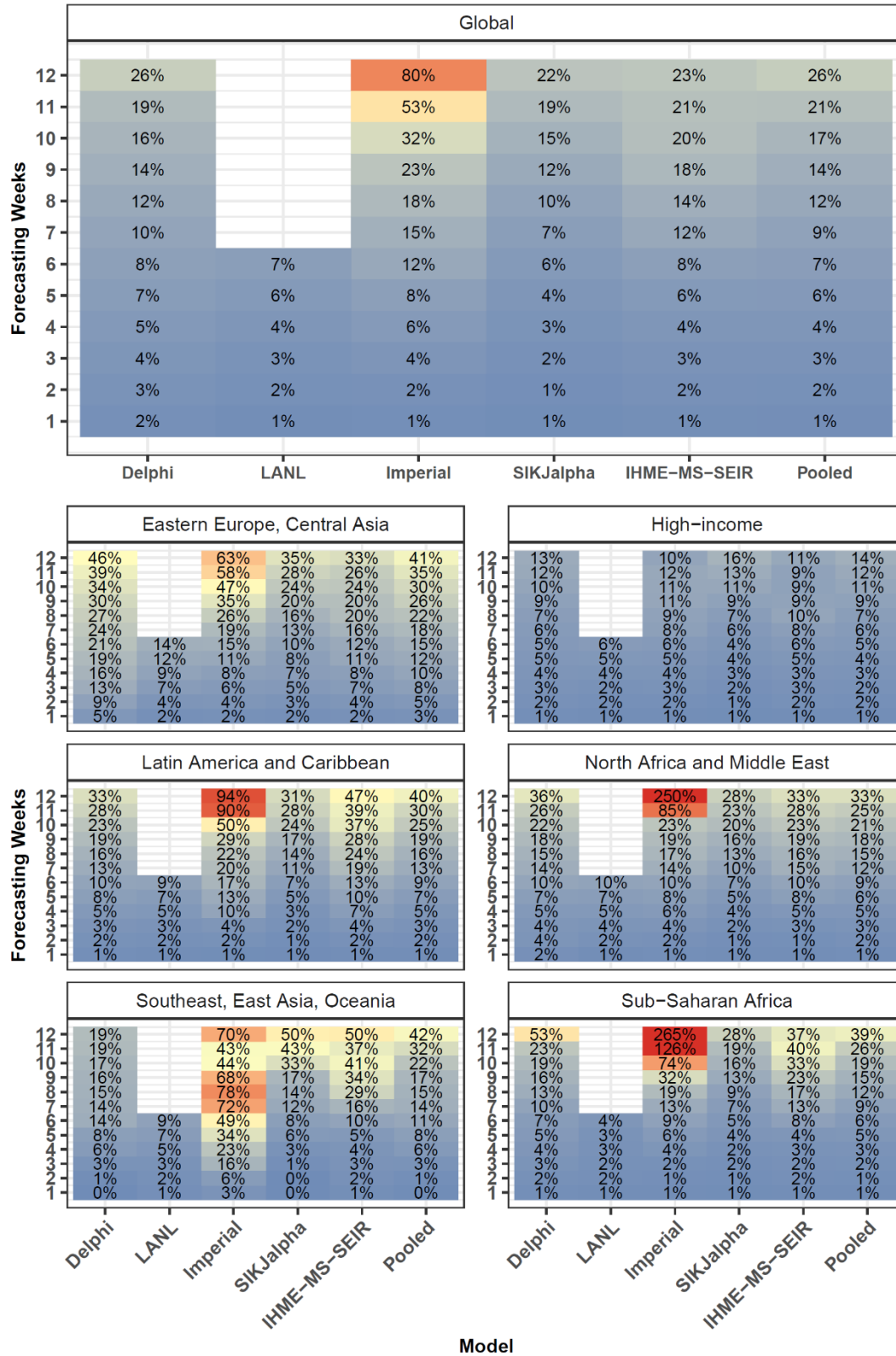


Figure 3. Most Current - Cumulative Mortality Accuracy – Median Absolute Percent Error

Median absolute percent error values, a measure of accuracy, were calculated across all observed errors at weekly intervals, for each model by weeks of forecasting and geographic region. Values that represent fewer than five locations are masked due to small sample size. Models were included in the global average when they included at least five locations in each region. Pooled summary statistics reflect values calculated across all errors from all models, in order to comment on aggregate trends by time or geography. Results are shown here for the most recent four week window allowing for the calculation of errors at each point of extrapolation (see Figure 2 and methods). Results from other months are shown in the supplement.

It is made available under a [CC-BY 4.0 International license](https://creativecommons.org/licenses/by/4.0/).

-100% -80% -60% -40% -20% 0% 20% 40% 60% 80% 100%

458

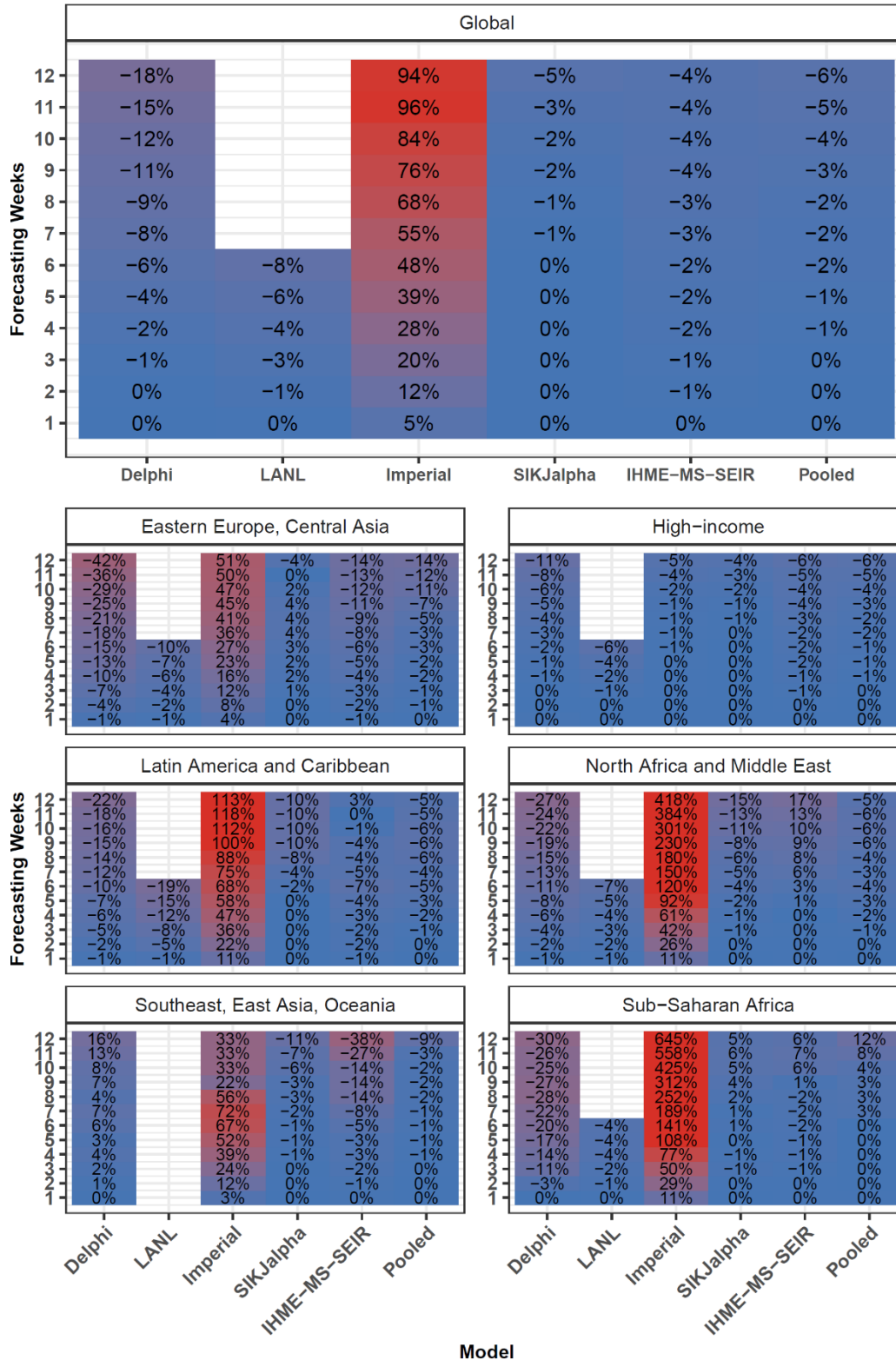


Figure 4. Month Stratified July Models - Cumulative Mortality Bias - Median Percent Error

Median percent error values, a measure of bias, were calculated across all observed errors at weekly intervals, for each model, by weeks of forecasting and geographic region. Values that represent fewer than five locations are masked due to small sample size. Models were included in the global average when they included at least five locations in each region. Pooled summary statistics reflect values calculated across all errors from all models, in order to comment on aggregate trends by time or geography. Results are shown here for models released in July, and results from other months are shown in the appendix.

It is made available under a [CC-BY 4.0 International license](https://creativecommons.org/licenses/by/4.0/).

459

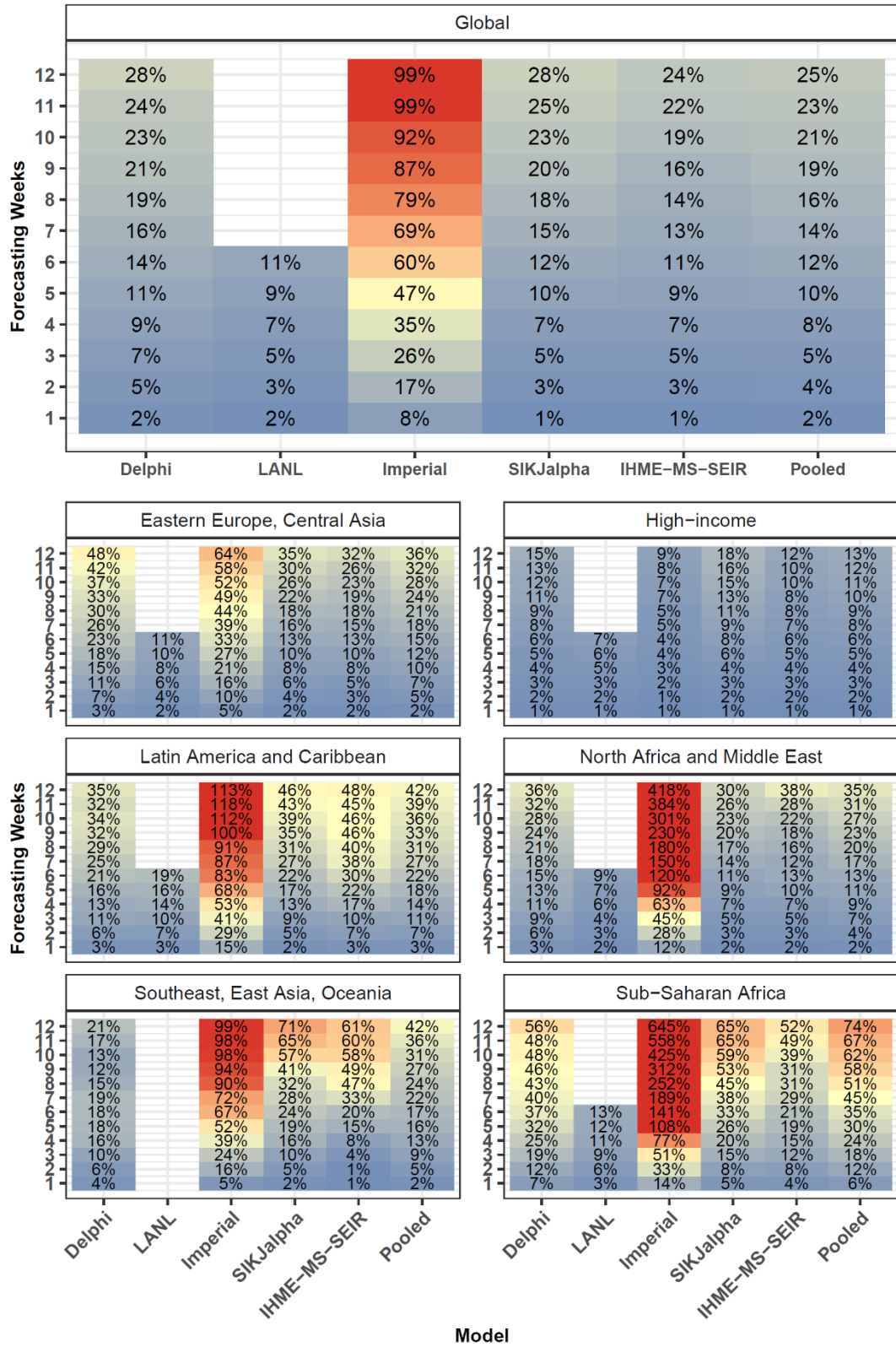


Figure 5. Month Stratified July Models - Cumulative Mortality Accuracy – Median Absolute Percent Error

Median absolute percent error values, a measure of accuracy, were calculated across all observed errors at weekly intervals, for each model by weeks of forecasting and geographic region. Values that represent fewer than five locations are masked due to small sample size. Models were included in the global average when they included at least five locations in each region. Pooled summary statistics reflect values calculated across all errors from all models, in order to comment on aggregate trends by time or geography. Results are shown here for models released in July, and results from other months are shown in the supplement.

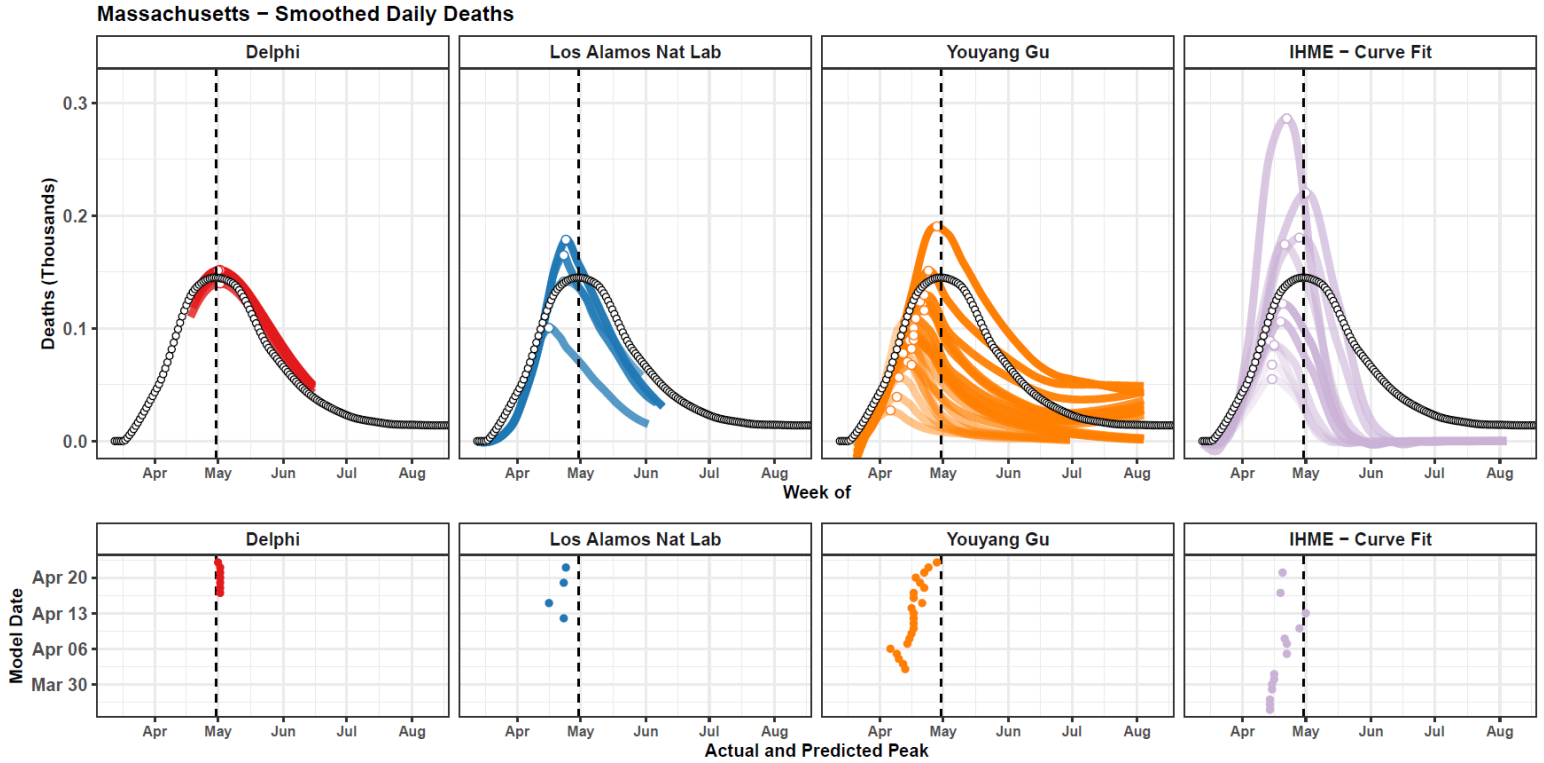


Figure 6. Observed vs Predicted Peak in Daily Deaths– Example for Massachusetts

Observed daily deaths, smoothed using a loess smoother, are shown as black-outlined dots (top). The observed peak in daily deaths is shown with a vertical black line (bottom). Each model version that was released at least one week prior to the observed peak is plotted (top) and its estimated peak is shown with a point (top and bottom). Estimated peaks are shown in the bottom panel with respect to their predicted peak date (x-axis) and model date (y-axis). Values are shown for the Massachusetts, and similar graphs for all other locations are available in the appendix. Massachusetts was chosen as the example location as the United States (used as the example for Figure 1) peaked earlier, only allowing for two models to provide peak timing errors, whereas Massachusetts peaked later, allowing for four models, making for a more illustrative example.

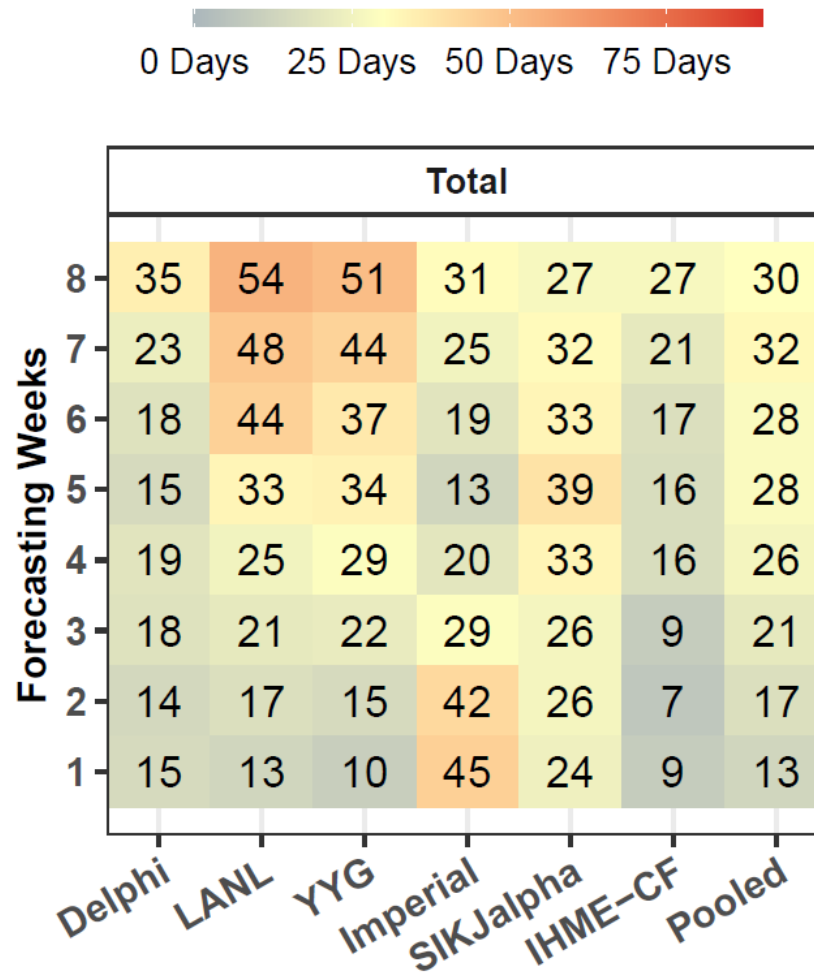


Figure 7. Peak Timing Accuracy – Median Absolute Error in Days

Median absolute error in days is shown by model and number of weeks of forecasting. Models that are not available for at least 40 peak timing predictions are not shown. Errors only reflect models released at least seven days before the observed peak in daily mortality. One week of forecasting refers to errors occurring from seven to 13 days in advance of the observed peak, while two weeks refers to those occurring from 14 to 20 days prior, and so on, up to six weeks, which refers to 42-48 days prior. Errors are pooled across month of estimation, as we found little evidence of change in peak timing performance by month (see appendix).