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OPEN Crystal structures and mechanical properties of osmium diboride at high pressure

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We have investigated the crystal structures and mechanical properties of osmium diboride (OsB₂) based on the density functional theory. The structures of OsB₂ from 0 to 400 GPa were predicted using the particle swarm optimization algorithm structure prediction technique. The orthorhombic Pmmn structure of OsB₂ (oP6-OsB₃) was found to be the most stable phase under zero pressure and it will transfer to the hexagonal P6₃/mmc structure (hP6-OsB₂) around 12.4 GPa. Meanwhile, we have discovered a new stable orthorhombic Immm structure (o/12-OsB₂) above 379.6 GPa. After that, a thorough and comprehensive investigation on mechanical properties of different OsB₂ phases is performed in this work. Further studies showed that the hardness of oP6-OsB2 and hP6-OsB2 at zero pressure is 15.6 and 20.1 GPa, while that for o/12-OsB₂ under 400 GPa is 15.4 GPa, indicating that these three phases should be potentially hard materials rather than superhard materials. Finally, the pressure-temperature phase diagram of OsB2 is constructed for the first time by using the quasi-harmonic approximation method. Our results showed that the transition pressures of oP6-OsB₂ $\rightarrow hP6$ -OsB₂ and hP6-OsB₂ $\rightarrow o/12$ -OsB₂ all decreases appreciably with the increase of temperature.

Hard and superhard materials have attracted considerable attention because of their excellent performance as cutting tools and abrasives. Diamond is an excellent superhard material, but it is difficult to synthesize artificially^{1,2}. Therefore, a lot of efforts have been invested to seek new hard materials in the past several decades. So far, one of the design principle of synthetic hard materials is to add light elements B, C, and N to electron-rich transition metals³, such as ReB₂⁴⁻⁷, OsB₂⁸⁻¹², WB₄^{13,14}, PtC¹⁵, Re₂C¹⁶, OsN₂¹⁷, PtN₂^{18,19}, etc. Among them, the transitionmetal borides have attracted considerable attention because of their excellent physicochemical property^{20,21}.

OsB₂ as a potential hard material, its structure and internal physical properties have been extensively studied in resent years^{8–12,22–27}. To our best knowledge, OsB₂ was first synthesized by Cumberland et al.⁸ through resistive heating method. They found that OsB₂ possess the orthorhombic Pmmn structure (oP6-OsB₂) at ambient condition, and it is an ultra-incompressible and hard material. It was soon confirmed by Gou et al.²² using first-principles total energy calculations, and showed that oP6-OsB₂ is not a superhard material. Later, Gu et al.⁹ synthesized oP6-OsB₂ compounds by arc melting and subsequent annealing method. They found that oP6-OsB₂ does not belong to the superhard materials, and its stability can reach up to 34 GPa. Except the oP6-OsB2 phase, other structures of OsB₂ have also been predicted by theoretical studies. For example, Hao et al.²⁸ reported that the orthorhombic *Pnma* structure of OsB₂ is thermodynamically and mechanically stable under environmental conditions. Moreover, using first-principles total energy calculations, Chen et al.²⁰ predicted that two hexagonal structures of P6₃/mmc and P6/mmm were also exist under pressure. Unfortunately, these phases have never been reported experimentally. Until 2014, Xie et al. 11 successfully synthesized hP6-OsB2 phase by means of mechanochemical method, and it was found to be stable at ambient conditions. Then, Ren et al.²³ investigated the structure stability of OsB2 under pressure through first-principles calculations. It is found that oP6-OsB2 is thermodynamically more stable than hP6-OsB₂ at 0 GPa. With the increase of pressure, oP6-OsB₂ will transfer to the hP6-OsB₂ at 10.8 GPa. Most recently, by using particle swarm optimization algorithm, Feng et al.²⁷ predicted two new high pressure phases Fddd and Cmcm of OsB₂ under pressure of 0-100 GPa. But, it is worth noting that the two high-pressure phases were both metastable structures.

As mentioned above, previous studies^{9,27,28} have predicted several stable OsB₂ structures under different pressures. However, the reported stable phases of OsB₂ were not in agreement with each other. Furthermore, most of the studies on this problem mainly concentrated in the low pressure stage, and few studies have done on high pressures^{23,27}. So far, the phase stability of OsB₂ under pressure up to 400 GPa is still unknown. As a

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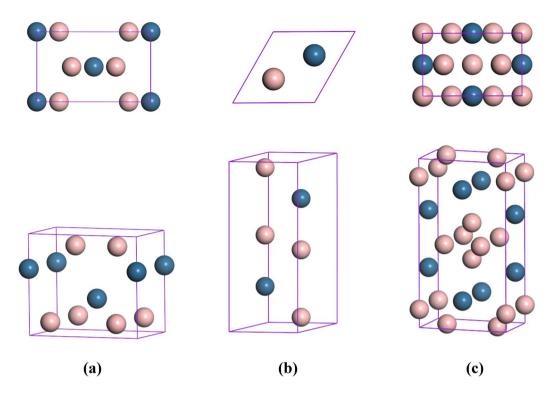


Figure 1. Top and three-dimensional views of the predicted crystal structures. (a) oP6-OsB₂ at 0 GPa, (b) hP6-OsB₂ at 20 GPa, and (c) oI12-OsB₂ at 400 GPa.

fundamental topic in condensed matter physics, revealing and elucidating the trend and mechanism of material high-pressure structural transformation is of great significance for its potential applications. Therefore, a thorough and comprehensive investigation on the phase stability of OsB_2 under high pressure is really necessary. In this work, we explored the crystal structures of OsB_2 from 0 to 400 GPa using particle swarm optimization (PSO) algorithm^{29,50} structure prediction technique. It is found that oP6- OsB_2 is the most stable structure at 0 GPa and it will transition to hP6- OsB_2 at low pressure range. Meanwhile, the orthorhombic *Immm* structure (oI12- OsB_2) is predicted for the first time under high pressure, and it will be the most stable phase above 379.6 GPa. Furthermore, a comprehensive investigation on mechanical properties of different OsB_2 phases also be performed in this work.

Computational details

We performed the structure prediction of OsB₂ at selected pressures of 0, 100, 200, 300, and 400 GPa using PSO algorithm²⁹ as implemented in the CALYPSO code³⁰. This method can predict stable or metastable crystal structures based on a given chemical compositions under specific external conditions. So far, it has been successfully applied not only to element solids, but also to binary and ternary compounds^{31–34}. Moreover, the ab initio optimizations and mechanical properties calculations for every structure generated by the CALYPSO code were performed using the VASP package³⁵ with the PBE generalized gradient approximation³⁶. The electron–ion interactions was dealt with PAW pseudopotentials³⁷ with $5p^65d^56s^2$ and $2s^22p^1$ valence configuration for Os and B, respectively. To achieve absolute convergences, the kinetic energy cutoff was set to 800 eV, and the Monkhorst–Pack k-point meshes³⁸ was selected to $8 \times 13 \times 9$ for oP6-OsB₂, $16 \times 16 \times 6$ for oP6-OsB₂, $15 \times 15 \times 3$ for oP6-OsB₂, oP6-OsB₂,

Results and discussion

Structure prediction and dynamical stability. According to the structure search results, oP6-OsB₂, hP6-OsB₂, hP6-OsB₂, tI6-OsB₂, tI6-OsB₂, and oC12-OsB₂ all possess lower enthalpy values under environmental pressure. Among them, oP6-OsB₂ (Fig. 1a) is the most stable phase at 0 GPa, which is consistent with previous experimental^{8,9,26} and theoretical^{22,23,27} results. Moreover, we found that hP6-OsB₂ (Fig. 1b) possesses the lowest enthalpy at the pressures of 100, 200 and 300 GPa. As the pressure increases further, a new oI12-OsB₂ (Fig. 1c) structure is discovered for the first time, which is the most stable structure under 400 GPa. The predicted structural parameters of different OsB₂ phases under pressure are listed in Table 1. For comparison the available experimental^{9,26} and theoretical^{24,25,27} data are also included. As shown, our obtained results agree well

Space group	Pearson symbol	Parameters	Atom	x	у	z	Ref
Pmmn (0 GPa)	oP6	a=4.702 b=2.892 c=4.092	Os(2a) B(4e)	0 0.3056	0 0.5	0.3449 0.1378	This work
		a=4.6756 b=2.8717 c=4.0670	Os(2a) B(1a)	0 0.3049	0 0.5	0.3463 0.1383	Cal. ²⁷
		a=4.696 c=4.094					Cal. ²⁴
		a=4.686 b=2.876 c=4.082					Exp.9
P63/mmc (0 GPa)	hP6	a=b=2.916 c=7.497	Os(2c) B(4f.)	0.3333 0.3333	0.6667 0.6667	0.25 0.5477	This work
		a=b=2.9185 c=7.3069	Os(2d) B(4f.)	0.3333 0.3333	0.6667 0.6667	0.25 0.4481	Cal. ²⁷
		a=b=2.906 c=7.301					Cal. ²⁵
		a=b=2.922 c=7.477					Exp. ²⁶
R-3 m (0 GPa)	hR9	a=b=2.912 c=11.191	Os(3a) B(6c)	0	0	0 0.1962	This work
		a=b=2.890 c=11.139	Os(3a) B(6c)	0	0	0 0.1965	Cal. ²⁷
I4/mmm (0 GPa)	tI6	a=b=2.848 c=6.840	Os(2a) B(4d)	0	0 0.5	0 0.25	This work
		a=b=2.830 c=6.803	Os(2b) B(4d)	0.5 0	0.5 0.5	0 0.25	Cal. ²⁷
P4/nmm (0 GPa)	tP6	a=b=2.828 c=6.751	Os(2c) B1(2c) B2(2b)	0 0 0.5	0.5 0.5 0.5	0.7539 0.833 0.5	This work
Cmcm (0 GPa)	oC12	a=2.933 b=7.247 c=5.447	Os(4c) B(8f.)	0.5 0.5	0.9223 0.2226	0.75 0.5933	This work
Immm (400 GPa)	oI12	a = 2.418 b = 3.825 c = 7.172	Os(4j) B1(4i) B3(4 h)	0 0 0.5	0.5 0 0.2083	0.1703 0.1072 0	This work

Table 1. Lattice constants and atomic coordinates of different OsB₂ structures, together with available experimental and theoretical results.

with other data, which proves the reliability of this research. In addition, we further evaluated the formation enthalpies of different OsB_2 phases at ambient condition by the equation: $\Delta H = H(OsB_2) - H(Os) - 2H(B)$, in which the R-3 m phase for B and the Fm-3 m phase for Os were selected as the reference structures. Our obtained formation enthalpies of oP6- OsB_2 , hP6- OsB_2 , hP6- OsB_2 , tP6- OsB_2 , tP6- OsB_2 , oC12- OsB_2 , and oI12- OsB_2 at zero pressure are -0.775, -0.751, -0.531, -0.476, -0.567, -0.633, and 0.910 eV/f.u., respectively. Among them, oP6- OsB_2 possesses the minimum formation enthalpy. Moreover, except for the high-pressure phase tI12- OsB_2 , the formation enthalpies of other structures is all negative, indicating that they are potential metastable structures of OsB_2 under environmental conditions.

To evaluate the transition pressures of OsB_2 at zero Kelvin, the calculated enthalpy differences of hP6-OsB₂, hR9-OsB₂, tP6-OsB₂, and oI12-OsB₂ with respect to oP6-OsB₂ phase under pressure are provided in Fig. 2. As shown, oP6-OsB₂ has lower enthalpy than other structures at 0 GPa, indicating that it is the most stable structure under ambient conditions. Moreover, the pressure-induced transformation from oP6-OsB₂ to hP6-OsB₂ occurs at about 12.4 GPa, which is in good agreement with the theoretical result of 10.8 GPa²³. After that, hP6-ReB₂ possesses structure stability in a wide pressure range. As the pressure increases further, the stability of oI12-OsB₂ gets enhanced gradually, and it becomes the most stable phase above 379.6 GPa. Thus, the phase transition sequence of OsB₂ under pressure should be oP6-OsB₂ $\rightarrow hP6$ -OsB₂ $\rightarrow oI12$ -OsB₂. Moreover, the vibrational phonon dispersion curves under a series of pressures are further calculated to assess their dynamic stability. The obtained results at selected pressures are presented in Fig. 3. We found that oP6-OsB₂, hP6-OsB₂, and oI12-OsB₂ do not show any imaginary frequencies under pressure of 0–200, 0–440, and 200–440 GPa, respectively, indicating that these phases should be dynamically stable within the corresponding pressure range. In addition, the equations of state of OsB₂ under pressure up to 450 GPa is further evaluated, as shown in Fig. 4. It is obvious that the volume decreases of 1.18% from oP6-OsB₂ to oP6-OsB₂ are first-order rather than continuous.

Mechanical properties. The elastic properties of OsB₂ under different pressures are investigated by strainstress method. Our calculated elastic constants of oP6-OsB₂, hP6-OsB₂, hP9-OsB₂, tI6-OsB₂, tP6-OsB₂, and oC12-OsB₂ under zero pressure are given in Table 2. It is obvious that our obtained results are consistent well

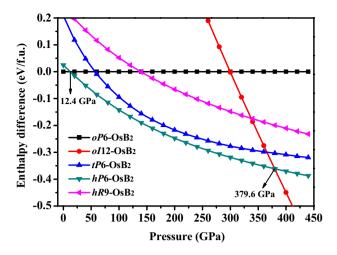


Figure 2. Enthalpy differences of predicted structures relative to oP6-OsB₂ structure under high pressure.

with the available theoretical data^{24,25,27,41}. Moreover, the obtained elastic constants of oI12-OsB₂ at 400 GPa are also included in Table 2, but unfortunately there is no data can be compared with them. In addition, we can judge the mechanical stability of crystals based on their elastic constant^{42,43}. For hexagonal structures of hP6-OsB₂ and hR9-OsB₂,

$$\tilde{C}_{44} > 0, \tilde{C}_{11} - \left| \tilde{C}_{12} \right| > 0, \left(\tilde{C}_{11} + \tilde{C}_{12} \right) \tilde{C}_{33} - 2 \tilde{C}_{13}^2 > 0.$$
 (1)

For tetragonal crystals of tI6-OsB₂ and tP6-OsB₂,

$$\tilde{C}_{ii} > 0$$
, $(i = 1, 3, 4, 6)$,

$$\tilde{C}_{11} - \tilde{C}_{12} > 0, \tilde{C}_{11} + \tilde{C}_{33} - 2\tilde{C}_{13} > 0, 2(\tilde{C}_{11} + \tilde{C}_{12}) + \tilde{C}_{33} + 4\tilde{C}_{13} > 0.$$
 (2)

For orthorhombic phases of oP6-OsB₂, oC12-OsB₂ and oI12-OsB₂,

$$\tilde{C}_{ii} > 0, (i = 1, 2, 3, 4, 5, 6),$$

$$\tilde{C}_{11} + \tilde{C}_{22} + \tilde{C}_{33} + 2(\tilde{C}_{12} + \tilde{C}_{13} + \tilde{C}_{23}) > 0,$$

$$\tilde{C}_{ii} + \tilde{C}_{jj} - 2\tilde{C}_{ij} > 0, (i, j = 1, 2, 3, i \neq j).$$
 (3)

where $\tilde{C}_{ii} = C_{ii} - P$ (i = 1, 2, 3, 4, 5, 6), $\tilde{C}_{ij} = C_{ij}$ (i = 1, 2, 3; j = 4, 5, 6), $\tilde{C}_{12} = C_{12} + P$, $\tilde{C}_{13} = C_{13} + P$, $\tilde{C}_{23} = C_{23} + P$, $\tilde{C}_{45} = C_{45}$, $\tilde{C}_{46} = C_{46}$, $\tilde{C}_{56} = C_{56}$. After careful check, the calculated elastic constants of oP6-OsB₂, hP6-OsB₂, tI6-OsB₂, tI6-OsB₂

In addition, for all OsB_2 structures, the calculated C_{11} , C_{22} , and C_{33} are obviously larger than other elastic constants, indicating that they should be hard to compress on the a, b, and c axes. As the hardest natural minerals, diamond possesses a high elastic constant C_{11} of 1079 GPa at ambient conditions⁴⁴. Interestingly, our obtained C_{33} of hP6-OsB $_2$ is about 887 GPa at zero pressure, close to the C_{11} value of diamond, which implies that hP6-OsB $_2$ may also be a hard material. For this reason, we further evaluated the hardness of different OsB $_2$ structures by an empirical model⁴⁵, which can be expressed as

$$H_{\nu} = 2(k^2G)^{0.585} - 3,$$
 (4)

in which k is equal to G/B. Through Voigt-Reuss-Hill approximation⁴⁶, the bulk modulus B, and shear modulus G can be calculated by the elastic constants C_{ij} . The obtained results, along with the other theoretical data^{24,25,27,41}, are presented in Table 3. It is obvious that our calculated B and G agree with the available calculated results. Moreover, we can judge the ductility or brittleness of a material by the B/G ratio⁴⁷. Usually, a material is ductile if B/G > 1.75, or else it is brittle. Under zero pressure, our calculated B/G of oP6-OsB₂, hP6-OsB₂, hP6-OsB₂, tP6-OsB₂, tP6-OsB₂, and oC12-OsB₂ is 1.90, 1.71, 1.50, 1.30, 1.62, and 1.54, respectively. This indicates that oP6-OsB₂ is ductile, and the other phases are all brittle under environmental conditions. Meanwhile, the high-pressure phase oI12-OsB₂ should be ductile at 400 GPa, because its B/G ratio is greater than the critical value under this pressure.

According to the obtained B and G, we can further calculated Young's modulus E and Poisson's ratio σ by

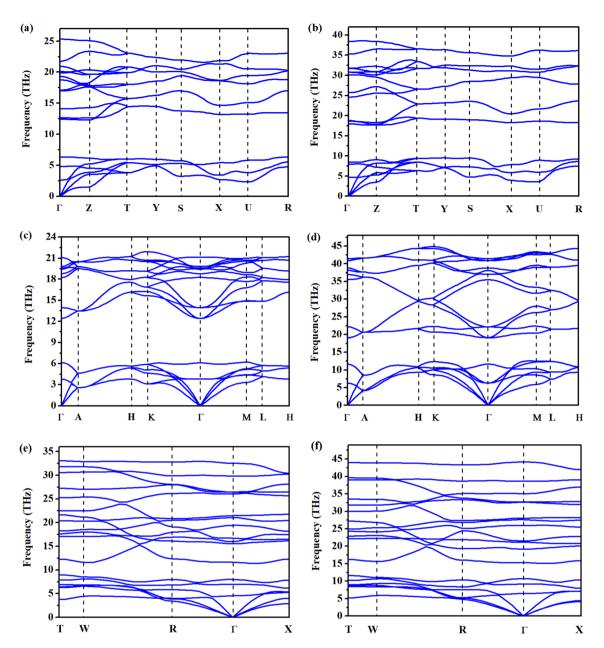


Figure 3. Calculated phonon dispersion curves of (**a,b**) *oP6*-OsB₂ at 0 and 200 GPa, (**c,d**) *hP6*-OsB₂ at 0 and 440 GPa, and (**e,f**) *oI*12-OsB₂ at 200 and 440 GPa, respectively.

$$E = \frac{9BG}{3B+G}, \quad \sigma = \frac{3B-2G}{6B+2G}.$$
 (5)

As shown in Table 3, our calculated results are consistent well with the available experimental⁴ or other calculated data 24,25,27,41 . Generally, a higher value of E indicates that the material is stiffer, while a smaller value of G indicates that the covalent bond is more directional. Accordingly, the order of stiffness of OsB_2 is tI6 > tP6 > hR9 > hP6 > oC12 > oP6, while the directionality degree of covalent bonds of OsB_2 should be tI6 > hR9 > oC12 > tP6 > hP6 > oP6 under ambient conditions. Furthermore, our calculated hardness of $oP6 - OsB_2$, $oP6 - OsB_2$,

Pressure–temperature phase diagram. After established the phase transition sequence of oP6-OsB₂ \rightarrow **hP**6-OsB₂ \rightarrow **oI**12-OsB₂ under pressure at zero Kelvin. We further investigated the stable region of each

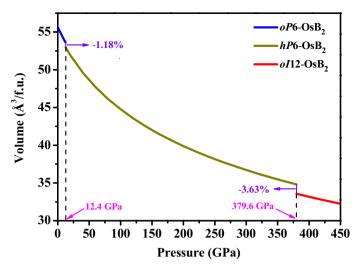


Figure 4. The equation of states (P-V curve) of OsB_2 . The purple lines indicate the volume reduction at 12.4 and 379.6 GPa.

Phase	C ₁₁	C ₁₂	C ₁₃	C ₂₂	C_{23}	C ₃₃	C ₄₄	C ₅₅	C ₆₆	Ref
oP6-OsB ₂ (0 GPa)	541	176	180	565	125	763	194	67	191	This work
	586	201	179	551	161	792	206	54	222	Cal. ²⁷
	549	164	183	538		744	203	77	199	Cal. ²⁴
	570	178	188	540		753	191	68	192	Cal.41
hP6-OsB ₂ (0 GPa)	478	179	216			887	212		150	This work
	404	178	294			873	227		113	Cal. ²⁷
	487	180	229			880	215		154	Cal. ²⁵
	453	183	218			870	206			Cal. ²⁴
hR9-OsB ₂ (0 GPa)	511	183	181			902	249		164	This work
	505	209	215			929	262		148	Cal. ²⁷
tI6-OsB ₂ (0 GPa)	627	66	194			913	301		153	This work
	650	80	214			969	306		107	Cal. ²⁷
tP6-OsB ₂ (0 GPa)	702	92	185			872	175		171	This work
oC12-OsB ₂ (0 GPa)	504	135	162	598	93	672	247	151	110	This work
oI12-OsB ₂ (400 GPa)	2619	1086	1397	2611	1313	2145	485	496	408	This work

Table 2. Calculated elastic constants C_{ij} (in GPa) of different OsB₂ structures, together with other theoretical results.

phases under high pressure and high temperature through the quasi-harmonic approximation (QHA)⁵⁰ method. In which, the Helmholtz free energy is given by

$$F(V,T) = E(V) + F_{\text{vib}}(V,T), \tag{6}$$

where E(V) is the static energy, $F_{vib}(V,T)$ is the nonequilibrium vibrational Helmholtz free energy

$$F_{vib}(V,T) = \int_0^\infty \left[\frac{\hbar \omega}{2} + \kappa_B T \ln \left(1 - e^{-\hbar \omega / \kappa_B T} \right) \right] g(\omega, T) d\omega, \tag{7}$$

in which $g(\omega, V)$ represents phonon density of state. Then, we can get the Gibbs free energy by

$$G_{\text{gibbs}} = F(V, T) - V\left(\frac{\partial F}{\partial V}\right)_{T}.$$
 (8)

Our phonon frequencies calculations in Sect. 3.1 indicates that oP6-OsB₂, hP6-OsB₂, and oI12-OsB₂ are dynamically stable within a large pressure range. Thus, according to the calculated Gibbs free energies of these three phases under different temperatures and pressures, the phase diagram of OsB₂ is constructed for the first time, as shown in Fig. 5. It can be seen that temperature has a significant effect on the structural stability of OsB₂. With the increase of temperature, the transition pressures of oP6-OsB₂ $\rightarrow hP6$ -OsB₂, and hP6-OsB₂ $\rightarrow oI12$ -OsB₂

	В	G	B/G	E	σ	$H_{ m V}$	Ref
	312	164	1.90	419	0.28	15.6	This work
	335	189	1.77	477	0.263	19.6	Cal. ²⁷
oP6-OsB ₂ (0 GPa)	304	172	1.77	434	0.262	21.9	Cal. ²⁴
	310	164	1.89	419	0.275		Cal.41
				410	0.27	21.6	Exp.4
	326	191	1.71	480	0.25	20.1	This work
hP6-OsB ₂ (0 GPa)	334	192	1.74	485	0.258	34.5	Cal. ²⁵
	357	174	2.05	449	0.290	15.7	Cal. ²⁷
hR9-OsB ₂ (0 GPa)	325	217	1.50	533	0.23	26.0	This work
nk9-Osb ₂ (0 GPa)	357	221	1.62	550	0.243	24.4	Cal. ²⁷
tI6-OsB ₂ (0 GPa)	331	255	1.30	609	0.19	34.7	This work
110-OSD ₂ (0 GFa)	365	261	1.40	632	0.211	32.3	Cal. ²⁷
tP6-OsB ₂ (0 GPa)	351	217	1.62	540	0.24	23.5	This work
oC12-OsB ₂ (0 GPa)	283	184	1.54	453	0.23	22.5	This work
oI12-OsB ₂ (400 GPa)	1661	503	3.30	1372	0.36	15.9	This work

Table 3. Calculated bulk modulus B (in GPa), shear modulus G (in GPa), B/G, Young's modulus E (in GPa), Poisson's ratio σ , and hardness H_V (in GPa) of different OsB₂ structures, together with available experimental and theoretical results.

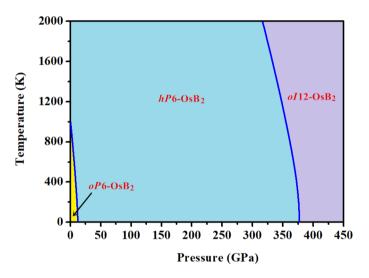


Figure 5. Calculated temperature–pressure phase diagram of OsB₂ based on the QHA.

all decreases appreciably. Moreover, oP6-OsB₂ is located only in a very small region at the lower left corner of phase diagram, and it will transition to hP6-OsB₂ with a temperature of ~ 1000 K at zero pressure. This is consistent with the previous experimental results of 873 K¹². Meanwhile, the phase transformation of hP6-OsB₂ \rightarrow oI12-OsB₂ occurs at 374.5 GPa under room temperature of 300 K.

Conclusions

We have investigated the structure stability of OsB_2 from 0 to 400 GPa through the ab initio PSO algorithm. The phase transition sequence of oP6- $OsB_2 \rightarrow hP6$ - $OsB_2 \rightarrow oI12$ - OsB_2 under pressure was established. Through high precision calculations, the transition pressures were determined as 12.4 and 379.6 GPa at zero Kelvin. Phonon frequencies calculations show that oP6- OsB_2 , hP6- OsB_2 , and oI12- OsB_2 possess dynamical stability under 0–200, 0–440, and 200–440 GPa, respectively. Moreover, the elastic constants and elastic-dependent properties of OsB_2 are also successfully investigated. Our calculated hardness suggests that oP6- OsB_2 , hP6- OsB_2 , and oI12- OsB_2 are both potential hard materials rather than superhard materials. Furthermore, the phase diagram of OsB_2 at high pressure and high temperature was constructed for the first time based on the QHA method. Our result shows that the transition pressures of oP6- $OsB_2 \rightarrow hP6$ - OsB_2 and hP6- $OsB_2 \rightarrow oI12$ - OsB_2 all decreases with the increase of temperature.

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Author contributions

Y.-X.W. conceived the research. Y.-X.W. and Y.-Y.L. performed atomic and electronic structure calculations. Y.-X.W., Y.-Y.L., Z.-X.Y., W.L., G.-L.Z., and K.-Z.X. analyzed the numerical results. Y.-X.W. wrote the manuscript and all the authors commented on it.

Competing interests

The authors declare no competing interests.

Additional information

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