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OPEN Resonant vortex-core reversal in magnetic nano-spheres as robust mechanism of efficient energy absorption and emission

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We report on novel vortex-core reversal dynamics in nano-spheres of single-vortex spin configuration as revealed by micromagnetic simulations combined with analytical derivations. When the frequency of an AC magnetic field is tuned to the frequency of the vortex-core precession around the direction of a given static field, oscillatory vortex-core reversals occur, and additionally, the frequency is found to change with both the strength of the applied AC field and the particle size. Such resonant vortex-core reversals in nano-spheres may provide a new and efficient means of energy absorption by, and emission from, magnetic nanoparticles, which system can be effectively implemented in bio-applications such as magnetic hyperthermia.

Non-uniform spin configurations in magnetic nano-elements exhibit contrasting magnetization reversal dynamics. For instance, the magnetic vortex, which consists of a uniformly magnetized core in a local central region and curling spin configuration around it in planar thin-film nano-dots^{1,2}, show, through the resonant dynamic effect, novel vortex-core gyration and switching dynamics with low-power consumption. Such novel dynamics as the mechanism³⁻⁵, criterion⁶⁻¹¹, and physical origin^{4,8,11} of the core reversals are well established in case of planar thin-film disks. As for soft-magnetic nano-spheres, our previous papers^{12,13} reported that they bear specific spiral magnetizations around a uniformly magnetized core region, the so-called vortex core, in cases where the particle diameter is larger than single-domain size but smaller than multiple-domain size. In our earlier work¹², we demonstrated successful fabrication of spherical Permalloy (Py) nanoparticles and conformed vortex-state magnetization configurations using the electron holography measurement technique. As shown in ref. 13, the vortex core in nano-spheres is found to exhibit a unique precession motion around the direction of an externally applied static field, and, further, the precession frequency is determined by the sphere size as well as the static field strength. The core precession thus can be excited with low-power consumption when the frequency of an externally applied AC magnetic field is tuned to the eigenfrequency of the core-precession mode, though the mechanism is completely different from that of vortex-core gyration in planar thin-film dots.

In the present study, we explored vortex-core reversals resonantly driven by AC magnetic fields with the assistance of excited vortex-core precession in soft magnetic nano-spheres. This vortex-core reversal is completely different from typical microwave-assisted magnetization switching in single-domain nanoparticles and vortex-core-gyration-assisted core reversals in planar thin-film dots. The relevant dynamics serve as a robust mechanism of efficient energy transfer into and from vortex-state magnetic particles: application of sufficiently weak AC magnetic fields allows for resonant energy absorption from external magnetic fields to vortex-state nano-spheres. Although the vortex-core precession in nano-spheres and its frequency dependence on particle size and the strength of the DC field have already been reported (see ref. 13), the vortex-core reversal and its underlying physics have as yet remained (until the present work) unexplored. The simulation and analytical numerical calculations in the present work revealed that the core-reversal frequency changes significantly with the AC field strength for a given particle diameter. The volume or mass-specific energy absorption rate of the magnetic nano-spheres showed good agreement with the simulation results. Such an efficient means of high-power-rate

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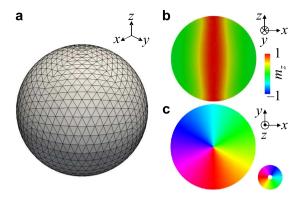


Figure 1. Sphere model and its ground-state magnetization configuration. (a) Finite-element Py sphere of diameter 2R = 80 nm. (b,c) represent the ground-state magnetization configuration viewed in the x-z plane at y = 0 nm and the x-y plane at z = 0 nm, respectively. The colors in (b,c) correspond to the z components of the local magnetizations ($m_z = M_z/M_s$), as indicated by the color bar, and to the in-plane components of the local magnetizations, as indicated by the color wheel.

energy absorption and subsequent emission can be implemented in possible future bio-diagnostic and magnetic-hyperthermia-treatment applications.

Results

Resonant vortex-core reversal. Figure 1 shows the ground state of a permalloy (Py) nano-sphere of 2R = 80 nm diameter, as obtained by relaxation from the saturated magnetizations in the +z-direction. The spin microstructure indicates a rather uniformly magnetized vortex core with spiral magnetizations around the core. To resonantly excite the core precession, we applied a counter-clockwise (CCW) circular-rotating field, owing to the fact that in the sphere, one of the intrinsic dynamic modes is the CCW core precession about a DC magnetic field applied in the +z-direction. The CCW circular-rotating field used is expressed mathematically as $\mathbf{H}_{\mathrm{CCW}} = \mathbf{\hat{x}} H_{\mathrm{AC}} \cos(2\pi f_{\mathrm{CCW}} t) + \mathbf{\hat{y}} H_{\mathrm{AC}} \sin(2\pi f_{\mathrm{CCW}} t)$, where f_{CCW} is the frequency of the rotating field with a strength of $H_{\mathrm{AC}} = 10$ Oe and a static magnetic field $+\mathbf{\hat{z}} H_{\mathrm{DC}}$ (here $H_{\mathrm{DC}} = 100$ Oe). When we applied $f_{\mathrm{CCW}} = 51$ MHz, which equaled the eigenfrequency of the core precession (See Methods), the core started to show precession, and then reversed its magnetization orientation at a certain time with respect to the direction of $+\hat{\mathbf{z}}H_{DC}$ (see Supplementary Movie). Figure 2a plots, in the 3D perspective, the trajectory of the core motion as represented by the unit vector Λ of the core orientation. The temporal evolutions of the x-, y-, z- components of Λ are shown in Fig. 2b. In detail, upon the application of the CCW rotation field, the core, of initial orientation $\Lambda = (0, 0, 1)$ at t=0 ns, begins its precession about the +z-direction in CCW rotational sense. The angle between Λ and $\hat{\mathbf{z}}$ increases with time until, at t = 109 ns, the core orientation flips to $\Lambda = (0, 0, -1)$. This core-reversal behavior discovery is the first for vortex-state nano-spheres. With continuous application of the CCW rotating field, the reversed core returns, at t = 200 ns, to the initial $\Lambda = (0, 0, 1)$ orientation via core precession of the same CCW rotation sense. This reversal occurs repeatedly in a periodic manner. From the FFTs of the temporal variations of the x-, y-, z-components of Λ shown in Fig. 2b, we obtained the frequencies of the core precession and reversal to be $f_{\rm prec} \sim 51$ MHz and $f_{\rm rev} \sim 5$ MHz respectively, for the given diameter of 80 nm and $H_{\rm DC} = 100$ Oe. We stress here that the mechanism of periodic core reversal via resonantly excited core precession differs completely not only $from \ that \ of \ microwave-assisted \ magnetization \ switching \ in \ single-domain \ magnetic \ elements^{14-20} \ but \ also \ from \ magnetic \ elements^{14-20} \ but \ also \ elements^{14-20} \ b$ that of vortex-core reversals driven by oscillating^{5-6,8,21} or pulse^{22,23} fields/currents in planar thin-film dots.

Next, we examined the variation of f_{rev} with H_{AC} . Figure 3a plots the temporal oscillations of Λ_z for different H_{AC} values, and Fig. 3b the total energy variation, during core precession and reversal. The FFTs of the Λ_z oscillations result in characteristic resonant peaks in FFT power versus f_{AC} according to H_{AC} (see Fig. 3c). Those peaks are sufficiently distinguishable with varying H_{AC} in steps of 10 Oe, indicating that the core reversal's frequency varies and is controllable with the strength of $H_{\rm AC}$, not with the static field strength $H_{\rm DC}$. This fact is key to the control of f_{rev} simply with the strength of H_{AC} for a given nano-sphere. With respect to one of our earlier studies, we reported that f_{prec} varies with the sphere diameter, 2R. Thus, in the present investigation, we also examined, in further simulations, the variation of f_{rev} with 2R. Figure 4 shows the linear relations between f_{rev} and H_{AC} but different slopes for different 2R values. For each diameter, we used the f_{CCW} value that equals the f_{prec} for the given 2R. The slope (f_{rev}/H_{AC}) is plotted as a function of 2R in the inset of Fig. 4. As can be seen, as 2R increases, the slope markedly decreases. For example, for single-domain states (2R = 20 and 30 nm), the slope is about $2.8 \,\mathrm{MHz/Oe}$ but for $2R = 60 \,\mathrm{nm}$, it decreases to $0.985 \,\mathrm{MHz/Oe}$. This value is about 65% smaller than that for single-domain spheres. It is noteworthy too, that for single-domain spheres, f_{rev}/H_{AC} does not change with 2R, while for vortex-state spheres, it varies significantly with 2R. From a technological point of view, it is advantageous that the resonant core reversal is very specific to the particle size for a given strength of H_{AC} . This means, crucially, that size-specific particle excitations, including core precession and reversal, are possible.

Analytical derivation. To understand the underlying physics of the dependences of f_{rev} on both H_{AC} and 2R, as revealed by the micromagnetic simulations, we derived the analytical form of f_{rev} as a function of both

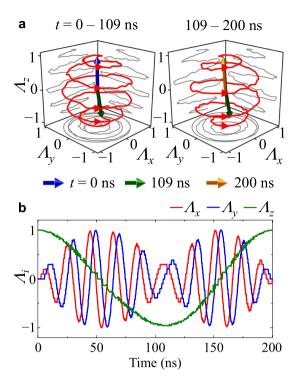


Figure 2. Temporal evolution of vortex-core orientation during resonant core precession and reversal. (a) Trajectories (red color) of vortex-core orientation $\mathbf{\Lambda} = (\Lambda_x, \Lambda_y, \Lambda_z)$, which motion is resonantly excited by a circular rotating field, $\mathbf{H}_{\text{CCW}} = \hat{\mathbf{x}} H_{\text{AC}} \cos(2\pi f_{\text{CCW}} t) + \hat{\mathbf{y}} H_{\text{AC}} \sin(2\pi f_{\text{CCW}} t)$ with $H_{\text{AC}} = 10$ Oe and $f_{\text{CCW}} = 51$ MHz, while applying a static field along the z axis ($\hat{\mathbf{z}} H_{\text{DC}}, H_{\text{DC}} = 100$ Oe). The left and right panels correspond to the core motions during t = 0–109 ns and t = 109–200 ns, respectively. The blue, green, and orange arrows represent the core orientation at t = 0, 109, and 200 ns, respectively. (b) Temporal variation of x, y, z components of core orientations, Λ_x , Λ_y , and Λ_z .

2R and $H_{\rm AC}$. By assuming a rigid vortex model and negligible Gilbert damping, we obtained the governing equation of the core motion in a vortex-state nano-sphere, $\dot{\Lambda} + |\gamma| \langle m_A \rangle \Lambda \times {\bf H} = 0$, where ${\bf H}$ is the external magnetic field and $\langle m_A \rangle$ is the average magnetization component over the sphere volume in the vortex-core orientation (see Methods for details). As in the micromagnetic simulations, we set ${\bf H} = {\bf H}_{\rm CCW} + \hat{\bf z} H_{DC}$ with ${\bf H}_{\rm CCW} = \hat{\bf x} H_{\rm AC} \cos(2\pi f_{\rm CCW} t) + \hat{\bf y} H_{\rm AC} \sin(2\pi f_{\rm CCW} t)$. By setting $f_{\rm CCW} = f_{\rm prec}$ and the initial core orientation as ${\bf \Lambda} = (0,0,1)$ at t=0, we obtained the relations

$$\Lambda_x(t) = \sin(2\pi f_{\text{rev}} t) \sin(2\pi f_{\text{prec}} t) \tag{1}$$

$$\Lambda_{y}(t) = -\sin(2\pi f_{\text{rev}}t)\cos(2\pi f_{\text{prec}}t)$$
(2)

$$\Lambda_z(t) = \cos(2\pi f_{\text{rev}} t),\tag{3}$$

where $2\pi f_{\rm rev} = \gamma \langle m_\Lambda \rangle H_{\rm AC}$ and $2\pi f_{\rm prec} = \gamma \langle m_\Lambda \rangle H_{\rm DC}$. As reported in ref. 13, the value of $\langle m_\Lambda \rangle$ varies markedly with 2R in vortex-state spheres ($\langle m_\Lambda \rangle = 1$ for single-domain spheres). In the present results, it was quite noticeable that the core reversal's frequency is a function of both $\langle m_\Lambda \rangle$ and $H_{\rm AC}$. The numerical calculation (i.e., analytical expression) of $2\pi f_{\rm rev} = \gamma \langle m_\Lambda \rangle H_{\rm AC}$ for different 2R values agreed well with the simulation results, as represented by the lines and symbols respectively, in Fig. 4. In the numerical calculation, we used $\langle m_\Lambda \rangle = 73.6 (l_{\rm ex}/2R)^{2.20}$ with $l_{\rm ex}$ the exchange length ($l_{\rm ex} \sim 5.3$ nm for Py), as reported in ref. 13. For the given material Py, $f_{\rm rev}$ is therefore a function of both $H_{\rm AC}$ and 2R for the vortex-state spheres, but only of $H_{\rm AC}$ for the single-domain spheres (i.e., $\langle m_\Lambda \rangle = 1$), independently of the particle size, as shown in the inset of Fig. 4.

Robust mechanism of efficient energy absorption and emission. Controllable nano-sphere vortex-core reversals driven by oscillation or pulse fields in vortex-state soft magnetic nanoparticles can be used as a robust mechanism of resonant energy absorption and emission. Via the novel dynamic effects of the observed resonant core precession and reversal, external magnetic field energy can be transferred efficiently to nano-spheres. Furthermore, the energy absorbed into nanoparticles can be emitted to proximate environments in the form of heat through magnetization dissipation^{24,25} (or via electromagnetic waves, though the energy is very weak). Such energy-exchange processes are efficiently achieved, via the resonant excitation of vortex-core

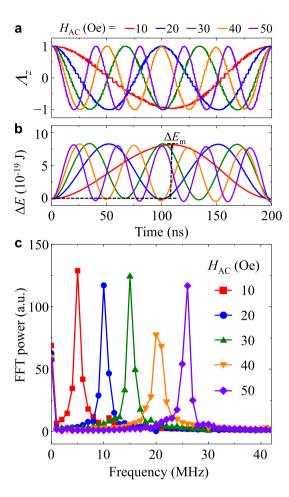


Figure 3. Core-reversal oscillation versus ac field strength. (a) Temporal evolution of Λ_z for different field strengths, $H_{\rm AC}=10$, 20, 30, 40, and 50 Oe. (b) Total energy variation ($\Delta E=E(t)-E(0)$) during resonant core reversal in Py nano-spheres of 2R=80 nm with $H_{\rm DC}=100$ Oe. $\Delta E_{\rm m}$ denotes the maximum energy increment for each $H_{\rm AC}$. (c) FFT power spectrum in frequency domain for different $H_{\rm AC}$ values, as obtained from Λ_z oscillations in (b) within t=0-1 μs period.

precession and reversal, by tuning the frequency of the AC field, whether circular rotating or linear, to the f_{prec} value for a given material, diameter, and H_{DC} .

In order to quantitatively determine the amount of the energy exchange and its transfer rate (i.e., power), we calculated the energy variation ΔE as a function of time for different $H_{\rm AC}$ values, as shown in Fig. 3b. The periodicities of the ΔE oscillations exactly equaled those of the Λ_z oscillations; thus $f_{\Delta E} = f_{\rm rev}$. The maximum energy increment $\Delta E_{\rm m}$ is constant with $H_{\rm AC}$. The 2R dependence of $\Delta E_{\rm m}$ differs from the single domain to the vortex-state spheres, as indicated in Fig. 5c by the open and closed symbols, respectively. Additionally, for the single-domain spheres (here $2R \leq 37.3$ nm), the frequency of ΔE oscillation (the top panel of Fig. 5d) is a constant value of 280 MHz, whereas for the vortex-state nano-spheres, it markedly varies with 2R. The energy absorption rate per unit mass (i.e., the power per mass), defined as $\Delta E_{\rm m} f_{\Delta E} / V \rho_{\rm Py}$, was calculated versus 2R from the simulation data using $\rho_{\rm Py} = 8.74\,{\rm g/cm^3}$ for Py, as shown in Fig. 5e. The energy absorption rate (EAR) versus 2R for the vortex-state particles differs from a constant value of $5.5 \times 10^4\,{\rm W/g}$ for the single-domain-state particles. The EAR is similar to the specific absorption rate (SAR) representative of heating efficiency in magnetic hyperthermia 26,27 .

To obtain further insight into the 2R-dependent EAR, we analytically derived the EAR as defined by $\Delta E_{\rm m}$ $f_{\Delta E}/V\rho_{\rm Py}$. As explained earlier, ΔE oscillations originate from the Zeeman energy variation due to the reversal of the core orientation with respect to the +z direction of the applied $H_{\rm DC}$. Thus, $\Delta E_{\rm m}$ can be rewritten in the form $2VM_{\rm s}$ $\langle m_{\Lambda} \rangle H_{\rm DC}^{13}$ along with $f_{\Delta E} = (\gamma/2\pi) \langle m_{\Lambda} \rangle H_{\rm AC}$. By applying $\langle m_{\Lambda} \rangle = 1$ for the single-domain and $\langle m_{\Lambda} \rangle = 73.6 (l_{\rm ex}/2R)^{2.2}$ for vortex-state particles, we obtained the analytic forms of $\Delta E_{\rm m} = (\pi/3) M_{\rm s} H_{\rm DC} (2R)^3$ and $f_{\Delta E} = (\gamma/2\pi) H_{\rm AC}$ for single-domain particles and of $\Delta E_{\rm m} = (73.6\pi/3) M_{\rm s} H_{\rm DC} l_{\rm ex}^{2.2} (2R)^{0.8}$ and $f_{\Delta E} = 73.6 (\gamma/2\pi) H_{\rm AC} l_{\rm ex}^{2.2} (2R)^{-2.2}$ for vortex-state particles. From these analytical expressions, we finally obtained EAR $= (1/\pi \rho_{\rm py}) \gamma M_{\rm s} H_{\rm DC} H_{\rm AC}$ for single-domain particles and EAR $= (73.6^2/\pi \rho_{\rm py}) \gamma M_{\rm s} H_{\rm DC} H_{\rm AC} (l_{\rm ex}/2R)^{4.4}$ for vortex-state particles. As shown in Fig. 5c–e, these analytic forms (the corresponding lines) were found to be in excellent agreement with the simulation results (the square symbols) for Py nano-spheres of different 2R.

As shown in Fig. 5e, the EAR per mass for single-domain Py particles is about 5.5×10^4 W/g, which is one or two orders of magnitude larger than typical SAR value ($\sim 10^2 - 10^3$ W/g) for magnetic hyperthermia²⁸. The EAR

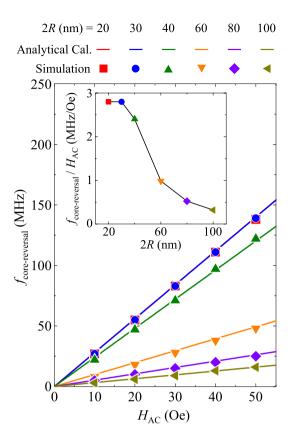


Figure 4. Core-reversal frequency as function of $H_{\rm AC}$ for different 2R values. The symbols denote the micromagnetic simulation results, while the solid lines correspond to the numerical calculations using $2\pi f_{\rm rev} = \gamma \langle m_{\Lambda} \rangle H_{\rm AC}$. The inset shows the corresponding slopes of the $f_{\rm rev}$ versus $H_{\rm AC}$ linear curves for the different 2R values.

for vortex-state particles varies with 2R, as indicative of particle-size specificity. Furthermore, for a given size of vortex-state nano-sphere, the specific $H_{\rm AC}$ and $H_{\rm DC}$ and values also determine $f_{\Delta E} = f_{\rm rev}$ and $\Delta E_{\rm m}$, respectively, thus characterizing specific EAR values. This factor, crucially, provides for vortex-state-nanoparticle-based EAR controllability not only by nanoparticle size but also, and simply, by tunable parameters (e.g., field strength and frequency) of externally applied AC and DC magnetic fields.

Discussion

We studied soft magnetic nano-spheres' vortex-core reversals assisted by the resonantly excited vortex-core precession. We found a novel dynamic behavior, which is the high dependence of the periodic core-reversal frequency on the strength of external AC magnetic fields as well as particle size. Although the core precession and its frequency dependence on the DC magnetic field and the particle size were explored in ref. 13, the aforementioned core reversal and its underlying physics have yet to be unveiled; thus, in the present work, we derived analytic forms of the core-reversal frequency as a function of the sphere diameter and AC field strength.

We suggest that these vortex-core-reversal dynamics' possible application to magnetic hyperthermia can provide benefits such as particle-size specificity and power efficiency. For example, magnetic nanoparticles can be guided to specific areas such as tumors, where the particles can efficiently absorb energy in the form of an AC magnetic field when its frequency corresponds to the resonant core-reversal frequency. Chemical functionalizations of bio-compatible materials such as magnetic iron oxides²⁹ can make this unique mechanism more technically available to bio-applications. In fact, because the magnetic EAR we calculated for vortex-core reversals of soft magnetic nano-spheres is of sufficiently high value and very specific to a given particle size as well as a given AC field strength, the vortex-core reversal dynamics might be a promising candidate for robust hyperthermia therapy of great power efficiency and/or entailing only the minimal intake of nanoparticles.

Several reports regarding the application of the magnetic vortex to bio-applications have been published. Kim *et al.*³⁰ experimentally demonstrated a protocol for *in vitro* cancer therapy with bio-functionalized magnetic vortex-state discs. The main mechanism is the transmission of a mechanical force induced by application of oscillating magnetic fields of a few tens of Hz to compromise membrane integrity and initiate magnetic-vortex-mediated cancer-cell destruction. Another notable implementation of magnetic hyperthermia utilizing the magnetic vortex was achieved by Liu *et al.*,³¹ who reported an enhanced therapeutic efficacy for hyperthermal tumor treatment with ferromagnetic vortex-domain nano-rings. However, from the standpoint of micro-magnetism, the two preceding studies above mentioned are in the regime of static responses that are usually controlled by a static magnetic field or an AC field of significantly low frequency range of 10 Hz–400 kHz.

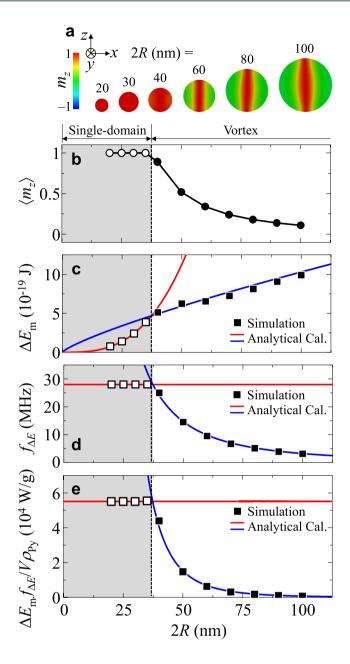


Figure 5. Energy absorption rate by resonant core reversal as function of 2R. (a) Ground-state magnetization configurations in Py nano-spheres of given diameters, as viewed in x-z plane at y = 0 nm. The core orientations are indicated by the m_z color bar. (b–e) represent $\langle m_z \rangle$, ΔE_m , $f_{\Delta E}$, and ΔE_m $f_{\Delta E}/V \rho_{\rm Py}$ as functions of 2R, as obtained from the micromagnetic simulation results (square symbols) and the numerical calculations (solid lines) of the analytical forms expressed in the text. The uniform single-domain state (gray region) and vortex state (white region) are distinguished by the vertical dotted line at 2R = 37.3 nm.

Our method, which differs completely from those two (notwithstanding their correspondent use of vortex states in magnetic nanoelements), utilizes the robust resonant dynamic characteristics of vortex-core reversals newly discovered in the present work. This work thus provides deeper insight into the fundamentals of vortex-core dynamics in soft-magnetic nano-spheres, and suggests, further, a technical new route to the achievement of efficient modes of magnetic-hyperthermia-applicable energy absorption and emission.

Methods

Micromagnetic simulation. We performed finite-element micromagnetic simulations of the magnetization dynamics of Py nano-spheres of varying diameter, 2R = 20-100 nm. For the numerical calculations of motions of the local magnetizations, we used the FEMME code (version 5.0.9)³², which utilizes the LLG equation. To prevent surface-irregularity-incurred numerical sphere-model errors, we discretized the surface of the nanosphere into triangles of roughly equal area using Hierarchical Triangular Mesh³³ as well as the inner volume into tetrahedral

meshes (mesh size \leq 5 nm) (see Fig. 1a). The magnetic parameters for the soft ferromagnetic Py material were as follows: saturation magnetization $M_{\rm s}=860\,{\rm emu/cm^3}$, exchange stiffness $A=1.3\times10^{-6}\,{\rm erg/cm}$, Gilbert damping constant $\alpha=0.01$, gyromagnetic ratio $\gamma=2\pi\times2.8\,{\rm MHz/Oe}$, and zero magneto crystalline anisotropy.

Determination of eigenfrequency of vortex-core precession. To estimate the eigenfrequency of the core precession in a nano-sphere of specific diameter, we applied a static magnetic field of 100 Oe in the +x direction for 1 μ s to the initial ground vortex state of the core aligned in the +z-direction. Then, we extracted the value of $\langle m_z \rangle$, defined as the average of $m_z (= M_z/M_s)$ over the sphere volume during the precession. The core-precession frequency was determined from the Fast Fourier Transformation (FFT) of the temporal variation of $\langle m_z \rangle$.

Analytical derivation. The core motion of the rigid vortex in a soft-magnetic nano-sphere can be expressed as ¹³

$$\dot{\Lambda} - \frac{|\gamma|}{M_s V} \Lambda \times \frac{\partial E}{\partial \Lambda} + \frac{\alpha}{V} \Lambda \times \frac{\partial F}{\partial \dot{\Lambda}} = 0, \tag{4}$$

where Λ is the unit vector of the core orientation, E the total magnetic energy, F the dissipative term, and V the volume of a sphere. The first, second and third terms correspond to the core motion, the potential energy and damping terms, respectively. The energy E is given as $E=E_{ex}+E_{ms}+E_{zeeman}$, with E_{ex} the exchange energy, E_{ms} the magnetostatic energy, and E_{Zeeman} the Zeeman energy. In order to derive the frequency of the periodic core reversal, the damping term can be neglected so that Eq. (4) simply becomes $\dot{\Lambda}+\gamma\langle m_{\Lambda}\rangle\Lambda\times\mathbf{H}=0$ with $\langle m_{\Lambda}\rangle=\frac{1}{M\cdot V}\int d\mathbf{r}(\mathbf{M}\cdot\mathbf{\Lambda})$.

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Author Contributions

S.-K.K. led the project and conceived the main idea along with J.L. J.L., M.-W.Y., M.-K.K. and J.-H.L. performed the micromagnetic simulations. J.L., M.-W.Y. and S.-K.K. interpreted the results. M.-W.Y. analytically derived eqs (1–3) for the description of vortex-core reversal and energy absorption rate. S.-K.K. wrote the manuscript along with M.-W.Y. All of the authors commented on the manuscript.

Additional Information

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