# Diffusion of a soluble protein, photoactivatable GFP, through a sensory cilium 

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#### Abstract

Transport of proteins to and from cilia is crucial for normal cell function and survival, and interruption of transport has been implicated in degenerative and neoplastic diseases. It has been hypothesized that the ciliary axoneme and structures adjacent to and including the basal bodies of cilia impose selective barriers to the movement of proteins into and out of the cilium. To examine this hypothesis, using confocal and multiphoton microscopy we determined the mobility of the highly soluble photoactivatable green fluorescent protein (PAGFP) in the connecting cilium (CC) of live Xenopus retinal rod photoreceptors, and in the contiguous subcellular compartments bridged by the CC, the inner segment (IS) and the outer segment (OS). The estimated axial diffusion coefficients are $D_{\mathrm{CC}}=2.8 \pm 0.3, D_{\mathrm{IS}}=5.2 \pm 0.6$, and $D_{\mathrm{OS}}=0.079 \pm 0.009 \mu \mathrm{~m}^{2} \mathrm{~s}^{-1}$. The results establish that the CC does not pose a major barrier to protein diffusion within the rod cell. However, the results also reveal that axial diffusion in each of the rod's compartments is substantially retarded relative to aqueous solution: the axial diffusion of PAGFP was retarded $\sim 18$-, 32 - and 1,000 -fold in the IS, CC, and OS, respectively, with $\sim 20$-fold of the reduction in the OS attributable to tortuosity imposed by the lamellar disc membranes. Previous investigation of PAGFP diffusion in passed, spherical Chinese hamster ovary cells yielded $D_{\text {CHO }}=20 \mu^{2} \mathrm{~s}^{-1}$, and estimating cytoplasmic viscosity as $D_{\mathrm{aq}} / D_{\mathrm{CHO}}=4.5$, the residual 3- to 10 -fold reduction in PAGFP diffusion is ascribed to sub-optical resolution structures in the IS, CC, and OS compartments.


## INTRODUCTION

Cilia are evolutionarily conserved subcellular organelles present on most cells of the body, and they serve many essential physiological functions, including vision, hearing, olfaction, and mechanosensation (Davis et al., 2006). The functions of many cilia remain undetermined, yet their importance is evident from the fact that mutations in genes encoding ciliary proteins give rise to devastating hereditary and often multi-organ disease, including Bardet-Biedl syndrome, Usher syndrome, combined polycystic kidney disease, and retinal degeneration (Pazour and Rosenbaum, 2002; Badano et al., 2006). Thus, a quantitative understanding of cilia construction, maintenance, and function is important for cell biology, physiology, and medicine.

All cilia are organized around a microtubule-based axoneme that is surrounded by a plasma membrane specialized with tissue-specific molecular sensors and ion channels (Fig. 1). The axoneme extends from and is anchored to basal bodies consisting of the centrioles

[^0]that organize the cytoskeleton of the ciliary axoneme and of the spindle apparatus during cell division. Recent proteomic analysis of primary cilia shows that they comprise several hundred (Blacque et al., 2005; Pazour et al., 2005) to a couple of thousand proteins (Liu et al., 2007), depending on the species. Cilia do not contain protein and membrane synthetic machinery; thus, a central problem in the study of cilia has been to determine the mode of delivery of proteins to and removal from this relatively isolated compartment.
A distinctive form of molecular motor transport, intraflagellar transport (IFT), is a hallmark of primary cilia (Rosenbaum and Witman, 2002). Originally discovered in Chlamydomonas (Kozminski et al., 1995), IFT is highly conserved in eukaryotes, involving kinesin and dyneinbased transport of large, multi-molecular particles along the microtubules of the ciliary axoneme (Rosenbaum and Witman, 2002). IFT transport has been proposed to subserve the coordinated delivery of both nonmem-brane-bound and membrane-bound molecular components to, and their removal from, the cilium, allowing it to grow and be renewed, despite its remove from the

[^1]
## A Olfactory receptor



B Hair cell


## C Kidney tubule epithelium



D Rod photoreceptor


Figure 1. Ultrastructures of a sampling of primary cilia. (A) Olfactory receptor cilia contain the molecular machinery of odorant transduction. Defects in ciliary genes lead to anosmia (Kulaga et al., 2004). (Left) Scanning EM of an embryonic rat olfactory receptor dendritic knob with multiple primary cilia (reproduced from Menco, 1997 with permission of Oxford University Press). (Right) Longitudinal section through an olfactory cilium (reproduced from Menco et al., 1997 [fig. 6] with permission from Springer Science and Business Media). Bar, $1 \mu \mathrm{~m}$. (B) Hair cells are mechanoreceptors. They generally have only one true cilium, the kinocilium, the longest structure found at the back of the ciliary bundle. Defects in ciliary genes lead to reduced hearing and deafness, such as in Usher's syndrome. (Left) Scanning EM of stereocilia from a frog saccule (reproduced from Vollrath et al., 2007 with permission). Bar, $1 \mu \mathrm{~m}$. (Middle and right) Sections through the kinocilia of teleost fish (reproduced from Flock and Duvall, 1965 with permission). (Middle) Longitudinal section through the kinocilium base. Bar, $0.5 \mu \mathrm{~m}$. (Right) Cross section showing a $9+2$ axonemal structure. Bar, $0.1 \mu \mathrm{~m}$. (C) Kidney tubule epithelial cells possess single cilia, whose function remains unknown, but it has been proposed that they serve some sensory role, such as the detection of fluid flow. Mutations in cilia genes lead to polycystic kidney disease and loss of renal function. (Left) Scanning EM of mouse kidney tubule epithelial cells showing several cilia projecting into the lumen (Pazour et al., 2000). (Middle and right) Longitudinal sections through the base of the cilia showing the basal body and centriole (reproduced from Ganote et al., 1968 with permission). (D) Photoreceptors in the retina are modified cilia that transduce light into visual signals. The OSs contain opsin molecules that absorb photons and pass the light signal down a transduction cascade that leads to channel closure in the plasma membrane. Mutations in ciliary genes lead to retinal degeneration and blindness, such as in retinitis pigmentosa. (Left) Scanning EM of a frog rod. (Middle) Longitudinal section through the CC showing the basal body and the associated centriole. Note the lamellar discs (D) of the OS and the mitochondria (M) of the IS compartments. Bar, $1 \mu \mathrm{~m}$. (Right) Cross section of the CC just distal to the basal body. Bar, $0.5 \mu \mathrm{~m}$. Images reproduced from Peters et al. (1983) with permission.
nucleus, ER, and Golgi. A hypothesis implicit in the proposed function of IFT is that both the membrane and the interior of the cilium are effectively separated from the plasma membrane and cytoplasm of the cell body. Indeed, it has been explicitly proposed that the basal bodies and the associated structures at the base of the cilium, including the transitional fibers that extend to the plasma membrane, provide either sieving mechanisms that limit the size of soluble molecules allowed to pass into and out of cilia to $\sim 10 \mathrm{kD}$ (Jensen et al., 2004; Praetorius and Spring, 2005), or serve as a gating mechanism that controls the passage of proteins between the ciliary compartment and the bulk cytoplasm (Deane et al., 2001; Trojan et al., 2008). Moreover, parallels have been drawn between the basal body complex and nuclear pore complexes in terms of control of protein
permeability (Deane et al., 2001). These proposals rest primarily on ultrastructural studies of cilia and flagella and on studies where IFT components have been genetically ablated or reduced, resulting in shortening, disorganization, or complete loss of the cilia or flagella. However, the structure of the primary cilium (Fig. 1), with its apparently patent central core, suggests that the cilium may not be isolated from the bulk cytoplasm and that a mode of transport distinct from IFT, namely diffusion, could also be available for transport of soluble proteins within cilia.
Here, for the first time, we report measurements of the diffusion of a soluble protein within a primary cilium, the connecting cilium (CC) of retinal rod photoreceptor. Photoreceptors provide both a rationale and a useful preparation for the investigation of diffusional
movement of proteins in primary cilia. A rationale comes from the massive light-dependent translocation of soluble phototransduction proteins, including arrestin ( $\sim 48 \mathrm{kD}$ ), transducin ( $\alpha$ subunit, $\sim 39 \mathrm{kD} ; \beta \gamma, \sim 46 \mathrm{kD}$ ), and recoverin $(\sim 23 \mathrm{kD})$ between the inner segment (IS) and outer segment (OS) compartments of rods (Broekhuyse et al., 1985; Philp et al., 1987; Peet et al., 2004; Strissel et al., 2005). The translocation of these proteins has been hypothesized to be governed by either IFT (Marszalek et al., 2000) or by diffusion driven by a gradient created by light-dependent changes in local binding (Nair et al., 2005; Calvert et al., 2006). Whether by IFT or by diffusion, the proteins must pass through the CC, i.e., a short segment of the whole photoreceptor sensory cilium that joins the OS and IS compartments, and which preserves the classical ultrastructure of a primary cilium with plasma membrane in close apposition to the axoneme (Fig. 1 D).

The utility of the retinal rod as a preparation for investigating diffusional movement through a primary cilium arises from the relatively large diameter of the rod cell on either side of the much narrower CC, and from two additional felicitous features of the adjoining IS and OS. The large diameter of the rod allows accurate, high resolution confocal measurement of fluorescent protein concentrations on either side of the CC (e.g., Peet et al., 2004). One of the felicitous features of rods is that the cytoplasm of the IS proximate to the CC, the myoid, is relatively unstructured, so that (as data presented here will demonstrate) it very rapidly equilibrates upon sudden, local changes in fluorescent protein concentration. In contrast, on the OS side of the CC the lamellar disc stack, which occupies most of the cross section of the rod, greatly retards the longitudinal diffusion of proteins so that concentration changes in the IS are not rapidly dissipated from the base of the OS after propagating there through the CC. It follows from these features that an experimenter, using appropriate methods of confocal microscopy, can quickly create a change in concentration of a soluble fluorescent protein in the IS, and then, by measuring the gradient of fluorescent protein across the CC and its redistribution between the two segments, estimate its apparent diffusion coefficient within the CC using Fick's first law or its embodiment in the full solution of appropriate diffusion equations.

## MATERIALS AND METHODS

## Generation of transgenic Xenopus laevis expressing photoactivatable green fluorescent protein (PAGFP)

A plasmid containing the coding sequence of PAGFP (Patterson and Lippincott-Schwartz, 2002) was provided by G.H. Patterson and J. Lippincott-Schwartz (National Institutes of Health [NIH], Bethesda, MD). Transgenic Xenopus laevis were generated using the REMI method (Kroll and Amaya, 1996). In brief, the coding
sequence of PAGFP was placed downstream from the Xenopus opsin promoter, which confined expression specifically to the rod photoreceptors (Mani et al., 2001). The plasmid was linearized with XhoI endonuclease and incubated with isolated Xenopus laevis sperm nuclei that were similarly digested. Eggs were fertilized by injection of the sperm nuclei. Transgenic embryos were identified by epifluorescent fundus imaging and allowed to develop into tadpoles and adult frogs.

## Tissue preparation

Xenopus tadpoles, stage 42-60, expressing PAGFP in rods were dark-adapted for at least 2 h before experiment. All subsequent procedures were performed under infrared illumination to minimize activation of the light receptor, rhodopsin. Tadpoles were anesthetized by bathing in $0.05 \%$ tricaine (Ethyl 3-aminobenzoate methanesulfonate; Sigma-Aldrich) and decapitated. Eyes were removed and retinas were dissected into frog Ringer's solution (in mM: $120 \mathrm{NaCl}, 2 \mathrm{KCl}, 10$ HEPES, $1.6 \mathrm{MgCl}_{2}, 10$ glucose, 0.03 EDTA, and $1.0 \mathrm{CaCl}_{2}$ ). Retinas were oriented ganglion cell side down in a $50-\mu \mathrm{l}$ bubble of Ringer's on a polypropylene sheet and sliced into strips $\sim 50-100-\mu \mathrm{m}$ wide and $100-200-\mu \mathrm{m}$ long. Slices were transferred to an imaging chamber that consisted of a $35-\mathrm{mm}$ polystyrene Petri dish, into the center of which a $5-\mathrm{mm}$ diameter hole was drilled and then covered with a No. 1 glass coverslip attached with tackywax, which formed the bottom of the chamber. A moist sponge was placed in the Petri dish and the lid was loosely applied, such that humidity prevented evaporation of the Ringer's solution while allowing free gas exchange. The chamber was then place onto the stage of the inverted confocal/multiphoton microscope. All procedures and experiments were performed at $21^{\circ} \mathrm{C}$ within 2 h of retinal dissection. Experiments were conducted in accordance with the NIH Guide for the Care and Use of Laboratory Animals.

## Multiphoton photoconversion of PAGFP and imaging in live Xenopus rods

Imaging and protein flux measurements were performed with a custom-built confocal/multiphoton microscope described previously (Peet et al., 2004; Calvert et al., 2007) that was modified by the addition of a custom LabVIEW-based software interface that allows for rapid (up to 12 Hz ) image acquisition and protocols that control the laser intensity and positioning for photoconversion of fluorescent molecules (designed and implemented in conjunction with Michael Coleman, Coleman Technologies Inc.).

Transgenic expression of proteins under the Xenopus opsin promoter results in heterogeneous protein levels across rods in a given animal's retina (Peet et al., 2004). Thus, 3-D scans of the retinal slices were performed before experiment to identify rods with sufficient PAGFP expression and that were well oriented with their long axis as close to parallel to the $x-y$ image plane as possible. The initial 3-D scans were performed with visible, confocal scanning using the 488-nm line of an argon-ion laser (model 163C; Newport Corp.) focused to the diffraction limit with a $60 \times$, 1.2 NA , water-immersion objective (Plan Apo VC; Nikon). The 3-D coordinates for the photoconversion pulse were manually selected from these initial scans using the LabVIEW interface.

PAGFP was photoconverted at the specified coordinates by multiphoton excitation from the Ti:S laser (Mai Tai HP; Newport Corp.) tuned to 820 nm and focused to the diffraction limit. The use of multiphoton excitation allowed the production of spatially well-defined fields of photoconverted molecules (Zipfel et al., 2003) and minimized the exposure of the tissue to visible light. The laser exposures ranged from 0.1 to 100 ms and 10 to 20 mW (average power). The equilibration of the photoconverted PAGFP was then monitored with serial $x-y$ scans with $488-n m$ confocal excitation that intersected the photoconversion site. Rapid focus
corrections were made before and after the photoconversion pulse to account for the measured focus difference between 820- and 488 -nm illumination caused by objective chromatic aberration (Calvert et al., 2007).

Raw images were processed using custom MATLAB (The MathWorks) routines to correct for slight field inhomogeneities inherent to the optical system and for nonlinearities in the photon detectors as follows. Full field scans with each laser in the system of solutions of fluorescein were averaged to generate image fieldflattening maps. Except where noted, no other image processing was done.

The 3-D point spread functions ( $p s f$ ) were estimated from spatial fluorescence distribution patterns obtained during 3-D scans of $0.1-\mu \mathrm{m}$ fluorescent microspheres (Polysciences, Inc.), as described previously (Calvert et al., 2007). The fluorescence profiles in $x, y$ and $x, z$ were approximated by peak normalized Gaussians with $\sigma_{x, y}=0.16$ and $\sigma_{z 1}=\sigma_{22}=0.68$ for the focused Ti:sapphire laser tuned to 820 nm (multiphoton excitation, cf. Eq. 6 in Theory section), and $\sigma_{x, y}=0.16$ and $\sigma_{z}=0.61$ for the 488-nm line of the argon ion laser.

## Online supplemental material

Although the approaches used to model the diffusional movement of PAGFP in the rod are presented in the Theory section, additional theoretical details of the methods used to obtain numerical solutions to equations, process and fit the data with theoretical curves generated by the model, as well as video clips of PAGFP diffusing in the IS and OS compartments and equilibrating throughout the rod cytoplasm are available at http://www .jgp.org/cgi/content/full/jgp.200910322/DC1.

## THEORY

In this section, we present three distinct approaches to the use of diffusion theory to characterize the movement of soluble proteins in living photoreceptors or in other elongated cells, such as many neurons that possess distinct, interconnected cytoplasmic compartments containing structural elements of variable densities. First, we present a general 3-D model applicable for determination of diffusivities within relatively homogeneous cytoplasm; this model is applied to the IS compartment. We also present two approaches that reduce the problem of diffusion between interconnected cytoplasmic compartments to 1-D; the application of these approaches depends on the hypothesis of "rapid radial equilibration," which is examined experimentally. One of these approaches is a direct application of Fick's first law to movement through the CC, whereas the second involves longitudinal or axial diffusion in and between all the interconnecting compartments and incorporates position-specific diffusivities and cross-sectional areas. The overall modeling incorporates two additional important features. The first is the description of the source of photoconverted GFP created by the Ti:sapphire laser, specified in terms of the measured multiphoton pointspread function. The second is a description of the analysis by which the confocal measurement of fluorescence intensity is transformed into local concentration (as required by the diffusion models) in cellular compartments with structurally inhomogeneous cytoplasm.

## 3-D model of PAGFP excitation and diffusional equilibration in the rod cytoplasm

A model describing the dynamic equilibration of proteins along a concentration gradient produced by the photoactivation of PAGFP in the cytoplasm of rods was developed to assess the mobility of molecules within and between rod compartments. We begin with the description of the distribution of PAGFP in the rod before, during, and after photoconversion. The photoconversion of PAGFP is treated as a rapid, irreversible change of state of the molecule from a basal, $B$, form to a photoconverted, $C$, form upon multiphoton absorption after illumination with a pulsed Ti:sapphire laser tuned to 820 nm ,

$$
\begin{equation*}
B \xrightarrow{h \vee} C . \tag{1}
\end{equation*}
$$

The time-dependent concentration distributions of PAGFP in the two forms are represented as $b(x, y, z, t)$, the basal or unconverted form of PAGFP, and $c(x, y, z, t)$, the converted form. (In the presentation that follows it is helpful to have names to distinguish the two forms; thus, we shall refer to them as "basal-PAGFP" and "con-verted-PAGFP" or the "b-form" and "c-form.") As will be explained further, these concentrations are referenced to the cytoplasm. With these considerations, the general system of equations governing the photoconversion and diffusion of PAGFP in three dimensions may be written:

$$
\begin{align*}
& \frac{\partial b}{\partial t}=D \nabla^{2} b-Q_{s}  \tag{2}\\
& \frac{\partial c}{\partial t}=D \nabla^{2} c+Q_{s}  \tag{3}\\
& Q_{s}=\alpha_{m}^{*} \gamma^{*} I^{m}(x, y, z, t) b, \quad 0 \leq t \leq \Delta T  \tag{4}\\
& =0, \quad t \geq \Delta T \\
& b(x, y, z, t)=b_{0}, \quad t \leq 0  \tag{5}\\
& c(x, y, z, t)=0, \quad t \leq 0
\end{align*}
$$

where $D$ is the diffusion coefficient of PAGFP, which is assumed to be identical for the basal and photoconverted states of the molecules, $\nabla^{2}$ is the Laplacian operator, and $Q_{s}$ is a source term that describes the generation of photoconverted molecules. The source term $Q_{s}$ embodies the intensity- and time-dependent photoconversion of PAGFP by a Ti:sapphire laser pulse of duration $\Delta T$, where $\alpha_{\mathrm{m}}^{*}$ is the effective multiphoton absorption cross section of the basal form of PAGFP, $\gamma^{*}$ is the quantum efficiency of photoconversion, and $I(x, y, z, t)$ is the photon flux density at spatial coordinate $(x, y, z)$ and time, $t$. The superscript $m$ is used to generalize the equation to include flux profiles determined by and describing multiphoton absorption (see below). Eq. 5 describes the initial concentration distributions of the two forms of PAGFP.

The distribution of the basal form of PAGFP in the rod
In addition to its role as the substrate creating the source from which the c-form of PAGFP diffuses, the b-form is of importance in several ways for the experiments and theory. First, because it is, albeit weakly, fluorescent with $488-\mathrm{nm}$ excitation, it serves to identify rods with high levels of expression of PAGFP, which are the most suitable for experimentation. Second, on the hypothesis (presented in detail below) that before photoconversion the b-form is in equilibrium with the water space of the cell, measuring its initial 3-D distribution in a rod targeted for photoconversion serves as a critical baseline for monitoring the progress toward equilibrium.

## The multiphoton point spread function and PAGFP photoconversion

The Ti:sapphire laser used to photoconvert PAGFP is focused into the sample to the diffraction limit; thus, the spatial profile of the photon flux density, $I(x, y, z)$, may be approximated as the following Gaussian function normalized to the flux density at the laser focus, $I_{0}=I(x=0, y=0, z=0)$,

$$
\begin{align*}
\frac{I^{m}(x, y, z)}{I_{0}^{m}} & =\frac{1}{(2 \pi)^{3 / 2} \sigma_{x y}^{2}} \exp \left(-\frac{1}{2} \frac{x^{2}+y^{2}}{\sigma_{x y}^{2}}\right)  \tag{6}\\
& \times\left\{\frac{a_{z 1}}{\sigma_{z 1}} \exp \left(-\frac{1}{2} \frac{z^{2}}{\sigma_{z 1}^{2}}\right)+\frac{a_{z 2}}{\sigma_{z 2}} \exp \left(-\frac{1}{2} \frac{z^{2}}{\sigma_{z 2}^{2}}\right)\right\}, a_{z i}>0,
\end{align*}
$$

where $\sigma$ 's are the standard deviations of the Gaussian profiles in the direction of the indicated axis, and $a_{z i}$ are scaling factors for the sum of two Gaussians used in the $z$ dimension.

The superscript $m$ used in Eqs. 4 and 6 is used to express the fact that the photoconversion of PAGFP, and indeed the measurement of the $I(x, y, z)$ profile, is achieved by multiphoton absorption by fluorescent molecules. Thus, the effective multiphoton excitation profile is a power law function of the photon flux profile (Zipfel et al., 2003), such that the exponent $m$ denotes the number of (infrared) photons that must be nearly simultaneously absorbed for excitation of a fluorescent molecule (cf. Calvert et al., 2007). Thus, we refer to $I^{m}(x, y, z)$ as the "multiphoton point spread function," or mppsf.

Source intensity rate parameter
In Eq. 4, the product $\alpha_{\mathrm{m}}^{\star} \gamma^{\star} I_{0}^{m}$ has the unit $\mathrm{s}^{-1}$ and thus may be treated as a composite "source intensity rate" parameter. This parameter is related to the "bleach depth" parameter of FRAP studies, but it is more general and has the distinct advantage in the context of Eqs. 2-4 that the photoconversion pulse does not need to be short relative to the diffusion of the photoconverted species (cf. Calvert et al., 2007).

## Coordinate system

The rod OS is approximately a right-circular cylinder, and other portions of the rod have circular symmetry (Fig. 2 B ); thus, it is convenient to describe 3-D positional information within the rod in cylindrical coordinates: two orthogonal coordinate axes, a longitudinal or axial $(z)$ and a radial $(r)$, and an angular coordinate, $\theta$, that describes the rotation about $z$ (Fig. 2 B). The spatial coordinate systems in Cartesian and cylindrical coordinates are:

$$
\begin{array}{ll}
\vec{r}=(x, y, z) & \text { (Cartesian coordinates) } \\
\vec{r}=(r \cos (\theta), r \sin (\theta), z) & \text { (cylindrical coordinates) }
\end{array}
$$

where $\theta$ is the azimuthal angle about the $z$ axis and $r=|\vec{r}|=\sqrt{x^{2}+y^{2}}$, with distance specified in $\mu \mathrm{m}$. The cylindrical coordinate system allows different values of $D$ for molecular diffusion along the two orthogonal axes, allowing for analysis of anisotropic movement. To implement potential difference in these diffusivities, we have included independent radial, $D_{r}$, and axial, $D_{z}$, variable diffusion coefficients in our analyses (supplemental text).

Note that the $z$ dimension of the psfintroduced above refers to the optical light propagation axis and is distinct from the $z$ dimension of the cylindrical coordinate system used in analysis of diffusion in the rod. All discussion of the model output refers to the latter cylindrical coordinate system.

## Boundary conditions (BCs)

PAGFP cannot cross the plasma membrane; the addition of 0 flux BCs at the plasma membrane is thus required to complete the system of equations:

$$
\frac{\partial c(r, z=l, t)}{\partial z}=\frac{\partial c(r, z=L, t)}{\partial z}=\frac{\partial c(r=0, z, t)}{\partial r}=\frac{\partial c\left(r=r_{0}, z, t\right)}{\partial r}=0
$$

Eq. 7 describes the case in which photoactivation is centered at $r=0$.

## Conservation of PAGFP

Eqs. 2-5, when combined with the no-flux BCs, Eq. 7, imply that that the total quantity of PAGFP in the cell, which includes both unconverted and photoconverted forms, should remain constant. Moreover, after a photoconversion exposure, given negligible bleaching by the $488-\mathrm{nm}$ scanning beam, the quantity of photoconverted PAGFP should remain constant as it redistributes throughout the cell. Testing for conservation is an important control for system and cell stability.

## Numerical solution of the system equations

To solve the system defined by Eqs. 2-7, we used the numerical methods of lines (Schiesser, 1991; Schiesser and

A


Figure 2. Coordinate systems and structural features of rod photoreceptors important for analyzing molecular motion. (A) Coordinate systems. (Top) The cylindrical coordinate system used in the 3-D model of diffusion in the OS and IS compartments. (Bottom) Coordinates used in the 1-D model of intercompartment diffusion (see Theory). (B) Transmission EM of a rod. A thin section along the central axis of a rod cell isolated from salamander retina showing the axial variation in the density of structures within the major rod compartments. OS, outer segment; IS, inner segment; E, mitochondria-filled ellipsoid; M, myoid; N, nucleus; ST, synaptic terminal; CC, connecting cilium (approximate position). The distal outer segment was truncated in this image. Bar, $10 \mu \mathrm{~m}$. (CC inset; left) Cross section of a rat rod CC showing the $9+0$ microtubule motif and the close juxtaposition of the plasma membrane, reproduced from Besharse et al. (1985) with permission. Bar, $0.3 \mu \mathrm{~m}$. (Right) Longitudinal section of a frog rod CC (reproduced from Peters et al., 1983 with permission). Bar, $1.0 \mu \mathrm{~m}$. (OS discs inset) Detail showing the stack of membranous discs orthogonal to the axis of the rod. Bar, $1 \mu \mathrm{~m}$. The isolated rod and the OS disc inset are from Townes-Anderson et al. (1985). (C) Effect of suboptical resolution structures on fluorescence intensity. The presence of structural inhomogeneities of rods in the volume of the psf result in variation in recorded GFP fluorescence, even when the aqueous concentration (green color) of the protein is uniform. Red circles in the top panel illustrate a cross section of the psfin an $x-y$ image plane of a rod that is occupied to varying degrees by different densities of subcellular structures. The bottom panel illustrates the expected variation in fluorescence $(F)$ (compare Peet et al., 2004).

Griffiths, 2009). In brief, the terms of the Laplacian ( $\nabla^{2}$ ) operator, expressed in cylindrical coordinates, were replaced by appropriate algebraic (finite difference) approximations. The resulting system of ordinary differential equations (ODEs) in time was coded in MATLAB and integrated with a sparse integrator in the MATLAB function library (ode15s). Various tests were used to determine the accuracy of the solutions, including comparison to analytical solutions of special cases of the
model (supplemental text). To compare the model output to fluorescence data, the blurring of the distribution of fluorescent molecules in the cell caused by the scanning $p s f$ was accounted for by convolving the model output with a kernel based on the measured psf (Materials and methods). This allowed the estimation of diffusion coefficients within relatively homogeneous cell compartments large enough to accommodate the "volume" of the $p s f$.

## Diffusion in the CC: alternative approaches

Some specific problems arise in the application of the general model (Eqs. 2-7) to the CC per se. First, the dimensions of the CC are below the resolution limit of the confocal microscope. Second, the CC presents a discontinuity in the cell radius $r_{0}$ between the IS and OS compartments that is difficult to accommodate in the full 3-D model. To circumvent these problems, we used two alternative theoretical approaches. These approaches rest on the assumption that PAGFP molecules equilibrate in the radial dimension of the rod much more quickly than in the longitudinal, thus reducing the problem to a single spatial dimension, the rod axis. This assumption is reasonable for small molecules in the OS of rods (Lamb et al., 1981; Olson and Pugh, 1993) and, as will be shown in Results, can be experimentally justified for PAGFP diffusion in the IS and OS compartments.

## Approach 1: Fick's law

The diffusivity of PAGFP in the CC can in principle be estimated with a straightforward application of Fick's first law:

$$
\begin{equation*}
f l u x_{\mathrm{CC}}(t)=D_{\mathrm{CC}} A_{\mathrm{CC}} \frac{\left[c_{\mathrm{IS}}(t)-c_{\mathrm{OS}}(t)\right]}{L_{\mathrm{CC}}} \tag{9}
\end{equation*}
$$

In this expression, $f l u x_{\mathrm{CC}}(t)$ is the net flux of the c-form of PAGFP into the OS through the CC at time $t$ after a photoconversion exposure in the IS, $c_{\mathrm{IS}}(t)$ and $\cos (t)$ are the concentrations of the protein in the IS and OS, respectively, at the locations adjacent to the CC, $L_{\mathrm{CC}}$ is the length and $A_{\mathrm{CC}}$ the cross-sectional area of the cilium patent to diffusion, and $D_{\mathrm{CC}}$ is the diffusion coefficient. To apply Eq. 9, the concentrations $\epsilon_{\mathrm{IS}}(t)$ and $c_{\mathrm{OS}}(t)$, as will be shown below, can be extracted with Eq. 20, and the parameters $L_{\mathrm{CC}}$ and $A_{\mathrm{CC}}$ are estimated from electron micrographs (Table I). The net flux into the OS can be estimated from the total mass of the c-form in the OS; thus, if $M_{\mathrm{OS}}(t)$ is the total mass of the c-form in the OS at time $t$, estimated from the spatially integrated fluorescence, then $f l u x_{\mathrm{CC}}(t)=\mathrm{d} M_{\mathrm{OS}}(t) / \mathrm{d} t$. Thus, we have the following relation from which $D_{C C}$ can be estimated:

$$
\begin{align*}
\frac{\mathrm{d} M_{\mathrm{OS}} / \mathrm{d} t}{\left[c_{\mathrm{IS}}(t)-c_{\mathrm{OS}}(t)\right]} & =\text { const }  \tag{10}\\
& =\frac{D_{\mathrm{CC}} A_{\mathrm{CC}}}{L_{\mathrm{CC}}}
\end{align*}
$$

An important feature of Eq. 10 is that it predicts that the ratio of two measureable time-varying quantities should be a time-independent constant.

## Approach 2: 1-D model of the rod

The assumption of rapid radial diffusion allows the photoreceptor to be modeled in one spatial dimension,

TABLE
Dimensions of Xenopus rod connecting cilia from $E M^{a}$, $\mu m$
(mean $\pm S D ; n=6$ )

| Parameter | Value |
| :--- | :---: |
| Length $^{\text {b }}$ | $0.88 \pm 0.10$ |
| Diameter IS $^{\text {c }}$ | $0.35 \pm 0.06$ |
| Diameter OS |  |

Difference in proximal and distal diameters not significant at the $\mathrm{P}=0.05$ level ( $\mathrm{P}=0.070$ ).
${ }^{\text {a Dimensions }}$ are based upon published and unpublished EM data (Besharse, J.C., personal communication).
${ }^{\mathrm{b}}$ Length is measured from the basal body to the first OS disk.
${ }^{\text {c }}$ Diameter of the IS end measured at the basal body to axoneme transition.
${ }^{\mathrm{d}}$ Diameter of the OS end measured at the point where the first bulge representing a new disk emerges.
with appropriate accommodations for the variable crosssectional area (Fig. 2, A and B). Thus, Fick's first law of diffusion in one spatial dimension may be expressed as follows (cf. Crank, 1975):

$$
\begin{equation*}
f / A=-D \frac{\partial c}{\partial z} \tag{11}
\end{equation*}
$$

where $f$ is the flux of molecules (number of molecules per unit time, $t$ ) passing through a cross section of area $A$ and, $\partial c / \partial z$ is the gradient of the diffusing species along the axial $(z)$ coordinate. Consideration of mass balance then allows one to write the rate of change of concentration in any volume element along $z$ as the spatial derivative of Eq. 11,

$$
\begin{equation*}
\frac{\partial c}{\partial t}=-\frac{\partial(f / A)}{\partial z} \tag{12}
\end{equation*}
$$

Rearrangement and substitution readily yield Fick's second law of diffusion in one spatial dimension for the case in which both the cross-sectional area and diffusion coefficient are dependent on the axial position (see supplemental text):

$$
\begin{equation*}
\frac{\partial c}{\partial t}=\frac{1}{A(z)} \frac{\partial\left(A(z) \cdot D(z) \cdot \frac{\partial c}{\partial z}\right)}{\partial z} \tag{13}
\end{equation*}
$$

Solution of Eq. 13 allows the time course of equilibration of a diffusing molecular species in the rod to be calculated, given experimental determinations of $A(z)$, $D(z)$, and $\partial c / \partial z$.

Initial and BCs
The natural physical BCs for the problem are " 0 flux" at the rod synaptic terminal and at the tip of the OS (Fig. 2 B). However, because the OS and IS differ radically in their
material density and structure, and because the IS equilibrates far more rapidly than the OS, it is convenient and warranted to impose a "pseudo boundary" at a $z$ position (identified as $z=0$ ) of our choosing. $c(z=0, t)$ may be derived from the measured fluorescence intensity at $z=0$ and used as a time-varying Dirichlet BC. These BCs are implemented as follows:

$$
\begin{align*}
& \frac{\partial c(z=L, t)}{\partial z}=0  \tag{14a}\\
& c(z=0, t)=f(t) \tag{14b}
\end{align*}
$$

Eq. 14a states that there is no flux at either end of the cell, i.e., the synaptic terminal $\left(L_{S T}\right)$ or the tip of the OS ( $L_{O S}$ ) of the rod, whereas Eq. 14b is the Dirichlet BC that states that the concentration at the specific axial position $z=0$ is a known function of time, $f(t)$.

As initial condition, the model assumes PAGFP to be completely equilibrated before the application of the photoconversion exposure and there to be none of the photoconverted form:

$$
\begin{align*}
& b(z, t=0)=b_{0} \text { for all } z, \text { and }  \tag{15}\\
& c(z, t=0)=c_{0}=0 .
\end{align*}
$$

Evidence supporting this assumption will be presented.

## Solutions

Eqs. 13-15 were solved by means of the numerical method of lines (Schiesser, 1991; Schiesser and Griffiths, 2009). Further explanation of the BCs and details of the method of solution are presented in the supplemental text.

## The relationship between measured fluorescence and PAGFP concentration

The application of alternative approaches 1 or 2 to measure the diffusion of PAGFP through the CC requires determination of the concentration gradient between the IS and OS compartments (Eqs. 10 and 13). The simplest approach to estimating the gradient would be to assume that the concentration of converted-PAGFP is everywhere proportional to the specific fluorescence attributable to that form of protein, with the same proportionality constant. This assumption is reasonable for cells such as Chinese hamster ovary ( CHO ) cells, whose cytosol is largely homogeneous (Calvert et al., 2007) but clearly invalid for rods (Fig. 2, B and C). Thus, the rod interior is to varying degrees occupied by organelles such as mitochondria in the IS or structural elements such as the discs of the OS, which exclude PAGFP. When the psf exceeds the size of such structures, a spatially varying fluorescence distribution is expected, even if

PAGFP is present at the same concentration throughout the cytosol (Fig. 2 C ) (Peet et al., 2004).

## The enhanced green fluorescent protein (EGFP)/PAGFP equilibration hypothesis

In a previous paper (Peet et al., 2004), we proposed and found support for a hypothesis about EGFP that provides a basis for resolving the problem of inferring concentrations from fluorescence in the presence of subcellular structures or organelles that cannot be resolved with confocal/multiphoton microscopy. The hypothesis proposes that EGFP equilibrates with the communicating water spaces of cells, such that at equilibrium each volume element of the cell contains a quantity of EGFP proportional to its accessible water space. Because PAGFP diffuses both in aqueous solutions and in live CHO cells with diffusion coefficients identical to those of EGFP (Calvert et al., 2007), it is reasonable to hypothesize that both the b-form and c-form of PAGFP equilibrate with the cytoplasm in the same manner as EGFP; therefore, here we generalize the name of the hypothesis to the "EGFP/PAGFP equilibration hypothesis."

The specific fluorescence $F$ recorded for $488-\mathrm{nm}$ excitation when the $p s f$ is centered at a location $\left(x_{0}, y_{0}, z_{0}\right)$ is the convolution of the psfand the concentrations of the two forms of the PAGFP:

$$
\begin{align*}
& F\left(x_{0}, y_{0}, z_{0}\right)  \tag{16}\\
& =K \iiint I\left(x-x_{0}, y-y_{0}, z-z_{0}\right)\left[\alpha_{b} \gamma_{b} b(x, y, z)+\alpha_{c} \gamma_{c} c(x, y, z)\right] d x d y d z \\
& =K I_{0} \iiint p s f\left(x-x_{0}, y-y_{0}, z-z_{0}\right)\left[\alpha_{b} \gamma_{b} b(x, y, z)+\alpha_{c} \gamma_{c} c(x, y, z)\right] d x d y d z
\end{align*}
$$

In Eq. 16, $K$ is a system constant that embodies the collection efficiency of the objective, and the optical transmission and capture of fluorescence emission by the system detectors, $\alpha_{\mathrm{b}}$ and $\alpha_{\mathrm{c}}$ are the effective molecular cross sections of the fluorescent species at the excitation wavelength, $\gamma_{\mathrm{b}}$ and $\gamma_{\mathrm{c}}$ are the quantum efficiencies of fluorescence given absorption, and $b(x, y, z)$ and $c(x, y, z)$ are the concentrations of the b-form and c-form of PAGFP in the elemental volume $d x d y d z$, understood to be a very small fraction of the $p s f$ volume. The second line of Eq. 16 restates the first in terms of the $p s f$, where $p s f(x, y, z) \equiv I(x, y, z) / I_{0}$ and $I_{0}$ is the photon flux density at the center of the $p s f$.

The efficiency $\alpha_{\mathrm{b}} \gamma_{\mathrm{b}}$ of exciting fluorescence from ba-sal-PAGFP with 488 -nm illumination is $\sim 1 \%$ that of the photoconverted state, $\alpha_{c} \gamma_{c}$ (Patterson and LippincottSchwartz, 2002). Nonetheless, the initial distribution $b(x, y, z)$ of the b-form can be measured, provided care is taken to exclude autofluorescence artifacts (Calvert et al., 2007). Before a photoconverting exposure, $c(x, y, z)$ in Eq. 16 is 0 , and in post-processing scan data, the fluorescence
attributable to the initial distribution $b(x, y, z)$ can be subtracted voxel by voxel to extract $c(x, y, z, t)$.

The EGFP/PAGFP equilibration hypothesis can be expressed in the terms of Eq. 16. Initially, before photoconversion, when only the b-form of PAGFP is present in the cell and equilibrated in the cytoplasm, the hypothesis is expressed as

$$
\begin{align*}
& F_{0}\left(x_{0}, y_{0}, z_{0}\right)  \tag{17}\\
& \equiv K \alpha_{\mathrm{b}} \gamma_{\mathrm{b}} \iiint I\left(x-x_{0}, y-y_{0}, z-z_{0}\right) b_{0}(x, y, z) d x d y d z \\
& =K \alpha_{\mathrm{b}} \gamma_{\mathrm{b}} b_{\mathrm{aq}, 0} I_{0} \iiint p s f\left(x-x_{0}, y-y_{0}, z-z_{0}\right) f_{\mathrm{aq}}(x, y, z) d x d y d z
\end{align*}
$$

whereas after a photoconversion exposure when the cell has again equilibrated, the hypothesis applied to the combined fluorescence from the b-form and c-form is

$$
\begin{align*}
& F_{\infty}\left(x_{0}, y_{0}, z_{0}\right)  \tag{18}\\
& \equiv K \iiint I\left(x-x_{0}, y-y_{0}, z-z_{0}\right)\left(\alpha_{\mathrm{b}} \gamma_{\mathrm{b}} b_{\infty}(x, y, z)+\alpha_{\mathrm{c}} \gamma_{\mathrm{c}} c_{\infty}(x, y, z)\right) d x d y d z \\
& =K\left(\alpha_{\mathrm{b}} \gamma_{\mathrm{b}} b_{\mathrm{aq}, \infty}+\alpha_{\mathrm{c}} \gamma_{\mathrm{c}} c_{\mathrm{aq}, \infty}\right) I_{0} \iiint p s f\left(x-x_{0}, y-y_{0}, z-z_{0}\right) f_{\mathrm{aq}}(x, y, z) d x d y d z .
\end{align*}
$$

In Eqs. 17 and 18, the subscripts " 0 " and " $\infty$ "represent the initial equilibrated prephotoconverted state and the final post-photoconverted state after reequilibration, respectively, and $f_{\mathrm{aq}}$ is the aqueous fraction of the volume element. The " $\equiv$ " signs in the first lines of Eqs. 17 and 18 indicate that the expression is definitional, whereas the second line embodies the equilibration hypothesis. Thus, in Eq. 17, $b_{\text {aq, }, 0}$ represents the initially equilibrated concentration of the b-form of PAGFP, whereas in Eq. 18, $b_{\mathrm{aq}, \infty}$ and $c_{\mathrm{aq}, \infty}$ are the finally equilibrated concentrations of the two forms in a volume element of pure cytosol, and $b_{\infty}(x, y, z), c_{\infty}(x, y, z)$ are the equilibrated concentrations in a partially obstructed volume element. It follows from Eq. 18 that in an equilibrated cell, the fractional water space at location $\left(x_{0}, y_{0}, z_{0}\right)$ can be estimated as

$$
\begin{aligned}
\bar{f}_{\mathrm{aq}}\left(x_{0}, y_{0}, z_{0}\right) & \equiv F_{\infty}\left(x_{0}, y_{0}, z_{0}\right) / F_{\mathrm{max}, \infty} \\
& =\frac{\iiint p f\left(x-x_{0}, y-y_{0}, z-z_{0}\right) f_{\mathrm{aq}}(x, y, z) d x d y d z}{\iiint p s f\left(x-x_{0}, y-y_{0}, z-z_{0}\right) d x d y d z}
\end{aligned}
$$

(cf. Peet et al., 2004); in the denominator of Eq. 19, $f_{\text {aq }}$ is presumed to be unity, that is, maximal fluorescence is obtained from volume elements that are "pure cytosol." Thus, $\bar{f}_{\text {aq }}$ is a volumetrically weighted average estimate of $f_{\text {aq }}(x, y, z)$, with the $p s f$ acting as the 3-D weighting function.

Consider now a time $t$ after a photoconversion exposure, and let $\Delta F(x, y, z, t)$ be the incremental fluorescence,
i.e., the measured fluorescence with the preexposure fluorescence due to the basal form of PAGFP subtracted. Then, the concentration of the c-form of the fluorescent protein in the cytosolic component of a volume element can be estimated as

$$
\begin{equation*}
\bar{c}(x, y, z, t)=\frac{\Delta F(x, y, z, t)}{I_{0} K \bar{f}_{\mathrm{aq}}(x, y, z) \alpha_{\mathrm{c}} \gamma_{\mathrm{c}}(1-\delta)}, \tag{20}
\end{equation*}
$$

where $\delta=\alpha_{b} \gamma_{b} / \alpha_{c} \gamma_{c} \approx 0.01$ and the $p s f$ volume is normalized. Two caveats for the application need to be mentioned. First, the volume of the $p s f$ sets the scale of relevant structural inhomogeneities. Second, there is no a priori guarantee that there exists in the cell a cytosolic volume the size of the psf that is not to some degree obstructed.

## Prediction of uniform scaling of fluorescence after photoconversion

Because the application of the diffusion model rests on the validity of the EGFP/PAGFP equilibration hypothesis via Eq. 20, it is worthwhile to make and test quantitative predictions of the hypothesis that do not depend on the model. The first such prediction follows readily from Eqs. 17 and 18 and relates the distribution of fluorescence $F_{\infty}(x, y, z)$ of the equilibrated c-form of PAGFP after a photoconversion exposure, with the initial fluorescence distribution $F_{0}(x, y, z)$ of the b-form:

$$
\begin{equation*}
F_{\infty}(x, y, z)=u F_{0}(x, y, z), \tag{21}
\end{equation*}
$$

with $\left.u=\left[\left(\alpha_{\mathrm{c}} \gamma_{\mathrm{c}} c_{\mathrm{aq}, \infty}+\alpha_{\mathrm{b}} \gamma_{\mathrm{b}} b_{\mathrm{aq}, \infty}\right) / \alpha_{\mathrm{b}} \gamma_{\mathrm{b}} b_{\mathrm{aq}, 0}\right)\right]$ a scalar quantity. This relationship follows because all distributions of fluorescence arising from equilibrated PAGFP must be proportional to one another, as they depend only on $f_{\mathrm{aq}}(x, y, z)$ and constants of the system and protein. A closely related prediction is that the scale factor $u$ in Eq. 21 can be obtained from the total or spatially integrated fluorescence:

$$
\begin{equation*}
F_{\mathrm{tot}, \infty}=u F_{\mathrm{tot}, 0} \tag{22}
\end{equation*}
$$

where $F_{\text {tot }}=\iiint F(x, y, z) d x d y d z$ is the integrated cell fluorescence. Confirmation of these predictions provides support of the PAGFP equilibration hypothesis, and of the estimation of $\bar{f}_{a q}(x, y, z)$ in the rod before exposure to a photoconversion stimulus, allowing $c(x, y, z, t)$ to be derived from Eq. 20.

## RESULTS

## Equilibration of photoconverted PAGFP between rod cytoplasmic compartments

Retinal slices were scanned in 3-D at 488 nm to find rod cells that had suitably high PAGFP expression levels and that were well aligned for imaging, i.e., with their longitudinal axis nearly parallel to the imaging plane (Fig. 3 A).

The central-most image plane in the $z$ dimension that contained a suitable cell was then selected as the focal plane ( $z$ coordinate) at which to photoconvert and monitor PAGFP over time (Fig. 3 B ). The $x-y$ coordi-
nates for PAGFP photoconversion were then manually selected from the image based on spatial cues, such that the photoconversion pulse would be localized to the myoid region of the IS (Fig. 3 B, red dot in the IS region),


Figure 3. Equilibration of PAGFP throughout the cytoplasm of a rod after photoactivation in the IS. (A) Infrared image of the retinal slice before experiment. The rod in which PAGFP was photoconverted is indicated by the arrowhead. (B-D) All images were obtained with the microscope operating in confocal mode, with the power of the $488-\mathrm{nm}$ argon ion laser line attenuated to $2 \mu \mathrm{~W}$ (at the sample). (B) Initial fluorescence distribution of PAGFP in the central $z$ image of the rod, intensity scaled to more clearly show the cell structure. The red dot in the center of the image is an overlay of the field intensity profile of the $p s f$, indicating the spatial position in $x-y$ and the dimensions of the multiphoton photoconversion pulse. OS, outer segment; IS, inner segment; N, nucleus; S, synaptic region. (C) The final time series image of the rod ( 25.5 min from the onset of photoconversion), where the boundary between the IS and OS was more clearly identifiable, was used to delineate regions (red polygons) over which fluorescence levels were integrated in each of the time series images. See results for details of the analysis. (D) Selected images of the fluorescence time series, starting with an image taken just before the photoconversion exposure. Photoconversion was effected by a $100-\mathrm{ms}, 20-\mathrm{mW}$ (at the sample) pulse from the Ti:S laser tuned to 820 nm . The times in subsequent images are measured from the moment of pulse initiation. The color bar to the right codes the fluorescence intensity in photon counts and is relevant to the images in C and D only. (E) The integrated fluorescence $(F)$ in the OS (Region 1 in C) and the IS (Region 2 in C), normalized to the integrated fluorescence within the respective region just before photoconversion $\left(F_{0}\right)$, as a function of time after the photoconversion pulse. The dashed line drawn at $F / F_{0}=5.3$ indicates the time-averaged magnitude of total cell fluorescence increase post-photoconversion, and thus represents the value of $F / F_{0}$ expected for all compartments upon equilibration (see Fig. 5 and Results for details). $T_{1 / 2}$ is the time required for the OS compartment to reach $1 / 2$ the $F / F_{0}$ value at equilibrium. (F) Integrated fluorescence over the entire cell image normalized to the integrated prepulse fluorescence $\left(F_{\text {tot }} / F_{\text {tot }, 0}\right)$, as a function of time from pulse onset. The total post-pulse fluorescence remains within $\sim 7 \%$ of the median post-pulse value. (A-D) Bars, $10 \mu \mathrm{~m}$. See Video 1 .
which was identified as the midpoint between the nucleus, the protuberance just distal to the synapse, and the ellipsoid, the region of lower florescence just proximal to the OS (Peet et al., 2004). Proper placement of the photoconversion pulse was confirmed after experiment from examination of the pattern of diffusing, photoactivated PAGFP. In a few cases, PAGFP was inadvertently activated in the nucleus, which was evident by rapid nuclear filling. These cells were excluded from the analysis.

## Time course of photoactivated PAGFP equilibration

To quantitatively examine the kinetics of photoactivated PAGFP equilibration throughout the entire cytoplasm, the fluorescence changes were evaluated in two subregions of the cell at $\sim 10$-s intervals, one that encompassed the OS and the other that included the IS photoconversion site, the nucleus, and the synapse (Fig. 3 C ; images just before and at several times after the photoconversion exposure are shown in Fig. 3 D; see Video 1). In this analysis, the final time course image ( 25.5 min for the cell shown in Fig. 3) was used to delineate the regions of fluorescence to be integrated because the boundary between the OS and the IS compartments was more clearly evident. The integrated florescence $(F)$ within the regions in each time course image was normalized to the integrated fluorescence in the respective regions in the prephotoconversion image ( $F_{0}$ ) and plotted as a function of time from the photoconversion pulse onset (Fig. 3 E ).

## Conservation of photoactivated PAGFP mass

To test mass conservation, the total fluorescence increase in the $x, y$ images taken after the photoactivation pulse ( $F_{\text {tot }}$ ) was normalized to the total fluorescence in the pre-conversion image ( $F_{\text {tot }, 0}$ ) and examined over the time course of the experiment (Fig. 3 F). Conservation was used as a criterion for cell integrity over the time course of the experiment, and cells failing this test were rejected from further analysis. The total fluorescence in the cell depicted in Fig. 3 increased
$5.3 \pm 0.10$-fold (mean $\pm \mathrm{SD}$ ) and varied little (SD $<2 \%$ of the time-averaged fluorescence increase), indicating that the mass of photoconverted PAGFP was stable throughout the experiment.

## Half-time of PAGFP equilibration between IS and OS

The ratio $F_{\text {tot }} / F_{\text {tot }, 0}$ provides the expected scaling factor for the fluorescence increase in any local region of the rod upon equilibration of PAGFP after a focal photoconversion exposure (Eqs. 21 and 22). For the rod of Fig. 3, $F_{\text {tot }} / F_{\text {tot }, 0,}=5.3$ (Fig. 3 E , dashed line). This value was used to estimate the half-time of equilibration of the OS after the photoconversion pulse. For the rod of Fig. 3, the time to $50 \%$ equilibration was 9.2 min (Fig. 3 E ), and it was $\sim 85 \%$ equilibrated at 25.5 min . On average, the time to half equilibration was $7.0 \pm 1.0 \mathrm{~min}$ (Table II). This result is in contrast to the time course of GFP equilibration in mouse rods after photobleaching in rod OSs at room temperature, which was reported to be complete within $\sim 3 \min \left(T_{1 / 2}, \sim 30 \mathrm{~s}\right)$ (Nair et al., 2005). This difference can be explained on the basis of the different sizes of these cells (see Discussion).

## PAGFP diffusion between compartments proximal

 to the OS-IS junctionThe diffusion of photoactivated PAGFP between IS compartments was examined by selecting smaller regions of interest (ROIs) within three major IS structures: the myoid, synaptic region, and nucleus (Fig. 4). The synaptic region equilibrated with the myoid relatively rapidly, within $\sim 5-10 \mathrm{~min}$. More precisely, the fluorescence in the synaptic region rose to a peak level approximately equal to that in the myoid within $\sim 5$ min, and then declined in parallel with the fluorescence in the myoid. This indicates that the cytoplasmic spaces of the myoid and the synaptic region are contiguous and relatively unobstructed. In contrast, the movement of PAGFP into the nucleus and OS compartments occurred much more slowly, indicating barriers to diffusion.

TABLE II
Whole cell PAGFP equilibration parameters

| Cell | $t_{1 / 2}$ equilibration | $D_{C G}$, Flux method | $D_{C C}, 1-\mathrm{D}$ rod model | $D_{O S}$, (axial) |
| :---: | :---: | :---: | :---: | :---: |
|  | min | $\mu m^{2} s^{-1}$ | $\mu m^{2} s^{-1}$ | $\mu m^{2} s^{-1}$ |
| 1 | 5 | 4.5 | 3.3 | 0.096 |
| 2 | 6.7 | 2.0 | 1.3 | 0.117 |
| 3 | 9.2 | 4.0 | 2.5 | 0.075 |
| 4 | 5.3 | 1.4 | 1.3 | 0.117 |
| 5 | nd | nd | 3.4 | 0.062 |
| 6 | 5 | 3.7 | nd | 0.074 |
| 7 | 11.5 | 1.0 | 1.4 | 0.033 |
| 8 | 9.9 | nd | 1.6 | 0.083 |
| 9 | 3.45 | nd | 2.0 | 0.050 |
| mean $\pm$ SEM | $7.0 \pm 1.0$ | $2.8 \pm 0.5^{\text {a,b }}$ | $2.1 \pm 0.3^{\text {a,b }}$ | $0.079 \pm 0.009^{\text {b }}$ |

[^2]It has been shown that GFP and its variants enter the nuclei of Xenopus photoreceptors (Peterson et al., 2003; Peet et al., 2004). The mechanism for nuclear filling is not understood. Some have posited that GFP and its variants are actively transported to the nucleus. Results shown in Fig. 4 reveal for the first time that the movement of PAGFP across the nuclear membrane is relatively slow, taking $\sim 20 \mathrm{~min}$ to equilibrate with the neighboring myoid and synapse compartments. Ongoing experiments and analyses are aimed at testing the hypothesis that this slow movement is purely passive. PAGFP transport into the nucleus provides the interesting prospect of using it as a tracer for the regulation of nuclear pore complex permeability and active protein transport across the nuclear membrane in living retinal photoreceptors, studies that are currently underway.

Test of the prediction of uniform scaling of fluorescence after photoconversion
The EGFP/PAGFP equilibration hypothesis (see Theory) predicts that upon equilibration after a photo-
conversion pulse, the fractional change in fluorescence ( $u$ ) at all locations within the cell (Eq. 21) will be the same as the fractional increase in total cellular fluorescence (Eq. 22). This prediction is borne out as shown in Fig. 5, which compares the florescence of PAGFP in the rod depicted in Figs. 3 and 4 at points along a line that intersects each of the cell's major compartments before and 50 min after photoactivation in the cell's myoid. The fluorescence varies considerably along the line in both images. This variation is interpreted to indicate differences in the aqueous fraction in the different compartments (see Theory; Eq. 19). The bottom panel in Fig. 5 B, which plots the fluorescence after internal normalization to the fluorescence of brightest fifth percentile of voxels in each original image, shows that the distribution of fluorescence is essentially the same before and after photoconversion, after sufficient time for equilibration. Moreover, the ratio of the fluorescence of the brightest voxels was $\sim 5$. 3 -fold, the same as the mean $F_{\text {tot }} / F_{\text {tot }, 0}$ in Fig. 3 F. Similar results were obtained with six cells examined in this way.


Figure 4. PAGFP diffusion in IS subcompartments. (A) The cell illustrated in Fig. 3 with fluorescence analayzed in the IS subcompartments indicated by red polygons. The red dot shows the site of PAGFP activation. (B) Selected images from the time series in Fig. 3 shown at a higher frequency and enlarged to reveal the dynamics of photoconverted PAGFP in the IS region. The color bar is relevant to images in $B$ only. (C) Integrated fluorescence in each of the regions defined in A, normalized to the integrated fluorescence of the respective regions in the prepulse image. Dashed line indicates the expected equilibrium level (see Fig. 3), which will only be reached when the slowly equilibrating OS is finally at equilibrium. (A and B) Bar, $10 \mu \mathrm{~m}$.

## Radial equilibration of PAGFP is rapid relative to

 intercompartmental transport in both the IS and OS The rates of radial equilibration in the OS and IS compartments (Figs. 6 and 7, respectively) were assessed using a "point blast-ROI scan" protocol (Calvert et al., 2007). Thus, the $x, y$ coordinates for a photoconversion pulse were selected within a confocal scan at the central $z$ plane of a rod cell, such that it would occur at the radial center of the cell. A 2-D ROI centered on the pulse site was then defined (Figs. 6 A and 7 A , green boxes). The ROI was scanned repeatedly before and after a multiphoton photoconversion pulse (Figs. 6 C and 7 C , and Videos 2 and 3). $F / F_{0}$ in smaller regions within the acquired ROI (subROIs) near the plasma membrane boundaries were then compared with $F / F_{0}$ measured for subROIs that encompassed the photoconversion sites at the radial center of the compartments (Figs. 6 B and 7 B , red boxes). Radial equilibration time was defined as the

Figure 5. The prediction of uniform scaling of fluorescence after photoconversion holds. (A) Images of the cell from Fig. 3 before and 50 min after the photoconversion (PA) exposure. The lines in the images indicate positions along which fluorescence counts were acquired and compared in B. (B) In the top panel, the raw fluorescence counts along the lines indicated in A are plotted as a function of distance relative to the IS-OS junction. The bottom panel plots the fluorescence normalized to the average of the brightest $5 \%$ of the voxels in each 3-D scan $\left(F_{0}\right)$.
time after the photoconversion pulse when the radial $F / F_{0}$ values merged with that of the photoconversion site (this definition was used because there is a much slower component of equilibration when OS intercompartmental transport is taken into consideration). The average radial equilibration time in the myoid region of the IS was $2.9 \pm 0.6 \mathrm{~s}$ ( $n=13$ cells), and in the OS it was $1.9 \pm 0.2 \mathrm{~s}$ ( $n=12$ cells). These values were not significantly different at the $\mathrm{P}=0.05$ level. Thus, PAGFP equilibrates radially within a few seconds in both the IS and OS compartments, much more quickly than the time required for equilibration between these compartments, which is on the order of tens of minutes (Fig. 3). This result justifies the assumption of rapid radial equilibration in both IS and OS compartments used in the 1-D models applied to measure PAGFP diffusion within the CC.

PAGFP diffusion is isotropic in the myoid and anisotropic in the OS
In addition to radial equilibration, axial equilibration time was assessed. SubROIs were defined at distances equal to those between the photoconversion site ROI and the radial ROIs, but at positions along the orthogonal, axial dimension of the rod (Figs. 6 B and 7 B , axial ROIs). This allowed a direct comparison of the equilibration times in the radial and axial dimensions for a given compartment. In the myoid region, the average axial equilibration time was $3.4 \pm 0.8 \mathrm{~s}$ ( $n=13$ cells), a value not significantly different from the radial equilibration time at the $\mathrm{P}=0.05$ level. To our knowledge, this is the first assessment of the directional uniformity of molecular diffusion in the IS compartment of rods. In contrast, and not surprisingly, the mean axial equilibration time of $14.5 \pm 1.2 \mathrm{~s}$ ( $n=12$ cells) in the OS compartment was nearly eightfold slower than that of the radial, presumably due to the highly tortuous axial diffusion path caused by membranous discs in the OS (cf. Fig. 2 B). It should be noted that as defined here, equilibration times are figures of merit and not directly convertible to diffusion coefficients, which must be determined by the application of an appropriate model.

Flux of PAGFP between IS and OS compartments: estimation of the diffusion coefficient in the CC
The flux of PAGFP between the OS and IS compartments was measured according to the direct application of Fick's first law (Eq. 10 and Fig. 8). Three regions (Fig. 8 A ) were selected for analysis in sequential time series images. Region 1, which encompassed the entire OS compartment, defined the area over which OS fluorescence was integrated. Regions 2 and 3, which were chosen within the IS and OS compartments in close proximity to the IS-OS junction, defined regions over which the fluorescence was averaged and to which Eq. 20 was applied to arrive at the water space-corrected relative concentration of protein (Fig. 8 B).


Figure 6. PAGFP equilibration in the myoid is isotropic and rapid. (A) $x-y$ image of the region of retinal slice at the central $z$ level of the cell that was the subject of the experiment. The region of the cell that was rapidly scanned before and after a $100-\mu s$ photoconversion pulse (the location of which is in the myoid, indicated by the red symbol) is delineated by the green box. (B) Pre-conversion scan of the region showing subregions where time courses of fluorescence change were recorded (red boxes). (C) Selected time course images showing the rapid myoid equilibration. (D) Time courses of fluorescence changes recorded from the regions shown in B. Note that the axial and radial regions change in parallel and ultimately merge with the fluorescence time course from region 1 , the site of photoconversion, at $\sim 1.5 \mathrm{~s}$. See Video 2 .

Using the radial symmetry of the OS, the time course of the flux of photoactivated PAGFP into the OS compartment, $d M_{\mathrm{OS}}(t) / d t$, was estimated from the time-dependent change in the mass of activated PAGFP detected in the $x, y$ scan plane, $M_{x y}$, as follows:

$$
\begin{equation*}
\frac{d M_{\mathrm{OS}}(t)}{d t}=\frac{\left(M_{x y}\left(t_{i+1}\right)-M_{x y}\left(t_{i}\right)\right) \cdot \frac{V_{\mathrm{OS}}}{V_{x y}}}{t_{i+1}-t_{i}} \tag{23}
\end{equation*}
$$

where $M_{x y}(t)=\iint\left(F(x, y, t)-F_{0}(x, y)\right) \cdot V_{\mathrm{vox}} d x d y, V_{\mathrm{vox}}$ is the volume of the voxel defined by the $x, y$ spatial sampling frequency, and the $p s f$ dimension in $z, V_{\mathrm{OS}} / V_{x y}$ is the ratio of total OS envelope volume and the $x, y$ scan plane volume. $V_{\text {OS }}$ was determined directly from 3-D scans of the cell as described in the supplemental text. $d M_{\mathrm{OS}}(t) / d t$ and $c_{\mathrm{IS}}(t)-c_{\mathrm{OS}}(t)$ for one cell are shown in Fig. 8 C. Eq. 10 predicts that the ratio $\left(d M_{\mathrm{OS}} / d t\right) /\left[c_{\mathrm{IS}}(t)-c_{\mathrm{OS}}(t)\right]$ will be constant over time, and this indeed appears to be the case through $\sim 6 \mathrm{~min}$ after the photoconversion pulse (Fig. 8 D ), after which the magnitude of the difference between them becomes too small to accurately measure. The average value of $\left(d M_{\mathrm{OS}} / d t\right) /\left[c_{\text {IS }}(t)-c_{\mathrm{OS}}(t)\right]$ over the initial 6 min after the photoconversion pulse for the cell depicted was $0.52 \mu^{3} \mathrm{~s}^{-1}$. Considering the average
dimensions of the CC (Table I), we obtain an axial diffusion coefficient of PAGFP in the CC of $D_{C C}=3.5 \mu^{2} \mathrm{~s}^{-1}$. Similar values were obtained from six cells (Table II).

## The diffusion coefficient of PAGFP in the myoid region of the IS

The diffusion coefficient $D_{\mathrm{IS}}$ in the myoid region of the IS was estimated using the point blast-line scan method (Fig. 9) (cf. Calvert et al., 2007), which provides much higher temporal resolution than the point blast-ROI scan method presented in Figs. 6 and 7. A brief multiphoton photoconversion pulse was applied to the radial center of the myoid, which was followed by rapid ( $\sim 1-\mathrm{KHz}$ ) line scans that intersected the photoconversion site (Fig. 9 A , left). The result is a spatiotemporal map of the relaxation of the photoconverted PAGFP within the IS cytoplasm (Fig. 9 A , right). We then applied the 3-D diffusion model described in Theory to the relaxation map varying the diffusion coefficient, $D$, which was assumed to be uniform for the radial and axial directions (Fig. 9 B ). The root mean square difference error between the model and the data was calculated (supplemental text) and plotted as a function of $D$ to arrive at the optimal estimate of $D_{\text {IS }}$ for the given cell. On average, $D_{\text {IS }}=5.16 \pm 0.62 \mu \mathrm{~m}^{2} \mathrm{~s}^{-1}$ ( $n=13$ cells).


Figure 7. Equilibration of PAGFP in the OS compartment is highly anisotropic. (A) $x-y$ image of the region of retinal slice showing the central $z$ level of the cell at which the experiment was performed. The region of the OS that was rapidly scanned before and after a $100-\mu \mathrm{s}$ photoconversion pulse (indicated by the red symbol) is delineated by the green box. (B) Prepulse scan of the region showing subregions where time courses of fluorescence change were recorded (red boxes). (C) Selected time course images showing the rapid radial and slower axial equilibration. (D) Time courses of fluorescence changes recorded from the regions shown in B. Radial positions 2 and 3 changed approximately in parallel and merge with the fluorescence time course from region 1 , the site of photoconversion, within $\sim 2$ s. The fluorescence at axial positions 4 and 5 required much longer, $>15 \mathrm{~s}$, to merge with the fluorescence of region 1 , demonstrating the high degree of anisotropy in PAGFP diffusion in the OS. See Video 3.

## The axial diffusion coefficient of PAGFP in the OS compartment

To estimate the coefficient of diffusion, $D_{\mathrm{OS}}$, of PAGFP along the axial dimension of the OS, the fluorescence levels of voxels within time course images were corrected according to Eq. 20. The corrected fluorescence, $F^{\prime}(x, z, t)$, was then averaged within a region that was confined to the OS along the radial dimension in each time course image, and $F^{\prime}(z, t=0)$ was subtracted to arrive at a spatiotemporal map of PAGFP concentration change, $F^{\prime}(z, t)$ (Fig. 10).

Predicted spatiotemporal maps of PAGFP equilibration, $F^{\prime}{ }_{\mathrm{m}}(z, t)$, in the OS compartment were then produced from the 1-D diffusion model presented in Theory (Eqs. 13-15). Time-varying Dirichlet BCs in Eq. 14 b, $F^{\prime}{ }_{\text {DB }}(t)$, were derived from the averaging of $n$ proximal $F^{\prime}(z, t)$ values from each of the time course images,

$$
\begin{equation*}
F_{\mathrm{DB}}^{\prime}(t)=\sum_{z=1}^{n} \frac{F^{\prime}(z(n), t)}{n}, \tag{24}
\end{equation*}
$$

and fitted with a sixth-order polynomial, the result of which was used in model calculations (Fig. 10 B ).

The OSs of pre-metamorphic Xenopus rods are not generally perfectly cylindrical, instead tapering prox-imo-distally along the axial dimension of the OS. To account for the tapering in model calculations, the area of cross section as a function of the rod axial position $(A(z)$ in Eq. 13) was determined with a MATLAB routine (see supplemental text). The axial diffusion coefficient in Eq. 13, $D(z)$, was assumed to be constant over all $z$.

Predicted profiles were thus calculated $\left(F^{\prime}{ }_{\mathrm{m}}(z, t)\right)$ (Fig. 10 D ) for a range of axial diffusion coefficients and compared with $F^{\prime}(z, t)$. $D_{\text {Os }}$ for PAGFP was determined as the value that produced the smallest $E_{R M S}$ between model prediction and data. For the rod depicted in Fig. $10, D_{\mathrm{OS}}=0.075 \mathrm{~m}^{2} \mathrm{~s}^{-1}$ produced the model output that best fit the data. $D_{\mathrm{OS}}$ values obtained from this and other cells are given in Table II.

## Alternative approach to estimating $D_{\mathrm{CC}}$

The 1-D diffusion model with variable cross-sectional area and variable $D$ (Eqs. 13-15) offers an alternative approach to quantifying the diffusion coefficient of PAGFP in the CC. The present analysis is similar to that


Figure 8. Flux of PAGFP through the CC. (A) Pre-photoconversion image of a rod showing the regions where fluorescence was monitored over time. (B) Relative concentration of photoactivated PAGFP in the IS (region 2) and OS (region 3) after an IS photoconversion pulse. (C) The concentration gradient (red line, left ordinate) and flux (blue line, right ordinate) of PAGFP between IS and OS compartments. (D) The "flux constant" (Eq. 10) as a function of time. Gray line indicates the average value over the first $6.5 \mathrm{~min}(0.52$ $\mu \mathrm{m}^{3} \mathrm{~s}^{-1}$ ), after which the $c_{\mathrm{IS}}-c_{\mathrm{OS}}$ difference fell below $\sim 10 \%$ of its original magnitude and became unreliable.
for the axial diffusion of PAGFP in the OS outlined in the previous section, except that the region defined for analysis was extended to include the portion of the cell just proximal to the interface between the IS and OS compartments, thus including the length of rod containing the CC (Fig. 11 A ). The predicted $F^{\prime}{ }_{\mathrm{m}}(z, t)$ was then calculated with diffusion coefficients that varied along the axial dimension of the rod. Three zones of differing diffusion coefficients used in the model, $D_{\mathrm{M}}(z)$, were defined as follows:

$$
\begin{array}{ll}
D_{\mathrm{M}}(z)=D_{\mathrm{IS}}, & z<z\left(C C_{l}\right) \\
D_{\mathrm{M}}(z)=D_{\mathrm{CC}}, & z\left(C C_{l}\right) \leq z \leq z\left(C C_{L}\right)  \tag{25}\\
D_{\mathrm{M}}(z)=D_{\mathrm{OS}} & z>z\left(C C_{L}\right),
\end{array}
$$

where $D_{I S}$ is the diffusion coefficient of PAGFP in the IS, the average value determined from point blast-line scan experiments in the IS described in Fig. 9 was used, $D_{\mathrm{CC}}$ is the axial diffusion coefficient of PAGFP in the CC, $D_{\mathrm{Os}}$ is the diffusion coefficient of PAGFP in the OS determined for the specific cell under investigation as shown in Fig. 10, and $z\left(C C_{l}\right)$ and $z\left(C C_{L}\right)$ are the axial boundaries of the CC. $F_{m}(z, t)$ was calculated for a range of $D_{\mathrm{CC}}$, and the best value of $D_{\mathrm{CC}}$ was considered to be that which produced the minimum value of $E_{R M S} . D_{\mathrm{CC}}=$ $2.5 \mu^{2} \mathrm{~s}^{-1}$ provided the best fit for the rod depicted in Fig. 11. Values for $D_{\mathrm{CC}}$ from this and other cells using this method are presented in Table II.

Summary: reduction of diffusion in the rod's compartments A useful summary of the results can be made by comparing the effective diffusion coefficients estimated for

PAGFP in the different rod compartments with that measured in aqueous solution and in the relatively unstructured, passed CHO cells. A useful metric capturing the comparison is the "fold-reduction" of the effective diffusion coefficient $D_{\text {eff }}$ from that in aqueous solution: ( $D_{\text {aq }} / D_{\text {eff }}$ ) (Table III).

## DISCUSSION

Quantitative characterization of the steady-state distributions, concentrations, and movements of soluble proteins in living cells is a goal of broad importance for understanding many cellular functions, including cell signaling kinetics and protein renewal mechanisms. Complex polarized cells such as sensory receptors pose many problems to achieving such characterization, for their subcellular "compartments" are differentiated ultrastructurally and often connected by or terminated in narrow constricted structures, such as cilia or axons, whose diameter is near or below the resolution of light microscopy (Figs. 1 and 2). Using the Xenopus rod photoreceptor as a model system and PAGFP as a reporter, we have shown how many of the problems can be addressed and in particular have, for the first time, measured the diffusion coefficient of a protein in a primary cilium, as well as in the other major compartments of a highly polarized cell, and also the overall time for the protein concentration to equilibrate within and between compartments.

## The CC poses a modest barrier to protein diffusion

 The basal body-axoneme complex has been compared with the nuclear pore complex in terms of regulating

Figure 9. Estimation of the diffusion coefficient of PAGFP in the myoid. (A; left) $x-y$ image of the region of retinal slice showing the $z$ level of the cell on which the experiment was performed. The region of the myoid that was exposed to a $100-\mu \mathrm{s}$ photoconversion pulse is indicated by the red symbol. The green line indicates the location of $2-\mathrm{KHz}$ line scans that intersected the photoconversion site. (Right) The spatiotemporal fluorescence map of the dissipation of the photoconverted PAGFP from the photoconversion site. (B) Fluorescence profiles of selected line scans after normalizing to the amplitude of the first post-pulse line scan recorded ( 1.176 ms ). The red lines are the result of model calculations with optimal $D$. (C) Root mean square (RMS) error calculated from the difference between line scan fluorescence and model prediction for indicated $D$. Minimal $E_{\text {RMS }}$ was achieved with $D=5 \mu \mathrm{~m}^{2} \mathrm{~s}^{-1}$.
protein access to the cilium (Deane et al., 2001), and it has been proposed that the permeability of the basal body-axoneme complex to protein transport may be regulated in a signal-dependent manner (Wolfrum et al., 2002). The 36 -fold reduction in the effective diffusion coefficient of PAGFP in the CC relative to aqueous solution (Table III) provides the first direct evidence that these structures do indeed impede soluble protein movement between the cell body and the cilium, and leaves open the possibility of signal-dependent control of cilium permeability. However, because $D_{\mathrm{CC}}$ is only twofold smaller than $D_{\text {IS }}$ (Table III) and PAGFP diffusion is more rapid in the IS than anywhere else in the cell, it is difficult to posit that the CC constitutes a highly distinctive barrier to protein movement.

The most distinctive feature of the CC seen in electron micrographs that would be expected to impact protein movement is the $9+0$ microtubule axoneme and associated structures, but the core of the axoneme appears to offer an unobstructed path for diffusion (cf. Fig. 2). Although the axonemal components will reduce the effective cross-sectional area available for diffusion, as the maximal diameter of each microtubule
doublet is $\sim 37 \pm 1 \mathrm{~nm}$ (Rosenkranz, 1977), the entire axonemal structure reduces the effective cross-sectional area by only $\sim 7 \%$, not nearly enough to account for the 36 -fold reduction from $D_{\text {aq. }}$. It remains possible that the cross-sectional area of the CC available for diffusion of PAGFP is much smaller than apparent from transmission electron micrographs (EMs). Electron tomographic examination of the centrosomal region of chondrocyte cilia (Jensen et al., 2004) shows it to be

TABLE III

| Magnitude of reduction of $D_{\text {aq, PAGFP }}$ within rod compartments |  |  |
| :--- | :---: | :---: |
| Cell/compartment | $D_{\text {eff }}$ | $D_{\mathrm{aq}} / D_{\text {eff }}$ ratio |
|  | $\mu m^{2} s^{-1}$ |  |
| CHO cell cytoplasm |  |  |
| CC | 20 | 4.5 |
| IS | 2.5 | 36 |
| OS | 5.2 | 17 |

The aqueous diffusion coefficient of EGFP, $D_{\text {aq, EGFP, }}$ was reported previously to be 87 (Swaminathan et al., 1997; Brown et al., 1999; Potma et al., 2001) and $91 \mathrm{~mm}^{2} \mathrm{~s}^{-1}$ (Calvert et al., 2007). $D_{\text {aq, PAGFP }}$ was reported to be $89 \mu^{2} \mathrm{~s}^{-1}$ (Calvert et al., 2007).
${ }^{\text {a }}$ Calvert et al. (2007).


Figure 10. Estimation of the axial diffusion coefficient of PAGFP in the OS compartment. (A) The spatiotemporal profile of activated PAGFP filling of the OS was obtained from the region bounded by the red box. (B) The Dirichlet BC used in calculations was defined by fitting $F^{\prime}{ }_{\mathrm{DB}}(t)$ for $n=5$ pixels in $z$ (filled circles) with a sixth-order polynomial (red line). (C) The spatiotemporal profile of activated PAGFP. (D) Eqs. 13-15 were solved with varying $D$ to find the best approximation of the spatiotemporal profile in C. Shown is the model profile, $\quad F_{\mathrm{m}}^{\prime}(z, t)$, obtained from the solution of best fit. The thick black lines in C and $D$ represent the Dirichlet boundary. (E) The data profile was subtracted from the model profile obtained for each value of $D_{\mathrm{OS}}$ to determine the difference error. Shown is the difference for $D=0.075 \mu^{2} \mathrm{~s}^{-1}$. (F) RMS error values plotted as a function of $D$.
crowded with fine filamentous material, transitional fibers, and vesicles. Moreover, the lumen of the basal bodies contains large vesicles and electron-dense "plugs" that may occlude or substantially reduce the cross-sectional area available for diffusion. However, as we now discuss, retarded diffusion elsewhere in the rod suggests that more general principles of differentiated cells are at play.

Protein diffusion in the IS is substantially retarded
The IS comprises the region of the rod between the ellipsoid and the nucleus. This region contains the major protein- and lipid-synthesizing and -degrading machinery of the rod and is expected to be homologous to similar regions in most cell types. Diffusion
in the IS of PAGFP is isotropic (Fig. 9) and faster than in any other region of the $\operatorname{rod}\left(D_{\mathrm{IS}}=5.2 \mu \mathrm{~m}^{2}\right.$ $\mathrm{s}^{-1}$ ). Nonetheless, PAGFP diffusion is substantially retarded in the IS, being 18 -fold lower than in aqueous solution and fourfold below that in CHO cells (Table III).

Axial diffusion of PAGFP in the OS is retarded 50-fold more than predicted by geometry
The effective coefficient for axial diffusion of PAGFP in the OS, $D_{\mathrm{OS}}$, is reduced 1,125 -fold from that in aqueous solution (Table III). The OS comprises densely stacked discs, paired membrane bilayers spaced at $\sim 30 \mathrm{~nm}$, which greatly reduce the patent cross-sectional area, so that most paths for axial diffusion are highly tortuous


Figure 11. Estimation of the axial diffusion coefficient of PAGFP within the CC using the 1-D model. (A) Region over which the fluorescence was averaged in the radial dimension from each time course image to produce the spatiotemporal fluorescence profile shown in C. Note that in this case the region begins at an axial position just proximal to the CC, $z(\mathrm{cc})$. (B) To produce the Dirichlet BC the proximal five pixels in the region were averaged and fitted as described in Fig. 10. (C) Spatiotemporal map of fluorescence changes along the axial extent of the region shown in A. (D) Model prediction $F^{\prime}{ }_{\mathrm{m}}(z, t)$ that best fitted the data. Eqs. 13-15 were solved with spatially varying $D(z): D(z=$ IS $), 5.2 \mu \mathrm{~m}^{2} \mathrm{~s}^{-1}$; $D(z=$ OS $), 0.08 \mathrm{~mm}^{2} \mathrm{~s}^{-1} ; D(z=$ CC ) was varied to obtain the best fit of the model to the data. The thick black lines in C and D represent the Dirichlet boundary constraint. (E) Area of cross section versus axial distance profile, $A(z)$, for the region of the cell analyzed and which was used in Eq. 13 to calculate model profiles; note the sharp drop in $A$ at the CC. The red symbols denote the transitions between IS and CC $\left(z\left(\mathrm{CC}_{1}\right)\right.$; left symbol) and the CC and OS ( $z\left(\mathrm{CC}_{L}\right)$; right symbol), and define the ranges over which $D(z)$ values described in D were applied. (F) RMS error values plotted as a function of $D_{\mathrm{CC}}$.
(Fig. 2) (cf. Rosenkranz, 1977). The impact of tortuosity on $D_{\text {OS }}$ may be predicted from a straightforward relation (Lamb et al., 1981):

$$
\begin{equation*}
\tau=\frac{F_{\mathrm{V}}}{F_{\mathrm{A}}} \tag{26}
\end{equation*}
$$

Here, $F_{\mathrm{V}}$ is of the fraction of the OS volume occupied by the discs, and $F_{\mathrm{A}}$ is the fraction of the cross section accessible to molecular diffusion (Lamb et al., 1981; Olson and Pugh, 1993). $F_{\mathrm{V}}$ has long been estimated to be $\sim 0.5$ (Rosenkranz, 1977; see also Peet et al., 2004), although a recent cryoelectron microscopy study of mouse rods suggests it could be as low as 0.3 (Nickell et al., 2007). $F_{\mathrm{A}}$ is determined by the gap between the discs and the plasma membrane ( $10-20 \mathrm{~nm}$ ), and by
the incisures, infoldings of the plasma membrane that invaginate the discs (Fig. 12). On average, a frog disc contains 27 incisures with lengths of $2.7 \mu \mathrm{~m}$ (Tsukamoto, 1987) and gaps of $\sim 10 \mathrm{~nm}$ (according to measurements made in salamander; Olson and Pugh, 1993). Accordingly, the area of a $7-\mu \mathrm{m}$ diameter frog rod OS available for axial diffusion is $\sim 1.0 \mu^{2}, 2.6 \%$ of the OS cross-sectional area. Thus, Eq. 23 gives $\tau=0.5 / 0.026$ $\sim 20$, and so predicts that tortuosity alone should reduce axial PAGFP diffusion 20 -fold from $D_{\text {aq. }}$. If the incisures were inaccessible to PAGFP diffusion, Eq. 26 would yield $\tau \sim 40$. Removing the contribution of tortuosity, we are left with an unaccounted 28 - to 56 -fold reduction in $D_{\mathrm{OS}}$ from $D_{\mathrm{aq}}$, and 6- to 12 -fold reduction from $D_{\text {CHO }}$ (Table III).

Mechanisms underlying the retarded diffusion of PAGFP in the rod
GFP and its variants, particularly EGFP, have been used in benchmark studies of protein diffusion in cellular aqueous compartments (for review see Verkman, 2002; see also Dix and Verkman, 2008). We have recently shown that the GFP variant used here, PAGFP, is indistinguishable from EGFP with respect to its diffusion in aqueous solutions of varied viscosity and in CHO cells, but provided substantially superior performance with respect to signal/noise and light load (Calvert et al., 2007). The diffusion coefficient of GFP variants in aqueous compartments of cultured cells is generally reduced approximately three- to fivefold from its value in water or physiological saline (Swaminathan et al., 1997; Partikian et al., 1998; Dayel et al., 1999; Calvert et al., 2007). It is thus striking that PAGFP diffusion is much more retarded in the aqueous compartments of rods (Table III) than in those of most cells previously investigated (for exceptions, see Elowitz et al., 1999; Konopka et al., 2009), and calls for some explanation.

Retarded diffusion of macromolecules, including GFP variants, in aqueous compartments of cells has been ascribed primarily to four factors: fluid-phase cytoplasmic viscosity, macromolecular crowding, binding interactions, and hydrodynamic boundary effects (Hou et al., 1990; Kao et al., 1993; Minton, 1997; Luby-Phelps, 2000; Verkman, 2002; Dix and Verkman, 2008; Zhou et al., 2008). The viscosity of the aqueous cytoplasm is governed by the concentration of small solutes and organizing effects of macromolecules on water (Clegg, 1984; Parsegian and Rau, 1984). Crowding reduces the volume fraction available for translational diffusion and thus the number of possible paths available to a diffusing molecule. Binding interactions include all inelastic collisions of the diffuser with nonsolvent particles and intracellular surfaces (e.g., ER and SER) and microfilaments. Retarding hydrodynamic friction occurs when a significant fraction of the paths available to the diffuser are put in close contact with solvent that is less mobile. (These factors are not completely distinct; see the citations just given.)

The retardation of PAGFP diffusion by several of these factors could be greater in photoreceptors than in previously investigated cells (e.g., CHO cells). Photoreceptors may use a relatively high density of cytoskeletal elements to maintain their highly structured, polarized morphology. Crowding by macromolecules may be exceptionally high in the cytoplasm of the IS and OS: interferometric measurements of cytoplasm, which probe particulate density, indicate that the refractive index of the OS is 1.41 (Sidman, 1957) and the core of the myoid region of cones has an index of 1.42 (Rowe et al., 1996). These values contrast with those of cultured mammalian cells, with reported refractive indices in the 1.36 to 1.37 range (Lanni et al., 1985). The high refractive index in the OS is due to dense packing of lipids and phototransduction


Figure 12. Morphology of OS discs. (A) Enface transmission electron micrographs of discs in the OSs of the bull frog Rana catesbeiana. Bar, $1.5 \mu \mathrm{~m}$. Discs in rod photoreceptors have a scalloped morphology formed by infoldings called "incisures" that penetrate deep into their radial dimension. $R$, red rod; $G$, green rod. Image reprinted from Tsukamoto (1987) with permission from Elsevier. (B) Schematic of half of a rod OS, showing two disc membranes (DM) and the plasma membrane (PM) architecture. Average measurements used to calculate the patent area of cross section available for axial diffusion of molecules are indicated.
proteins, and in the IS it may reflect denser packing of protein-synthetic machinery needed to support the high turnover of phototransduction components in the OS, which, in the case of frogs, renews $\sim 2 \%$ of its large complement of proteins daily (Young, 1967). Finally, the lamellar membranes of the OS and the putative high density cytoskeletal components offer an increased surface area that may retard the diffusion of PAGFP by weak binding interactions or hydrodynamic friction.
Strong binding interactions between PAGFP and subcellular structures do not appear to be involved because in the cells examined, the diffusion coefficients in the CC and OS did not correlate with the concentration of expressed PAGFP, which varied more than 200 -fold in the rods investigated (see supplemental text). Another possible mechanism for slowed diffusion of PAGFP is
self-crowding. However, the highest expression level in the cells examined was $\sim 100 \mu \mathrm{M}$, at least 10 -fold below the theoretical threshold for crowding effects (see supplemental text).

The value of $D_{\mathrm{OS}}\left(0.079 \mathrm{~mm}^{2} \mathrm{~s}^{-1}\right)$ reported here for PAGFP differs considerably from the value ( $3.3 \mu \mathrm{~m}^{2} \mathrm{~s}^{-1}$ ) recently reported for EGFP expressed in Xenopus rods (Wang et al., 2008). Several factors may explain this discrepancy, including the harsh conditions used to isolate the cells and an inadequate description of the FRAP bleach pattern. The manipulations used by Wang et al. (2008) to isolate, immobilize, and permeabilize the cells could cause cell swelling (increasing the water space) and depolymerization of cytoskeleton components (decreasing crowding). Our approach strictly maintains physiological intactness of the photoreceptors, as we imaged only rods that were in retinal slices and maintained normal morphology. The diffusion model applied by Wang et al. (2008) assumes uniform bleaching along the entire width of the rod OS, which was fixed to the coverslip. However, both bleaching and scanning were performed at a single focus level with a 1.3-NA oil-immersion objective. The radius of the diffraction-limited illumina-
tion volume along the axis of focus (the Rayleigh or Abbe limit) is $r=\lambda / \mathrm{NA}^{2} \sim 0.3 \mu \mathrm{~m}$ at 488 nm . Given an average Xenopus rod diameter of $6-7 \mu \mathrm{~m}$, a substantial fraction of the OS width would have been minimally bleached; therefore, the fluorescence recovery signals were likely much sped up by unbleached molecules diffusing radially into the scan plane from out of focus regions (cf. Figs. 6, 7, and 9).

## Could advection due to active transport within the CC contribute to soluble PAGFP movement into the OS?

 An alternative mechanism to diffusive transport of PAGFP to the OS compartment that warrants consideration is transport by advective flow of cytoplasm that may be generated by motor-based transport carriers. At a concentration of $\sim 3 \mu \mathrm{M}$ in the OS, rhodopsin is the most abundant protein in the rod and, given the well-established rate of renewal of the OS disc membranes ( $\sim 14 \mathrm{~d}$ in Xenopus), can be estimated to be transported to the OS compartment via post-Golgi vesicles at a maximal rate of approximately one $\sim 300-\mathrm{nm}$ diameter vesicle per second. It is controversial whether these vesicles transit the CC to reach the OS, or rather

Figure 13. Impact of changes in areas of cross section on equilibration kinetics: predictions from the diffusion model. (A) Idealized cells with the geometry of frog or mouse rods and for an idealized ciliated cell for which equilibration time courses were modeled by solving Eqs. 13-15. The rod ISs or the cell body (CB) were initially uniformly filled with diffusing substance (black), and the OS and cilia were empty. Equilibration after some period of time is indicated by uniform gray in all compartments. Arrow thickness denotes relative speed of equilibration (see B-D). (B) Time courses of equilibration into rod OS compartments. The lengths of each compartment were: IS, $5 \mu \mathrm{~m}$; CC, $0.8 \mu \mathrm{~m}$; OS, $25 \mu \mathrm{~m}$. The CC had the same diameter in all cases, $0.4 \mu \mathrm{~m}$ (average diameter from Table I). A range of rod IS and OS diameters were modeled, including $7 \mu \mathrm{~m}$, representative of frog rods, and $1.4 \mu \mathrm{~m}$, based on the most recent measurements of mouse rod dimensions (Daniele et al., 2005). In all cases, $D_{\mathrm{IS}}=5 \mu \mathrm{~m}^{2} \mathrm{~s}^{-1}, D_{\mathrm{CC}}=2 \mu \mathrm{~m}^{2} \mathrm{~s}^{-1}$, and $D_{\mathrm{OS}}=0.1 \mu \mathrm{~m}^{2} \mathrm{~s}^{-1}$. The mass in the OS normalized to the equilibrated OS mass is plotted. (C) Dependence of the $T_{1 / 2}$ of equilibration on the ratio of CC and IS-OS radii. Line is drawn through the points. (D) Time course of cilium equilibration. Ciliated cells ( $10-\mu \mathrm{m}$ long cell body and $5 \mu \mathrm{~m}$ in diameter, possessing a cilium $0.4 \mu \mathrm{~m}$ in diameter and varied length) were modeled. The mass of the diffusing substance in the cilium normalized to the equilibrated mass is plotted for cilia of indicated length.
fuse with the plasma membrane in the IS near the cilium transition zone and are carried to the OS via IFT. However, if the mechanism of transport of rhodop-sin-laden membrane were shown to be motor-based movement of vesicles through the core of the CC, the $\sim 300$-nm diameter vesicles would be large enough to occlude most of the CC lumen, and could possibly produce a peristaltic flow of cytoplasm toward the OS. To examine the possibility of such an "advective" transport of PAGFP, the 1-D model of diffusion in the rod cell described in Theory was extended to include an advective term. This advection/diffusion model predicts that the steady-state PAGFP concentration in the OS compartment would exceed that in the IS compartment by $>30 \%$ (see supplemental text). Contrary to this prediction, in none of the cells examined in the present paper, nor in the large population expressing EGFP examined in a previous paper (Peet, et al. 2004), did the steady-state concentration of PAGFP or EGFP in the OS compartment exceed that of the IS. It is thus unlikely that advection plays a significant role in the transport of soluble proteins between rod photoreceptor compartments.

## Impact of variation in cell dimensions on the time course of soluble protein equilibration

Although diffusivities govern the local movements of protein in the cells, the overall time to equilibrate is greatly affected by cellular and subcellular dimensions. Consider the cases of frog and mouse rod photoreceptors. The CC of frog and mouse rods are the same diameter, yet the diameter of the cells are very different: frog rods are on average $\sim 7 \mu \mathrm{~m}$ in diameter, whereas those of mice are $\sim 1.4 \mu \mathrm{~m}$. As a consequence, the frog rod cilium involves an $\sim 330$-fold reduction in the cross section available for diffusion, whereas the corresponding reduction in the mouse rod is only $\sim 19$-fold. In a threecompartment simulation, these differences resulted in equilibration times that differ approximately sevenfold (Fig. 13).

We similarly examined the equilibration time predicted for a ciliated epithelial cell where the cilium diameter is constant but attached to a large cytoplasmic reservoir, as, for example, for an olfactory cilium (cf. Fig. 1). Assuming the diffusion coefficients of the cell body and the cilium to be equal and $\sim 5 \mu \mathrm{~m}^{2} \mathrm{~s}^{-1}$, the equilibration was remarkably fast (Fig. 13 D). Although the equilibration time varied significantly with cilium length, equilibration half-times were $<1 \mathrm{~min}$ for lengths up to $20 \mu \mathrm{~m}$ (Fig. 13 D ), suggesting that diffusion could be a viable means of soluble protein transport into all primary cilia.

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    Abbreviations used in this paper: BC, boundary condition; CC, connecting cilium; CHO, Chinese hamster ovary; EFGP, enhanced green fluorescent protein; EM, electron micrograph; IFT, intraflagellar transport; IS, inner segment; ODE, ordinary differential equation; OS, outer segment; PAGFP, photoactivatable green fluorescent protein; ROI, region of interest.

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[^2]:    ${ }^{a}$ Difference between $D_{\mathrm{CC}}$ obtained by flux method and that obtained from the 1-D rod model was not significant $(\mathrm{P}=0.21)$.
    ${ }^{\mathrm{b}}$ Differences between $D_{\mathrm{CC}}$ measured by either method and $D_{\mathrm{OS}}$ were significant at the $\mathrm{P}=0.01$ level.

