

1 **Efficient Coding in Motor Planning**

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9 **Abstract**

10 A paramount challenge for the brain is to precisely model the world and control behavior within the  
11 confines of limited encoding capacities. Efficient coding theory posits a unified framework for  
12 understanding how neural systems enhance encoding accuracy by tuning to environmental statistics.  
13 While this theory has been thoroughly explored within the perceptual realm, it is less clear how efficient  
14 coding applies to the motor system. Here, we probe the core principles of efficient coding theory through  
15 center-out reaching tasks. Our results reveal novel sequential effects in motor planning. Specifically,  
16 current movements are biased in a direction opposite to recent movements, and movement variance  
17 increases with the angular divergence between successive actions. These effects are modulated by the  
18 variability within the motor system: a larger repulsive bias is observed when movements are performed  
19 with the nondominant hand compared to the dominant hand, and in individuals exhibiting higher motor  
20 variance compared to those with lower variance. These behavioral findings align with the predictions of  
21 an efficient coding model, suggesting that the motor system rapidly adapts to the context to enhance  
22 accuracy in motor planning.

## 23 Introduction

24 Our experiences shape the way we perceive and interact with the world. A fundamental mechanism that  
25 contributes to this adaptive behavior is efficient coding, a unified theory positing that neural systems  
26 allocate limited resources to optimally encode information from the environment<sup>1-4</sup>. For instance, the  
27 system may preferentially allocate more coding resources to stimuli that appear more frequently and  
28 fewer resources to those that are rarer, thereby maximizing overall accuracy<sup>5,6</sup>.

29  
30 The principle of efficient coding has been extensively examined in perceptual systems<sup>7-9</sup>. The key  
31 assumption of efficient coding is that encoding accuracy for a stimulus increases when it is closer to the  
32 prior expectation and decreases as it deviates from this prior. This non-uniform resource allocation can  
33 introduce systematic perceptual distortions, constrained by the prior distribution<sup>10</sup>. This model  
34 successfully explains how environmental statistics shape the systematic biases in various visual tasks,  
35 including orientation, location, and color perception<sup>11,12</sup>. Moreover, efficient coding has also been applied  
36 to understand sequential biases in visual perception that are induced by trial-by-trial updating of the  
37 encoding resource<sup>13</sup>. Beyond visual perception, efficient coding explains the prioritization of certain  
38 sounds over others based on environmental relevance and frequency of occurrence<sup>4</sup>. Additionally,  
39 efficient coding principles extend to the processing of abstract information. For instance, the biases and  
40 variability associated with encoding subjective values are modulated by the statistical context in a manner  
41 that improves accuracy and reduces redundancy<sup>14,15</sup>.

42  
43 While efficient coding is generally applicable to perceptual systems, it remains less clear whether those  
44 principles can be applied to other systems. For example, organisms must plan their movements rapidly  
45 and precisely for survival. However, motor planning involves computations in high-dimensional spaces,  
46 which can demand substantial computational resources<sup>16-18</sup>. As such, it is plausible to propose that the  
47 motor system adapts to environmental statistics by adhering to efficient coding principle, which, in turn,  
48 enhance movement accuracy.

49  
50 To examine whether motor planning follows the principles of efficient coding, we examined experience-  
51 dependent modulations in reaching. As mentioned above, efficient coding theory assumes that neural  
52 systems adapt to the environmental statistics by allocating resources preferentially to more probable  
53 stimuli or movements (Fig 1c)<sup>1,15</sup>. This can be achieved by sharpening the tuning curve of the units around  
54 the prior and/or modifying the density of the tuning units over space. In either case, a movement

55 direction aligned with the prior will be more precisely encoded, and the variability in movement will  
56 escalate when its direction diverges from the prior (Fig 1d).

57

58 Moreover, the differential allocation of coding resources across the space will introduce an encoding  
59 bias<sup>10,11</sup>. In visual perception, efficient coding leads to aftereffects, where perception is biased in the  
60 direction opposite to previously viewed stimuli<sup>19</sup>. This mechanism reduces redundancy in sensory  
61 representation and enhances sensitivity to new information. Similarly, when encoding a specific  
62 movement direction, the efficient coding model suggests that the encoding resources are imbalanced on  
63 the two sides of the movement direction. As a result, the population distributional response to this  
64 movement direction will also be asymmetric, with a higher encoding accuracy on the prior side and a flat  
65 tail pointing away from the prior mean (Fig 1e). As such, the mean direction encoded by the neural  
66 population will be biased in a direction opposite the prior mean (Fig 1f).

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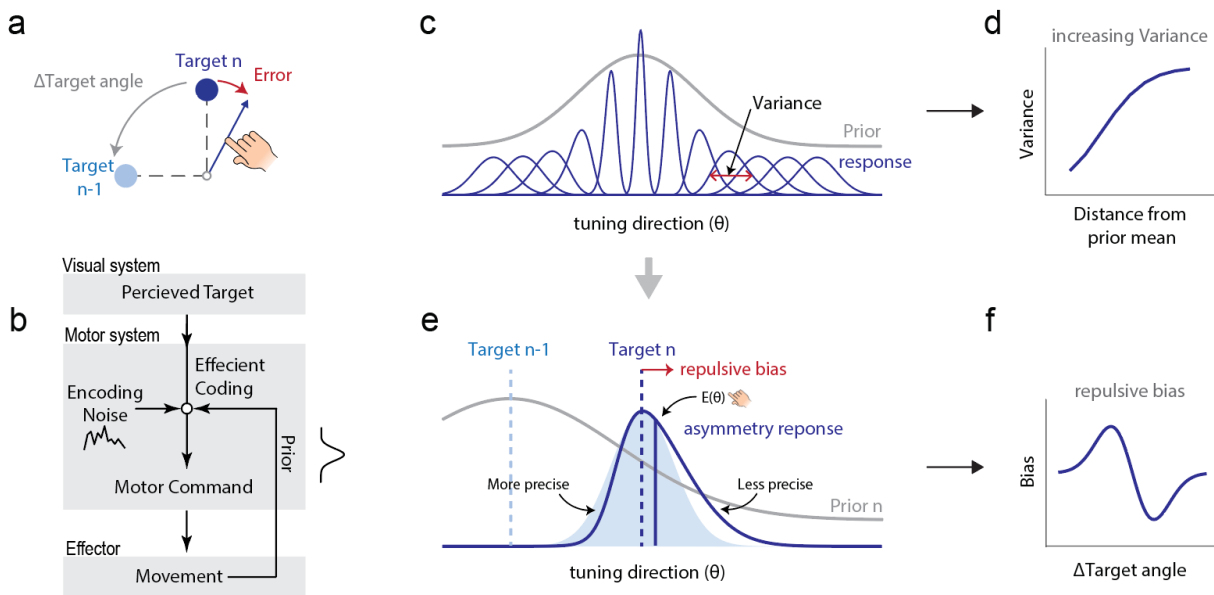
68 Other models offer alternative frameworks for understanding how prior expectations improve encoding  
69 accuracy<sup>10,20</sup>. For example, Bayesian models suggest that perception arises from combining prior  
70 expectations with incoming sensory information to compute a posterior estimate. As a result, they predict  
71 that current movements or perceptions will be biased toward prior expectations. Importantly, this is  
72 opposite to the repulsive biases predicted by the efficient coding model. The Bayesian framework has  
73 been successful in explaining various perceptual and motor biases<sup>11,21,22</sup>. Therefore, we consider the  
74 Bayesian model as an alternative to compare with our efficient coding model in predicting sequential  
75 effects in motor tasks.

76

77 While the visual world is relatively stable and continuous, motor goals can vary significantly over short  
78 time scales<sup>23</sup>. Consider, for example, the actions required when shopping: reaching for a milk box, placing  
79 it in a cart, and pushing the cart away, all within a matter of seconds. Instead of relying on a static prior  
80 for motor planning, the sensorimotor system may continuously update its priors based on the current  
81 motor goal to facilitate efficient coding. In other words, priors for motor planning might be largely shaped  
82 by recent movements. Based on this assumption, the efficient coding theory will predict specific  
83 sequential effects on movement bias and variance in a center-out reaching task (Fig 1d&f). Other  
84 frameworks, such as Bayesian models, make different predictions. We aim to test these competing  
85 predictions in the following experiments.

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89 **Figure 1. An efficient coding framework for motor control.** a) Illustration of a reaching task. b) Schematic of an  
 90 efficient coding framework. The motor system encodes a motor command based on the perceived target. The  
 91 effector implements the motor command, which serves as a prior that drives the motor system to re-allocate its  
 92 coding resource following the efficient coding rule. c) The precision of encoding the direction of movement is  
 93 influenced by the prior. d) The model posits that as the current movement diverges from the prior mean, the variance  
 94 in movement direction escalates. e) For a given movement direction, encoding is more precise on the side closer to  
 95 the prior and less accurate on the opposite side. As a result, the representation of a movement direction becomes  
 96 asymmetric, with a flatter tail extending away from the prior.  $E(\theta)$  represents the mean of this distribution, which is  
 97 biased in the direction opposite to the prior mean. The shaded blue distribution illustrates the response in the  
 98 absence of efficient coding. In this context, we assume the prior is primarily influenced by the movement direction  
 99 in the previous (n-1) trial. f) The efficient coding model predicts a repulsive sequential bias in reaching tasks.

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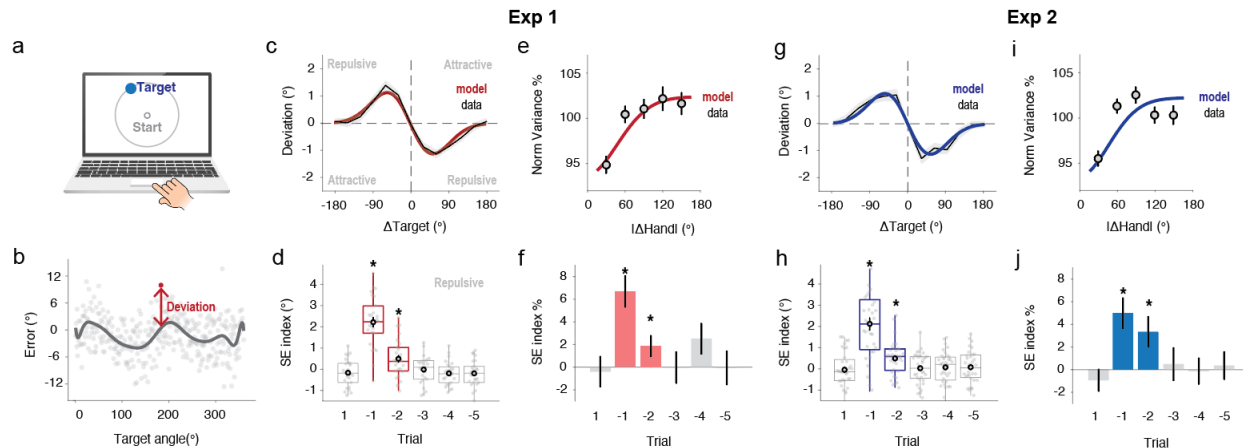
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## 102 Results

### 103 Sequential effects in reaching aligns with the efficient coding model

104 To examine sequential effects predicted by the efficient coding theory, in Exp 1, we employed an online  
 105 reaching experiment where participants control a cursor with a trackpad. In each trial, a target appeared  
 106 at a random position along an invisible circle and participants made a center-out reaching movement from  
 107 a central start position towards the target (Fig 2a). The cursor was invisible during the movement to

108 prevent online corrections. Endpoint feedback was provided after the movement to indicate the hand  
 109 position at the target radius.  
 110  
 111



112  
 113 **Figure 2. Sequential effects in reaching.** a) An illustration of the repulsive bias predicted by the efficient coding  
 114 model. b) The motor bias of a sample participant. The gray curve shows the smoothed motor bias function. The  
 115 deviation was defined as the difference between the current response and the bias. d) Sequential bias in Exp 1: The  
 116 motor deviation of trial n was plotted as a function of the difference in the target angle between trial N and trial N-  
 117 1 ( $\Delta\text{target}$ ). This figure shows a repulsive sequential effect. The black curve indicates data, and the red curve indicates  
 118 the prediction of the efficient coding model. e) SE index showing the influence of the target in trial N+1, and trials  
 119 N-1 to N-5 on the direction of reaching in trial n. f) The normalized movement variance increased with the distance  
 120 between movement N and the movement N-1 ( $|\Delta\text{hand}|$ ). g) Sequential effect (SE) index derived from a general  
 121 linear model between normalized movement variance and  $|\Delta\text{hand}|$  for trial N+1, and trials N-1 to N-5. h-k).  
 122 Sequential effects in Exp 2. The only difference between Exp 1 and 2 was the lack of feedback in Exp 2. Results were  
 123 very similar to panel c-f. Error bars and shaded areas indicate standard error. \*,  $p < .02$ .

124  
 125 To obtain an accurate assessment of the sequential effect, we eliminated the impact of systematic bias  
 126 by fitting a motor bias function based on the target position (Fig S1) for each participant. The residual  
 127 error, representing the deviation from this fitted motor bias function (Fig 2b), was defined as the  
 128 deviation<sup>13,24-26</sup> and was used to analyze the sequential effects.

129  
 130 To examine the sequential effect in reaching biases, we plotted movement deviation as a function of the  
 131 angular difference between the current and previous targets ( $\Delta\text{Target}$ ). We found that the direction of  
 132 movement in the current trial (trial n) was biased away from the previous target (trial n-1, Fig 2c), with

133 the magnitude of this repulsive effect increasing with  $\Delta$ Target, peaking at  $1.5^\circ$  for a  $\Delta$ Target of  
134 approximately  $60^\circ$ . This bias function aligned well with predictions from an efficient coding model. To  
135 quantify the size of the sequential bias, we calculated a sequential effect (SE) index, defined as the  
136 difference between the average bias for  $\Delta$  Target from  $-90^\circ$  to  $0^\circ$  and  $0^\circ$  to  $90^\circ$ . A positive SE index signified  
137 a repulsive effect. We found an SE index significantly larger than 0 in trial N-1 ( $t(25)=9.5$ ,  $p<.001$ ,  $d=1.9$ )  
138 and trial N-2 ( $t(25)=2.8$ ,  $p=.010$ ,  $d=0.55$ ), but not in trial N-3 ( $t(25)=-0.10$ ,  $p=0.92$ ,  $d=-0.02$ ; Fig 2d). With a  
139 median trial duration of 2.08s (SD: 1.05s), this result suggested rapid updating of prior expectations by  
140 the motor system.

141  
142 We then measured the sequential effect as a function of movement variance. Again, consistent with the  
143 prediction of the efficient coding model, the movement variance increased with the distance between the  
144 directions of the two consecutive movements (Fig 2g-h). We quantified this effect by fitting a sigmoid  
145 function with motor variance as the dependent variable and the difference in hand angle as the  
146 independent variable, pooling data from all participants. The SE index was defined as the sigmoid  
147 amplitude predicted by the best-fit function (Fig 2e). Similar to what we have observed for the sequential  
148 bias, this SE index of the movement variance dropped rapidly across trials: a significant effect was found  
149 for trial N-1 ( $p<0.001$ , Bootstrap) and N-2 ( $p=0.026$ , Fig 2f), measured by bootstrap resampling. The effect  
150 disappeared for trial N-3 ( $p=0.98$ ), which occurred only  $\sim 6$  seconds prior.

151  
152 In Exp 1, we showed that the sequential effects in the motor bias and movement variation are consistent  
153 with the efficient coding model. However, we noted that endpoint feedback was provided after reaching,  
154 facilitating the recalibration of the sensorimotor system. This recalibration process might be specific to  
155 areas near the recently reached positions, potentially contributing to the observed sequential effect in  
156 motor variance. To eliminate the potential influence of sensorimotor recalibration, we conducted a  
157 replication of Exp 1 without endpoint feedback (Exp 2). The results showed remarkably similar sequential  
158 effects in both movement bias and variance (Fig 2g-j), confirming that these effects were independent of  
159 visual feedback or sensorimotor recalibration.

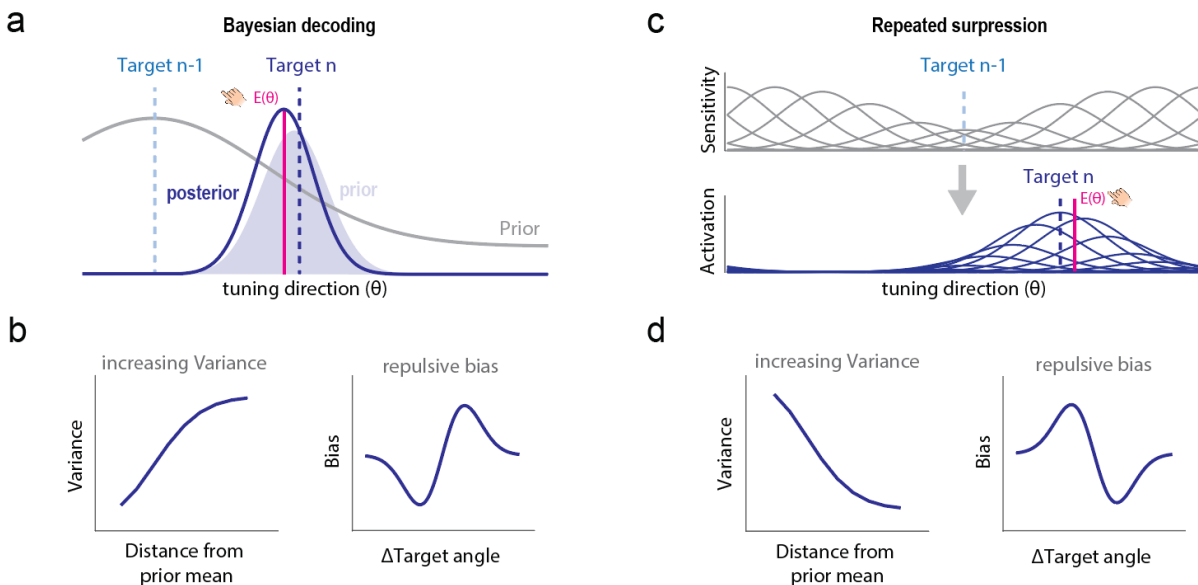
160  
161 The results in Exp 1-2 established a sequential effect in reaching movements that aligns with the  
162 predictions of the efficient coding model. In the following session, we considered two alternative models  
163 proposed to explain sequential effects. The first model we evaluated was the Bayesian model<sup>20,21,27</sup>, which  
164 is widely used to explain how prior expectations influence behavior. According to Bayesian principles, the

165 system integrates prior knowledge with current observations to form a posterior estimate (Fig 3a). This  
 166 process allows the system to reduce encoding noise. However, importantly, the posterior skews the  
 167 average response toward the prior and leads to an attractive sequential bias (Fig 3b), which contradicts  
 168 the repulsive bias as observed in behavioral results (Fig 2c).

169

170 Another alternative model we evaluated was the repeated suppression model<sup>28,29</sup>. This model suggests  
 171 that after observing a stimulus or executing a movement, neurons tuned to that direction become less  
 172 sensitive due to fatigue or active suppression, a mechanism that favors novel stimuli to avoid encoding  
 173 redundancy. The suppression model predicts a repulsive sequential bias due to the asymmetric response  
 174 of units on the suppressed and unsuppressed sides (Fig 3c). However, unlike the efficient coding model,  
 175 which facilitates the processing of repeated stimuli, the suppression mechanism increases sensitivity to  
 176 stimuli that change<sup>30,31</sup>. As a result, the model posits that movements closer to the previous one are  
 177 encoded with less precision and exhibit greater variability compared to movements further away (Fig 3d).  
 178 This prediction stands in opposition to the sequential effects observed in our experiments (Fig 2e). As such,  
 179 the unique sequential effects in reaching suggest that motor planning follows efficient coding principles.

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181

182 **Figure 3. The repeated suppression model and Bayesian model cannot explain the sequential effects in reaching.**

183 a) Schematic of the Bayesian decoding model. b) This model predicts increasing variance and attractive bias. c)  
 184 Schematic of the Repeated suppression model. The sensitivity of the unit tuned to the previous movement decreases,  
 185 which causes an asymmetric representation of the subsequent movement direction. d) The Repeated suppression



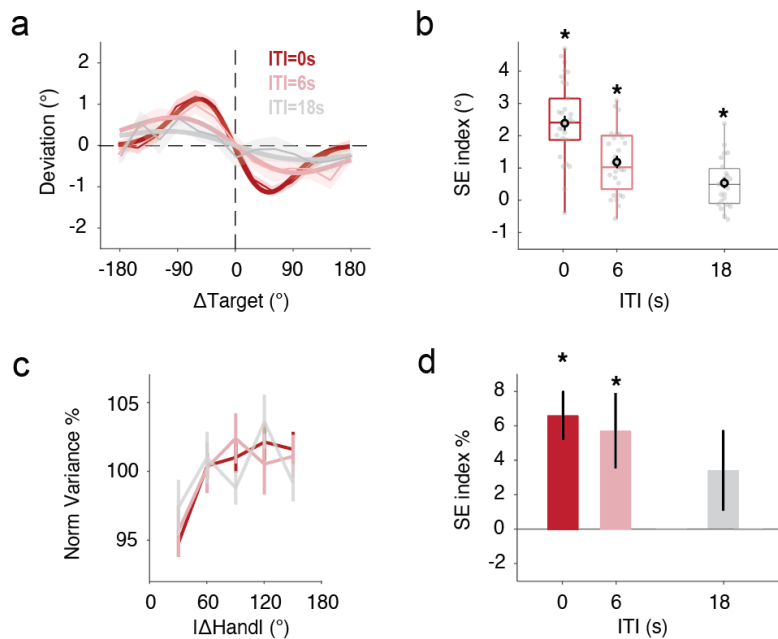
186 model predicts decreasing variance and repulsive bias. Neither of these models were able to explain the sequential  
187 effects observed in behavioral results (Fig. 2).

188

### 189 Temporal dynamics of the sequential effect

190 In Exp 1-2, we observed a repulsive effect only from the 1-back and 2-back trials. This motivated us to  
191 further examine the temporal regulation of the repulsive sequential effect. We tested whether the rapid  
192 drop in the sequential effect solely depended on time, or whether it also depended on the number of  
193 trials. As such, in Exp 3, we extended the inter-trial interval (ITI) to either 6s or 18s for two groups of  
194 participants and compared the results with Exp 1 (0s ITI) (Fig 4). While the strength of the sequential  
195 effects decreased with time, both the repulsive bias ( $t(26)=5.9$ ,  $p<0.001$ ,  $d=1.2$ ) and the variance  
196 modulation ( $p<0.001$ , Bootstrap) could be observed for trial N-1 if participants simply wait for 6s between  
197 two trials. This result contrasted with the N-3 trial in Exp 1, which was ~6s prior to the current movement  
198 (Fig 4b, d), but no sequential was observed. Moreover, the repulsive bias remained significant even in the  
199 18s ITI condition (Fig 4b,  $t(22)=3.4$ ,  $p=0.002$ ,  $d=0.72$ ). The SE index of the motor variance in the 18s ITI  
200 conditions showed a positive trend but did not reach significance ( $p=0.16$ , Fig 4d). These results suggested  
201 that the attenuation of the sequential effects depended on both passing time and intervening information.

202



203

204 **Figure 4. Temporal dynamics of the Sequential effects in reaching.** (a) Sequential effect in movement direction for  
205 three ITI conditions. The thinner lines indicate the data, and the thicker lines indicate the prediction of the efficient  
206 coding model. (b) SE index with different ITI. Different from what has been observed in the 3-back condition in Exp

207 1 (which had a ~6s delay), the SE index was significant in the 6s and 18s ITI conditions, indicating the effect decreased  
208 with both time and trial number. Error bar and shaded area indicate standard error. (c-d) Sequential effect in motor  
209 variance was modulated by ITI. A significant SE index was found in the 6s ITI condition. \*,  $p < .002$ .

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### 211 Dissociating sequential effect in movement and perception.

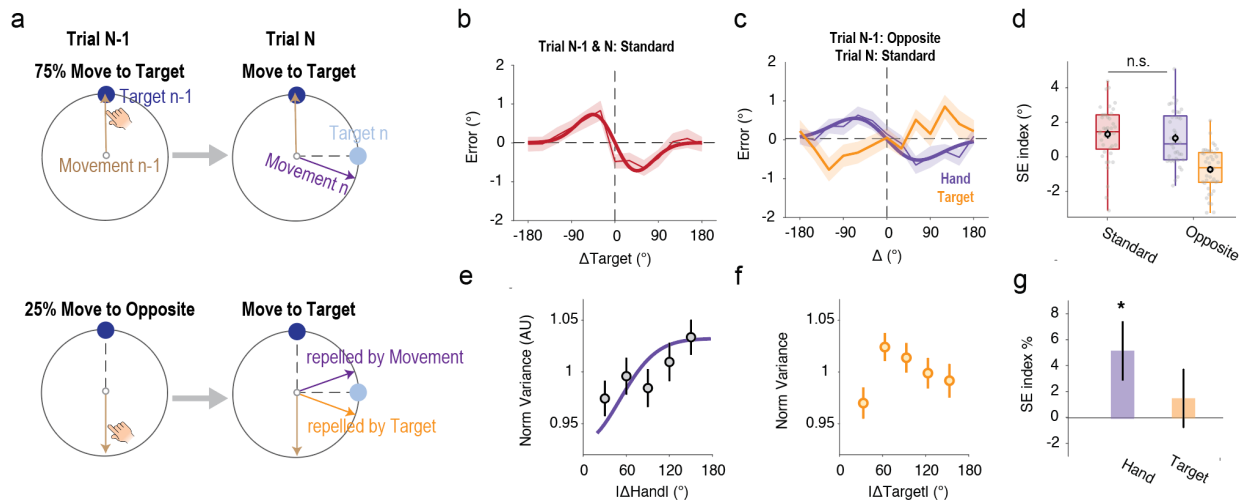
212 Sequential effects have been widely observed in perceptual tasks<sup>22,32,33</sup>. While we tried to minimize the  
213 role of visual uncertainty and perceptual working memory in Exp 1, a more rigorous examination was  
214 necessary to differentiate effects originating in the motor versus the perceptual systems<sup>34</sup>. To this end, in  
215 Experiment 4 we implemented a design where participants were instructed to either move directly  
216 towards the target (Standard condition, 75% of trials) or in the opposite direction (Opposite condition, 25%  
217 of trials). As a critical test of the source of these sequential effects in Exp 1, we analyzed scenarios where  
218 trial N-1 was an Opposite trial and trial N was a Standard trial (Fig 5a, bottom). In such cases, the  
219 inconsistency between movement direction and target in trial N allowed us to disentangle the influences  
220 of target location representation from the motor control itself. If the repulsive bias was primarily driven  
221 by motor factors, the direction in trial N would be repelled by the movement in trial N-1. Conversely, if  
222 perception of the target location was the cause, trial N's reaching direction would be repelled by the  
223 perceived location of the target in trial N-1.

224

225 When two consecutive trials were both Standard trials (Fig 5a, top), we observed a repulsive bias similar  
226 to that in Exp 1 (Fig 5b). Crucially, when trial N-1 was an Opposite trial and trial N was a Standard trial, the  
227 direction in trial N was repelled away by the previous *reaching movement* ( $t(40)=4.4$ ,  $p < .001$ ,  $d=0.68$ ), not  
228 by the previous target location (Fig 5c). The magnitude of this repulsive effect from the previous  
229 movement was comparable to that observed when both trials N and N-1 were Standard conditions,  
230 indicated by the SE indexes ( $t(40)=0.70$ ,  $p=.49$ ,  $d=0.11$ ; Fig 5d). Moreover, when examining the sequential  
231 effect on motor variance, we found that variance increased with the difference in hand angle ( $p < .001$ ,  
232 Bootstrap, Fig 5e) rather than the difference in target angle ( $p=.20$ , Fig 5f-g). These results suggested that  
233 the sequential effects in Exp 1-2 were rooted in the motor system rather than the perceptual system.

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**Figure 5. Sequential effects in reaching were associated with motor movement rather than perception.** a) Design of Exp 3: In 75% of trials, participants were directed to move towards the target (Standard), and in 25% of trials, they were directed to move in the opposite direction of the target (Opposite). A repulsive effect was expected when both trials N and N-1 were Standard trials (top row). In cases where trial N was a Standard trial and trial N-1 was an Opposite trial, the design allowed examination of whether the repulsive effect was triggered by target perception or movement (bottom row). b-c) The sequential effect of motor bias when both trial N and trial N-1 were Standard trials (b) or when trial N-1 was an Opposite trial and trial N was a Standard trial (c). The thin lines with shaded error bars indicate data, and the thick curve indicates the prediction of the efficient coding model. d) The sequential bias was similar across panels b and e when the SE index after the Opposite trial was measured based on  $\Delta$ hand rather than  $\Delta$ target. e-f) After an Opposite trial, movement variance increased as a function of  $\Delta$ hand (e) rather than  $\Delta$ target (f). The motor variance increased with  $\Delta$ hand rather than  $\Delta$ target. g) The coefficients of linear regression measured from panel e-f. Error bars and shaded areas indicate standard error. \*,  $p < .001$ .

We have shown that the sequential bias in Exp 1-4 was caused by movement; However, it remains possible that this effect could be mediated by perception. For instance, the movement from trial N-1 might repulse the perception in trial N, thereby affecting the subsequent movement (mediated hypothesis). Alternatively, the current movement could be directly repelled away by the previous movement (direct hypothesis). To distinguish between these hypotheses, we examined cases where trial N-1 was a Standard trial and trial N an Opposite trial (Fig S2a). Under the mediated hypothesis, the current perception is repelled away from the previous movement, so that we would expect the current movement to be attracted towards the movement N-1 when participants are instructed to move in a direction opposite that of target N. In contrast, the direct hypothesis predicts the current movement to be repelled from the

259 target/movement in N-1 (Fig S2b). Our findings aligned with the direct hypothesis (Fig S2c-d). Based on  
260 the results in Exp 4, we concluded that the current movement was directly influenced by the previous  
261 movement.

262

263 We also observed a priming effect in reaction time in Exp 1-4. Consistent with the notion of efficient  
264 coding, reaction times were shorter when the current target was close to the previous target (Fig S3a-b).  
265 However, this effect may pertain more to target detection than motor planning. The reaction time for the  
266 current trial was influenced by targets presented more than 10 trials in the past (Fig S3c-d), which was  
267 very different from the temporal dynamics of sequential effects in movement direction or motor variance  
268 (Fig 3e). Moreover, in Exp 4, the reaction time priming effect was similar after both Opposite and Standard  
269 trials (Fig S3e), suggesting the effect may be related to target detection rather than reaching, per se.

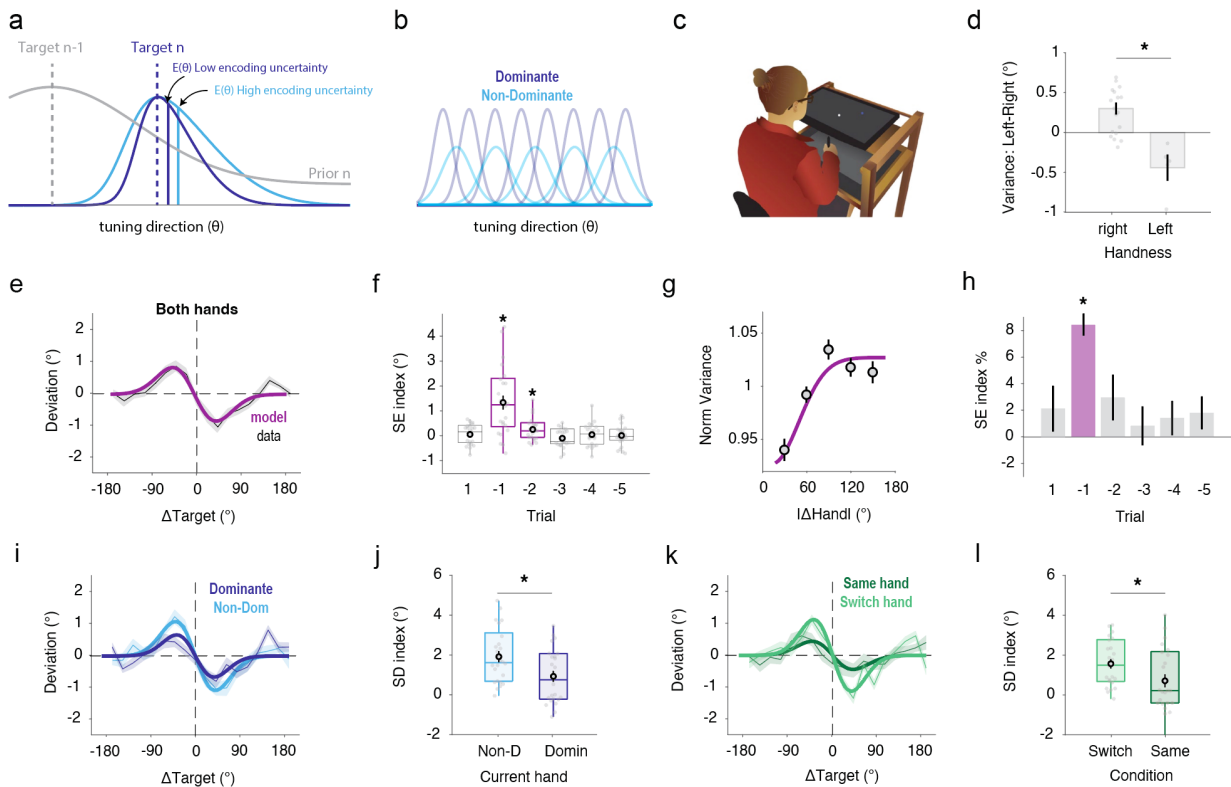
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271 Encoding noise enhances the repulsive sequential bias.

272 Another key prediction of the efficient coding theory is that the sequential bias should be modulated by  
273 encoding noise. Specifically, increased noise within the system should lead to a broader distribution of  
274 the response signal. Consequently, the average response of the system will exhibit a larger repulsive bias  
275 relative to the prior mean (Fig 6a). To examine this, we compared the sequential bias in reaching  
276 movements between the dominant hand and the non-dominant hand, with the premise that encoding a  
277 movement with the non-dominant hand incorporates more noise (Fig 6b), which should increase the  
278 repulsive bias. In Exp 5, we performed a similar center-out reaching task and participants were randomly  
279 instructed to use one hand per trial. To make sure that participants adhered to the instruction, we  
280 performed this experiment in a lab setup with the experimenter supervising the task (Fig 6c). Participants  
281 moved their occluded hand on a tablet, with the visual stimulus displayed on a monitor directly above (Fig  
282 6c). Consistent with our assumption, participants showed significantly lower motor variability with the  
283 dominant hand compared to the non-dominant hand ( $t(23)=4.9$ ,  $p<.001$ ,  $d=1.0$ ; Fig 6d).

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287 **Figure 6. The repulsive sequential bias increased with the encoding noise in the motor system.** a) Illustration of  
 288 how encoding noise increases the repulsive bias based on the efficient coding model. b) We assumed that the non-  
 289 dominant hand has fewer movement planning units with higher encoding uncertainty, indicated by a broader tuning  
 290 profile. c) Illustration of the lab-based setup. d) Difference in motor variance between the left and right hand. Right-  
 291 handed participants showed noisier movements using their left hand and vice versa. e-f) The sequential effect of  
 292 motor bias (e) and the SE index (f) when data from both hands were collapsed. g-h) Sequential effect of motor  
 293 variance (g) and (h) the estimated coefficients from a general linear model. i-j) A stronger repulsive bias was observed  
 294 when the current movement was performed using the non-dominant hand compared to the dominant hand. k-l) A  
 295 stronger repulsive bias was observed when participants switched hands compared to the situation when they used  
 296 the same hand for trial N-1 and trial N. Error bars and shaded areas indicate standard error. \*,  $p < .001$ .

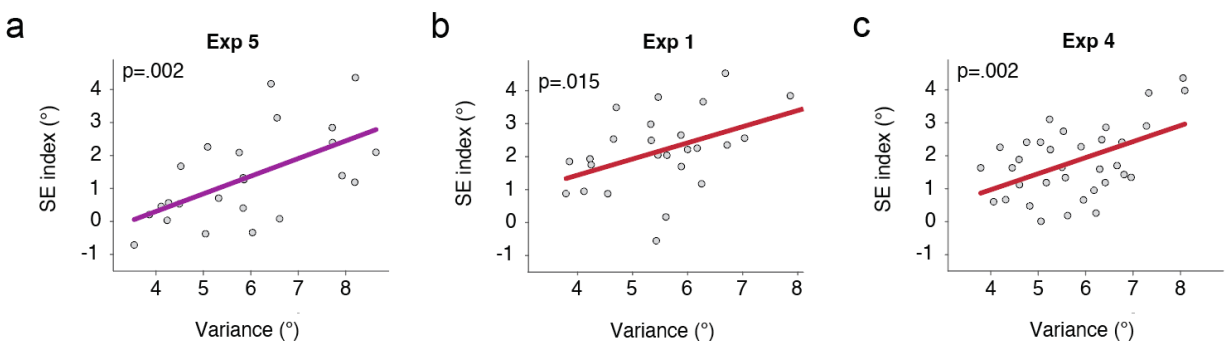
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298 The results from Exp 5 provide compelling support for the efficient coding model. All main results were  
 299 consistent with what we had observed in the online experiments. When we combined the data across the  
 300 two hands, we observed a repulsive sequential bias (N-1:  $t(23)=4.7$ ,  $p < .001$ ,  $d=0.96$ ; N-2:  $t(23)=2.6$ ,  $p=.02$ ,  
 301  $d=0.55$ ; Fig 6e-f) and increased movement variance (N-1:  $p < .001$ , Bootstrap, Fig 6g-h). Importantly, we  
 302 observed a larger sequential bias when the current movement was performed using the non-dominant  
 303 hand compared to the dominant hand ( $t(23)=4.7$ ,  $p < .001$ ,  $d=0.97$ ; Fig 6i-j), supporting the prediction of

304 the efficient coding theory that bias escalates with encoding noise in the motor system. Interestingly, we  
305 also observed a larger sequential bias when participants switched their hands (namely using different  
306 hands in trial N and N-1) compared to using the same hand ( $t(23)=6.7$ ,  $p<0.001$ ,  $d=1.4$ ; Fig 6k-l). This effect  
307 is likely due to dynamic allocation of encoding resources across hands, leading to increased encoding  
308 variability immediately after a hand switch and, consequently, a larger bias. Alternatively, more units  
309 might be recruited when repeating a movement with one hand, reducing encoding noise as well as the  
310 sequential bias.

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312 To further examine how the variability in the motor system influences the sequential bias, we analyzed  
313 the correlation between motor variance and the SE index in Exp 5. Consistent with the prediction of the  
314 efficient coding theory, we found a positive correlation between individual differences in variance and the  
315 SE index for both hands (Fig 7a). A positive correlation was also found when we re-examined the data  
316 from Exp 1 and 4 (Fig 7b-c). Those results together further supported the hypothesis that motor planning  
317 follows the principles of efficient coding.

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321 **Figure 7. The repulsive sequential bias increased with the motor variability across participants.** Correlation  
322 between the SE index and the motor variance for Exp 5 (a), Exp 1 (b), and Exp 4 (c). Each dot is one participant. The  
323 colored line shows the best-fitted linear model. The p-value was measured from the Pearson correlation.

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325

## 326 Discussion

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328 Motor planning requires rapid computations in high-dimensional spaces<sup>17,35,36</sup>. Our study investigated  
329 whether the motor system employs efficient coding mechanisms to improve encoding accuracy. Efficient  
330 coding, a theory initially applied to perceptual systems, posits that neural systems allocate resources in a

331 manner that optimizes the overall information encoded<sup>1,4,14</sup>. Specifically, the system prioritizes encoding  
332 resources for more probable stimuli/movements over less frequent ones, leading to heterogeneous  
333 accuracy across the task space as well as systematic biases in the percepts/movements<sup>10-13,15</sup>. The current  
334 study confirmed these key predictions of efficient coding in a series of experiments using planar reaching  
335 tasks, suggesting that motor planning is indeed subject to efficient coding principles.

336  
337 When testing the efficient coding model, we identified two novel sequential effects in reaching tasks. First,  
338 reaching variability increased when the current reaching direction deviated significantly from the previous  
339 direction. This modulation in variability suggests that the motor system dynamically adjusts its encoding  
340 resources based on recent movements, resulting in movements closer to prior expectations being  
341 encoded with higher precision. Second, the current reaching direction was biased away from the previous  
342 reaching direction. This repulsive bias is a by-product of the efficient coding model: due to the asymmetric  
343 representation of movement directions, the noise distribution causes movements to shift in the opposite  
344 direction from the prior.

345  
346 Additionally, we observed that the strength of this bias increases with encoding noise. This correlation  
347 was evident both within participants, where the non-dominant hand showed a stronger sequential effect  
348 compared to the dominant hand, and between participants, where individuals with higher motor  
349 variability exhibited a stronger repulsive bias. Together, these results confirmed that efficient coding  
350 principles hold for motor planning.

351  
352 The temporal dynamics of the sequential effect highlighted the flexibility in the motor system to  
353 dynamically reallocate resources. The principles of efficient coding have been tested through systematic  
354 biases shaped by long-term priors<sup>14,15</sup>, often influenced by life-long experiences<sup>10,11</sup>. In our study, we  
355 extended this principle to explain trial-by-trial biases in movement. Remarkably, the repulsive effect  
356 extinguished after only 3 trials (or 6 seconds), suggesting that priors in the motor system updated rapidly.  
357 This rapid adaptability might be optimal for motor planning, given the frequent and swift variations in the  
358 goals and interactions of the motor system with objects over time<sup>23</sup>. In line with the notion of dynamic  
359 priors, the sequential effect decreased when participants consistently used one hand, as opposed to  
360 alternating between hands. This observation suggested that encoding resources are preferentially  
361 allocated to the active hand, thereby reducing encoding noise.

362

363 While previous studies suggest that uncertainty in visual perception can also generate sequential  
364 effects<sup>22,37–39</sup>, our design specifically minimized the influence of those visual effects. Typical visual tasks  
365 embed high visual uncertainty: the targets are often vague, presented for a short duration, and disappear  
366 when participants make their response<sup>33</sup>. In contrast, our study presented a high-contrast target that  
367 remained visible during the movement. This design would minimize perceptual serial dependence, as  
368 previous studies found<sup>24</sup>.

369

370 Our results also clearly dissociated the current motor sequential effects from the visual serial dependence  
371 reported in other studies. First, the direction of the motor sequential bias observed in our study is  
372 opposite to the serial dependence typically seen in visual tasks<sup>22,24,33,39</sup>. In our motor tasks, the current  
373 movement is repulsed away from the previous movement, whereas in visual perception tasks, the  
374 perceived target is usually attracted towards the previous target position. Second, the tuning properties  
375 of the sequential effects differ between visual and motor tasks; the repulsive bias in motor tasks peaks at  
376 around 60°, whereas the sequential effect in vision is usually narrower, peaking at less than 30°<sup>33</sup>. Third,  
377 our sequential effects are significantly modulated by handedness, further suggesting an association with  
378 movement rather than perception.

379

380 The opposite directions of the sequential biases in motor and visual systems might reflect their different  
381 functional purposes and underlying mechanisms. In visual perception, maintaining a stable and consistent  
382 representation of the world is crucial<sup>40–42</sup>. This stability is achieved through Bayesian decoding<sup>13,43–45</sup>,  
383 where the system interprets current evidence based on prior knowledge. This mechanism ensures a  
384 coherent and reliable perception of the environment, albeit at the potential cost of an attractive bias.  
385 Because objects in the world are, typically, physically stable, these attractive biases can be beneficial<sup>46,47</sup>.

386

387 While the objects of perception in the world have identities that are physically stable, the actions we need  
388 to make upon these objects can and do change from moment to moment. The motor system, therefore,  
389 operates under distinct constraints. Motor planning, at least by definition, is an encoding process rather  
390 than a decoding process<sup>48,49</sup>, making the Bayesian decoding mechanism less applicable. Additionally,  
391 motor goals can vary quickly over time<sup>23</sup>, so assimilation of past movements does not present a clear  
392 benefit for the motor system. Instead, a decorrelation mechanism can be beneficial for minimizing  
393 repetitive mistakes or biases induced by the perceptual system and other sources<sup>50</sup>. As such, the repulsive



394 effect observed in our study serves these purposes, promoting the exploration of diverse motor strategies  
395 in a dynamic environment while avoiding redundancy.

396  
397 Interestingly, the sequential bias identified in our study contrasts with a history-influenced effect known  
398 as use-dependent learning in motor control. Use-dependent learning refers to a bias toward repeated  
399 movements in the same direction<sup>51-53</sup>. However, the time course of use-dependent learning is very  
400 different from the repulsive sequential bias we observed. First, use-dependent learning typically requires  
401 multiple trials to manifest<sup>51,54,55</sup>, whereas the current repulsive effect emerges after a single trial.  
402 Moreover, use dependent learning usually last for tens of trials while the repulsive sequential effect lasted  
403 for only two trials.

404  
405 Our results suggest that the differing timescales of use-dependent learning and efficient coding may  
406 reflect a progressive shift of motor control strategy in developing a skilled movement. The repulsive bias  
407 induced by efficient coding could be beneficial in a volatile environment for several reasons, such as  
408 reducing repeated errors and enhancing sensitivity to changes in the environment or target<sup>17,50</sup>. However,  
409 there are instances where repeated, stable movement is desirable, such as when hammering a nail while  
410 holding it steady with one's fingers. Initially, efficient coding may increase the precision of movements.  
411 Those movement might be slow and performed with caution so that the system can correct for undesired  
412 exploratory errors with online control. As the activity continues, use-dependent learning dominates to  
413 stabilize the movement, facilitating smooth and stable repetition without conscious control. Future  
414 studies should explore the intriguing possibility that there is a transition between efficient coding and use-  
415 dependent learning, which may reveal how the system balances the competing needs of flexibility and  
416 stability in motor planning.

417  
418

## 419 **Methods**

420  
421 Participants

422 Testing was conducted online for Exp 1, 2, 3, 4 and in the lab for Exp 5. For the online studies, 154 young  
423 adults (76 female, age:  $26.7 \pm 4.9$  y) were recruited using the Prolific.io. The participants performed the  
424 experiment on their personal computers through a web-based platform for motor learning experiments.  
425 Based on a prescreening survey employed by Prolific, the participants were right-handed and had normal

426 or corrected-to-normal visions. These participants were paid \$8/h. For the lab-based experiments, we  
427 recruited 24 undergraduate students (15 female, mean age = 21.42y, SD = 3.78y) from the University of  
428 California, Berkeley community. 19 of the participants were right-handed and 5 of them were left-handed  
429 based on their scores on the Edinburgh handedness test<sup>56</sup> and had normal or corrected-to-normal vision.  
430 These participants were paid \$20/h. All experimental protocols were approved by the Institutional Review  
431 Board at the University of California, Berkeley. Informed consent was obtained from all participants.

432

### 433 Design and procedure

#### 434 *Experiment 1*

435 Exp 1-4 were performed using our web-based experimental platform<sup>57,58</sup>. The code was written in  
436 JavaScript and presented via Google Chrome, designed to run on any laptop computer. Visual stimuli were  
437 presented on the laptop monitor and movements were produced on the trackpad. Data was collected and  
438 stored using Google Firebase.

439

440 26 participants (20 females) took part in Exp 1. To start each trial, the participant moved the cursor to a  
441 white circle (radius: 1% of the screen height) positioned in the center of the screen. After 500 ms, a blue  
442 target circle (radius: 1% of the screen height) appeared with the radial distance set to 40% of the screen  
443 size. Target locations were randomly generated from 1°-360° with a minimum step of 1°. The participant  
444 was instructed to produce a rapid shooting movement, attempting to move through the target. A  
445 feedback cursor (radius: 0.6% of screen height) appeared for 100 ms when the amplitude of the  
446 movement reached the target distance, indicating the angular position of the hand at that distance. The  
447 feedback cursor and target were then extinguished. If the movement time was >300 ms, the message  
448 "Too Slow" was presented on the screen for 500ms. At the end of the trial, the position of the cursor was  
449 reset to a random position within a circle centered at the start position with a radius 4% of the target  
450 distance. The participant moved the cursor back to the start position to initiate the next trial. Each  
451 participant completed 1080 trials in total.

452

#### 453 *Experiment 2*

454 To confirm the effect observed in Exp 1a was not due to the existence of endpoint feedback, we replicated  
455 Exp 1 in 2 without presenting any feedback after the movement. Other details of Exp 2 were identical to  
456 Exp 1. 36 participants (21 females) took part in Exp 2.

457

458 *Experiment 3*

459 We aimed to examine the temporal modulation of serial dependence in Exp 3. Compared to Exp 1, we  
460 extended the inter-trial interval to either 6s (n = 28, 10 females) or 18s (n = 23, 12 females) for two groups  
461 of participants, respectively. A message "wait" would be presented on the monitor between two trials.  
462 Participants were instructed to put their right hand on the trackpad and rest until they saw the message  
463 "move to center" which indicated the start of a new trial. Participant completed 880 (6s condition) or 360  
464 trials (18s condition).

465

466 *Experiment 4*

467 Exp 4 was designed to examine whether the sequential effect was induced by perception or movement.  
468 41 participants (13 females) took part in Exp 4. The procedure of Exp 4 was essentially the same as in Exp  
469 1. To evaluate whether this repulsive effect was perception-based or motor-based, we included trials (25%)  
470 in which the participants were instructed to move in the opposite direction of the target. Before each trial,  
471 an instruction message would appear on the screen to instruct participants to either "move to target" or  
472 "move to opposite." There were no consecutive "opposite" trials. Each participant completed 960 trials  
473 in total.

474

475 *Experiment 5*

476 Exp 5 was designed to examine how motor variability influences the sequential reaching bias. 24  
477 participants (15 females, 19 right-handed and 5 left-handed) performed the experiment in the lab setup.  
478 Participants performed a center-out reaching task, holding a digitizing pen in the right or left hand to make  
479 horizontal movements on a digitizing tablet (49.3cm x 32.7cm, sampling rate= 100 Hz; Wacom, Vancouver,  
480 WA). The stimuli were displayed on a 120 Hz, 17-in. monitor (Planar Systems, Hillsboro, OR), which was  
481 mounted horizontally above the tablet (25 cm), to preclude vision of the limb. The experiment was  
482 controlled by custom software coded in MATLAB (The MathWorks, Natick, MA), using Psychtoolbox  
483 extensions, and ran on a Dell OptiPlex 7040 computer (Dell, Round Rock, TX) with Windows 7 operating  
484 system (Microsoft Co., Redmond, WA).

485

486 Participants made reaches from the center of the workspace to targets positioned at a radial distance of  
487 8 cm. The start position and target location were indicated by a white annulus (1.2 cm diameter) and a  
488 filled blue circle (1.6 cm), respectively. Vision of the hand was occluded by the monitor, and the lights  
489 were extinguished in the room to minimize peripheral vision of the arm. Feedback, when provided, was

490 in the form of a 4 mm white cursor that appeared on the computer monitor, aligned with the position of  
491 the digitizing pen.

492

493 To start each trial, a letter “R” or “L” would be presented within the start circle to inform participant which  
494 hand to use on this trial. Participants used the instructed hand to hold the pen and put the other hand on  
495 the side. The experimenter supervised the whole experiment to make sure the participant applied the  
496 correct hand. After maintaining the cursor within the start circle for 500 ms, a target appeared. The  
497 participant was instructed to make a rapid slicing movement through the target. Right after their  
498 movement amplitude reached 8 cm, a cursor would be presented at that position for 1 s, providing  
499 feedback of the accuracy of the movement (angular position with respect to the target). After this interval,  
500 the target and cursor were extinguished. Another letter appeared at the start position and participants  
501 changed hand accordingly. To guide the participant back to the start position without providing angular  
502 information about hand position, a white ring appeared denoting the participant’s radial distance from  
503 the start position. Once the participant moved within 2 cm of the start position, the ring was extinguished,  
504 and a veridical cursor appeared to allow the participant to move their hand to the start position. If the  
505 movement time was >300 ms, the audio "Too Slow" was played right after the reaching.

506

507 The required hand was pseudorandomized so there were 4 left-hand and 4 right-hand trials within every  
508 8 trials. Target locations were randomized in a way that both hands would visit targets from 1°-360° (with  
509 a step of 1°) within every 720 trials. The whole experiment included 2160 trials and took about 4 h.  
510 However, we allowed participants to end the experiment based on their convenience. 14 out of 24  
511 participants finished all trials; other participants finished 1000~2000 trials.

512

### 513 Data Analysis

514 We calculated the error of hand angle as a difference between the hand position when it reached the  
515 target distance and the target position. A positive hand angle denoted that the hand position was more  
516 clockwise than the target at the target radius. Trials with a movement duration longer than 500 ms or an  
517 error larger than 60° were excluded from the analyses. For the web-based experiment, 1.5% trials were  
518 removed. For the lab-based experiment, 0.4% of trials were removed.

519

520 To analyze the sequential effect in movement, we regressed out the influence of systematic bias.  
521 Specifically, we fitted a function between motor bias and target angle using a polynomial function with a

522 maximal power of 10 for each participant. We then subtracted this motor bias function from the motor  
523 error. The residual error was defined as motor “deviation” and applied to analyze the sequential  
524 effect<sup>13,24–26</sup>.

525  
526 To analyze the sequential bias of the movement direction, we measured the function of how motor  
527 deviation changed as a function of the difference of target position between trial N-1 and trial N (defined  
528 as  $\Delta\text{Target}$ ). A function lies in Quadrants II and IV will suggest that the movement error was in the opposite  
529 direction of the previous target. To quantify sequential bias, we introduced the SE index that takes the  
530 difference between the average error within  $-90^\circ\text{-}0^\circ \Delta\text{Target}$  and the average error within  $0^\circ\text{-}90^\circ \Delta\text{Target}$ .  
531 A positive SE index means a repulsive sequential effect and vice versa.

532  
533 To further examine how the variability in the motor system influences the sequential bias, we calculated  
534 the Pearson correlation between motor variance and the SE index, for Exp 1, Exp 5, and Exp 4 (only for  
535 trials after a standard trial). We did not perform the correlation analysis for Exp 2-3. The motor variance  
536 was very large in the no-feedback condition of Exp 2 compared to all other experiments, likely because of  
537 the drifting sensorimotor map without visual calibration<sup>59,60</sup>. As such, the motor variance in Exp 2 was not  
538 a good measurement of encoding variability. We also excluded Exp 3 given the temporal decay of the  
539 sequential effect due to the long ITI.

540  
541 To analyze the sequential effect in motor variance, we calculated the absolute difference between the  
542 movement N-1 and movement N ( $|\Delta\text{Hand}|$ ). We flipped the sign of the deviation if  $\Delta\text{Hand}$  was negative.  
543 Then we calculated the variance of deviation within each bin of  $30^\circ$ . The variance was then normalized by  
544 the average the average variance for each participant. To examine the tendency of how variance changed  
545 as a function of  $|\Delta\text{Hand}|$ , we applied a general linear model:

546 
$$variance = a + \frac{b-a}{e^{-c|\Delta\text{Hand}|}} \quad [1]$$

547 where  $a$ ,  $b$ ,  $c$  are the three free parameters. The SE index was defined as the change in the output of the  
548 function when  $|\Delta\text{Hand}|$  increases from  $30^\circ$  to  $150^\circ$ . To estimate the distribution of the SE index, we  
549 applied bootstrap resampling 1000 times.

550  
551  
552 To analyze the priming effect in the reaction direction, we normalized the reaction time (RT) by  
553 subtracting the average reaction of each participant. We then plotted a function of how the normalized

554 RT changes as a function of  $|\Delta\text{Target}|$ . The RT SE index is the difference between the average normalized  
555 RT within  $180^\circ\text{-}90^\circ$   $|\Delta\text{Target}|$  and the average RT within  $0^\circ\text{-}90^\circ$   $|\Delta\text{Target}|$ . Simple t-tests were conducted  
556 to determine whether the SE indexes were significantly different from 0. We confirmed that the data met  
557 the assumptions of a Gaussian distribution and homoscedasticity for all tests. The significance level was  
558 set at  $p < 0.05$  (two-tailed).

559

## 560 **Model**

### 561 Efficient coding model

562 We assumed that the motor system encodes a movement direction ( $m$ ) based on an observed target  
563 direction ( $\theta$ ) following the rule of efficient coding. This model is based on previous models of efficient  
564 coding in perception<sup>10,12,15</sup>. A key assumption of the model is that the encoding system allocates its  
565 resources to maximize the mutual information  $I[\theta, m]$  between input  $\theta$  and output  $m$ . By imposing a  
566 constraint to bound the total coding resources of the system<sup>10</sup>, this requires the Fisher information  $J(\theta)$  to  
567 be matched to the stimulus prior distribution ( $p(\theta)$ ):  $p(\theta) \propto J(\theta)$ . As such, coding resources are allocated  
568 such that the most likely movement direction is coded with the highest accuracy.

569

570 We next calculated the likelihood functions of how the system responds to different target directions with  
571 constraints of the prior distribution. Technically, the likelihood functions can be computed by assuming a  
572 symmetric Gaussian noise structure in a space where the Fisher information is uniform (the motor space,  
573  $\tilde{\theta}$ ), and then transforming those symmetric likelihood functions back to the target space ( $\theta$ ). To construct  
574 a motor space with uniform Fisher information based on the prior distribution of  $\theta$ , one defines a mapping  
575  $F$  from the target space ( $\theta$ ) to the motor space ( $\tilde{\theta}$ ), following<sup>10</sup>:

$$576 \quad \tilde{\theta} = F(\theta) = \int_0^\theta p(\chi) d\chi \quad [2]$$

577

578 Given an input  $\theta$ , the output  $m$  is computed as follows<sup>15</sup>. We first calculated the response value  $r$ , which  
579 would be of the form  $\theta + \epsilon$ , where  $\epsilon$  represents an error due to the intrinsic encoding noise of the system.  
580 Note that  $\epsilon$  follows an asymmetric distribution in the target space (Fig 1b). Let  $\tilde{\epsilon}$  represent the  
581 transformation of  $\epsilon$  to the motor space. Since we were assuming  $\tilde{\epsilon}$  has a symmetric Gaussian distribution,  
582 the response value in the motor space would be  $\tilde{r} = F(\theta) + \tilde{\epsilon}$ , where  $\tilde{\epsilon} \sim N(0, \sigma^2)$ ; which gives a  
583 response value in the target space of:

$$584 \quad r = F^{-1}(F(\theta) + \tilde{\epsilon}) \quad [3]$$

585

586 Next, we assumed that the system knows that its response  $r$  is noisy. Therefore, it generates a  
587 distribution of the form  $r + \delta$ , where  $\delta$  follows the same distribution as  $\epsilon$ . If  $\tilde{\delta}$  represents the  
588 transformation of  $\delta$  to the motor space, this distribution will be of the form  $F^{-1}(r + \delta)$ , where  
589  $\tilde{\delta} \sim N(0, \sigma^2)$ . Finally, the system returns the expected value of this distribution as the output  $m$ :

$$590 \quad m = E((F^{-1}(r + \delta)); \tilde{\delta}) \quad [4]$$

591

592 where  $E(X; z)$  means the expected  $X$  as  $z$  varies. We defined  $\phi(\tilde{\theta}) = F^{-1}(\tilde{\theta})$ . In the small-noise limit, we  
593 can take a second-order Taylor expansion:

$$594 \quad F^{-1}(F(\theta) + \epsilon) \approx F^{-1}(F(\theta)) + \phi'(F(\theta)) \times (\epsilon + \delta) + (1/2)\phi''(F(\theta)) \times (\epsilon + \delta)^2 \quad [5]$$

595

596 Considering [3]-[5] together, we have:

$$597 \quad m \approx \theta + \phi'(F(\theta))\epsilon + \frac{1}{2}\phi''(\sigma^2 + \epsilon^2) \quad [6]$$

598 To estimate the motor bias predicted by the model, we calculated the expected value of  $m$  ( $\hat{m}$ ) when  $\epsilon$   
599 varies can be expressed as:

$$600 \quad \hat{m} = E(m; \tilde{\epsilon}) \approx \theta + \phi'' \sigma^2 \quad [7]$$

601 And the variance of  $m$  across trials can be expressed as:

$$602 \quad \text{var}(m) \approx (\phi' \sigma)^2 \quad [8]$$

603

604 Since the sequential effect in movement is influenced principally by the last movement, we assumed the  
605 prior of the motor planning system is a mix of a uniform distribution across the whole space and a  
606 Gaussian distribution centered at the last target direction ( $\theta_{n-1}$ ):

$$607 \quad p(\theta) \propto k * U(0, 360) + (1 - k)N(\theta_{n-1}, \rho^2) \quad [9]$$

608 where  $k$  is a scale factor controlling the relative contribution of the two distributions;  $\rho$  indicates the width  
609 of influence from the previous trial. To simulate the bias and the variance predicted by this efficient coding  
610 model, we computed the numerical approximation of  $\phi''$  and  $\phi'$  based on this prior function using an  
611 incremental approach.

612

### 613 Repeated Suppression model

614 We considered two alternative models to explain the sequential effects in the motor planning. The first  
615 model is a repeated suppression model, which assumes that neurons tuned to a specific direction become

616 less sensitive after repeating a similar movement. Those modulations can enhance the sensitivity to the  
617 changes in the environment or/and encourage exploration. Here we applied a population coding model  
618 with a group of neurons with Gaussian-shaped tuning functions. For a target direction  $\theta$ , the unit tuned  
619 to  $i$  ( $i \in [0, \pi]$ ) direction generates a response  $r_i$  as follow:

$$620 \quad r_i = \text{Norm}(\theta, i, d) \quad [10]$$

621 where  $\text{Norm}(\theta, i, d)$  is the probability density function of a Gaussian distribution with a mean of  $i$  and  
622 standard deviation of  $d$ . The output of the system is determined by summing the activation of all neurons:

$$623 \quad \mathbf{m} = \sum_i s_i r_i \mathbf{v}_i \quad [11]$$

624 where  $\mathbf{v}_i$  is a vector representing the tuning direction of unit  $i$ ,  $\mathbf{m}$  is a vector pointing towards the  
625 movement direction, and  $s_i$  is the sensitivity of unit  $i$ . After a movement in trial  $n$ ,  $s_i$  is updated based on  
626 the strength of the activation in unit  $i$ :

$$627 \quad s_i(n+1) = 1 - a r_i(n) \quad [12]$$

628 where  $a \in [0, 1]$  is the suppression rate. As such, units that response more to the target in trial  $n$  will be  
629 more suppressed in the next trial.

630

### 631 Bayesian Decoding model

632 The second alternative model we applied is a classic Bayesian Decoding model that utilizes the prior  
633 distribution of  $\theta$  to improve performance<sup>20,21,61</sup>. The system generates a response  $r$  based on a target  
634 direction  $\theta$ . Considering Gaussian encoding noise, the relationship between  $r$  and  $\theta$  can be expressed as  
635 follows:

$$636 \quad p(r|\theta) = \text{Norm}(\theta, \sigma) \quad [13]$$

637 Importantly, the model assumes that the system utilizes both the prior and this likelihood function to form  
638 a posterior estimation following Bayesian rules:

$$639 \quad p(\theta|r) = \frac{p(\theta)p(r|\theta)}{p(r)} \quad [14]$$

640 where  $p(r)$  is a constant;  $p(\theta)$  is the prior;  $p(r|\theta)$  is the likelihood; and  $p(\theta|r)$  is the posterior. The  
641 output of the system ( $m$ ) is the posterior mean. For the Bayesian model, we used the same prior  
642 distribution (see [9]) as the efficient coding model.

643

644

### 645 **Funding**

646 David Whitney is funded by NIH R01CA236793.

647



648 **Acknowledgments**

649 We thank Richard Ivry for helpful discussions.

650

651 **Competing interests**

652 We have nothing to declare.

653

654 **Data availability**

655 All data and code are available at <https://github.com/shion707/MotorEC>.

656

657 **Reference**

658

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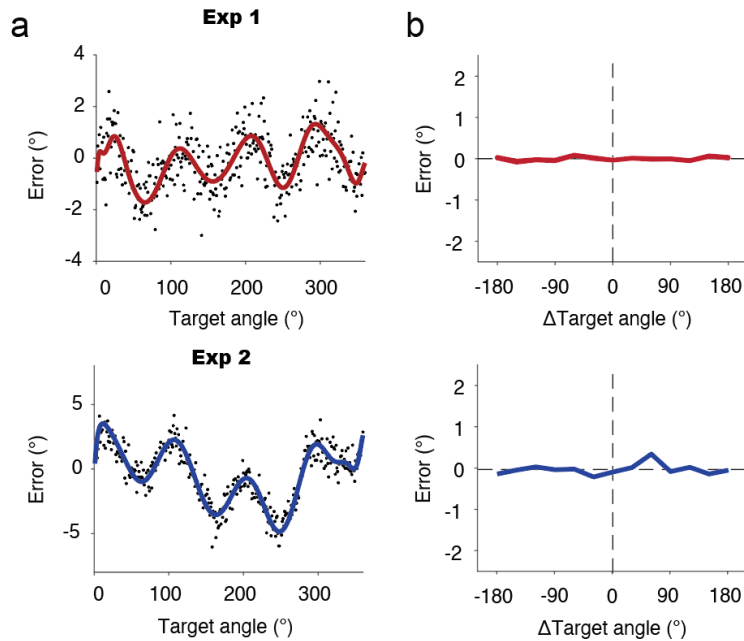
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779 **Supplementary figures**

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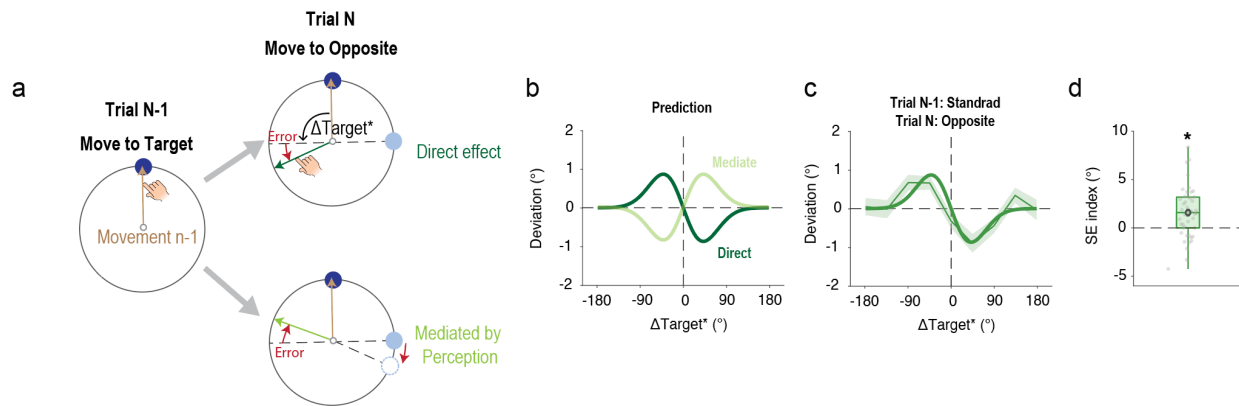


781

782 **Figure S1. Systematic motor biases did not generate sequential effects.** a) Systematic motor bias relative to target  
783 position in Exp 1 (upper panel) and 2 (lower panel). Participants exhibited greater bias in Exp 2, where feedback was  
784 absent. Black dots indicate data. The thick line represents a smoothed function, obtained by fitting a polynomial  
785 function with a maximum degree of 20. b) Simulation of sequential bias based on the motor bias function and the  
786 sequence of targets presented to participants. The systematic motor bias did not generate any sequential effect.

787

788



789

790 **Figure S2. The current movement was directly influenced by the previous movement, with no mediation of**

791 **perception.** a) When trial N was an Opposite trial and trial N-1 was a Standard trial, it allowed for examination of

792 whether the effect was directly caused by the previous movement repelling the current movement (direct

793 hypothesis). Alternatively, it could be that the previous movement repelled the perception of the current target's

794 position, thus indirectly influencing the movement direction (mediated hypothesis). Here,  $\Delta Target^*$  was defined as

795 the difference between the opposite position of the current target and the position of the previous target. b)

796 Different predictions of the sequential bias following the direct hypothesis and mediated hypothesis, respectively.

797 c) Sequential bias observed in Exp 3 was consistent with the direct hypothesis. The thin lines with shaded error bars

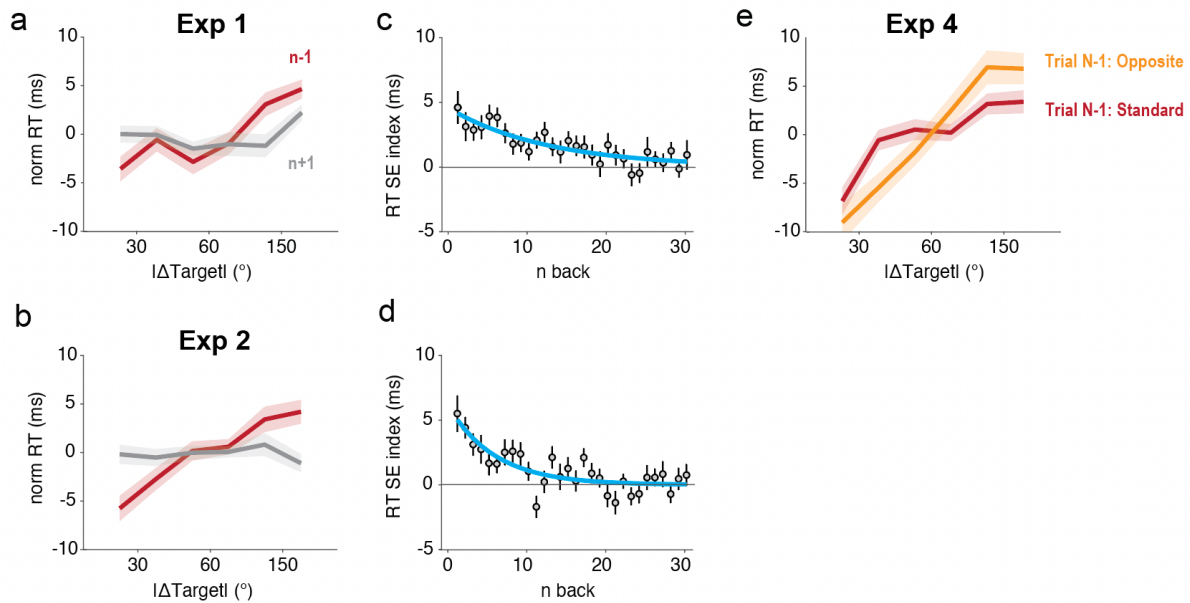
798 indicate data, and the thick curve indicates the prediction of the efficient coding model. Shaded areas indicate

799 standard error. d) SE index indicates that the current movement was significantly repelled away from the previous

800 movement. \*,  $p < .001$ .

801





802

803 **Figure S3. Priming of Reaction Times.** a-b) Reaction time increased when the target in the previous (n-1) trial was

804 further away from the current (n) trial in Exp 1-2. Reaction time was not correlated with the future trial (n+1). c-d)

805 The SE index for reaction time lasted for more than 10 trials, differing from the temporal dynamics of sequential

806 effects in movement direction or motor variance. e) The priming of reaction time was similar after an Opposite trial

807 or a Standard trial in Exp 4, suggesting that the reaction time priming is mainly associated with previous target

808 detection or localization.

809