# Lanthanide(III) Complexes Based on an 18-Membered Macrocycle Containing Acetamide Pendants. Structural Characterization and paraCEST Properties 

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#### Abstract

We report a detailed investigation of the coordination properties of macrocyclic lanthanide complexes containing a 3,6,10,13-tetraaza-1,8(2,6)-dipyridinacyclotetradecaphane scaffold functionalized with four acetamide pendant arms. The X-ray structures of the complexes with the large $\mathrm{Ln}^{3+}$ ions ( La and Sm ) display 12- and 10 -coordinated metal ions, where the coordination sphere is fulfilled by the six N atoms of the macrocycle, the four O atoms of the acetamide pendants, and a bidentate nitrate anion in the $\mathrm{La}^{3+}$ complex. The analogous $\mathrm{Yb}^{3+}$ complex presents, however, a 9coordinated metal ion because one of the acetamide pendant arms remains uncoordinated. ${ }^{1} \mathrm{H}$ NMR studies indicate that the $10-$ coordinated form is present in solution throughout the lanthanide series from La to Tb , while the smaller lanthanides form 9-  coordinated species. ${ }^{1} \mathrm{H}$ and ${ }^{89} \mathrm{Y}$ NMR studies confirm the presence of this structural change because the two species are present in solution. Analysis of the ${ }^{1} \mathrm{H}$ chemical shifts observed for the $\mathrm{Tb}^{3+}$ complex confirms its $D_{2}$ symmetry in aqueous solution and evidences a highly rhombic magnetic susceptibility tensor. The acetamide resonances of the $\mathrm{Pr}^{3+}$ and $\mathrm{Tb}^{3+}$ complexes provided sizable paraCEST effects, as demonstrated by the corresponding Z spectra recorded at different temperatures and studies on tube phantoms recorded at $22^{\circ} \mathrm{C}$.


## INTRODUCTION

Magnetic resonance imaging (MRI) is a technique commonly used in medical diagnosis that provides three-dimensional images of soft tissues with very high resolution and unlimited depth penetration. ${ }^{1}$ MRI takes advantage of the ${ }^{1} \mathrm{H}$ NMR signal of water proton nuclei present in the body, generating contrast due to changes in the density of protons and their longitudinal $\left(T_{1}\right)$ or transverse $\left(T_{2}\right)$ relaxation times. ${ }^{2}$ Both $T_{1}$ and $T_{2}$ can be shorted in the surrounding of paramagnetic species such as $\mathrm{Gd}^{3+}$ or $\mathrm{Mn}^{2+}$ chelates, and thus complexes of these metal ions were proposed as contrast agents about 4 decades ago, ${ }^{3}$ subsequently entering clinical practice. ${ }^{4}$

The continuous interest of the MRI community in $\mathrm{Gd}^{3+}$ based and, to a lesser extent, $\mathrm{Mn}^{2+}$-based contrast agents generated a number of molecular systems with improved properties. This contributed significantly to obtaining new insights in the coordination chemistry of these metal ions in aqueous media. ${ }^{5,6}$ Furthermore, a wide range of the so-called smart or responsive contrast agents were designed to provide a response to different physiologically relevant parameters, such as the pH , temperature, or presence of anions or cations relevant in vivo. ${ }^{7}$ The main drawback of the responsive $\mathrm{Gd}^{3+}$ probes is the difficulty of their direct detection: they operate by
modifying the NMR signal of water proton nuclei already present in the body, which causes the presence of significant background signals. As a consequence, quantification of the response of $\mathrm{Gd}^{3+}$ contrast agents in vivo remains a difficult task because the observed signal depends both on the physiological parameter that induces relaxivity changes and on the probe concentration. ${ }^{8}$

Paramagnetic contrast agents relying on the chemical exchange saturation transfer (paraCEST) approach have attracted great attention during the last 2 decades as alternatives to the Gd- or Mn-based probes. ${ }^{9}$ These agents possess exchangeable protons (typically amide, hydroxyl, or coordinated water molecules) in intermediate-to-slow exchange with bulk water. The paramagnetic shift induced by the metal ion moves the signal of exchangeable protons away

[^0]from that of bulk water. Consequently, the application of a presaturation pulse at the frequency of the exchanging protons transfers the energy from the saturated spins to the water pool, which decreases its signal intensity. ${ }^{10}$ The relatively large chemical shift difference between the signals of exchangeable protons and bulk water $(\Delta \omega)$, induced by the paramagnetic ion, implies that the proton exchange rate ( $k_{\mathrm{ex}}$ ) can be faster, while still maintaining the slow-to-intermediate exchange regime $\left(k_{\text {ex }} \leq \Delta \omega\right)$ to observe the CEST effect. ${ }^{11}$ Moreover, the paramagnetic shift can, in some cases, cause the differentiation of two nonequivalent exchangeable protons to result in two separate CEST signals. This feature is beneficial because it allows for ratiometric analyses and thus possibly quantitative estimation of the physiological parameters. ${ }^{12}$

Because of such an advantageous prospective, complexes of both paramagnetic lanthanide and transition-metal ions were extensively investigated as potential paraCEST candidates. ${ }^{13-15}$ In the particular case of lanthanide ions, most of the complexes investigated in this context were derivatives of cyclen because this type of chelator often forms very stable and inert complexes when functionalized with four pendant arms. ${ }^{16}$ However, azamacrocyclic platforms other than cyclen were also investigated as possible chelators to form inert complexes with affirmative CEST features. For instance, the 18 -membered macrocyclic ligand $\mathrm{L}^{1}$ (Chart 1) was functionalized with

Chart 1. Ligands Discussed in the Present Work

$L^{1}$

$\mathrm{L}^{3}$

$L^{5}$

$L^{2}$

$L^{4}$

$L^{6}$
different pendant arms to accommodate the high coordination numbers usually observed for the $\mathrm{Ln}^{3+}$ ions in solution. Along these lines, the derivatives containing acetate ${ }^{17}$ and methylenephosphonic acid ${ }^{18}$ groups ( $\mathrm{L}^{2}$ and $\mathrm{L}^{3}$, respectively) were prepared and reported more than 15 years ago. Moreover, the same macrocyclic platform was also functionalized with neutral pyridyl ${ }^{19}$ and hydroxyethyl ${ }^{20,21}$ pendant arms ( $\mathrm{L}^{4}$ and $\mathrm{L}^{5}$ ). This family of ligands generally provides 10 -coordinated complexes, although in some cases, decoordination of one of the pendant arms is observed along the second half of the lanthanide series. Interestingly, the $\left[\mathrm{LnL}^{5}\right]^{3+}$ complexes containing hydroxyl groups were found to be exceptionally inert with respect to complex dissociation, remaining intact in a 1 M HCl solution over periods of months. Finally, in a recent work, we reported the derivative $L^{6}$ containing acetamide pendants and demonstrated that its $\mathrm{Eu}^{3+}$ complex displays high kinetic inertness and provides a strong pH -sensitive CEST effect due to the amide protons. ${ }^{22}$

Following these encouraging results, we performed further studies with this promising chelator. Herein we report a detailed investigation of the structure of several lanthanide complexes of $\mathrm{L}^{6}$, both in the solid state and in solution. The Xray structures of three complexes are presented $\left(\mathrm{La}^{3+}, \mathrm{Sm}^{3+}\right.$, and $\left.\mathrm{Yb}^{3+}\right)$. The structure in solution was assessed through a detailed study of the ${ }^{1} \mathrm{H}$ and ${ }^{89} \mathrm{Y}$ NMR spectra, including a detailed analysis of the paramagnetic shifts observed for the $\mathrm{Tb}^{3+}$ derivative. Finally, the paraCEST spectra of the $\mathrm{Pr}^{3+}$ and $\mathrm{Tb}^{3+}$ complexes recorded at different temperatures are presented and analyzed quantitatively using the BlochMcConnell (BM) theory to determine the exchange rates of amide protons.

## RESULTS AND DISCUSSION

Synthesis and Characterization of the Ligand and Metal Complexes. Ligand $\mathrm{L}^{6}$ was obtained by alkylation of the 3,6,10,13-tetraaza-1,8(2,6)-dipyridinacyclotetradecaphane precursor $\left(\mathrm{L}^{1}\right)^{23}$ with bromoacetamide, as described previously. ${ }^{22}$ Compounds with the formula $\left[\mathrm{LnL}^{6}\right]\left(\mathrm{NO}_{3}\right)_{3} \cdot x \mathrm{H}_{2} \mathrm{O}$ ( $\mathrm{La}-\mathrm{Lu}$, except Pm and $\mathrm{Eu}, x=2-4$ ) were isolated with good yields ( $59-86 \%$ ) after direct reaction in methanol of $L^{6}$ with the corresponding hydrated lanthanide nitrate. The peaks due to the $\left[\operatorname{Ln}\left(\mathrm{L}^{6}-\mathrm{H}\right)\left(\mathrm{NO}_{3}\right)\right]^{+}$and $\left[\operatorname{Ln}\left(\mathrm{L}^{6}-2 \mathrm{H}\right)\right]^{+}$entities observed in the mass spectrometry (MS) spectra (positive-mode electrospray ionization, $\mathrm{ESI}^{+}$) confirm formation of the complexes.

X-ray Crystal Structures. Crystals of $\left[\mathrm{LaL}^{6}\left(\mathrm{NO}_{3}\right)\right]_{2}[\mathrm{La}-$ $\left.\left(\mathrm{NO}_{3}\right)_{6}\right] \cdot \mathrm{NO}_{3} \cdot 4 \mathrm{CH}_{3} \mathrm{OH}$ were obtained by the slow evaporation of a methanolic solution of the ligand containing an excess of $\mathrm{La}\left(\mathrm{NO}_{3}\right)_{3}$. This compound crystallizes in the centrosymmetric $C 2 / c$ monoclinic space group, and the asymmetric unit encompasses the $\left[\mathrm{LaL}^{6}\left(\mathrm{NO}_{3}\right)\right]^{2+}$ complex, half of a $\left[\mathrm{La}\left(\mathrm{NO}_{3}\right)_{6}\right]^{3-}$ anion, half of a nitrate anion, and two methanol molecules. The $\left[\mathrm{La}\left(\mathrm{NO}_{3}\right)_{6}\right]^{3-}$ entity (Figure S1) was previously found in crystals of different cationic $\mathrm{La}^{3+}$ complexes, presumably aiding crystallization because of its large size. ${ }^{24}$

The $\left[\mathrm{LaL}^{6}\left(\mathrm{NO}_{3}\right)\right]^{2+}$ cation shows that the $\mathrm{La}^{3+}$ ion is coordinated by the six N atoms of the macrocycle skeleton, the four O atoms from the amide groups, and two of the O atoms of a nitrate group acting as a bidentate ligand, which results in coordination number 12. The bond distances of the metal coordination environment are collected in Table 1, while a view of the structure of the complex is presented in Figure 1.

Table 1. Bond Distances ( $\AA$ ) of the Metal-Coordination Spheres Obtained for the $\left[\mathrm{LnL}^{6}\right]^{3+}$ Complexes with X-ray Diffraction Measurements

|  | La | Sm | Yb |
| :--- | :---: | :---: | :---: |
| $\operatorname{Ln}(1)-\mathrm{N}(1)$ | $2.865(7)$ | $2.589(8)$ | $2.4787(16)$ |
| $\operatorname{Ln}(1)-\mathrm{N}(2)$ | $2.919(7)$ | $2.641(8)$ | $2.6436(17)$ |
| $\operatorname{Ln}(1)-\mathrm{N}(3)$ | $2.841(6)$ | $2.672(8)$ | $2.5790(17)$ |
| $\operatorname{Ln}(1)-\mathrm{N}(4)$ | $2.826(6)$ | $2.572(7)$ | $2.4831(16)$ |
| $\operatorname{Ln}(1)-\mathrm{N}(5)$ | $2.876(6)$ | $2.659(8)$ | $2.6278(16)$ |
| $\operatorname{Ln}(1)-\mathrm{N}(6)$ | $2.887(6)$ | $2.669(8)$ | $2.5467(16)$ |
| $\operatorname{Ln}(1)-\mathrm{O}(1)$ | $2.569(6)$ | $2.511(7)$ | $2.3135(14)$ |
| $\operatorname{Ln}(1)-\mathrm{O}(2)$ | $2.622(5)$ | $2.487(8)$ | $2.2704(14)$ |
| $\operatorname{Ln}(1)-\mathrm{O}(3)$ | $2.611(5)$ | $2.573(8)$ |  |
| $\operatorname{Ln}(1)-\mathrm{O}(4)$ | $2.654(5)$ | $2.535(7)$ | $2.2746(14)$ |
| $\operatorname{Ln}(1)-\mathrm{O}(1 \mathrm{~N})$ | $2.733(6)$ |  |  |
| $\operatorname{Ln}(1)-\mathrm{O}(2 \mathrm{~N})$ | $2.710(5)$ |  |  |



Figure 1. Structure of the $\left[\mathrm{LaL}^{6}\left(\mathrm{NO}_{3}\right)\right]^{2+}$ cation present in crystals of $\left[\mathrm{LaL}^{6}\left(\mathrm{NO}_{3}\right)\right]_{2}\left[\mathrm{La}\left(\mathrm{NO}_{3}\right)_{6}\right] \cdot \mathrm{NO}_{3} \cdot 4 \mathrm{CH}_{3} \mathrm{OH} . \mathrm{H}$ atoms are omitted for simplicity. The ORTEP plot is at the $30 \%$ probability level.

The coordination polyhedron around the $\mathrm{La}^{3+}$ ion can best be described as a twisted icosahedron (Figure S2), as indicated by the analysis performed with the SHAPE program. ${ }^{25,26}$ The nitrate anion in $\left[\mathrm{LaL}^{6}\left(\mathrm{NO}_{3}\right)\right]^{2+}$ provides a slightly asymmetric bidentate coordination, with $\mathrm{La}-\mathrm{O}$ distances similar to those reported for other 12 -coordinated $\mathrm{La}^{3+}$ complexes containing bidentate ligands. ${ }^{27}$

The $\left[\mathrm{LaL}^{6}\left(\mathrm{NO}_{3}\right)\right]^{2+}$ complex presents an unprecedented conformation of the ligand in which the four pendant arms of $L^{6}$ are oriented to the same side of the macrocyclic unit, giving a syn conformation. The macrocyclic unit is not folded or twisted but shows a plateau conformation. The four amine N atoms define a least-squares plane [root-mean-square (rms) = $0.238 \AA$ ] that contains the $\mathrm{La}^{3+}$ ion, while the pyridine N atoms are ca. $1.07 \AA$ below that plane. As a result, the $\mathrm{N}(4)-$ $\mathrm{La}(1)-\mathrm{N}(1)$ angle $\left[125.17(19)^{\circ}\right.$ ] is not linear. The pyridyl units are slightly tilted with respect to each other, with the least-squares planes intersecting at $28.2^{\circ}$. The two chelate rings associated with binding of the ethylenediamine units adopt the
same conformation, which can be defined as $\delta \delta$ or $\lambda \lambda .{ }^{28}$ The layout of the four acetamide pendant groups provides the second source of chirality, leading to the presence of (centrosymmetrically related) $\Lambda(\lambda \lambda)$ or $\Delta(\delta \delta)$ enantiomers in the crystal lattice. ${ }^{29}$

Crystals of the formula $\left[\mathrm{SmL}^{6}\right]\left(\mathrm{NO}_{3}\right)_{2.91} \cdot \mathrm{Br}_{0.09}$ and $\left[\mathrm{YbL}^{6}\right]$ $\left(\mathrm{NO}_{3}\right)_{2.7} \cdot \mathrm{Br}_{0.3} \cdot 3 \mathrm{H}_{2} \mathrm{O}$ were obtained by the slow evaporation of an aqueous solution of the complex. The small fraction of bromide anions present in these crystals is likely due to the presence of KBr impurities in the batch of ligands used for preparation of the complex. $\mathrm{Sm}^{3+}$ crystals also contain the $\left[\mathrm{SmL}^{6}\right]^{3+}$ cation (Figure 2) and nitrate anions. This compound


Figure 2. Structure of the $\left[\mathrm{SmL}^{6}\right]^{3+}$ cation present in crystals of $\left[\mathrm{SmL}^{6}\right]\left(\mathrm{NO}_{3}\right)_{2.91} \cdot \mathrm{Br}_{0.09} . \mathrm{H}$ atoms are omitted for simplicity. The ORTEP plot is at the $30 \%$ probability level.
crystallizes in the noncentrosymmetric monoclinic $C_{2}$ space group, and the asymmetric units contain one and two halves of the $\left[\mathrm{LnL}^{6}\right]^{3+}$ units, six nitrate anions, and water molecules.

The $\left[\mathrm{SmL}^{6}\right]^{3+}$ cation contains a 10 -coordinated metal ion that is directly coordinated by the six donor atoms of the macrocyclic fragment and the four O atoms of the acetamide pendants. The overall structure is very similar to that reported previously for the $\mathrm{Eu}^{3+}$ and $\mathrm{Y}^{3+}$ derivatives. ${ }^{22}$ The ligand adopts a twist-wrap conformation characterized by a nearly linear $\mathrm{N}(1)-\mathrm{Sm}(1)-\mathrm{N}(4)$ angle $\left[179.3(4)^{\circ}\right] .{ }^{17}$ The pyridyl rings are twisted with respect to the $\mathrm{N}(1)-\mathrm{Sm}(1)-\mathrm{N}(4)$ axis, with their least-squares planes intersecting at $18.2^{\circ}$. The (5membered) chelate rings generated by coordination of the ethylenediamine groups adopt identical conformations [ $(\delta \delta)$ or $(\lambda \lambda)]$. The coordination polyhedron can best be defined as a sphenocorona (Figure S3), ${ }^{30}$ where the quadrangular faces are defined by $\mathrm{N}(1), \mathrm{N}(2), \mathrm{O}(1)$, and $\mathrm{O}(3)(\mathrm{rms}=0.234 \AA)$ and $\mathrm{O}(1), \mathrm{O}(3), \mathrm{N}(4)$, and $\mathrm{N}(5)(\mathrm{rms}=0.228 \AA)$.

Crystals of the $\mathrm{Yb}^{3+}$ compound contain the $\left[\mathrm{YbL}^{6}\right]^{3+}$ complex, in which the metal ion is 9 -coordinated by the ligand (Figure 3). One of the acetamide pendant arms remains uncoordinated, with the ligand adopting a twist-fold conformation characterized by a $\mathrm{N}(1)-\mathrm{Yb}(1)-\mathrm{N}(4)$ angle of $144.04(5)^{\circ}$ and a dihedral angle between the pyridine units of


Figure 3. Structure of the $\left[\mathrm{YbL}^{6}\right]^{3+}$ cation present in crystals of $\left[\mathrm{YbL}^{6}\right]\left(\mathrm{NO}_{3}\right)_{2.7} \cdot \mathrm{Br}_{0.3} \cdot 3 \mathrm{H}_{2} \mathrm{O}$. H atoms are omitted for simplicity. The ORTEP plot is at the $30 \%$ probability level.
72.4(1) ${ }^{\circ}$. A similar structure was found for complexes formed by the carboxylate analogue $\mathrm{L}^{2}$ and the heaviest lanthanide ions. ${ }^{17}$ Changes in the coordination number from 10 to 9 across the lanthanide series coming as a result of lanthanide contraction are fairly common. ${ }^{31}$ The coordination geometry is close to a spherical tricapped trigonal prism (Figure S4). The upper tripod of the polyhedron is defined by $\mathrm{O}(1), \mathrm{O}(4)$, and $\mathrm{N}(5)$, while the lower tripod contains $\mathrm{N}(3), \mathrm{N}(1)$, and $\mathrm{O}(2)$. These two triangular faces are almost parallel, intersecting at $3.6^{\circ}$. The capping tripod is occupied by $\mathrm{N}(2), \mathrm{N}(4)$, and $\mathrm{N}(6)$.

The syn structure of the $\mathrm{La}^{3+}$ complex is characterized by $\mathrm{Ln}-\mathrm{N}$ distances involving the pyridyl donor atoms [ $\mathrm{N}(1)$ and $\mathrm{N}(4)$ ] comparable to those with amine N atoms. However, the $\mathrm{Ln}-\mathrm{N}(1)$ and $\mathrm{Ln}-\mathrm{N}(4)$ bonds are significantly shorter than those involving amine N atoms in $\left[\mathrm{SmL}^{6}\right]^{3+}$ and $\left[\mathrm{YbL}^{6}\right]^{3+}$, a situation that is commonly observed when the pendant arms coordinate from both sides of the macrocyclic mean plane. ${ }^{17-22}$ The $\mathrm{Sm}-\mathrm{O}$ and $\mathrm{Sm}-\mathrm{N}$ distances observed for the $\left[\mathrm{SmL}^{6}\right]^{3+}$ complex are very similar to those observed for the carboxylate analogue $\left[\mathrm{SmHL}^{2}\right] .{ }^{17}$ The $\mathrm{Yb}-\mathrm{O}$ distances in $\left[\mathrm{YbL}^{6}\right]^{3+}$ are in the normal range observed for 9 -coordinated $\mathrm{Yb}^{3+}$ complexes containing amide pendant groups. ${ }^{32}$

Structures of the Complexes in Solution. The ${ }^{1} \mathrm{H}$ NMR spectrum of diamagnetic $\left[\mathrm{LaL}^{6}\right]^{3+}$ recorded in a $\mathrm{D}_{2} \mathrm{O}$ solution is rather complex, which indicates the presence of two species in solution (Figure 4, spectrum a). The spectrum changes slowly and irreversibly with time, a process that speeds up upon heating of the solution. The spectrum obtained after heating is well-resolved, showing the eight signals expected for a $D_{2}$ symmetry in solution. We attribute this behavior to the formation of a kinetic species with a syn conformation of the macrocycle, as observed in the X-ray structure ( $C_{2}$ symmetry), which evolves to the thermodynamically stable species with $D_{2}$


| 9.0 | 8.0 | 7.0 | 6.0 | 5.0 | 4.0 | 3.0 | 2.0 | 1.0 |
| :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- |

Figure 4. ${ }^{1} \mathrm{H}$ NMR spectra of $\left[\mathrm{LaL}^{6}\right]^{3+}\left(\mathrm{D}_{2} \mathrm{O}, 400 \mathrm{MHz}, \mathrm{pH} 7.0,25\right.$ ${ }^{\circ} \mathrm{C}$ ): (a) immediately after dissolution of the complex; (b) after 3 days at RT; (c) after heating of the solution at $80^{\circ} \mathrm{C}$ for 10 min .
symmetry in solution. The spectrum of the $\mathrm{Ce}^{3+}$ complex is poorly defined, likely for the same reason.

The complexes with $\mathrm{Pr}^{3+}, \mathrm{Nd}^{3+}, \mathrm{Sm}^{3+}, \mathrm{Eu}^{3+}$, and $\mathrm{Tb}^{3+}$ present well-resolved spectra with eight paramagnetically shifted resonances, which points to a $D_{2}$ symmetry of the complexes in solution (Figures 5 and $\mathrm{S} 5-\mathrm{S} 8$ ). These results are in full agreement with the X-ray structures described above. The ${ }^{1} \mathrm{H}$ NMR spectra of the $\left[\mathrm{LnL}^{6}\right]^{3+}$ complexes ( $\mathrm{Ln}=\operatorname{Pr}-$ Tb , except Pm ) were assigned on the basis of COSY spectra and line-width analysis (Table 2). The observed chemical shifts are similar to those previously reported for the $\left[\operatorname{LnL}^{5}\right]^{3+}$


Figure 5. ${ }^{1} \mathrm{H}$ NMR spectrum of the $\left[\mathrm{TbL}^{6}\right]^{3+}$ complex recorded in a $\mathrm{D}_{2} \mathrm{O}$ solution ( $400 \mathrm{MHz}, \mathrm{pH} 7.0,25^{\circ} \mathrm{C}$ ) and plot of the experimental ${ }^{1} \mathrm{H}$ NMR shifts versus those calculated from the contact and pseudocontact contributions (see the text). The red line is the identity line.

Table 2. ${ }^{1} \mathrm{H}$ NMR Shifts $\left(\mathrm{D}_{2} \mathrm{O}, 25{ }^{\circ} \mathrm{C}, \mathrm{pH} 7.0,400 \mathrm{MHz}\right)$ Observed for $\left[\mathrm{LnL}^{6}\right]^{3+}$ Complexes $^{\boldsymbol{a}}$

|  | H1 | H2 | H3ax | H3eq | H4ax | H4eq | H5ax | H5eq |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| La ${ }^{\text {b }}$ | 8.04 | 7.58 | 3.98 | 4.68 | 2.84 | 3.30 | 3.58 | 3.87 |
| Ce | 9.92 | 8.64 | 14.10 | 9.92 | 15.26 | 13.89 | -8.08 | 2.25 |
| Pr | 9.40 | 10.28 | 20.56 | 15.53 | 22.32 | 23.48 | -15.20 | 4.08 |
| Nd | 13.83 | 15.22 | 14.45 | 15.22 | 1.49 | 12.22 | -6.64 | 1.19 |
| $\mathrm{Sm}^{c}$ | 8.36 | 8.07 | 7.00 | 4.82 | 4.43 | 3.15 | 1.52 | 2.73 |
| Eu | 2.45 | -0.77 | -9.43 | -15.05 | -1.62 | -19.13 | 18.50 | 0.72 |
| Tb | 15.20 | 24.79 | 133.14 | 44.08 | 133.14 | 68.63 | -130.44 | -24.14 |

${ }^{a}$ See Chart 1 for labeling. ${ }^{b_{3}} J_{1,2}={ }^{3} J_{2,1}=7.9 \mathrm{~Hz} ;{ }^{2} J_{3 \mathrm{ax}, 3 \mathrm{eq}}={ }^{2} J_{3 \text { eq }, 3 \mathrm{ax}}=15.9 \mathrm{~Hz} ;{ }^{3} J_{4 a x, 4 e q}={ }^{3} J_{\text {4eq }, 4 \mathrm{ax}}=10.0 \mathrm{~Hz} ;{ }^{2} J_{\text {Sax, }, \text { eq }}={ }^{2} J_{\text {Seq, }, 5 \mathrm{ax}}=16.6 \mathrm{~Hz} .{ }^{c} J_{1,2}={ }^{3} J_{2,1}=$


Table 3. Paramagnetic ${ }^{1} \mathrm{H}$ NMR Shifts ( $\delta^{\text {para }}, \mathrm{D}_{2} \mathrm{O}, 25^{\circ} \mathrm{C}, \mathrm{pH} 7.0,400 \mathrm{MHz}$ ), Hyperfine Coupling Constants $(A / \hbar)$, and Pseudocontact and Contact and Contributions Obtained for the [ $\left.\mathrm{TbL}^{6}\right]^{3+}$ Complex ${ }^{a}$

|  | H1 | H2 | H3ax | H3eq | H4ax | H4eq | H5ax | H5eq |
| :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- |
| $\delta^{\text {para }}$ | 7.16 | 17.21 | 129.16 | 39.4 | 130.3 | 65.33 | -134.02 |  |
| $A / \hbar / 10^{6} \mathrm{rad} \mathrm{s}^{-1 b}$ | -0.0271 | -0.0253 | 0.07848 | -0.3145 | 0.00000 | -0.5870 | 0.10267 | -28.01 |
| $\delta^{\text {con }}$ | -1.67 | -1.56 | 4.85 | -19.43 | 0.00 | -36.27 | 6.34 | -15.76 |
| $\delta^{\text {pson }}$ | 8.83 | 18.77 | 124.31 | 58.83 | 130.3 | 101.6 | -140.36 | -12.25 |

${ }^{a}$ See Chart 1 for labeling. ${ }^{b}$ Calculated for $\left[\mathrm{GdL}^{6}\right]^{3+}$ at the TPSSh/SCRECP/EPR-III level (see the Computational Details).
complexes, ${ }^{21}$ indicating similar magnetic anisotropies and thus similar solution structures. ${ }^{33}$

The structure in solution of the $\left[\mathrm{TbL}^{6}\right]^{3+}$ complex was further investigated by analyzing the observed ${ }^{1} \mathrm{H}$ NMR shifts, which are the result of diamagnetic ( $\delta^{\text {dia }}$ ) and paramagnetic ( $\delta^{\text {para }}$ ) contributions (eq 1 ).

$$
\begin{equation*}
\delta^{\mathrm{obs}}=\delta^{\mathrm{dia}}+\delta^{\mathrm{para}}=\delta^{\mathrm{dia}}+\delta^{\mathrm{con}}+\delta^{\mathrm{pscon}} \tag{1}
\end{equation*}
$$

The diamagnetic contributions to the observed shifts were obtained from the chemical shifts observed for the diamagnetic $\left[\mathrm{LaL}^{6}\right]^{3+}$ analogue (Table 2). The paramagnetic shifts induced by $\mathrm{Tb}^{3+}$ are the result of both the contact ( $\delta^{\text {con }}$ ) and pseudocontact ( $\delta^{\text {pscon }}$ ) mechanisms, ${ }^{34}$ but only the latter encodes information on the position of the observed nuclei with respect to the paramagnetic center. Thus, we estimated the contact contributions by calculating the hyperfine coupling constants $A / \hbar$ responsible for the contact shifts using density functional theory (DFT). Contact shifts are directly proportional to the hyperfine coupling constant at the observed nuclei, as given by eq 2 , where $\left\langle S_{z}\right\rangle$ is the spin expectation value of the lanthanide ion, ${ }^{35} \gamma_{\mathrm{I}}$ is the nuclear gyromagnetic ratio, $k$ is the Boltzmann constant, and $\beta$ is the Bohr magneton. ${ }^{36}$

$$
\begin{equation*}
\delta^{\mathrm{con}}=\left\langle S_{z}\right\rangle \frac{\beta}{3 k T \gamma_{\mathrm{I}}} \frac{A}{\hbar} \times 10^{6} \tag{2}
\end{equation*}
$$

The values of $A / \hbar$ were estimated using calculations on the $\left[\mathrm{GdL}^{6}\right]^{3+}$ analogue, following the methodology reported previously. ${ }^{37}$ DFT provides a 10 -coordinated structure for $\left[\mathrm{GdL}^{6}\right]^{3+}$ very similar to those observed in the solid state for the $\mathrm{Sm}^{3+}, \mathrm{Eu}^{3+}$, and $\mathrm{Y}^{3+}$ derivatives (Figure S9). Contact shifts were subsequently obtained by using $\left\langle S_{z}\right\rangle=22.0 .^{21}$

Separation of the contact and pseudocontact shifts shows that the paramagnetic shifts are generally dominated by the pseudocontact mechanism, with the contact shift being more important for equatorial protons (Table 3). This has been attributed to distinct $\mathrm{Ln}-\mathrm{N}-\mathrm{C}-\mathrm{H}$ dihedral angles characterizing the axial $\left(\sim 80^{\circ}\right)$ and equatorial $\left(\sim 175^{\circ}\right)$ protons because contact shifts show a Karplus-like behavior on this angle. ${ }^{37}$

The pseudocontact contribution can be expressed as in eq 3 if the reference frame coincides with the main directions of the magnetic susceptibility tensor $\chi^{38}$ where $r=\sqrt{x^{2}+y^{2}+z^{2}}$ and $x, y$, and $z$ are the Cartesian coordinates of the observed nucleus relative to the position of a $\mathrm{Ln}^{3+}$ ion placed at the origin, while $\Delta \chi_{\mathrm{ax}}$ and $\Delta \chi_{\mathrm{rh}}$ are the axial and rhombic components of the diagonalized magnetic susceptibility tensor.

$$
\begin{equation*}
\delta^{\mathrm{pscon}}=\frac{1}{12 \pi r^{3}}\left[\Delta \chi_{\mathrm{ax}}\left(\frac{3 z^{2}-r^{2}}{r^{2}}\right)+\frac{3}{2} \Delta \chi_{\mathrm{rh}}\left(\frac{x^{2}-y^{2}}{r^{2}}\right)\right] \tag{3}
\end{equation*}
$$

A comparison of the experimental and calculated pseudocontact shifts, obtained with the geometry of $\left[\mathrm{TbL}^{6}\right]^{3+}$ optimized by means of DFT, is presented in Figure 5 (see also Table S1). The excellent agreement between the two sets of data unambiguously establishes that the $\left[\mathrm{TbL}^{6}\right]^{3+}$ complex presents a structure in solution very similar to that observed in the solid state for the $\mathrm{Sm}^{3+}$ and $\mathrm{Eu}^{3+}$ analogues (see also Figure 5).

The best fit of the data provided a highly rhombic susceptibility tensor characterized by $\Delta \chi_{\mathrm{ax}}=-20.5 \pm 0.5 \times$ $10^{-32}$ and $\Delta \chi_{\mathrm{rh}}=-19.9 \pm 1.1 \times 10^{-32} \mathrm{~m}^{3}$. These values are very similar to those determined previously for $\left[\mathrm{TbL}^{5}\right]^{3+}$, confirming that the two complexes present similar structures in solution.

The ${ }^{1} \mathrm{H}$ NMR spectra of the complexes with the heaviest $\mathrm{Ln}^{3+}$ ions (Dy-Lu) are complicated likely because of the fact that one of the pendant arms of the ligand is not coordinated to the $\mathrm{Ln}^{3+}$ ion, which is in line with the X-ray structure of the $\mathrm{Yb}^{3+}$ complex. The spectrum of the $\mathrm{Yb}^{3+}$ complex is welldefined, showing 30 signals expected for a 9 -fold coordination of the ligand in the range $\sim 151$ to -70 ppm (Figure S10).

The ${ }^{1} \mathrm{H}$ NMR spectrum of the $\left[\mathrm{YL}^{6}\right]^{3+}$ complex displays two sets of signals, one due to a symmetrical $D_{2}$ species and a second one with higher intensity due to a complex species having $C_{1}$ symmetry (Figure 6). The ionic radius of $\mathrm{Y}^{3+}(1.075$ $\AA$ for coordination number 9 ) is very similar to those of the heaviest $\mathrm{Ln}^{3+}$ ions ( $1.072 \AA$ for $\mathrm{Ho}^{3+}$ with coordination number 9). ${ }^{39}$ To investigate in more detail the nature of the


Figure 6. ${ }^{1} \mathrm{H}-{ }^{89} \mathrm{Y}$ HMQC NMR spectrum of $\left[\mathrm{YL}^{6}\right]^{3+}\left(\mathrm{D}_{2} \mathrm{O}, 500\right.$ $\mathrm{MHz}, \mathrm{pH} 7.0,25^{\circ} \mathrm{C}$ ). The signals of the major (9-coordinated) and minor (10-coordinated) species present in solution are highlighted in blue and red, respectively.
species present in solution, we sought to apply an empirical correlation developed recently, which relates the observed ${ }^{89} \mathrm{Y}$ NMR shifts and the types of donor atoms coordinated in solution. ${ }^{40}$ Thus, we measured the ${ }^{89} \mathrm{Y}$ NMR shifts in an attempt to confirm the presence in solution of both the 10 - and 9 -coordinated species suggested by the crystallographic study. The ${ }^{89}$ Y NMR shifts were obtained by using ${ }^{1} \mathrm{H}-{ }^{89} \mathrm{Y}$ HSQC NMR experiments, which allow a fast acquisition by overcoming the very long relaxation times of the ${ }^{89} \mathrm{Y}$ nucleus. ${ }^{41}$ The ${ }^{1} \mathrm{H}-{ }^{89} \mathrm{Y}$ HSQC NMR spectrum presents cross-peaks relating the signals of the major species in solution and an ${ }^{89} \mathrm{Y}$ NMR signal at 157 ppm , while for the minor species present in solution, the ${ }^{89} \mathrm{Y}$ NMR signal was observed at 51 ppm (Figure 6). These chemical shifts are in excellent agreement with those calculated using the relationship shown in eq 4 , where $S_{\mathrm{N}_{\mathrm{am}}}$, $S_{\mathrm{N}_{\mathrm{py}}}$, and $S_{\mathrm{O}_{\mathrm{a}}}$ are the shielding contributions of amine, pyridine, and amide donor atoms (68.1, 85.7, and 89.5 ppm , respectively) and $n_{\mathrm{Nam}_{\mathrm{am}}} n_{\mathrm{N}_{\mathrm{py}},}$ and $n_{\mathrm{O}_{\mathrm{a}}}$ are the number of donor atoms of each type: ${ }^{\frac{a n}{}}$

$$
\begin{equation*}
\delta^{\text {calc }}\left({ }^{\text {c9}} \mathrm{Y}\right)=863-\left(S_{\mathrm{Nam}} n_{\mathrm{Nam}}+S_{\mathrm{N}_{\mathrm{py}}} n_{\mathrm{N}_{\mathrm{py}}}+S_{\mathrm{O}_{\mathrm{a}}} n_{\mathrm{O}_{\mathrm{a}}}\right) \tag{4}
\end{equation*}
$$

Using $n_{\mathrm{N}_{\mathrm{am}}}=4, n_{\mathrm{N}_{\mathrm{py}}}=2$, and $n_{\mathrm{O}_{\mathrm{a}}}=4$ gives a calculated ${ }^{89} \mathrm{Y}$ chemical shift of 61.2 ppm , which is in very good agreement with the experimental value of 51 ppm . An identical analysis but using $n_{\mathrm{O}_{\mathrm{a}}}=3$ gives a calculated value of 150.7 ppm , again in excellent agreement with the experimental value observed for the major (unsymmetrical) species present in solution (157 $\mathrm{ppm})$. Thus, these results confirm the presence in solution of 9 -coordinated species in the case of the smallest $\mathrm{Ln}^{3+}$ ions and $\mathrm{Y}^{3+}$, with a smaller population of the 10 -coordinated species having $D_{2}$ symmetry.

The ${ }^{89} \mathrm{Y}$ shielding constants of the 10 - and 9 -coordinated forms of $\left[\mathrm{YL}^{6}\right]^{3+}$ were calculated using DFT (see the Computational Details). The chemical shielding values obtained from these calculations are compiled in Table 4. The subsequent calculation of ${ }^{89} \mathrm{Y}$ chemical shifts requires determination of the shielding constant of a reference, generally $\left[\mathrm{Y}\left(\mathrm{H}_{2} \mathrm{O}\right)_{8}\right]^{3+}(0.0 \mathrm{ppm}) .{ }^{42}$ The shielding constants calculated for the 9 - and 10 -coordinated forms of $\left[\mathrm{YL}^{6}\right]^{3+}$ differ by 105.7 ppm , in nice agreement with the experimental value of $\Delta \delta=106 \mathrm{ppm}$. This value is close to the empirical contribution of an amide donor of $S_{\mathrm{O}_{\mathrm{a}}}=89.5 \mathrm{ppm} .{ }^{40}$ However,

Table 4. Isotropic ${ }^{89} \mathrm{Y}$ Shielding Constants ( $\sigma_{\text {iso }}$ ), Paramagnetic ( $\sigma_{\mathrm{p}}$ ) and Diamagnetic Contributions $\left(\sigma_{\mathrm{d}}\right)$, and ${ }^{89}$ Y Chemical Shifts Calculated with DFT ${ }^{a}$

|  | $\sigma_{\text {iso }}$ | $\sigma_{\mathrm{d}}$ | $\sigma_{\mathrm{P}}$ | $\delta_{\text {calc }}$ |
| :--- | :---: | :---: | ---: | ---: |
| $\left[\mathrm{Y}\left(\mathrm{L}^{6}\right)\right]^{3+}(\mathrm{CN}=10)$ | 2568.8 | 3783.4 | -1214.6 | 180.8 |
| $\left[\mathrm{Y}\left(\mathrm{L}^{6}\right)\right]^{3+}(\mathrm{CN}=9)$ | 2674.5 | 3777.6 | -1103.1 | 75.1 |
| $\left[\mathrm{Y}\left(\mathrm{H}_{2} \mathrm{O}\right)_{6}\right]^{3+}$ | 2813.9 | 3761.6 | -947.7 |  |
| $\left[\mathrm{Y}\left(\mathrm{H}_{2} \mathrm{O}\right)_{6}\right]^{3+} \cdot 16 \mathrm{H}_{2} \mathrm{O}$ | 2749.6 | 3771.7 | -1022.1 | 0 |

${ }^{a}$ DFT calculations using the GIAO method in aqueous solution (PCM) at the TPSSh/DKH2/Def2-TZVPP level.
the use of the shielding constant of $\left[\mathrm{Y}\left(\mathrm{H}_{2} \mathrm{O}\right)_{8}\right]^{3+}$ provided ${ }^{89} \mathrm{Y}$ NMR chemical shifts with large deviations from the experimental value. We recently showed that the agreement between the experimental and calculated ${ }^{71} \mathrm{Ga}$ chemical shifts improved significantly upon inclusion of an explicit second solvation shell. ${ }^{43}$ We thus performed calculations on the $\left[\mathrm{Y}\left(\mathrm{H}_{2} \mathrm{O}\right)_{8}\right]^{3+} \cdot 16 \mathrm{H}_{2} \mathrm{O}$ system, which includes 16 water molecules in the second sphere involved in hydrogen bonds with the coordinated water molecules (Figure S11). The structure calculated for $\left[\mathrm{Y}\left(\mathrm{H}_{2} \mathrm{O}\right)_{8}\right]^{3+}$ presents the expected square-antiprismatic coordination environment with $\mathrm{Y}-\mathrm{O}$ distances in the range of $2.360-2.371 \AA$, in good agreement with the distances observed in the solid state $(2.31-2.38 \AA) .^{44}$ Inclusion of the second solvation shell broadens the range of Y-O distances ( $2.35-2.47 \AA$ ). The second solvation shell significantly affects the isotropic shielding constant, which decreases by $\sim 64 \mathrm{ppm}$. The ${ }^{89} \mathrm{Y}$ NMR chemical shifts of $\left[\mathrm{Y}\left(\mathrm{H}_{2} \mathrm{O}\right)_{8}\right]^{3+}$ calculated using $\left[\mathrm{Y}\left(\mathrm{H}_{2} \mathrm{O}\right)_{8}\right]^{3+} \cdot 16 \mathrm{H}_{2} \mathrm{O}$ as a reference (Table 4) are in reasonably good agreement with the experimental values of 157 and 51 ppm . $\sigma_{\text {iso }}$ can be separated into the usual diamagnetic ( $\sigma_{\mathrm{d}}$ ) and paramagnetic $\left(\sigma_{\mathrm{p}}\right)$ contributions (Table 4). ${ }^{45}$ The results show that the distinct chemical shifts are mainly related to variations in the $\sigma_{\mathrm{p}}$ values, which originate from the ability of the applied field to mix excited states into the ground state. The $\sigma_{\mathrm{d}}$ values calculated for all systems are, however, very similar, as would be expected.

CEST Experiments. The crystal structures of the $\mathrm{Pr}^{3+}$ and $\mathrm{Tb}^{3+}$ complexes revealed that the complexes are lacking coordinated water molecules. However, they possess exchangeable amide proton pools suitable for exploitation of the CEST effect. Thus, to investigate the potential application of these complexes as paraCEST agents, we conducted a series of NMR and MRI studies. Both solutions of $\left[\mathrm{TbL}^{6}\right]^{3+}$ and $\left[\mathrm{PrL}^{6}\right]^{3+}$ showed two notable paraCEST signals at different temperatures. For the $\mathrm{Pr}^{3+}$ complex, two CEST peaks at -2.8 and -8.0 ppm are strong but close to the peak of water protons at $25^{\circ} \mathrm{C}$ (Figure S12). For the $\mathrm{Tb}^{3+}$ complex, we performed a set of experiments with the temperature ranging from 10 to $40^{\circ} \mathrm{C}$. For each temperature, we recorded the Z-spectra using seven different saturation powers from 2.5 to $30 \mu \mathrm{~T}$ (see the Experimental Section). The results allowed us to follow the position (shift) of the CEST peaks, as well as to calculate the exchange rates of these two exchangeable protons as a function of the temperature.

The CEST signals of $\left[\mathrm{TbL}^{6}\right]^{3+}$ are highly paramagnetically shifted and strongly dependent on the temperature: these two peaks shift from -64 and -76 ppm to -60 and -70 ppm from 25 to $37{ }^{\circ} \mathrm{C}$, respectively (Figure 7). Over the entire temperature range examined, the sensitivity of the chemical shift to temperature was 0.54 or $0.41 \mathrm{ppm} /{ }^{\circ} \mathrm{C}$ for the low or


Figure 7. Top: CEST spectra recorded at 7 T of a solution containing $\left[\mathrm{TbL}^{6}\right]^{3+}(10 \mathrm{mM}$ in 25 mM PBS, pH 7.0$)$ at different temperatures using a saturation time of 8 s and a saturation power of $B_{1}=20 \mu \mathrm{~T}$. Bottom: Variation of the chemical shifts of amide protons with temperature.
high field signal, respectively (Figure 7). This is an interesting result because this particular feature of $\left[\mathrm{TbL}^{6}\right]^{3+}$ can be potentially exploited for measuring the temperature distribution in a living subject: here both signals can be used to determine the temperature while concurrently acting as controls for the other peak; i.e., the distance between these two peaks is also temperature-dependent. The temperature coefficients determined for $\left[\mathrm{TbL}^{6}\right]^{3+}$ are similar to those reported for ${ }^{1} \mathrm{H}$ resonances of paramagnetic cobalt(II) and iron(II) complexes suggested for registration of the temperature. ${ }^{46}$

The exchange rates of the CEST-active protons, $k_{\text {ex }}$, were determined using the previously established qCEST method, ${ }^{47}$ by fitting a series of multi- $B_{1}$ Z-spectra according to the BM equations. As expected, the $k_{\text {ex }}$ values are quite low at lower temperatures and less sensitive compared to those in the higher-temperature region. The $k_{\text {ex }}$ values are as low as $<100$ Hz at $10^{\circ} \mathrm{C}$, increasing to up to 3 kHz at $40^{\circ} \mathrm{C}$ (Table S2). Of the two peaks, the one with lower shift always exchanges faster. The $k_{\text {ex }}$ values determined at different temperatures for $\left[\mathrm{TbL}^{6}\right]^{3+}$ were used to estimate the activation parameters for amide proton exchange using the Eyring equation (Figure S14). The most shifted signal is characterized by $\Delta H^{\ddagger}=45.3$ $\pm 2.6 \mathrm{~kJ} \mathrm{~mol}^{-1}$ and $\Delta S^{\ddagger}=-38.4 \pm 2.0 \mathrm{~J} \mathrm{~mol}^{-1} \mathrm{~K}^{-1}$. The signal with a smaller shift (and fast exchange) yields $\Delta H^{\ddagger}=47.4 \pm$ $2.2 \mathrm{~kJ} \mathrm{~mol}^{-1}$ and $\Delta S^{\ddagger}=-27.5 \pm 1.2 \mathrm{~J} \mathrm{~mol}^{-1} \mathrm{~K}^{-1}$. The enhanced exchange rate of the latter amide protons appears to be related to a substantially lower entropy barrier, presumably due to the formation of a more favored (i.e., less ordered) transition state, which likely possesses a more extensive dispersion of charge. ${ }^{48}$

Importantly, the $k_{\mathrm{ex}}$ values at $37^{\circ} \mathrm{C}$ are in the optimal range of $1.5-2.5 \mathrm{kHz}$, which combined with the high number of the NMR equivalent and shifted protons (two groups, each with four protons) makes this platform very attractive for the further development of potent paraCEST probes. ${ }^{15,22}$ Concurrently, the obtained exchange rates for $\left[\mathrm{PrL}^{6}\right]^{3+}$ were in a range similar to that for $\left[\mathrm{TbL}^{6}\right]^{3+}$ (Table S2), albeit exhibiting somewhat slower exchange rates. Nevertheless, the low paramagnetic shift of the CEST peaks limits the potential use of this complex in future paraCEST MRI studies.

We also performed MRI experiments on the tube phantoms at 7 T magnetic field. We prepared the solutions of $\left[\mathrm{TbL}^{6}\right]^{3+}$ and $\left[\mathrm{PrL}^{6}\right]^{3+}$ in the same concentrations as those used in NMR experiments. We then obtained CEST MRI images using different saturation times and powers and compared the results to those obtained by means of NMR. Both complexes still showed strong CEST signals at room temperature (RT; Figure 8). However, because of the lower temperature in the MRI


Figure 8. CEST MRI on tube phantoms with $\left[\mathrm{PrL}^{6}\right]^{3+}$ and $\left[\mathrm{TbL}^{6}\right]^{3+}$ ( $10 \mathrm{mM}, 25 \mathrm{mMPBS}, \mathrm{pH} 7.0$, RT, saturation time 5 s , saturation power $10 \mu \mathrm{~T})$.
scanner ( $\sim 21-22^{\circ} \mathrm{C}$ ) and hence the slower exchange rates of amide protons during these experiments, the resulting CEST effect was lower (Table S2). Expectedly, the CEST MRI signals at a slightly shorter saturation time ( 3 s instead of 5 s ) showed similar values when the saturation power was kept the same $(10 \mu \mathrm{~T})$, whereas a weaker saturation power ( $5 \mu \mathrm{~T}$ instead of $10 \mu \mathrm{~T}$ ) resulted in much weaker CEST effects (Figure S13). Overall, the results obtained with $\left[\mathrm{TbL}^{6}\right]^{3+}$ showed that it remains good candidate for further CEST MRI studies and is an excellent basis for the development of other potent paraCEST probes.

## CONCLUSIONS

The detailed structural investigation reported here evidences that the $\left[L_{L} L^{6}\right]^{3+}$ complexes adopt different structures depending on the size of the lanthanide ion. The X-ray structure of the $\mathrm{La}^{3+}$ complex contains 12 -coordinated metal ions, with the four pendant arms coordinating from the same side of the macrocyclic unit and a nitrate anion coordinating from the opposite side. However, NMR studies demonstrate that this unusual structure evolves to a 10 -coordinated structure with an effective $D_{2}$ symmetry in solution. The large $\mathrm{Ln}^{3+}$ ions adopt this structure in solution until $\mathrm{Tb}^{3+}$,
while for the small ions, 9 -coordinated structures are observed. The 10 -coordinated structure of $\left[\mathrm{TbL}^{6}\right]^{3+}$ was established by analyzing the paramagnetic shifts observed in the ${ }^{1} \mathrm{H}$ NMR spectrum. The ${ }^{1} \mathrm{H}$ and ${ }^{89} \mathrm{Y}$ NMR spectra indicate that the major species present in solution is 9-coordinated, with a small proportion of the symmetrical $D_{2}$ structure also being present ( $\sim 14 \%$ ).

The $\left[\mathrm{TbL}^{6}\right]^{3+}$ complex contains two pools of amide protons with relatively large chemical shifts showing strong temperature dependence (ranging from $\sim 69$ to 85 ppm depending on the temperature). These amide protons are characterized by a rather slow exchange rate with bulk water $(1.5-2.5 \mathrm{kHz})$. Furthermore, each of the CEST signals originates by four magnetically equivalent protons, which results in strong CEST responses even at low saturation powers. Thus, $\left[\mathrm{TbL}^{6}\right]^{3+}$ can be regarded as a very attractive platform to develop CEST MRI agents.

## - EXPERIMENTAL SECTION

General Methods. ${ }^{1} \mathrm{H}$ NMR spectra were obtained at $25^{\circ} \mathrm{C}$ using a Bruker ARX400 spectrometer and solutions of the complexes in $\mathrm{D}_{2} \mathrm{O}$. Chemical shifts were referenced with respect to the residual HDO proton signal $(\delta=4.79 \mathrm{ppm}) .{ }^{49}$ Elemental analyses were obtained with a Carlo-Erba EA 1108 microanalyzer. Fourier transform infrared spectra were recorded using the attenuated total reflection method (ATR-FTIR) with a Bruker VECTOR 22 spectrometer ( KBr disks). Mass spectra were obtained with a microTOF (focus) mass spectrometer (Bruker Daltonics, Bremen, Germany) equipped with an ApolloII (ESI) source for electrospray ionization.

Preparation of the Complexes. All complexes were prepared by the reaction of a solution of $\operatorname{Ln}\left(\mathrm{NO}_{3}\right)_{3} \cdot x \mathrm{H}_{2} \mathrm{O}(0.040 \mathrm{mmol})$ and $\mathrm{L}^{6}$. $\mathrm{H}_{2} \mathrm{O}(0.023 \mathrm{~g}, 0.040 \mathrm{mmol})$ in methanol $(15 \mathrm{~mL})$, following the same procedure as that described for the europium and yttrium analogues. ${ }^{22}$ Slow concentration of the solutions of the complexes in methanol yielded polycrystalline solids with the formula $\left[\mathrm{LnL}^{6}\right]$ $\left(\mathrm{NO}_{3}\right)_{3} \cdot x \mathrm{H}_{2} \mathrm{O}(x=2-4)$ that were isolated by filtration and dried.
$\left[\mathrm{LaL}^{6}\right]\left(\mathrm{NO}_{3}\right)_{3} \cdot 3 \mathrm{H}_{2} \mathrm{O} . \mathrm{L}^{6} \cdot \mathrm{H}_{2} \mathrm{O}(0.023 \mathrm{~g}, 0.040 \mathrm{mmol})$ and $\mathrm{La}\left(\mathrm{NO}_{3}\right)_{3} \cdot$ $5 \mathrm{H}_{2} \mathrm{O}(0.017 \mathrm{~g}, 0.040 \mathrm{mmol})$ were reacted. Yield: $0.029 \mathrm{~g}, 79 \%$. Elem anal. Calcd for $\mathrm{C}_{26} \mathrm{H}_{44} \mathrm{~N}_{13} \mathrm{O}_{16} \mathrm{La}$ : C, 33.5; H, 4.8; N, 19.5. Found: C, 33.7; H, 5.0; N, 19.4. ESI-MS. Found (calcd): $m / z 754.2$ (754.2) for $\left[\mathrm{La}\left(\mathrm{L}^{6}-\mathrm{H}\right)\left(\mathrm{NO}_{3}\right)\right]^{+}, 691.2$ (691.2) for $\left[\mathrm{La}\left(\mathrm{L}^{6}-2 \mathrm{H}\right)\right]^{+}$. IR $\left(\mathrm{cm}^{-1}\right)$ : $1600(\mathrm{~s}), 1454(\mathrm{~s})[\nu(\mathrm{C}-\mathrm{C}) / \nu(\mathrm{C}-\mathrm{C})$; pyridine], 1648 (s) [carbonyl stretch], $3165(\mathrm{~m})\left[\nu\left(\mathrm{NH}_{2}\right)\right], 1293(\mathrm{~s}), 817(\mathrm{~m}), 827(\mathrm{~m}), 732(\mathrm{~m})$ [ $\mathrm{N}-\mathrm{O}$, nitrate].
$\left[\mathrm{LaL}^{6}\left(\mathrm{NO}_{3}\right)\right]_{2}\left[\mathrm{La}\left(\mathrm{NO}_{3}\right)_{6}\right] \cdot \mathrm{NO}_{3} \cdot 4 \mathrm{CH}_{3} \mathrm{OH}$. The synthesis followed the same procedure as that described above but using a $1.5: 1 \mathrm{La}\left(\mathrm{NO}_{3}\right)_{3}$. $5 \mathrm{H}_{2} \mathrm{O} / \mathrm{L}^{6}$ molar ratio. $\mathrm{L}^{6} \cdot \mathrm{H}_{2} \mathrm{O}(0.023 \mathrm{~g}, 0.040 \mathrm{mmol})$ and $\mathrm{La}\left(\mathrm{NO}_{3}\right)_{3}$. $5 \mathrm{H}_{2} \mathrm{O}(0.025 \mathrm{~g}, 0.060 \mathrm{mmol})$. Yield: $0.053 \mathrm{~g}, 60 \%$. Elem anal. Calcd for $\mathrm{C}_{56} \mathrm{H}_{92} \mathrm{~N}_{29} \mathrm{O}_{39} \mathrm{La}_{3}$ : C, 30.4; H, 4.2; N, 18.4. Found: C, 30.5; H, 4.7; N, 18.8. MS (ESI ${ }^{+}$). Found (calcd): $m / z 754.2$ (754.2) for $\left[\mathrm{La}\left(\mathrm{L}^{6}-\mathrm{H}\right)\left(\mathrm{NO}_{3}\right)\right]^{+}, 691.2$ (691.2) for $\left[\mathrm{La}\left(\mathrm{L}^{6}-2 \mathrm{H}\right)\right]^{+}$. IR $\left(\mathrm{cm}^{-1}\right)$ : 1594 (s), 1458 (s) $[\nu(\mathrm{C}-\mathrm{C}) / \nu(\mathrm{C}-\mathrm{C})$; pyridine], 1656 (s) [carbonyl stretch], $3280(\mathrm{~m})\left[\nu\left(\mathrm{NH}_{2}\right)\right], 1296(\mathrm{~s}), 818(\mathrm{~m}), 731(\mathrm{~m})[\mathrm{N}-\mathrm{O}$, nitrate]. Crystals suitable for X -ray diffraction were obtained with the formula $\left[\mathrm{LaL}^{6}\left(\mathrm{NO}_{3}\right)\right]_{2}\left[\mathrm{La}\left(\mathrm{NO}_{3}\right)_{6}\right] \cdot \mathrm{NO}_{3} \cdot 4 \mathrm{CH}_{3} \mathrm{OH}$.
$\left[\mathrm{CeL}^{6}\right]\left(\mathrm{NO}_{3}\right)_{3} \cdot 3 \mathrm{H}_{2} \mathrm{O} . \mathrm{L}^{6} \cdot \mathrm{H}_{2} \mathrm{O}(0.023 \mathrm{~g}, 0.040 \mathrm{mmol})$ and $\mathrm{Ce}\left(\mathrm{NO}_{3}\right)_{3}$. $6 \mathrm{H}_{2} \mathrm{O}(0.017 \mathrm{~g}, 0.040 \mathrm{mmol})$ were reacted. Yield: $0.024 \mathrm{~g}, 65 \%$. Elem anal. Calcd for $\mathrm{C}_{26} \mathrm{H}_{44} \mathrm{~N}_{13} \mathrm{O}_{16} \mathrm{Ce}$ : C, 33.4; H, 4.7; $\mathrm{N}, 19.5$. Found: C, 33.6; H, 5.1; N, 19.4. MS (ESI ${ }^{+}$). Found (calcd): $m / z 755.2$ (755.2) for $\left[\mathrm{Ce}\left(\mathrm{L}^{6}-\mathrm{H}\right)\left(\mathrm{NO}_{3}\right)\right]^{+}, 692.2(692.2)$ for $\left[\mathrm{Ce}\left(\mathrm{L}^{6}-2 \mathrm{H}\right)\right]^{+}$. IR $\left(\mathrm{cm}^{-1}\right)$ : 1593 (s), $1458(\mathrm{~s})[\nu(\mathrm{C}-\mathrm{C}) / \nu(\mathrm{C}-\mathrm{C})$; pyridine], 1655 (s) [carbonyl stretch], $3283(\mathrm{~m})\left[\nu\left(\mathrm{NH}_{2}\right)\right], 1240(\mathrm{~s}), 1225(\mathrm{~m}), 835(\mathrm{~m})[\mathrm{N}-\mathrm{O}$, nitrate].
$\left[P r L^{6}\right]\left(\mathrm{NO}_{3}\right)_{3} \cdot 4 \mathrm{H}_{2} \mathrm{O} . \mathrm{L}^{6} \cdot \mathrm{H}_{2} \mathrm{O}(0.023 \mathrm{~g}, 0.040 \mathrm{mmol})$ and $\operatorname{Pr}\left(\mathrm{NO}_{3}\right)_{3}$. $5 \mathrm{H}_{2} \mathrm{O}(0.017 \mathrm{~g}, 0.040 \mathrm{mmol})$ were reacted. Yield: $0.030 \mathrm{~g}, 80 \%$. Elem anal. Calcd for $\mathrm{C}_{26} \mathrm{H}_{46} \mathrm{~N}_{13} \mathrm{O}_{17} \mathrm{Pr}$ : C, 32.7; H, 4.8; N, 19.1. Found: C, 32.7; H, 5.0; N, 19.0. MS (ESI ${ }^{+}$). Found (calcd): $m / z 756.2$ (756.2) for $\left[\operatorname{Pr}\left(\mathrm{L}^{6}-\mathrm{H}\right)\left(\mathrm{NO}_{3}\right)\right]^{+}, 693.2(693.2)$ for $\left[\operatorname{Pr}\left(\mathrm{L}^{6}-2 \mathrm{H}\right)\right]^{+} . \mathrm{IR}\left(\mathrm{cm}^{-1}\right)$ :

1601 (s), 1460 (s) $[\nu(\mathrm{C}-\mathrm{C}) / \nu(\mathrm{C}-\mathrm{C})$; pyridine], 1654 (s) [carbonyl stretch], $3163(\mathrm{~m})\left[\nu\left(\mathrm{NH}_{2}\right)\right], 1313(\mathrm{~s}), 827(\mathrm{~m})[\mathrm{N}-\mathrm{O}$, nitrate $]$.
$\left[\mathrm{NdL}^{6}\right]\left(\mathrm{NO}_{3}\right)_{3} \cdot 3 \mathrm{H}_{2} \mathrm{O} . \mathrm{L}^{6} \cdot \mathrm{H}_{2} \mathrm{O}(0.023 \mathrm{~g}, 0.040 \mathrm{mmol})$ and $\mathrm{Nd}-$ $\left(\mathrm{NO}_{3}\right)_{3} \cdot 6 \mathrm{H}_{2} \mathrm{O}(0.017 \mathrm{~g}, 0.040 \mathrm{mmol})$ were reacted. Yield: 0.028 g , $75 \%$. Elem anal. Calcd for $\mathrm{C}_{26} \mathrm{H}_{44} \mathrm{~N}_{13} \mathrm{O}_{16} \mathrm{Nd}$ : C, 33.3; H, 4.7; N, 19.4. Found: C, 33.7; H, 5.0; N, 19.3. MS (ESI ${ }^{+}$). Found (calcd): $\mathrm{m} / \mathrm{z}$ 757.2 (757.7) for $\left[\mathrm{Nd}\left(\mathrm{L}^{6}-\mathrm{H}\right)\left(\mathrm{NO}_{3}\right)\right]^{+}, 694.2$ (694.2) for $\left[\mathrm{Nd}\left(\mathrm{L}^{6}-\right.\right.$ $2 \mathrm{H})]^{+}$. IR $\left(\mathrm{cm}^{-1}\right): 1593(\mathrm{~s}), 1458(\mathrm{~s})[\nu(\mathrm{C}-\mathrm{C}) / \nu(\mathrm{C}-\mathrm{C})$; pyridine $]$, 1655 (s) [carbonyl stretch], 3284 (m), $3225(\mathrm{~m})$ [ $\left.\nu\left(\mathrm{NH}_{2}\right)\right], 1299$ (s), $838(\mathrm{~m}), 734(\mathrm{~m})[\mathrm{N}-\mathrm{O}$, nitrate $]$.
$\left[\mathrm{SmL}^{6}\right]\left(\mathrm{NO}_{3}\right)_{3} \cdot 3 \mathrm{H}_{2} \mathrm{O} . \mathrm{L}^{6} \cdot \mathrm{H}_{2} \mathrm{O}(0.023 \mathrm{~g}, 0.040 \mathrm{mmol})$ and $\mathrm{Sm}-$ $\left(\mathrm{NO}_{3}\right)_{3} \cdot 6 \mathrm{H}_{2} \mathrm{O}(0.018 \mathrm{~g}, 0.040 \mathrm{mmol})$ were reacted. Yield: 0.032 g , $86 \%$. Elem anal. Calcd for $\mathrm{C}_{26} \mathrm{H}_{44} \mathrm{~N}_{13} \mathrm{O}_{16} \mathrm{Sm}$ : C, 33.0; H, 4.7; N, 19.3. Found: C, 32.9; H, 5.0; N, 19.4. MS (ESI ${ }^{+}$). Found (calcd): $m / z$ $767.2(766.2)$ for $\left[\operatorname{Sm}\left(\mathrm{L}^{6}-\mathrm{H}\right)\left(\mathrm{NO}_{3}\right)\right]^{+}, 704.2(704.2)$ for $\left[\mathrm{Sm}\left(\mathrm{L}^{6}-\right.\right.$ $2 \mathrm{H})]^{+}$. IR $\left(\mathrm{cm}^{-1}\right): 1594(\mathrm{~s}), 1458(\mathrm{~s})[\nu(\mathrm{C}-\mathrm{C}) / \nu(\mathrm{C}-\mathrm{C})$; pyridine $]$, 1656 (s) [carbonyl stretch], $3158(\mathrm{~m})\left[\nu\left(\mathrm{NH}_{2}\right)\right], 1295(\mathrm{~s}), 842(\mathrm{~m})$, 736 (m) [ $\mathrm{N}-\mathrm{O}$, nitrate]. Crystals suitable for X-ray diffraction with the formula $\left[\mathrm{SmL}^{6}\right]\left(\mathrm{NO}_{3}\right)_{2.91} \cdot \mathrm{Br}_{0.09}$ were obtained from a solution of the complex in water after evaporation at RT.
$\left[\mathrm{GdL}^{6}\right]\left(\mathrm{NO}_{3}\right)_{3} \cdot 4 \mathrm{H}_{2} \mathrm{O} . \mathrm{L}^{6} \cdot \mathrm{H}_{2} \mathrm{O}(0.023 \mathrm{~g}, 0.040 \mathrm{mmol})$ and $\mathrm{Gd}-$ $\left(\mathrm{NO}_{3}\right)_{3} \cdot 6 \mathrm{H}_{2} \mathrm{O}(0.018 \mathrm{~g}, 0.040 \mathrm{mmol})$ were reacted. Yield: 0.028 g , $72 \%$. Elem anal. Calcd for $\mathrm{C}_{26} \mathrm{H}_{46} \mathrm{~N}_{13} \mathrm{O}_{17} \mathrm{Gd}: \mathrm{C}, 32.2 ; \mathrm{H}, 4.8 ; \mathrm{N}, 18.8$. Found: C, 32.7; H, 5.0; N, 18.4. MS (ESI ${ }^{+}$). Found (calcd): $m / z$ 773.2 (773.2) for $\left[\mathrm{Gd}\left(\mathrm{L}^{6}-\mathrm{H}\right)\left(\mathrm{NO}_{3}\right)\right]^{+}, 710.2$ (710.2) for $\left[\mathrm{Gd}\left(\mathrm{L}^{6}-\right.\right.$ $2 \mathrm{H})]^{+}$. IR $\left(\mathrm{cm}^{-1}\right): 1593(\mathrm{~s}), 1455(\mathrm{~s})[\nu(\mathrm{C}-\mathrm{C}) / \nu(\mathrm{C}-\mathrm{C})$; pyridine $]$, 1664 (s) [carbonyl stretch], $3277(\mathrm{~m}), 3215(\mathrm{~m})\left[\nu\left(\mathrm{NH}_{2}\right)\right], 1294$ (s), $814(\mathrm{~m}), 741(\mathrm{~m})$ [ $\mathrm{N}-\mathrm{O}$, nitrate].
$\left[\mathrm{TbL}^{6}\right]\left(\mathrm{NO}_{3}\right)_{3} \cdot 3 \mathrm{H}_{2} \mathrm{O} . \mathrm{L}^{6} \cdot \mathrm{H}_{2} \mathrm{O}(0.023 \mathrm{~g}, 0.040 \mathrm{mmol})$ and $\mathrm{Tb}\left(\mathrm{NO}_{3}\right)_{3}$. $6 \mathrm{H}_{2} \mathrm{O}(0.018 \mathrm{~g}, 0.040 \mathrm{mmol})$ were reacted. Yield: $0.027 \mathrm{~g}, 70 \%$. Elem anal. Calcd for $\mathrm{C}_{26} \mathrm{H}_{44} \mathrm{~N}_{13} \mathrm{O}_{16} \mathrm{~Tb}$ : C, 32.7; H, 4.6; N, 19.1. Found: C, 32.7; H, 4.8; N, 19.0. MS (ESI ${ }^{+}$). Found (calcd): $m / z 774.2$ (774.2) for $\left[\mathrm{Tb}\left(\mathrm{L}^{6}-\mathrm{H}\right)\left(\mathrm{NO}_{3}\right)\right]^{+}, 711.2(711.2)$ for $\left[\mathrm{Tb}\left(\mathrm{L}^{6}-2 \mathrm{H}\right)\right]^{+}$. IR $\left(\mathrm{cm}^{-1}\right)$ : 1590 (s), 1456 (s) $[\nu(\mathrm{C}-\mathrm{C}) / \nu(\mathrm{C}-\mathrm{C})$; pyridine], 1655 (s) [carbonyl stretch $], 3160(\mathrm{~m})\left[\nu\left(\mathrm{NH}_{2}\right)\right], 1315(\mathrm{~s}), 828(\mathrm{~m})[\mathrm{N}-\mathrm{O}$, nitrate $]$.
$\left[D y L^{6}\right]\left(\mathrm{NO}_{3}\right)_{3} \cdot 2 \mathrm{H}_{2} \mathrm{O} . \mathrm{L}^{6} \cdot \mathrm{H}_{2} \mathrm{O}(0.023 \mathrm{~g}, 0.040 \mathrm{mmol})$ and Dy$\left(\mathrm{NO}_{3}\right)_{3} \cdot 5 \mathrm{H}_{2} \mathrm{O}(0.017 \mathrm{~g}, 0.040 \mathrm{mmol})$ were reacted. Yield: 0.026 g , $68 \%$. Elem anal. Calcd for $\mathrm{C}_{26} \mathrm{H}_{42} \mathrm{~N}_{13} \mathrm{O}_{15} \mathrm{Dy}$ : C, 33.2; H, 4.5; N, 19.4. Found: C, 33.0; H, 4.8; N, 19.4. MS (ESI ${ }^{+}$). Found (calcd): $m / z$ $779.2(779.2)$ for $\left[\mathrm{Dy}\left(\mathrm{L}^{6}-\mathrm{H}\right)\left(\mathrm{NO}_{3}\right)\right]^{+}, 716.2(716.2)$ for $\left[\mathrm{Dy}\left(\mathrm{L}^{6}-\right.\right.$ $2 \mathrm{H})]^{+}$. IR $\left(\mathrm{cm}^{-1}\right): 1589(\mathrm{~s}), 1459(\mathrm{~s})[\nu(\mathrm{C}-\mathrm{C}) / \nu(\mathrm{C}-\mathrm{C})$; pyridine $]$, 1655 (s) [carbonyl stretch], $3176(\mathrm{~m})\left[\nu\left(\mathrm{NH}_{2}\right)\right], 1281(\mathrm{~s}), 813(\mathrm{~m})$, $744(\mathrm{~m})[\mathrm{N}-\mathrm{O}$, nitrate].
$\left[\mathrm{HoL}^{6}\right]\left(\mathrm{NO}_{3}\right)_{3} \cdot 3 \mathrm{H}_{2} \mathrm{O} . \mathrm{L}^{6} \cdot \mathrm{H}_{2} \mathrm{O}(0.023 \mathrm{~g}, 0.040 \mathrm{mmol})$ and Ho$\left(\mathrm{NO}_{3}\right)_{3} \cdot 5 \mathrm{H}_{2} \mathrm{O}(0.017 \mathrm{~g}, 0.040 \mathrm{mmol})$ were reacted. Yield: 0.023 g , $59 \%$. Elem anal. Calcd for $\mathrm{C}_{26} \mathrm{H}_{44} \mathrm{~N}_{13} \mathrm{O}_{16}$ Ho: C, 32.5; H, 4.6; N, 19.0. Found: C, 32.7; H, 4.8; N, 18.8. MS (ESI ${ }^{+}$). Found (calcd): $m / z$ $780.2(780.2)$ for $\left[\mathrm{Ho}\left(\mathrm{L}^{6}-\mathrm{H}\right)\left(\mathrm{NO}_{3}\right)\right]^{+}, 717.2(717.2)$ for $\left[\mathrm{Ho}\left(\mathrm{L}^{6}-\right.\right.$ $2 \mathrm{H})]^{+}$. IR $\left(\mathrm{cm}^{-1}\right): 1591(\mathrm{~s}), 1459(\mathrm{~s})[\nu(\mathrm{C}-\mathrm{C}) / \nu(\mathrm{C}-\mathrm{C})$; pyridine $]$, 1660 (s) [carbonyl stretch], $3168(\mathrm{~m})\left[\nu\left(\mathrm{NH}_{2}\right)\right], 1324(\mathrm{~s}), 827(\mathrm{~m})$, 779 (m) [ $\mathrm{N}-\mathrm{O}$, nitrate].
$\left[E r L^{6}\right]\left(\mathrm{NO}_{3}\right)_{3} \cdot 3 \mathrm{H}_{2} \mathrm{O} . \mathrm{L}^{6} \cdot \mathrm{H}_{2} \mathrm{O}(0.023 \mathrm{~g}, 0.040 \mathrm{mmol})$ and $\mathrm{Er}\left(\mathrm{NO}_{3}\right)_{3}$. $5 \mathrm{H}_{2} \mathrm{O}(0.017 \mathrm{~g}, 0.040 \mathrm{mmol})$ were reacted. Yield: $0.026 \mathrm{~g}, 68 \%$. Elem anal. Calcd for $\mathrm{C}_{26} \mathrm{H}_{44} \mathrm{~N}_{13} \mathrm{O}_{16} \mathrm{Er}$ : C, 32.5; H, 4.6; N, 19.0. Found: C, 32.3; H, 4.9; N, 19.1. MS (ESI ${ }^{+}$). Found (calcd): $m / z 782.2$ (781.4) for $\left[\operatorname{Er}\left(\mathrm{L}^{6}-\mathrm{H}\right)\left(\mathrm{NO}_{3}\right)\right]^{+}, 718.2(718.2)$ for $\left[\operatorname{Er}\left(\mathrm{L}^{6}-2 \mathrm{H}\right)\right]^{+}$. IR $\left(\mathrm{cm}^{-1}\right)$ : 1591 (s), 1459 (s) $[\nu(\mathrm{C}-\mathrm{C}) / \nu(\mathrm{C}-\mathrm{C})$; pyridine], 1655 (s) [carbonyl stretch $], 3171(\mathrm{~m})\left[\nu\left(\mathrm{NH}_{2}\right)\right], 1294(\mathrm{~s}), 811(\mathrm{~m}), 746(\mathrm{~m})[\mathrm{N}-\mathrm{O}$, nitrate].
$\left[T m L^{6}\right]\left(\mathrm{NO}_{3}\right)_{3} \cdot 4 \mathrm{H}_{2} \mathrm{O} . \mathrm{L}^{6} \cdot \mathrm{H}_{2} \mathrm{O}(0.023 \mathrm{~g}, 0.040 \mathrm{mmol})$ and $\mathrm{Tm}-$ $\left(\mathrm{NO}_{3}\right)_{3} \cdot 5 \mathrm{H}_{2} \mathrm{O}(0.018 \mathrm{~g}, 0.040 \mathrm{mmol})$ were reacted. Yield: 0.030 g , $78 \%$. Elem anal. Calcd for $\mathrm{C}_{26} \mathrm{H}_{46} \mathrm{~N}_{13} \mathrm{O}_{17}$ Tm: C, 31.8; H, 4.7; N, 18.6. Found: C, 31.9; H, 4.6; N, 18.4\%. MS (ESI ${ }^{+}$). Found (calcd): $m / z$ $784.2(784.2)$ for $\left[\operatorname{Tm}\left(\mathrm{L}^{6}-\mathrm{H}\right)\left(\mathrm{NO}_{3}\right)\right]^{+}, 721.2(721.2)$ for $\left[\mathrm{Tm}\left(\mathrm{L}^{6}-\right.\right.$ $2 \mathrm{H})]^{+}$. IR $\left(\mathrm{cm}^{-1}\right): 1606(\mathrm{~s}), 1460(\mathrm{~s})[\nu(\mathrm{C}-\mathrm{C}) / \nu(\mathrm{C}-\mathrm{C})$; pyridine $]$, 1655 (s) [carbonyl stretch], $3177(\mathrm{~m})\left[\nu\left(\mathrm{NH}_{2}\right)\right], 1288(\mathrm{~s}), 812(\mathrm{~m})$, $748(\mathrm{~m})[\mathrm{N}-\mathrm{O}$, nitrate $]$.
$\left[\mathrm{YbL} L^{6}\right]\left(\mathrm{NO}_{3}\right)_{3} \cdot 3 \mathrm{H}_{2} \mathrm{O} . \mathrm{L}^{6} \cdot \mathrm{H}_{2} \mathrm{O}(0.023 \mathrm{~g}, 0.040 \mathrm{mmol})$ and $\mathrm{Yb}\left(\mathrm{NO}_{3}\right)_{3}$. $5 \mathrm{H}_{2} \mathrm{O}(0.018 \mathrm{~g}, 0.040 \mathrm{mmol})$ were reacted. Yield: $0.027 \mathrm{~g}, 69 \%$. Elem anal. Calcd for $\mathrm{C}_{26} \mathrm{H}_{44} \mathrm{~N}_{13} \mathrm{O}_{16} \mathrm{Yb}$ : C, 32.3; H, 4.8; N, 18.8. Found: C,

Table 5. Crystallographic and Structure Refinement Data for $\left[\mathrm{LaL}^{6}\left(\mathrm{NO}_{3}\right)\right]_{2}\left[\mathrm{La}\left(\mathrm{NO}_{3}\right)_{6}\right] \cdot \mathrm{NO}_{3} \cdot 4 \mathrm{CH}_{3} \mathrm{OH},\left[\mathrm{SmL}^{6}\right]\left(\mathrm{NO}_{3}\right)_{2.91}$. $\mathrm{Br}_{0.09}$, and $\left[\mathrm{YbL}^{6}\right]\left(\mathrm{NO}_{3}\right)_{2.7} \cdot \mathrm{Br}_{0.3} \cdot 3 \mathrm{H}_{2} \mathrm{O}$

| formula | $\mathrm{C}_{28} \mathrm{H}_{46} \mathrm{~N}_{14.5} \mathrm{O}_{19.5} \mathrm{La}_{1.5}$ | $\mathrm{C}_{26} \mathrm{H}_{37} \mathrm{~N}_{12.91} \mathrm{O}_{12.74} \mathrm{Br}_{0.09} \mathrm{Sm}$ | $\mathrm{C}_{26} \mathrm{H}_{44} \mathrm{~N}_{12.71} \mathrm{O}_{15.13} \mathrm{Br}_{0.29} \mathrm{Yb}$ |
| :---: | :---: | :---: | :---: |
| MW | 1106.16 | 891.56 | 972.94 |
| cryst syst | monoclinic | monoclinic | triclinic |
| space group | C2/c | C2 | $P^{1}$ |
| $a / \AA$ | 27.765(3) | 24.934(3) | 10.2831(7) |
| $b / \AA$ | 21.204(2) | 12.0748(13) | 10.4226(7) |
| c/Å | 17.5621(19) | 24.057(3) | 7.7173(12) |
| $\alpha /$ deg |  |  | 85.062(2) |
| $\beta /$ deg | 125.119(2) | 91.131(2) | 87.922(2) |
| $\gamma /$ deg |  |  | 75.771(2) |
| $V / \AA^{3}$ | 8457.1(16) | 7241.4(13) | 1833.6(2) |
| Z | 8 | 8 | 2 |
| $D_{\text {calc }} / \mathrm{g} \mathrm{cm}^{-3}$ | 1.738 | 1.636 | 1.762 |
| $\mu / \mathrm{mm}^{-1}$ | 1.596 | 1.795 | 2.951 |
| Flack parameter |  | 0.381(17) |  |
| $R_{\text {int }}$ | 0.0657 | 0.0509 | 0.0324 |
| R1 ${ }^{a}$ | 0.0564 | 0.0477 | 0.0204 |
| wR2 (all data) ${ }^{b}$ | 0.1632 | 0.1158 | 0.0432 |
| ${ }^{a} \mathrm{R} 1=\sum\left\\|F_{o}\|-\| F_{c}\right\\| / \sum$ | $\sum\left[w\left(\\|\left. F_{\mathrm{o}}\right\|^{2}-\left\|F_{\mathrm{c}}\right\|^{2} \mid\right)^{2}\right.$ |  |  |

32.3; H, 5.0; N, 18.5. MS (ESI ${ }^{+}$). Found (calcd): $m / z 789.2$ (789.2) for $\left[\mathrm{Yb}\left(\mathrm{L}^{6}-\mathrm{H}\right)\left(\mathrm{NO}_{3}\right)\right]^{+}, 726.2(726.2)$ for $\left[\mathrm{Yb}\left(\mathrm{L}^{6}-2 \mathrm{H}\right)\right]^{+}$. IR $\left(\mathrm{cm}^{-1}\right)$ : 1592 (s), $1460(\mathrm{~s})[\nu(\mathrm{C}-\mathrm{C}) / \nu(\mathrm{C}-\mathrm{C})$; pyridine], 1664 (s) [carbonyl stretch], 3175 (m) [ $\left.\nu\left(\mathrm{NH}_{2}\right)\right], 1325$ (s), 826 (m) [N-O, nitrate]. Crystals of $\left[\mathrm{YbL}^{6}\right]\left(\mathrm{NO}_{3}\right)_{2.7} \cdot \mathrm{Br}_{0.3} \cdot 3 \mathrm{H}_{2} \mathrm{O}$ suitable for X-ray diffraction measurements were obtained from a solution of the complex in water, which was left to evaporate slowly at RT.
$\left[L^{6}\right]\left(\mathrm{NO}_{3}\right)_{3} \cdot 4 \mathrm{H}_{2} \mathrm{O} \cdot \mathrm{L}^{6} \cdot \mathrm{H}_{2} \mathrm{O}(0.023 \mathrm{~g}, 0.040 \mathrm{mmol})$ and $\mathrm{Lu}\left(\mathrm{NO}_{3}\right)_{3}$. $\mathrm{H}_{2} \mathrm{O}(0.015 \mathrm{~g}, 0.040 \mathrm{mmol})$ were reacted. Yield: $0.032 \mathrm{~g}, 80 \%$. Elem anal. Calcd for $\mathrm{C}_{26} \mathrm{H}_{46} \mathrm{~N}_{13} \mathrm{O}_{17} \mathrm{Lu}$ : C, 31.6; H, 4.8; N, 18.4. Found: C, 31.7; H, 5.1; N, 18.2. MS (ESI ${ }^{+}$). Found (calcd): $m / z 790.2$ (790.2) for $\left[\mathrm{Lu}\left(\mathrm{L}^{6}-\mathrm{H}\right)\left(\mathrm{NO}_{3}\right)\right]^{+}, 727.2(727.2)$ for $\left[\mathrm{Lu}\left(\mathrm{L}^{6}-2 \mathrm{H}\right)\right]^{+}$. IR $\left(\mathrm{cm}^{-1}\right)$ : 1599 (s), 1460 (s) [ $\nu(\mathrm{C}-\mathrm{C}) / \nu(\mathrm{C}-\mathrm{C})$; pyridine], 1654 (s) [carbonyl stretch], 3177 (m) [ $\left.\nu\left(\mathrm{NH}_{2}\right)\right], 1294(\mathrm{~s}), 812(\mathrm{~m}), 751(\mathrm{~m})[\mathrm{N}-\mathrm{O}$, nitrate].

Crystal Structure Determinations. X-ray diffraction data of $\left[\mathrm{LaL}^{6}\left(\mathrm{NO}_{3}\right)\right]_{2}\left[\mathrm{La}\left(\mathrm{NO}_{3}\right)_{6}\right] \cdot \mathrm{NO}_{3} \cdot 4 \mathrm{CH}_{3} \mathrm{OH}$ and $\left[\mathrm{SmL}^{6}\right]\left(\mathrm{NO}_{3}\right)_{2.91}$. $\mathrm{Br}_{0.09}$ were recorded at 273 (2) K using a Bruker Smart-CCD-1000 diffractometer and graphite-monochromated Mo $\mathrm{K} \alpha$ radiation ( $\lambda=$ $0.71073 \AA$ ). Corrections for Lorentz and polarization effects were applied to all data. For $\left[\mathrm{YbL}^{6}\right]\left(\mathrm{NO}_{3}\right)_{2.7} \cdot \mathrm{Br}_{0.3} \cdot 3 \mathrm{H}_{2} \mathrm{O}$, X-ray diffraction data were obtained at $100(2) \mathrm{K}$ with Mo $\mathrm{K} \alpha$ radiation and a Bruker D8 Venture Photon 100 CMOS detector. Collection of frames of data, reflection indexing, and lattice parameter determination were achieved with the APEX3 software. Integration of the intensity of the reflections was carried out with SAINT. ${ }^{50}$ The software SADABS ${ }^{51}$ was used in all cases for scaling and empirical absorption correction. All structures were refined by full-matrix least squares based on $F^{2}$ with the SHELXT program. ${ }^{52}$ Non-H atoms were refined with anisotropic displacement parameters. H atoms were included in calculated positions and refined with isotropic displacement parameters. For $\left[\mathrm{SmL}^{6}\right]\left(\mathrm{NO}_{3}\right)_{2.91} \cdot \mathrm{Br}_{0.09}$, a solvent masking routine was applied to correct the reflection data for the diffuse scattering associated with disordered water molecules present in the crystal. Molecular graphics were generated using OLEX2. ${ }^{53}$ Crystal data and details on data refinement are provided in Table 5.

CEST Studies. NMR experiments of $\left[\mathrm{PrL}^{6}\right]^{3+}$ and $\left[\mathrm{TbL}^{6}\right]^{3+}(10$ $\mathrm{mM}, \mathrm{pH} 7.0$, PBS 25 mM ) were recorded using a 300 MHz Bruker Avance III NMR instrument (Bruker, Ettlingen, Germany). The recordings were done using a saturation time of 8 s at different temperatures ( 25 and $37^{\circ} \mathrm{C}$ for $\left[\mathrm{PrL}^{6}\right]^{3+}$ and 10, 15, 20, 25, 30, 35, 37 , and $40{ }^{\circ} \mathrm{C}$ for $\left.\left[\mathrm{TbL}^{6}\right]^{3+}\right)$. Variable saturation powers $\left(B_{1}=2.5,5\right.$, $10,15,20,25$, and $30 \mu \mathrm{~T}$ ) were used for each temperature, employing a constant saturation time. The longitudinal $\left(T_{1}\right)$ and transverse $\left(T_{2}\right)$ relaxation times were determined with the standard inversion-
recovery and Carr-Purcell-Meiboom-Gill pulse sequences, respectively. ${ }^{54,55}$ The exchange rates $k_{\text {ex }}$ were assessed with the BM equations. ${ }^{47}$

MRI measurements were recorded from tube phantoms with a 300 MHz Bruker 70/30 USR magnet and a Bruker volume coil (RF RES 300 1H 075/040 QSN TR). Images were processed with Paravision 5.1 software provided by Bruker. MRI phantoms consisted of $2 \times 400$ $\mu \mathrm{L}$ vials placed inside the holder, inserted in the 60 mL syringe filled with water. The vials contained $10 \mathrm{mM}\left[\mathrm{TbL}^{6}\right]^{3+}$ and $\left[\mathrm{PrL}^{6}\right]^{3+}(\mathrm{pH}$ 7.0, 25 mM PBS), respectively.

CEST MRI images were acquired at RT using rapid acquisition with relaxation enhancement (RARE) pulse sequence with the following imaging parameters: repetition time/echo time $=16280 /$ 3.26 ms , field of view $=32 \times 32 \mathrm{~mm}$, matrix size $=64 \times 64$, slice thickness $=2 \mathrm{~mm}$, rare factor $=64$, number of excitation $=1$, acquisition time $=35 \mathrm{~min} 49 \mathrm{~s}$. MT parameters were as follows: saturation pulse duration 3 and 5 s , saturation power 5 and $10 \mu \mathrm{~T}$, 131 irradiation offsets in the range -100 to +100 ppm .

Image analysis was performed in MATLAB (MathWorks, USA). Initially, CEST MRI images were linearly interpolated and shifted to the center frequency in order to remove $B_{0}$ inhomogeneity artifacts. Thereafter, pairs of Z-spectrum images were extracted for the irradiation offsets of the CEST peaks $(+\Delta \omega)$ for the complexes ( -3 and -8.5 ppm for $\left[\mathrm{PrL}^{6}\right]^{3+}$ and -68.5 and -85.0 ppm for $\left.\left[\mathrm{TbL}^{6}\right]^{3+}\right)$, and their corresponding opposites $(-\Delta \omega)$ with respect to bulk water.

Quantification of the CEST effect was achieved using an inverse asymmetry analysis of the normalized Z-magnetization, using the inverse difference of the magnetization transfer ( $\mathrm{MTR}_{\text {ind }}$ in eq 5). The latter is calculated from the unsaturated water magnetization $\left(M_{0}\right)$ and magnetizations of the on-resonance at the frequency $+\Delta \omega\left(M_{z+}\right)$ and the off-resonance at $-\Delta \omega\left(M_{z-}\right)$ with respect to the bulk water signal. ${ }^{56}$

$$
\begin{equation*}
\operatorname{MTR}_{\mathrm{ind}}=\frac{M_{0}}{M_{z+}}-\frac{M_{0}}{M_{z-}} \tag{5}
\end{equation*}
$$

Computational Details. Full geometry optimization of the $\left[\mathrm{GdL}^{6}\right]^{3+}$ complex and the subsequent frequency analysis were carried out within the framework of DFT (TPSSh ${ }^{57}$ exchange correlation functional) employing the Gaussian 09 package (revision D.01). ${ }^{58}$ The inner electrons of $\mathrm{Gd}\left(46+4 \mathrm{f}^{7}\right)$ were described with a large-core quasi-relativistic effective core potential (RECP), while a [5s 4 p 3 d$]$-GTO basis set was used for the outermost 11 electrons. ${ }^{59}$ All other atoms were described using the $6-31 G(d, p)$ basis set.

Hyperfine coupling constants $(A / \hbar)$ were calculated using a smallcore relativistic effective core potential, which places 28 electrons of Gd in the core. The valence space of Gd was described with the ECP28MWB_GUESS basis set, ${ }^{60}$ while the EPR-III ${ }^{61}$ basis set was used for the ligand atoms. The effects of bulk water were incorporated in all calculations using the integral equation formalism of the polarized continuum model. ${ }^{62}$ The $\mathrm{Y}^{3+}$ complexes were optimized using a similar approach, with the TPSSh functional, the ECP28MWB quasi-relativistic ECP, and its associated basis set for Y and the standard $6-311 \mathrm{G}(\mathrm{d}, \mathrm{p})$ basis set for all other atoms. ${ }^{63}$ The ${ }^{89} \mathrm{Y}$ NMR shielding tensors were calculated with the GIAO ${ }^{64}$ method and the TPSSh functional, ${ }^{57}$ using the ORCA program package (version 4.2.0 $)^{65}$ and the $\mathrm{DKH} 2^{66}$ relativistic method. In these calculations, we used the old-DKH-TZVPP basis set, as implemented in previous versions of ORCA (see the Supporting Information), which is based on the TZVPPAll basis set of Aldrich ${ }^{67}$ and was recontracted for DKH2 calculations. The resolution of identity approximation for both Coulomb- and exchange-type integrals (RIJK) was used for both selfconsistent field and calculation of the NMR chemical shielding constants. ${ }^{68,69}$ Auxiliary basis sets were generated with the Autoaux procedure implemented in ORCA. ${ }^{70}$ Bulk solvents were considered using the SMD solvation model. ${ }^{71}$

## - ASSOCIATED CONTENT

## (s) Supporting Information

The Supporting Information is available free of charge at https://pubs.acs.org/doi/10.1021/acs.inorgchem.0c03385.

Coordination polyhedra, NMR spectra, Cartesian coordinates obtained with DFT, calculated pseudocontact shifts, Eyring plots, and additional CEST data (PDF)

## Accession Codes

CCDC 2044164-2044166 contain the supplementary crystallographic data for this paper. These data can be obtained free of charge via www.ccdc.cam.ac.uk/data_request/cif, or by emailing data_request@ccdc.cam.ac.uk, or by contacting The Cambridge Crystallographic Data Centre, 12 Union Road, Cambridge CB2 1EZ, UK; fax: +44 1223336033.

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## Author Contributions

The manuscript was written through contributions of all authors. All authors have given approval to the final version of the manuscript.

## Notes

The authors declare no competing financial interest.

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