

1 **Title: Continuous integration of heading and goal directions guides steering**

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10

11 **Abstract**

12 Navigating animals must integrate a diverse array of sensory cues into a single locomotor  
13 decision. Insects perform intricate navigational feats using a brain region termed the central  
14 complex in which an animal's heading direction is transformed through several layers of circuitry  
15 to elicit goal-directed locomotion. These transformations occur mostly in the fan-shaped body  
16 (FB), a major locus of multi-sensory integration in the central complex. Key aspects of these  
17 sensorimotor computations have been extensively characterized by functional studies,  
18 leveraging the genetic tools available in the fruit fly. However, our understanding of how  
19 neuronal activity in the FB dictates locomotor behaviors during navigation remains enigmatic.  
20 Here, we manipulate the activity of two key neuronal populations that input into the FB—the  
21 PFN<sub>a</sub> and PFN<sub>d</sub> neurons—used to encode the direction of two complex navigational cues: wind  
22 plumes and optic flow, respectively. We find that flies presented with unidirectional optic flow  
23 steer along curved walking trajectories, but silencing PFN<sub>d</sub> neurons abolishes this curvature. We  
24 next use optogenetic activation to introduce a fictive heading signal in the PFNs to establish the  
25 causal relationship between their activity and steering behavior. Our studies reveal that the  
26 central complex guides locomotion by summing the PFN-borne directional signals and shifting  
27 movement trajectories left or right accordingly. Based on these results, we propose a model of  
28 central complex-mediated locomotion wherein the fly achieves fine-grained control of sensory-  
29 guided steering by continuously integrating its heading and goal directions over time.

30 **Main**

31 Insects perform complex navigational tasks with relatively simple nervous systems. These tasks  
32 vary in range and complexity, from path integration in foraging ants over hundreds of meters<sup>1</sup> to  
33 the seasonal migration of monarch butterflies over thousands of kilometers<sup>2</sup>. Despite this vast  
34 range in navigational capabilities, a brain region conserved across insect species—the central  
35 complex—is thought to underlie these behaviors<sup>3-5</sup>. The central complex consists of four main  
36 compartments (Fig. 1a) that communicate via several populations of columnar neurons, the  
37 architecture and synaptic connectivity of which have been delineated in the fruit fly, *Drosophila*  
38 *melanogaster*<sup>6,7</sup>. One such compartment, the ellipsoid body (EB), intrinsically generates a  
39 representation of the fly's world-centric, also known as allocentric, orientation in space. This  
40 representation takes the form of a neuronal activity “bump” within a circular arrangement of  
41 columnar neurons termed the EPGs that is yoked to the fly's heading when landmarks are

42 present (Fig. 1b)<sup>8-12</sup>. When flies perform navigational tasks that require a stable landmark, the  
43 EB activity bump is recruited<sup>11,13</sup>. In parallel, neural projections to the noduli (NO) are thought to  
44 encode body-centric, also known as egocentric, left-right sensory signals<sup>14-16</sup>. A population of  
45 neurons termed PFNs receives information from both pathways<sup>6</sup> and conveys this information to  
46 the FB (Fig. 1b, c), a brain center where various sensory cues<sup>17-19</sup> and aspects of the animal's  
47 internal state<sup>19,20</sup> are represented. The PFNs incorporate the egocentric sensory signals to  
48 transpose the heading signal and construct allocentric vector representations of these dynamic  
49 sensory cues<sup>14,16</sup>. Different PFN subpopulations perform this vector transposition for different  
50 complex navigational cues, such as wind plumes<sup>15</sup> and optic flow<sup>14,16</sup>. The processing of these  
51 vector codes of sensory information culminates in the generation of a goal signal, which is  
52 represented as an activity bump in the FB. This goal signal, also expressed in allocentric  
53 coordinates, is used to guide locomotion during navigation<sup>21,22</sup>. Thus, the anatomical and  
54 functional properties of PFNs render them the likely origin of the fly's goal-oriented steering  
55 behavior. Further, these neurons likely act as a key circuit node for transforming navigational  
56 cues into locomotion. Hence, we sought to determine the contribution of neuronal activity in the  
57 PFNs to navigational behaviors through thermo- and optogenetic manipulation of genetically  
58 defined subpopulations of PFNs.

### 59 **PFNs control body orientation during forward walking bouts**

60 We first wished to devise a behavioral paradigm in which the PFN circuitry would be recruited.  
61 PFNs transform sensory signals from ego- to allocentric coordinate systems<sup>14,16</sup>. Different PFN  
62 populations perform this transformation for distinct sensory cues: PFN<sub>a</sub> neurons represent wind  
63 plumes, and PFN<sub>d</sub> neurons represent optic flow<sup>14-17</sup>. Both wind plumes and optic flow are  
64 complex cues that inherently convey relevant directional information to the navigating fly.  
65 Therefore, the fly must incorporate information from both when computing its movement  
66 decision. PFN<sub>a</sub> and PFN<sub>d</sub> neurons, however, target nonoverlapping regions of the FB (Fig. 1b)  
67 and input onto divergent circuits<sup>6</sup>. We hypothesized that PFN<sub>a</sub> and PFN<sub>d</sub> neurons perform  
68 parallel functions in navigational behaviors. We hence designed a behavioral paradigm that  
69 would rely on the activity in one subpopulation of PFNs (PFN<sub>a</sub> or PFN<sub>d</sub> neurons) but not the  
70 other. We decided to focus on the characterization of how optic flow contributes to navigational  
71 behaviors because of the simpler nature of the signal and the ability to precisely manipulate it  
72 compared to the dynamic and unpredictable nature of turbulent wind plumes.

73 When a landmark is present and other sensory cues are absent, flies display a behavior termed  
74 menotaxis in which they maintain a stable heading in an arbitrary goal direction relative to the  
75 landmark<sup>11,23,24</sup>. In addition, it incorporates self-motion cues to ensure that its movement is  
76 aligned with this goal direction. We hypothesized that optic flow constitutes one of these self-  
77 motion cues and that the fly uses PFN<sub>d</sub>-borne representations of optic flow to maintain a stable  
78 heading trajectory. We, therefore, sought to characterize how flies respond behaviorally to  
79 manipulations that misalign the optic flow and their heading direction as well as how activity in  
80 PFN<sub>d</sub> neurons, in turn, affects these responses.

81 We thus designed a behavioral paradigm in which flies were presented with unidirectional optic  
82 flow as they move through space. To this end, we placed the flies in a circular chamber<sup>25</sup> that is  
83 surrounded by green LED arrays programmed to display a series of vertical bars (Extended  
84 Data Fig. 1). By rotating the positions of the vertical bars around the circumference of the arena  
85 in a clockwise or counterclockwise fashion, the LED arrays produced an optical illusion of  
86 rotational movement. We tethered this visual stimulus to the fly's movement by rotating it only

87 when the fly moves so that the stimulus would better mimic optic flow cues indicating self-  
88 motion (Fig. 1e). We recorded videos of the behavioral responses of the flies to this stimulus  
89 paradigm and performed automatic kinematic tracking<sup>26</sup> to quantify the results.

90 During locomotion, a fly must continuously update its body position (translational motion) and  
91 orientation (angular motion) in space (Fig 1d). We quantified both variables in the kinematic  
92 data and used these metrics to determine how the flies responded to our stimulus paradigm. We  
93 first presented control flies with unidirectional optic flow during bouts of forward walking. We  
94 found that these flies exhibited circular movement trajectories when close to the center of the  
95 arena (Fig. 1f-h, Extended Data Fig. 2a-c). Further, angular velocity values shifted significantly  
96 in the direction of the rotating stimulus and coincided with bouts of translational velocity  
97 (Extended Data Fig. 2d, e). While eliciting these trajectories, flies would maintain a stable  
98 angular velocity during discrete bouts of continuous movement that last upwards of 10s  
99 (Extended Data Fig. 2c). We termed these epochs of circular movement trajectories  
100 “reorientation bouts.” We then sought to understand how the brain coordinates translational and  
101 angular motion to produce reorientation bouts.

102 We hypothesized that flies elicit reorientation bouts by updating their internal goal coordinate to  
103 align with visual feedback that acts as a self-motion cue. We, therefore, wished to examine  
104 whether these reorientation bouts relied on neuronal activity in core components of the central  
105 complex. We thus thermogenetically silenced targeted populations of central complex columnar  
106 neurons in walking flies while subjecting them to our behavioral paradigm. To achieve that, we  
107 used driver lines that narrowly target individual neuronal subpopulations in the central complex<sup>7</sup>  
108 to express *shibire<sup>TS</sup>*, an allele that reversibly blocks neurotransmission at temperatures greater  
109 than 28°C. We first turned to the EPG neurons, which encode the heading direction of the fly  
110 and act as a “master compass” for the central complex<sup>11,24,27,28</sup>. Flies of this cohort spent  
111 significantly less time in the center of the arena where curved walking trajectories are typically  
112 observed (Extended Data Fig. 3). Instead, these flies were usually located at the edge of the  
113 arena chasing the stimulus at a range where only one bar would be visible to them. This  
114 behavior is reminiscent of bar fixation, a behavior not thought to be controlled by the central  
115 complex circuitry. This result is thus aligned with previous observations that flies resort to more  
116 reflexive orientation behaviors in the absence of EPG neurons<sup>11,24</sup>. Since reorientation bouts are  
117 only observed in the center of the arena, we observed no such behavior when the EPGs were  
118 silenced. We, therefore, conclude that the central complex circuitry is engaged in our behavioral  
119 paradigm and that neuronal activity in the EPGs is likely used to produce the curved  
120 reorientation bouts.

121 The EPG activity bump, which represents the fly’s heading direction, is duplicated across the  
122 protocerebral bridge (PB), where it is inherited by neurons termed PFNs, the next layer of the  
123 central complex columnar circuit. PFNs incorporate asymmetric sensory signals from the NO to  
124 modulate the amplitude of the left and right activity bumps. The sum of the left and right PFN  
125 activity bumps produces a new activity bump in the next layer of circuitry. This new activity bump  
126 represents the direction of a particular sensory cue that is now transformed into allocentric  
127 coordinates<sup>14,16</sup>. These transformations ultimately generate a “goal direction” activity bump in the  
128 FB, which is compared to the heading direction represented by the EPG activity bump in the EB.  
129 The relative positions of the EB heading direction, and the FB goal direction are thought to drive  
130 angular movement during epochs of goal-directed locomotion<sup>21,22</sup>. We, therefore, predict that  
131 silencing PFNs would result in constitutive alignment of the heading and goal signals. Thus, it

132 would prevent the fly from eliciting movements to align the two coordinates. To test this  
133 prediction, we used *shibire*<sup>TS</sup> to selectively silence two populations of PFNs previously  
134 implicated in sensory guided forward motion—the PFN<sub>a</sub><sup>15,17</sup> and PFN<sub>d</sub><sup>14,16</sup> subtypes—while the  
135 flies perform the angular motion assay.

136 For flies performing the goal-directed walking assay at 21°C—a permissive temperature at which  
137 *shibire*<sup>TS</sup> allows neurotransmission—angular motion was preserved, and the flies performed  
138 reorientation bouts across experimental groups (Fig. 1f-h, l-m). By contrast, flies bearing  
139 *shibire*<sup>TS</sup> in PFN<sub>d</sub> neurons that underwent the behavioral paradigm at 31°C—a restrictive  
140 temperature at which *shibire*<sup>TS</sup> blocks neurotransmission—exhibited a “stop-and-turn” phenotype;  
141 their walking trajectories were straightened, and they only turned between bouts of forward  
142 walking (Fig. 1i-k). Hence, at the restrictive temperature, the values of translational and angular  
143 velocity were no longer coincidental (Fig. 1k). Over the duration of each trial, the translational  
144 velocity values in flies with silenced PFN<sub>d</sub> neurons were significantly reduced, indicating deficits  
145 in forward motion (Fig. 1l). Similarly, the angular velocity values in these flies were shifted  
146 towards zero, albeit slightly (Fig. 1m). Notably, PFN<sub>a</sub> neurons were dispensable for this behavior  
147 (Fig. 1l, m), indicating that the PFN<sub>a</sub> and PFN<sub>d</sub> subtypes perform specialized roles in  
148 navigational behaviors, which is in line with our predictions.

149 We observed that flies in the behavioral paradigm tended to walk forward in short bouts of  
150 translational velocity followed by periods of resting. In a five-minute experiment, animals with  
151 silenced PFN<sub>d</sub> neurons walked overall shorter distances than control animals, as represented by  
152 the translational velocity values (Fig. 1l). This decrease in translational velocity could reflect a  
153 reduction in overall walking speeds. Alternatively, it could result from shorter bouts of activity at  
154 comparable speeds to control flies, resulting in a lower average walking speed overall. To  
155 differentiate between these possibilities, we decomposed our kinematic tracking data for each  
156 fly into the discrete walking bouts elicited within each trial. This analysis enabled us to  
157 determine the number of walking bouts, average distance travelled in each bout, and average  
158 translational velocity for each bout. When comparing these metrics to the control animals, we  
159 found that silencing PFN<sub>d</sub> neurons led to no change in the number of walking bouts (Fig. 1m),  
160 but to a significant decrease in the overall distance travelled in each bout (Fig. 1n). The  
161 translational velocity values during these bouts of movement were comparable to those  
162 observed in control animals (Fig. 1o). Thus, this analysis indicates that the decrease in  
163 translational velocity observed when silencing PFN<sub>d</sub> neurons is due to shorter bouts of  
164 movement at comparable velocities to those of controls. These observations are consistent with  
165 a role for PFN<sub>d</sub> neurons in eliciting continuous bouts of forward movement with curved walking  
166 trajectories. We conclude that PFNs are necessary for instructing locomotion by driving bouts of  
167 forward walking that are curved towards the left or right direction.

### 168 **Additive effects of parallel PFN pathways on locomotion**

169 It is noteworthy that silencing PFN<sub>d</sub> neurons resulted in angular motion that was diminished but  
170 not altogether abolished. Therefore, it is possible that PFNs constitute one of multiple parallel  
171 steering systems and that the other systems are not perturbed by our manipulations. Such an  
172 organization would enable fine-grained control of body orientation during movement. We  
173 hypothesized that neuronal activity in PFNs is sufficient to elicit changes in the fly’s locomotor  
174 behavior. Should this indeed be the case, we would predict that exogenous activation of PFNs  
175 would elicit a shift in the fly’s ongoing heading direction in the absence of any navigational cues.  
176 To test this prediction, we optogenetically activated PFNs during locomotion and quantified

177 changes in the fly's heading. We expressed the light-gated cation channel CsChrimson in either  
178 PFN<sub>a</sub> or PFN<sub>d</sub> neurons using our selective driver lines. However, our thermogenetic silencing  
179 experiments revealed that PFN<sub>a</sub> neurons were dispensable in the optic flow assay. This result  
180 may indicate that the two subtypes of PFNs are functionally subdivided and hence constitute  
181 parallel circuits. The distinct cues represented by PFN<sub>a</sub> and PFN<sub>d</sub> neurons both affect  
182 navigational behaviors. Further, the ultimate heading direction should be coherent and represent  
183 the integration of both cues. We thus hypothesized that the parallel PFN circuits sum their  
184 signals to produce a single, unified heading direction. To test this hypothesis, we employed an  
185 additional driver line that targets both PFN<sub>a</sub> and PFN<sub>d</sub> subtypes (PFN<sub>a+d</sub>) to simultaneously  
186 activate both populations. We activated the PFNs in freely walking flies by subjecting them to an  
187 optogenetic stimulus paradigm during which a red light illuminates the behavioral arena for 20s  
188 with 20s resting periods before and after each stimulation. Each fly underwent three total  
189 stimulation periods while in an otherwise dark chamber (Fig 2a). Because red light is not  
190 detected by the fly visual system<sup>29</sup>, this experimental design enables us to profile changes in the  
191 fly's locomotion without introducing a goal stimulus through visual cues.

192 Activation of PFN<sub>a</sub> or PFN<sub>d</sub> neurons alone elicited no observable changes in translational (Fig.  
193 2e-h) or angular (Extended Data Fig. 4a, b) velocity. However, simultaneous activation of both  
194 populations via our PFN<sub>a+d</sub> driver resulted in an overall decrease in locomotion. Interestingly, in  
195 some cases, optogenetic stimulation of the PFN<sub>a+d</sub> neurons led flies to stop moving altogether  
196 and completely freeze during the stimulation period (Extended Data Fig. 5). Plotting the  
197 averaged translational velocity values of flies during each stimulation bout reveals that  
198 translational motion continually decreases when PFN<sub>a+d</sub> neurons are activated and slowly  
199 recovers to baseline levels at the end of the post-stimulus period (Fig. 2e). Thus, this line of  
200 investigation reveals that transient, simultaneous activation of both PFN<sub>a</sub> and PFN<sub>d</sub> populations  
201 results in a reversible cessation of locomotion.

## 202 **Asymmetric activation of PFNs biases heading direction**

203 We hypothesized that PFN<sub>a+d</sub>-mediated suppression of locomotion is due to a summation of  
204 PFN<sub>a</sub> and PFN<sub>d</sub> heading signals in the FB. We further hypothesized that such a summation  
205 mechanism should exist to integrate the parallel sensory pathways into a single left/right motor  
206 command because the two PFN populations encode different classes of navigational cues<sup>14-17</sup>.  
207 However, since in our previous line of investigation we analyzed the contributions of the PFNs to  
208 locomotion by activating entire populations of PFN subtypes, we could not test this hypothesis.  
209 The general manipulations of entire PFN populations obscure the natural dynamics of these  
210 circuits because neuronal activity in the PFNs typically takes the form of a sinusoidal bump, the  
211 peak of which is localized in a particular column<sup>9,14,16</sup>. Therefore, we reasoned that uncovering a  
212 more nuanced relationship between neuronal activity in the PFNs and locomotion would require  
213 a more selective targeting of the activated PFN population. Such targeted manipulation of a  
214 subpopulation of PFNs would better recapitulate their functional dynamics, and thus, more  
215 accurately mimic a specific directional signal. Further, a more targeted analysis of PFNs would  
216 better elucidate the mechanism of how exogenous activation of PFN<sub>a</sub> and PFN<sub>d</sub> neurons  
217 controls steering behavior to allow for orientation. We thus employed a mosaic strategy to  
218 optogenetically activate sparse and stochastically selected subsets of the PFNs.

219 We stimulated sparse and stochastically selected subpopulations of the neurons targeted by the  
220 PFN<sub>a+d</sub> driver line via SPARC<sup>30</sup> and employed the same optogenetic paradigm we used to  
221 activate all PFNs of a particular subtype. We stimulated these sparse PFN subsets in the



222 absence of any navigational cues and tracked the locomotor behaviors of the flies. We then  
223 employed a *post-hoc* dissection and immunohistochemical analysis to determine which PFN  
224 neurons were activated in each fly.

225 Sparse activation of PFNs led to observable shifts in angular velocity, typically following the  
226 onset of delivery of the optogenetic stimulus (Fig. 3e, f, black arrowhead). We investigated  
227 whether the direction and magnitude of these shifts in heading direction could be predicted  
228 based on which PFNs were activated in each experiment. Because left/right sensory information  
229 is conveyed to the PFNs via asymmetric activity in the NO<sup>14,15</sup>, we tested whether asymmetric  
230 PFN activation elicits unilateral shifts in the fly's heading direction. To achieve this, we first  
231 computed an index for asymmetric labeling of PFNs in our SPARC experiments by quantifying  
232 CsChrimson::tdTomato fluorescent signal in the corresponding left and right noduli. This  
233 analysis allows us to quantify the levels of asymmetric PFN activation and compare these  
234 values to the changes in heading elicited upon optogenetic stimulation. Because PFN<sub>a</sub> and  
235 PFN<sub>d</sub> neurons can be distinguished by the noduli from which they receive input<sup>6</sup>, this strategy  
236 allows us to additionally profile the relative contributions of the individual PFN subpopulations to  
237 changes in heading. We term the indices of PFN asymmetry  $\Delta\text{NO}_a$  and  $\Delta\text{NO}_d$  for PFN<sub>a</sub> and  
238 PFN<sub>d</sub> neurons, respectively (Fig. 3a).

239 To quantify the contributions of asymmetric PFN activity to heading direction, we computed a  
240 Pearson correlation between the  $\Delta\text{NO}_a$  or  $\Delta\text{NO}_d$  indices and the mean changes in angular  
241 velocity upon optogenetic stimulation. This correlation was stronger for the  $\Delta\text{NO}_d$  index than for  
242 the  $\Delta\text{NO}_a$  index, indicating that PFN<sub>d</sub> neurons elicited stronger changes in lateral movement  
243 (Fig. 3b, c). This result suggests that the activation of PFN<sub>d</sub> neurons evokes stronger changes in  
244 heading direction than the activation of PFN<sub>a</sub> neurons in this particular context.

245 Plotting the  $\Delta\text{NO}_a$  or  $\Delta\text{NO}_d$  indices against the mean changes in angular velocity for each  
246 experiment revealed the slopes of both trend lines (Fig. 3b, c). We inferred that the sign of these  
247 slopes, albeit statistically insignificant trends, indicates the direction of locomotor heading bias  
248 for each PFN population. The value of the  $\Delta\text{NO}_a$  index increased as the measured changes in  
249 angular velocity became more positive (Fig. 3b). By contrast, the value of the  $\Delta\text{NO}_d$  index  
250 increased as the measured changes in angular velocity became more negative (Fig. 3c). We  
251 then computed a third index for PFN asymmetry,  $\Delta\text{NO}_{a-d}$ , to quantify any interactions between  
252 PFN<sub>a</sub> and PFN<sub>d</sub> subtypes while accounting for the inferred sign of their contributions (see  
253 methods). Comparing the  $\Delta\text{NO}_{a-d}$  index with the mean changes in angular velocity upon  
254 optogenetic activation revealed a statistically significant correlation ( $P=0.0297$ ) between the two  
255 variables that was much stronger than the  $\Delta\text{NO}_a$  or  $\Delta\text{NO}_d$  indices alone (Fig. 3d).

256 To better assess the relative effects of PFN<sub>a</sub> and PFN<sub>d</sub> neurons on shifts in heading, we  
257 computed a weighted  $\Delta\text{NO}_{a-d}$  index that varied from -1 to 1, with -1 indicating that only PFN<sub>d</sub>  
258 neurons contributed to the index, 0 indicating that PFN<sub>a</sub> and PFN<sub>d</sub> neurons contributed equally,  
259 and 1 indicating that only PFN<sub>a</sub> neurons contributed (see methods). During optogenetic  
260 stimulation, this weighted  $\Delta\text{NO}_{a-d}$  index was most correlated with angular velocity when both  
261 populations were weighted about equally ( $\Delta\text{NO}_{a-d}$  weight = 0.075) (Fig. 3g, h). We interpret  
262 these data as evidence for a summative effect between PFN<sub>a</sub> and PFN<sub>d</sub> neurons in controlling  
263 angular motion during movement. The observation that PFN<sub>a</sub> and PFN<sub>d</sub> neurons have opposing  
264 signs regarding their effects on movement may indicate that the two subsystems are configured  
265 in counterphase. Activation of all PFN<sub>a</sub> and PFN<sub>d</sub> neurons simultaneously may, therefore, lead to

266 destructive interference between the two heading signals, ultimately suppressing locomotion, as  
267 we observed when activating all neurons contained in our PFN<sub>a+d</sub> driver (Fig. 2e, f).

268 Our data indicate that the degree of symmetry of the sparse PFN population activated in a given  
269 fly affects its angular velocity. We would thus predict that activation of a sparse population of  
270 symmetric PFNs would not elicit changes in angular velocity. We tested this prediction by driving  
271 CsChrimson with a driver that targets a sparse but symmetric subset of PFN<sub>a</sub> neurons  
272 (SS00081-Gal4) and subjected these flies to the optogenetic stimulation paradigm. We  
273 compared these trials to the same number of a randomly sampled subset of the PFN > SPARC  
274 CsChrimson trials. Remarkably, only in the PFN > SPARC experiments did we observe a spike  
275 in angular velocity at the onset of delivery of the optogenetic stimulus. This observation is  
276 consistent with a bout of reorientation upon asymmetric PFN activation. By contrast, SS00081 >  
277 CsChrimson flies exhibited a spike in angular velocity only upon offset of the optogenetic  
278 stimulus (Fig. 3j). That symmetric PFN activation elicited reorientation upon stimulus offset could  
279 have indicated that angular motion was suppressed during optogenetic stimulation. However,  
280 we observed a similar spike in angular motion in a control experiment using SS00081 >  
281 CsChrimson animals raised on a diet lacking all-*trans* Retinal (ATR), a necessary cofactor for  
282 CsChrimson functionality (Extended Data Fig. 6). We, therefore, suspect that the offset spike in  
283 angular velocity values observed during symmetric PFN activation (SS00081 > CsChrimson  
284 flies) is an artifact of the optogenetic stimulus delivery. Intriguingly, only PFN > SPARC  
285 CsChrimson flies, but not SS00081 > CsChrimson flies, exhibited increased translational velocity  
286 during the optogenetic stimulus bout (Fig. 3k, l). Our interpretation of these observations is that  
287 indeed, asymmetric, but not symmetric, activation of PFNs elicits reorientation and forward  
288 motion.

### 289 **Antiphase relationship between PFN<sub>a</sub> and PFN<sub>d</sub> neurons predicted by the connectome**

290 Asymmetric activation of either PFN<sub>a</sub> or PFN<sub>d</sub> neurons leads to a shift in angular motion, but the  
291 effects of the two populations are in opposite directions (Fig. 3b-d). These results could indicate  
292 that the two populations of neurons are arranged in an antiphase configuration. We, therefore,  
293 sought to examine whether the circuit connectivity of the FB would predict antiphasic relation  
294 between PFN<sub>a</sub> and PFN<sub>d</sub> neurons. To achieve that, we mapped the circuitry downstream of the  
295 two PFN populations using a recently completed connectome of a fly brain<sup>31</sup>. In our  
296 connectomic studies, we focused on the main postsynaptic targets of the PFN neurons, the  
297 hDelta interneurons. We, hence, sought to identify a pathway that would link PFNs via the  
298 hDelta interneurons to PFL3 neurons, a population of columnar neurons that translates goal  
299 signals in the FB into premotor steering commands<sup>21,22</sup> (Fig. 4a).

300 Each hDelta neuron innervates one ipsilateral and one contralateral column of the FB with an  
301 offset of four columns. Given the phasic organization of the FB, this offset corresponds to an  
302 approximately 180° shift (Fig. 4b). This morphology of the hDelta neurons positions them as a  
303 potential mediator of the antiphase relation between the PFN<sub>a</sub> and PFN<sub>d</sub> neurons, which is then  
304 ultimately inherited by the PFL3 neurons via additional intermediate neurons. Should this indeed  
305 be the case, a given column of PFL3 neurons would receive information from one PFN subtype  
306 (a or d) via the ipsilateral neurites of hDelta neurons and from the other PFN subtype via the  
307 contralateral neurites of other hDelta neurons. In this manner, the sinusoidal activity bump of  
308 one PFN population would be offset by 180° and, hence inverted, while the activity bump of the  
309 other PFN population would be unperturbed.

310 To determine whether the hDelta neurons indeed perform this signal inversion, we mapped their  
311 connectivity. Our analysis revealed that PFN<sub>d</sub> neurons connect to PFL3 neurons via hDeltaB  
312 neurons (Fig. 4c, d), and, further, that hDeltaBs map onto PFL3s via their ipsilateral neurites  
313 (Fig. 4d). Thus, the phase of the PFN<sub>d</sub>-borne sensory signal is likely untransformed through this  
314 layer of the circuit. By contrast, the PFN<sub>a</sub> neurons connect to PFL3 neurons via the contralateral  
315 neurites of the hDeltaC neurons (Fig. 4e, f). This anatomy indicates that the sensory-scaled  
316 representation of the navigational vector from PFN<sub>a</sub> neurons, but not from PFN<sub>d</sub> neurons, is  
317 inverted before being incorporated into the fly's goal signal (Fig. 4g). Thus, the antiphase  
318 relationship that we observed in our optogenetic activation experiments is likely due to the  
319 anatomical substrates that we identified in the FB connectivity.

## 320 **A model for PFN-instructed steering in walking flies**

321 Our results suggest a mechanism wherein the fly controls its steering maneuvers by comparing  
322 its internal heading signal to an external goal direction. This mechanism is supported by  
323 functional analysis of the FB<sup>21,22</sup>. Our results further suggest that asymmetric activation of PFN  
324 neurons transposes the fly's goal relative to its current heading. Because silencing PFNs  
325 produced straightened walking trajectories, we hypothesized that the fly continuously compares  
326 its heading with its goal to determine its angular velocity at any given moment. Thus, when  
327 PFNs are silenced, the heading and goal signals are constantly aligned, and when PFNs are  
328 asymmetrically activated, the fly performs a corresponding turn to align its heading with its goal  
329 direction (Fig. 5a-c). These behaviors indicate that the fly compares its heading and goal  
330 orientations during movement, and that the integration of these two parameters relative to each  
331 other over time enables the fly to produce smoothly curved walking trajectories.

332 To gain insight into how these two parameters—heading and goal directions—are integrated  
333 continuously to produce movement with a smooth curvature, we sought to construct a  
334 mathematical model for this behavior. We thus constructed a series of ordinary differential  
335 equations wherein the relative positions of the fly's heading ( $\theta$ ) and goal ( $\gamma$ ) determine its  
336 angular velocity ( $d\theta/dt$ ). Recent studies have proposed that steering commands from the central  
337 complex are proportional in their magnitude to the degree of offset between  $\theta$  and  $\gamma$ <sup>21,22</sup>. We  
338 hence modeled  $d\theta/dt$  as proportional to (*i.e.*, exhibiting a linear relationship with) the difference  
339 between  $\theta$  and  $\gamma$  (Fig. 5d). We then sought to characterize the forward motion trajectories that  
340 such a relationship between  $\theta$  and  $\gamma$  would produce when  $\theta$  and  $\gamma$  are misaligned.

341 We defined  $\gamma$  as a static value ( $d\gamma/dt = 0$ ), which produces a solvable system of ordinary  
342 differential equations. Varying the initial values for  $\theta$  and  $\gamma$  in these solved equations  
343 demonstrates how angular velocity changes depending on the degree of offset between goal  
344 and heading signals. We thus initialized  $\theta$  as equal to zero radians and varied the values of  $\gamma$   
345 between  $-\pi$  and  $\pi$  radians to cover the full range of potential offset angles between heading  
346 and goal orientations. Plotting this modeled orientation  $\theta$  over time showed smooth curves that  
347 were sharpest at the onset of the experiment before settling to straight lines as  $\theta$  approached  $\gamma$   
348 (Fig. 5e). Similarly, plotting the angular velocity  $d\theta/dt$  over time revealed curves that were  
349 sharpest during the onset of the experiment but resolved to zero over time (Fig. 5f). This pattern  
350 of angular velocity values mirrors our results for optogenetic activation of PFNs, in which  
351 angular velocity values shifted most dramatically upon the onset of stimulation before returning  
352 to baseline levels (Fig. 3f, j).



353 We next modeled how these predicted angular velocity values would manifest as walking  
354 trajectories. Our behavioral data indicated that bouts of translational motion tend to be at a  
355 stable walking speed (Extended Data Fig. 2d). Thus, we calculated theoretical walking  
356 trajectories by computing the movements in the x and y directions given our modeled  $\theta$  and  
357 assuming a constant walking speed. Our calculation produces smoothly curved walking  
358 trajectories that straighten once the flies are aligned to their respective  $\gamma$  values (Fig. 5g).

359 We next sought to define the parameters of the model such that they would reflect the fly's  
360 heading and goal coordinates when presented with a unidirectional optic flow stimulus. We  
361 hypothesized that when flies are presented with optic flow that emulates rotational self-motion,  
362 their goal direction is continuously offset from the heading proportionally to the rotational speed  
363 of the optic flow. We modeled this by defining  $\gamma$  to rotate in concert with angular velocity ( $d\gamma/dt =$   
364  $d\theta/dt$ ). Such a configuration causes constitutive misalignment of  $\theta$  and  $\gamma$  to various degrees  
365 according to the initial values of the two variables. As with our previous model, we initialized the  
366 value of  $\theta$  to equal 0 and varied the values of  $\gamma$  between  $-\pi$  and  $\pi$  radians to cover the full range  
367 of potential offset angles between heading and goal orientations.

368 In this configuration of the model,  $\theta$  changes linearly, and the rate of this change is proportional  
369 to the degree of offset between  $\theta$  and  $\gamma$  (Fig. 5h). Hence, the angular velocity values are fixed  
370 and are manifested as straight lines when plotted over time (Fig. 5i), mimicking the stable  
371 angular velocity values we observed in reorientation bouts (Fig. 1h, Extended Data Fig. 2b, c).  
372 Similarly, computing theoretical walking trajectories from the modeled values reveals circular  
373 movement patterns (Fig. 5j) that are analogous to those observed in reorientation bouts (Fig. 1f,  
374 g, Extended Data Fig. 2a). We conclude that these modeling results indicate a possible strategy  
375 used by the fly brain to integrate goal and heading signals to control the curvature of forward  
376 walking bouts during navigational behaviors.

## 377 Discussion

378 Surprisingly little is known about how neuronal activity in the FB drives locomotor behaviors.  
379 Our studies address this clear gap in knowledge by establishing a causal relationship between  
380 neuronal activity in the PFNs, a major input population to the FB, and steering movements. We  
381 demonstrate that thermogenetic silencing of PFNs resulted in the inability to elicit forward  
382 walking bouts with curved trajectories, which we interpret as deficits in steering control.  
383 However, optogenetic activation of PFNs was not wholly sufficient to elicit curved walking  
384 trajectories, such as those observed when descending command neurons for forward walking  
385 are optogenetically activated<sup>32</sup>. Our studies instead indicate that the steering commands to align  
386 the heading and goal signals are elicited only during the onset of asymmetric stimulation of  
387 PFNs. Beyond this onset period, shifts in angular motion during PFN stimulation are more  
388 consistent with biases in steering direction. PFNs may, therefore, function under natural  
389 conditions to maintain a stable heading during navigational behaviors by allowing the fly to  
390 smoothly adjust its movement trajectories in response to a dynamic influx of sensory cues. Such  
391 a role for the PFNs would, therefore, explain their necessity for curved walking bouts in our optic  
392 flow assay despite the apparent lack of an explicit goal coordinate in this behavioral paradigm.

393 Optomotor behaviors, such as those exhibited for gaze stabilization, are thought to be reflexive,  
394 *i.e.* reliant on simple sensorimotor transformations<sup>33-35</sup>. Therefore, our observation that the  
395 neural circuitry of the central complex is used to produce reorientation bouts in response to optic  
396 flow is intriguing. It is well established that PFN<sub>d</sub> neurons encode information about the direction

397 of the optic flow and contribute to building vectorial representations of the fly's ongoing travelling  
398 direction<sup>14,16</sup>. Nevertheless, how the information that PFN<sub>d</sub> neurons encode is used by the fly to  
399 elicit goal-directed behaviors remains unknown. Our observation that PFN<sub>d</sub> neurons are  
400 necessary for the fly to elicit curved bouts of continuous movement to align with the direction of  
401 optic flow may indicate that the fly uses self-motion cues to maintain a stable goal coordinate. If  
402 this is indeed the case, optic flow signals in the central complex can be likened to an error  
403 correction mechanism, where heading, travelling, and goal directions are continuously  
404 compared to compute movement decisions.

405 Our optogenetic activation experiments revealed that the PFN<sub>a</sub> and PFN<sub>d</sub> subtypes are  
406 correlated and anticorrelated with angular motion, respectively. We interpret these data to  
407 indicate that the two populations are configured in antiphase, an interpretation that is supported  
408 by our connectomic analyses of the FB circuit. This antiphase relationship may explain why the  
409 simultaneous activation of PFN<sub>a</sub> and PFN<sub>d</sub> neurons resulted in decreased locomotion as the  
410 sum of two counterphase sine waves results in destructive interference. In the most extreme  
411 case, such an interference would manifest as a complete cessation of movement, as we  
412 sometimes observed.

413 During navigational behaviors, animals must integrate disparate sensory cues into a single  
414 movement decision. The brain must, therefore, contain a mechanism for comparing these cues  
415 and executing locomotor behaviors in accordance. One such mechanism would employ a  
416 “winner takes all” strategy, where the brain weighs the various sensory cues and selects only  
417 the most salient for its heading decision. An alternative would employ a “summation” strategy in  
418 which the brain incorporates all the various relevant sensory cues and computes its movement  
419 decision accordingly. We found that the parallel sensory signals in PFN<sub>a</sub> and PFN<sub>d</sub>  
420 subpopulations and their relationships with locomotor behavior were consistent with a  
421 summation strategy. Similar summation mechanisms that function within PFN subtypes  
422 responding to the same sensory modality have been shown<sup>14,16</sup>. However, no such mechanism  
423 has been described to perform an analogous transformation across parallel PFN subsystems  
424 responding to different modalities. Our studies thus lay the groundwork for future research to  
425 identify the nodes of convergence between the PFN<sub>a</sub> and PFN<sub>d</sub> pathways that mediate these  
426 summative properties.

427 It is noteworthy that our optogenetic activation experiments were designed to study the effects  
428 of exogenous neuronal activity in the central complex while minimizing any influence from  
429 external sensory cues. Flies are capable of complex navigational behaviors like path integration  
430 while relying on an entirely idiothetic sense of space<sup>36-38</sup>. However, some of the PFNs analyzed  
431 in this study are known to be negatively correlated with heading in the absence of visual cues  
432 and positively correlated with heading in the presence of visual feedback<sup>9</sup>. Additionally, the  
433 influence of wind-tracking PFNs on movement depends on the presence and valence of  
434 odorants in the environment<sup>17</sup>. We, therefore, expect our results to represent only a narrow  
435 range of the properties demonstrated by this circuitry under natural conditions. Finally, since our  
436 manipulations were performed in walking flies, whether the mechanisms we identified extend to  
437 similar directional maneuvers during flight is yet unknown. That said, the PFN circuitry is indeed  
438 engaged during flight<sup>9,16</sup>. Therefore, we expect that in airborne flies the PFNs perform similar  
439 computations to those described in this study.

440 The activity bumps in the central complex operate as vectorial representations of sensory  
441 information<sup>14,16</sup>. The topographical organization of the central complex has rendered it an

442 attractive system for studying how neural circuits can transform these vector codes into  
443 navigational behavior outputs. Such characterization has led to the establishment of basic  
444 principles for how ensembles of neurons can perform fundamental mathematical operations like  
445 vector addition<sup>14,16,21,22</sup> and inversion<sup>39</sup>. Our studies contribute to this growing body of knowledge  
446 by revealing how the fly brain may integrate the relative positions of various vector codes over  
447 time to guide movement. These basic principles could potentially extend to vertebrate systems  
448 where the animal may perform more complex navigation tasks. Vector codes are indeed  
449 ubiquitous in the mammalian brain<sup>40</sup>, including head direction-representing cells that are  
450 analogous to the EB-born heading signal<sup>41-43</sup>. Further, modelling studies predict that the  
451 cognitive maps of space in the mammalian hippocampus are constructed via vectorial  
452 representations of environmental boundaries and landmarks<sup>44,45</sup>. Understanding the neural  
453 connectivity motifs underlying the function of the *Drosophila* central complex may, therefore,  
454 provide a fundamental basis for understanding how the brain performs navigational tasks in  
455 diverse animal species.

## 456 **Materials and methods**

### 457 **Fly genetics**

458 All fly stocks were maintained at either 18°C or 21°C on standard cornmeal-molasses-agar  
459 media. Crosses and their progeny, unless otherwise stated, were kept at 25°C in a humidity-  
460 controlled incubator with a 12-hour light and 12-hour dark cycle. The fly lines that were used in  
461 this study were as follows: W1118 (BDSC #5905), UAS-shibire<sup>TS</sup> 46, SS02255-Gal4 (BDSC  
462 #75923), SS00078-Gal4 (BDSC #75854), R16D01-Gal4 (BDSC #48722), SS00090-Gal4  
463 (BDSC #75849), SS54549-Gal4 (BDSC #86603), SS00081-Gal4 (BDSC #75848), UAS-  
464 CsChrimson::Venus (BDSC #55135), nSyb-IVS-PhiC31 (BDSC #84151), UAS-IVS-PhiC31  
465 (BDSC #84154), UAS-SPARC2-S-CsChrimson::tdTomato (BDSC #84145), UAS-SPARC2-I-  
466 CsChrimson::tdTomato (BDSC #84144).

### 467 **Locomotion assay**

468 All behavior experiments were performed in a temperature and humidity-controlled chamber.  
469 Unless otherwise stated, behavior experiments were performed at 25°C and 60% humidity. We  
470 performed our locomotion assays in an arena based on previously established FlyBowl<sup>25</sup> with  
471 several modifications. Briefly, a circular piece of white delrin plastic was cut to feature sloped  
472 walls according to the FlyBowl dimensions<sup>25</sup> to construct the arena. A plexiglass cover was cut  
473 to serve as the ceiling of the chamber. A custom-built circular LED array featuring IR and red  
474 (650nm) lights (LEDSupply) was positioned underneath the arena. Red LEDs were wired via a  
475 1000mA BuckPuck driver (LEDSupply) to enable variable intensities of light. A diffuser sheet  
476 was placed above the LED array to ensure lighting was even throughout the arena. LED  
477 systems and diffusers were placed inside 3D printed opaque cylinders to focus the LEDs' light to  
478 the arena. The LED system was connected to a Pololu server controller via a relay module to  
479 achieve computer control. Fixed above the arena, we positioned a digital camera (FLIR Blackfly  
480 S U3-13Y3M-C) with a varifocal lens (LMVZ990-IR) that was fitted with a near-IR bandpass  
481 (Midopt BP850) to record the behavior trials. Videos were recorded via Bonsai at 1280x1040  
482 resolution and 30 FPS. All behavior trials were recorded in this arena. All trials except  
483 optogenetic activation assays were performed under white light (~45 μW/cm<sup>2</sup>) with a polarizing  
484 filter to act as a celestial landmark.

### 485 **Thermogenetic silencing**

486 Flies that were assayed for our shibire<sup>TS</sup> experiments were analyzed at either 21°C or 31°C by  
487 adjusting the temperature in our behavior chamber. Flies that were analyzed as part of these  
488 experiments were placed in 21°C temperature- and humidity-controlled incubators upon  
489 eclosion. Flies in the 31°C groups were placed in the chamber for at least 30 minutes before  
490 being assayed to allow flies to acclimate to the temperature increase. Flies were analyzed at  
491 age 6-9 days old. One fly was subjected to the paradigm at a time. During the assay, we placed  
492 a custom-built arrangement of 15 8x8 green LED arrays (Adafruit) on top of the chamber such  
493 that the LEDs encircled the behavior arena. LED arrays were wired in parallel and connected to  
494 an Arduino to control the position of vertical bar stimulus. Custom Arduino scripts were written  
495 for the different stimulus paradigms: clockwise, counterclockwise, and still green vertical bars.  
496 Using bonsai, we tracked the fly's position to calculate its translational velocity in real time.  
497 When this value was greater than 1 pixel, a signal is sent to the VR Arduino to permit moving  
498 the stimulus. For clockwise and counterclockwise moving vertical bars, the bar positions would  
499 update every 25ms—thus a full rotation around the circumference of the arena takes 3s. For the  
500 still bars paradigm, one of the eight possible bar positions was chosen at random during the  
501 program's onset and the bar remained still at that position for the duration of the experiment. All  
502 15 8x8 arrays were wired in such a way that each array received the same instructions and thus  
503 depicted bars in the same position at each timestep to thus display a uniform visual field.

#### 504 **Transient optogenetic activation assay**

505 Progeny from crosses for optogenetic activation experiments were divided into two groups. The  
506 first group was raised on a diet of standard *Drosophila* media with all-trans retinal (ATR) (Sigma  
507 R2500) mixed in with a final concentration of 400 µM. This group is denoted as ATR+. The  
508 second group was raised on a diet of standard *Drosophila* media that was mixed with 100%  
509 ethanol, the solvent that was used for the ATR. The volume of ethanol added was equivalent to  
510 the volume of ATR added in the ATR+ vials. This group is denoted as ATR-. Flies used for  
511 optogenetics experiments were raised in an incubator in the absence of any light. Each trial  
512 consists of a single male fly. Red light intensity was calibrated to ~5.0 mW/cm<sup>2</sup> and shown  
513 continuously throughout the stimulus bouts. A single stimulus bout was defined as a single 20s  
514 delivery of red light with 20s rest periods before and after stimulus delivery. A small red light was  
515 placed in view of the camera during all trials to indicate when the optogenetic stimulus was  
516 delivered in each video.

#### 517 **Sparse activation of columnar neurons**

518 Sparse activation of PFNs was achieved through the previously established SPARC method<sup>30</sup>.  
519 PFN SPARC experiments were performed using the nSyb-IVS-PhiC31 SPARC configuration to  
520 achieve sparse labeling since the driver line contained off-target neurons that would be more  
521 likely to be included in sparse labeling experiments if the UAS-IVS-Phic31 allele was used. We  
522 used the UAS-SPARC2-S-CsChrimson::tdTomato allele to achieve sparse labeling since it  
523 labeled the smallest proportion of neurons from the starter population. SPARC animals were  
524 dissected less than 24 hours after behavioral profiling and then subjected to our IHC protocol.  
525 Each fly was stained independently and labeled with a unique identifier number to ensure that  
526 each dissected brain preparation could be matched to their respective behavior trials. Trials  
527 from 72 total flies were included as part of our final dataset.

#### 528 **Immunohistochemistry and tissue processing**



529 Immunohistochemistry was performed on adult brains as previously described<sup>47</sup> but with slight  
530 variations. Briefly, adult flies were cold anesthetized on ice and dissected in cold 0.05% PBS-T  
531 (T stands for Triton X-100; Fisher Bioreagents, BP151-500). All following steps were performed  
532 while brains were nutating. Brains were fixed in 2% PFA/0.5% PBS-T at 4°C overnight. Samples  
533 were then washed 4X in 0.5% PBS-T for 15 min each at RT. Brains were then blocked for 30  
534 min at RT in 5% heat-inactivated equine serum (diluted from 100% with 0.5% PBS-T) and then  
535 incubated with primary antibodies for two overnights at 4°C. Brains were then again washed 4X  
536 in 0.5% PBS-T for 15 min each and then incubated with secondary antibodies for two overnights  
537 at 4°C. The samples were then washed again 4X in 0.5% PBS-T for 15 min each before being  
538 mounting on a slide (Fisherbrand Superfrost Plus, 12-550-15) in Fluoromount-G mounting  
539 medium (SouthernBiotech, 0100-01). The primary antibodies that were used in this study were:  
540 Goat anti-GFP (Rockland #600-101-215, 1:1000), Guinea Pig anti-RFP (Gift from Susan  
541 Brenner-Morton, Columbia University, 1:10,000), and anti-Brp mouse (nc82, DSHB, 1:50).  
542 Secondary antibodies were diluted to 1:1,000. The secondary antibodies used in this study  
543 were: donkey anti-Goat Alexa Fluor 488, donkey anti-Guinea pig Alexa Fluor 555, and donkey  
544 anti-Mouse 647. Images were taken using confocal microscopy (Zeiss, LSM800) using Zen  
545 software (Zeiss). Images were formatted and processed using FIJI (<http://fiji.sc>).

546

## 547 **Quantification and statistical analysis**

### 548 **Analysis of locomotor behavior videos**

549 Automated kinematic tracking of behavior trials was performed via FlyTracker<sup>26</sup>. FlyTracker  
550 outputs x and y coordinates and orientation angle for every frame of the behavior videos.  
551 Custom R scripts were written to calculate translational and angular velocity from FlyTracker  
552 outputs. Translational velocity was calculated as the Euclidean distance between x and y  
553 coordinates between successive frames. Angular velocity was calculated as the distance  
554 between orientation angle between successive frames. Data was then smoothed using a  
555 Gaussian filter with a spread of 10 frames. When computing mean velocity values in our  
556 shibire<sup>TS</sup> experiments, only frames when the fly was less than 30 mm from the center were  
557 considered, since this is the region of the of the arena where the flies perform circular walking  
558 trajectories. Mean  $\Delta$  angular velocity and mean  $\Delta$  translational velocity were calculated as the  
559 difference between the means of the velocity value for the frames during which the optogenetic  
560 stimulus was off and the frames during which the optogenetic stimulus was on. When  
561 translational velocity values were compared in our optogenetics experiments, we normalized  
562 translational velocity values by dividing all values by the maximum translational velocity value  
563 for that particular fly. This enabled comparison between flies while accounting for variability in  
564 each fly's walking speed. All statistical comparisons were performed using a one-way anova  
565 followed by a *post hoc* Tukey test for multiple comparisons. R code that was used to generate  
566 figures is available upon request.

### 567 **Quantification of CsChrimson expression**

568 CsChrimson expression was quantified via fluorescence intensity in FIJI. In our PFN SPARC  
569 experiments, we determined the level of CsChrimson expression in a nodulus by manually  
570 selecting an ROI of a collapsed z-stack of the noduli. We calculated the intensity of labeling as  
571 the raw integrated density of signal divided by the area of the noduli.  $\Delta NO_a$  and  $\Delta NO_d$  indices  
572 were calculated with the following formula:

$$\frac{\text{Right NO Signal} - \text{Left NO signal}}{\text{Right NO signal} + \text{Left NO signal}}$$

573 The  $\Delta\text{NO}_{a-d}$  was calculated via the following formula:

$$\frac{\text{Right NOa Signal} - \text{Left NOa signal} - \text{Right NOd Signal} + \text{Left NOd Signal}}{\text{Right NOa signal} + \text{Left NOa signal} + \text{Right NOd signal} + \text{Left NOd Signal}}$$

574 We computed our weighted  $\Delta\text{NO}_{a-d}$  index via the following formula.

$$\frac{(1 + \text{weight}) * (\text{Right NOa Signal} - \text{Left NOa Signal}) - (1 - \text{weight}) * (\text{Right NOd signal} - \text{Left NOd signal})}{(1 + \text{weight}) * (\text{Right NOa Signal} + \text{Left NOa Singal}) + (1 - \text{weight}) * (\text{Right NOa Signal} + \text{Left NOa Signal})}$$

575 With *weight* being a value that ranges from -1 to 1.

### 576 **ODE model for goal-oriented steering**

577 The system of equations that we used for our model for central complex-mediated steering  
578 control in which the goal coordinate was fixed was as follows:

$$\frac{d\theta}{dt} = k * (\theta - \gamma)$$
$$\frac{d\gamma}{dt} = 0$$

579 Here,  $\theta$  equals the fly's heading direction and  $\gamma$  equals an external goal direction. The constant  $k$   
580 represents the value of the fly's alignment speed, i.e., the rate at which the fly turns to align its  
581 heading and goal parameters. For our experiments, we set this constant  $k$  to an arbitrary value  
582 of 1. Our system of equations solves to the following functions for  $\theta$  and  $\gamma$ , given the initial  
583 values  $\theta_0$  and  $\gamma_0$ :

$$\theta(t) = \frac{\theta_0}{e^{k*t}} + \frac{\gamma_0}{e^{k*t}} - \gamma_0$$
$$\gamma(t) = \gamma_0$$

584 We initialized the values of  $\theta_0$  as 0 and varied  $\gamma_0$  between  $-\pi$  and  $\pi$ . We then used these equations  
585 to determine the values of  $d\theta/dt$  and  $\theta$  from  $t=0$  to  $t=5$ . We transformed these values of  $\theta$  into  $x$  and  
586  $y$  coordinates in space using the following equations:

$$x(t) = x_{t-1} + s * \cos(\theta_t)$$
$$y(t) = y_{t-1} + s * \sin(\theta_t)$$

587 Here,  $s$  denotes an arbitrary constant for the fly's magnitude of translational motion. In our  
588 calculations, we used a value of 1 for  $s$ . We initialized  $x_0$  and  $y_0$  to both equal 0.

589 In the case where the heading and goal coordinates were constitutively offset, we used the  
590 following system of equations:

$$\frac{d\theta}{dt} = k * (\theta - \gamma)$$

$$\frac{d\gamma}{dt} = k * (\theta - \gamma)$$

591 We solved this system with k equaling 1 as above and given the initial values of  $\theta$  and  $\gamma$  as  $\theta_0$   
592 and  $\gamma_0$  respectively to produces the following equations:

$$\theta(t) = k * t * (\theta_0 - \gamma_0) + \theta_0$$

$$\gamma(t) = k * t * (\theta_0 - \gamma_0) + \gamma_0$$

593 We then set  $\theta_0$  to equal 0 and varied  $\gamma_0$  between  $-\pi$  and  $\pi$  as above. We modeled walking  
594 trajectories that would arise from the modeled  $\theta$  values by calculating x, y coordinates for each  
595 timepoint as described above.

### 596 **Circuit reconstructions of electron microscopy data**

597 Reconstructions of central complex neuropil segmentations and PFN, hDelta, and PFL3  
598 neurons from were accessed via the publicly available Neuprint server for querying data from  
599 the hemibrain connectome<sup>48,49</sup>. 3-D reconstructions were obtained as .obj files and  
600 visualized/rendered in blender. Colors were manually selected to correspond to their anatomy.  
601 Information on the synaptic connectivity for individual neurons was accessed via Flywire  
602 (flywire.ai)<sup>31</sup>. As part of our analysis, we only considered neurons that connect via at least 5  
603 synapses to be connected.

### 604 **Data availability**

605 Upon acceptance and publication of this manuscript, all kinematic data and analysis code used  
606 for this study will be made available at [github.com/anthonycrown/](https://github.com/anthonycrown/)

607

### 608 **Acknowledgements**

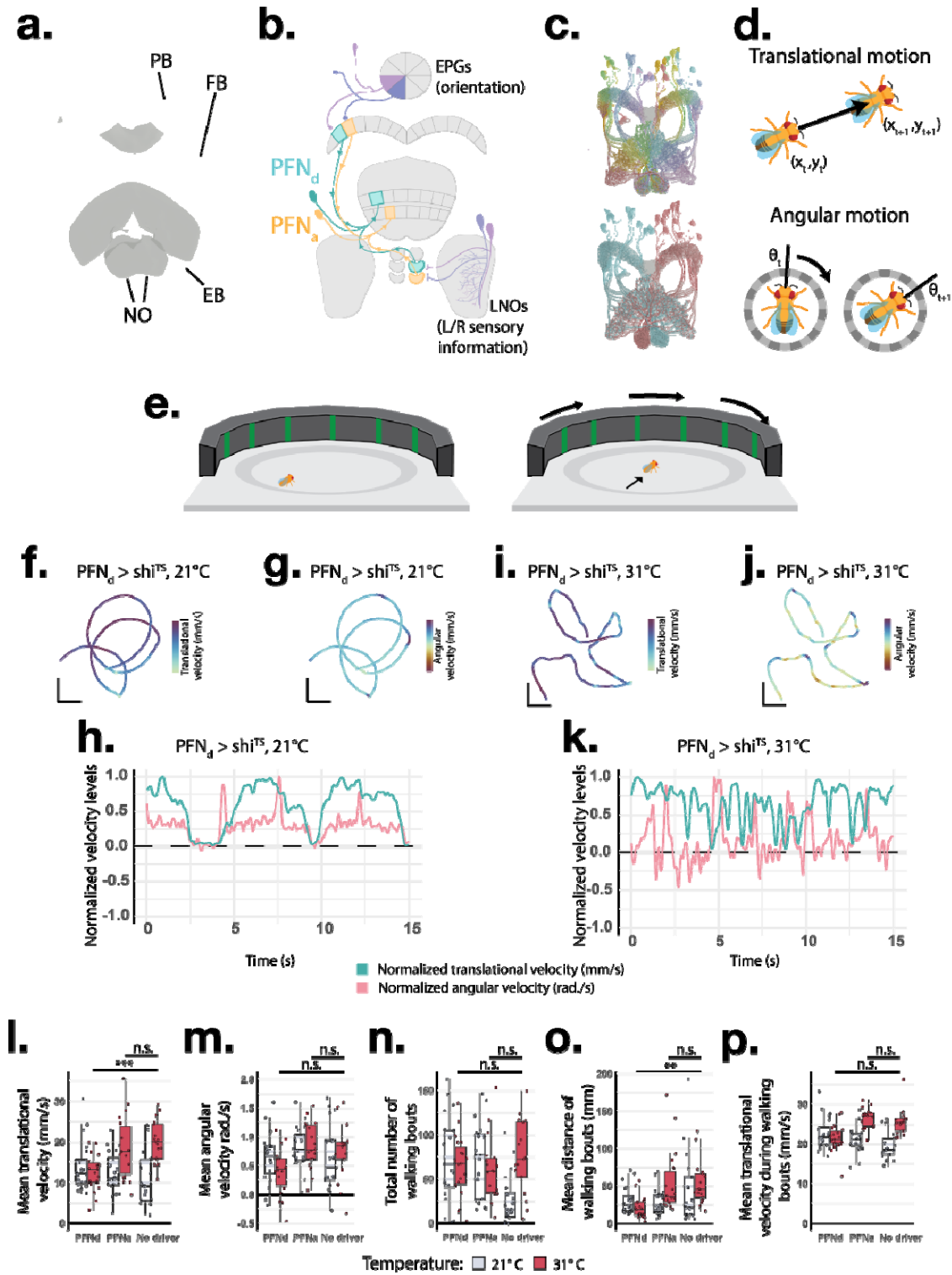
609 We thank Dr. Vanessa Ruta, Dr. Charlie Dowell, Dr. Alexander Fleischmann, and the members  
610 of the Barnea Laboratory for critical reading of the manuscript. We are grateful to Susan Morton  
611 for sharing reagents. We thank John Murphy from the Brown BioMed Machine Shop for aiding  
612 in the construction of our behavior chamber. This work was supported by NIH NINDS grant  
613 5R01NS133238 (G.B.), and NIH/NIDCD award F31DC019540 (A.M.C.). Stocks obtained from  
614 the Bloomington *Drosophila* Stock Center (NIH P40OD018537) were used in this study.

615

### 616 **Author contributions**

617 A.M.C. and G.B. conceived the project. Behavioral experiments and pre-processing of the  
618 resultant data were performed by A.M.C., H.W., and L.H. Immunohistochemical analyses were  
619 performed and analyzed by A.M.C. Data analysis and modeling were performed by A.M.C. Data  
620 were interpreted by A.M.C. and G.B. The manuscript was written by A.M.C. and G.B.

621



622 Figure 1. PFNs are necessary for controlling curvature of walking trajectories.



623 **(a)** EM reconstructions of the main compartments of the central complex. **(b)** Schematic  
624 representation of the flow of information to the PFNs. EPG neurons (two shades of purple,  
625 above), encode the fly's heading direction. Axons from an EPG neuron innervate a column of  
626 the PB. LNO neurons (two shades of purple, below) encode various left-vs-right sensory  
627 signals. Each LNO neuron innervates either a left or right nodulus. LNO neurons that encode  
628 different sensory signals innervate different noduli. Single PFN<sub>a</sub> neurons (orange) and PFN<sub>d</sub>  
629 neurons (blue) receive input from a single PB column and a single nodulus. **(c)** EM  
630 reconstructions of PFN neurons colored by either their FB column position (above) or the noduli  
631 from which they receive input (below). **(d)** Parameters used for quantifying translational (above)  
632 and angular (below) locomotion. **(e)** Cartoon representation of the behavioral paradigm. Flies  
633 are presented with unidirectional optic flow, which is locked in closed loop with their translational  
634 motion. **(f-k)** Representative walking trajectories from a unidirectional optic flow assay. Flies  
635 express the thermogenetic silencer *Shibire*<sup>TS</sup> in PFN<sub>d</sub> neurons. (f-k) depict 15s of walking at the  
636 permissive 21°C (f-h) and restrictive 31°C (i-k) temperatures. Trajectories are colored to depict  
637 either translational (f, i) or angular (g, j) velocity values. (h, k) depict translational velocity (cyan)  
638 and angular velocity (red) values over the course of the 15s walking bout. Velocity values were  
639 normalized to enable comparisons of how the two values vary over time. **(l-p)** Boxplots depicting  
640 changes in mean translational (l) and angular (m) velocity values, total number of walking bouts  
641 (n), average distance of walking bouts (o), and average translational velocity values during  
642 walking bouts (p) for 21°C and 31°C trials. Positive angular velocity values in (g, h, j, k, m) are  
643 towards the direction of the stimulus. One-way ANOVA with post-hoc Tukey's multiple  
644 comparison test was used for statistical testing (\* =  $p < 0.05$ , \*\* =  $p < 0.01$ , \*\*\* =  $p < 0.001$ ).  
645 Scale bars in f, g = 10mm, i, j = 20mm.

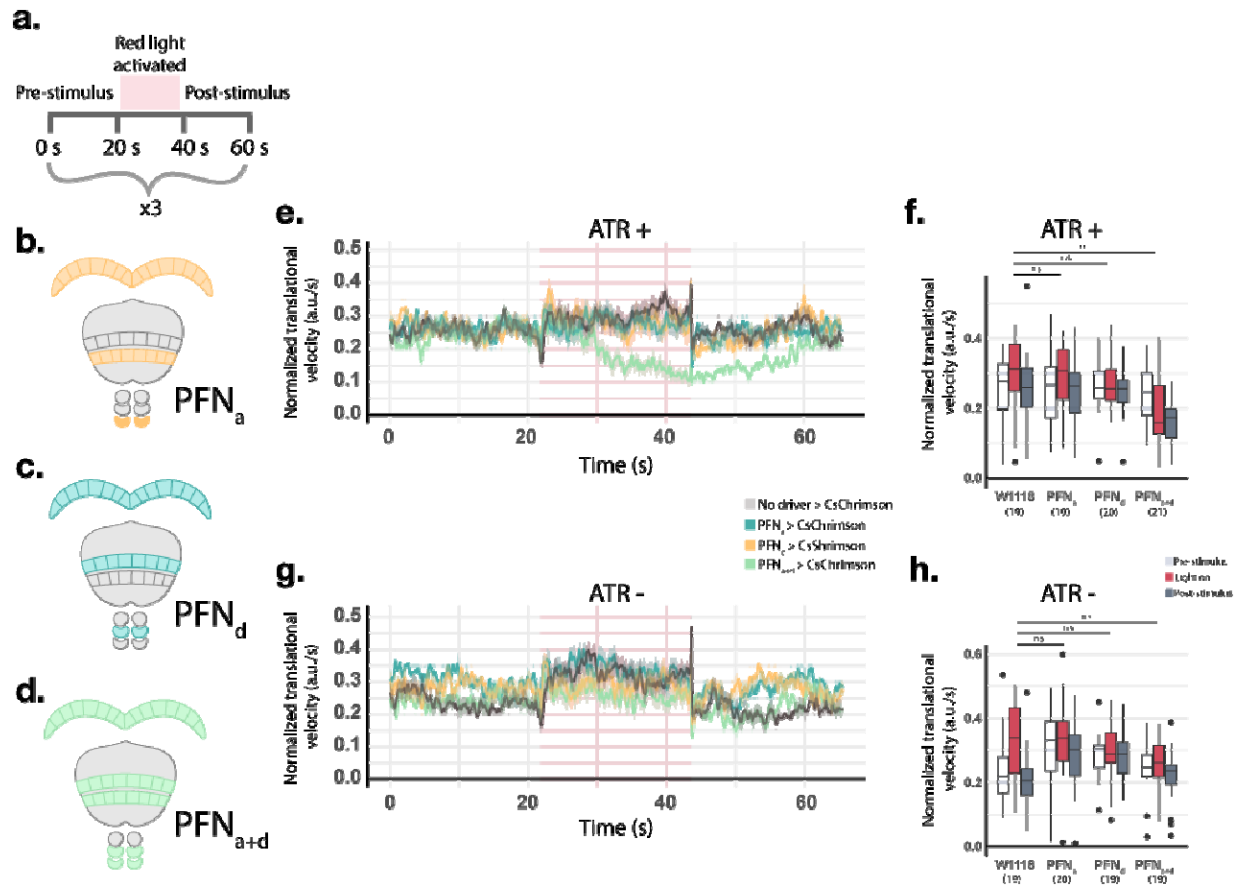
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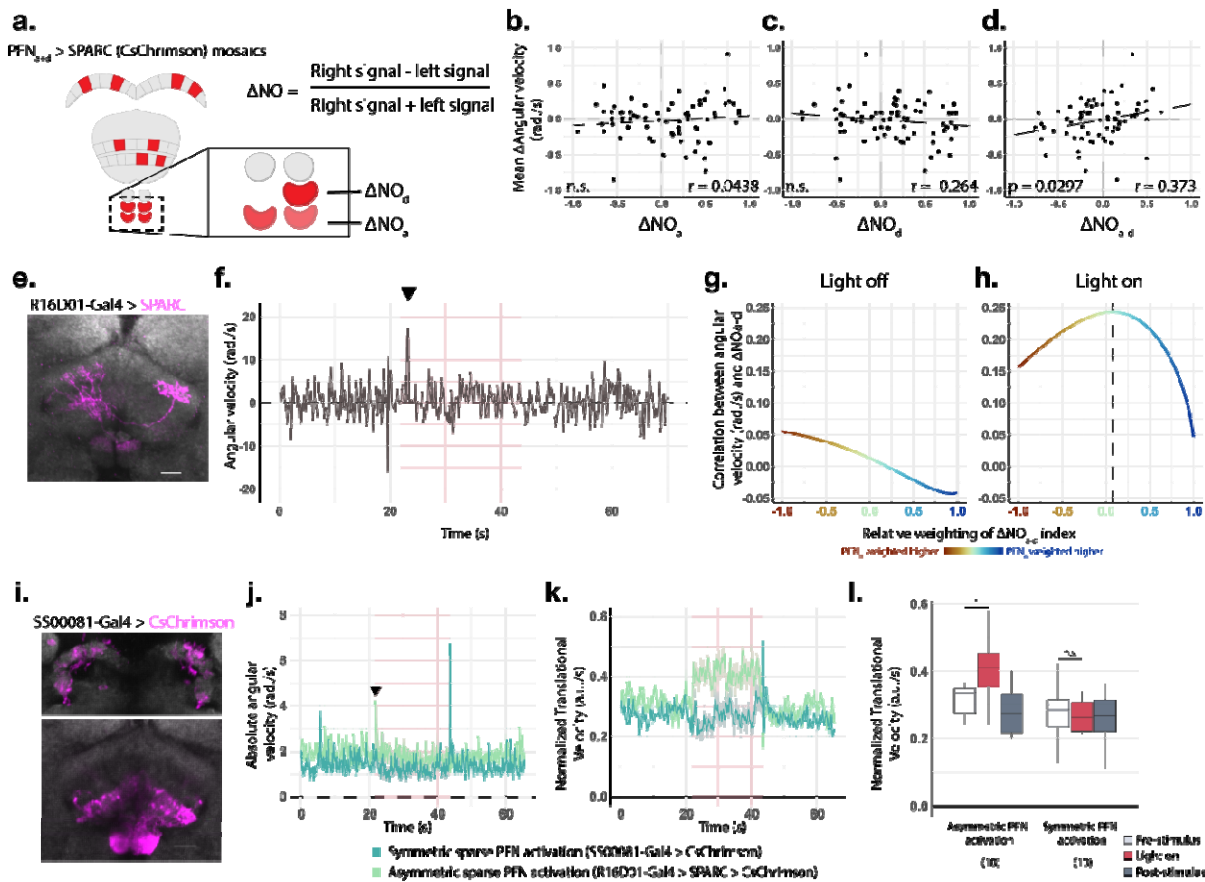
652 **Figure 2. Simultaneous activation of PFN<sub>a</sub> and PFN<sub>d</sub> neurons suppresses locomotion.**

653 **(a)** Paradigm for optogenetic activation experiments. Flies are exposed to 20s of red light, with  
 654 20s rest periods before and after each stimulus. Each fly is exposed to three stimulus bouts  
 655 total. **(b-d)** Cartoon depiction of the cell-types targeted by each driver line. Driver lines that  
 656 target either PFN<sub>a</sub> neurons individually (b, blue), PFN<sub>d</sub> neurons individually (c, yellow), or both  
 657 PFN<sub>a</sub> and PFN<sub>d</sub> populations (d, green), were employed. **(e)** line plot depicting averaged  
 658 translational velocity values ( $\pm$ s.e.) for each stimulus bout for the various genotypes. Flies were  
 659 raised on diet supplemented with all-trans retinal (ATR+), the necessary cofactor for  
 660 CsChrimson. Red box indicates time interval when the optogenetic stimulus was delivered. See  
 661 **(f)** for the numbers of trials (N) that were averaged in each group. **(f)** Boxplot of mean  
 662 translational velocity values during each optogenetic stimulus bout for the various genotypes in  
 663 the ATR+ condition. Values are shown for the optogenetic stimulus period as well as for pre- and  
 664 post-stimulus periods. **(g)** and **(h)** correspond to **(e)** and **(f)** respectively, but for flies that were  
 665 raised on diets without ATR. In e-h, translational velocity values for each fly were normalized  
 666 such that the maximum for each fly equals 1 to account for variability in flies' walking speeds.  
 667 One-way ANOVA2 with post hoc Tukey's multiple comparison test was used for statistical  
 668 testing. ( \*\* =  $p < 0.01$  )

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672 **Figure 3. Asymmetric activation of PFNs shifts heading direction.**

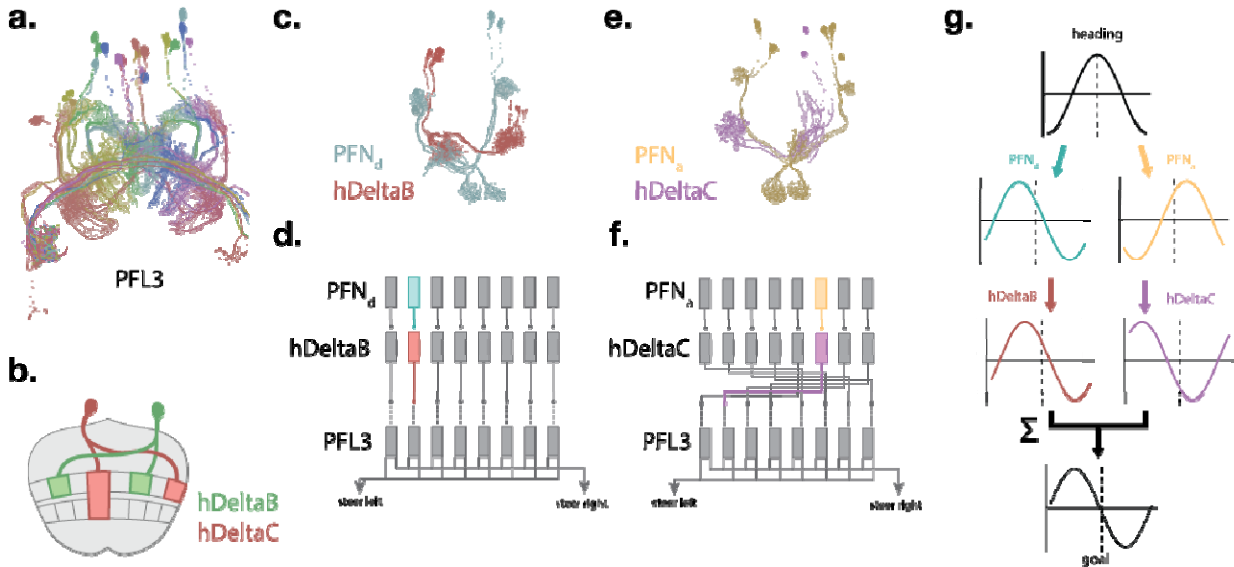
673 **(a)** Schematic representation of how  $\Delta NO$  indices of PFN asymmetry were calculated amongst  
 674 PFN<sub>a+d</sub> mosaic flies (see methods for details). **(b-d)** Scatterplot of PFN<sub>a+d</sub> > SPARC  
 675 experiments. Y-axis represents the change in mean angular velocity between time periods when  
 676 the optogenetic stimulus was off versus when the optogenetic stimulus was on. X-axis depicts  
 677  $\Delta NO$  indices for (b) PFN<sub>a</sub> neurons ( $\Delta NO_a$ ), (c) PFN<sub>d</sub> neurons ( $\Delta NO_d$ ), and (d) summed  
 678 contributions of both populations ( $\Delta NO_{a+d}$ ).  $r$  values represent the Pearson correlation  
 679 coefficients. **(e)** Representative image of PFN<sub>a+d</sub> > SPARC CsChrimson expression pattern  
 680 (magenta) in the FB and NO. **(f)** Line plot depicting angular velocity values for the fly depicted in  
 681 (e). One optogenetic stimulus bout is shown. **(g, h)** Line plot of relative contributions of PFN<sub>a</sub>  
 682 and PFN<sub>d</sub> neurons to angular velocity values by computing weighted  $\Delta NO_{a+d}$  indices. Y-axis  
 683 shows the Pearson correlation between the  $\Delta NO_{a+d}$  index and mean angular velocity values for  
 684 PFN<sub>a+d</sub> > SPARC CsChrimson trials. (g) and (h) depict the time intervals when the optogenetic  
 685 stimulus was off and on respectively. X-axis and colors depict relative weighting of PFN<sub>d</sub> neurons  
 686 (red, -1) and PFN<sub>a</sub> neurons (blue, +1). Dotted line in (h) denotes the maximum point. **(i)**  
 687 Targeted expression pattern of CsChrimson (magenta) in the PB (upper panel) and the FB/NO  
 688 (lower panel) via the sparse but symmetric PFN<sub>a</sub> driver (SS00081-Gal4). **(j-k)** Line plots of  
 689 averaged absolute angular velocity values (j) and normalized translational velocity values (k)  
 690 when activating symmetric (SS00081-Gal4 > CsChrimson) or asymmetric (PFN<sub>a+d</sub> > SPARC  
 691 CsChrimson) sparse PFN subsets. Averaged values for ten trials shown. **(l)** Boxplot of mean  
 692 normalized translational velocity values during the various optogenetic stimulation periods for  
 693 trials depicted in (k). Scale bars in e, i = 10 $\mu$ m. One-way ANOVA with *post hoc* Tukey's multiple  
 694 comparison test was used for statistical testing in (i). (\* =  $p < 0.05$ )





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698 **Figure 4. Mapping of PFN-born sensory signals onto central complex output neurons.**

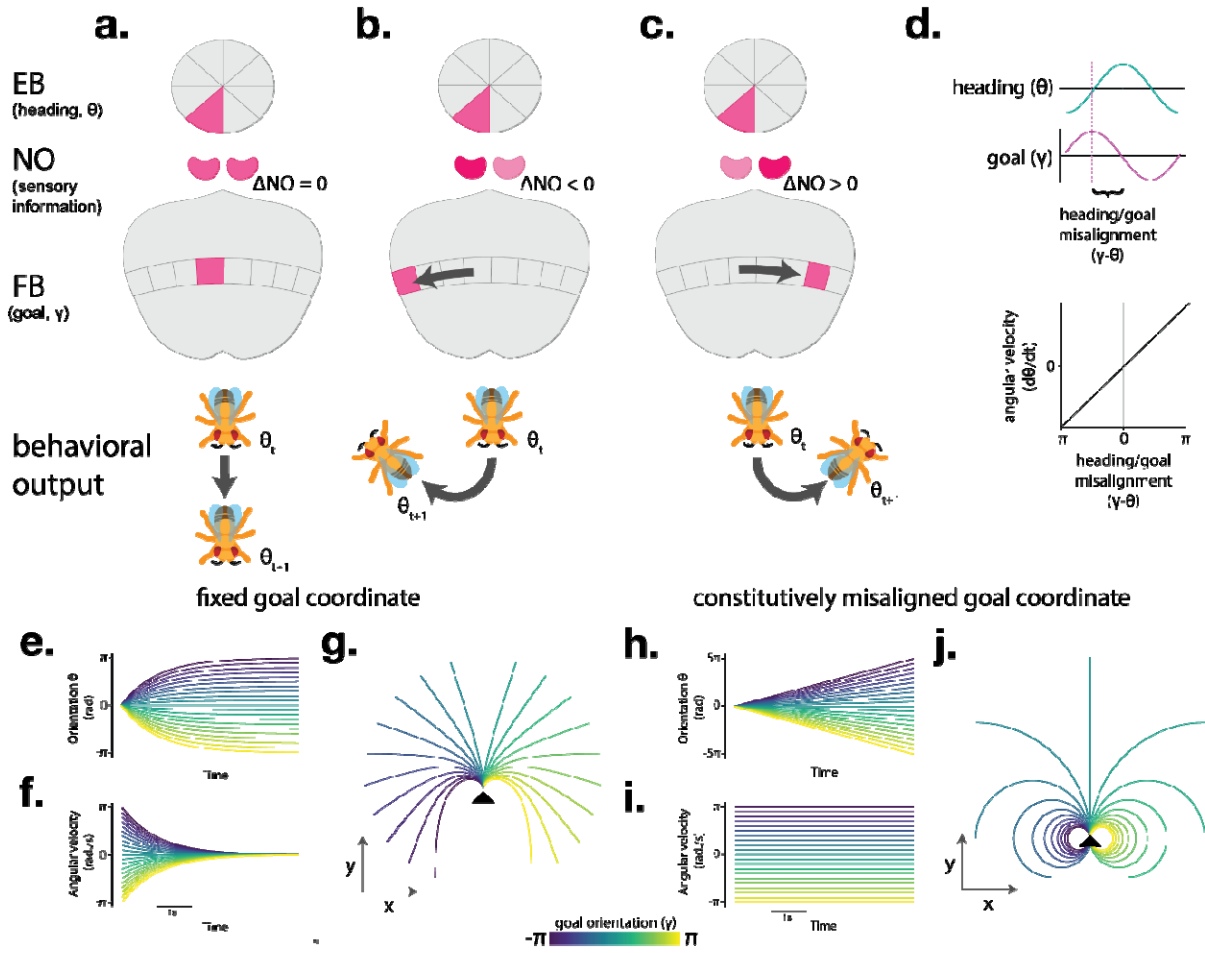
699 **(a)** EM reconstruction of PFL3s, putative outputs of the central complex circuit, colored by FB  
 700 column position. **(b)** Cartoon depiction of hDeltaB and hDeltaC neurons. Each hDelta neuron  
 701 projects both ipsilateral and contralateral neurites. The ipsi- and contralateral neurites of a given  
 702 hDelta neuron are offset by four FB columns. **(c-f)** EM reconstructions of the PFN neurons and  
 703 hDelta neurons that are upstream of the PFL3s. For simplicity, only the populations that are  
 704 upstream of the PFL3 neurons in the second FB column are shown. (c) EM reconstructions of  
 705 the PFN<sub>d</sub> neurons and hDeltaB neurons that are upstream of the PFL3s. (d) Cartoon depiction  
 706 of the mapping of PFN<sub>d</sub> neurons onto the PFL3s. Colors correspond to neurons depicted in (c).  
 707 (e) Same as (c) but for PFN<sub>a</sub> neurons and hDeltaC neurons. (f) Same as (d) but for PFN<sub>a</sub>  
 708 neurons. Colors correspond to neurons depicted in (e). Note that in (e, f) the depicted PFN<sub>a</sub>  
 709 neurons are offset from the second FB column and instead innervate the sixth column of the FB.  
 710 **(g)** Example of the transformations that the heading signal, depicted as a sine wave, undergoes  
 711 before forming a goal signal. PFN<sub>d</sub> and PFN<sub>a</sub> neurons offset the heading signal based on left-vs-  
 712 right sensory information. hDeltaB neurons inherit the PFN<sub>d</sub> sensory signal and leave it  
 713 untransformed. hDeltaC neurons inherit the PFN<sub>a</sub> sensory signal and invert its phase. The sum  
 714 of the hDeltaB and hDeltaC signals forms a goal signal that is relayed to the PFL3s for eliciting  
 715 steering commands. The dotted line depicts the position of the heading signal.

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721 **Figure 5. A model for central complex-mediated steering control.**

722 **(a-c)** Cartoon depictions of the relationship between heading signals, goal signals, and  
 723 locomotion. From top to bottom: the heading signal in the EB, varying levels of asymmetric NO  
 724 activation (depicted by color intensity), transposed goal signal in the FB, and hypothetical  
 725 resultant walking trajectories ( $\theta_t$  represents initial timepoint,  $\theta_{t+1}$  represents end timepoint).  
 726 Symmetric NO activation in (a) results in aligned heading and goal signals. Asymmetric  
 727 activation in the NO as depicted in (b, c) transposes the goal signal and guides steering  
 728 movements in the corresponding directions. **(d)** Parameters of model for central complex-  
 729 mediated steering control. Angular velocity is directly proportional to the offset between heading  
 730 and goal coordinates. **(e-g)** Modelling fly movement during orientation towards a fixed goal  
 731 coordinate ( $dy/dt = 0$ ). Predicted orientation (d), angular velocity (e), and walking trajectories (f)  
 732 are depicted. **(h-j)** Same as (e-g) but for modelling fly movement when heading and goal  
 733 coordinates are constitutively misaligned at a fixed distance ( $dy/dt = d\theta/dt$ ). Black arrowheads in  
 734 (g, h) represent starting position for walking trajectories. Initial offsets between orientation and  
 735 goal signals in (e-j) are displayed as  $\gamma$  values ranging from  $-\pi$  to  $\pi$ .

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<b>Cell Type</b>	<b>Acronym</b>	<b>Driver line</b>
protocerebral bridge – fan-shaped body – noduli(anterior)	PFN <sub>a</sub>	SS02255-Gal4
protocerebral bridge – fan-shaped body – noduli(dorsal)	PFN <sub>d</sub>	SS00078-Gal4
protocerebral bridge – fan-shaped body – noduli(anterior AND dorsal populations)	PFN <sub>a+d</sub>	R16D01-Gal4
ellipsoid body – protocerebral bridge – gall	EPG	SS00090-Gal4
protocerebral bridge – fan-shaped body – lateral accessory lobe (3)	PFL3	NA

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738 **Extended Data Table 1. Acronyms used for central complex columnar neurons**

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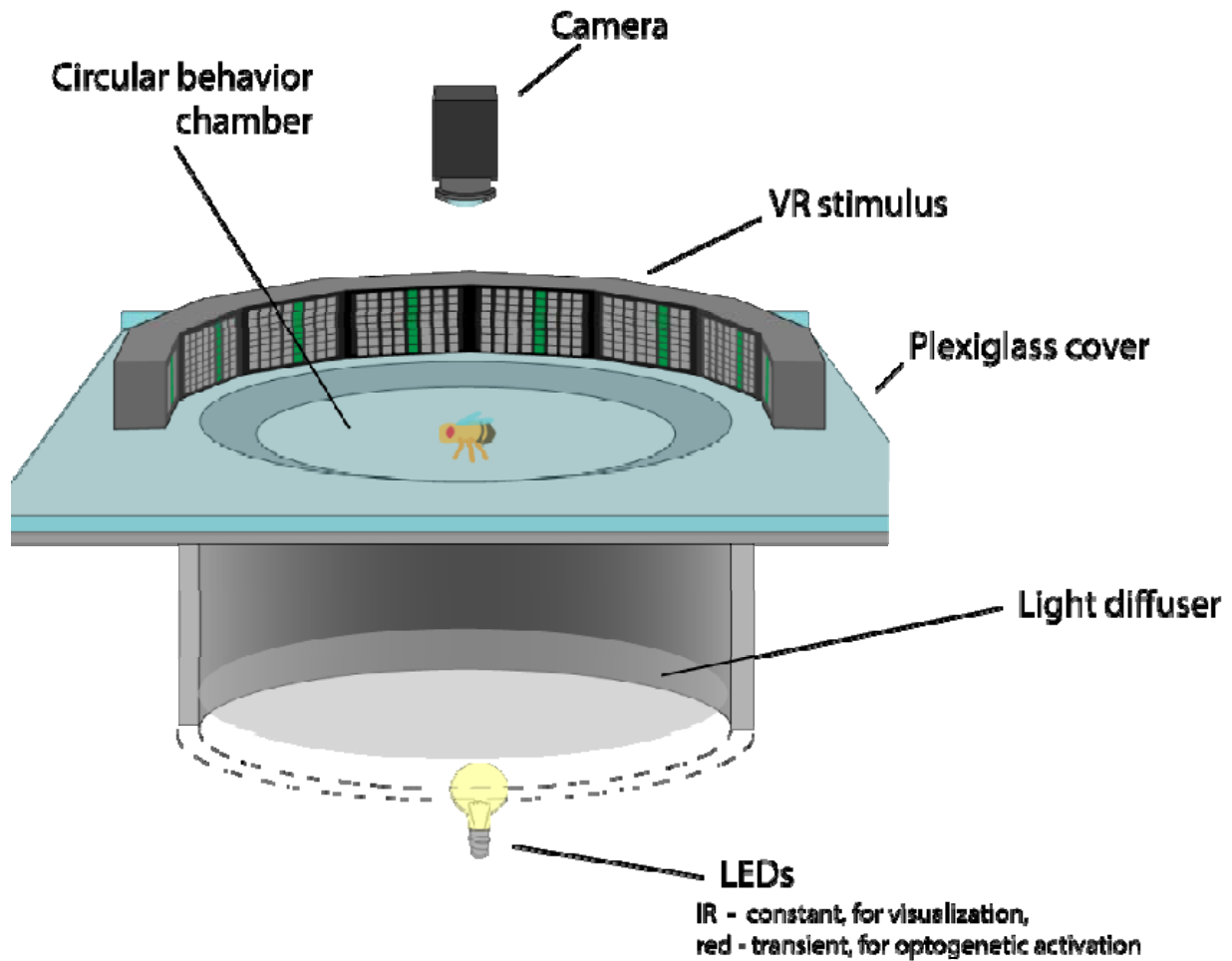


<b>Figure</b>	<b>Shorthand</b>	<b>Genotype</b>
Fig. 1f-m	PFNd >Shi <sup>TS</sup>	w <sup>1118</sup> ; R16D01-p65ADZp/+ ; R15E01-ZpGdbd/UAS-Shi <sup>TS</sup>
Fig. 1l, m	PFNa >Shi <sup>TS</sup>	w <sup>1118</sup> ; R16D01-p65ADZp/+ ; VT016114-ZpGdbd/UAS-Shi <sup>TS</sup>
Fig. 1l, m, Extended Data Fig. 2	EPG >Shi <sup>TS</sup>	w <sup>1118</sup> ; R19G12-p65ADZp/+ ; R15C03-ZpGdbd/UAS-Shi <sup>TS</sup>
Fig. 1l, m, Extended Data Fig. 2	No driver > Shi <sup>TS</sup>	w <sup>1118</sup> ; +/+ ; UAS- Shi <sup>TS</sup> /+
Fig. 2e-h, Extended Data Fig. 4	No driver > CsChrimson	w <sup>1118</sup> ; UAS-CsChrimson ; +/+
Fig. 2e-h, Extended Data Fig. 4	PFNa > CsChrimson	w <sup>1118</sup> ; R16D01-p65ADZp/ UAS-CsChrimson ; R15E01-ZpGdbd/+
Fig. 2e-h, Extended Data Fig. 4	PFNd > CsChrimson	w <sup>1118</sup> ; R16D01-p65ADZp/ UAS-CsChrimson ; VT016114-ZpGdbd/+
Fig. 2e-h, Extended Data Fig. 4, 5	PFNa+d > CsChrimson	w <sup>1118</sup> ; UAS-CsChrimson ; R16D01-Gal4/+
Fig. 3	R16D01- Gal4 > SPARC	nSyb-IVS-PhiC31 ; UAS-SPARC2-S-CsChrimson::TdTomato/+; R16D01-Gal4
Fig. 3i-l, Extended Data Fig. 6	SS00081 > CsChrimson	w <sup>1118</sup> ; R16D01-p65ADZp/ UAS-CsChrimson ; R21H11-ZpGdbd/+
Extended Data Fig. 2	WT	w <sup>1118</sup> ;;

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742 **Extended Data Table 2. Genotypes used for each figure**

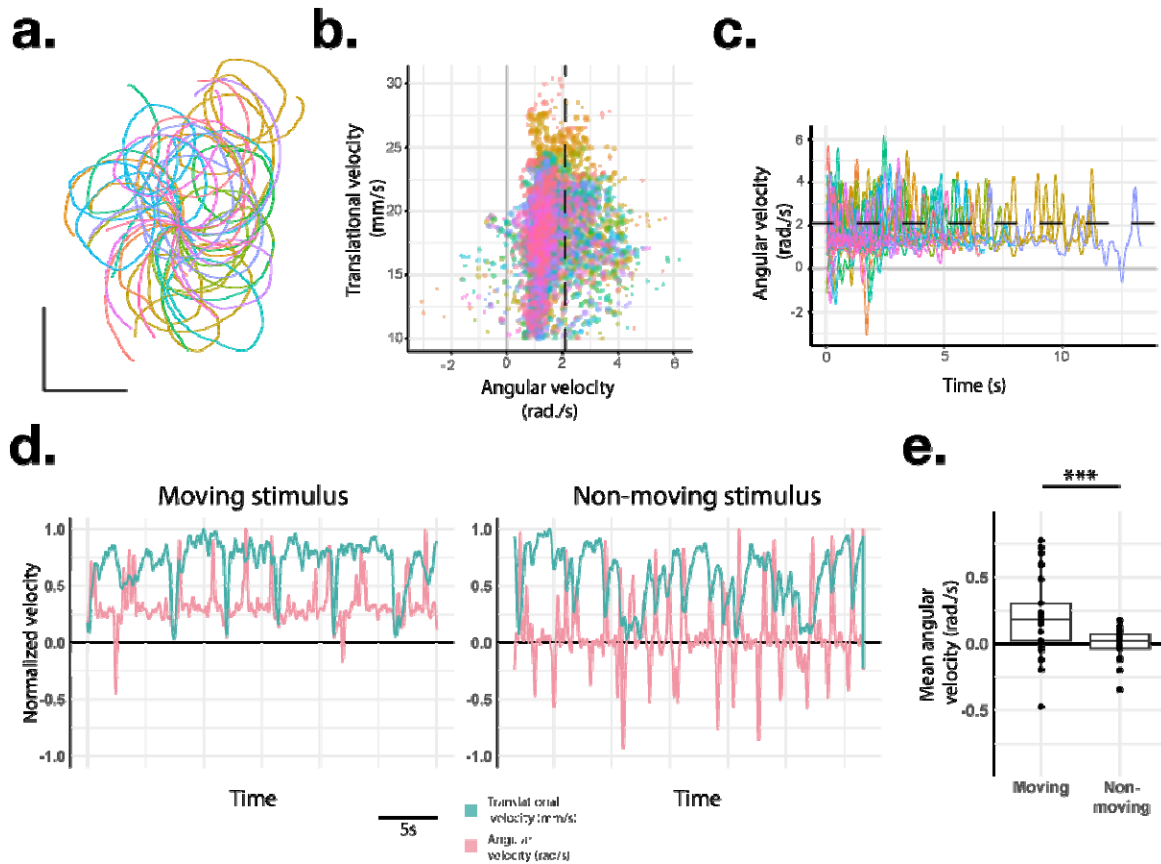


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744 **Extended Data Figure 1. Apparatus used for quantifying locomotor behaviors**

745 Schematic of the custom-made behavior arena used for the locomotor tracking experiments.  
746 Cross-section of VR stimulus and lighting chamber is shown. Flies are placed in the arena  
747 beneath a plexiglass ceiling while a camera records their behavior.

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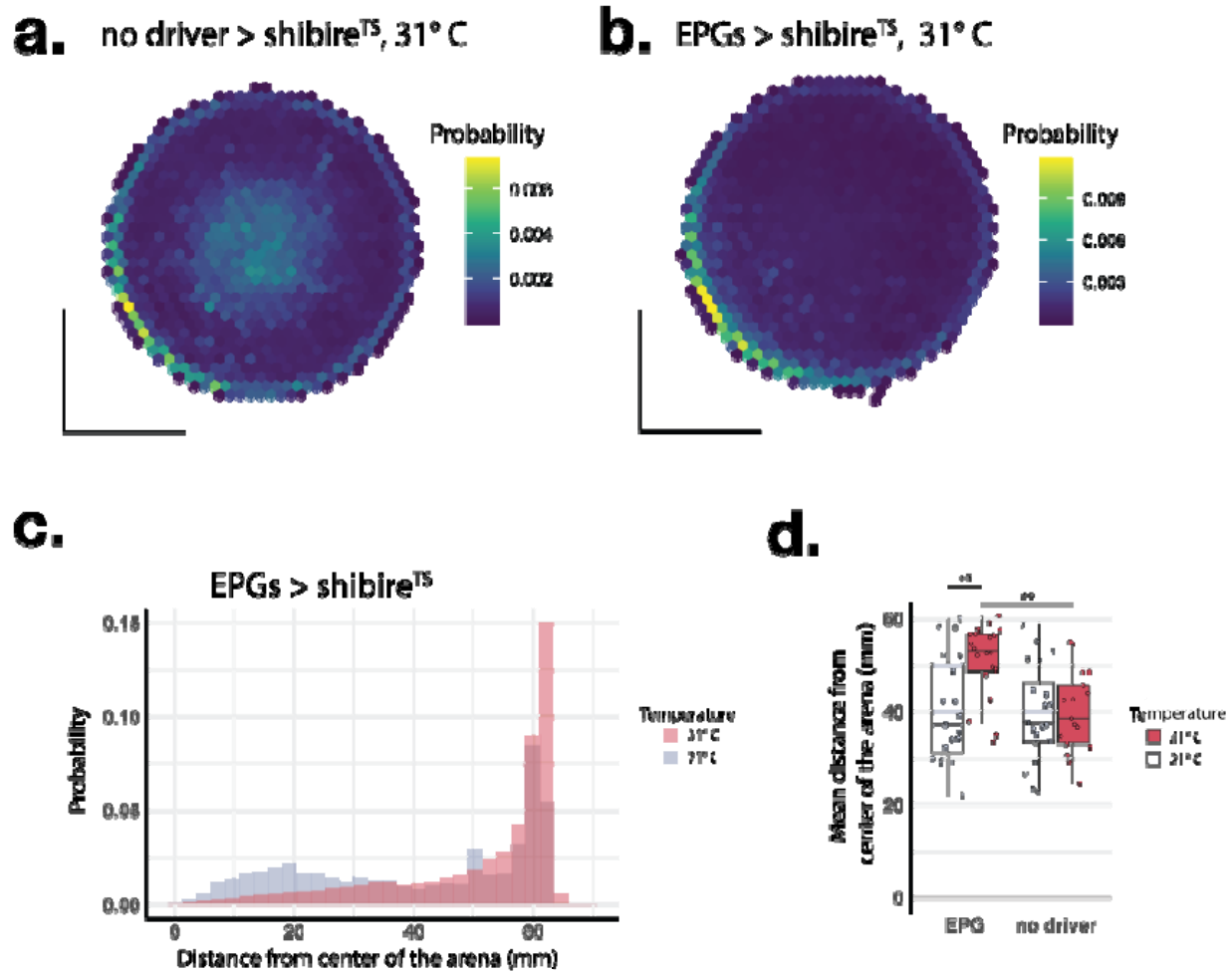
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## 751 Extended Data Figure 2. Quantifying reorientation bouts in WT flies

752 **(a-c)** Representative data from angular motion behavioral paradigm. One trial from a WT fly is  
753 depicted. Each color depicts a single walking bout. (a) walking trajectories whose x and y  
754 coordinates were translated to a common starting position. (b) scatter plot of the translational  
755 and angular velocity values for each timepoint. (c) line plot of angular velocity values over time.  
756 Dashed line in (b, c) depicts rotational velocity of VR stimulus. **(d)** Line plots depicting  
757 translational and angular velocity values for a single fly during 30s of walking in the VR stimulus  
758 paradigm. Translational and angular velocity values are coincident when the VR stimulus bar is  
759 moving (left panel) but not when the bar is still (right panel). Velocity values are normalized such  
760 that the maxima equal 1 to enable comparisons between translational and angular velocity  
761 values. **(e)** boxplot of angular velocity values Average of entire 5 min trial is shown. Positive  
762 angular velocity values indicate towards the direction of the stimulus. Scale bar in (a) equals  
763 10mm. Wilcoxon ranked sum test was used for statistical testing (\*\*\*) = p < 0.001)

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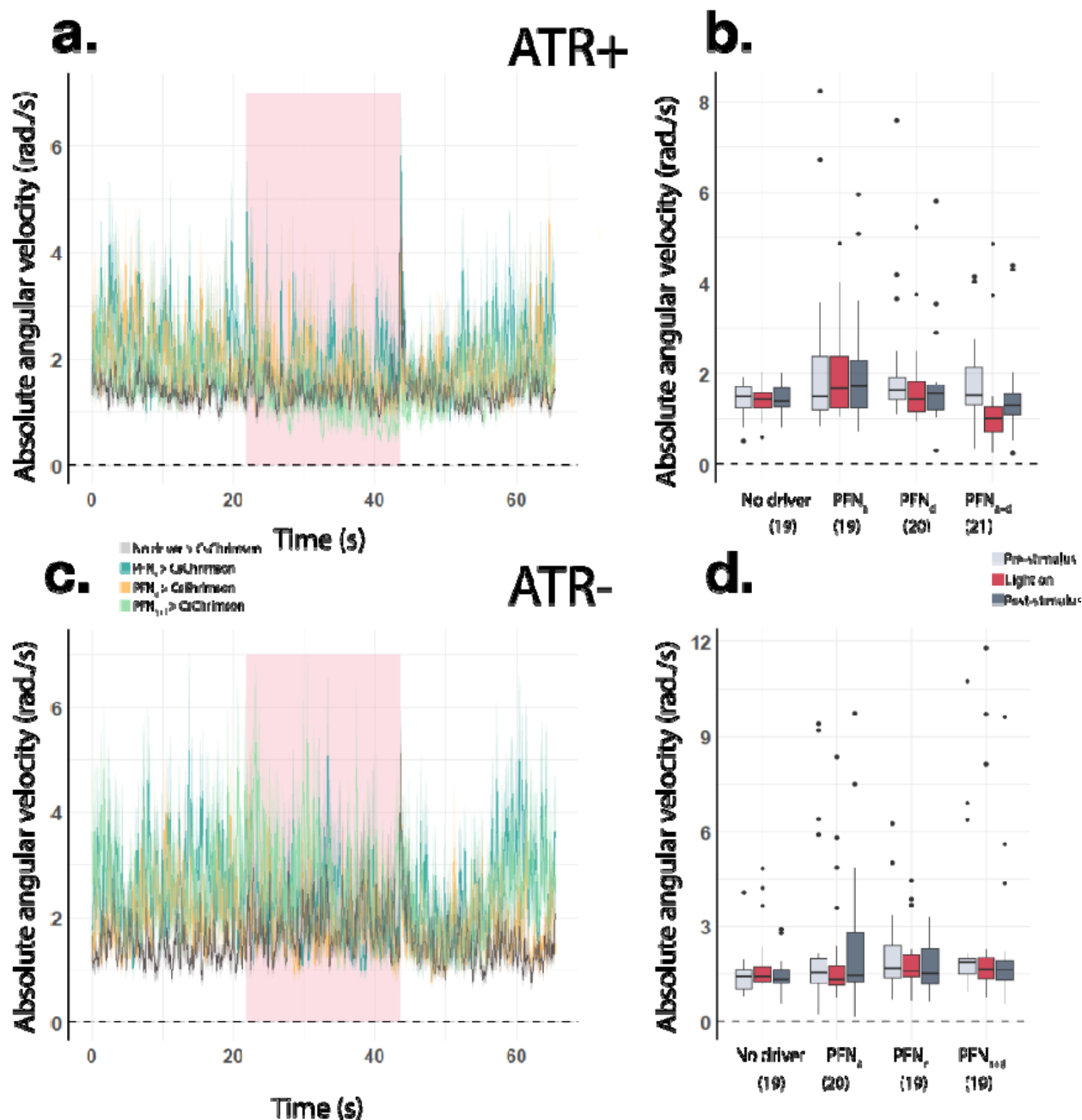


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### 766 Extended Data Figure 3. Reorientation bouts require neurotransmission from EPGs

767 **(a, b)** Two-dimensional density plots depicting the probability of flies' x/y coordinates across  
768 trials during our optic flow assay. (a) depicts the 31° C trials with control flies carrying shibire<sup>TS</sup>  
769 but no genetic driver. (b) depicts the 31° C trials where flies expressed shibire<sup>TS</sup> in EPG  
770 neurons. When EPG neurons were silenced by shibire<sup>TS</sup>, flies were noticeably less present in  
771 the center of the arena, the region where we observe reorientation bouts. **(c)** Probability  
772 histogram of the distance from the center of the arena for each time point across trials for the  
773 EPG > shibire<sup>TS</sup> group. 21° C (grey) and 31° C (red) trials are plotted. Note that values are  
774 bimodal in the 21° C condition, with one peak centered close to the center of the arena and  
775 another centered at the edge while values in the 31° C condition are unimodal with one peak at  
776 the edge of the arena. **(d)** Boxplot of values of mean distances from the center of the behavior  
777 arena. Silencing EPGs led to flies walking predominantly at the edges of the arena, while we  
778 observe no such trend in the other groups.

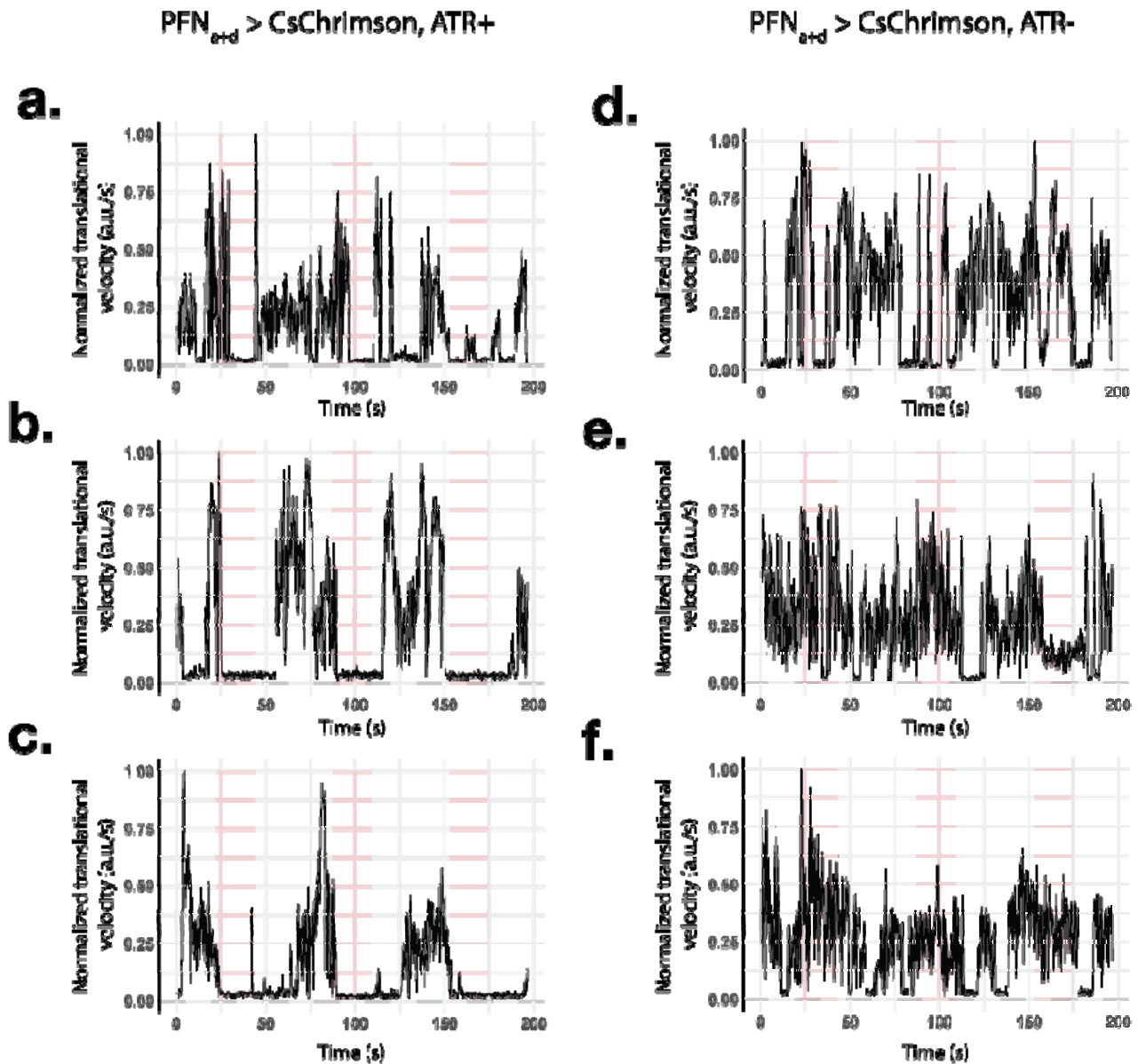
779



780 **Extended Data Figure 4. Angular velocity values do not change during bulk activation of**  
 781 **PFNs.**

782 **(a-d)** Quantification of angular velocity values from optogenetic experiments depicted in Fig. 2e-  
 783 h. (a) Line plot of mean absolute angular velocity values ( $\pm$ s.e.) across stimulus bouts for the  
 784 various genotypes in the ATR+ condition. Red box denotes time interval of delivery of the  
 785 optogenetic stimulus. See (b) for the numbers of trials (N) that were averaged in each group. (b)  
 786 Boxplot of mean absolute angular velocity values during each trial in the ATR+ condition. Values  
 787 are shown for the optogenetic stimulus period as well as for the pre- and post-stimulus periods.  
 788 (c, d) Same as (a, b) but for the ATR- groups.

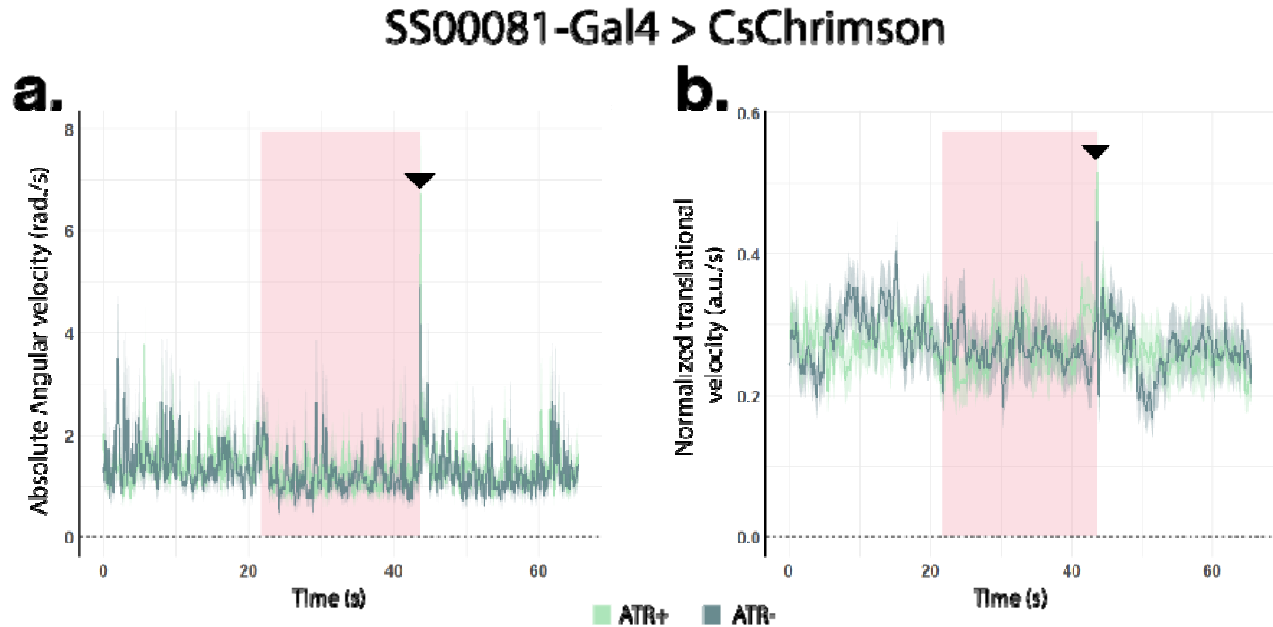




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790 **Extended Data Figure 5. Representative trials for freezing behavior during PFN<sub>a+d</sub>**  
791 **activation.**

792 **(a-c)** Normalized translational velocity values plotted over time for PFN<sub>a+d</sub> activation trials for the  
793 ATR+ condition. Each plot depicts normalized translational velocity values for an individual fly  
794 over the course of an experiment. Red boxes indicate the time interval in which the optogenetic  
795 stimulus was delivered. **(d-f)** Same as (a-c) but in the ATR- condition. Translational velocity  
796 values drop to zero during optogenetic stimulus delivery in the ATR+ condition but not the ATR-  
797 condition.



798 **Extended Data Figure 6. Sparse symmetric activation of PFNs elicits no change in**  
799 **locomotion**

800 **(a, b)** Line plots of averaged absolute angular velocity (a) and normalized translational velocity  
801 (b) values ( $\pm$ s.e.) while optogenetically activating the sparse but symmetric population of PFNs  
802 that is targeted by SS00081-Gal4. Trials where flies were raised on a diet supplemented with  
803 ATR (ATR+) (N=10) or without (ATR-) (N=11) are shown. Red box indicates time interval of  
804 delivery of optogenetic stimulus. Spikes in angular and translational velocity are observed upon  
805 offset of the optogenetic stimulus in both ATR+ and ATR- conditions (black arrowheads).

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