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# A Coupled EXAFS–Molecular Dynamics Study on PuO<sub>2</sub><sup>+</sup> and NpO<sub>2</sub><sup>+</sup> Hydration: The Importance of Electron Correlation in Force-Field Building

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**ABSTRACT:** The physicochemical properties of the monovalent actinyl cations,  $PuO_2^+$ and  $NpO_2^+$ , in water have been studied by means of classical molecular dynamic simulations. A specific set of cation-water intermolecular potentials based on ab initio potential energy surfaces has been built on the basis of the hydrated ion concept. The TIP4P water model was adopted. Given the paramagnetic character of these actinyls, the cation-water interaction energies were computed from highly correlated wave functions using the NEVPT2 method. It is shown that the multideterminantal character of the wave function has a relevant effect on the main distances of the hydrated molecular cations. Several structural, dynamical, and energetic properties of the aqueous solutions have been obtained and analyzed. Structural RDF analysis gives  $An-O_{yl}$  distances of 1.82 and 1.84 Å and An-O(water) distances of 2.51 and 2.53 Å for  $PuO_2^+$  and  $NpO_2^+$  in water,



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respectively. Experimental EXAFS spectra from dilute aqueous solutions of  $PuO_2^+$  and  $NpO_2^+$  are revisited and analyzed, assuming tetra- and pentahydration of the actinyl cations. Simulated EXAFS spectra have been computed from the snapshots of the MD simulations. Good agreement with the experimental information available is found. The global analysis leads us to conclude that both  $PuO_2^+$  and  $NpO_2^+$  cations in water are stable pentahydrated aqua ions.

# INTRODUCTION

The actinyl forms of actinoids are their trans-dioxo molecular cations,  $AnO_2^{+/2+}$ , present in the high oxidation states, V and VI.<sup>1</sup> They exhibit high solubilities in water what leads to a rich solution chemistry in a wide set of scenarios where their chemical behavior may be quite different: ligand complexation, hydrolysis processes coupled to acidity or basicity of the medium, adsorption on surfaces, polymerization, and others.<sup>2–7</sup> It is of primary interest the proper structural characterization of the hydration of such actinyls in order to further understand their physicochemical properties in the different environments that they may face. It has been shown that these actinyls in water are surrounded by water molecules defining stable aqua ions,  $[AnO_2(H_2O)_n]^{+/2+}$ , being generally accepted to have a hydration number of five, <sup>3,8-13</sup> although four has also been proposed in some cases.<sup>14-16</sup> The actinyl aqua ion chemistry is intimately joined to nuclear technology due to its role in spent nuclear fuel, reprocessing, temporary and permanent storage, and environmental speciation.<sup>6,1</sup>

The structural characterization of these cations has been conducted by both experimental and theoretical techniques. Among the experimental ones, the technique giving a more direct information is the X-ray absorption spectroscopy (XAS), in particular the extended X-ray absorption fine structure (EXAFS).<sup>4,17–20</sup> The great advantage of this technique is its ability to supply short-range structural information around an

specific atom, the absorbing atom, with a structural precision of 0.01 Å for the first coordination shell distance and one unit in the coordination number.<sup>10,12,19,21,22</sup> Given that no long-range order is needed and submillimolar concentrations of the absorbing atom can be detected, EXAFS is a really powerful and very suitable tool for the study of solutions containing actinoid cations.<sup>4,17,20,23</sup>

Among the theoretical techniques, quantum-mechanical methods and computer simulations have also provided valuable information. In the first case, the studies usually combine the molecular cation with a small number of water molecules forming the hydrated ion and adding solvent boundary conditions by means of a continuum solvation model.<sup>24–29</sup> A general solvent molecular description can be reached by using statistical techniques, either assuming ab initio molecular dynamics (AIMD) at reliable QM levels or classical MD simulations employing in this case reliable force fields.

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				$R_{An-O_1}$				
method	CN	$R_{\rm An-Oyl}$ (Å)	$\sigma_{\mathrm{An-Oyl}}{}^2 (\mathrm{\AA}^2)$	(Å)	$\sigma^2$ (An–O <sub>I</sub> )	ref		
	$[PuO_2(H_2O)_n]^+$							
QM(NEVPT2)	5	1.806		2.506		this work		
QM(NEVPT2)	4	1.800		2.448		this work		
POT5(NEVPT2)	5	1.805		2.505		this work		
POT5(NEVPT2)	4	1.799		2.437		this work		
POT4(NEVPT2)	4	1.795		2.450		this work		
MD_POT5 (300 K)	5	1.822	0.0007	2.507	0.008	this work		
MD_POT4 (300 K)	4	1.809	0.00035	2.454	0.0013	this work		
EXAFS	4	1.821	0.030	2.48	0.072	Panak et al. <sup>14</sup>		
EXAFS	3.3	1.81	0.0020	2.47	0.0044	Di Giandomenico et al. <sup>15</sup>		
EXAFS	5.3	1.81	0.002	2.47	0.009	Dalodière et al. <sup>20</sup>		
QM(B3LYP)	5	1.808		2.61		Hay et al. <sup>25</sup>		
QM(PBE)	5	1.86		2.53		Rizhkov et al. <sup>35</sup>		
QM (B3LYP)	5	1.76		2.53		Pomogaev et al. <sup>58</sup>		
MD_POT5 (300 K)	5	1.77		2.56		Pomogaev et al. <sup>58</sup>		
MD/PBE (300 K)	5	1.82		2.55		Odoh et al. <sup>16</sup>		
MD/PBE (300 K)	4	1.85		2.47		Odoh et al. <sup>16</sup>		
			[NpO <sub>2</sub> (2	$(H_2O)_n]^+$				
QM(NEVPT2)	5	1.831		2.522		this work		
QM(NEVPT2)	4	1.825		2.466		this work		
POT5(NEVPT2)	5	1.825 (1.83)		2.529 (2.52)		this work (Pérez-Conesa et al.) <sup>38</sup>		
MD_POT5 (300 K)	5	1.842 (1.84)	0.0007 (0.0007)	2.528 (2.54)	0.008 (0.011)	this work (Pérez-Conesa et al.) <sup>38</sup>		
EXAFS	5	1.822	0.002	2.488	0.006	Reich et al. <sup>9</sup>		
EXAFS	5.2	1.84	0.002	2.49	0.007	Ikeda et al. <sup>12</sup>		
EXAFS	4.4	1.83	0.0056	2.51	0.0040	Di Giandomenico et al. <sup>15</sup>		
HEXS	5	1.82		2.46		Skanthakumar et al. <sup>13</sup>		
QM(B3LYP)	5	1.81		2.61		Hay et al. <sup>25</sup>		
QM(MP2)	5	1.81		2.52		Tsushima et al. <sup>24</sup>		
QM (B3LYP)	5	1.79		2.55		Pomogaev et al. <sup>58</sup>		
QM (B3LYP)	5	1.79		2.59		Danilo et al. <sup>28</sup>		
QM (B3LYP)	5	1.78		2.59		Pérez-Conesa et al. <sup>38</sup>		
MD (300 K)	5	1.80		2.54		Pomogaev et al. <sup>58</sup>		
'All experimental EXAFS are obtained at highly acidic pH, with non-coordinating counterions.								

#### Table 1. Gas-Phase QM and Force-Field Optimizations, MD First-Shell Distances at 300 K, and Debye–Waller factors $(\sigma^2)^{\alpha}$

The combination of XAS spectroscopy and MD simulations has been revealed as an useful strategy<sup>30–33</sup> to refine the structural properties of solutions when the standard fitting of the experimental spectra are clouded by different factors as complexity of the system, low concentrations, spectroscopical phenomena as multiexcitations, low signal/noise ratio, and others.<sup>34</sup> The good reproduction of an experimental spectrum by means of the use of the structural information derived from a statistical simulation has a double consequence.<sup>23</sup> On the one hand, it allows access to a direct EXAFS structure assignment provided by the atomistic picture of the statistical trajectory. On the other hand, the agreement shows the ability of the interaction potentials employed in the statistical simulation when using classical force fields or the quantum-mechanical level in AIMD simulations to describe properly the system.

Within the actinyl series,  $PuO_2^+$  has been scarcely studied due to its trend to disproportionate to lower, e.g.,  $Pu^{4+}$ , and higher, e.g.,  $PuO_2^{2+}$ , oxidation states. EXAFS studies have dealt with  $PuO_2^+$  acidic aqueous solutions.<sup>14,15,20</sup> The main distances,  $Pu-O_{yl}$  and  $Pu-O_{y}$  and the hydration number are collected in Table 1. The EXAFS fitting supplies a reduced range for the main distances,  $Pu-O_{yl}$  and  $Pu-O_{y}$  but the coordination numbers proposed vary from 3.3 to 5.3. Bearing in mind the typical uncertainty in the coordination number determination from EXAFS fitting due to multiparameter correlation, additional information must be included to elucidate this issue. Some QM calculations had concluded that coordination number is 5 with distances quite different from those obtained by EXAFS, as collected in Table 1.<sup>35</sup> Dalodière et al.,<sup>20</sup> in a recent study on the PuO<sub>2</sub><sup>+</sup> aqua ion, showed an interesting synthesis method of this species based on sonochemistry which allowed them to reach millimolar PuO<sub>2</sub><sup>+</sup> solutions free of other Pu oxidation states. They recorded the EXAFS spectrum of this species and compared it with simulated spectra computed from the QM [PuO<sub>2</sub>(H<sub>2</sub>O)<sub>5</sub>]<sup>+</sup>(H<sub>2</sub>O)<sub>10</sub> and [PuO<sub>2</sub>(H<sub>2</sub>O)<sub>4</sub>]<sup>+</sup>(H<sub>2</sub>O)<sub>8</sub> clusters, obtained by B3LYP optimizations and Debye–Waller factors computed from the QM frequencies of these clusters. They concluded that the best theoretical–experimental agreement corresponds to the PuO<sub>2</sub><sup>+</sup> tetrahydrate.

corresponds to the PuO<sub>2</sub><sup>+</sup> tetrahydrate. In previous works,<sup>36–38</sup> we have conducted classical MD simulations of actinyls,  $AnO_2^{+/2+}$ , in water using interaction potentials based on first-principles QM calculations. EXAFS and XANES spectra have been simulated using the structural information and the theoretical scattering phases and amplitude functions computed by the ab initio FEFF code (v.9.6).<sup>39</sup> Whereas the theoretical–experimental agreement was quite satisfactory for UO<sub>2</sub><sup>2+</sup>, NPO<sub>2</sub><sup>2+</sup>, and PuO<sub>2</sub><sup>2+</sup> using force fields derived from B3LYP potential energy surfaces, the NpO<sub>2</sub><sup>+</sup> case was not satisfactory.<sup>38</sup> This fact compelled us to develop for NpO<sub>2</sub><sup>+</sup> a new force field based on QM wave functions with explicit inclusion of the dynamic and non-dynamic electron correlation, as NEVPT2 method does.<sup>40,41</sup> The simulated EXAFS spectrum gave a fair comparison with the experimental spectra. As far we know, there is not a simulated spectra based on statistical computations for PuO<sub>2</sub><sup>+</sup>, with the coordination number and geometrical parameter remaining controversial.

The aim of this work is to confirm the importance of the use of multideterminantal wave functions as reference QM computations to provide accurate enough force fields when dealing with a higher multiplet open-shell system, as it is that of the  $PuO_2^+$  cation. Likewise, we envisage to develop and test a simpler formulation of the actinyl potential model. For these reasons, we have built a new  $NpO_2^+-H_2O$  interaction potential to double check the validity of this new formulation. A revisited analysis of former experimental EXAFS spectra of  $PuO_2^+$  and  $NpO_2^+$  aqueous solutions<sup>15</sup> has also been carried out on the light of the theoretical results.

## METHODS

Quantum Chemical Calculations. A main motivation of this study is to get insight into the impact that static and dynamic electron correlation may have on the structure and the dynamical and structural disorder of the close environment of the actinyls. Multireference  $\text{NEVPT2}^{40-42}$  calculations, which incorporate both types of electron correlation, were conducted using the ORCA45 program. The chosen active space was the set of atomic-like f-orbitals in addition to the molecular orbitals resulting from combining actinide f orbitals and  $\boldsymbol{O}_{yl}\ p$  orbitals. The active space involves 10 molecular orbitals,  $2\pi_{u}$ ,  $3\sigma_{u}$ ,  $1\phi_{u}$ ,  $1\delta_{u}$ ,  $4\sigma_{u}^{*}$ , and  $3\pi_{u}^{*}$ , as shown by Denning in Figure 1 of his study.<sup>44</sup> The main atomic orbital composition of these molecular orbitals is given in Table S1. A similar selection was adopted by Gendron et al. $^{45}$  for neptunyl(VI) complexes. This resulted in CASSCF(8,10) configurations for  $NpO_2^+$  and CASSCF(9,10) configurations for  $PuO_2^+$ . A more complete active space would include non bonding, bonding and antibonding molecular orbitals resulting of the inclusion of 6d actinide orbitals and their combination with  $O_{yl}$  2s and 2p orbitals. However, this would lead up to a 16-orbital active space what increased dramatically the number of configurations, e.g., for the  $PuO_2^+$  case the number of configurations for the (9,10) one is  $\sim 7 \times 10^3$ , whereas for the (15,16) is  $\sim 4.9 \times 10^6$ . Bearing in mind that we have to deal with the hydrated actinyl aqua ions, both optimizing their geometries and producing a significant numbers of single points to build the interaction potentials, we have adopted the 10-orbital active space also used in precedent studies of complexes of similar sizes.<sup>28,45</sup> Since the triplet and quartet ground states for NpO2+ and PuO2+, respectively, are degenerate, calculations were carried out using a state average over the degenerate states excluding excited states. The perturbational step of the calculation was done using quasi-degenerate perturbation theory. The basis sets used were ma-def2-TZVP for O, def2-SVP for  $H^{46,47}$  and SD(60,MWB)//def-TZVP for actinoids.<sup>48</sup> The calculations were accelerated using the RI and RIJK pseudospectral methods with "autoaux" auxiliary basis sets. Due to the lack of analytical gradients, geometry optimizations were conducted numerically by evenly changing the M-O<sub>vl</sub> and M-O<sub>I</sub> distances in a 2D grid with a step of ~0.005 Å. The structure was assumed to be optimized when the energy of the predicted optimized structure within the grid differs from the QM value obtained for such optimized geometry in less than  $10^{-5} E_{\rm h}$ , otherwise a reduced 2D grid, with a smaller step, around this point is computed to estimate the minimum.

Interaction Potentials for  $AnO_2^+$  in Water. To describe the interactions of  $PuO_2^+$  and  $NpO_2^+$  in aqueous solution, we have

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developed a procedure based on our statistical implementation of the hydrated ion concept,<sup>49,50</sup> particularly adapted for the case of monovalent molecular cations.<sup>36,51</sup> Figure 1 displays a sketch of the interaction potentials involved in the system definition.



Figure 1. Interaction potentials defined in the system: IMC (intramolecular cation interaction), IW1 (molecular cation–water first-shell interactions, and HIW (hydrated ion–bulk water interactions). The water–water interactions are described by the TIP4P model.<sup>52</sup>

The basic idea is that the hydrated ion<sup>53</sup> is the representative species interacting with the bulk water,  $([AnO_2(H_2O)_n]^+-H_2O)$  by means of a hydrated ion–bulk water potential (HIW). For this aim, the QM interaction energy,  $E_{\rm int}^{\rm QM}$ , is described by two potentials, of which one is the TIP4P potential<sup>52</sup> that describes the interaction among the first-shell and bulk water molecules and the other collects the interactions between the bulk water molecules and the actinyl cation. The functional form is

$$E_{\text{int}}^{\text{QM}} = E_{\text{HIW}} = \sum_{i}^{\text{sites}} \sum_{j}^{\text{sites}} \left( \frac{C_{ij}^{ij}}{r_{ij}^{4}} + \frac{C_{6}^{ij}}{r_{6}^{6}} + \frac{C_{8}^{ij}}{r_{ij}^{8}} + \frac{C_{12}^{ij}}{r_{ij}^{12}} + \frac{q_{i}q_{j}}{r_{ij}} \right) + \sum_{i}^{\text{sites}} \sum_{j}^{\text{Bulk water}} E_{ij}^{\text{TIP4P}}$$

$$(1)$$

The interaction of the molecular cation with its first hydration shell (IW1) was parametrized by a series of  $r^{-n}$  terms with n = 4, 6, 8, and 12 plus the Coulombic term.

$$E_{\rm IW1} = \sum_{i}^{\rm AnO_2} \frac{C_4^{\rm iO}}{r_{iO}^4} + \frac{C_6^{\rm iO}}{r_{iO}^6} + \frac{C_8^{\rm iO}}{r_{iO}^8} + \frac{C_{12}^{\rm iO}}{r_{iO}^8} + \sum_{i}^{\rm AnO_2} \frac{V_{\rm Water}}{V_{iO}^{\rm iO}} + \frac{Q_i^2 q_j}{r_{ij}}$$
(2)

At this point it should be noted that the first-shell water molecules are ruled by an interaction potential with the actinyl cation (IW1) different from that of bulk water molecules (HIW). This supplies a refined definition of the interaction within the aqua ion and with the bulk water which allows classical optimized geometries of the aqua ion, as those shown in Table 1, very close to the QM ones, but requiring computational times of seconds instead of tens of hours. The shortcoming associated with this methodological advantage is the fact that no exchange of water molecules between the first-shell and the bulk must occur. Along the MD simulations no water molecule release from the aqua ions to the bulk was observed. Finally, to describe the intrinsic dynamics of the actinyl cation we have adopted for the intramolecular cation (IMC) potential a new functional form with respect to our previous development.<sup>36–38,51</sup> We have replaced an interatomic potential based on a power series, as in the  $E_{\rm HIW}$  or  $E_{\rm IW1}$  functional forms, by an anharmonic potential to describe the An–O<sub>vl</sub> bonds and a harmonic potential for the bending.

$$E_{\rm IMC} = \sum_{i}^{\rm O_{yl}} [k_{\rm An-Oyl,i}(r_i - r_0)^2 + k'_{\rm An-Oyl,i}(r_i - r_0)^3] + k''_{\rm Oyl-An-Oyl}(\theta - \theta_0)^2$$
(3)

Figure 2 displays some representative structures used to build the intermolecular potentials. A total of 64 structures were used for the



Figure 2. Representative type of structures employed to fit the potentials defined in the system: IMC (intramolecular cation interaction), IW1 (molecular cation-water first-shell interactions), and HIW (hydrated ion-bulk water interactions).

HIW potential, while 220 structures were used for the IW1 and 87 were used for the IMC. For this development, it has been assumed that the aqua ions are pentahydrates. Figures S1 and S2 show the fitting of the set of  $PuO_2^+$  and  $NpO_2^+$  potentials. Potential coefficients are given in Tables S2–S5, which include their corresponding standard deviations.

To check the fitted potentials, we have examined the interaction energy of a bulk water molecule approaching the hydrated actinyl from different regions. Figure S3 shows the good correlation between the QM interaction energy and the value predicted by the force field. It must be stressed that these structures were taken from 50 snapshots of an MD simulation where the closest water molecule to the actinyl aqua ion in each angular region was taken. Given that for the  $PuO_2^+$  aqueous solution, several authors<sup>14,15,20</sup>

Given that for the  $PuO_2^+$  aqueous solution, several authors<sup>14,15,20</sup> have pointed out that its aqua ion is a tetrahydrate instead of a pentahydrate, a specific force field assuming that the hydrated ion is  $[PuO_2(H_2O)_4]^+$  was also developed. A fitting procedure similar to that explained for the pentahydrated plutonyl was applied to define

the new IMC potential, and the new  $PuO_2^+$  polarization on the tetrahydrate was reflected in the Pu and  $O_{yl}$  effective charges collected in Table S2. Figure S4 shows the goodness of the fit by comparing the QM interaction energy with the values derived from the IW1 and HIW potentials of the force field.

**Molecular Dynamics Simulations.** MD simulations were run in a similar way to our previous studies on actinyls.<sup>36,38,51</sup> A single hydrated actinyl ion,  $[AnO_2(H_2O)_n]^+$  (An = Np and Pu), and 1490 TIP4P water molecules were placed in a cubic box at the experimental water density. The simulations were run at 300 K in the *NVT* ensemble using the Noosé–Hoover thermostat with  $\tau = 0.5$  ps. Nonbonded interactions were cut at 12 Å, and the Ewald sum was used for the computation of electrostatic interactions. The equations of motion were integrated using a 0.5 fs time step for a total simulation time of 5 ns. All simulations were run using a modified version of DL\_POLY Classic<sup>54</sup> which includes the functional forms of the force field employed. The convergence of MD trajectories has been checked by the analysis of structural, energetic and dynamic properties of the actinyl cations as shown in refs 36, 38, and 51.

The translational self-diffusion coefficient of actinyls,  $D_{\text{AnO2}}$ , has been obtained using mean-square displacements (MSD).<sup>55</sup> This function was computed using multiple time origins up to half of the simulation period for each series. This procedure is particularly appropriate when describing the mobility of only one ion in the system. The 5 ns trajectory was employed to get an average value of  $D_{\text{AnO2}}$ , analyzing five series of 1 ns. From it, the average value and an estimation of the error by its standard deviation were conducted. To compute ion hydration enthalpies,  $\Delta H_{\text{hydr}}$ , NPT MD simulations of 1 ns production at 300 K were also conducted. These simulations used the Nosé–Hoover thermostat and barostat with  $\tau = 0.5$  ps in both cases. The standard deviation of the average configurational enthalpies was computed by the blocking average method proposed by Flyvbjerg and Petersen<sup>56</sup> for the error estimation on correlated data.

**Simulated XAS Spectra.** A total of 500 evenly spaced configurations of  $[AnO_2(H_2O)_n]^+$  were extracted from 1 ns MD trajectories, i.e., the time interval between two consecutive snapshots is 2 ps, which guarantees noncorrelated statistical information. It has been checked that the use of longer MD trajectories leads to the same simulated spectrum. The configurations included water molecules up to the first solvation shell since we have found the second shell to have no influence on the spectra. Average  $L_{III}$ -edge spectra were obtained from the individual spectra using the FEFF code (version 9.6)<sup>39</sup> including multiple scattering up to four-legged paths. Details of the spectrum simulation method can be found elsewhere.<sup>23,31,38,51</sup> An example of the FEFF input files can be found in Figure S5.  $S_0^2$  and  $\Delta E_0$  values have been chosen in the simulated NpO<sub>2</sub><sup>+</sup> and PuO<sub>2</sub><sup>+</sup> spectrum in order to match the first resonance of the corresponding experimental spectrum.

**Experimental EXAFS Spectra.** Experimental EXAFS spectra of  $NpO_2^+$  and  $PuO_2^+$  aqueous solutions have been recorded as described in ref 15. Revisited analysis of the previous published spectra was conducted with the ATHENA and ARTEMIS codes of Demeter 0.9.25 package<sup>57</sup> in fluorescence mode for Np and in transmission mode for Pu.

### RESULTS AND DISCUSSION

**Table 1** collects the An– $O_{yl}$  and An– $O_I$  distances for the two hydrated actinyl cations,  $[AnO_2(H_2O)_n]^+$  (n = 4 and 5), obtained at the QM level by the NEVPT2 method. Likewise, we have included the optimized geometry obtained by using the classical force fields developed (see "POTn (NEVPT2)" rows in the table). It must be underlined that the structural agreement between the QM and force field results is within the hundredth of angstrom. When average distances in solution (see "MD\_POTn (300 K)" rows in the table) are considered, it is seen that the An– $O_{yl}$  distance increases slightly ~0.017 Å due to solvent effects. For PuO<sub>2</sub><sup>+</sup>, the value of POT5-(NEVPT2) is 1.805 Å, and that for MD POT5(300 K) is

1.822 Å. For NpO2<sup>+</sup>, the corresponding values are 1.825 and 1.842 Å. When analyzing the solvent effects for the  $An-O_{I}$ distance the change is very small, on the order of 0.001 Å. Thus, Table 1 shows for the  $PuO_2^+$  case that POT5(NEVPT2) gives 2.505 Å, and MD\_POT5 (300 K) gives 2.507 Å. For the  $NpO_2^+$  case, the corresponding values are 2.529 and 2.528 Å. As expected, for the hydrate in gas phase, the Np $-O_{vl}$  distance is larger than that of the  $Pu-O_{yl}$  and the same trend is observed for the  $An-O_I$  bond. In water, the hydration effects do not change the gas-phase distance order. For the sake of comparison the scarce experimental data are also collected in Table 1. Our theoretical simulations agree fairly well with available experiments. In the plutonyl case, the experimental EXAFS data presented in this work are also in the narrow range of the previous data. As a matter of fact, no optimization geometry at the highly correlated NEVPT2 level of calculation had been previously reported for plutonyl, and as already observed for the neptunyl case in our previous work on actinyls,<sup>38</sup> the most sensitive parameter to the electron correlation is the oxo bond. This effect involves a lengthening of the Pu–O<sub>yl</sub> bond by 0.05 Å (1.81 Å this work and 1.76 Å with B3LYP),<sup>58</sup> and a similar change is observed in this work for neptunyl (1.83 Å) and B3LYP (1.78-1.81 Å).<sup>25,38,58</sup> This lengthening causes an An-O<sub>I</sub> distance shortening of some hundreths of an angstrom. For the PuO2<sup>+</sup> case, the value obtained is 2.51 Å (QM(NEVPT2) for CN = 5 row in Table 1) in this work, whereas the B3LYP values are 2.53 and 2.61 Å.<sup>58,25</sup> For NpO<sub>2</sub><sup>+</sup>, this work finds 2.52 Å (QM(NEVPT2) for CN = 5 row in Table 1), and previous B3LYP values are in the range of 2.55–2.61 Å.<sup>25,38,58</sup> In the case of NpO<sub>2</sub><sup>+</sup>, we can compare the performance of the new formulation of the IMC potential, based on harmonic and anharmonic functions, to describe the flexibility of the actinyl entity, with respect to the previous forms, based on a set of  $r^{-n}$  powers. The optimized geometry for  $[NpO_2(H_2O)_5]^+$  using the new potential, POT5(NEVPT2), predicts distance changes smaller than 0.01 Å with respect to the previous values (see values in parentheses in the POT5(NEVPOT2) row).

Due to the sensitivity of the main geometrical parameters to the different QM methods, we have explored for the two actinyl aqua ions the  $An-O_y$  and  $An-O_I$  distance change when going from HF to NEVPT2(*n*,10) computations. Table 2

Table 2. Optimized Distances (Å) of  $[NpO_2(H_2O)_5]^+$ ,  $[PuO_2(H_2O)_5]^+$ , and  $[UO_2(H_2O)_5]^{2+}$  Obtained via Different QM Methods

$[PuO_2(H_2O)_5]^+$		$[NpO_2(H_2O)_5]^+$		$[UO_{2}(H_{2}-O)_{5}]^{2+}$	
Pu-O <sub>yl</sub>	Pu-O <sub>I</sub>	Np-O <sub>yl</sub>	Np-O <sub>I</sub>	U-O <sub>yl</sub>	U-O <sub>1</sub>
1.77	2.53	1.78	2.54	1.74	2.40
1.74	2.63	1.76	2.64		
1.81	2.51	1.83	2.52		
1.78	2.42	1.80	2.48	1.78	2.45
1.78	2.55	1.79	2.55		
	[PuO <sub>2</sub> (H Pu-O <sub>yl</sub> 1.77 1.74 1.81 1.78 1.78	$\begin{array}{c c} \left[ PuO_2(H_2O)_5 \right]^+ \\ \hline Pu-O_{yl} & Pu-O_l \\ \hline 1.77 & 2.53 \\ 1.74 & 2.63 \\ 1.81 & 2.51 \\ 1.78 & 2.42 \\ 1.78 & 2.55 \end{array}$	$\begin{tabular}{ c c c c c c } \hline & [PuO_2(H_2O)_5]^+ & [NpO_2(H_2O)_5]^+ \\ \hline & Pu-O_{yl} & Pu-O_1 & Np-O_{yl} \\ \hline & 1.77 & 2.53 & 1.78 \\ \hline & 1.74 & 2.63 & 1.76 \\ \hline & 1.81 & 2.51 & 1.83 \\ \hline & 1.78 & 2.42 & 1.80 \\ \hline & 1.78 & 2.55 & 1.79 \\ \hline \end{tabular}$	$\begin{tabular}{ c c c c c } \hline & & & & & & & & & & & & & & & & & & $	$\begin{array}{c ccccccccccccccccccccccccccccccccccc$

collects these two optimized distances obtained from different methods. When passing from the HF to CASSCF(n,10) wave functions, the inclusion of static electron correlation provides multideterminantal wave functions that are eigenfunctions of the total electron spin operators, a quartet for the plutonyl(V) aqua ion and a triplet for the neptunyl(V) aqua ion. This effect shortens by 0.02–0.03 Å the An–O<sub>vl</sub> and lengthens the An–

 $O_I$  by ~0.1 Å. The inclusion of the dynamic correlation into these CASSCF wave functions by means of the NEVPT2 method leads to a significant increase of the oxo-bonds by ~0.07 Å what contributes to a strong decreasing of the An $-O_{I}$ by ~0.12 Å. For the multideterminantal wave functions of  $[PuO_2(H_2O)_5]^+$  and  $[NpO_2(H_2O)_5]^+$  when passing from the CASSCF(n,10) to the NEVPT2(n,10), the first-order correction to the wave function is expanded over a set of properly chosen multireference functions which correctly take into consideration the two-electron interactions occurring among the active electrons.<sup>42</sup> The MP2 method induces a slight increases of the An-O<sub>vl</sub> bond and a strong decrease of the An-O<sub>1</sub> with respect to the HF results. This unbalanced effects must be reflecting the fact of perturbing an uncorrelated unrestricted-spin wave function. We have included in the table the case of the uranyl pentahydrate, a closed-shell case, computed at the HF and MP2 level. In this case it is observed how for the one-determinantal wave function, the dynamic electron correlation introduced by MP2 leads to a lengthening of both distances.

The B3LYP method includes an approach of the wave function dynamically correlated via the electron density estimation what leads to modest increases of the  $An-O_{yl}$ bond as well as of the  $An-O_I$ . The fact we are dealing with multireferencial wave functions makes hard to separate the effects that static and dynamic electron correlation causes on the geometries. Nevertheless, it is generally accepted that the most rigorous way to undertake this type of systems is via a methodology which allows a balanced combination of static and dynamic electron correlation such as the NEVPT2 method provides.<sup>40,41</sup>

Figure 3 shows the An–O and An-H RDFs for the NpO<sub>2</sub><sup>+</sup> (red lines) and  $PuO_2^+$  (black lines) cations in aqueous solution derived from the MD simulations. The RDFs of both cations are quite similar, only a slight shifting toward longer distances in the mean values is observed (see Table 1 MD POTn (300 K) rows) when passing from  $PuO_2^+$  to  $NpO_2^+$ . This is a consequence of the native quantum-mechanical trend observed in the minimized pentahydrates. Thus, the QM gap of  $R_{An-Ovl}$ between NpO2<sup>+</sup> and PuO2<sup>+</sup> hydrates is 0.025 Å, whereas the RDFs shows a gap of 0.02 Å. The trend of the  $An-O_I$ parameter is similar to that of the  $An-O_{vl}$ : the  $Np-O_{I}$ distance is ~0.02 Å longer than that of  $Pu-O_{I}$ , and the gap in solution is similar because the mean distance changes induced by solvation are only ~0.001 Å. The number of water molecules in the second shell is  $\sim 21$  for the two cations, these values are similar to those corresponding to their divalent cations (see Figures 2 and 3 of ref 51).

Figure 4 shows the distribution of water molecules around the different angular regions in one hemisphere that can be defined taking advantage of the system symmetry. The equatorial region ( $60-90^{\circ}$  and  $90-120^{\circ}$ ) presents two welldefined shells; the An-O and An-H first peaks correspond to the first hydration shell, already shown in Figure 3, as well as a second hydration shell that integrates to ~9.2 molecules centered at 4.8 Å for the oxygen atoms. The comparison for each angular region of the An-O and An-H peak position sheds light on the relative orientation of water molecules. Thus, in the equatorial region, hydration shells take an iondipole orientation, because the An-H peak is shifted ~0.7 Å from the An-O peak. In the intermediate zones ( $30-60^{\circ}$  and  $120-150^{\circ}$ ), the running integration number is ~9 centered far from the actinyl, ~4.5 Å, and the An-O and An-H peaks



**Figure 3.** An–O (top) and An–H (bottom) radial distribution functions and their coordination numbers for Np(V) (red) and Pu(V) (black) in aqueous solution as obtained from the MD simulations.

overlap, which means that the water molecules orientation is rather a compromise of their interactions among the molecular cation and the hydration water molecules. In the axial regions, ~3.4 molecules are associated with the main peak which is centered at ~4.5 Å from the actinide. This rather depopulated axial region shows that hydrogen atoms are closer to the metal cation than to the oxygen atoms due to the presence of  $O_{\rm yl}$ atoms. Bearing in mind that the An– $O_{\rm yl}$  distance is ~1.8 Å, the mean distance of one water hydrogen atom to the  $O_{\rm yl}$  atom is ~2.2 Å. This weak hydrogen bond pattern was not found in the previous cases studied of divalent actinyl.<sup>51</sup> The last two regions can be envisaged as hydration structures that build the condensed medium around the aqua ion as well as they solvate slightly the actinyl cation.

Table 3 collects a set of energetic and dynamical properties of the monovalent aqueous solutions. The hydration enthalpies agree well with the estimated experimental values given by Gibson et al.<sup>59</sup> It must be indicated that the sensitivity of  $PuO_2^+$  electron wave function to its close environment have caused a large uncertainty in the hydration energy among different authors<sup>29</sup> as indicated by Ryzhkov et al.<sup>35</sup> in their recent study on Pu complexes in water. Taking into account the uncertainties, one can conclude that the hydration enthalpy of both cations is almost the same. Regarding the aqua ion dynamics, their size-corrected diffusion coefficient values for neptunyl and plutonyl are also quite similar. The calculated ion



Figure 4. An–O and An–H angle-solved RDFs Np(V) (red) and Pu(V) (black) in aqueous solution as obtained from the MD simulations.

Table 3. Energetic and Dynamical Properties Calculatedfrom the MD Simulations

property	NpO <sub>2</sub> <sup>+</sup>	PuO2 <sup>+</sup>
$\Delta H_{\rm hyd}~( m kcal~mol^{-1})$	$-166 \pm 3$	$-165 \pm 3$
$\Delta H_{ m hyd}^{ m exp59}$ (kcal mol <sup>-1</sup> )	$-180 \pm 20$	$-178 \pm 20$
$D_{\rm An}~(10^{-5}~{ m cm}^2~{ m s}^{-1})$	$1.1 \pm 0.2$	$1.1 \pm 0.2$
$D_{\rm An}^{\rm \ corr} (10^{-5} {\rm \ cm}^2 {\rm \ s}^{-1})$	$1.4 \pm 0.2$	$1.4 \pm 0.2$
$D_{\mathrm{An}}/D_{\mathrm{W}}$	$0.44 \pm 0.04$	$0.43 \pm 0.04$

mobility is affected by the water mobility, which depends on the water model employed, in our case TIP4P. This model overestimates the water diffusion coefficient,  $3.3 \times 10^{-5} \text{ cm}^2$  $s^{-1}$ , <sup>60</sup> as the experimental value is  $2.3 \times 10^{-5}$  cm<sup>2</sup> s<sup>-1</sup>. For this reason, a better test is needed to compare the values normalized by the water self-diffusion coefficient. The  $D_{\rm An}/$  $D_{\rm w}$  values are 0.44 and 0.43 for NpO<sub>2</sub><sup>+</sup> and PuO<sub>2</sub><sup>+</sup>, respectively. Tiwari et al.<sup>61</sup> have computed the diffusion coefficient for the monovalent actinyls using the SPC/E water model, their normalized values of the size-corrected  $D_{Ap}/D_{w}$ are 0.46 and 0.45 for NpO2<sup>+</sup> and PuO2<sup>+</sup>, respectively. Their corresponding values for the divalent actinyls, NpO22+ and  $PuO_2^{2+}$ , computed in our previous work<sup>38'</sup> with the same methodology but using a B3LYP-based force field are 0.38, that represents a low limit of diffusion for  $PuO_2^+$  and  $NpO_2^+$  as they are singly charged. Simonin et al.<sup>62</sup> have determined experimentally for  $UO_2^{2+}$  at infinite dilute aqueous solution a normalized value of 0.30. Our theoretical normalized value for the divalent uranyl, which was also computed in our previous work<sup>38</sup> was 0.37.

Another illustrative test of the actinyl dynamics in aqueous solutions is the analysis of the most representative vibrational normal modes. Table 4 shows the symmetric  $(1A_1)$  and

Table 4. Experimental and MD Normal Mode Frequencies  $(cm^{-1})$ 

frequencies	method	$E_1$	$2A_1$	$1A_1$	$A_2$
$[NpO_2(H_2O)_5]^*$	MD (gas phase)	393	251	819	870
	MD (solution)	227	305	798	853
	exp <sup>63,64</sup>			767	824
$[PuO_2(H_2O)_5]^+$	MD (gas phase)	441	250	780	828
	MD (solution)	276	296	764	811
	exp <sup>65</sup>			748	

asymmetric (A2) An–O $_{yl}$  stretching normal modes, the  $O_{vl}-$ An- $O_{yl}$  bending  $(E_1)$  and the water breathing stretching (2A1). To account for the solvent effects, the gas-phase frequencies of the two pentahydrates have been included in the table. Interestingly, one can observe that for the two actinyl stretching modes the solvation induces redshifts of their frequencies of about  $15-20 \text{ cm}^{-1}$ . This is a consequence of the interactions with second-shell water molecules in the intermediate and axial regions. On the contrary, solvent effects induce a blueshift of  $\sim 50$  cm<sup>-1</sup> in the water-breathing mode. This is due to the strong aqua ion-water interactions in the equatorial region, where second-shell water molecules causes a compactness of the first-shell water molecules, then increasing the corresponding frequency of the water breathing vibrational mode. Only three experimental frequencies have been reported in the literature;  $^{63-\overline{65}}$  the error of our estimation is smaller than 4% and the sequence predicted by our potentials is the same than the experimental one.

Figures 5 and 6 display the comparison of the experimental EXAFS spectrum reported in the literature from several authors for  $NpO_2^+$  and  $PuO_2^+$  in dilute aqueous solutions, together with the revisited spectra previously reported by Di Giandomenico et al.<sup>15</sup> In the  $NpO_2^+$  case, we can see the reasonable agreement of our simulated spectrum with the three experimental ones.<sup>9,12,15</sup> Because the experimental difficulties for the X-ray absorption spectrum recording, the difference among the experimental spectra is similar to that observed for the experimental-theoretical comparison. In the bottom of Figure 5 we have included the simulated EXAFS spectrum obtained using our previous NEVPT2-based intermolecular potential.<sup>38</sup> This spectrum almost matches the spectrum obtained in this work which employs a simplified version of the intramolecular actinyl potential (IMC).

Regarding the  $PuO_2^+$  EXAFS spectra, Figure 6 also shows that the differences among them are similar to the relative discrepancy of our simulated spectrum with the three experimental spectra. From the set of EXAFS measurements carried out by one of us on the actinyls in a previous work,<sup>15</sup> the revisited PuO<sub>2</sub><sup>+</sup> spectrum recorded in transmission mode has been analyzed and included in Figure 6. The spectrum is similar to the spectrum published in that article, although signal/noise is higher as well as global intensity. (cf., "revisited spectrum" in Figure 6 with  $Pu(V)/HClO_4$  in Figure 4 of ref 15). The complicated shape of the EXAFS spectrum is reproduced well by the simulated one in the five oscillations experimentally recorded.

The striking question is the fact that the  $S_0^2$  values needed to match the main oscillations (maximum at  $k = 5 \text{ Å}^{-1}$ ) are small,



Figure 5. Top: Simulated (dashed black line) vs experimental (solid line green (ref 12), blue (ref 9), red (reanalyzed from ref 15)) Np L<sub>III</sub>edge  $k^3$ -weighted EXAFS spectra for NpO<sub>2</sub><sup>+</sup> in water. Bottom: Comparison between the two simulated EXAFS spectra computed by means of the new NEVPT2 force field developed in this work (black) and the force field developed in a previous work (magenta).<sup>3</sup>

0.7 for the transmission mode spectrum,<sup>15</sup> 0.6 for that of Dalodière et al.,<sup>20</sup> and 0.45 for that of Panak et al. one.<sup>14</sup> In the case of the  $NpO_2^+$ , the values needed are in the range of 0.7– 0.9. This fact might be related to the reduction of the coordination number from 5 water molecules in NpO<sub>2</sub><sup>+</sup> aqueous solution to 4 in the  $PuO_2^+$  case.

To find out on this issue we have undertaken three additional analysis: (i) quantum-mechanical computation of the relative stability of the two hydrates in water at the same level of calculation employed to develop the force field, (ii) experimental fitting of the previously recorded plutonyl EXAFS spectrum assuming the constraint of a hydration number 4 or 5, and (iii) development a force field for  $PuO_2^+$  in water based on a tetrahydrate cation and the analysis of results derived from the corresponding MD simulation at 300 K.

A direct procedure to estimate quantum-mechanically the relative stability of  $[PuO_2(H_2O)_4]^+$  and  $[PuO_2(H_2O)_5]^+$  in water is the computation of the equilibrium

$$[PuO_{2}(H_{2}O)_{4}]^{+}(aq) + H_{2}O(aq) \rightleftharpoons [PuO_{2}(H_{2}O)_{5}]^{+}(aq)$$
(4)

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**Figure 6.** Simulated (dashed black line) vs experimental (solid line blue (ref 20), green (ref 14) and red (reanalyzed from ref 15)) Pu  $L_{III}$ -edge  $k^3$ -weighted EXAFS spectra for  $PuO_2^+$  in water.

This equation can be envisaged as the difference between the  $PuO_2^+$  hydration free energy corresponding to the formation of the tetrahydrate and pentahydrate aqua ions in water

$$PuO_{2}^{+}(g) + 4H_{2}O(g)$$

$$\xrightarrow{\Delta G_{g}^{\circ}} [PuO_{2}(H_{2}O)_{4}]^{+}(g)$$

$$\xrightarrow{\Delta G_{solv}^{*}} [PuO_{2}(H_{2}O)_{4}]^{+}(aq)$$
(5)

$$PuO_{2}^{+}(g) + 5H_{2}O(g)$$

$$\xrightarrow{\Delta G_{g}^{\circ}} [PuO_{2}(H_{2}O)_{5}]^{+}(g)$$

$$\xrightarrow{\Delta G_{solv}^{*}} [PuO_{2}(H_{2}O)_{5}]^{+}(aq) \qquad (6)$$

$$nH_2O(g) \xrightarrow{\Delta G_{solv}^*} nH_2O(aq)$$
 (7)

The hydration free energy of  $PuO_2^+$  is then computed by the addition of the gas-phase hydrate formation,  $\Delta G_{g}^\circ$ , its solvation in water,  $\Delta G_{solv}^*$  computed by means of the continuum polarizable model, <sup>66</sup> CPCM, <sup>67</sup> as implemented in the ORCA program, <sup>43</sup> the vaporization free energy of *n* water and the standard state correction associated with the gas phase-solution transfer, as given by Goddard et al.<sup>68</sup> The values of the

hydration energy are -124 and -128 kcal/mol for the tetraand pentahydrate, respectively. Table S6 collects the different contributions to these estimations. From these data, the free energy of eq 4 is -4 kcal/mol, which indicates the preference for the pentahydration of PuO<sub>2</sub><sup>+</sup> in water from a quantummechanical semicontinuum model of solvation.<sup>69</sup>

Figure 7 shows the revisited experimental  $L_3$ -edge  $k^3$ -weighted EXAFS spectra of NpO<sub>2</sub><sup>+</sup> and PuO<sub>2</sub><sup>+15</sup> and their fits



**Figure 7.** Np (top) and Pu (bottom)  $L_{III}$ -edge  $k^3$ -weighted EXAFS spectra for NpO<sub>2</sub><sup>+</sup> and PuO<sub>2</sub><sup>+</sup> in water: experimental (red solid line)<sup>15</sup> and fits assuming a hydration number of four (cyan dashed line) or five (black dashed line).

obtained when the first hydration shell is constrained to 4 (cyan dashed line) or 5 (black dashed line). It is observed that the two fits are very similar, and that conclusion is verified by examining Table 5, which collects the main parameters of the fits. This leads to the fact that the assumption of a given coordination number does not change the values of the fitted parameters, since the quality of the fits are almost the same. As already indicated, the sensitivity of the EXAFS for these spectra with such a low signal/noise ratio, due to the high experimental complexity of the measurements, blurs the subtle discrimination of one unit coordination number. Regarding the main An-O distances, one can compare the sequence of distances derived from our MD simulations (MD POT5 (300 K) rows in Table 1) with the EXAFS fit of Table 5. The trend with the change of actinoid is the same, i.e.,  $R(NpO_{vl}) >$  $R(PuO_{vl})$  and  $R(NpO_{l}) > R(PuO_{l})$ . Even more, the distance changes when going from Np to Pu given by MD simulations

Table 5. EXAFS Best-Fit Parameters of  $\rm NpO_2^+$  and  $\rm PuO_2^+$  in  $\rm HClO_4$ 

fit parameters	$\frac{\text{NpO}_2^+}{(\text{CN}=4)}$	$\frac{\text{NpO}_2^+}{(\text{CN}=5)}$	$PuO_2^+$ (CN = 4)	$\frac{PuO_2^+}{(CN = 5)}$
$R(An-O_{yl})$ (Å)	1.83(1)	1.83(1)	1.80(1)	1.80(1)
$\sigma^2(An-O_{yl}) \ (A^2)$	0.0003	0.0000	0.0019	0.0015
$R(An-O_I)$ (Å)	2.51(1)	2.51(1)	2.47(1)	2.47(1)
$\sigma^2(An-O_I) \ (A^2)$	0.0034	0.0044	0.0061	0.0074
$S_0^{2}$	0.9	0.8	0.8	0.7
$E_0$ (eV)	6.0	5.6	6.4	6.1
$R_{\rm factor}$ (%)	2.5	2.6	4.9	6.5

and the EXAFS fittings are close:  $\Delta R_{AnOyl}$  is -0.02 Å (MD) and -0.03 Å (EXAFS fit);  $\Delta R_{AnOI}$  is -0.02 Å (MD) and -0.04 Å (EXAFS fit).

The final analysis deals with the use of a force field developed on the basis of the intramolecular and intermolecular interactions of  $[PuO_2(H_2O)_4]^+$ . When running a free MD simulation at 300 K, the plutonyl cation hydration always evolves to a pentahydrate. Pomogaev et al.<sup>58</sup> in their MD simulations of a set of monovalent actinyl cations showed how the initial tetrahydrate cation, defined as starting hydrated ion, became a pentahydrate when the system evolved. To get a deeper insight into this issue, we envisage a strategy to get a set of snapshots derived from a simulation of a PuO<sub>2</sub><sup>+</sup> aqueous solution, where the cation first-shell was formed by only four water molecules. Toward this aim, we added to our HIW force field for the plutonyl tetrahydrate an additional repulsive Pu-O term,  $(C/r^{-8})$ , that prevented the presence of bulk water molecules inside the first shell. This penalty function vanishes beyond the first shell such as the first-shell-second-shell interactions are those provided by the original force field built from the tetrahydrate. Table 1 collects the main geometrical parameters of the optimized clusters, POT4(NEVPT2) for CN = 4, that compare fairly well with the corresponding QM optimizations of the same hydrates  $(R(PuO_{vl})$  is 1.800 Å (QM) and 1.795 (POT4) Å;  $R(PuO_1)$  is 2.448 Å (QM) and 2.450 Å (POT4)). The Pu-O and Pu-H RDFs for the MD simulation using POT4(NEVPT2) are plotted in Figure S6, as well as the RDFs derived of the POT5(NEVPT2). The mean values derived from these POT4(NEVPT2) RDFs are also collected in Table 1 and show the same slight changes due to bulk solvent effects already observed for the POT5(NEVPT2) RDFs. Figure 8 compares the simulated EXAFS spectrum of  $PuO_2^+$  in water obtained by the force field developed under the assumption of a pentahydration, which was already compared with the experimental spectra in Figure 6 and the spectrum obtained with the force field built imposing a tetrahydration. For the sake of comparison, the experimental PuO<sub>2</sub><sup>+</sup> EXAFS spectrum revisited from Di Giandomenico et al.<sup>15</sup> has also been included in Figure 8. Two important facts can be drawn from this figure. The first one is that the tetrahydrate-derived EXAFS does not reproduce the spectrum shape in the peculiar 6-8 Å<sup>-1</sup> region. The second one is that the intensity of both spectra is similar, although the coordination number, 5 versus 4, of their first hydration shell could lead to expect a higher intensity for the first spectrum. Certainly, the similarity between both spectra shows the great difficulty to discriminate



**Figure 8.** Simulated Pu  $L_{III}$ -edge  $k^3$ -weighted EXAFS spectra for PuO<sub>2</sub><sup>+</sup> in water using the restricted 4 first-shell water molecules force field, POT4(NEVPT2) (cyan), or the pentahydrate force field, (POT5(NEVPT2) (black) vs. the experimental one.<sup>15</sup>

a hydration number when experimental signal/noise ratio is low.

The relationship between the change of shape of the PuO<sub>2</sub><sup>+</sup> EXAFS spectrum in the 6-8  $Å^{-1}$  region and the Pu-O<sub>vl</sub> and Pu-O<sub>I</sub> distances deserves a final comment. Hydration effects on the aqua ions described by means of the MD simulations, induce changes on the distances which are in the order of 0.01–0.02 Å. The corresponding changes when going from  $[PuO_2(H_2O)_4]^+$  to  $[PuO_2(H_2O)_5]^+$  are much more important, in particular, for the An $-O_I$  distance that increases by ~0.05 Å. This is already observed in the QM(NEVPT2) and in the intermolecular potentials developed POT5/4(NEVPT2) optimized structures. Since solvent effects are small, the gap of the Pu–O<sub>I</sub> distance between the tetra- and the pentahydrate holds up in the in-solution simulations MD-POT4/5 (300 K) giving rise to the different shape of the EXAFS spectrum in the 6-8 Å<sup>-1</sup> region. This subtle change is responsible for the good agreement found and supports the prevalence of the PuO<sub>2</sub><sup>+</sup> pentahydration in water. Interestingly, it can be seen how the experimental fittings shown in Table 5 give the same  $An-O_{I}$ distance for both coordination numbers in order to provide a good reproduction of such challenging region.

#### CONCLUDING REMARKS

The use of highly correlated wave functions to build the force fields of the paramagnetic actinyls,  $NpO_2^+$  and  $PuO_2^+$ , in aqueous solutions has been shown to improve the accuracy of physicochemical properties of the systems. In particular, the sensitivity of EXAFS spectrum shape to the structural features points out that the comparison of experimental and simulated spectra is a valuable tool to validate the microscopical structure provided by the statistical simulations.

The structural differences between these actinyl cations in aqueous solutions are small. The quantum mechanical description of the aqua ions are already small:  $R(Np-O_{yl}) = 1.83$  Å versus  $R(Pu-O_{yl}) = 1.81$  Å, and  $R(Np-O_{l}) = 2.52$  Å and  $R(Pu-O_{l}) = 2.51$  Å. Given that these actinyl aqua ions are monovalent, the impact of the rest of the solvent on their geometries is small, changing only slightly the internal parameters of the aqua ions. They are pentahydrates. This conclusion is based on the quantum-mechanical and statistical descriptions of  $PuO_2^+$ , the similarity observed at the same

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calculation level for  $NpO_2^+$ , where the hydration number is widely accepted as 5 and the good agreement with the experimental EXAFS spectra. The tetracoordination proposal based on EXAFS fitting could be biassed by the general low intensity of the recorded spectrum signal, for instance, when compared to the neptunyl case. To the generally accepted uncertainty of  $\pm 1$  units in the coordination number provided by the EXAFS fitting, we must add the intrinsic experimental difficulties joined to the preparation and recording of these hazardous complexes radioactive samples. Modelization of ionic solutions with ad-hoc intramolecular potentials has helped to refine the analysis of intriguing radioactive species in water and validate future uses of these potentials to further simulations of these radioactive species in water. In particular, the revisiting of previously studied lower computational level actinyl divalent cations,<sup>37,38</sup> such as  $PuO_2^{2+}$ ,  $NpO_2^{2+}$ , and  $AmO_2^{2+}$ , as well as actinoid aqua ions,<sup>70</sup> appear as challenging next steps in the study of the actinides in aqueous solutions.

#### ASSOCIATED CONTENT

#### **G** Supporting Information

The Supporting Information is available free of charge at https://pubs.acs.org/doi/10.1021/acs.inorgchem.2c00461.

Description of the intermolecular potential formalism. Tables with parameters force field obtained for  $AnO_2^+$ - $H_2O$  (M = Np, Pu). Figures showing the representative set of structure types employed in the fitted potentials. Plots showing the correlation between the QM interaction energies and the predicted values by the developed force field. Examples of input FEFF files used for the XAS spectrum simulations. Details of the QM computation of the PuO<sub>2</sub><sup>+</sup> tetrahydrate and pentahydrate equilibrium. Pu-O and Pu-H RDFs of the MD simulation conducted with the POT4(NEVPT2) potential (PDF)

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#### Notes

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#### REFERENCES

(1) Cotton, S. Lanthanide & Actinide Chemistry; Wiley: London, 2006.

(2) Rizkalla, E. M.; Choppin, G. Handbook on the Physics and Chemistry of Rare Earths; Elsevier: North-Holland, 1991; Vol. 15, Chapter 103.

(3) Aaberg, M.; Ferri, D.; Glaser, J.; Grenthe, I. Structure of the hydrated dioxouranium (VI) ion in aqueous solution. An x-ray diffraction and proton NMR study. *Inorg. Chem.* **1983**, *22*, 3986–3989.

(4) Allen, P. G.; Bucher, J. J.; Shuh, D. K.; Edelstein, N. M.; Reich, T. Investigation of aquo and chloro complexes of  $UO_2^{2+}$ ,  $NpO_2^+$ ,  $Np^{4+}$ , and  $Pu^{3+}$  by X-ray absorption fine structure spectroscopy. *Inorg. Chem.* **1997**, *36*, 4676–4683.

(5) Wahlgren, U.; Moll, H.; Grenthe, I.; Schimmelpfennig, B.; Maron, L.; Vallet, V.; Gropen, O. Structure of Uranium(VI) in Strong Alkaline Solutions. A Combined Theoretical and Experimental Investigation. J. Phys. Chem. A **1999**, *103*, 8257–8264.

(6) McKibben, J. M. Chemistry of the Purex Process. Radiochim. Acta 1984, 36, 3-15.

(7) Altmaier, M.; Gaona, X.; Fanghänel, T. Recent Advances in Aqueous Actinide Chemistry and Thermodynamics. *Chem. Rev.* 2013, 113, 901–943.

(8) Bardin, N.; Rubini, P.; Madic, C. Hydration of Actinyl(VI),  $MO_2^{2+}(aq)$  (M = U, Np, Pu). An NMR Study. *Radiochim. Acta* **1998**, 83, 189–194. and references therein.

(9) Reich, T.; Bernhard, G.; Geipel, G.; Funke, H.; Hennig, C.; Roßberg, A.; Matz, W.; Schell, N.; Nitsche, H. The Rossendorf Beam Line ROBL – a dedicated experimental station for XAFS measurements of actinides and other radionuclides. *Radiochim. Acta* 2000, *88*, 633–637.

(10) Antonio, M. R.; Soderholm, L.; Williams, C. W.; Blaudeau, J. P.; Bursten, B. E. Neptunium redox speciation. *Radiochim. Acta* 2001, *89*, 17–26.

(11) Neuefeind, J.; Soderholm, L.; Skanthakumar, S. Experimental Coordination Environment of Uranyl(VI) in Aqueous Solution. *J. Phys. Chem. A* **2004**, *108*, 2733–2739.

(12) Ikeda-Ohno, A.; Hennig, C.; Rossberg, A.; Funke, H.; Scheinost, A. C.; Bernhard, G.; Yaita, T. Electrochemical and complexation behavior of neptunium in aqueous perchlorate and nitrate solutions. *Inorg. Chem.* **2008**, *47*, 8294–8305.

(13) Skanthakumar, S.; Antonio, M.; Soderholm, L. A Comparison of Neptunyl(V) and Neptunyl(VI) Solution Coordination: The Stability of Cation-Cation Interactions. *Inorg. Chem.* **2008**, *47*, 4591–4595.

(14) Panak, P.; Booth, C. H.; Caulder, D.; Bucher, J.; Shuh, D.; Nitsche, H. X-ray absorption fine structure spectroscopy of plutonium complexes with bacillus sphaericus. *Radiochim. Acta* **2002**, *90*, 315–321.

(15) Di Giandomenico, M. V.; Le Naour, C.; Simoni, E.; Guillaumont, D.; Moisy, P.; Hennig, C.; Conradson, S. D.; Den Auwer, C. Structure of early actinides(V) in acidic solutions. *Radiochim. Acta* 2009, *97*, 347–353.

(16) Odoh, S.; Bylaska, E.; de Jong, W. Coordination and hydrolysis of Plutonium ions in aqueous solution using Car-Parrinello molecular dynamics free energy simulations. *J. Phys. Chem. A* **2013**, *117*, 12256–12267.

(17) Denecke, M. A. Actinide Speciation Using X-Ray Absorption Fine Structure Spectroscopy. *Coord. Chem. Rev.* **2006**, *250*, 730–754.

Article

(18) Conradson, S. D. Application of X-ray absorption fine structure spectroscopy to materials and environmental science. *Appl. Spectrosc.* **1998**, *52*, 252A–279A.

(19) Knope, K. E.; Soderholm, L. Solution and Solid-State Structural Chemistry of Actinide Hydrates and Their Hydrolysis and Condensation Products. *Chem. Rev.* **2013**, *113*, 944–994.

(20) Dalodière, E.; Virot, M.; Dumas, T.; Guillaumont, D.; Illy, M.; Berthon, C.; Guerin, L.; Rossberg, A.; Venault, L.; Moisy, P.; Nikitenko, S. I. Structural and magnetic susceptibility characterization of Pu(V) aqua ion using sonochemistry as a facile synthesis method. *Inorg. Chem. Front.* **2018**, *5*, 100–111.

(21) Reich, T.; Geipel, G.; Funke, H.; Hennig, C.; Roßberg, A.; Bernhard, G. XANES and EXAFS measurements of plutonium hydrates. In *Biannual Report 1999/2000, FZR-322*; Project-Group ESRF-Beamline (ROBL-CRG), 2001; pp 27–32.

(22) Hennig, C.; Schmeide, K.; Brendler, V.; Moll, H.; Tsushima, S.; Scheinost, A. C. EXAFS Investigation of U(VI), U(IV), and Th(IV) Sulfato Complexes in Aqueous Solution. *Inorg. Chem.* **200**7, *46*, 5882–5892.

(23) Galbis, E.; Hernández-Cobos, J.; Den Auwer, C.; Le Naour, C.; Guillaumont, D.; Simoni, E.; Pappalardo, R. R.; Sánchez Marcos, E. Solving the Hydration Structure of the Heaviest Actinide Aqua Ion Known: The Californium (III) Case. *Angew. Chem., Int. Ed.* **2010**, *122*, 3899–3903.

(24) Tsushima, S.; Suzuki, A. Hydration numbers of pentavalent and hexavalent uranyl, neptunyl, and plutonyl. *J. Mol. Struct.*(*THEO-CHEM*) **2000**, *529*, 21–25.

(25) Hay, P. J.; Martin, R. L.; Schreckenbach, G. Theoretical Studies of the Properties and Solution Chemistry of  $AnO_2^{+}$  and  $AnO_2^{+}$  Aquo Complexes for An = U, Np, and Pu. *J. Phys. Chem. A* **2000**, *104*, 6259–6270.

(26) Moskaleva, L.; Krüger, S.; Spörl, A.; Rösch, N. Role of Solvation in the Reduction of the Uranyl Dication by Water:A Density Functional Study. *Inorg. Chem.* **2004**, *43*, 4080–4090.

(27) Gutowski, K.; Dixon, D. Predicting the Energy of the Water Exchange Reaction and Free Energy of Solvation for the Uranyl Ion in Aqueous Solution. *J. Phys. Chem. A* **2006**, *110*, 8840–8856.

(28) Danilo, C.; Vallet, V.; Flament, J.-P.; Wahlgren, U. Effects of the first hydration sphere and the bulk solvent on the spectra of the f2 isoelectronic actinide compounds:  $U^{4+}$ ,  $NpO_2^+$ , and  $PuO_2^{2+}$ . *Phys. Chem. Chem. Phys.* **2010**, *12*, 1116–1130.

(29) Clark, A. E.; Samuels, A.; Wisuri, K.; Landstrom, S.; Saul, T. Sensitivity of Solvation Environment to Oxidation State and Position in the Early Actinide Period. *Inorg. Chem.* **2015**, *54*, 6216–6225.

(30) Palmer, B. J.; Pfund, D. M.; Fulton, J. L. Direct Modeling of EXAFS Spectra from Molecular Dynamics Simulations. *J. Phys. Chem.* **1996**, *100*, 13393–13398.

(31) Merkling, P. J.; Muñoz-Páez, A.; Sánchez Marcos, E. Exploring the Capabilities of X-Ray Absorption Spectroscopy for Determining the Structure of Electrolyte Solutions: Computed Spectra for Cr<sup>3+</sup> or Rh<sup>3+</sup> in Water Based on Molecular Dynamics. *J. Am. Chem. Soc.* **2002**, *124*, 10911–10920.

(32) Muñoz-Páez, A.; Sánchez Marcos, E. In *Comprehensive Inorganic Chemistry II: From Elements to Applications*, 2nd ed.; Reedijk, J., Poeppelmeier, K., Eds.; Elsevier, 2013; Vol. 9, pp 133– 159.

(33) D'Angelo, P.; Martelli, F.; Spezia, R.; Filipponi, A.; Denecke, M. A. Hydration Properties and Ionic Radii of Actinide (III) Ions in Aqueous Solution. *Inorg. Chem.* **2013**, *52*, 10318–10324.

(34) Provost, K.; Beret, E. C.; Bouvet Muller, D.; Michalowicz, A.; Sánchez Marcos, E. EXAFS Debye-Waller factors issued from Car-Parrinello molecular dynamics: Application to the fit of oxaliplatin and derivatives. J. Chem. Phys. **2013**, *138*, 084303.

(35) Ryzhkov, M. V.; Enyashin, A. N.; Delley, B. Plutonium complexes in water: new approach to ab initio modeling. *Radiochim. Acta* **2021**, *109*, 327–342.

(36) Pérez-Conesa, S.; Torrico, F.; Martínez, J. M.; Pappalardo, R. R.; Sánchez Marcos, E. A Hydrated Ion Model of  $[UO_2]^{2+}$  in Water:

Structure, Dynamics, and Spectroscopy from Classical Molecular Dynamics. J. Chem. Phys. 2016, 145, 224502.

(37) Pérez-Conesa, S.; Martínez, J. M.; Pappalardo, R. R.; Sánchez Marcos, E. Extracting the Americyl Hydration from an Americium Cationic Mixture in Solution: A Combined X-ray Absorption Spectroscopy and Molecular Dynamics Study. *Inorg. Chem.* **2018**, *57*, 8089–8097.

(38) Pérez-Conesa, S.; Martínez, J. M.; Pappalardo, R. R.; Sánchez Marcos, E. Combining EXAFS and computer simulations to refine the structural description of actinyls in water. *Molecules* **2020**, *25*, No. 5250.

(39) Rehr, J. J.; Kas, J. J.; Vila, F. D.; Prange, M. P.; Jorissen, K. Parameter-free calculations of x-ray spectra with FEFF9. *Phys. Chem. Chem. Phys.* **2010**, *12*, 5503–5513.

(40) Angeli, C.; Cimiraglia, R.; Malrieu, J.-P. N-electron valence state perturbation theory: a fast implementation of the strongly contracted variant. *Chem. Phys. Lett.* **2001**, *350*, 297–305.

(41) Angeli, C.; Cimiraglia, R.; Malrieu, J.-P. n-electron valence state perturbation theory: A spinless formulation and an efficient implementation of the strongly contracted and of the partially contracted variants. *J. Chem. Phys.* **2002**, *117*, 9138–9153.

(42) Angeli, C.; Cimiraglia, R.; Evangelisti, S.; Leininger, T.; Malrieu, J.-P. Introduction of n-electron valence states for multireference perturbation theory. *J. Chem. Phys.* **2001**, *114*, 10252– 10264.

(43) Neese, F.; Wennmohs, F.; Becker, U.; Riplinger, C. The ORCA quantum chemistry program package. *J. Chem. Phys.* **2020**, *152*, 224108.

(44) Denning, R. G. Electronic Structure and Bonding in Actinyl Ions and their Analogs. J. Phys. Chem. A 2007, 111, 4125–4143.

(45) Gendron, F.; Páez-Hernández, D.; Notter, F.-P.; Pritchard, B.; Bolvin, H.; Autschbach, J. Magnetic Properties and Electronic Structure of Neptunyl(VI)Complexes: Wavefunctions, Orbitals, and Crystal-Field Models. *Chem. - Eur. J.* **2014**, *20*, 7994–8011.

(46) Zheng, J.; Xu, X.; Truhlar, D. Minimally augmented Karlsruhe basis sets. *Theor. Chem. Acc.* 2011, 128, 295–305.

(47) Weigend, F.; Ahlrichs, R. Balanced basis sets of split valence, triple zeta valence and quadruple zeta valence quality for H to Rn: Design and assessment of accuracy. *Phys. Chem. Chem. Phys.* **2005**, *7*, 3297–3305.

(48) Cao, X.; Dolg, M.; Stoll, H. Valence basis sets for relativistic energy-consistent small-core actinide pseudopotentials. *J. Chem. Phys.* **2003**, *118*, 487–496.

(49) Pappalardo, R. R.; Sánchez Marcos, E. Recovering the concept of the Hydrated Ion for model ionic solutions: A Monte Carlo study of the  $Zn^{2+}$  in water. *J. Phys. Chem.* **1993**, *97*, 4500–4504.

(50) Martínez, J. M.; Pappalardo, R. R.; Sánchez Marcos, E. Firstprinciples Ion-Water interaction potentials for highly charged monoatomic cations. Computer simulations of  $Al^{3+}$ ,  $Mg^{2+}$  and  $Be^{2+}$ . *J. Am. Chem. Soc.* **1999**, *121*, 3175–3184.

(51) Pérez-Conesa, S.; Torrico, F.; Martínez, J. M.; Pappalardo, R. R.; Sánchez Marcos, E. A General Study of Actinyl Hydration by Molecular Dynamics Simulations Using ab initio Force Fields. *J. Chem. Phys.* **2019**, *150*, 104504.

(52) Jorgensen, W. L.; Chandrasekhar, J.; Madura, J. D.; Impey, R. W.; Klein, M. L. Comparison of Simple Potential Functions for Simulating Liquid Water. J. Chem. Phys. **1983**, 79, 926–935.

(53) Richens, D. T. The Chemistry of Aqua Ions; John Wiley: Chichester, U.K., 1997.

(54) Todorov, I. T.; Smith, W.; Trachenko, K.; Dove, M. T. DL POLY 3: New Dimensions in Molecular Dynamics Simulations

Via Massive Parallelism. J. Mater. Chem. 2006, 16, 1911–1918.

(55) Allen, M.; Tildesley, D. Computer Simulation of Liquids; Clarendon Press: New York, 1983; Chapter 6.

(56) Flyvbjerg, H.; Petersen, H. G. Error Estimates on Averages of Correlated Data. J. Chem. Phys. 1989, 91, 461-466.

(57) Ravel, B.; Newville, M. ATHENA, ARTEMIS, HEPHAESTUS: data analysis for X-ray absorption spectroscopy using IFEFFIT. J. Synchrotron Radiat. 2005, 12, 537–541.

(58) Pomogaev, V.; Tiwari, S. P.; Rai, N.; Goff, G. S.; Runde, W.; Schneider, W. F.; Maginn, E. J. Development and Application of Effective Pairwise Potentials for  $UO_2^{n+}$ ,  $NpO_2^{n+}$ ,  $PuO_2^{n+}$ , and  $AmO_2^{n+}$  (n= 1, 2) Ions With Water. *Phys. Chem. Chem. Phys.* **2013**, *15*, 15954–15963.

(59) Gibson, J. K.; Haire, R. G.; Santos, M.; Marçalo, J.; Pires de Matos, A. Oxidation Studies of Dipositive Actinide Ions,  $An^{2+}$  (An = Th, U, Np, Pu, Am) in the Gas Phase: Synthesis and Characterization of the Isolated Uranyl, Neptunyl, and Plutonyl Ions  $UO_2^{2+}(g)$ ,  $NpO_2^{2+}(g)$  and  $PuO_2^{2+}(g)$ . J. Phys. Chem. A **2005**, 109, 2768–2781. (60) Watanabe, K.; Klein, M. L. Effective Pair Potentials and the Properties of Water. Chem. Phys. **1989**, 131, 157–167.

(61) Tiwari, S. P.; Rai, N.; Maginn, E. J. Dynamics of Actinyl Ions in Water: A Molecular Dynamics Simulation Study. *Phys. Chem. Chem. Phys.* **2014**, *16*, 8060–8069.

(62) Simonin, J.-P.; Billard, I.; Hendrawan, H.; Bernard, O.; Lützenkirchen, K.; Sémon, L. Study of kinetic electrolyte effects on a fast reaction in solution: The quenching of fluorescence of uranyl ion up to high electrolyte concentration. *Phys. Chem. Chem. Phys.* **2003**, *5*, 520–527.

(63) Basile, L. J.; Sullivan, J. C.; Ferraro, J. R.; LaBonville, P. The Raman scattering of uranyl and transuranium V, VI, and VII ions. *Appl. Spectrosc.* **1974**, *28*, 142–145.

(64) Jones, L. H.; Penneman, R. A. Infrared spectra and structure of uranyl and transuranium (V) and (VI) ions in aqueous perchloric acid solution. *J. Chem. Phys.* **1953**, *21*, 542–544.

(65) Madic, C.; Begun, G. M.; Hobart, D. E.; Hahn, R. L. Raman Spectroscopy of Neptunyl and Plutonyl Ions in Aqueous Solution: Hydrolysis of Np(VI) and Pu(VI) and Disproportionation of Pu(V). *Inorg. Chem.* **1984**, *23*, 1914–1921.

(66) Tomasi, J.; Mennucci, B.; Cammi, R. Quantum mechanical continuum solvation models. *Chem Rev.* **2005**, *105*, 2999–3094.

(67) Barone, V.; Cossi, M. Quantum Calculation of Molecular Energies and Energy Gradients in Solution by a Conductor Solvent Model. J. Phys. Chem. A **1998**, *102*, 1995–2001.

(68) Bryantsev, V. S.; Diallo, M. S.; Goddard, W. A., III Calculation of Solvation Free Energies of Charged Solutes Using Mixed Cluster/ Continuum Models. J. Phys. Chem. B 2008, 112, 9709–9719.

(69) Martínez, J.; Pappalardo, R.; Sánchez Marcos, E.; Mennucci, B.; Tomasi, J. Analysis of the Opposite Solvent Effects Caused by Different Solute Cavities on the Metal-Water Distance of Monoatomic Cation Hydrates. *J. Phys. Chem. B* **2002**, *106*, 1118– 1123.

(70) Caralampio, D.; Martínez, J. M.; Pappalardo, R. R.; Sánchez Marcos, E. Hydration Structure of the Elusive Ac(III) Aqua Ion: Interpretation of X-ray Absorption Spectroscopy (XAS) Spectra on the Basis of Molecular Dynamics (MD) Simulations. *Inorg. Chem.* **2019**, *58*, 2777–2783.