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## Mechanistic and environmental control of the prevalence and lifetime of amyloid oligomers

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### Abstract

Amyloid fibrils are self-assembled protein aggregates implicated in a number of human diseases. Fragmentation-dominated models for the self-assembly of amyloid fibrils have had important successes in explaining the kinetics of amyloid fibril formation but predict fibril length distributions that do not match experiments. Here we resolve this inconsistency using a combination of experimental kinetic measurements and computer simulations. We provide evidence for a structural transition that occurs at a critical fibril mass concentration, or 'CFC', above which fragmentation of fibrils is suppressed. Our simulations predict the formation of distinct fibril length distributions above and below the CFC, which we confirm by electron microscopy. These results point to a new picture of amyloid fibril growth in which structural transitions that occur during self-assembly have strong effects on the final population of aggregate species with small, and potentially cytotoxic, oligomers dominating for long periods of time at protein concentrations below the CFC.

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A wide variety of peptides and proteins form self-assembled filamentous structures known as amyloid fibrils. A universal feature of all amyloid aggregates, regardless of the amino acid sequence or native conformation of the starting peptide or protein, is the formation of cross-sheet structure<sup>1-4</sup>. Amyloid fibrils are most commonly associated with human diseases such as Alzheimer's Disease and type-2 diabetes<sup>5</sup>, however, they are also garnering interest in biomaterials applications<sup>6-13</sup>.

Understanding the molecular mechanism(s) leading to amyloid fibril assembly is a key focus of current research. Mechanistic models of amyloid fibril self-assembly are often tested by monitoring the kinetics of formation using absorbance or fluorescence spectroscopy. The kinetics of amyloid fibril formation is typified by a lag phase followed by the onset of rapid growth. This has been attributed to the formation of a critical nucleus via primary nucleation<sup>14</sup> (which may be very rapid) followed by growth via fragmentation, heterogeneous nucleation or branching<sup>15</sup>. This classical picture has been extended to include subtle effects of protein concentration<sup>16</sup>, multi-stage kinetics<sup>17-20</sup>, catalytic conformational conversion<sup>21,22</sup>, and competition between multiple pathways<sup>23</sup>.

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#### Author Contributions:

RM, KE, LJ, RY: data collection; RM: data assembly, analysis and interpretation, experimental design, writing of manuscript; KE: data modelling, manuscript editing; RJA: data modelling and interpretation, model assembly, manuscript editing; CEM: experimental design, data interpretation, writing of manuscript. RM and KE contributed equally to this work.

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Recent research has focused on the role of fragmentation in fibril formation kinetics. Xue *et al.*<sup>24</sup> first noted that fragmentation is central to explaining the kinetics of  $\beta$ -2-microglobulin aggregation, which cannot be described by a straightforward nucleated assembly model. More recently, analytical results show that several important features of fibril growth kinetics can be explained by a model in which fragmentation is the dominant process in fibril assembly<sup>25-28</sup>. The classical picture<sup>29</sup>, in which the lag time, i.e. the duration of the lag phase, is determined by the formation of a thermodynamically unfavourable critical nucleus followed by fibril elongation by monomer addition, predicts that the lag time should

scale with protein concentration as  $\tau_{\text{lag}} \sim c_p^{-\gamma_c}$  where  $\gamma_c = \frac{n_c + 1}{2}$ <sup>15</sup>. Since the critical nucleus size  $n_c > 1$ , in these classical nucleation-elongation models the scaling exponent will always be greater than unity. In contrast, a model dominated by fragmentation, in which fibril fragmentation acts as a positive feedback mechanism producing new ends that can then

grow, is predicted to exhibit a scaling exponent  $\gamma_{\text{frag}} = \frac{1}{2}$ <sup>25</sup>. This prediction appears to be largely consistent with experimental observations of many known amyloidogenic protein systems. However, fragmentation-dominated models predict exponentially decaying fibril length distributions, while experimental measurements typically show distributions peaked at intermediate fibril length<sup>30-32</sup>.

Here we resolve this apparent contradiction by presenting a qualitatively new model for amyloid fibril assembly. Using a series of experiments on bovine insulin, combined with stochastic simulations, we find evidence to support the existence of a critical fibril mass concentration (CFC) above which fibrils undergo a structural transition that suppresses fragmentation. We attribute the onset of arrested fragmentation to a transition of the amyloid fibril solution from a viscous fluid to a viscoelastic gel. Our model predicts the formation of qualitatively distinct fibril length distributions for protein concentrations above and below a critical threshold and we confirm these by experiment. Moreover we show that the concept of a structural transition that arrests the effects of fragmentation enables us to successfully predict the influence of environmental conditions on the fibril assembly pathway. Our results suggest a possible explanation for the observed variation in amyloid disease progression among apparently similar individuals: since the lengths of fibril formed depend critically on the protein concentration and are influenced by environmental conditions, in some individuals the intra- and/or inter-cellular environment may favour the formation of predominantly short and possibly toxic fibrillar species, while in other individuals conditions may result in benign fibril loads.

## RESULTS

### Deviation from fragmentation-dominated models of assembly

The kinetics of bovine insulin amyloid fibril formation was monitored using ThT fluorescence in 96-well microwell plates coated with a hydrophilic polymer. At least 140 replicates were performed for each set of conditions. The growth rate,  $k_{\text{gr}}$ , and the lag time,  $\tau_{\text{lag}}$ , were extracted from the kinetic traces, averaged over replicates (as illustrated in Supplementary Fig. S1). Previous reports have shown the lag times measured for identical protein samples to vary by as much as hours and this has been attributed to the stochastic nature of the nucleation process<sup>33,34</sup>; in our experiments, due to careful control of experimental conditions, the variation in the lag time has been reduced to minutes (Supplementary Fig. S2 shows individual kinetic curves for a typical experiment). Our method thus enables us to identify subtle changes in insulin amyloid fibril growth kinetics upon changing the experimental parameters.

Fig. 1a shows how  $t_{lag}$  scales with the insulin concentration: the scaling exponent,  $\alpha = -0.37 \pm 0.02$ . Since  $\alpha < 1$ , the data are broadly consistent with a model dominated by fragmentation<sup>25</sup>. However, other features of our kinetic data cannot be explained by existing models. For example, the mean maximal fluorescence, i.e. fluorescence at long times, rises sharply between 0.75 and 1.5 mg ml<sup>-1</sup> insulin - an effect that is not predicted by fragmentation-dominated models (Fig. 1b). This effect is not caused by a change in the total fibril mass; pelleting the aggregated material by centrifugation and measuring the remaining protein in the supernatant by UV-Vis spectroscopy confirmed that more than 99% of the total insulin present is in the pellet regardless of the initial protein concentration. Instead, we attribute the sudden order-of-magnitude increase in fluorescence to structural or morphological differences (presumably affecting the binding of the fluorophore) between fibrils formed at 'high' and 'low' insulin concentrations. It is known that the structural characteristics of amyloid fibrils are important in the binding of ThT<sup>35-37</sup>. For example, it has been shown that glucagon fibrils formed at 'high' (> 1 mg ml<sup>-1</sup>) and 'low' (< 1 mg ml<sup>-1</sup>) protein concentrations demonstrate markedly different structural characteristics and ThT fluorescence emission signals<sup>38</sup>. We measured circular dichroism (CD) spectra of insulin amyloid fibrils prepared at concentrations between 0.25 mg ml<sup>-1</sup> and 4 mg ml<sup>-1</sup> and found that the spectra of the fibrils prepared at high (1-4 mg ml<sup>-1</sup>) and low (0.25-0.75 mg ml<sup>-1</sup>) protein concentrations are qualitatively different (Supplementary Fig. S3). Indeed, we observed a striking transition in the circular dichroism signal between 0.75 and 1.5 mg ml<sup>-1</sup>, consistent with the transition seen in our fluorescence measurements (Fig 1b).

To better understand the nature of this transition we performed bead tracking microrheology on amyloid fibril samples at a range of insulin concentrations. We find a transition from a viscous fluid to a gel state for fibrils formed at protein concentrations above 0.75 mg ml<sup>-1</sup> (Supplementary Fig. S4). We propose that in these high concentration samples fragmentation is arrested due to the formation of a gel-like network of fibrils. Taken together, these findings lead us to propose that there exists some critical fibril mass concentration, or 'CFC', above which fragmentation is suppressed, and that for insulin this becomes manifest in our kinetic data at protein concentrations at or above a threshold  $c_T \sim 0.75$  mg ml<sup>-1</sup> (see Fig 1d).

### Kinetic simulations suggest a structural transition

To investigate the effects of such a structural transition on the kinetics of amyloid fibril formation and on the resulting fibril length distributions, we performed stochastic simulations of a fragmentation-dominated model of fibril growth. We first simulated a model with fragmentation and elongation only. The kinetic parameters used in the simulations were obtained by fitting our experimental data at low protein concentrations to analytical results derived by Knowles *et al.*<sup>25</sup> This resulted in fibril elongation and fragmentation rates of  $5 \times 10^4$  M<sup>-1</sup>s<sup>-1</sup> and  $3 \times 10^{-8}$ s<sup>-1</sup>, respectively (for details see Methods) and these parameters were used to generate predicted kinetic curves for a range of protein concentrations. These results were compared with our experimental data in which we normalized the growth curves to their maximal values (to decouple the growth rate measurements from the change in maximal fluorescence) and extracted the maximal growth rate,  $k_{gr}$  (Fig. 1c). For low protein concentrations we find that the values of  $k_{gr}$  predicted by our simulations are in good agreement with our experiments. For protein concentrations above 0.75 mg ml<sup>-1</sup>, however, our simulations of the fragmentation-dominated model fail to match our experimental results (blue curve in Fig. 1c). To test our hypothesis that a structural transition is involved we modified our simulations so that fragmentation is arrested when the total fibril mass concentration exceeds a critical value (the CFC). Using a value for the CFC of 0.4 mg ml<sup>-1</sup> our simulations with fragmentation arrest reproduce our experimental results for  $k_{gr}$  very well over the entire protein concentration range. The

protein concentration  $c_T$  at which the effects of the structural transition become apparent in our simulations is also in good agreement with our experimental results:  $c_T \approx 0.75 \text{ mg ml}^{-1}$ .

Indeed, we would expect that the CFC  $\approx \frac{c_T}{2}$ , since for the structural transition to have any effect on the maximal growth rate  $k_{gr}$ , it must happen before the maximal growth rate is reached, which occurs when at most half the total protein has aggregated. Fig. 1a shows the simulated lag times as a function of protein concentration for comparison with experiment; our simulations incorporating the CFC give a scaling exponent of  $-0.42 \pm 0.001$ , in reasonable agreement with the experimental results. It should be noted that the precise nature of the cut-off that suppresses fragmentation in our simulations has little effect on these results (Supplementary Fig. S5).

### Experimental length distributions match predictions

Our simulations further predict, in the long time limit, qualitatively distinct fibril length distributions for initial protein concentrations above and below the critical threshold  $c_T$ . For initial protein concentrations less than  $c_T$ , fibrils continue to fragment throughout the simulation, and in the long-time limit our simulations predict that the fibril length distribution will be exponential and dominated by short fibrils (Fig. 2a). In contrast, when the initial protein concentration is greater than  $c_T$ , the mass concentration of fibrils exceeds the CFC at some time during the exponential growth phase so that fragmentation ceases. At timepoints after the CFC is reached, the fibrils still grow by monomer addition but the shape of the length distribution is fixed. This results in a log-normal fibril length distribution with a clear peak even at long times (Fig. 2c), in agreement with published experimental observations<sup>30-32</sup>. Supplementary Figs. S6 and S7 show simulated length distributions for the two regimes ( $c_p < c_T$  and  $c_p > c_T$ ) at different times during the protein aggregation kinetics. We note that fragmentation-dominated models also predict peaked distributions, but only at very early times (Supplementary Fig. S6); in our model incorporating the CFC, fragmentation arrest causes these to persist.

To test these predictions we used transmission electron microscopy (TEM) to obtain length distributions for amyloid fibrils formed at initial protein concentrations above and below our predicted  $c_T$  of  $0.75 \text{ mg ml}^{-1}$  (Figs. 2b,d; see Supplementary Fig. S8 for examples of TEM images). Our experimental results are in close correspondence with our simulation predictions: we observe an exponential distribution of fibril lengths when the protein concentration is below  $c_T$  and a peaked distribution, even at long times, for protein concentration above  $c_T$  (Figs. 2a,c). Other studies have also reported peaked fibril length distributions<sup>30-32</sup>. We hypothesize that a structural transition may also be operating in these systems, and that these experiments may have been carried out in the high protein concentration regime where  $c_p > c_T$ .

### Adding salt enhances fibril elongation and shifts the CFC

Our model further allows us to rationalize non-trivial changes in the kinetic curves when the environmental conditions are altered. It is well known that the addition of salt screens electrostatic charge, thereby decreasing the Debye length and influencing protein-protein interactions<sup>39</sup>. As a model environmental perturbation, we therefore repeated our kinetic experiments in the presence of increasing concentrations of NaCl.

Fig. 3a shows  $k_{gr}$  as a function of insulin concentration for a range of NaCl concentrations. It is clear that adding NaCl results in complicated and non-monotonic trends in the kinetics of fibril growth. In the absence of salt, our data are not dissimilar to those previously attributed to a catalytic conformational conversion at the growing end of the fibrils<sup>21,22</sup>; the addition of salt, however, results in qualitatively and significantly different behaviour. While

these trends are not readily captured by variation of the parameters in fragmentation-dominated models, our simulations in which a structural transition is included are in good agreement with the data if we make the simple assumption that salt affects both the elongation rate ( $k_+$  in Eq. 1) and the CFC, but not the fragmentation rate. Such a change in the CFC is supported by our experimental data; the transition in the ThT fluorescence (as a function of protein concentration) which we plot in Fig. 1b in the absence of salt, shifts to lower insulin concentrations as the NaCl concentration is increased (Supplementary Fig. S9). The results of our simulations are shown in Fig. 3b. Firstly, the increase in growth rates between 0 M and 0.1 M NaCl is consistent with a  $\sim 20$  fold enhancement of the fibril elongation rate to  $10^6 \text{ M}^{-1}\text{s}^{-1}$ . Secondly, we capture the complex, salt-dependent and non-monotonic trends of the growth rate with protein concentration in Fig. 3a by allowing the CFC to decrease with salt concentrations above 0.1M. It should be emphasized that the changes in the simulated curves at 0.25-0.5 M NaCl arise only from a change in the CFC; the elongation rate is held constant at  $10^6 \text{ M}^{-1}\text{s}^{-1}$ . We note that this elongation rate is subdiffusive, consistent with a requirement for some form of conformational change at the growing fibril end prior to the addition of each new monomer<sup>21,22,25</sup>. Further increasing the elongation rate does not account for the complex behaviour observed in Fig. 3a; the presence of a structural transition in the model is essential in order to explain the experimental data.

Our structural transition model also helps us to understand how the lag time,  $t_{\text{lag}}$ , varies with salt concentration. The results of both simulation and experiment (Figs. 3c,d) show that as the salt concentration increases, the lag time becomes more protein concentration-dependent. This makes sense since our simulations indicate that adding salt has the two-fold effect of increasing the elongation rate and shifting the CFC to lower values, so that at high salt concentrations  $t_{\text{lag}}$  is dominated by the concentration-dependent process of fibril elongation rather than the concentration-independent process of fragmentation.

### The model predicts effects of adding salt during assembly

If our model correctly represents the molecular mechanism of fibril assembly then it should be able to predict what happens when the conditions are changed *during* the process of fibril growth. In the absence of a structural transition, we would expect that adding salt at any time before the point of maximal growth is reached will have a dramatic effect on the kinetics of fibril assembly. This is because adding salt increases the fibril elongation rate, which plays a major role in determining the growth rate in fragmentation-dominated models. Plotting the growth rate as a function of the time salt is added, we would therefore expect to obtain results that follow the dashed line in Fig. 4. However, in a model with a structural transition, salt should not influence the kinetics if it is added after the structural transition has happened - i.e. after the fibril mass has exceeded the CFC. We would therefore expect to obtain the red line in Fig. 4. Indeed, this prediction is realized in our experiments. Based on our simulation results, we predict that the CFC for the 0.3M salt concentration used in these experiments is  $0.1 \text{ mg ml}^{-1}$ , and that the CFC should be reached at approximately 110 minutes. Indeed, we find that adding NaCl at any time before the predicted CFC is reached (i.e. before 110 minutes) results in a strong increase in  $k_{\text{gr}}$ , but after 110 minutes, adding salt has no effect - i.e. our experiments indeed follow the red line rather than the dashed line in Fig. 4.

### Prevalence of small molecular weight species

Small molecular weight species, including short fibrils, that are present during the assembly of amyloid fibrils are of particular interest because they are thought to be the causative agents of toxicity<sup>40-43</sup>. Our model makes a strong prediction that the prevalence of short fibrils should be very different for protein concentrations above and below the critical threshold. Figs. 5a,b shows the prevalence of short fibril species in our simulations as a

function of time. For  $c_p > c_T$  we predict the transient formation of a small population of short fibrils, peaking approximately half-way through the growth phase before returning to low levels (Fig. 5b). When  $c_p < c_T$ , however, the number of short fibrils is predicted to be much greater and increasing with time (Fig. 5a). Thus the structural transition has a dramatic influence on the prevalence of potentially cytotoxic species during amyloid fibril assembly.

## DISCUSSION

The key finding in this study is the identification of a critical fibril mass concentration above which insulin amyloid fibrils undergo a structural transition that suppresses fragmentation. Using a very simple model that includes this feature we are able to successfully simulate the complex behaviour that we observe in our kinetic experiments under a variety of solution conditions. Indeed, the shapes of the length distributions we found from simulation and TEM experiments for fibrils formed above the critical concentration are similar to those found in previous experiments<sup>30-32</sup> while both simulations and our TEM experiments show very different, exponential-like length distributions at protein concentrations below the predicted structural transition.

It has become the general consensus that small oligomeric aggregates are the causative agents of cytotoxicity<sup>40-44</sup> while the mature, long fibrils are the inert end product of assembly<sup>45,46</sup>. Importantly, Xue and co-workers have demonstrated that it is not just the oligomers formed during self-assembly that are toxic, but that short fibrils generated through the fragmentation of mature fibrils also cause cell death<sup>47</sup>. Intriguingly, multiple studies have shown that there is no direct correlation between fibril load within tissue (i.e. mass of long fibrillar material) and loss of function<sup>45,46,48-53</sup>. Indeed, it has been shown that a significant fraction of members of the Nun study<sup>54</sup> possessed neuritic  $\alpha$ -amyloid plaques and neurofibrillary tangles at the time of death without exhibiting any cognitive dysfunction. The observation that in some cases fibrils can be present but not cause measurable functional impairment could be due to amyloid fibril assembly pathways that favour the rapid formation of longer inert fibrils as a result of the local intracellular environment. Our observation of two distinct length distributions that are determined only by the environmental conditions, one of which is comprised of long, potentially inert fibrils microns in length while the other is dominated by very short, possibly toxic, fibrillar species, may have consequences for determining the propensity of intracellular conditions to bias toward either benign or cytotoxic fibrillar loads.

To this end, we have shown that salt concentration has a strong impact on the value of the critical fibril mass concentration. Higher salt concentrations shift the CFC to lower values, stabilizing the length distribution for lower initial concentrations of protein. In our study we chose salt as a tool to alter protein-protein and fibril-fibril interactions, but any additive or solution condition that can affect the charge characteristics or protein structure, such as pH, temperature, or the presence of hydrophobic surfaces, could affect the value of CFC. This could have far-reaching consequences for toxicity in intracellular environments, where salt gradients, pH differences, the presence of chaperones and other co-factors could bias toward the formation of toxic or non-toxic fibrillar species.

Interestingly, Taylor *et al.* map the level of A $\beta$  (1-40) cytotoxicity to the kinetic profile of fibril formation<sup>55</sup>, reporting a peak in cytotoxicity during the exponential growth phase of assembly. After this peak is reached, cytotoxicity decays back to baseline levels at the point in the kinetic profile where fibril assembly approaches and reaches the final plateau. The results of Taylor *et al.* may be interpreted in the context of our structural transition model: a population of small molecular weight species is generated through fragmentation, and then depleted by the combined influence of fragmentation inhibition due to a structural transition

and fibril elongation. Applying our model to the data presented in<sup>55</sup> we would predict the CFC for A (1-40) to be approximately  $0.15 \text{ mg ml}^{-1}$  ( $\sim 35 \text{ }\mu\text{M}$ ). In our simulations at high protein concentrations, the presence of short, potentially cytotoxic oligomeric species shows very similar kinetics to the kinetics of cytotoxicity reported by Taylor *et al.* (Fig. 5b). For simulations in which the initial protein concentration is above  $c_T$  we find an analogous peak in small molecular weight species mid-way through the exponential growth phase which is followed by a decay back to baseline levels. In contrast, when the concentration of protein is below  $c_T$ , the residence time of small, potentially toxic species is significantly longer: indeed they remain present in high abundance even at very long times (Fig. 5a). This could have profound consequences for the propensity for cellular damage or death when intracellular conditions are such that short fibrils are the more likely species to be present. If this is indeed the case, then it may be possible to devise therapeutic measures that take advantage of these insights to alter cellular conditions so as to bias toward the accumulation of longer inert fibrils and away from the shorter toxic species.

Amyloid and amyloid-like fibrils have also received attention for their potential use biomaterials or components in composite materials<sup>13</sup>. For example, Reches and Gazit have used fibrils to template metal nanowires<sup>10</sup>, Channon *et al.*, has used them as the basis for light harvesting structures<sup>6</sup>, and a number of authors (e.g. Zhang<sup>7,8</sup> and Gras *et al.*<sup>56</sup>) have used them as the basis for cell scaffolds. A significant challenge remains in controlling the length distribution of fibres, and the viscoelasticity of the resulting hydrogel. Our current findings suggest mechanisms for manipulating both, and for predicting and controlling the homogeneity of the resulting population.

## METHODS

### Insulin Sample Preparation

Bovine insulin was obtained from Sigma-Aldrich (I5500, lot #0001434060). The zinc content was approximately 0.5 % (w/w). The samples in this study were dissolved in 25 mM HCl (pH 1.6) immediately prior to the experiment. All solvents and solutions were filtered through a  $0.22 \text{ }\mu\text{m}$  filter (Millipore). Concentrations were checked via UV-Vis absorption spectroscopy. ThT was added to each solution to a final concentration of  $20 \text{ }\mu\text{M}$ .

### ThT Fluorescence Kinetic Measurements

The ThT fluorescence measurements were conducted using a BMG Labtech Fluostar plate reader and Corning NBS 96-well plates (Corning 3641). Each well of the plate was filled with  $100 \text{ }\mu\text{L}$  of solution. Experiments for each protein concentration were replicated across 2-3 whole plates. The plates were incubated at  $60^\circ \text{C}$  and fluorescence readings were taken from the bottom of the plate at wavelengths of  $450 \text{ nm}$  for excitation and  $485 \text{ nm}$  for emission. Readings were taken every 10 minutes. The final number of individual experiments for a given concentration ranged from 140-200.

### Transmission electron microscopy

Samples were deposited onto 400 mesh copper grids (Taab, Aldermaston, U.K.) coated with formvar and carbon. Insulin solutions were incubated at  $60^\circ \text{C}$  in eppendorf tubes. The  $4 \text{ mg ml}^{-1}$  sample was subsequently diluted 20 fold. Aliquots of  $3 \text{ }\mu\text{L}$  insulin fibrils were placed on the grids. After 5 minutes the grids were washed with  $10 \text{ }\mu\text{L}$  MilliQ water followed by an application  $4 \text{ }\mu\text{L}$  of 2% uranyl acetate (w/v). The uranyl acetate was left on the sample grid for 30 seconds. Excess water and stain were removed with filter paper and the grids were left to air-dry for 20 minutes. Imaging was performed using a Philips (FEI) CM120 Biotwin transmission electron microscope with an operating voltage of  $-80 \text{ kV}$ . Fibrils lengths were determined using ImageJ image analysis software.

## CD spectroscopy

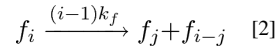
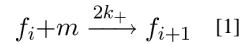
Readings were taken using a Jasco J-810 spectropolarimeter. Samples were prepared in microwell plates as described above and then transferred to a quartz cuvette with a path length of 0.1mm. Spectra were obtained by averaging over 5 accumulations. A bandwidth of 1nm and sensitivity of 100mdeg was used in all experiments.

## Bead tracking microscopy

Insulin samples were incubated at 60° C and the resulting fibril solution were placed on a glass slides. 1µm beads latex beads were added and the slides sealed with a glass cover slip and petroleum jelly. Images were captured using a Nikon Ti-U inverted microscope, 40× ELWD objective and a Mikrotron EoSens CCD camera with a capture rate of 100 fps. Subsequent images were analyzed using standard particle tracking software in IDL <sup>57</sup>.

## Stochastic simulations

Our simulations utilized the Gillespie algorithm <sup>58</sup>. Our simulation model consists of the following set of chemical reactions:



Here,  $f_i$  denotes a fibril of length  $i$  and  $m$  denotes a protein monomer. We assume that the shortest possible fibril length is 2 monomer units (i.e. the “nucleus size” is 2). Reaction (1) represents elongation by monomer addition, with rate constant  $k_+$  (the factor of 2 arises from the fact that monomers can be added at either end of a fibril). Reaction (2) represents fragmentation of a fibril into two shorter fibrils:  $k_f$  is the fragmentation rate, which we assume to be independent of the position along the fibril at which fragmentation happens. Note that this reaction also incorporates monomer loss from the fibril ends (here  $f_1 = m$ ).

In our simulations, we track explicitly the growth and fragmentation of individual fibrils. For reasons of computational speed, we used a system volume of 0.83 pL. We find that our simulations best fit our experimental data (in particular for the scaling of lag time with protein concentration) if they were started with a single dimer. Each simulation data point shown represents the average of 150 replicate runs, each comprising  $10^5$  s of simulated time. The values of  $k_+$  and  $k_f$  were obtained by fitting our experimental data, in the low concentration regime  $c_p \ll c_T$ , to the analytical result for a simple fragmentation model,

presented by Knowles *et al.* This provides the composite parameter  $\kappa = \sqrt{2m_{\text{tot}}k_+k_f}$  from which we choose elongation and fragmentation rates, setting the fragmentation rate in accordance with our previous findings <sup>59</sup> ( $k_+ = 5 \times 10^4 \text{ M}^{-1}\text{s}^{-1}$ ;  $k_f = 3 \times 10^{-8}\text{s}^{-1}$ ). Within the constraint set by  $\kappa$ , the precise choice of  $k_+$  and  $k_f$  influences the average fibril length at long times, but does not significantly affect our predictions for the growth kinetics. Fitting to the data from experiments performed with the lowest salt concentration (0.1M NaCl) yields  $k_+ = 10^6 \text{ M}^{-1}\text{s}^{-1}$  and  $k_f = 3 \times 10^{-8}\text{s}^{-1}$ .

For simulations which include the structural transition, the fragmentation rate  $k_f$  is switched

to zero when the fibril mass concentration  $F = \sum_i i f_i$  exceeds the CFC. We also investigated the effect of implementing a softer transition. Here, we instead scale the fragmentation rate by a factor  $y = (1/2)[1 - \tanh(A(F - \text{CFC}))]$ , where the coefficient  $A$  controls the sharpness of the transition; this corresponds to the hard cut-off when  $A \rightarrow \infty$ . This softening of the



cut-off does not result in significant changes to the kinetics. For more details see Supplementary Fig. S5.

## Supplementary Material

Refer to Web version on PubMed Central for supplementary material.

## Acknowledgments

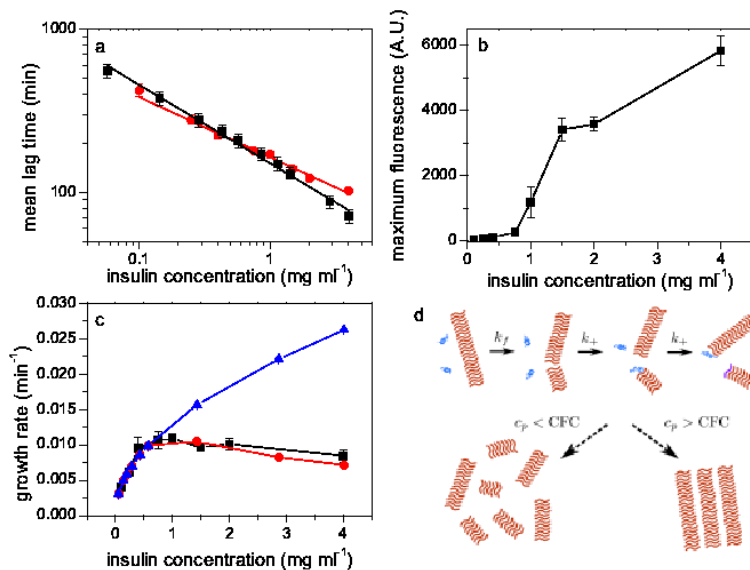
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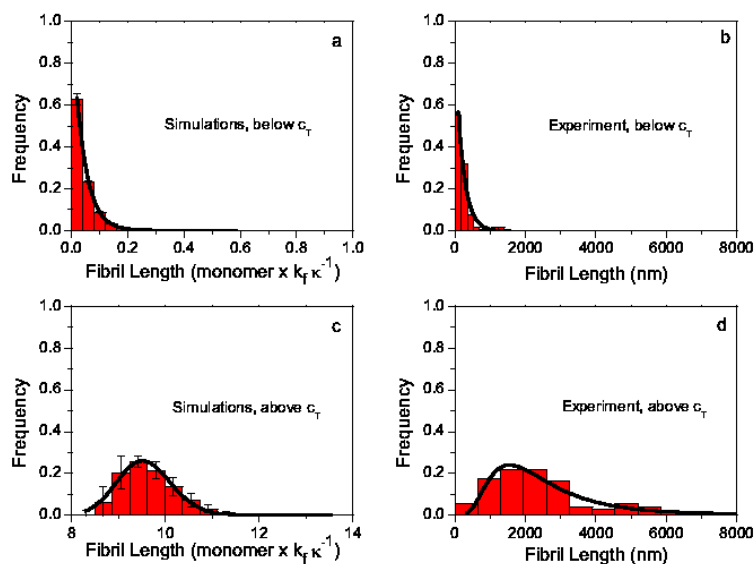
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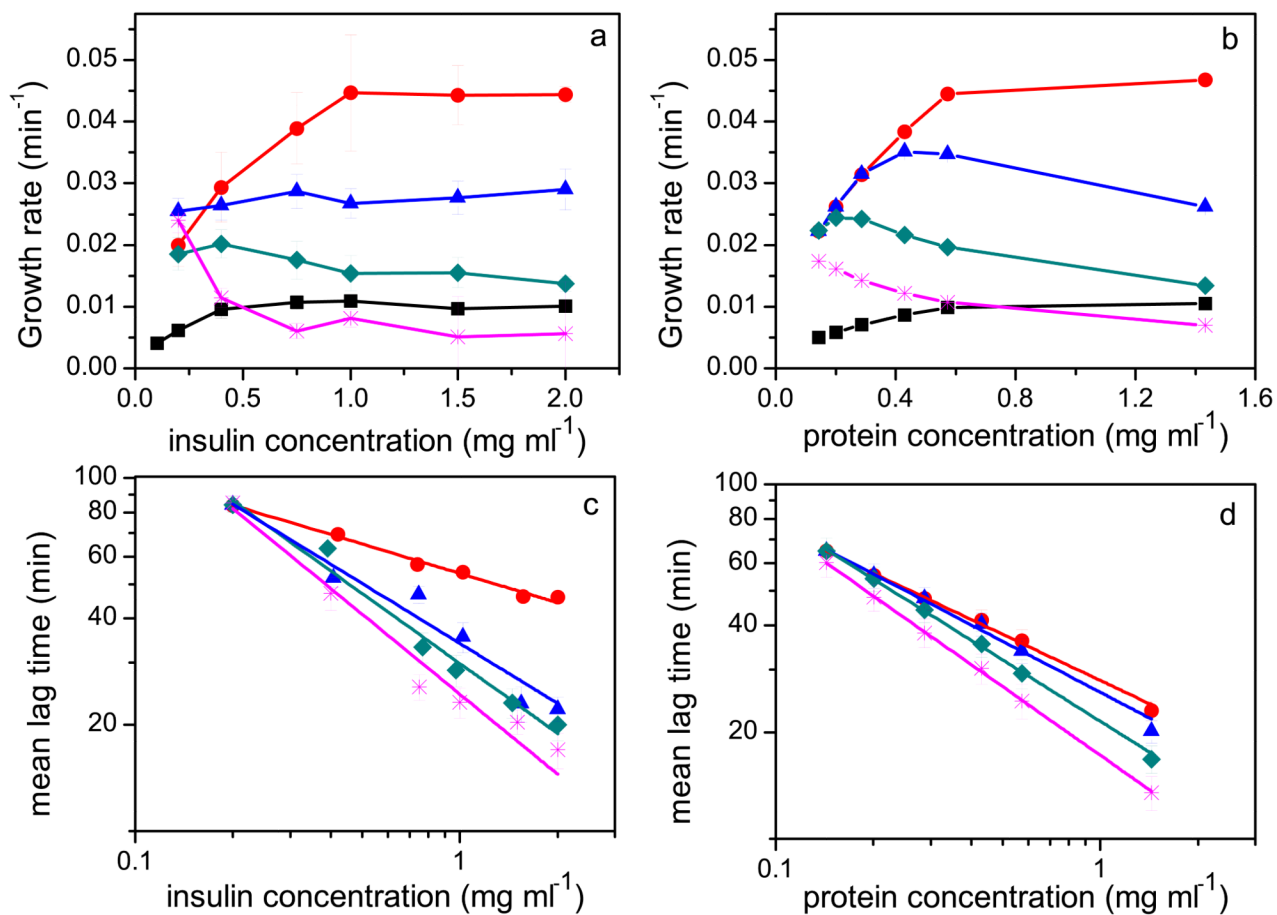
**Figure 1. A fragmentation model incorporating a structural transition fits kinetic data for insulin fibril assembly**

(a) Lag time as a function of protein concentration. The experimental data (squares) are fitted to the function  $y = Ax^x$  with an exponent  $x = -0.37 \pm 0.02$ . The simulation data (circles) have exponent  $x = -0.42 \pm 0.001$ ,  $k_+ = 5 \times 10^4 \text{ M}^{-1} \text{ s}^{-1}$  and  $k_f = 3 \times 10^{-8} \text{ s}^{-1}$ . (b) Mean maximal ThT fluorescence as a function of insulin concentration. (c) Growth rate,  $k_{gr}$ , is plotted as a function of insulin concentration. The experimental data (squares) were obtained from kinetic curves normalized to the fluorescence maxima. The simulation data were obtained from 150 simulations per concentration using a simple fragmentation-dominated model (triangles), including suppression of fragmentation once the fibril mass reaches a CFC of  $0.4 \text{ mg ml}^{-1}$  (circles). All data points show mean  $\pm$  s.d. (d) In our model, fibrils grow via two processes: fragmentation, and elongation via monomer addition. These processes are characterised by their respective rates  $k_f$  and  $k_+$ . Our model predicts distinct fibril length distributions for protein concentrations,  $c_p$  greater or less than  $c_T \approx 2CFC$ .



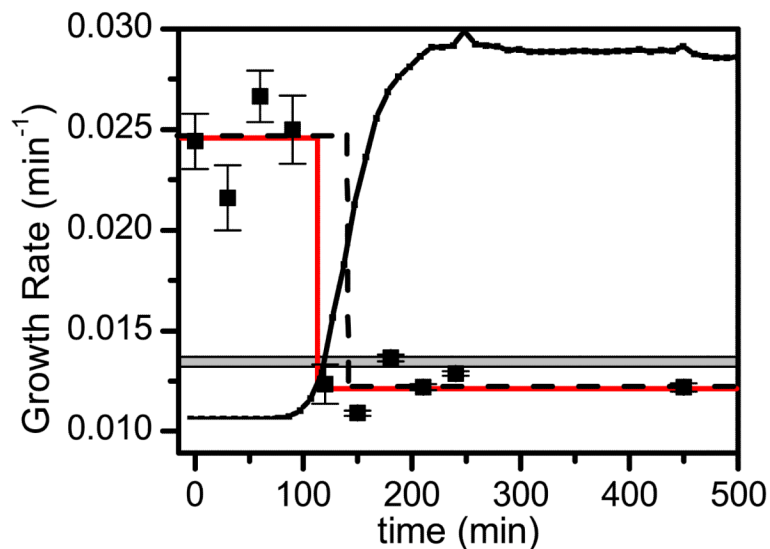
**Figure 2. Length distributions obtained from simulation and experiment**

Fibril length distributions obtained by simulation (**a**) below  $c_T$  ( $0.2 \text{ mg ml}^{-1}$ ) and (**c**) above  $c_T$  ( $4 \text{ mg ml}^{-1}$ ). We express the fibril length in terms of the composite parameter  $\kappa/k_f$ . Our simulations do not make absolute predictions of fibril length because the choice of values of  $k_+$  and  $k_f$  is not strongly constrained (see methods), whereas the shape of the length distribution (plotted as a function of monomer units  $\times k_f/\kappa$ ) is independent of this choice. The length distribution in (**a**) is best described by an exponential distribution; (**c**) is well-fitted by a log-normal distribution (black fit lines). Fibril length distributions extracted from TEM, (**b**) below  $c_T$  ( $0.2 \text{ mg ml}^{-1}$ ,  $N=75$ , bars) and (**d**) above  $c_T$  ( $4 \text{ mg ml}^{-1}$ ,  $N=159$ , bars). As predicted by the model, fibrils formed at protein concentrations below the CFC are significantly shorter (mean length of  $231.5 \pm 230.4 \text{ nm}$ ) and the distribution is exponential (black curve). Length distributions above  $c_T$  show a log-normal distribution (black curve) with a mean fibril length of  $2441.5 \pm 1590.3 \text{ nm}$  (mean  $\pm$  s.d.).



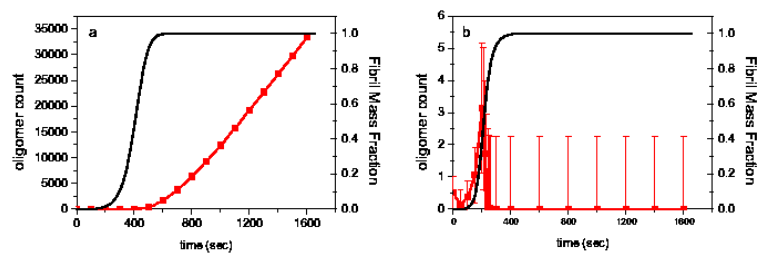
**Figure 3. A model incorporating a structural transition explains the effects of NaCl on aggregation kinetics**

(a) Experimental  $k_{gr}$  as a function of insulin concentration obtained from normalized traces at NaCl concentrations of 0M (black squares), 0.1M (red circles), 0.24M (blue triangles), 0.34M (dark cyan diamonds), and 0.49M (pink stars). (b) Simulated data obtained by varying the elongation rate and the threshold for fragmentation cut-off. Parameters used in the simulations were CFC = 0.4 mg ml<sup>-1</sup>,  $k = 5 \times 10^4$  M<sup>-1</sup>s<sup>-1</sup> (squares); CFC = 0.4 mg ml<sup>-1</sup>,  $k_+ = 10^6$  M<sup>-1</sup>s<sup>-1</sup> (circles); CFC = 0.2 mg ml<sup>-1</sup>,  $k_+ = 10^6$  M<sup>-1</sup>s<sup>-1</sup> (triangles); CFC = 0.1 mg ml<sup>-1</sup>,  $k_+ = 10^6$  M<sup>-1</sup>s<sup>-1</sup> (diamonds); and CFC = 0.05 mg ml<sup>-1</sup>,  $k_+ = 10^6$  M<sup>-1</sup>s<sup>-1</sup> (stars). For all simulations  $k_f = 3 \times 10^{-8}$  s<sup>-1</sup>. (c)  $t_{lag}$  as a function of insulin concentration. The data are fit with same function as Fig. 1(a) resulting in scaling exponents of  $-0.27 \pm 0.01$  (0.1M NaCl, circles),  $-0.56 \pm 0.05$  (0.24M NaCl, triangles),  $-0.65 \pm 0.04$  (0.34M NaCl, diamonds),  $-0.75 \pm 0.06$  (0.49M NaCl, stars). (d)  $t_{lag}$  as a function of protein concentration obtained from simulations employing  $k_+ = 10^6$  M<sup>-1</sup>s<sup>-1</sup> and  $k_f = 3 \times 10^{-8}$  s<sup>-1</sup>. The scaling exponents are  $-0.43 \pm 0.01$  (circles)  $-0.47 \pm 0.02$  (triangles),  $-0.57 \pm 0.01$  (diamonds), and  $-0.64 \pm 0.01$  (stars) when the CFC is 0.4 mg ml<sup>-1</sup>, 0.2 mg ml<sup>-1</sup>, 0.1 mg ml<sup>-1</sup> and 0.05 mg ml<sup>-1</sup>, respectively. Experimental and simulation data points show mean  $\pm$  s.d.



**Figure 4. The influence of environment on the growth kinetics**

A series of  $1.5 \text{ mg ml}^{-1}$  insulin samples were incubated simultaneously. At specific time points during the kinetics of self-assembly (every 30 minutes), NaCl was added to three samples. The mean value of  $k_{\text{gr}}$  from the resulting kinetic traces of each group of samples is plotted against the time at which the NaCl was added (squares). To illustrate where on the kinetic profile the NaCl was added, the kinetic trace for the control is also shown (triangles). The grey box corresponds to the mean  $k_{\text{gr}} \pm \text{s.d.}$  for this salt-free control. In the absence of any structural transition, we would expect to observe the behaviour shown by the dashed line, with enhanced growth rates during the early stages of fibril assembly, returning to control values if salt is added after the point at which  $k_{\text{gr}}$  is measured ( $\sim 160$  min). With the existence of a CFC, we would expect instead the trend in  $k_{\text{gr}}$  as shown by the solid line; the decrease in  $k_{\text{gr}}$  now occurs the moment the CFC is reached. Indeed, we observe that  $k_{\text{gr}}$  decreases to the control value when salt is added at any time after 120 minutes, consistent with the sample having reached the CFC, which for  $1.5 \text{ mg ml}^{-1}$  insulin under these conditions we estimate to occur at 110 minutes.



**Figure 5. Oligomer populations as a function of time**

The number of short fibrils, of 100 monomer units, plotted as a function of time (red squares); kinetic traces of the total fibril mass (normalized, right axes) are also shown (black lines). **(a)** At  $c_p = 0.2 \text{ mg ml}^{-1}$ , the protein concentration is below  $c_T$  and a large number of short fibrillar species persist for long periods of time. **(b)** At  $c_p = 0.85 \text{ mg ml}^{-1}$ , a maximum in short species occurs at a time approximately coincident with the CFC being reached. Once the CFC is reached and the structural transition takes place, this population diminishes due to the suppression of fragmentation. Experimental and simulation data points show  $\text{mean} \pm \text{s.d.}$