

ORIGINAL RESEARCH

Modeling the Progression of Cardiac Catecholamine Deficiency in Lewy Body Diseases

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BACKGROUND: Lewy body diseases (LBDs) feature deficiency of the sympathetic neurotransmitter norepinephrine in the left ventricular myocardium and sympathetic intra-neuronal deposition of the protein alpha-synuclein (α S). LBDs therefore are autonomic synucleinopathies. Computational modeling has revealed multiple functional abnormalities in residual myocardial sympathetic noradrenergic nerves in LBDs, including decreased norepinephrine synthesis, vesicular storage, and recycling. We report an extended model that enables predictions about the progression of LBDs and effects of genetic predispositions and treatments on that progression.

METHODS AND RESULTS: The model combines cardiac sympathetic activation with autotoxicity mediated by the dopamine metabolite 3,4-dihydroxyphenylacetaldehyde. We tested the model by its ability to predict longitudinal empirical data based on cardiac sympathetic neuroimaging, effects of genetic variations related to particular intra-neuronal reactions, treatment by monoamine oxidase inhibition to decrease 3,4-dihydroxyphenylacetaldehyde production, and post-mortem myocardial tissue contents of catecholamines and α S. The new model generated a triphasic decline in myocardial norepinephrine content. This pattern was confirmed by empirical data from serial cardiac ^{18}F -dopamine positron emission tomographic scanning in patients with LBDs. The model also correctly predicted empirical data about effects of genetic variants and monoamine oxidase inhibition and about myocardial levels of catecholamines and α S.

CONCLUSIONS: The present computational model predicts a triphasic decline in myocardial norepinephrine content as LBDs progress. According to the model, disease-modifying interventions begun at the transition from the first to the second phase delay the onset of symptomatic disease. Computational modeling coupled with biomarkers of preclinical autonomic synucleinopathy may enable early detection and more effective treatment of LBDs.

Key Words: catecholaldehyde ■ catecholamine ■ computational modeling ■ DOPAL, Lewy body ■ norepinephrine ■ sympathetic nervous system

Lewy body diseases (LBDs) are a family of aging-related neurodegenerative disorders that have in common the occurrence of Lewy bodies (LBs), cytoplasmic inclusions found in particular types of brainstem neurons. LBs contain the protein alpha-synuclein (α S),¹ and LBDs are in a family of diseases termed synucleinopathies. In LBDs α S deposition occurs both in neuronal cell bodies and in nerve fibers (Lewy neurites).

LBDs Entail Catecholamine Deficiencies in the Brain and Heart

LBDs are also characterized by deficiencies of the catecholamines norepinephrine and dopamine. Dopamine depletion in the nigrostriatal system, especially in the putamen,² causes the movement disorder that defines the most well-known LBD, Parkinson disease (PD).

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CLINICAL PERSPECTIVE

What Is New?

- We present a computational model to predict the progression of cardiac norepinephrine deficiency in Lewy body diseases and effects of genetic predispositions and treatments on that progression; the model applies the concepts of homeostasis/allostasis and of catecholamine autotoxicity mediated by the catecholaldehyde 3,4-dihydroxyphenylacetaldehyde in cardiac sympathetic nerves.
- The model predicts triphasic loss of myocardial norepinephrine stores (Phase 1=homeostasis, Phase 2=dyshomeostasis, Phase 3=symptomatic advanced disease).
- Attenuated 3,4-dihydroxyphenylacetaldehyde production via decreased monoamine oxidase activity results in later onset of symptomatic disease, while attenuated 3,4-dihydroxyphenylacetaldehyde metabolism via decreased aldehyde dehydrogenase activity results in earlier onset of symptomatic disease.

What Are the Clinical Implications?

- Treatment targeting 3,4-dihydroxyphenylacetaldehyde production and effects that is initiated in symptomatic disease produces only transient benefit, whereas the same treatment initiated at the transition from homeostasis to dyshomeostasis substantially delays the onset of symptomatic disease.
- The results reinforce the need to identify biomarkers of preclinical disease, to maximize efficacy of disease-modifying treatment.

Nonstandard Abbreviations and Acronyms

| | |
|----------------------------|---|
| ¹⁸F-DA | ¹⁸ F-dopamine |
| ¹⁸F-DOPA | ¹⁸ F-3,4-dihydroxyphenylalanine |
| ALDH | aldehyde dehydrogenase |
| cTnT | cardiac troponin T |
| DBH | dopamine-beta-hydroxylase |
| DHPG | 3,4-dihydroxyphenylglycol |
| DOPAC | 3,4-dihydroxyphenylacetic acid |
| DOPAL | 3,4-dihydroxyphenylacetaldehyde |
| DOPALc | cytoplasmic 3,4-dihydroxyphenylacetaldehyde |
| DOPEGAL | 3,4-dihydroxyphenylglycolaldehyde |
| kALDH | rate constant for aldehyde dehydrogenase |

| | |
|---------------------|--|
| kALDH_DOPALc | rate constant for aldehyde dehydrogenase acting on cytoplasmic 3,4-dihydroxyphenylacetaldehyde |
| kAR_DOPEGALc | rate constant for aldehyde/aldose reductase acting on cytoplasmic 3,4-dihydroxyphenylglycolaldehyde |
| kDBH | rate constant for dopamine-beta-hydroxylase |
| kDHPGc_Loss | rate constant for loss of cytoplasmic 3,4-dihydroxyphenylglycol |
| kDOPAc_Loss | rate constant for loss of cytoplasmic 3,4-dihydroxyphenylalanine |
| kDOPACc_Loss | rate constant for loss of cytoplasmic 3,4-dihydroxyphenylacetic acid |
| kLAAAD | rate constant for L-aromatic-amino-acid decarboxylase |
| kLeak_DA | rate constant for leakage of dopamine from vesicles into cytoplasm |
| kLeak_NE | rate constant for leakage of norepinephrine from vesicles into cytoplasm |
| kMAO_DA | rate constant for monoamine oxidase acting on cytoplasmic dopamine |
| kMAO_NE | rate constant for monoamine oxidase acting on cytoplasmic norepinephrine |
| kNE_Release | rate constant for release of vesicular norepinephrine |
| kNEe_Loss | rate constant for loss of extracellular fluid norepinephrine |
| kTH | rate constant for tyrosine hydroxylase |
| kTYR_Loss | rate constant for tyrosine loss |
| kTYR_Uptake | rate constant for tyrosine uptake |
| kU1 | rate constant for neuronal uptake via the cell membrane norepinephrine transporter |
| kVMAT_DA | rate constant for vesicular uptake of cytoplasmic dopamine mediated by the vesicular monoamine transporter |
| kVMAT_NE | rate constant for vesicular uptake of cytoplasmic norepinephrine mediated by the vesicular monoamine transporter |

| | |
|-----------------|--|
| LAAAD | L-aromatic-amino-acid decarboxylase |
| LBDs | Lewy body diseases |
| Log10_VR | log of vascular relaxation |
| MAO_DA | monoamine oxidase acting on cytoplasmic dopamine |
| mCi | milliCuries |
| nCi | nanoCuries |
| NEv | vesicular norepinephrine |
| PAF | pure autonomic failure |
| PD | Parkinson disease |
| PUT/OCC | putamen/occipital cortex ratio |
| SMA | alpha-smooth muscle actin |
| TH | tyrosine hydroxylase |
| VMAT2 | type 2 vesicular monoamine transporter |
| VR | vascular relaxation |
| αS | alpha-synuclein |

LBDs also feature profound cardiac catecholamine deficiency. This was first suspected by sympathetic neuroimaging demonstrating decreased left ventricular ¹⁸F-dopamine (¹⁸F-DA)-derived radioactivity by positron emission tomographic (PET) scanning in PD and the related LBD pure autonomic failure (PAF).³ Post-mortem analyses have documented drastically reduced (by ≥90%) myocardial norepinephrine content in patients with LBDs compared with control subjects.⁴

Denervation Combined With Functional Abnormalities in Residual Sympathetic Nerves Explains the Cardiac Catecholamine Deficiency Attending LBDs

What underlies cardiac catecholamine deficiency in LBDs? A seemingly straightforward answer would be loss of cardiac sympathetic nerve fibers that contain dopamine and norepinephrine —ie, denervation. The extent of myocardial catecholamine depletion, however, is greater than can be accounted for by denervation alone. The disparity suggests that dysfunctions in residual neurons contribute to the neurotransmitter deficiencies.

In confirmation of this suggestion, application of a computational modeling approach to account for the main known steps in synthesis, storage, release, reuptake, and metabolism of catecholamines in cardiac sympathetic nerves (Figure 1) has revealed multiple specific, functional intra-neuronal abnormalities in LBDs.⁵ These dysfunctions include decreased vesicular uptake of cytoplasmic catecholamines via the type 2 vesicular monoamine transporter (VMAT2); increased

passive leakage from storage vesicles into the cytoplasm; decreased activities of the enzymes tyrosine hydroxylase (TH) and L-aromatic amino acid decarboxylase (LAAAD), which are required for the synthesis of dopamine and norepinephrine; and decreased neuronal norepinephrine recycling via the Uptake-1 process mediated by the cell membrane norepinephrine transporter. In vivo and post-mortem studies of patients with LBD have reported evidence for all these abnormalities.^{6–8}

Modeling Disease Progression in LBDs

The published model⁵ does not deal with the progression from the healthy to the diseased state, nor the effects of particular genetic variants or treatments on that progression. In PD, longitudinal neuroimaging studies have indicated an inverse exponential curve for striatal dopamine deficiency, with a rapid early decline followed by a slow late decline.⁹ Based on this curvilinearity one would expect disease-modifying treatments to be more effective early than late in the disease.

During an even earlier phase, it seems likely that neurotransmitter stores are maintained within healthy narrow bounds (homeostasis). A key purpose of extending the original published model is to explore the transition from the relatively stable homeostatic phase (Phase 1) to the unstable phase (Phase 2) when there would be an escape from homeostasis (dyshomeostasis).

To explain this transition we invoked the “catecholaldehyde hypothesis.”¹⁰ The catecholaldehyde 3,4-dihydroxyphenylacetaldehyde (DOPAL), an obligate intermediate of dopamine metabolism, is produced continuously in the cytoplasm of catecholaminergic neurons (Figure 1). According to the catecholaldehyde hypothesis, DOPAL is an “autotoxin”¹¹ that can harm or destroy the neurons in which it is produced.¹² From the point of view of computational modeling as applied to processes in cardiac sympathetic nerves, an appealing aspect of the catecholaldehyde hypothesis is that DOPAL is known to interfere with key reactions in catecholaminergic cells, including TH,¹³ LAAAD,¹⁴ and trans-membrane catecholamine transport.¹⁵

How might DOPAL-induced autotoxicity be linked to αS deposition, which as noted above is a characteristic feature of LBDs? DOPAL potently oligomerizes, forms quinoprotein adducts with (quinonizes), and aggregates αS.¹⁴ DOPAL-induced αS oligomers in turn exert a variety of potentially harmful effects, including interference with vesicular⁷ and mitochondrial¹⁶ functions, which may precipitate rapid neurodegeneration.

Testing the Model

We tested the model by its ability to predict empirical data about the course of catecholamine

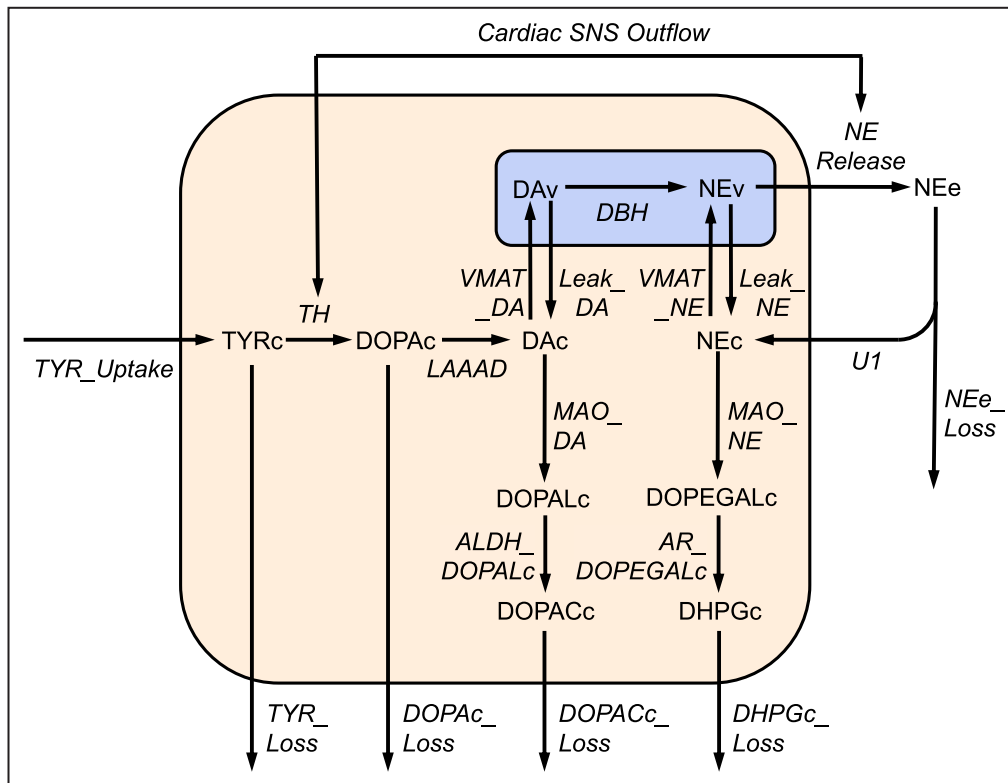


Figure 1. Pictorial representation of neuronal reactants and reactions in the computational model.

There are 11 reactants: (1) cytoplasmic tyrosine (TYRc), (2) cytoplasmic 3,4-dihydroxyphenylalanine (DOPAc), (3) cytoplasmic dopamine (DAc), (4) cytoplasmic 3,4-dihydroxyphenylacetic acid (DOPAcC), (5) vesicular dopamine (DAv), (6) vesicular norepinephrine (NEv), (7) extracellular fluid norepinephrine (NEe), (8) cytoplasmic norepinephrine (NEc), (9) cytoplasmic 3,4-dihydroxyphenylglycol (DHPGc), (10) cytoplasmic 3,4-dihydroxyphenylacetaldehyde (DOPALc), and (11) cytoplasmic 3,4-dihydroxyphenylglycolaldehyde (DOPEGALc). There are 19 reactions: (1) neuronal uptake of tyrosine (TYR_Uptake), (2) tyrosine loss from the neuron (TYR_Loss), (3) tyrosine hydroxylase (TH), (4) L-aromatic-amino-acid decarboxylase (LAAAD), (5) DOPA loss from the neuron (DOPAc_Loss), (6) vesicular leakage of vesicular dopamine (Leak_DA), (7) vesicular uptake of cytoplasmic dopamine (VMAT_DA), (8) monoamine oxidase acting on cytoplasmic dopamine (MAO_DA), (9) aldehyde dehydrogenase acting on DOPALc (ALDH_DOPALc), (10) DOPAc loss from the neuron (DOPAcC_Loss), (11) dopamine-beta-hydroxylase acting on vesicular dopamine (DBH), (12) vesicular uptake of cytoplasmic norepinephrine (VMAT_NE), (13) leakage of vesicular norepinephrine (Leak_NE), (14) exocytotic norepinephrine release (Norepinephrine Release), (15) neuronal uptake of extracellular fluid norepinephrine (U1), (16) loss of extracellular fluid norepinephrine (NEe_Loss), (17) monoamine oxidase acting on cytoplasmic norepinephrine (MAO_NE), (18) aldehyde/aldehyde reductase acting on cytoplasmic 3,4-dihydroxyphenylglycolaldehyde (AR_DOPEGALc), and (19) cytoplasmic 3,4-dihydroxyphenylglycol loss from the neuron (DHPGc_Loss). Homeostatic (reflexive) or allostatic (feed-forward) cardiac sympathetic noradrenergic system stimulation increases rate constant for release of vesicular norepinephrine (kNE_Release) and kTH.

deficiency in LBDs, effects of mutations of genes encoding enzymes or transporters in catecholaminergic neurons, results of preclinical and clinical testing of MAO inhibition, and post-mortem data about myocardial contents of catecholamines and α S in LBDs. These four aspects are described in more detail below.

Determining whether the model correctly predicts trends in norepinephrine stores requires a means to track myocardial norepinephrine content in living patients. For this we used cardiac sympathetic

neuroimaging data. Cardiac ^{18}F -DA-derived radioactivity measured by positron emission tomography is correlated with post-mortem myocardial norepinephrine content.¹⁷ Analogously, as an in vivo biomarker of nigrostriatal dopaminergic innervation we used the putamen/occipital cortex (PUT/OCC) ratio of ^{18}F -3,4-dihydroxyphenylalanine (^{18}F -DOPA)-derived radioactivity.¹⁸

We tested the model by its ability to predict alterations in disease onset or progression because of hypofunctional variations in the genes encoding TH, LAAAD, VMAT2, the cell membrane norepinephrine

transporter, aldehyde dehydrogenase (ALDH, the main enzyme that detoxifies DOPAL), and MAO.

Since MAO inhibition would be expected to decrease DOPAL production and attenuate catecholaminergic neurodegeneration, we reviewed data from clinical trials about effects of MAO inhibitors on the symptomatic progression of PD.^{19,20} We also explored whether combining MAO inhibition with treatment decreasing DOPAL effects would delay further the onset of symptomatic disease compared with MAO inhibition alone.

Finally, we examined whether predictions about α S buildup in sympathetic noradrenergic nerves fit with empirical post-mortem data about myocardial tissue contents of catecholamines and immunoreactive α S in the same specimens from patients with LBDs. With a view to extending to a potential in vivo biomarker, we also asked whether α S buildup in biopsiable scalp skin is associated with myocardial α S buildup and norepinephrine depletion in LBDs.

METHODS

The authors declare that all supporting data are available within the article online supplementary files.

Mathematical Underpinnings

The extended model is in the form of a system of 11 non-linear, parameterized, first-order ordinary differential equations that account for 25 reactions, including 19 intra-neuronal reactions (Figure 1, Tables S1 and S2). We investigated the model using the numerical continuation and bifurcation software `Cl_MatContL`^{21,22} (see Table S3 for code).

A stable equilibrium solution of this system accounts for a physiological state. A method for numerical investigation of such systems is numerical bifurcation analysis, which is based on continuation of solutions to well-defined operator equations. The equilibrium solutions are continued with respect to the input parameter, vascular relaxation (VR), which results in increased cardiac sympathetic outflow. A bifurcation signifies a sharp qualitative change in the solution when the continuation parameter changes only slightly. In the present model, an escape from or a breakdown of homeostasis occurs at the first Hopf bifurcation point, which results in a loss of stability and an onset of oscillations. Identifying such situations can mean acceleration of the disease process.

`Cl_MatCont` is the command line MATLAB package for studying smaller-size dynamical systems and their bifurcations. `Cl_MatContL`²² is an extension of `Cl_MatCont` to large-scale computations of bifurcations of equilibria via subspace reduction, based on the Continuation of Invariant Subspaces algorithm.²³ Key features of `Cl_MatContL` include Continuation of

Invariant Subspaces-based, continuous, well-scaled test functions for codimension 1 and 2 bifurcations, allowing accurate detection of bifurcations for large systems.

The models for the physiological processes under consideration are of the general form:

$$\dot{x}(t) = f(x(t), \alpha),$$

where $x(t)$ is the state and α contains the parameter(s). A system exhibits homeostasis if some output variable remains constant, or almost constant, when an input variable or parameter changes by a relatively large amount. An example in autonomic medicine is cerebral autoregulation, in which cerebral blood flow is kept within a narrow range across blood pressures (BP). When we consider homeostasis defined as the output parameter being constant across a range of input parameters (Figure S1), homeostasis is a bifurcation of infinite codimension that can only be detected under special circumstances. The state x_0 at the output node(s) typically is not completely independent of the input parameter(s) α . The dependence there is more like a cubic function that is approximately constant in a certain range. This motivates the study of homeostasis in a local (infinitesimal) setting. For current mathematical models of mechanisms of homeostasis, we refer the reader to an article by Golubitsky et al²⁴ and references there.

When there is only one parameter α , infinitesimal homeostasis is observed at a point $\alpha = \alpha_0$ when $x'_0(\alpha_0) = 0$. Higher-order homeostasis cases occur when higher derivatives of $x_0(\alpha)$ vanish in a point. When there are multiple input parameters, the derivatives of x_0 with respect to all considered parameters are required to be zero at a homeostasis point. The type of homeostasis point is then characterized by the higher-order derivatives at the homeostasis point.

An example of a homeostasis point in a biological network with two input parameters is shown in Figure S1C.²⁵ Here extracellular dopamine varies depending on the activities of TH and the cell membrane dopamine transporter. There are several different types of homeostatic points for two input parameters that are characterized by the higher-order derivatives of x_0 . A healthy state corresponds to a point on the infinitesimal homeostasis surface. The exact shape of the surface is determined by individual factors such as development, environmental exposures, psychological stress, drug effects, and aging.

The model of two-parameter homeostasis in Figure 2C does not incorporate progression from a healthy to a diseased condition. From our conceptual framework, when there is such progression, the value for the key dependent variable (in this case vesicular norepinephrine [NEv]) falls below the infinitesimal homeostasis surface.

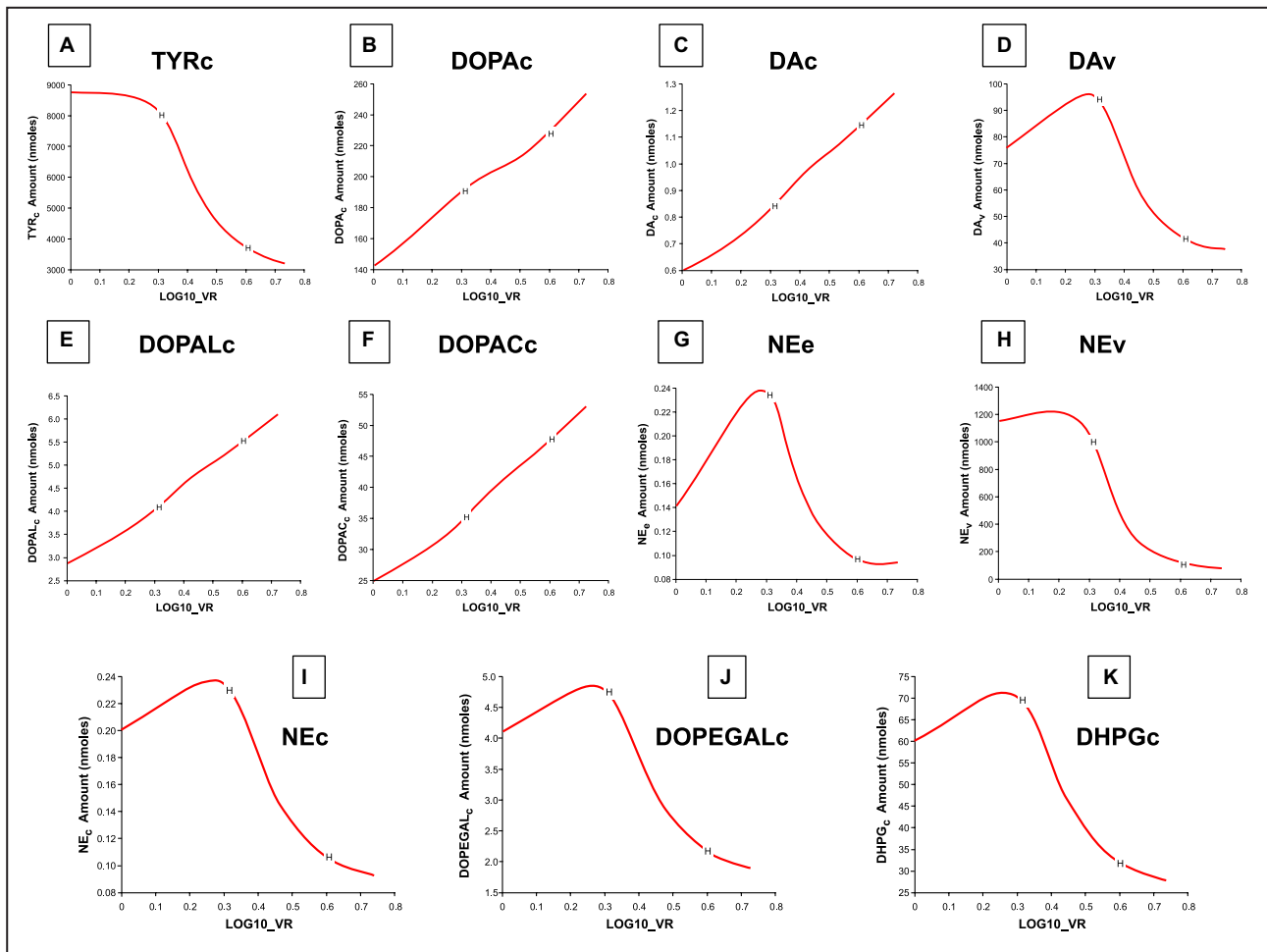


Figure 2. Model-predicted trends in amounts of reactants (nmoles).

The model predicts triphasic trends in cytoplasmic tyrosine, cytoplasmic norepinephrine, vesicular dopamine, vesicular norepinephrine, cytoplasmic norepinephrine, cytoplasmic 3,4-dihydroxyphenylglycolaldehyde, and cytoplasmic 3,4-dihydroxyphenylglycol and generally linear trends in cytoplasmic tyrosine, cytoplasmic dopamine, cytoplasmic 3,4-dihydroxyphenylacetaldehyde, and cytoplasmic 3,4-dihydroxyphenylacetic acid. H symbols correspond to Hopf bifurcations. DAc indicates cytoplasmic dopamine; DAv, vesicular dopamine; DHPGc, cytoplasmic 3,4-dihydroxyphenylglycol; DOPAc, cytoplasmic 3,4-dihydroxyphenylalanine; DOPACc, cytoplasmic 3,4-dihydroxyphenylacetic acid; DOPALc, cytoplasmic 3,4-dihydroxyphenylacetaldehyde; DOPEGALc, cytoplasmic 3,4-dihydroxyphenylglycolaldehyde; LOG10_VR, log of vascular relaxation; NEc, cytoplasmic norepinephrine; NEe, extracellular fluid norepinephrine; NEv, vesicular norepinephrine; and TYRc, cytoplasmic tyrosine.

Effects of Cardiac Sympathetic Activation

The model examined the consequences of chronic cardiac sympathetic activation, either as a compensatory homeostatic response to systemic vasodilation or an anticipatory allostatic adjustment.²⁶ In principle, both would exert the same intra-neuronal effects; however, there are abundant empirical data about the effects of reflexive sympathetic stimulation.

Increased Rate Constant for NE Release

Administration of a drug that produces VR reflexively increases sympathetic noradrenergic outflows. By decreasing BP, VR releases sympathetic noradrenergic system outflows from baroreflexive restraint.

Sympathetic noradrenergic system outflows to the heart and other organs increase. In the model, the reflexive increase in sympathetic noradrenergic system outflow increases the rate constant for NE release ($k_{NE_Release}$) (Figure 1). This augments delivery of norepinephrine to the extracellular fluid and adrenoceptors, producing a vasoconstrictor effect that attenuates or eliminates the drug-evoked vasodilation. The reflexive increases in sympathetic noradrenergic system outflows to the heart and other organs maintain BP at or close to the baseline level.

Empirical data about effects of VR on BP were obtained from a study of infusion of nitroprusside on BP in the setting of trimethaphan-induced ganglion blockade.²⁷ Ganglion blockade eliminates baroreflexive

stimulation of sympathetic noradrenergic outflows. BP then falls approximately linearly as a function of the log of the nitroprusside infusion rate. In the model, the systolic BP is related to the log of vascular relaxation (Log10_VR).

With intact baroreflexes, when BP falls because of vascular relaxation sympathetic noradrenergic outflows increase reflexively. In humans, intravenous nitroprusside infusion increases cardiac sympathetic outflow as indicated by the rate of entry of norepinephrine into the cardiac venous drainage.²⁸ As a result of the reflexively increased sympathetic outflows, for a given rate of nitroprusside infusion the decrease in BP is attenuated.

One may presume that extracellular fluid norepinephrine (NE_e) is directly related to kNE_Release if the pool of NE_v is maintained. The concentration of norepinephrine at the neuroeffector junctions can be estimated from the plasma norepinephrine concentration during systemic norepinephrine infusion and during manipulations altering exocytotic norepinephrine release.²⁹

Increased Rate Constant for TH

Sympathetic stimulation and exposure to stressors that increase sympathetic outflows do not normally decrease cardiac tissue norepinephrine concentrations. This is because of concurrently increased activity of TH, the rate-limiting enzyme in norepinephrine synthesis. Thus, when new synthesis of norepinephrine is prevented by alpha-methyl-para-tyrosine, which blocks TH, manipulations increasing cardiac sympathetic outflow decrease myocardial norepinephrine stores.³⁰ In the model, sympathetic stimulation increases the rate constant for TH (kTH), which maintains NE_v despite increased kNE_Release.

Cardiac exocytotic norepinephrine release can increase by many-fold during severe stresses; however, TH activity increases by only at most 2- to 3-fold. In exercising healthy humans, cardiac norepinephrine spillover averages almost 18 times baseline, whereas in the same subjects cardiac DOPA spillover, an index of TH activity, averages 2.4 times baseline.³¹

Autotoxicity from Catecholaldehyde Buildup

Increased TH activity augments the production of dopamine in the neuronal cytoplasm, and this increases cytoplasmic DOPAL (DOPAL_c) production via oxidative deamination catalyzed by monoamine oxidase (increased kMAO_DA; Figure 1). Thus, mice that over-express TH have increased striatal tissue DOPAL content.³² Incubation of catecholaminergic rat pheochromocytoma PC12 cells with DOPA, the immediate precursor of dopamine, also increases endogenous DOPAL production.³³

DOPAL inhibits TH¹³ and LAAAD¹⁴ and decreases synaptosomal dopamine uptake.¹² In the model DOPAL_c was presumed to exert equal inhibitory effects on kTH, the rate constant for LAAAD (kLAAAD), the rate constant vesicular uptake of cytoplasmic dopamine via the vesicular monoamine transporter (kVMAT_DA), and the rate constant for vesicular uptake of cytoplasmic norepinephrine mediated by the vesicular monoamine transporter (kVMAT_NE), while increasing the rate constants for vesicular leakage (kLeak) of dopamine (kLeak_DA) and of norepinephrine (kLeak_NE) (Figure S2).

Among the many proteins modified by DOPAL, one is αS. DOPAL potently oligomerizes αS,^{14,34} and αS oligomers may be the toxic form of the protein, although this matter is unsettled. DOPAL-induced αS oligomers interfere with synaptic vesicular⁷ and mitochondrial¹⁶ functions. Vesicle permeabilization by αS oligomers⁷ would increase values for kLeak in the model (Figure 1). Because of the absence of literature about the relative contributions of DOPAL, αS, and DOPAL-αS interactions to autotoxicity, the model lumps these 3 factors.

The model incorporates the catecholaldehyde 3,4-dihydroxyphenylglycolaldehyde (DOPEGAL), produced by the action of MAO on cytoplasmic norepinephrine (Figure 1); however, since there are no empirical data about DOPEGAL-induced toxicity or DOPEGAL-αS interactions in catecholaminergic neurons, the model does not include effects of DOPEGAL.

With reference to the homeostatic surface in Figure 2C, accumulation of DOPAL_c or of DOPAL_c-modified αS shrinks the homeostatic surface. When the homeostatic surface has shrunk sufficiently, the white disks “fall” from it.

To estimate the amount of DOPAL in the neuronal cytoplasm (DOPAL_c) we used empirical data about putamen tissue concentrations of DOPAL and 3,4-dihydroxyphenylacetic acid (DOPAC) (in nmol/g wet weight).^{35,36} In control subjects, putamen DOPAL=0.316 nmol/g and DOPAC=2.687 nmol/g, so that the DOPAC/DOPAL concentration ratio=8.498. Assuming the same DOPAC/DOPAL ratio obtains in myocardial sympathetic nerves, for a cytoplasmic DOPAC amount of 25 nmoles, DOPAL_c=25/8.498=2.9 nmoles. Presuming ALDH is the sole route of metabolism of DOPAL, the DOPAC production rate=the DOPAL production rate=0.18 nmol/min.

In myocardium the rate of loss of 3,4-dihydroxyphenylglycol (DHPG) from the tissue is 1.2 nmol/min, which means the rate of metabolism of DOPEGAL to DHPG by aldehyde/aldose reductase is 1.2 nmol/min. Based on our unpublished observations from concurrent measurements of DOPEGAL and DHPG in sympathetic ganglion tissue from 3 control subjects, tissue DOPEGAL is about 7% of tissue DHPG.

The model includes progressive sympathetic noradrenergic denervation in LBDs, under the presumption that a loss of cardiac sympathetic nerves in LBDs is a result of a buildup of DOPAL. Our preliminary empirical data from patients with LBD indicate that by 16 years from symptom onset (a movement disorder or orthostatic intolerance due to orthostatic hypotension) there is about a 65% loss of cardiac sympathetic innervation; and published data from patients with PAF suggests a 41% decrease in innervation by 4.8 years.³⁷ In the model, neuronal loss is reflected by a decrease in the uptake of tyrosine—ie, decreased k_{Tyr_Uptake} .

Dopamine-beta-hydroxylase (DBH) is essential for intra-vesicular norepinephrine synthesis in sympathetic nerves; however, the rate-limiting enzyme in norepinephrine formation is TH.³⁸ Our model predictions agree with this, in that in controls k_{TH} is 0.00020 min^{-1} , while rate constant for DBH (k_{DBH}) is much higher at 0.018 min^{-1} . The rate of norepinephrine synthesis in sympathetic nerves depends not only on functional DBH enzyme but also on several other processes, which our model incorporates along with DBH. Mathematical application of the model has revealed that LBDs entail decreased catecholamine biosynthesis via TH and LAAAD, decreased vesicular uptake, and augmented vesicular leakage, all of which would be expected to decrease availability of substrate for DBH. The calculated k_{DBH} is not decreased in patients with LBD.⁵ Because of this, we did not include predictions about effects of alterations in k_{DBH} .

Clinical Study Approval

Data were obtained from patients with LBDs and control subjects who had participated in ≥ 1 clinical research protocols approved by the Institutional Review Board of the National Institute of Neurological Disorders and Stroke. All research procedures were done after the participants had given written informed consent. Concerning the post-mortem observations, the National Institutes of Health Office of Human Subjects Research Protections determined that the post-mortem study was exempt from the requirement of Institutional Review Board approval. In all cases, the tissues were harvested for research purposes after the consent of the next of kin.

PET Scanning

The procedures for ^{18}F -DA PET scanning were the same as described previously.⁵ For ^{18}F -DOPA PET scanning 7 mCi of ^{18}F -DOPA was administered without carbidopa pretreatment. PUT/OCC ratios and washout percents of ^{18}F -DOPA-derived radioactivity were calculated as also described previously.¹⁸ Image analyses were done by personnel who were blinded as to the clinical diagnosis until the data were tabulated.

Follow-up PET scanning data were obtained from 2 groups, those with initially normal cardiac ^{18}F -DA-derived radioactivity and a subsequent decline (Group 1) and those with radioactivity that was already low upon initial testing (Group 2).

In a PD patient with normal myocardial ^{18}F -DA-derived radioactivity we tracked trends in radioactivity over more than 16 years of serial scanning. In another patient, PAF evolved over years to dementia with Lewy bodies and late PD. In this patient we reviewed data not only about cardiac ^{18}F -DA-derived radioactivity but also PUT/OCC ratio data from ^{18}F -DOPA scanning that were available for years before the onset of signs of central catecholamine deficiency.

Post-Mortem Data

Six patients with LBD who had undergone ^{18}F -DA PET scanning while alive underwent post-mortem tissue harvesting. Frozen apical myocardial tissue was assayed for contents of catecholamines, as described previously.³⁹

Immunoreactive αS was assayed in the same myocardial specimens and in scalp skin when samples were available. Data about catecholamines and immunoreactive αS were also analyzed from post-mortem PD and control samples obtained under a Material Transfer Agreement with the Banner Sun Health Research Institute. The samples were embedded in optimum cutting temperature compound and sliced into 8- to 10- μm thick sections (Histoserv, Germantown, MD). αS was expressed relative to alpha-smooth muscle actin (SMA) in scalp skin or to cardiac troponin T (cTnT) in myocardium. The primary antibody to αS was mouse IgG1 monoclonal anti- αS (1:1000; Santa Cruz Biotechnology, Santa Cruz, CA), to SMA was mouse IgG2a monoclonal anti-SMA (1:400; Santa Cruz Biotechnology), and to cTnT was mouse IgG2a monoclonal human anti-cTnT (1:250; Pel-Freez Biologicals). The secondary antibodies for visualizing the immunoreactions were Alexa 488-conjugated anti-mouse IgG1, Alexa 555-conjugated anti-rabbit, and Alexa 647-conjugated anti-mouse IgG2a (Thermo Scientific, Inc, Rockford, IL). Immunofluorescence confocal microscopy was done using a Zeiss LSM 880 confocal laser scanning microscope (Carl Zeiss, Oberkochen, Germany).

RESULTS

Model-Predicted Changes in Levels of Reactants

Figure 2 shows model-predicted changes in levels of the 11 reactants as a function of Log_{10_VR} . In general, levels of NEV, cytoplasmic tyrosine, vesicular dopamine, and

cytoplasmic DHPG decreased in a triphasic manner, while levels of cytoplasmic 3,4-dihydroxyphenylalanine, cytoplasmic dopamine, DOPALc, and cytoplasmic DOPAC increased approximately linearly.

Model-Predicted Triphasic Decline in NEv in LBDs

The model predicted a triphasic curvilinear relationship between NEv and Log10_VR (Figure 2H). At low values of Log10_VR, NEv was maintained and actually increased (Phase 1). At higher Log10_VR values NEv decreased markedly (Phase 2). Finally, NEv decreased slowly at high Log10_VR values (Phase 3). As shown in Figure 2, the 3 phases were separated by Hopf bifurcations (marked by H), indicating a segment involving oscillations of NEv.

Presuming a linear relationship between Log10_VR and time, with the onset of symptoms after 80% loss of NEv, Phase 2 would last about 4 years (Figure 3).

Individual data were analyzed from 3 patients with LBD with initially normal cardiac ^{18}F -DA-derived radioactivity (Group 1) and 9 with initially low radioactivity

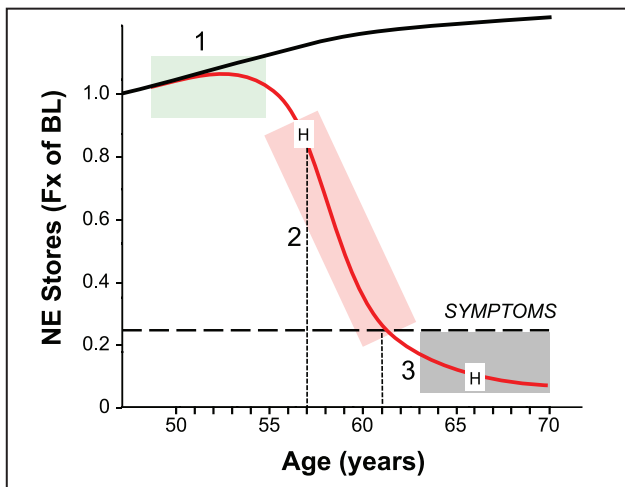


Figure 3. Model-predicted trends in myocardial norepinephrine stores as a function of age, with (red curve) and without (black curve) effects of cytoplasmic 3,4-dihydroxyphenylacetaldehyde on intra-neuronal reactions. Reactions affected by cytoplasmic 3,4-dihydroxyphenylacetaldehyde are depicted pictorially in Figure S2. When effects of cytoplasmic 3,4-dihydroxyphenylacetaldehyde are included (red curve), values for myocardial vesicular norepinephrine stores expressed as a fraction of the baseline value change in 3 phases (1 green, 2 pink, and 3 gray). Symptoms are presumed to occur when vesicular norepinephrine falls <25% of baseline (horizontal dashed line). A Hopf bifurcation (H) occurs at about the transition from Phase 1 to Phase 2. About 4 years intervene between Hopf bifurcation (H) and symptom onset (vertical dotted lines). When effects of cytoplasmic 3,4-dihydroxyphenylacetaldehyde are not included (black curve), vesicular norepinephrine increases over time, there is no Hopf bifurcation, and symptomatic disease does not develop. Fx of BL indicates fraction of the baseline value.

(Group 2) (Table S4). In the Group 1 subjects radioactivity declined exponentially at a rate of 7.8% per year. Among Group 2 subjects ^{18}F -DA-derived radioactivity during follow-up remained below the lower limit of normal.

Six patients with autopsy-proven LBDs had ^{18}F -DA PET scanning while alive and had post-mortem tissue harvesting. All 6 had markedly decreased apical myocardial concentrations of norepinephrine and dopamine (Table S5). The same patients had low interventricular septal myocardial concentrations of ^{18}F -DA-derived radioactivity.

In a patient with PD who was followed with serial ^{18}F -DA scanning over almost 17 years, during the first 8 years there was no clear trend in septal myocardial ^{18}F -DA-derived radioactivity (Figure 4). Then ^{18}F -DA-derived radioactivity fell rapidly, with about an 80% decline over the next 4.5 years. For the remainder of the follow-up period there was no further trend in radioactivity. The model-predicted triphasic curve applied well to the time-related changes in ^{18}F -DA-derived radioactivity in this patient (manually placed blue curve in Figure 3A).

A patient with PAF (Group 2, Patient 1 in Table S3) reported the onset of visual hallucinations at about 2 years of follow-up. At about 4 years the patient was diagnosed with dementia with Lewy bodies, and he developed parkinsonism late in the disease course. As shown in Figure 4B, during follow-up the patient's PUT/OCC ratio of ^{18}F -DOPA-derived radioactivity decreased rapidly; the relationship between the PUT/OCC ratio and years of follow-up was triphasic. The patient died, was autopsied, and was found to have brainstem Lewy bodies, markedly decreased myocardial catechol contents (Patient LBD2 in Table S4), and low PUT dopamine content (4.1 pmol/mg wet weight, about 30% of control).

Dependence of the Triphasic Decline on DOPALc

When the model did not include dependences of the rate constant for TYR uptake ($k_{\text{TYR_Uptake}}$), k_{TH} , k_{LAAAD} , $k_{\text{VMAT_DA}}$, $k_{\text{VMAT_NE}}$, the rate constant for U1 (k_{U1}), or k_{Leak} on DOPALc, there was no model-predicted decline in NEv (Figure 3, black curve). NEv actually was predicted to increase slightly over years.

Model-Predicted Effects of Genetic Mutations

We queried the effects of congenitally decreased k_{TH} , k_{LAAAD} , the rate constant for MAO acting on cytoplasmic DA ($k_{\text{MAO_DA}}$), $k_{\text{VMAT_DA}}$, the rate constant for ALDH (k_{ALDH}), and k_{U1} on the relationship of NEv versus Log10_VR (Figure S3). Decreasing

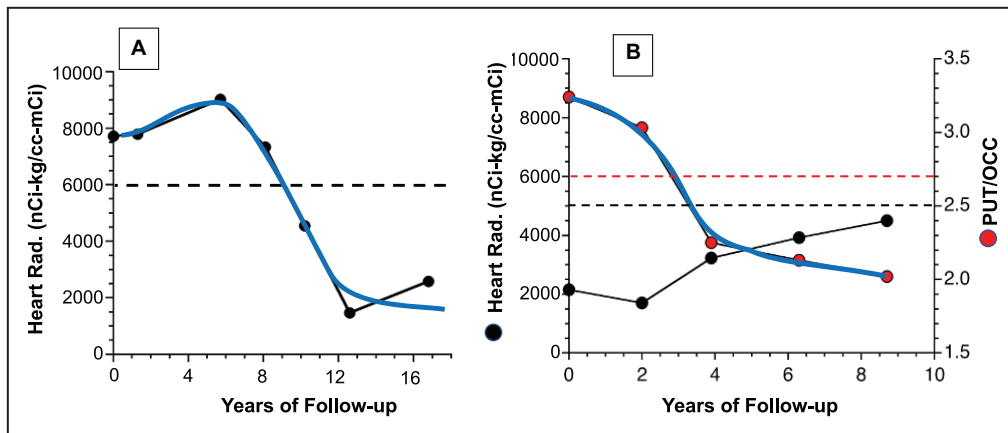


Figure 4. Empirical data for trends in indices of myocardial noradrenergic and putamen dopaminergic innervation during longitudinal follow-up of patients with Lewy body diseases. Blue curves of best fit placed manually. **(A)** Interventricular septal myocardial concentrations of ^{18}F -dopamine-derived radioactivity (in units of nanoCuries (nCi)/cc adjusted for the radioactive dose in milliCuries (mCi) per kg of body mass) during longitudinal follow-up of a patient with Parkinson disease. **(B)** Myocardial ^{18}F -dopamine-derived radioactivity concentrations (black circles) and concurrent putamen/occipital cortex ratios of ^{18}F -3,4-dihydroxyphenylalanine (^{18}F -DOPA)-derived radioactivity (red circles) during longitudinal follow-up of a patient with pure autonomic failure who developed dementia after about 4 years and parkinsonism after about 8 years. In the patient with Parkinson disease in **(A)**, ^{18}F -dopamine-derived radioactivity was above the lower limit of normal (horizontal black dashed line) for about 8 years and then rapidly decreased. In the patient with pure autonomic failure (PAF) in **(B)** ^{18}F -dopamine-derived radioactivity was low at the time of initial evaluation and remained sub-normal. The putamen/occipital cortex ratio of ^{18}F -3,4-dihydroxyphenylalanine-derived radioactivity was above the lower limit of normal (horizontal red dashed line) for about 3 years and then rapidly decreased. Note the triphasic declines in ^{18}F -dopamine-derived radioactivity in the patient with Parkinson disease and of the putamen/occipital cortex ratio of ^{18}F -3,4-dihydroxyphenylalanine-derived radioactivity in the patient with PAF during longitudinal follow-up, as predicted by the model. PUT/OCC indicates putamen/occipital cortex.

kVMAT_DA or kALDH by 30% shifted the curve to the left (Figure S3A and S3B), indicating earlier depletion of vesicular norepinephrine stores. These shifts were associated with changes in the occurrence of Hopf bifurcations (H marks in the curves in Figure S3). The largest shifts were for 30% decreases in kTH (Figure S3E) and kMAO_DA (Figure S3F).

Model-Predicted Effects of Treatments

MAO inhibition decreasing the rate constant for MAO acting on cytoplasmic DA (kMAO_DA) and the rate constant for MAO acting on cytoplasmic NE (kMAO_NE) by 30% beginning at the first Hopf bifurcation rapidly increased NEv, with a subsequent decline (blue curve and arrow in Figure S4A). The same treatment but initiated after symptoms resulted in a smaller rapid increase in NEv and a brief asymptomatic period (green curve and arrow).

The addition of a treatment inhibiting the influences of DOPALc on the rate constants kTH, kLAAAD, kMAO_DA, kVMAT_DA, kALDH, and kU1 (ie, mimicking the effects of treatment with an antioxidant to mitigate DOPALc- αS interactions) exerted little effect, prolonging the asymptomatic period by about 1 year (Figure S4B, magenta curve).

Post-Mortem Immunoreactive αS in Skin and Myocardium and Myocardial Norepinephrine

According to the model, there should be an accumulation of αS in the myocardium in patients with LBD, associated with decreased NEv. One half of the 14 patients with LBD had elevated post-mortem immunoreactive αS adjusted for cTnT in the myocardium, while all 14 had elevated αS adjusted for SMA in arrector pili muscles in scalp skin (Figure 5A). Twelve of the 14 patients with LBD had both elevated arrector pili αS /SMA ratios and myocardial norepinephrine content below the control range (Figure 5B).

All the patients with LBDs had αS /cTnT ratios in myocardium that were above the control range also had αS /SMA ratios in arrector pili muscles that were above the control range (Figure 5A). Similarly, all patients with LBDs and low myocardial norepinephrine had elevated αS /SMA ratios (Figure 5B).

DISCUSSION

We report a computational model that predicts the progression of cardiac catecholamine deficiency in

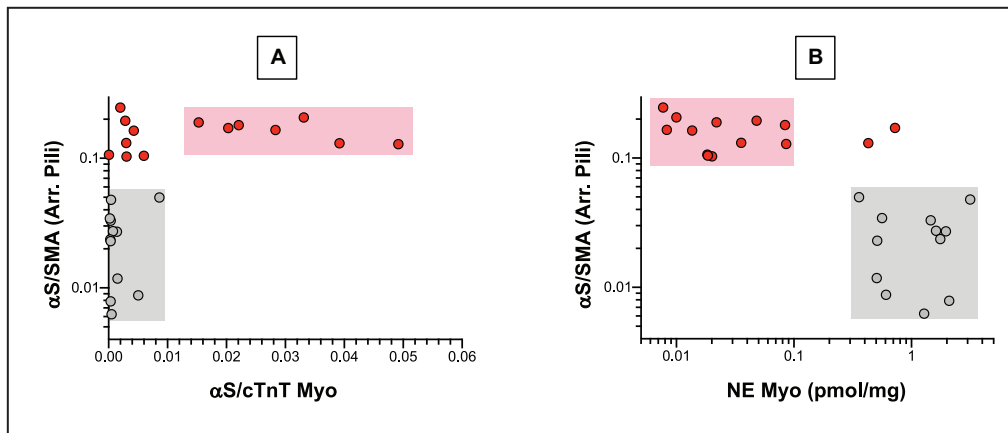


Figure 5. Post-mortem immunoreactive α S/smooth muscle actin in arrector pili muscles in scalp skin, expressed as functions of (A) apical myocardial α S/cardiac-specific troponin T (α S/cardiac troponin T) and (B) Apical myocardial norepinephrine content in patients with Lewy body diseases (red) and control subjects (gray). Light gray rectangles placed to indicate ranges of control values and pink rectangles values in Patients with Lewy body diseases who are outside the control ranges. Note that in (A) all patients with Lewy body diseases with elevated myocardial α S/cardiac troponin T ratios and in (B) all patients with Lewy body diseases with low apical myocardial norepinephrine levels have elevated arrector pili α S/smooth muscle actin ratios. α S indicates alpha-synuclein; Arr. Pili, arrector pili muscles; cTnT, cardiac troponin T; Myo, apical myocardial; and SMA, alpha smooth muscle actin.

LBDs. The model incorporates effects of homeostatic or allostatic increases in sympathetic noradrenergic outflow to the heart and autotoxicity from DOPAL. Key predictions from the model are (A) triphasic progression of catecholamine deficiency, (B) particular effects of genetic variants of intra-neuronal enzymes and processes on that progression, (C) effects of treatments that decrease DOPAL production or actions; and (D) cytoplasmic accumulation of α S in a manner associated with DOPAL buildup and catecholamine depletion. Empirical *in vivo* and post-mortem data largely confirm these predictions.

Catecholamine Deficiency in LBDs Progresses in 3 Phases

Longitudinal follow-up studies of patients with PD have suggested that the pattern of progression fits better with an inverse exponential curve than with a down-sloping straight line.⁹ These studies followed patients from the onset of symptomatic PD; however, according to our model, by the time a patient manifests symptomatically the loss of vesicular catecholamine stores is already advanced. The model predicts a critically important preclinical phase (Phase 1). Before the reported inverse exponential decline neurotransmitter stores are generally maintained. The reported inverse exponential curve represents rapid effects of dyshomeostasis in Phase 2 followed by a slower further decline during advanced disease in Phase 3.

To test the prediction that a triphasic pattern characterizes the loss of vesicular norepinephrine stores in cardiac sympathetic nerves we used empirical

serial data about myocardial ^{18}F -DA-derived radioactivity, which is a validated *in vivo* biomarker of cardiac noradrenergic innervation.¹⁷ One of our patients with PD underwent serial cardiac ^{18}F -DA PET scanning over almost 17 years (Figure 4A). As predicted by the model, ^{18}F -DA-derived radioactivity was normal upon initial evaluation and during 8 years of follow-up (Phase 1). Thereafter the radioactivity fell rapidly and substantially, with about an 80% decline over 4.5 years (Phase 2). Subsequently, ^{18}F -DA-derived radioactivity remained subnormal during further follow-up over several years (Phase 3). These data demonstrate the model-predicted triphasic curve for the decline in NEv.

The findings in 1 of our patients with PAF indicated the same triphasic temporal pattern of catecholamine loss can obtain in the nigrostriatal system of the brain (Figure 4B). The patient had PAF that progressed to dementia with Lewy bodies. As is typical of PAF, upon initial evaluation cardiac ^{18}F -DA-derived radioactivity was already low, and the PUT/OCC ratio of ^{18}F -DOPA-derived radioactivity was normal (Phase 1). During follow-up, the PUT/OCC ratio declined rapidly over a few years (Phase 2). Post-mortem analyses confirmed the co-occurrence of markedly decreased myocardial norepinephrine content, low putamen dopamine content, and brainstem LBs in this patient.

A triphasic disease progression pattern has been noted in other clinical conditions such as Alzheimer disease,⁴⁰ bicuspid aortic stenosis,⁴¹ and post-myocarditis cardiomyopathy.⁴² No previous model of LBDs has been applied to the preclinical period.

Increases in Cytosolic Dopamine and DOPAL as Part of the Pathogenetic Process

According to the model, decreased vesicular uptake coupled with increased TH activity results in a progressive increase in cytoplasmic dopamine levels. Empirical data support both decreased vesicular monoamine transporter activity⁴³ and increased cytoplasmic dopamine in PD.⁴⁴

We did not detect DOPAL in any myocardial sample. An explanation may be extensive binding of DOPAL to intracellular peptides or proteins.¹⁴ Consistent with this possibility, a recent study identified covalent adducts of DOPAL with L-cysteine and carnosine.⁴⁵

The model does not include the potential of DOPEGAL as an autotoxic factor. Burke et al reported that exogenously administered DOPEGAL is toxic to rat pheochromocytoma PC12 cells,⁴⁶ and recent literature has provided evidence that exogenously administered DOPEGAL is toxic to myofibroblasts.⁴⁷ PubMed searches related to endogenous DOPEGAL yielded no study describing DOPEGAL levels in sympathetically innervated organs. This may be related to the challenge of accurately measuring this catecholaldehyde in body fluids and tissues.

Our model is a mechanistic model that generates testable predictions for the disease course based on empirical data about the disease processes and on theoretical understanding about how these processes are inter-related. We did not evaluate the model by calculations of true positives, false positives, etc., or train the model, since the purpose was not to establish diagnosis (for which these calculations would be appropriate) but to model the underlying physiological processes that impact disease progression. To refine the model, more empirical data are needed, especially about DOPAL- α S interactions in clinical samples.

Model-Predicted Effects of Genetic Variations on the Triphasic Decline

The model was tested by comparing predictions with empirical data for the effects of specific genetic variants on the onset of the triphasic decline in vesicular catecholamine stores (Figure S3). As discussed in detail below, all the model-predicted effects of genetic variations have empirical support from animal models.

Congenitally decreased ALDH activity produces a lifetime increase in DOPALc, and mice with double knockout of the genes encoding mitochondrial and cytosolic ALDH have aging-related central dopaminergic neurodegeneration and motor dysfunction.⁴⁸ The model predicted that genetically determined decreased VMAT2 activity would result in relatively early depletion of catecholamine stores (Figure 4B). In confirmation of

this prediction, mice with congenital very low VMAT2 activity have decreased catecholamine contents in the brain and heart.^{39,49}

Regarding predictions based on genetic variants in reactions in sympathetic nerves, there are reports about the extents of decrease in transporter or enzyme activities in affected patients with genetic deficiencies of VMAT2, MAO-A, or LAAAD. Genetic VMAT2 deficiency manifests as a lethal pediatric disease that includes parkinsonism. In affected members of a consanguineous family transmitting mutation of the *SLC18A2* gene encoding VAMT2, transporter activity was reported to be decreased by $\geq 90\%$ based on incubation of membrane preparations with ³H-serotonin.⁵⁰ MAO-A deficiency is transmitted as an X-linked trait; affected males have virtually no fibroblast MAO-A activity, while carriers have about 30% of normal activity.⁵¹ In patients with genetic LAAAD deficiency, enzymatic activity can be undetectable.⁵² In a screening neonatal study, 3-O-methyl DOPA in blood spots was increased by about 3-fold, suggesting about one third of normal enzyme activity.⁵³ We therefore used an estimated 30% decrease in enzyme or transporter activities, which we believe was reasonable based on the above literature.

Implications for Preclinical Biomarkers

The results emphasize the importance of identifying pre-symptomatic biomarkers to detect the transition from Phase 1 to Phase 2. As demonstrated by the longitudinal follow-up data in LBD cases followed over many years, trends in ¹⁸F-DA-derived radioactivity may identify the key transition from Phase 1 to Phase 2. Data from the prospective NINDS PDRisk study (NIH Clinical Protocol 09N0010, "Biomarkers of Risk of Parkinson Disease") fit with this prediction,⁵⁴ by showing that low ¹⁸F-DA-derived radioactivity in at-risk healthy individuals identified those who later developed symptomatic PD (Phase 2–3).

Another promising preclinical biomarker of LBDs is increased α S in sympathetic nerves in skin biopsies. Patients with Lewy body forms of neurogenic orthostatic hypotension have increased α S/smooth muscle actin (SMA) ratios in cutaneous arrector pili muscles, blood vessels, and sweat glands, in a manner related to low myocardial ¹⁸F-DA-derived radioactivity.⁵⁵ In the current study, all the patients with LBDs who had low myocardial norepinephrine levels also had elevated α S/SMA ratios in arrector pili muscles from scalp skin (Figure 5). Longitudinal follow-up studies are needed to document whether analysis of α S/SMA ratios can detect the transition from Phase 1 to Phase 2.

Implications for Treatment

The present model predicts which interventions might be beneficial and, importantly, the optimal timing for the

interventions to be effective. For instance, the model predicts that MAO inhibition should immediately increase catecholamine stores (Figure S4A) and thereby improve symptoms temporarily. This prediction is confirmed by review of empirical data from the ADAGIO (Attenuation of Disease Progression With Azilect Given Once Daily) multi-center clinical trial of the MAO inhibitor rasagiline (Figure S4C).¹⁹ The model predicts that the same intervention but begun at the transition from Phase 1 to Phase 2 would substantially delay the onset of symptoms (Figure S4A).

The model presumes that DOPALc inhibits several reactions in sympathetic noradrenergic nerves—TH, LAAAD, vesicular uptake, and neuronal reuptake—while increasing leakage from the vesicles to the cytoplasm. These effects cause the triphasic decline in NEv, since the triphasic progression pattern is not predicted when they are excluded (Figure 3). According to the model, however, in order to slow the decline of NEv by inhibiting DOPALc effects there would have to be very substantial attenuation of those effects. A 30% decrease from the start of Phase 2 would only slightly delay symptom onset (Figure S4B).

Limitations

Although DOPAL effects are sufficient and provide a parsimonious explanation, there is no evidence that DOPAL actually causes the progression of catecholamine deficiency in LBDs. The catecholaldehyde hypothesis remains a hypothesis. There are probably several other models that would predict a triphasic decline in norepinephrine stores, based on compensatory increases in nerve pathway traffic and toxicity from downstream intra-neuronal consequences of the increased traffic. To be acceptable, however, these would also have to predict empirical data about levels of the reactants and the effects of genetic predispositions and treatments.

Our model does not include several processes that likely would be required for a comprehensive picture over the lifespan, such as neurogenesis, neuroplasticity, or resilience.

The exact meaning of “interactions” of DOPAL with α S is ambiguous, because the relative roles of enzymatic or spontaneous catecholamine oxidation and α S in PD pathogenesis⁵⁶ have not been clarified.

The model-predicted triphasic decline in NEv is expressed as a function of cumulative effects of cardiac sympathetic activation, not time. We assumed a linear relationship between Log10_VR and follow-up years in LBDs. There are no empirical data to support this assumption.

Among the patients with LBDs, one half had myocardial α S/cTnT ratios within the control range. We used post-mortem myocardial α S/cTnT ratios to adjust α S signal intensities for the amounts of tissue in the

samples. Since all the patients with LBDs had arrector pili α S/SMA ratios above the control range, the relationship between α S deposition in the skin and α S deposition in the myocardium seems to be complex. The implications for using cutaneous α S/SMA ratios in sympathetic noradrenergically innervated structures as in vivo biomarkers of myocardial α S deposition remain to be determined.

Perspective

We envision further development of mathematical modeling to enable predictions about complex interactions among genetic predispositions, environmental exposures, and drugs in the clinical manifestations and treatment of catecholaminergic neurodegeneration. More generally, computational modeling holds promise for enhancing patient-oriented research about autonomic and catecholamine-related disorders.

ARTICLE INFORMATION

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Disclosures

None.

Supplemental Material

Tables S1–S5
Figures S1–S4
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SUPPLEMENTAL MATERIAL

Table S1. Initial reactant amounts, reaction rates, and rate constants in the kinetic model.***AMOUNTS***

| REACTANT | PARAMETER | VALUE | RANGE |
|-----------------|------------------|--------------|--------------|
| 1 TYRc | TYRc Amount | 8747 | |
| 2 DOPAc | DOPAc Amount | 142 | 105-200 |
| 3 DAc | DAc Amount | 0.6 | |
| 4 DOPACc | DOPACc Amount | 25 | 10-75 |
| 5 DAv | DAv Amount | 76 | 30-110 |
| 6 NEv | NEv Amount | 1150 | 885-1771 |
| 7 NEe | NEe Amount | 0.14 | |
| 8 NEc | NEc Amount | 2.1 | |
| 9 DHPGc | DHPGc Amount | 60 | 47-165 |
| 10 DOPALc | DOPALc Amount | 2.9 | |
| 11 DOPEGALc | DOPEGALc Amount | 4.1 | |

RATES

| REACTION | PARAMETER | VALUE | RANGE |
|-----------------|----------------------------------|--------------|--------------|
| 1 TYR_Uptake | TYR Uptake Rate to TYRc | 56 | 34-89 |
| 2 TYR_Loss | TYRc Loss Rate to ECF | 54 | 33-87 |
| 3 TH | TYRc Conversion Rate to DOPAc | 1.8 | 1.1-2.8 |
| 4 LAAAD | DOPAc Conversion Rate to DAc | 1.5 | 1.2-1.8 |
| 5 DOPAc_Loss | DOPAc Exit Rate from the Model | 0.22 | 0.15-0.33 |
| 6 Leak_DA | DAv Loss Rate to Cytoplasm | 0.87 | 0.66-1.08 |
| 7 VMAT_DA | DAc Vesicular Uptake Rate | 2.2 | 1.8-2.7 |
| 8 MAO_DA | DAc Conversion Rate to DOPACc | 0.18 | 0.11-0.29 |
| 9 ALDH_DOPALc | DOPALc Conversion Rate to DOPACc | 0.18 | |
| 10 DOPACc_Loss | DOPACc Exit Rate from the Model | 0.18 | 0.11-0.29 |

| | | | | |
|----|-------------|-----------------------------------|------|-----------|
| 11 | DBH | DAv Conversion Rate to NEv | 1.4 | 1.4-3.6 |
| 12 | VMAT_NE | Vesicular Uptake Rate of NEc | 14 | 11-22 |
| 13 | Leak_NE | NEv Loss Rate to Cytoplasm | 13 | 10-20 |
| 14 | NE_Release | NEv Release Rate to ECF | 2.6 | 1.4-3.7 |
| 15 | U1 | NEe Reuptake Rate to NEc | 2.4 | 1.3-3.5 |
| 16 | NEe_Loss | NEe Exit Rate from the Model | 0.21 | 0.11-0.29 |
| 17 | MAO_NE | NEc Conversion Rate to DHPGc | 1.2 | 0.8-1.8 |
| 18 | AR_DOPEGALc | DOPEGALc Conversion Rate to DHPGc | 1.2 | |
| 19 | DHPGc_Loss | DHPGc Exit Rate from the Model | 1.2 | 0.8-1.8 |

Rate constants for 19 reactions were generated mathematically and are tabulated below.

RATE CONSTANTS

| REACTION | | PARAMETER | VALUE |
|-----------------|--------------|----------------------------------|--------------|
| 1 | kTYR_Uptake | TYR Uptake Rate to TYRc | 56 |
| 2 | kTYR_Loss | TYRc Loss Rate to ECF | 54 |
| 3 | kTH | TYRc Conversion Rate to DOPAc | 0.00020 |
| 4 | kLAAAD | DOPAc Conversion Rate to DAc | 0.011 |
| 5 | kDOPAc_Loss | DOPAc Exit Rate from the Model | 0.0016 |
| 6 | kLeak_DA | DAv Loss Rate to Cytoplasm | 0.011 |
| 7 | kVMAT_DA | DAc Vesicular Uptake Rate | 3.76 |
| 8 | kMAO_DA | DAc Conversion Rate to DOPACc | 0.30 |
| 9 | kALDH_DOPALc | DOPALc Conversion Rate to DOPACc | 0.061 |
| 10 | kDOPACc_Loss | DOPACc Exit Rate from the Model | 0.0072 |
| 11 | kDBH | DAv Conversion Rate to NEv | 0.018 |
| 12 | kVMAT_NE | Vesicular Uptake Rate of NEc | 6.72 |
| 13 | kLeak_NE | NEv Loss Rate to Cytoplasm | 0.011 |
| 14 | kNE_Release | NEv Release Rate to ECF | 0.0023 |
| 15 | kU1 | NEe Reuptake Rate to NEc | 17.1 |

| | | | |
|----|--------------|-----------------------------------|-------|
| 16 | kNEe_Loss | NEe Exit Rate from the Model | 1.49 |
| 17 | kMAO_NE | NEc Conversion Rate to DHPGc | 0.57 |
| 18 | kAR_DOPEGALc | DOPEGALc Conversion Rate to DHPGc | 0.29 |
| 19 | kDHPGc_Loss | DHPGc Exit Rate from the Model | 0.020 |

All reactant amounts are in nmoles and all rates in nmoles/min. Listed ranges are based on 25% and 75% quartiles of empirical median values.⁵ See Figure 1 for a pictorial representation of the reactants and reactions in the model.

Table S2. Model Equations.

In the equations below, several rate constants are listed that are nonlinear functions obtained from the curves approximating/interpolating the data. The Appendix contains the MATLAB code. The reactions are depicted pictorially in Figure 1.

The repressors are: k_{TH} , a function of BP and k_{TH} , k_{LAAAD} , k_{VMAT_DA} , k_{VMAT_NE} , k_{U1} , k_{TYR_Uptake} , functions of DOPALc.

The activators are: k_{Leak_DA} , k_{Leak_NE} , functions of DOPALc.

- (1) $d[TYRc]/dt = k_{TYR_Uptake} - (k_{TH} + k_{TYR_Loss}) * [TYRc]$
- (2) $d[DOPAc]/dt = k_{TH} * [TYRc] - (k_{DOPA_Loss} + k_{LAAAD}) * [DOPAc]$
- (3) $d[DAc]/dt = k_{LAAAD} * [DOPAc] + k_{Leak_DA} * [DAv] - (k_{MAO_DA} + k_{VMAT_DA}) * [DAc]$
- (4) $d[DOPACc]/dt = k_{ALDH_DOPALc} * [DOPALc] - k_{DOPAC_Loss} * [DOPACc]$
- (5) $d[DAv]/dt = k_{VMAT_DA} * [DAc] - (k_{Leak_DA} + k_{DBH}) * [DAv]$
- (6) $d[NEv]/dt = k_{DBH} * [DAv] + k_{VMAT_NE} * [NEc] - (k_{Leak_NE} + k_{NE_Release}) * [NEv]$
- (7) $d[NEe]/dt = k_{NE_Release} * [NEv] - k_{U1} * [NEe] - k_{NEe_Loss} * [NEe]$
- (8) $d[NEc]/dt = k_{Leak_NE} * [NEv] + k_{U1} * [NEe] - (k_{VMAT_NE} + k_{MAO_NE}) * [NEc];$
- (9) $d[DHPGc]/dt = k_{AR_DOPEGALc} * [DOPEGALc] - k_{DHPG_Loss} * [DHPGc]$
- (10) $d[DOPALc]/dt = k_{MAO_DA} * [DAc] - k_{ALDH_DOPALc} * [DOPALc]$
- (11) $d[DOPEGALc]/dt = k_{MAO_NE} * [NEc] - k_{AR_DOPEGALc} * [DOPEGALc]$

where the reactant abbreviations were: (1) TYRc=cytoplasmic tyrosine, (2) DOPAc=cytoplasmic 3,4-dihydroxyphenylalanine, (3) DAc=cytoplasmic dopamine, (4) DAc=cytoplasmic dopamine, (5) DOPACc=cytoplasmic 3,4-dihydroxyphenylacetic acid; (6) NEv=vesicular norepinephrine, (7) NEc=cytoplasmic norepinephrine, (8) DHPGc=cytoplasmic 3,4-dihydroxyphenylglycol; (9) NEe=norepinephrine in the extracellular fluid; (10) DOPALc=cytoplasmic 3,4-dihydroxyphenylacetaldehyde; (11) DOPEGALc=cytoplasmic 3,4-dihydroxyphenylglycolaldehyde.

Abbreviations: (1) TYR_Uptake=neuronal uptake of tyrosine, (2) TYR_Loss=loss of tyrosine from the nerves, (3) TH=tyrosine hydroxylase, (4) LAAAD=L-aromatic-amino-acid decarboxylase, (5) DOPA_Loss=loss of DOPAC from the nerves, (6) VMAT_DA=vesicular uptake of cytoplasmic DA via the VMAT, (7) MAO_DA=MAO acting on cytoplasmic DA, (8) DOPAC_Loss=loss of DOPAC from the nerves, (9) DBH=DA-beta-hydroxylase acting on vesicular DA to form vesicular NE, (10) Leak_DA=leakage of vesicular DA into the cytoplasm, (11) VMAT_NE=vesicular uptake of cytoplasmic NE via the VMAT, (12) MAO_NE=monoamine oxidase acting on cytoplasmic norepinephrine to form DHPG, (13) Leak_NE=leakage of vesicular NE into the cytoplasm, (14) NE_Release=NE release by vesicular exocytosis, (15) U1=neuronal uptake of NE via the cell membrane norepinephrine transporter (NET), (16) DHPG_Loss=loss of DHPG from the nerves, and (17) NE_Loss=loss of extracellular NE from the nerves.

Table S5. MATLAB function Parkinson_11d1.

For our ODE system, where the reactions and reactants are depicted in Figure 1, we have the following MATLAB function and subfunctions.

```
function out = Parkinson_11d1_symbolic()
out[1] = @init;
out[2] = @fun_eval;
end
% -----
function x0 = init(logV)
% TYRc DOPAc DAc DOPACc DAv NEv NEe NEc DHPGc DOPALc DOPEGALc
x0 = [8747 142 0.6 25 76 1150 0.14 20 60 2.9 4.1]';
end
% -----
function dydt = fun_eval(~,y, logVR)
% unused parameter is t
% input: initial approximate rates r0 and initial reactants y0
% output: initial accurate rates r_s (scaled)
TYRc = y(1); DOPAc = y(2); DAc = y(3); DOPACc = y(4); DAv = y(5); NEv = y(6);
NEe = y(7); NEc = y(8); DHPGc = y(9); DOPALc = y(10); DOPEGALc = y(11);
%
kTYR_Uptake0 = 5.589189955455429e+01; %
kTYR_Loss = 6.185036797562349e-03; %
kTH0 = 2.047996668888087e-04; % baseline, initial for DOPALc,
kLAAAD0 = 1.106515697265155e-02; % baseline, initial for DOPALc
kDOPAc_Loss = 1.550214057463951e-03; %
kLeak_DA0 = 1.133781834294390e-02; % baseline, min, initial for DOPALc
kVMAT_DA0 = 3.755398997515088e+00; % baseline, initial for DOPALc
```

```

kMAO_DA = 2.994784761187236e-01; %
kALDH_DOPALc = 6.196106402455661e-02; %
kDOPACc_Loss = 7.187483426848048e-03; %
kDBH = 1.831006847954365e-02; %
kVMAT_NE0 = 7.056699257453658e-01;% baseline, initial for DOPALc
kLeak_NE0 = 1.121932409485655e-02;% baseline, min, initial for DOPALc
kNE_Release0 = 2.263253052406611e-03;% 14 baseline, kNE_Release varies
kU10 = 1.710237097742159e+01;% baseline, initial for DOPALc
kNEe_Loss = 1.488636238775596e+00;%
kMAO_NE = 5.915780655083667e-02;% , orig: 5.634076814365396e-01
kAR_DOPEGALc = 2.885746661016436e-01;%
kDHPGc_Loss = 1.971926885027911e-02;%
% repressor BP -> kTH, kNE_Release
k1 = 83; % feedback parameters start here
BP = 120 - k1*logVR; %
% -----
x_BP = BP;
x_BP_min = 50; % initial value of x_BP
x_BP_max = 120;
% -----
y_kTH_BP_min = kTH0;
y_kTH_BP_max = kTH0*2.5;
n_kTH_BP = log(y_kTH_BP_min/y_kTH_BP_max)/(x_BP_min - x_BP_max);
kTH_BP = y_kTH_BP_max*exp(n_kTH_BP*(x_BP_min - x_BP));
% -----
y_kNE_Release_min = kNE_Release0;
y_kNE_Release_max = kNE_Release0*4; % 0.0091;

```

```

n_kNE_Release = log(y_kNE_Release_min/y_kNE_Release_max)/(x_BP_min - x_BP_max);
% 0.019804

kNE_Release = y_kNE_Release_max*exp(n_kNE_Release*(x_BP_min - x_BP));
% -----

% repressor DOPALc: kTH, kLAAAD, kVMAT_DA, kVMAT_NE, kU1, kTYR_Uptake
x_DOP = DOPALc;

x_DOP_min = 2.9; % initial value of x_DOP

K = 1.8; %

n = 5;

coef = 0.35;

% -----

kTH_ = kTH0*((1 - coef)*K^n/(K^n + (x_DOP-x_DOP_min)^n) + coef);
kTH = kTH_BP + kTH_DOPALc - kTH0; % Step 3a,b

% -----

kLAAAD = kLAAAD0*((1 - coef)*K^n/(K^n + (x_DOP-x_DOP_min)^n) + coef);

% -----

kVMAT_DA = kVMAT_DA0*((1 - coef)*K^n/(K^n + (x_DOP-x_DOP_min)^n) + coef);

% -----

kVMAT_NE = kVMAT_NE0*((1 - coef)*K^n/(K^n + (x_DOP-x_DOP_min)^n) + coef); %

% -----

kU1 = kU10*((1 - coef)*K^n/(K^n + (x_DOP-x_DOP_min)^n) + coef);

% -----

kTYR_Uptake = kTYR_Uptake0*((1 - coef)*K^n/(K^n + (x_DOP-x_DOP_min)^n) + coef);

% -----

% activator DOPALc: kLeak_DA kLeak_NE,

n_a = 4;

K_a = 2.2;

```



```

coef_a = 3;
kLeak_DA = kLeak_DA0*((coef_a - 1)*(x_DOP - x_DOP_min)^n_a...
/(K_a^n_a + (x_DOP - x_DOP_min)^n_a) + 1 );% Step 3d
% -----
kLeak_NE = kLeak_NE0*((coef_a - 1)*(x_DOP - x_DOP_min)^n_a...
/(K_a^n_a + (x_DOP - x_DOP_min)^n_a) + 1 );% Step 3d
f1 = kTYR_Uptake - (kTYR_Loss+kTH)*TYRc; % 1, TYRc
f2 = kTH*TYRc - (kLAAAD+kDOPAc_Loss)*DOPAc; % 2, DOPAc
f3 = kLAAAD*DOPAc + kLeak_DA*DAv-(kVMAT_DA+kMAO_DA)*DAc; % 3, DAc
f4 = kALDH_DOPALc*DOPALc - kDOPACc_Loss*DOPACc; % 4, DOPACc rev
f5 = kVMAT_DA*DAc - (kLeak_DA+kDBH)*DAv; % 5, DAv
f6 = kDBH*DAv + kVMAT_NE*NEc - (kLeak_NE+kNE_Release)*NEv;% 6, NEv
f7 = kNE_Release*NEv - kU1*NEe - kNEe_Loss*NEe; % 7, NEe
f8 = kLeak_NE*NEv + kU1*NEe - (kVMAT_NE+kMAO_NE)*NEc; % 8, NEc
f9 = kAR_DOPEGALc*DOPEGALc - kDHPGc_Loss*DHPGc; % 9, DHPGc rev
f10 = kMAO_DA*DAc - kALDH_DOPALc*DOPALc; %10, DOPALc new
f11 = kMAO_NE*NEc - kAR_DOPEGALc*DOPEGALc; %11, DOPEGALc new
dydt = [f1; f2; f3; f4; f5; f6; f7; f8; f9; f10; f11];
end

```

Table S4, Individual data for interventricular septal myocardial ¹⁸F-dopamine- (¹⁸F-DA) derived radioactivity as a function of years of follow-up (F/u).

| GROUP 1 | N | Sex | Age | Diagnosis | Initial | F/u 1 | F/u 2 | F/u 3 | F/u 4 | F/u 5 | F/u 6 |
|----------------------------------|----------|------------|------------|------------------|----------------|--------------|--------------|--------------|--------------|--------------|--------------|
| F/u years | 1 | M | 53 | PD | 0.0 | 1.3 | 5.7 | 8.1 | 10.2 | 12.6 | 16.8 |
| ¹⁸ F-DA | 1 | | | | 7723 | 7791 | 9027 | 7335 | 4547 | 1469 | 2582 |
| ¹⁸ F-DA Fx Initial | 1 | | | | 1.00 | 1.01 | 1.17 | 0.95 | 0.59 | 0.19 | 0.33 |
| F/u years | 2 | M | 53 | PAF | 0.0 | 1.8 | 3.8 | 7.7 | 10.1 | | |
| ¹⁸ F-DA | 2 | | | | 7487 | 5654 | 3643 | 3192 | 3110 | | |
| ¹⁸ F-DA Fx Initial | 2 | | | | 1.00 | 0.76 | 0.49 | 0.43 | 0.42 | | |
| F/u years | 3 | M | 63 | PD | 0.0 | 2.9 | 4.0 | 6.4 | 13.4 | 16.8 | |
| ¹⁸ F-DA | 3 | | | | 6993 | 6110 | 8349 | 5190 | 6443 | 4061 | |
| ¹⁸ F-DA Fx Initial | 3 | | | | 1.00 | 0.87 | 1.19 | 0.74 | 0.92 | 0.58 | |
| Mean F/u years | | | | | 0.0 | 1.9 | 4.1 | 6.7 | 11.3 | 14.7 | 16.8 |
| Mean ¹⁸F-DA | | | | | 7401 | 6518 | 7006 | 5239 | 4700 | 2765 | 2582 |
| Mean ¹⁸F-DA Fx | | | | | 0.75 | 0.66 | 0.71 | 0.53 | 0.48 | 0.26 | 0.17 |

| GROUP 2 | N | Sex | Age | Diagnosis | Initial | F/u 1 | F/u 2 | F/u 3 | F/u 4 |
|-------------------------------|----------|------------|------------|------------------|----------------|--------------|--------------|--------------|--------------|
| F/u years | 1 | M | 70 | PAF/DLB | 0.0 | 2.0 | 3.9 | 6.3 | 8.7 |
| ¹⁸ F-DA | 1 | | | | 2151 | 1702 | 3231 | 3923 | 4498 |
| ¹⁸ F-DA Fx Initial | 1 | | | | 1.00 | 0.79 | 1.50 | 1.82 | 2.09 |
| F/u years | 2 | M | 63 | PAF | 0.0 | 6.0 | 11.0 | 13.6 | 15.7 |
| ¹⁸ F-DA | 2 | | | | 2184 | 3905 | 2532 | 3199 | 3390 |

| | | | | | | | | | |
|-------------------------------|---|---|----|------------|------|---------|------|------|------|
| ¹⁸ F-DA Fx Initial | 2 | | | | 1.00 | 1.79 | 1.16 | 1.46 | 1.55 |
| F/u years | 3 | F | 67 | PAF | 0.0 | 2.3 | 4.0 | 6.2 | 8.2 |
| ¹⁸ F-DA | 3 | | | | 1948 | 3422 | 4157 | 2581 | 2594 |
| ¹⁸ F-DA Fx Initial | 3 | | | | 1.00 | 1.76 | 2.13 | 1.33 | 1.33 |
| F/u years | 4 | M | 58 | PD | 0.0 | 0.5 | 2.6 | 10.5 | |
| ¹⁸ F-DA | 4 | | | | 2096 | No data | 1830 | 868 | |
| ¹⁸ F-DA Fx Initial | 4 | | | | 1.00 | | 0.87 | 0.41 | |
| F/u years | 5 | F | 72 | PD/DLB | 0.0 | 3.2 | 10.4 | | |
| ¹⁸ F-DA | 5 | | | | 2344 | 2381 | 570 | | |
| ¹⁸ F-DA Fx Initial | 5 | | | | 1.00 | 1.02 | 0.24 | | |
| F/u years | 6 | F | 57 | PAF | 0.0 | 1.8 | 8.6 | | |
| ¹⁸ F-DA | 6 | | | | 4830 | 3204 | 4212 | | |
| ¹⁸ F-DA Fx Initial | 6 | | | | 1.00 | 0.66 | 0.87 | | |
| F/u years | 7 | M | 62 | PAF | 0.0 | 1.1 | 9.6 | | |
| ¹⁸ F-DA | 7 | | | | 5294 | 1990 | 3269 | | |
| ¹⁸ F-DA Fx Initial | 7 | | | | 1.00 | 0.38 | 0.62 | | |
| F/u years | 8 | F | 57 | PAF/DLB/PD | 0.0 | 1.9 | 3.0 | 4.4 | 6.1 |
| ¹⁸ F-DA | 8 | | | | 3194 | 3289 | 3472 | 3193 | 2346 |
| ¹⁸ F-DA Fx Initial | 8 | | | | 1.00 | 1.03 | 1.09 | 1.00 | 0.73 |
| F/u years | 9 | F | 66 | PD | 0.0 | 1.5 | 3.2 | 4.6 | 6.2 |
| ¹⁸ F-DA | 9 | | | | 5351 | 4546 | 5835 | 7133 | 7246 |
| ¹⁸ F-DA Fx Initial | 9 | | | | 1.00 | 0.85 | 1.09 | 1.33 | 1.35 |

| | | | | | | | | | |
|-------------------------------------|--|--|--|--|-------------|-------------|-------------|-------------|-------------|
| F/u years | | | | | 0.0 | 2.3 | 6.3 | 7.6 | 9.0 |
| ¹⁸F-DA | | | | | 3266 | 3055 | 3234 | 3483 | 4015 |
| ¹⁸F-DA Fx Initial | | | | | 1.0 | 1.0 | 1.1 | 1.2 | 1.4 |

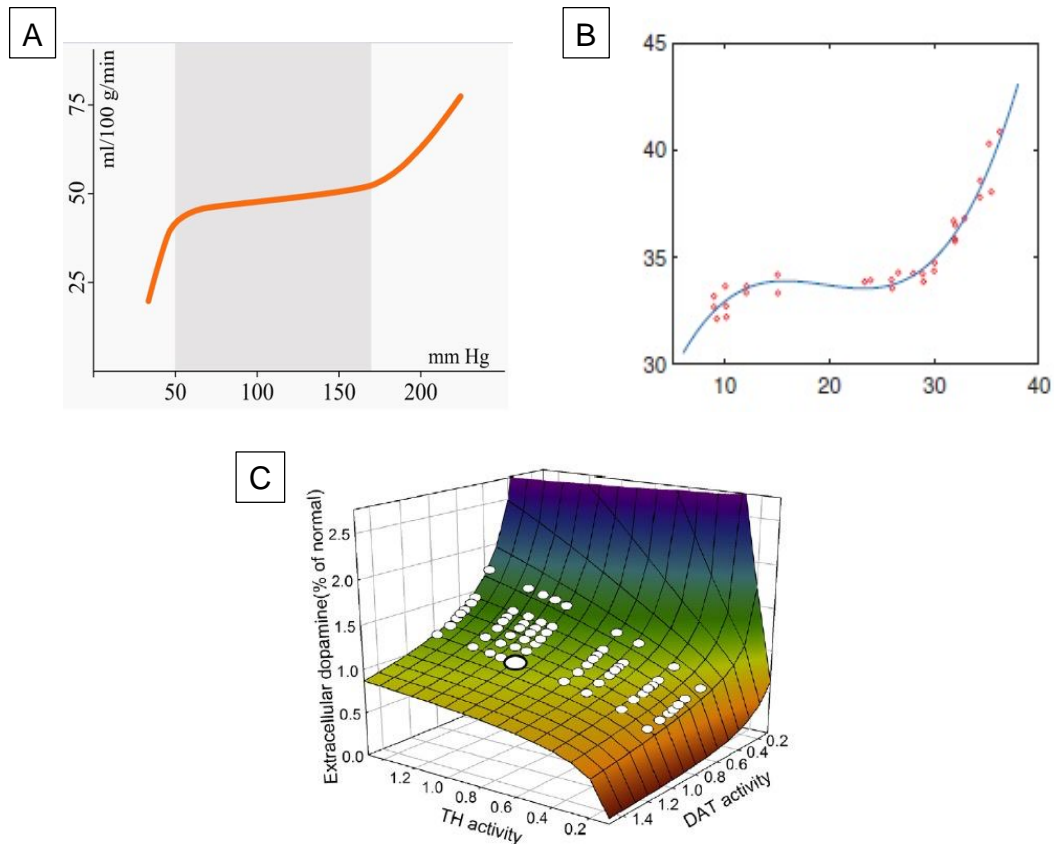
In Group 1 (N=3) initial radioactivity was normal (above 6000 nCi-kg/cc-mCi)⁵⁴ and fell to below normal during follow-up. In Group 2 (N=9) initial radioactivity was subnormal (below 6000 nCi-kg/cc-mCi), with low radioactivity persisting during follow-up. Listed ages are in years. DLB=dementia with Lewy bodies; Dx=diagnosis; F=female; Fx Initial=fraction of initial value; M=male; PAF=pure autonomic failure; PD=Parkinson disease; PDRisk=multiple risk factors for PD, enrolled in the intramural NINDS PDRisk study. Diagnoses with slashes (/) indicate the temporal trends in symptoms.

Table S5. Post-mortem apical myocardial concentrations of catecholamines (norepinephrine (NE), dopamine (DA)) and in vivo interventricular septal myocardial ¹⁸F-dopamine- (¹⁸F-DA)-derived radioactivity in patients with Lewy body diseases (LBDs).

| Patient | Sex | Age | Diagnosis | NE | DA | ¹⁸ F-DA |
|---------|------|-----|------------|-------|--------|--------------------|
| LBD1 | F | 84 | PD | 0.036 | 0.0019 | 2526 |
| LBD2 | M | 78 | PD/DLB | 0.432 | 0.0059 | 3729 |
| LBD3 | F | 74 | PAF | 0.007 | 0.0000 | 1733 |
| LBD4 | M | 69 | PAF | 0.034 | 0.0033 | 3218 |
| LBD5 | F | 83 | PD/DLB | 0.048 | 0.0020 | 2381 |
| LBD6 | M | 79 | PAF/DLB/PD | 0.019 | 0.0000 | 4498 |
| Control | N=25 | 78 | | 1.77 | 0.13 | |

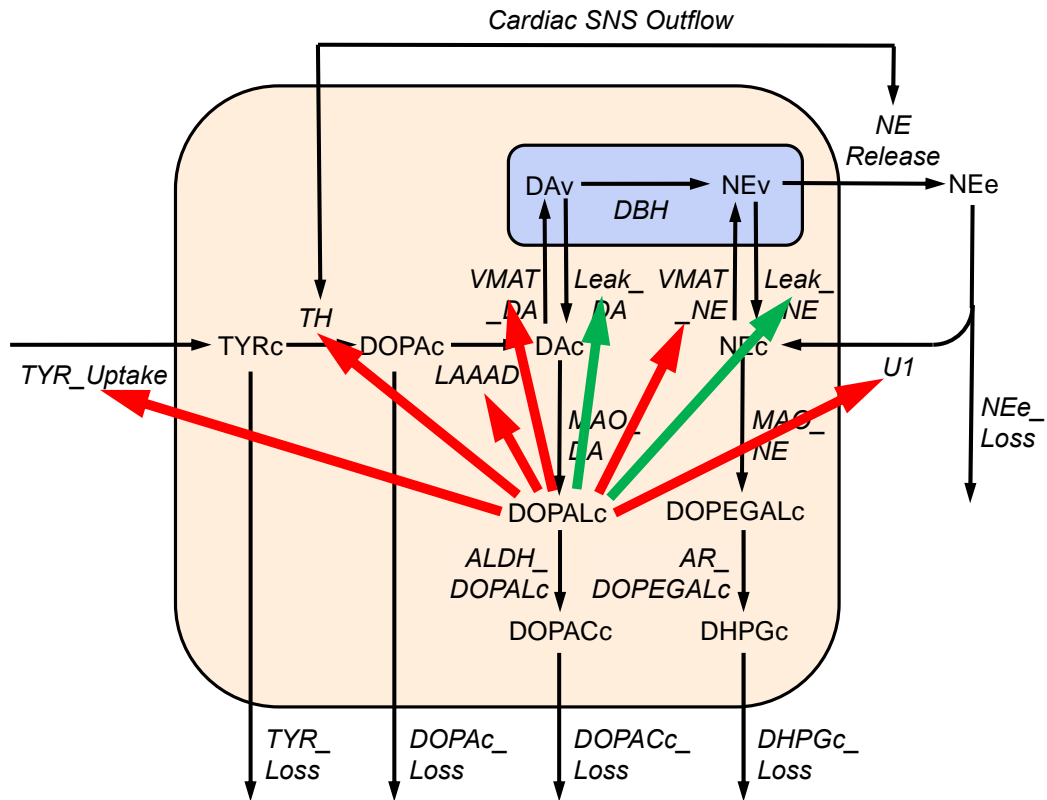
Data are also shown from an ongoing database of age-matched control subjects who did not have LB pathology. Listed ages are in years. Catecholamine concentrations are in units of pmol/mg wet weight and ¹⁸F-DA-derived radioactivity in units of nCi-kg/cc-mCi. Abbreviations: CON=control; DLB=dementia with Lewy bodies; F=female; M=male; PAF=pure autonomic failure. Diagnoses with slashes (/) indicate the temporal trends in symptoms. The LBD patients have drastically decreased myocardial NE and DA contents. All the patients had low ¹⁸F-DA-derived radioactivity during life (normal ≥ 6000 nCi-kg/cc-mCi).⁵⁴

Figure S1. Curves depicting (A) cerebrovascular autoregulation, (B) body temperature regulation, and (C) extracellular dopamine (DA) as a function of genetic variation in activities of the cell membrane DA transporter (DAT) and tyrosine hydroxylase (TH).



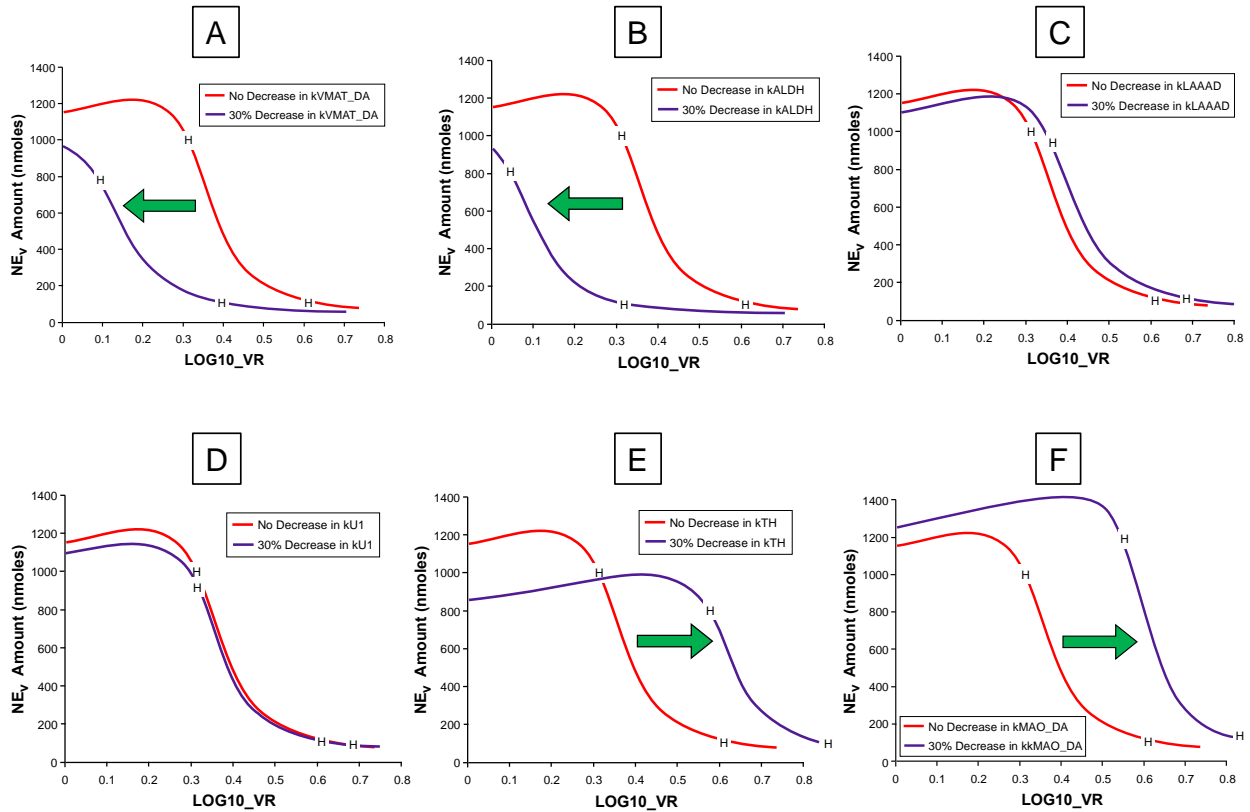
In (A), across a range of blood pressures (horizontal axis), cerebral blood flow (vertical axis) is kept within a relatively small range. At extremes of blood pressure, autoregulation breaks down (https://commons.wikimedia.org/wiki/File:Cerebrovascular_autoregulation.svg). In (B), body temperature of a brown opossum (vertical axis) is shown as a function of the ambient temperature (horizontal axis).^{25, 57} (C) displays a homeostatic surface, where the state at the output node (in this case extracellular DA) is unaffected by changes in values for the two independent parameters TH and DAT activities.^{24, 25} On this surface, the wild-type genotype is indicated by the large white circle. The smaller white circles indicate positions corresponding to genetic polymorphisms. All points on the surface are homeostatic. One can conceptualize the homeostatic surface changing as a result of accumulated stress (allostatic load). Dyshomeostasis would correspond to extracellular DA falling below the homeostatic surface. Panels B and C are reproduced from the Nijhout et al²⁵ with permission. Copyright © 2014 Elsevier.

Figure S2. Pictorial representation of inhibitory (red) and stimulatory (green) effects of cytoplasmic DOPAL (DOPALc) on reactions in the computational model.



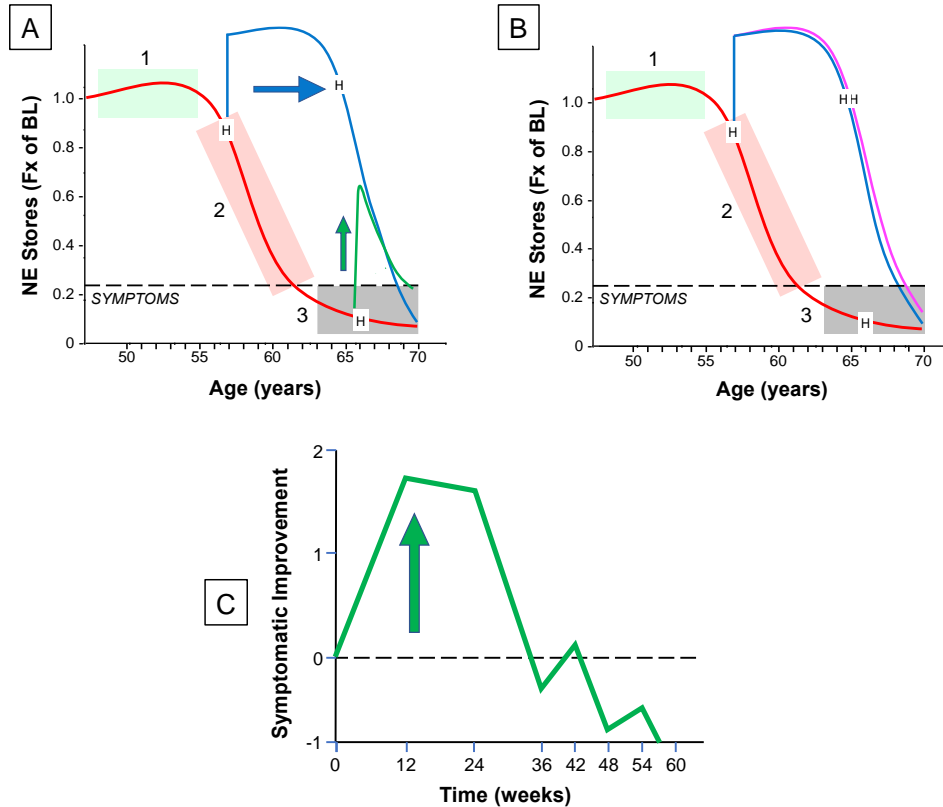
The model lumps effects of DOPAL, α -synuclein (α S), and DOPAL- α S interactions. For definitions of abbreviations see the legend for Figure 1.

Figure S3. Model-predicted effects of genetic variants on myocardial norepinephrine content (NE_v).



(A) 30% decrease in kVMAT_DA; (B) 30% decrease in kALDH; (C) 30% decrease in kLAAAD; (D) 30% decrease in kU1; (E) 30% decrease in kTH; (F) 30% decrease in kMAO_DA. In each panel the red curve indicates the relationship between NE_v and the log of the vascular relaxation (Log10_VR), the stimulus for reflexively increased cardiac sympathetic outflow. H symbols indicate Hopf bifurcations. Green arrows indicate shifts in position of the curves for genetic variants (blue). The model predicts earlier Hopf bifurcations for 30% decreases in kVMAT_DA and kALDH and later Hopf bifurcations for 30% decreases in kTH and kMAO_DA.

Figure S4. Model-predicted effects of treatments on trends in cardiac norepinephrine stores (NEv).



(A) Predicted effects of decreasing k_{MAO_DA} by 30% beginning at the time of the first Hopf bifurcation, corresponding to the beginning of pre-symptomatic Phase 2 (blue) and the same decrease in k_{MAO_DA} beginning at the time of the second Hopf bifurcation in symptomatic Phase 3 (green). (B) Predicted curve after decreasing k_{MAO_DA} by 30% and decreasing by 30% the effects of DOPALc on k_{TYR_Uptake} , k_{TH} , k_{LAAAD} , k_{VMAT_DA} , k_{VMAT_NE} , k_{U1} , and k_{Leak} at the time of the first Hopf bifurcation (magenta). Treatment decreasing k_{MAO_DA} by 30% starting at the beginning of Phase 2 produces an immediate increase in NEv, shifts to the right the curve relating NEv vs. age (blue arrow), and delays the onset of symptomatic disease by about 7 years. The same treatment initiated in Phase 3 produces a smaller immediate increase in NEv and transiently alleviates symptoms, with symptoms recurring after about 4 years (green arrow). Additional treatment decreasing by 30% the effects of DOPALc on k_{TYR_Uptake} , k_{TH} , k_{LAAAD} , k_{VMAT_DA} , k_{VMAT_NE} , k_{U1} , and k_{Leak} produces only a slight (about 1 year) delay in symptom onset. (C) Symptomatic improvement vs. duration of treatment with the MAO-B inhibitor rasagiline in PD (data derived from Olanow et al.¹⁹).