

Supporting Information

Biophysical and Structural Analyses of the Interaction between the SHANK1 PDZ Domain and an Internal SLiM

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1. Supplementary tables and figures

Table S1. Selection of the tested internal ligands.

Name	Sequence
FAM-Ahx-ARAP3 ₁₄₁₄₋₁₄₂₉ -CONH ₂	FAM-Ahx-FPELIQDTSTSFSTTR-CONH ₂
FAM-Ahx-ELFN1 ₅₇₉₋₅₉₄ -CONH ₂	FAM-Ahx-ESTSFQGVKSGPVSV-CONH ₂
Fluorophore-labelled SLiM	FAM-Ahx-EESTSFQGP-CONH ₂
SLiM modelled by PSSM	Ac-EESTSFQGP-CONH ₂

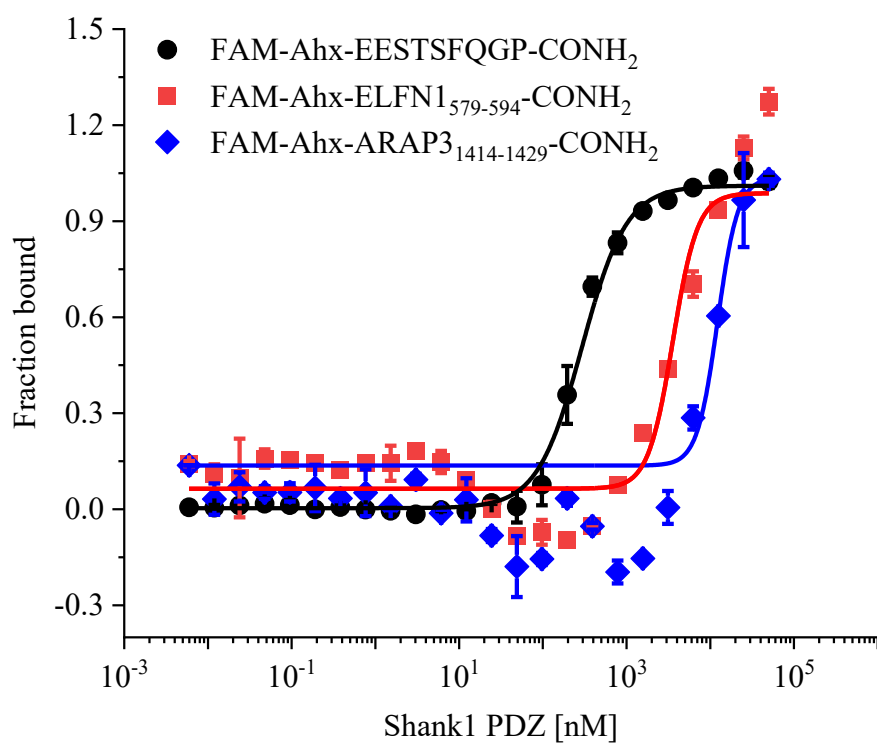


Figure S1. Fluorescence anisotropy direct titration of SHANK1-PDZ in 50 mM NH₄OAc, pH 6.5 buffer using 50 nM FAM-Ahx-ARAP3₁₄₁₄₋₁₄₂₉-CONH₂ ($12.2 \pm 8.3 \mu\text{M}$), FAM-Ahx-ELFN1₅₇₉₋₅₉₄-CONH₂ ($3.6 \pm 0.7 \mu\text{M}$), and FAM-Ahx-EESTSFQGP-CONH₂ ($0.8 \pm 0.1 \mu\text{M}$) as tracers. Plates were read after 24 hr incubation at room temperature.

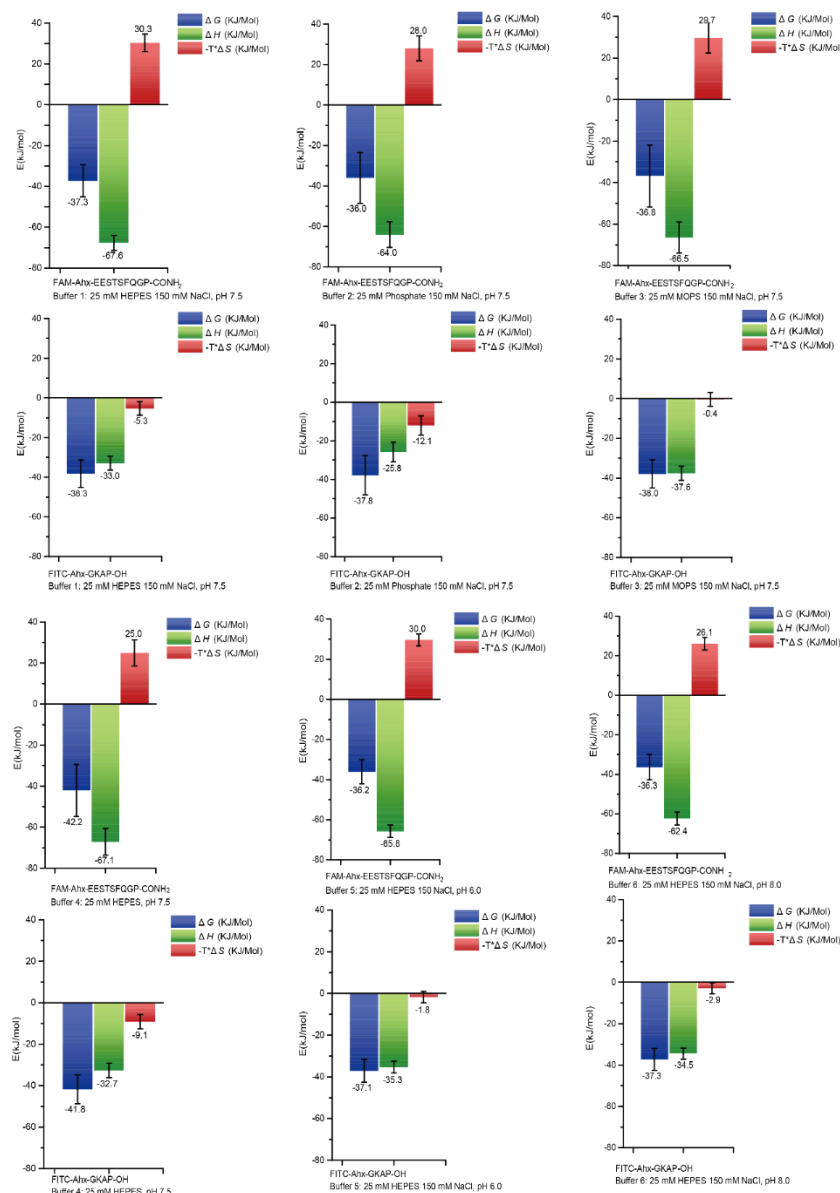


Figure S2. VT-FA assay results of the SHANK1-PDZ with its *N*-terminally fluorophore-labelled internal ligand FAM-Ahx-EESTSFQGP-CONH₂ and C-terminal ligand FITC-Ahx-EAQTRL-OH. The *K_d* values were collected from the results of titrating 600 μM SHANK1-PDZ to 50 nM tracers in different buffers (Buffer 1: 25 mM HEPES [4-(2-hydroxyethyl)-1-piperazineethanesulfonic acid], 150 mM NaCl, pH 7.5; Buffer 2: 25 mM phosphate, 150 mM NaCl, pH 7.5; Buffer 3: 25 mM MOPS [3-(*N*-morpholino)propanesulfonic acid], 150 mM NaCl, pH 7.5; Buffer 4: 25 mM HEPES, pH 7.5; Buffer 5: 25 mM HEPES, 150 mM NaCl, pH 6.0; Buffer 6: 25 mM HEPES, 150 mM NaCl, pH 8.0) at 25 °C, 27.5 °C, 30 °C, 32.5 °C, 35 °C, 37.5 °C and 40 °C. The ΔG , ΔH and $-T\Delta S$ were further calculated using the Arrhenius equation and the Gibbs free energy change equation.

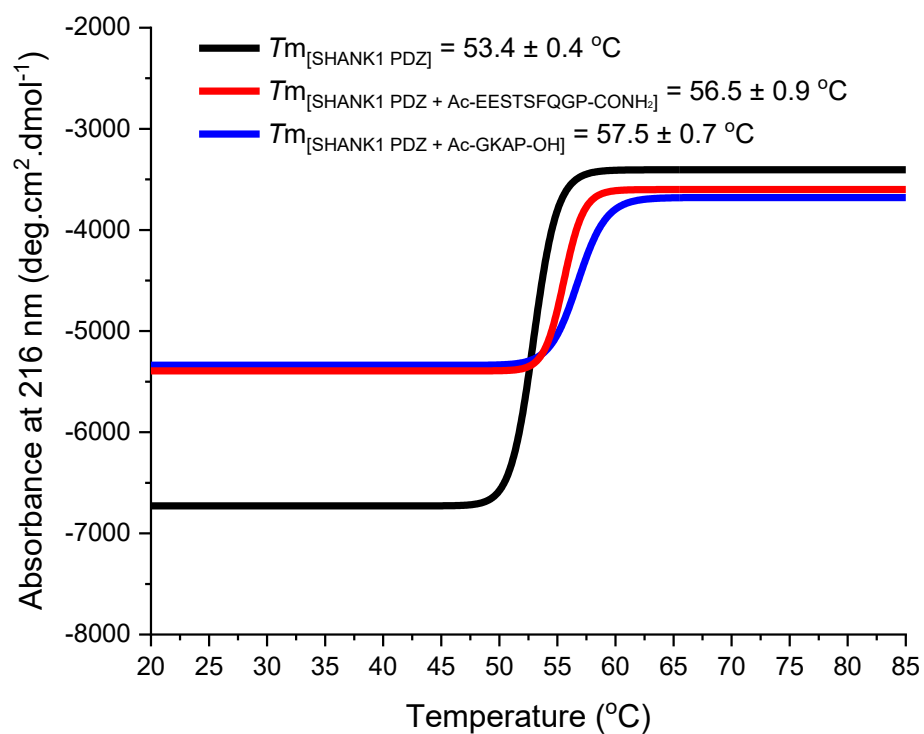


Figure S3. Normalized-fitted temperature melting curves of apo SHANK1-PDZ, SHANK1-PDZ/Internal ligand Ac-EESTSFQGP-CONH₂ complex and SHANK1-PDZ/C-terminal ligand Ac-EAQTRL-OH complex.

Table S2. Collection and refinement statistics for obtained SHANK1-PDZ/Ac-EESTSFQGP-CONH₂ co-crystal structure

Data Collection Statistics			
X ray source	DLS Beamline i24		
Average unit cell	a, b, c, (Å): 149.10, 149.10, 64.07 α, β, γ (°): 90, 90, 120		
Processed using	Xia2 dials		
/Space group	P 3 2 2 1		
	Overall	Inner shell	Outer shell
Low resolution limit	129.16	129.43	2.01
High resolution limit	1.98	5.37	1.98
R _{merge} (all I+ and I-)	0.123	0.061	1.661
R _{meas} (all I+ and I-)	0.129	0.064	1.754
R _{pim} (all I+ and I-)	0.039	0.019	0.560
Total number of obs	1184571	60633	54186
Total number unique	57199	3009	2827
Mean((I)/sd(I))	14.7	51.4	1.2
Completeness	100.0	100.0	100.0
Multiplicity	20.7	20.2	19.2
CC Half	0.999	0.999	0.831
Wilson B Factor (Å²)	34.9		
Model Refinement			
Protein molecules in au	4		
Rwork/Rfree (%)	21.7/23.6		
Number of atoms			
Protein	3321		
Ligand	291		
Water	115		
Mean B factors (Å)			
Protein	50.7		
Ligand	49.2		
Water	42.5		
R.m.s. deviations			
Bond length (Å)	0.01		
Bond angles	1.79		
Ramahandran statistics			
% favoured	98.2		
% allowed	100.0		
% outliers	0		
PDB accession code	8S1R		

Table S3. Observed residual interactions between protomers.

Interactions of protomer I Chain A: promoter II Chain B	Distance (Å)
Thr663 main chain NH: Leu653 main chain C=O	3.0
Glu661 main chain NH: Ser655 main chain C=O	2.9
Ile659 main chain NH: Tyr657 main chain C=O	2.9
Ile659 main chain C=O: Tyr657 main chain NH	2.8
Tyr657 main chain C=O: Ile659 main chain NH	3.0
Tyr657 main chain NH: Ile659 main chain C=O	2.9
Ser655 main chain C=O: Glu661 main chain NH	3.0
Leu653 main chain C=O: Thr663 main chain NH	2.9
Interactions of protomer I Chain A: promoter III Chain G	Distance (Å)
Glu707 main chain OH: Ser ⁻¹ side chain OH	3.1
Interactions of protomer III Chain C: promoter IV Chain D	Distance (Å)
Arg713 side chain NH: Gln667 main chain C=O	3.2
Gln667 main chain C=O: Ser671 side chain NH	2.9
Met750 side chain CH: Glu707 side chain C=O	3.3
Leu665 main chain NH: Gly708 main chain C=O	2.9

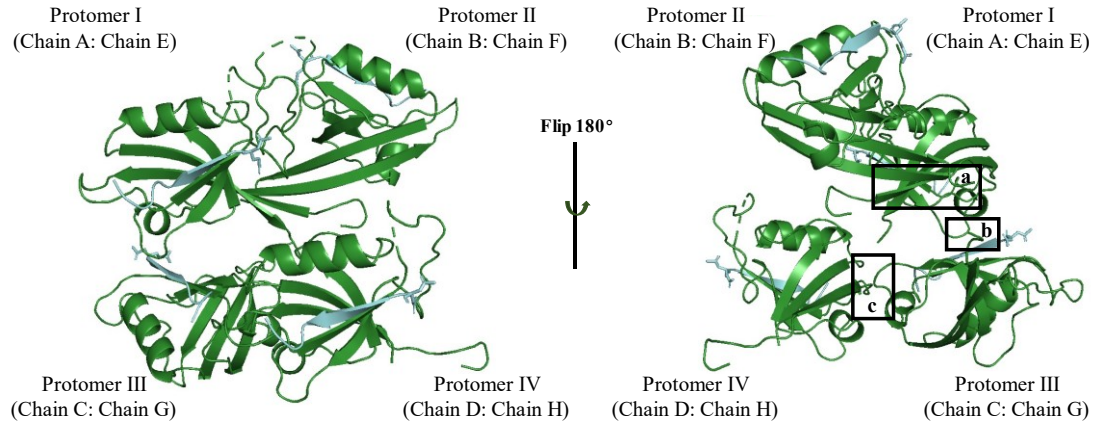


Figure S4. Observed complex of four SHANK1/Ac-EESTSFQGP-NH₂ protomers I, II, III and IV stacking in one asymmetric unit cell.

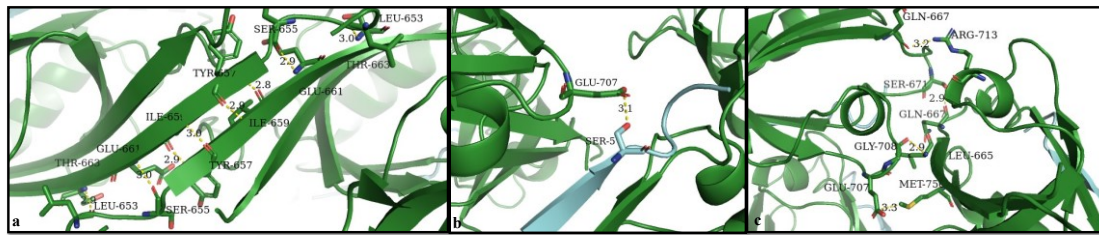


Figure S5. Observed interactions between different protomers: **a.** Antiparallel interaction of β -strands between protomer I and II occurs from residues Leu653^{PDZ}, Ser655^{PDZ}, Tyr657^{PDZ}, Ile659^{PDZ}, Glu661^{PDZ} and Thr663^{PDZ} from Chain A and Chain B (distances of 2.9 – 3.0 Å); **b.** Protomer I interacts with protomer III by forming one hydrogen bond (3.1 Å) between Chain A Glu707^{PDZ} and Chain G Ser(-1); **c.** Protomer III contacts protomer IV by forming four pairs of hydrogen bonds between Chain C residues Arg713^{PDZ}, Gln667^{PDZ}, Met750^{PDZ}, Leu665^{PDZ} and Chain D residues Gln667^{PDZ}, Ser671^{PDZ}, Glu707^{PDZ}, Gly708^{PDZ}.

Table S4. Observed residual interactions between the internal PBM Ac-EESTSFQGP-CONH₂ and SHANK1 PDZ domain.

Interactions	Distance (Å)			
	E-A	F-B	G-C	H-D
Glu ⁻⁵ -Tyr701 ^{PDZ} (Side chain OH to side chain OH)	2.9	3.0	3.3	2.9
Glu ⁻⁵ -Arg679 ^{PDZ} (Side chain C=O to side chain NH)	3.0	-	3.2	-
Glu ⁻⁵ -Arg679 ^{PDZ} (Side chain C=O to side chain NH ₂)	3.1	-	-	-
Glu ⁻⁴ -Gly680 ^{PDZ} (Main chain NH to main chain C=O)	2.9	3.0	3.1	3.3
Glu ⁻⁴ -Gly680 ^{PDZ} (Main chain C=O to main chain NH)	3.0	3.1	3.1	3.0
Glu ⁻⁴ -Arg736 ^{PDZ} (Side chain C=O to side chain NH ₂)	3.2	3.4	-	-
Glu ⁻⁴ -Arg736 ^{PDZ} (Side chain OH to side chain NH ₂)	3.4	2.8	-	-
Glu ⁻⁴ -Arg736 ^{PDZ} (Side chain C=O to side chain NH)	-	3.2	2.6	-
Glu ⁻⁴ -Arg736 ^{PDZ} (Side chain OH to side chain NH)	-	3.3	3.0	-

Ser ⁻³ -Glu703 ^{PDZ} (Side chain OH to side chain C=O)	2.6	2.9	2.6	3.2
Thr ⁻² -Leu678 ^{PDZ} (Main chain NH to main chain C=O)	2.8	2.8	2.8	3.4
Thr ⁻² -Leu678 ^{PDZ} (Main chain C=O to main chain NH)	2.9	2.8	3.0	2.9
Thr ⁻² -His735 ^{PDZ} (Side chain OH to imidazole ring H)	2.5	2.6	2.5	2.8
Ser ⁻¹ -Glu707 ^{PDZ} (Side chain OH to main chain OH)	-			
Phe ⁰ - Phe674 ^{PDZ} (Main chain C=O to main chain NH)	3.1	3.0	3.1	3.0
Phe ⁰ -Gly675 ^{PDZ} (Main chain C=O to main chain NH)	2.9	2.8	2.9	3.0
Phe ⁰ -Phe676 ^{PDZ} (Main chain NH to main chain C=O)	2.7	2.7	2.9	2.8
Gln ¹ -Asp706 ^{PDZ} (Side chain NH to side chain C=O)	3.0	2.9	2.8	3.4

Table S5. RMSD values calculated for different parts of the sequences for the SHANK1/GKAP PBM (grey, PDB code: 1Q3P) and SHANK1/Ac-EESTSFQGP-CONH₂ (green, PDB code: 8S1R) structures.

Superimposed sequence	RMSD (Å)
Full length	0.45
α A	0.097
α B	0.135
β A	0.552
β B	0.110
β C	0.125
β D	0.088
β E	0.029
β F	0.292
Loop V705-G709	0.342
Loop Q667-G675	0.311
Loop G745-T748	0.250
Loop N726-G727	0.025
Loop G680-Q700	0.629
Loop N729-G734	0.094
Loop A714-G719	0.150

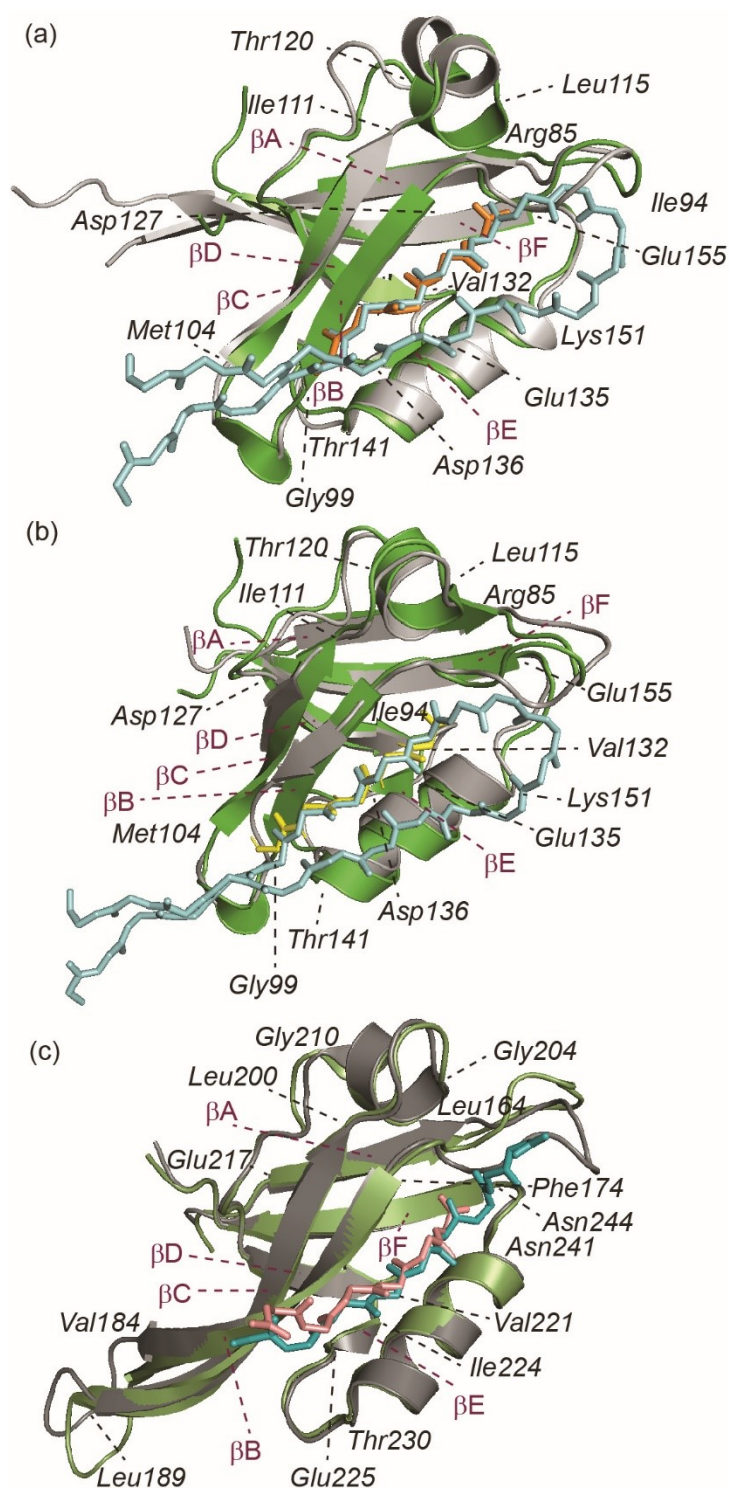


Figure S6. Superimposed crystal structures of (a) Syntrophin PDZ (light grey)/C-terminal PBM (light orange, PDB code: 7QQN) and Syntrophin PDZ (light green)/Internal ligand (light cyan, PDB code: 1QAV) with a full-length calculated RMSD of 0.79 Å; (b) Syntrophin PDZ (light grey)/C-terminal PBM (yellow, PDB code: 2PDZ) and Syntrophin PDZ (light green)/Internal ligand (light cyan, PDB code: 1QAV) with a full-length calculated RMSD of 1.153 Å and (c) Par-6 PDZ (dark grey)/C-terminal PBM (salmon orange, PDB code: 1X8S) and Par-6 PDZ (smudge green)/Internal ligand (teal cyan, PDB code: 1RZX) with a full-length calculated RMSD of 0.542 Å.

Table S6. RMSD values calculated for different parts of the sequences for the Syntrophin PDZ/C-terminal PBM (PDB code: 7QQN) and Syntrophin PDZ/Internal terminal PBM (PDB code: 1QAV) structures.

Superimposed sequence	RMSD (Å)
Full length	0.786
α A	0.160
α B	0.296
β A	0.163
β B	0.337
β C	0.474
β D	0.160
β E	0.000
β F	0.306
Loop R85-I94	2.365
Loop K151-E155	0.489
Loop V132-E135	0.041
Loop D136-T141	0.002
Loop G99-M104 (including α C)	0.157
Loop I111-L115	0.072
Loop T120-D127	0.183

Table S7. RMSD values calculated for different parts of the sequences for the Syntrophin PDZ/C-terminal PBM (PDB code: 2PDZ) and Syntrophin PDZ/Internal terminal PBM (PDB code: 1QAV) structures.

Superimposed sequence	RMSD (Å)
Full length	1.153
α A	0.156
α B	0.362
β A	0.410
β B	0.352
β C	0.601
β D	0.498
β E	0.016
β F	0.421
Loop R85-I94	1.829
Loop K151-E155	0.378
Loop V132-E135	0.054
Loop D136-T141	0.585
Loop G99-M104 (including α C)	0.314
Loop I111-F112	0.427
Loop T120-D127	0.768

Table S8. RMSD values calculated for different parts of the sequences for the Par-6 PDZ/C-terminal PBM (PDB code: 1X8S) and Syntrophin PDZ/Internal terminal PBM (PDB code: 1RZX) structures.

Superimposed sequence	RMSD (Å)
Full length	0.542
α A	0.271
α B	0.281
β A	0.478
β B	0.505
β C	0.443
β D	0.082
β E	0.001
β F	0.210
Loop L164-F174	2.032
Loop N241-N244	0.129
Loop V221-I224	0.072
Loop E225-T230	0.098
Loop V184-L189	0.378
Loop L200-G204	0.291
Loop G210-E217	0.190

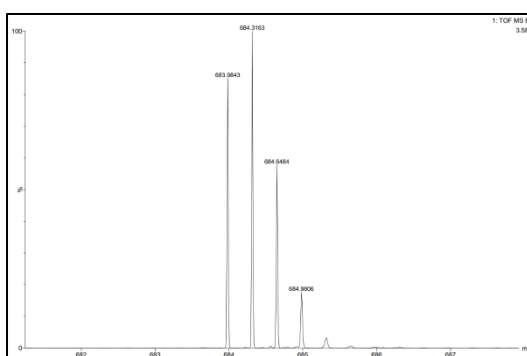
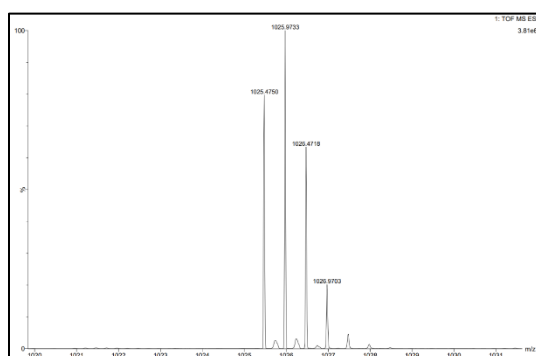
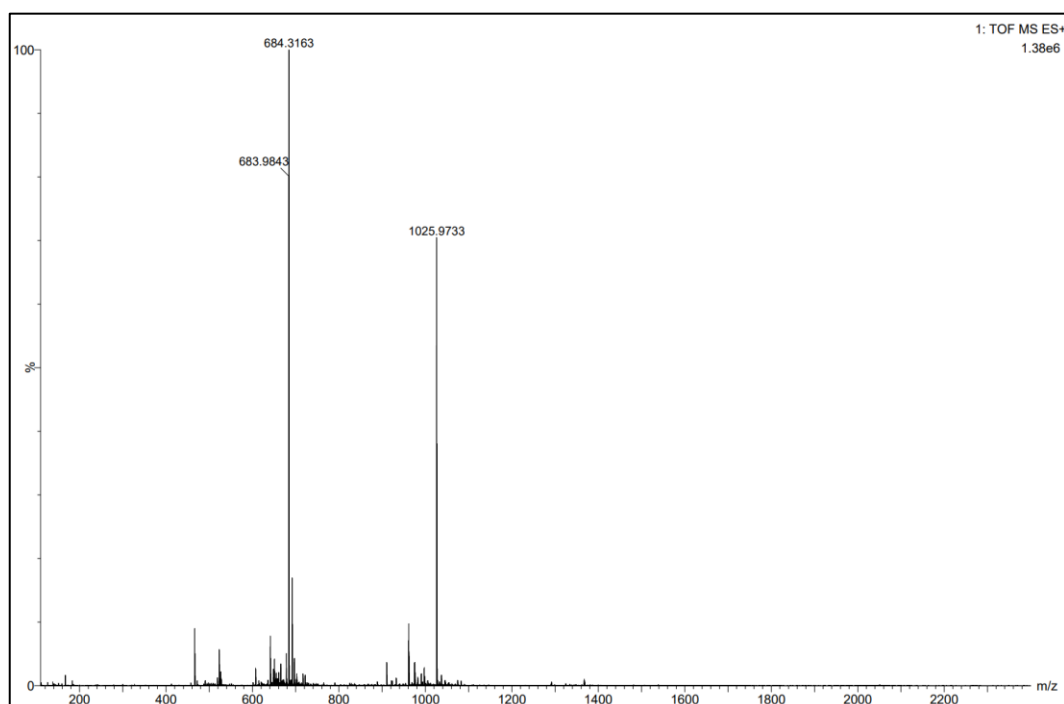
2. Characterisation data

2.1 Mass spectra data of the tested peptides

FAM-Ahx-ELFN1₅₇₉₋₅₉₄

Exact Mass: 2048.9367

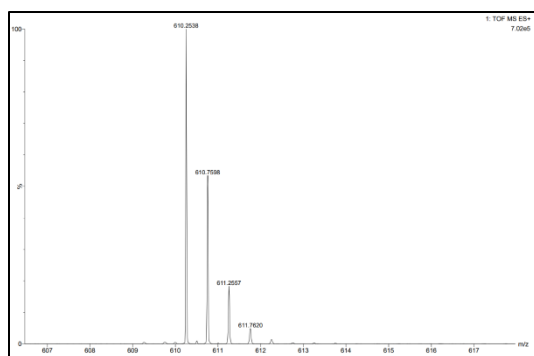
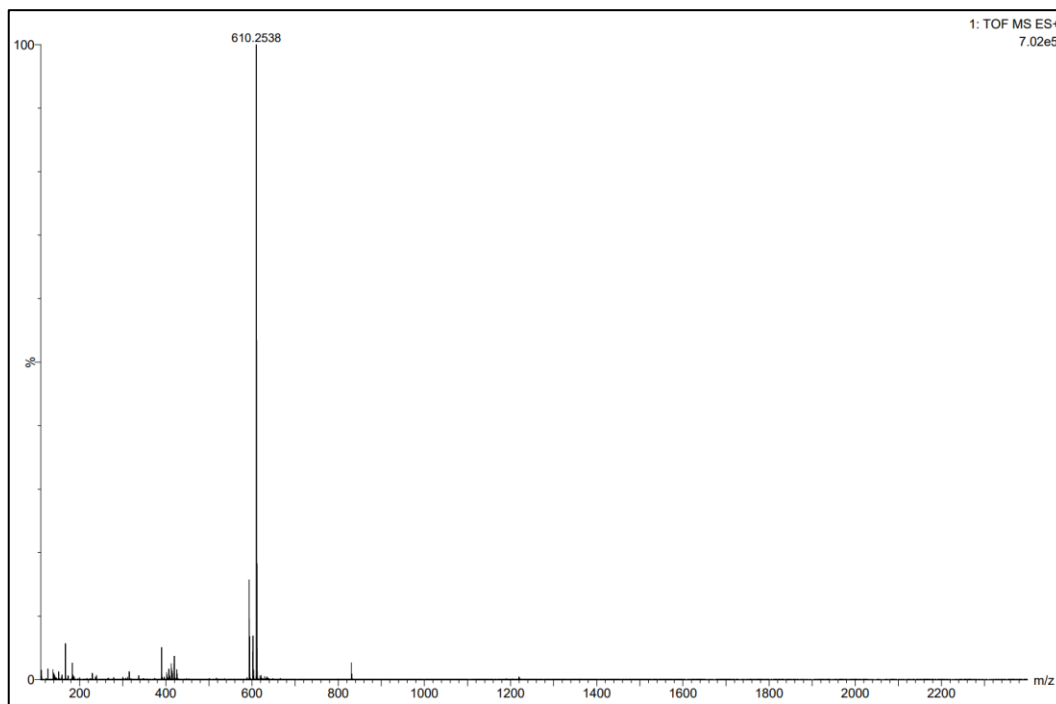
Expected [M+2H] ²⁺	Measured [M+2H] ²⁺
1025.4764	1025.4750
Expected [M+3H] ³⁺	Measured [M+3H] ³⁺
683.9869	683.9843



FITC-Ahx-GKAP-OH

Exact Mass: 1218.5016

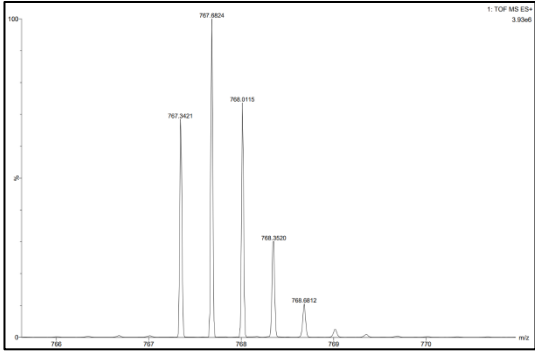
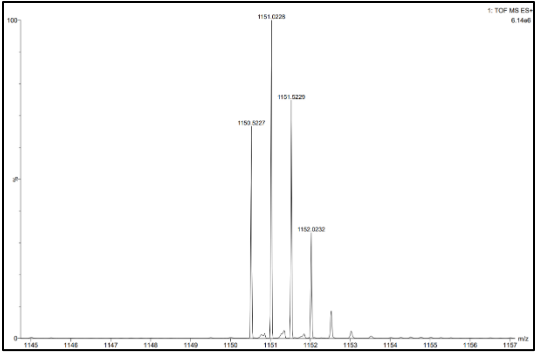
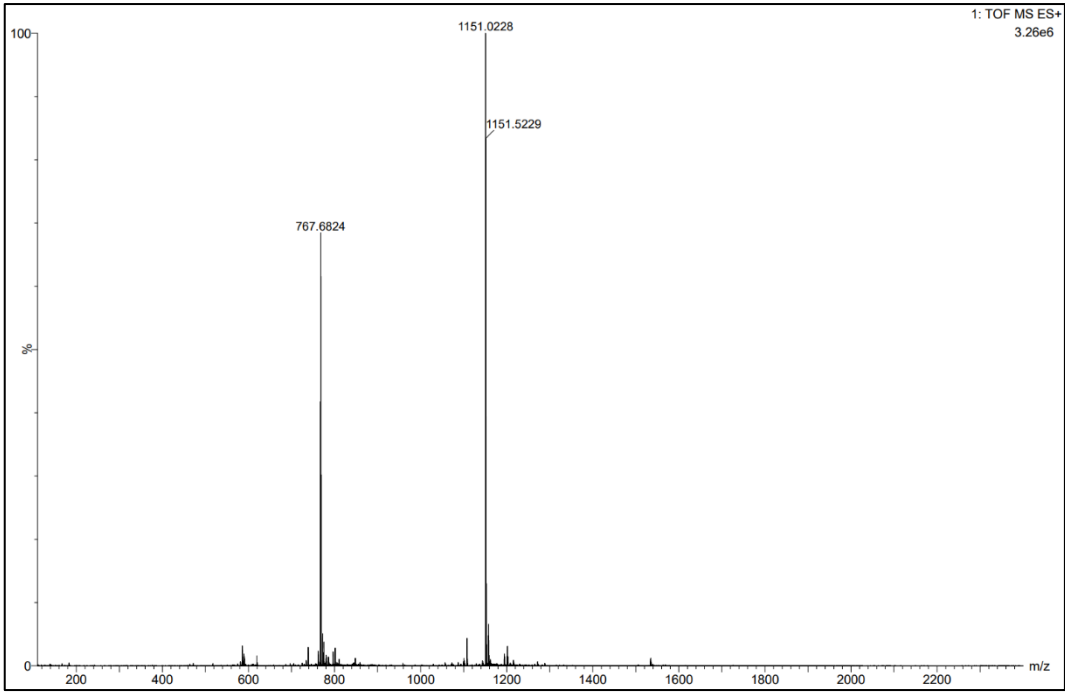
Expected $[M+2H]^+^{2+}$	Measured $[M+2H]^+^{2+}$
610.2588	610.2538



FAM-Ahx-ARAP3₁₄₁₄₋₁₄₂₉

Exact Mass: 2299.0321

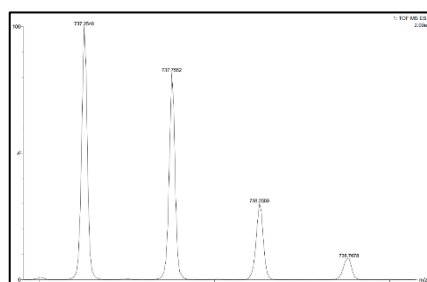
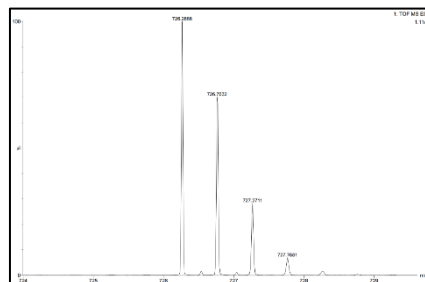
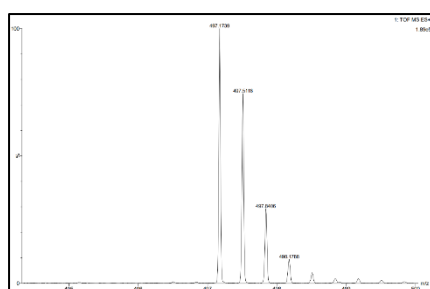
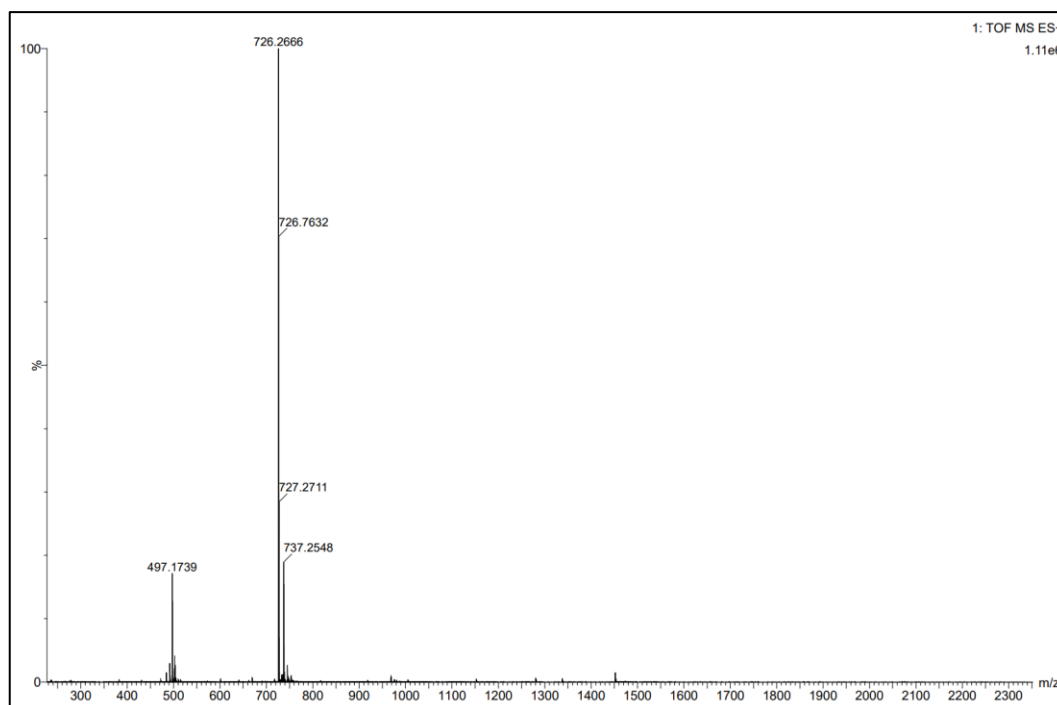
Expected [M+2H] ²⁺	Measured [M+2H] ²⁺
1150.5241	1150.5227
Expected [M+3H] ³⁺	Measured [M+3H] ³⁺
767.3520	767.3421



FAM-Ahx-EESTSFQGF-CONH₂

Exact Mass: 1450.5565

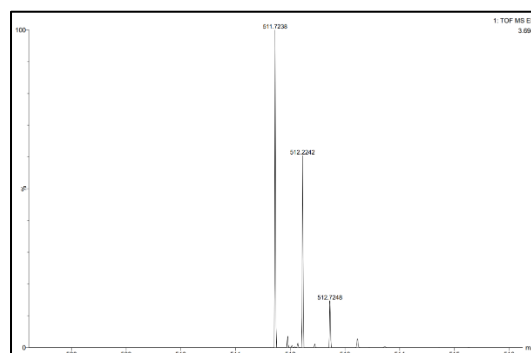
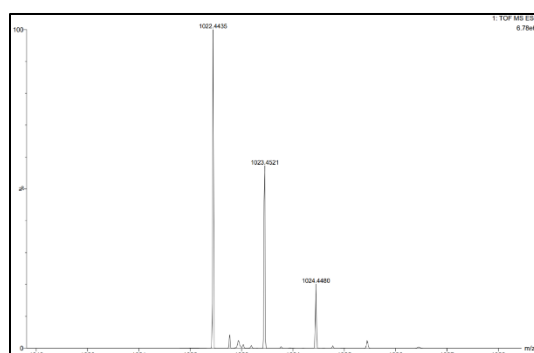
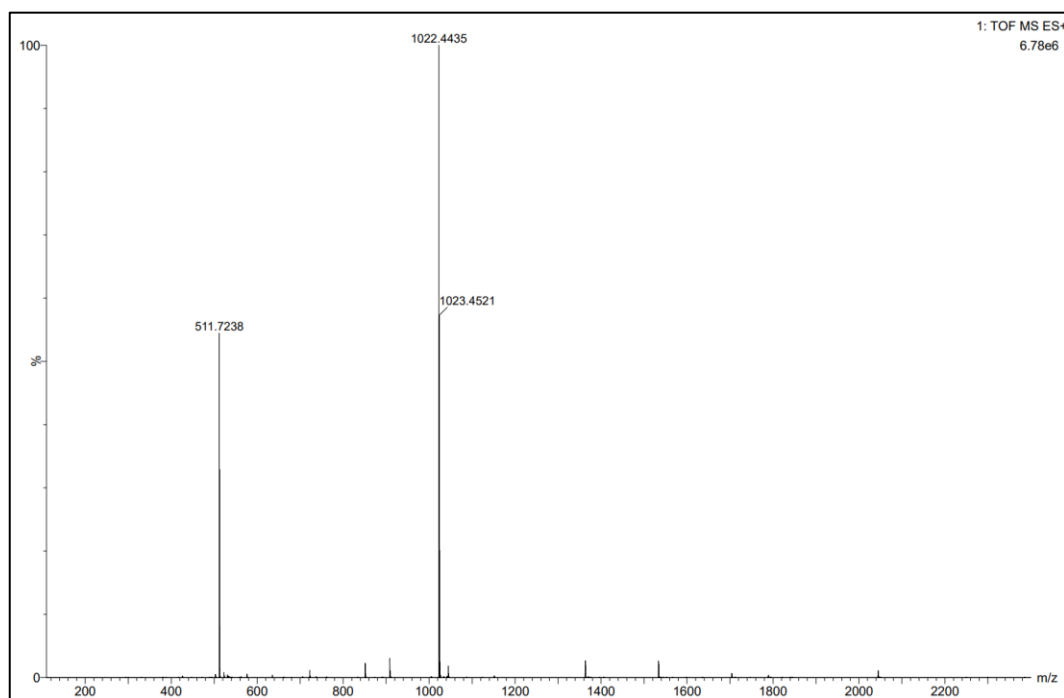
Expected [M+2H]²⁺	Measured [M+2H]²⁺
726.2783	726.2666
Expected [M+H⁺+Na]²⁺	Measured [M+H⁺+Na]²⁺
737.2668	737.2548
Expected [M+2H⁺+K]³⁺	Measured [M+2H⁺+K]²⁺
497.1784	497.1739



Ac-EESTSFQGP-CONH₂

Exact Mass:1021.4353

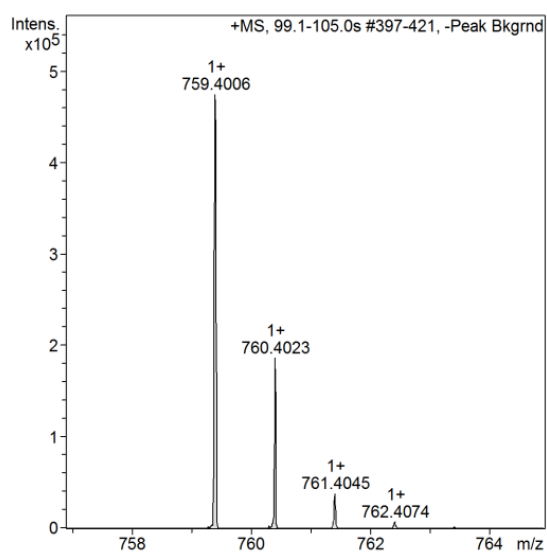
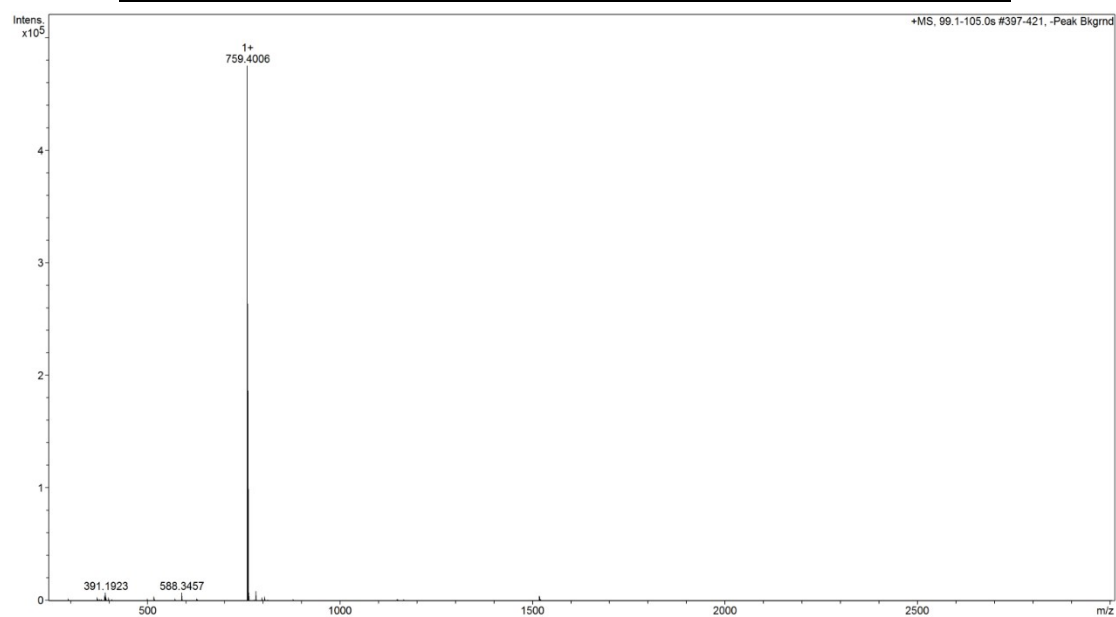
Expected [M+H]⁺	Measured [M+H]⁺
1022.4425	1022.4435
Expected [M+2H]²⁺	Measured [M+2H]²⁺
511.7257	511.7238



Ac-EAQTRL-CONH₂

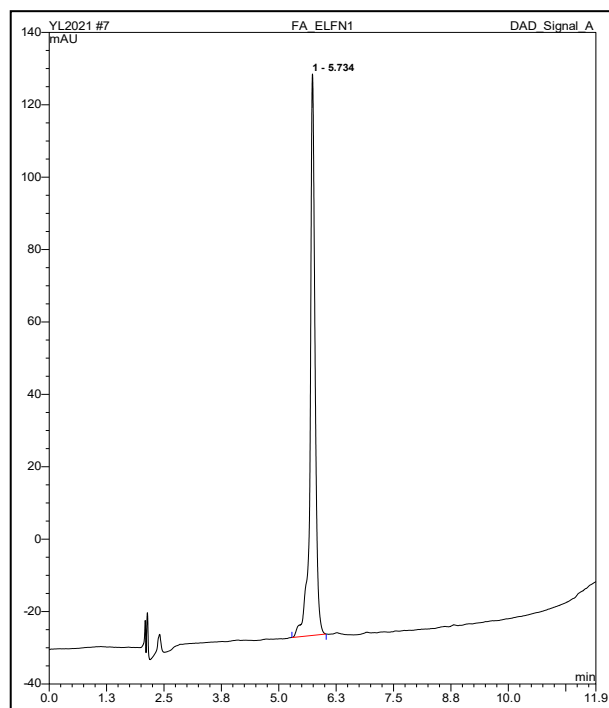
Exact Mass:758.3923

Expected [M+H] ⁺	Measured [M+H] ⁺
759.3995	759.4006

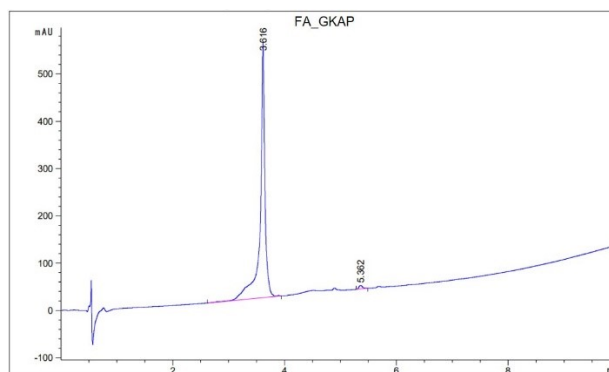


2.2 HPLC analytical purity data of the tested peptides

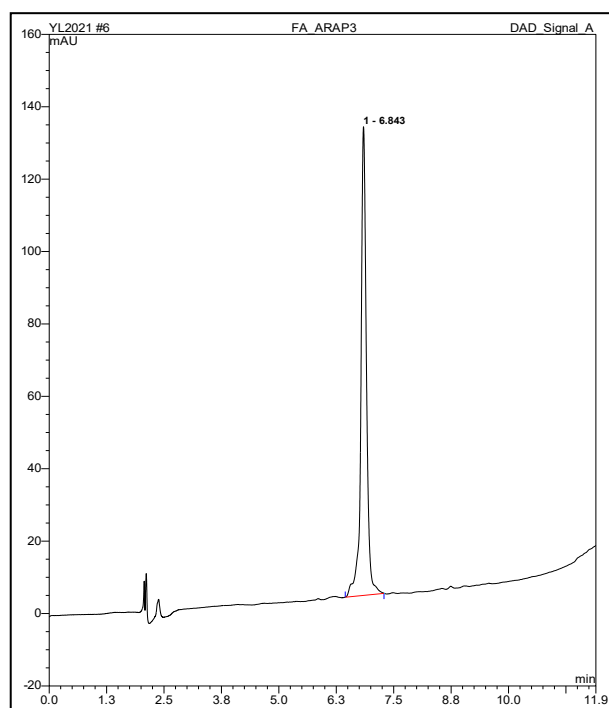
FAM-Ahx-ELFN1₅₇₉₋₅₉₄



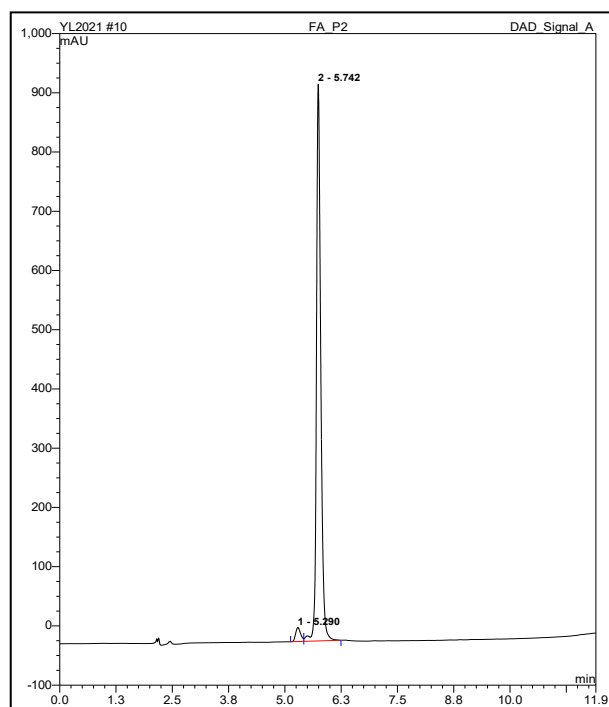
FAM-Ahx-GKAP-OH



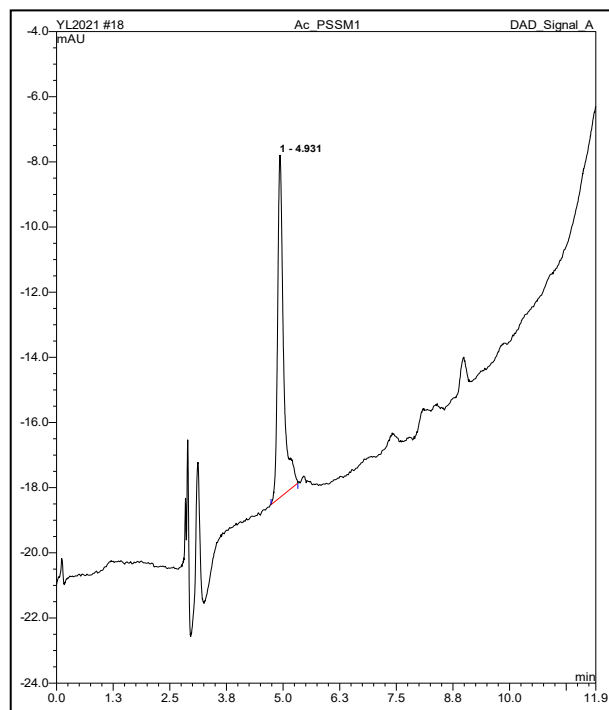
FAM-Ahx-ARAP3₁₄₁₄₋₁₄₂₉



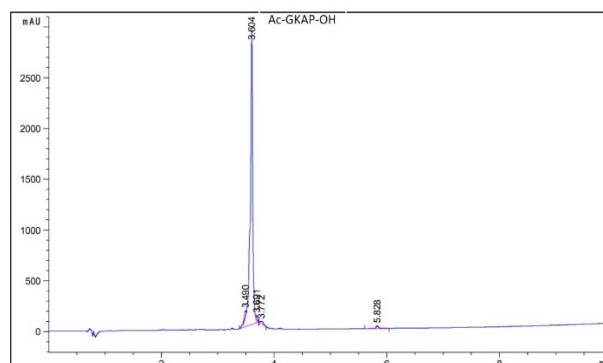
FAM-Ahx-EESTSFQGP-CONH₂



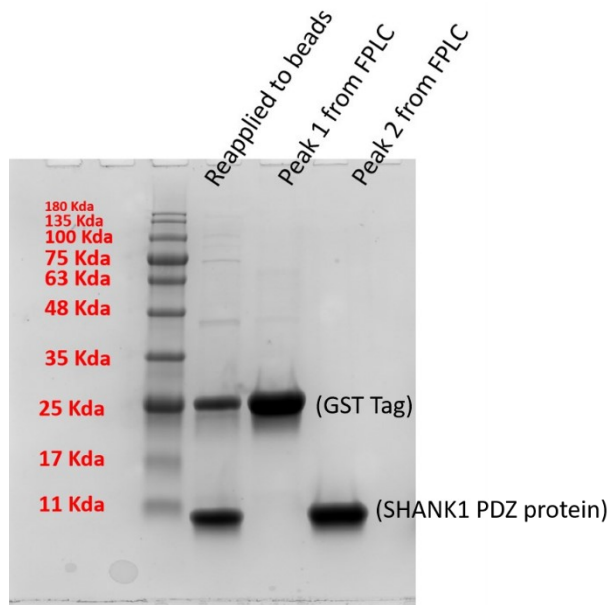
Ac-EESTSFQGP-CONH₂



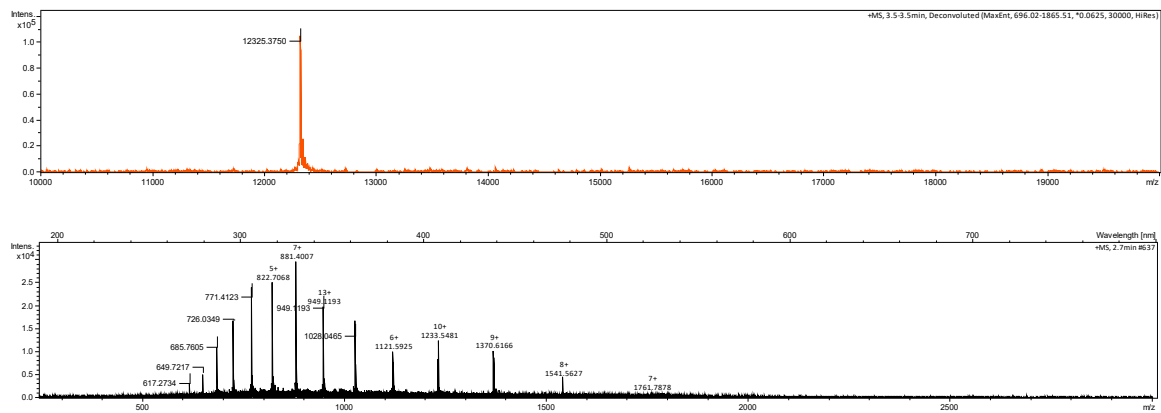
Ac-EAQTRL-CONH₂



2.3 SDS-PAGE gel for the SHANK1 PDZ protein expression and purification



2.4 Mass spectrum of the SHANK1 PDZ protein expression



2.5 Chromatographic conditions for preparative HPLC^a

Time (min)	Mobile phase A (%)	Mobile phase B (%)	Flow (mL/min)
0	90	10	15
20	50	40	15

Time (min)	Mobile phase A (%)	Mobile phase B (%)	Flow (mL/min)
25	20	80	15
30	0	100	15
33	0	100	15
35	90	10	15

^α. Reversed Phase C18 column, mobile phase A (0.1% TFA in water), mobile phase B (0.1% TFA in ACN).

2.6 Equations for data calculation in fluorescent anisotropy direct titration

The intensity and anisotropy were calculated by using Equations 1 and 2. The data was fitted to a sigmoidal logistic model to obtain $r_{\min}$ and $r_{\max}$, and the L_b was further calculated (Equation 3). Finally, the data was fitted to a nonlinear curve model (Equation 4), to obtain the value of K_D .

$$I = (2PG) + S \quad \text{Equation 1}$$

$$r = (S-PG)/I \quad \text{Equation 2}$$

$$L_b = (r - r_{\min}) / [\lambda(r_{\max} - r) + (r - r_{\min})] \quad \text{Equation 3}$$

$$y = \{[k+x+[FL]] - \sqrt{[k+x+[FL]]^2 - 4*[FL]}\} / 2 \quad \text{Equation 4}$$

I = total intensity, r = anisotropy, P = perpendicular intensity, S = parallel intensity, G is an instrument gain factor, L_b = fraction ligand bound, $\lambda = I_{\text{bound}}/I_{\text{unbound}} = 1$, $[FL]$ = concentration of fluorescent ligand, $k = K_D$ and x = [added titrant].

2.7 Equations for data calculation in fluorescent anisotropy competition assays

The calculated average anisotropy values and their standard deviation were fitted using a sigmoidal logistic model (Equation 5).

$$y = r_{\max} + (r_{\min} - r_{\max}) / (1 + (x/x_0)^p) \quad \text{Equation 5}$$

$y = r$ = anisotropy, x_0 = mid-point of the curve between the $r_{\max}$ and $r_{\min}$ plateau.