# Linguistic intuitionistic fuzzy multi-attribute bilateral matching considering satisfaction and fairness degree 

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#### Abstract

Aiming at the multi-attribute bilateral matching problem with unknown attribute weights under a linguistic intuitionistic fuzzy environment, a decision method based on TODIM considering satisfaction and fairness degrees is proposed. First, the theories of linguistic intuitionistic fuzzy sets and bilateral matching are given, and the multi-attribute bilateral matching problem under a linguistic intuitionistic fuzzy environment is described. To solve this problem, according to linguistic intuitionistic fuzzy preference matrices, the overall attribute dominances are calculated based on TODIM; considering group consensus, a new method is proposed to calculate attribute weights based on linguistic intuitionistic fuzzy induced ordered weighted averaging (LIFIOWA) operator; then, the overall dominances of bilateral subjects are obtained by aggregating the overall attribute dominances and attribute weights. Furthermore, the overall dominances are standardized to calculate the satisfaction degrees of bilateral subjects; the fairness degrees of bilateral subjects are calculated considering the loss attenuation coefficient. Based on satisfaction degree matrices, fairness degree matrices and bilateral matching matrices, multiple bilateral matching models are established and then solved to obtain the optimal bilateral matching scheme. Finally, an example shows the effectiveness, reliability and accuracy of the proposed method. The research results indicate the following main characteristics of the proposed method: (1) A new method for calculating the unknown attribute weights using LIFIOWA operator is proposed. (2) According to the TODIM idea, a calculation method for fairness degree considering the loss attenuation coefficient is proposed. (3) Considering satisfaction and fairness degrees, multiple bilateral matching models under a linguistic intuitionistic fuzzy environment are established.


## 1. Introduction

Bilateral matching decision refers to how to use a reasonable matching method to match the bilateral subjects according to their preference information. In real life, there are many bilateral matching problems, such as stable ride-sharing matching [1], person-position matching [2], matching between hospitals and patients [3], venture capital [4], volunteer allocation for emergency tasks [5]. Additionally, scholars have carried out a lot of research on the stability of bilateral matching [6], matching mechanism and related theories [7,8]. Considering that the choice of bilateral matching scheme directly affects the improvement of the satisfaction

[^0]degree of the matching subjects, thus the research on bilateral matching theories and methods has important theoretical and practical significance.

In actual decision environment, due to the complexity of the decision problem and the cognitive differences of people, it is difficult for decision makers to express their preferences for objective things with clear and specific values. Therefore, it is inevitable to introducing fuzzy information into the bilateral matching decision. In the process of bilateral matching decision, different types of fuzzy evaluation information are often provided by the bilateral subjects, such as intuitionistic fuzzy sets, hesitant fuzzy sets and linguistic term sets [9-11]. Among them, linguistic intuitionistic fuzzy sets can consider the membership degree, non-membership degree and hesitation degree of linguistic evaluation information at the same time, and reflect the fuzziness of bilateral decision process [12]. Many scholars have applied linguistic intuitionistic fuzzy set theories into problems of group decision, multi-criteria decision and multi-attribute decision [13-15]. Thus, linguistic intuitionistic fuzzy sets are also used to express preferences of subjects in bilateral matching decision.

In bilateral matching decision, there are few studies on psychological behaviors of bilateral subjects. TODIM is a decision method based on the prospect theory [16] considering psychological behaviors of decision makers, which can better express preferences of decision makers by comparing all alternatives. It has been well developed and applied in various fields. For example, Jiang et al. (2017) proposed a new interval TODIM method to solve the I-multi-attribute decision problem, which considers behavioral characteristics of decision makers [17]. Xu et al. (2020) proposed a new method based on PROMETHEE and TODIM to solve the multi-attribute decision problem under the single-valued neutrosophic environment [18]. Thus, TODIM is used to solve the considered linguistic intuitionistic fuzzy bilateral matching decision problem.

In addition, the determination of attribute weights has always been a concern in multi-attribute decision. Many scholars have made some research on the theory and method of multi-attribute decision with the linguistic preference information. For example, Liu et al. (2020) proposed an approach for uncertain multi-attribute group decision making based on linguistic-valued intuitionistic fuzzy preference relations [19]. Garg and Kaur (2018) proposed a new measure to measure the fuzzy degree of intuitionistic fuzzy sets, and applied it into multi-attribute decision making in an intuitionistic fuzzy set environment [20]. Darko et al. (2023) developed a novel decision evaluation model and multi-attribute decision-making with probabilistic linguistic information to identify m-payment usage attributes and utilize these attributes [21]. Yu (2024) established a novel multi-objective decision model for the grade assessment of network security situation based on the two-tuple linguistic operator [22]. From the above reference, it can be known that the linguistic aggregation operator has a great significance on multi-attribute bilateral decision. However, these methods with different linguistic information are not applicable to the linguistic intuitionistic fuzzy multi-attribute bilateral decision involved in this paper. Especially, in Ref. [22], the two-tuple linguistic operator is proposed and a grade assessment decision model is established, which cannot be directly used to solve the considered problem in this paper. Thus, the determination of attribute weights under a linguistic intuitionistic fuzzy environment needs more attention.

In summary, research motivations of this study are as follows: (1) The application of linguistic intuitionistic fuzzy sets in bilateral matching decision is still imperfect. (2) In the bilateral matching decision making, utilization of TODIM method that considers the psychological behavior of bilateral subjects is worth more attention. (3) In the linguistic intuitionistic fuzzy bilateral matching environment, the determination for attribute weights is not perfect. (4) The bilateral matching decision model under a linguistic intuitionistic fuzzy environment can express the uncertainty and ambiguity of decision process more flexibly and in detail. Therefore, it is necessary to develop bilateral matching decision models under a linguistic intuitionistic fuzzy environment.

Main contributions of this paper are as follows: (1) A multi-attribute bilateral matching decision method considering satisfaction and fairness degrees under a linguistic intuitionistic fuzzy environment is explored, which provides theoretical and practical references for solving linguistic intuitionistic fuzzy bilateral matching problems. (2) Calculation for satisfaction degree under a linguistic intuitionistic fuzzy environment is developed based on TODIM, which can well reflect subjects' preferences. (3) An unknown attribute weight calculation method is proposed based on the linguistic intuitionistic fuzzy induced ordered weighted averaging (LIFIOWA) operator, which can well reflect the group consistency of subjects. (4) Multiple bilateral matching models under a linguistic intuitionistic fuzzy environment are established, which considers satisfaction and fairness degrees of bilateral subjects.

In view of this, a linguistic intuitionistic fuzzy multi-attribute bilateral matching decision method considering satisfaction and fairness degrees is proposed. According to the TODIM idea, the overall attribute dominances of the bilateral subjects are obtained. Considering the consistency of group opinions, a new method is proposed to calculate the weights of unknown attributes by using LIFIOWA operator. Then the global dominance of bilateral subjects is obtained by aggregating the overall attribute dominance and attribute weight. According to the overall dominances, the satisfaction degrees are calculated, and then the fairness degree considering the fair attenuation coefficient is calculated. Finally, multiple bilateral matching models under a linguistic intuitionistic fuzzy environment are constructed and solved according to satisfaction and fairness degree matrices, and thus the optimal bilateral matching scheme is obtained.

The remainder of this paper is organized as follows: Section 2 explores some concepts of linguistic intuitionistic fuzzy numbers and bilateral matching. Section 3 describes a multi-attribute bilateral matching problem under a linguistic intuitionistic fuzzy environment. Section 4 presents the bilateral matching decision method under a linguistic intuitionistic fuzzy environment based on TODIM. Section 5 gives steps of linguistic intuitionistic fuzzy bilateral matching decision. Section 6 uses a bilateral matching case to reveal the effectiveness and feasibility of the proposed method and to discuss the sensitivity of the proposed method. Section 7 summarizes this paper.

## 2. Preparatory knowledge

### 2.1. Theory of linguistic intuitionistic fuzzy numbers

Definition 1. [23] Let $S=\left\{s_{\theta} \mid \theta=0,1, \ldots, 2 t\right\}$ be a non-empty discrete uniform linguistic assessment scale set. For linguistic variables $s_{i}, s_{j} \in S$, it satisfies: 1) Regularity: if $i \geq j$, then $s_{i} \geq s_{j} ; 2$ ) inverse operation: if $\operatorname{neg}\left(s_{i}\right)=s_{j}$, then $i+j=2 t$. The algorithm of linguistic assessment scale is defined as: 1) $s_{i} \oplus s_{j}=s_{i+j}$;2) $\lambda s_{i}=s_{\lambda i}$ and $\lambda \in[0,1]$;3) if $i>j$, then $s_{i}>s_{j}$.
Definition 2. [24] Let $\mu_{a}=s_{\mu_{a}}, v_{a}=s_{v_{a}} ; s_{\mu_{a}}, s_{v_{a}} \in S=\left\{s_{\theta} \mid \theta=0,1, \ldots, 2 t\right\}$. If $s_{0} \leq s_{\mu_{a}} \oplus s_{v_{a}} \leq s_{2 t}$, then $a=\left(\mu_{a}, v_{a}\right)$ is called a linguistic intuitionistic fuzzy number, where $\mu_{a}$ and $v_{a}$ are a linguistic membership degree and a linguistic non-membership degree respectively, and $s_{2 t}-\mu_{a}-v_{a}$ is a linguistic hesitation degree.

This paper studies the linguistic intuitionistic fuzzy numbers. For the convenience of description, $a$ and $b$ are called the abbreviation of $a=\left(\mu_{a}, v_{a}\right)$ and $b=\left(\mu_{b}, v_{b}\right)$. For example, considering the ordered linguistic term assessment scale set $S=\left\{s_{0}\right.$ : extremely poor; $s_{1}$ : very poor; $s_{2}$ : poor; $s_{3}$ : middle-lower; $s_{4}$ : middle; $s_{5}$ : middle-upper; $s_{6}$ : good; $s_{7}$ : very good; $s_{8}$ : extremely good\}, a linguistic intuitionistic fuzzy evaluation of an enterprise to a candidate under the attribute 'personal quality' is ( $s_{6}, s_{1}$ ), then the satisfaction degree of enterprise to the candidate is $s_{6}$, and the dissatisfaction degree of enterprise to the candidate is $s_{1}$.
Definition 3. [25] Let $a_{1}=\left(\mu_{a_{1}}, v_{a_{1}}\right)$ and $a_{2}=\left(\mu_{a_{2}}, v_{a_{2}}\right)$ be linguistic intuitionistic fuzzy numbers, where $\mu_{a_{1}}=s_{i}, v_{a_{1}}=s_{j}, \mu_{a_{2}}=$ $s_{m}, v_{a_{2}}=s_{n}$, and $s_{i}, s_{j}, s_{m}, s_{n} \in S$, then the algorithm between $a_{1}$ and $a_{2}$ is as follows:

1) $a_{1} \oplus a_{2}=\left(s_{f\left(\mu_{a_{1}}\right)+f\left(\mu_{a_{2}}\right)-f\left(\mu_{a_{1}}\right) \times f\left(\mu_{a_{2}}\right)}, s_{f\left(v_{a_{1}}\right) \times f\left(v_{a_{2}}\right)}\right)$,
2) $a_{1} \otimes a_{2}=\left(s_{f\left(\mu_{a_{1}}\right) \times f\left(\mu_{a_{2}}\right)}, s_{f\left(v_{a_{1}}\right)+f\left(v_{a_{2}}\right)-f\left(v_{a_{1}}\right) \times f\left(v_{a_{2}}\right)}\right)$,
3) $\lambda a_{1}=\left(s_{1-\left(1-f\left(\mu_{a_{1}}\right)\right)^{2}}, s_{f\left(v_{a_{1}}\right)^{\lambda}}\right)$,
4) $a_{1}^{\lambda}=\left(s_{f\left(\mu_{a_{1}}\right)^{\lambda}}, s_{1-\left(1-f\left(v_{a_{1}}\right)\right)^{\lambda}}\right)$,

Where $f\left(\mu_{a_{1}}\right)=\frac{i}{2 t}, f\left(v_{a_{1}}\right)=\frac{j}{2 t}, f\left(\mu_{a_{1}}\right)=\frac{m}{2 t}, f\left(v_{a_{1}}\right)=\frac{n}{2 t}$, $f\left(s_{\theta}\right)=\frac{\theta}{2 t}(\theta=0,1, \ldots, 2 t)$ is a linguistic scale function.
Definition 4. [26] Let $S=\left\{s_{\theta} \mid \theta=0,1, \ldots, 2 t\right\}$ be a linguistic assessment scale set, and $a_{1}=\left(\mu_{a_{1}}, v_{a_{1}}\right)$ and $a_{2}=\left(\mu_{a_{2}}, v_{a_{2}}\right)$ be linguistic intuitionistic fuzzy numbers; then, the distance and the similarity measure between $a_{1}$ and $a_{2}$ are respectively as follows:

$$
\begin{align*}
& D\left(a_{1}, a_{2}\right)=\frac{1}{2}\left[\left|f\left(s_{\mu_{1}}\right)-f\left(s_{\mu_{2}}\right)\right|+\left|f\left(s_{v_{1}}\right)-f\left(s_{v_{2}}\right)\right|+\left|f\left(s_{\pi_{1}}\right)-f\left(s_{\pi_{2}}\right)\right|\right]  \tag{1}\\
& P\left(a_{1}, a_{2}\right)=1-\frac{1}{2}\left(\left|s_{\mu_{a_{1}}}-s_{\mu_{a_{2}}}\right|+\left|s_{v_{a_{1}}}-s_{v_{a_{2}}}\right|+\left|s_{\pi_{a_{1}}}-s_{\pi_{a_{2}}}\right|\right) . \tag{2}
\end{align*}
$$

Definition 5. [27] Let $S=\left\{s_{\theta} \mid \theta=0,1, \ldots, 2 t\right\}$ be a linguistic assessment scale set, and $a=\left(\mu_{a}, v_{a}\right)$ be a linguistic intuitionistic fuzzy number. The score function and the exact function are respectively as follows:

$$
\begin{align*}
& R(a)=f\left(s_{\mu_{a}}\right)-f\left(s_{v_{a}}\right),  \tag{3}\\
& Q(a)=f\left(s_{\mu_{a}}\right)+f\left(s_{v_{a}}\right) . \tag{4}
\end{align*}
$$

For linguistic intuitionistic fuzzy numbers $a_{1}=\left(\mu_{a_{1}}, v_{a_{1}}\right)$ and $a_{2}=\left(\mu_{a_{2}}, v_{a_{2}}\right)$, the comparison rules of $a_{1}$ and $a_{2}$ are as follows:

1) If $R\left(a_{1}\right)>R\left(a_{2}\right)$, then $a_{1}>a_{2}$;
2) if $R\left(a_{1}\right)<R\left(a_{2}\right)$, then $a_{1}<a_{2}$;
3) when $R\left(a_{1}\right)=R\left(a_{2}\right)$, if $Q\left(a_{1}\right)=Q\left(a_{2}\right)$, then $a_{1}=a_{2}$; if $Q\left(a_{1}\right)>Q\left(a_{2}\right)$, then $a_{1}>a_{2}$; if $Q\left(a_{1}\right)<Q\left(a_{2}\right)$, then $a_{1}<a_{2}$.

Definition 6. [28] Let $a_{k}=\left(\mu_{a_{k}}, v_{a_{k}}\right)(k=1,2, \ldots, \sigma)$ be a set of linguistic intuitionistic fuzzy numbers, and $\omega_{k}(k=1,2, \ldots, \sigma)$ be its corresponding weight, where $0 \leq \omega_{k} \leq 1$ and $\sum_{k=1}^{\sigma} \omega_{k}=1$. The linguistic intuitionistic fuzzy weighted averaging (LIFWA) operator is calculated as follows:

$$
\operatorname{LIFWA}\left(a_{1}, a_{2}, \ldots, a_{\sigma}\right)=\sum_{k=1}^{\sigma} \omega_{k} a_{k}=\left(\begin{array}{c}
s  \tag{5}\\
\left.1-\prod_{k=1}^{\sigma}\left(1-f\left(\mu_{a_{k}}\right)\right)^{\omega_{k}}, s \prod_{k=1}^{\sigma} f\left(v_{a_{k}}\right)^{\omega_{k}}\right) . . . ~ . ~
\end{array}\right.
$$

Based on the idea of [29], the definition of LIFIOWA operator is given.
Definition 7. Let $a_{k}=\left(\mu_{k}, v_{k}\right)(k=1,2, \ldots, \sigma)$ be a set of linguistic intuitionistic fuzzy numbers, and $\omega_{k}(k=1,2, \ldots, \sigma)$ be its corresponding weight, satisfying $0 \leq \omega_{k} \leq 1$ and $\sum_{k=1}^{s} \omega_{k}=1$. Let $u_{k}$ be the induced value of $\widetilde{a}_{k}$, and $\widetilde{a}_{k}=\left(\mu_{\tilde{a}_{k}}, v_{\tilde{a}_{k}}\right)(k=1,2, \ldots, \sigma)$ be the
linguistic intuitionistic fuzzy number pair corresponding to the $k$-th large element $u_{k}$ in the LIFIOWA operator. Then the LIFIOWA operator is calculated as follow:

$$
\begin{equation*}
\operatorname{LIFIOWA}\left(\left\langle u_{1}, \tilde{a}_{1}\right\rangle,\left\langle u_{2}, \widetilde{a}_{2}\right\rangle, \ldots,\left\langle u_{\sigma}, \widetilde{a}_{\sigma}\right\rangle\right)=\sum_{k=1}^{\sigma} \omega_{k} \widetilde{a}_{k}=\binom{s}{1-\prod_{k=1}^{\sigma}\left(1-f\left(\mu_{\tilde{a}_{k}}\right)\right)^{\omega_{k}}, \prod_{k=1}^{\sigma} f\left(v_{\tilde{a}_{k}}\right)^{\omega_{k}}} \tag{6}
\end{equation*}
$$

where the weighted vector is set to meet the characteristics from large to small. The smaller the order value $u_{k}$ is, the greater the role of the decision maker in the group is, and the greater the weight $\omega_{k}$ is.

### 2.2. Bilateral matching

Let $\partial=\left(\partial_{1}, \partial_{2}, \ldots, \partial_{h}\right)$ be one subject set, and $\ell=\left(\ell_{1}, \ell_{2}, \ldots, \ell_{t}\right)$ be the other subject set, where $\partial_{i}$ is the $i$-th subject in set $\partial$, and $\ell_{j}$ is the $j$-th subject in set $\ell$, where $H=\{1,2, \ldots, h\}, T=\{1,2, \ldots, t\}, h \leq t$.

Definition 8. [30] Assume that $\wp: \partial \cup \ell \rightarrow \partial \cup \ell$ is a mapping. If the mapping $\wp$ meets these conditions: 1) $\wp\left(\partial_{i}\right) \in \ell$; 2) $\wp\left(\partial_{i}\right) \in \partial \cup$ $\left\{\ell_{j}\right\}$; 3) $\wp_{0}\left(\partial_{i}\right)=\ell_{j}$ if and only if $\wp_{0}\left(\ell_{j}\right)=\partial_{i}$, then $\wp$ is called a bilateral matching.

In Definition $8, \wp\left(\partial_{i}\right)=\ell_{j}$ (or $\left(\partial_{i}, \ell_{j}\right)$ ) represents $\partial_{i}$ and $\ell_{j}$ are matched and $\wp\left(\ell_{j}\right)=\ell_{j}$ (or $\left(\ell_{j}, \ell_{j}\right)$ ) represents $\ell_{j}$ is unmatched (single).


Fig. 1. Solution idea of linguistic intuitionistic fuzzy multi-attribute bilateral matching decision
Note: The calculation process of the unknown attribute weight vectors $\omega^{c}=\left(\omega_{1}^{c}, \omega_{2}^{c}, \ldots, \omega_{p}^{c}\right)$ and $\omega^{d}=\left(\omega_{1}^{d}, \omega_{2}^{d}, \ldots, \omega_{q}^{d}\right)$ is as follows: According to the linguistic intuitionistic fuzzy matrices $\widetilde{\boldsymbol{A}}^{\left(\partial_{k}\right)}=\left[\tilde{a}_{i j}^{k}\right]_{t \times p}$ and $\widetilde{\boldsymbol{B}}^{\left(/{ }_{i}\right)}=\left[\widetilde{b}_{k g}^{i}\right]_{h \times q}$, the group opinion matrices $\boldsymbol{R}^{(\partial)}=\left[r_{\tilde{a}_{i j}}\right]_{t \times p}$ and $\boldsymbol{R}^{(\rho)}=\left[r_{\tilde{b}_{i j}}\right]_{h \times q}$ are calculated by using LIFIOWA operator; and then the group opinion score matrices are obtained by Eqs. (14) and (19); lastly the attribute weights are calculated by Eqs. (15) and (20). The specific calculation method is shown in Section 4.3.

## 3. Description of multi-attribute bilateral matching problem under a linguistic intuitionistic fuzzy environment

In the problem of multi-attribute bilateral matching under a linguistic intuitionistic fuzzy environment, let $\partial=\left\{\partial_{1}, \partial_{2}, \ldots, \partial_{h}\right\}$ and $\ell=\left\{\ell_{1}, \ell_{2}, \ldots, \ell_{t}\right\}$ be sets of bilateral subjects, where $\partial_{k}$ represents the $k$-th subject in set $\partial$ and $\ell_{i}$ represents the $i$-th subject in set $\ell$. Let $C=\left\{c_{1}, c_{2}, \ldots, c_{p}\right\}$ be the attribute set of side $\partial$ to side $\ell$, and $D=\left\{d_{1}, d_{2}, \ldots, d_{q}\right\}$ be the attribute set of side $\ell$ to side $\partial$, where $c_{j}$ represents the $j$-th attribute in set $C$ and $d_{g}$ represents the $g$-th attribute in set $D$. Let $\omega^{c}=\left(\omega_{1}^{c}, \omega_{2}^{c}, \ldots, \omega_{p}^{c}\right)$ be the weight vector of the attribute set $C$, and $\omega^{d}=\left(\omega_{1}^{d}, \omega_{2}^{d}, \ldots, \omega_{q}^{d}\right)$ be the weight vector of the attribute set $D$, where the weight vector $\omega^{c}$ and $\omega^{d}$ are unknown. The linguistic assessment scale set $S=\left\{s_{1}, s_{2}, \ldots, s_{\tau}\right\}$ is considered in this paper. $\widetilde{\boldsymbol{A}}^{\left(\partial_{k}\right)}=\left[\tilde{a}_{i j}^{k}\right]_{t \times p}$ is set as the multi-attribute linguistic intuitionistic fuzzy matrix of subject $\partial_{k}$ to subject $\ell_{i}$ under the attribute $c_{j}$, where the linguistic intuitionistic fuzzy number $\tilde{a}_{i j}^{k}=\left(\mu_{\tilde{a}_{i j}}\right.$, $\left.v_{\tilde{a}_{i j}^{k}}\right), \mu_{\tilde{a}_{i j}^{k}}$ represents the satisfaction degree of subject $\partial_{k}$ to subject $\ell_{i}$ under the attribute $c_{j}$, and $v_{\hat{a}_{\hat{a}_{j} k}}$ represents the dissatisfaction degree of subject $\partial_{k}$ to subject $\ell_{i}$ under the attribute $c_{j}, \mu_{\tilde{a}_{i j}^{k}}, v_{\tilde{a}_{i j}^{k}} \in S . \widetilde{\boldsymbol{B}}^{\left(\gamma_{i}\right)}=\left[\widetilde{b}_{k g}^{i}\right]_{h \times q}$ is the linguistic intuitionistic fuzzy matrix of subject $\ell_{i}$ to subject $\partial_{k}$ under the attribute $d_{g}$, where the linguistic intuitionistic fuzzy number $\widetilde{b}_{k g}^{i}=\left(\mu_{\tilde{b}_{k g}^{i}}, v_{\tilde{b}_{k g}}\right), \mu_{\tilde{b}_{k g}^{i}}$ represents the satisfaction degree of subject $\ell_{i}$ to subject $\partial_{k}$ under the attribute $d_{g}$, and $\nu_{\tilde{b}_{k g} i}$ represents the dissatisfaction degree of subject $\ell_{i}$ to subject $\partial_{k}$ under the attribute $d_{g}$.

This paper consider to solve the linguistic intuitionistic fuzzy multi-attribute bilateral matching decision problem according to the linguistic intuitionistic fuzzy matrices $\widetilde{\boldsymbol{A}}^{\left(\partial_{k}\right)}=\left[\tilde{a}_{i j}^{k}\right]_{t \times p}$ and $\widetilde{\boldsymbol{B}}^{(/ i)}=\left[\tilde{b}_{k g}^{i}\right]_{h \times q}$, and weight vectors $\omega^{c}=\left(\omega_{1}^{c}, \omega_{2}^{c}, \ldots, \omega_{p}^{c}\right)$ and $\omega^{d}=\left(\omega_{1}^{d}, \omega_{2}^{d}, \ldots\right.$, $\left.\omega_{q}^{d}\right)$. The procedure of the proposed decision method considering satisfaction and fairness degrees are as follows: First, the overall dominances are calculated based on the TODIM idea, and the attribute weights are calculated by using LIFIOWA operator. Then, the global dominance of bilateral subjects is obtained by aggregating the overall attribute dominance and attribute weight. Third, the satisfaction and fairness degrees are calculated by using the TODIM idea and the fair attenuation coefficients respectively. Finally, multiple bilateral matching models under a linguistic intuitionistic fuzzy environment are constructed and solved to obtain the optimal bilateral matching scheme (see Fig. 1).

## 4. Multi-attribute bilateral matching decision under a linguistic intuitionistic fuzzy environment

### 4.1. Calculation of overall attribute dominances

First, the overall attribute dominances of bilateral subjects are calculated by comparing the individual subjects with all subjects in the other side based on the TODIM idea [31].

For the side $\partial$, when subject $\partial_{k}$ compares subject $\ell_{i}$ with the other subject $\ell_{m}$ of side $\ell$, let $\varphi_{i m}^{k}\left(\widetilde{a}_{i j}^{k}, \tilde{a}_{m j}^{k}\right)$ be the attribute dominance of subject $\ell_{i}$ relative to subject $\ell_{m}$, then $\varphi_{i m}^{k}\left(\widetilde{a}_{i j}^{k}, \tilde{a}_{m j}^{k}\right)$ is calculated as follows:

$$
\varphi_{i m}^{k}\left(\tilde{a}_{i j}^{k}, \tilde{a}_{m j}^{k}\right)=\left\{\begin{array}{l}
\sqrt{d\left(\widetilde{a}_{i j}^{k}, \tilde{a}_{m j}^{k}\right)}, \tilde{a}_{i j}^{k} \geq \tilde{a}_{m j}^{k}, i, m \in T, k \in H  \tag{7}\\
-\frac{1}{\theta} \sqrt{d\left(\widetilde{a}_{i j}^{k}, \tilde{a}_{m j}^{k}\right)}, \quad \tilde{a}_{i j}^{k}<\tilde{a}_{m j}^{k}, i, m \in T, k \in H
\end{array}\right.
$$

In Eq. (7), $d\left(a_{i j}, a_{i k}\right)$ can be calculated by Eq. (1), and the values of $\widetilde{a}_{i j}^{k}$ and $\widetilde{a}_{m j}^{k}$ can be compared by Eqs. (3) and (4) in Definition 5 ; $\theta$ is the loss attenuation coefficient, indicating the degree of loss avoidance. The smaller $\theta$ is, the greater the degree of loss avoidance is. According to reference [32], when $\theta=2.25$, it is most in line with the decision maker's attitude towards risk.

Let $\delta_{i j}^{k}$ be the overall attribute dominance of subject $\partial_{k}$ with respect to subject $\ell_{i}$ to all other subjects of side $\ell$. Then $\delta_{i j}^{k}$ is calculated as follows:

$$
\begin{equation*}
\delta_{i j}^{k}=\sum_{m=1, i \neq m}^{h} \varphi_{i m}^{k}\left(\tilde{a}_{i j}^{k}, \tilde{a}_{m j}^{k}\right), i, m \in T, k \in H . \tag{8}
\end{equation*}
$$

By Eqs. (7) and (8), the overall attribute dominance matrix $\boldsymbol{Z}^{\left(\partial_{k}\right)}=\left[\delta_{i j}^{k}\right]_{t \times p}$ of subject $\partial_{k}$ to subject $\ell_{i}$ under the attribute $C_{j}$ is constructed.

Analogously, for side $\ell$, when subject $\ell_{i}$ compares subject $\partial_{k}$ with the other subject $\partial_{n}$ of side $\partial$, let $\varphi_{k n}^{i}\left(\widetilde{b}_{k g}^{i}, \widetilde{b}_{n g}^{i}\right)$ be the attribute dominance of subject $\partial_{k}$ relative to subject $\partial_{n}$, then $\varphi_{k n}^{i}\left(\widetilde{b}_{k g}^{i}, \widetilde{b}_{n g}^{i}\right)$ is calculated as follows:

$$
\varphi_{k n}^{i}\left(\widetilde{b}_{k g}^{i}, \widetilde{b}_{n g}^{i}\right)=\left\{\begin{array}{l}
\sqrt{d\left(\widetilde{b}_{k g}^{i}, \widetilde{b}_{n g}^{i}\right)}, \quad \widetilde{b}_{k g}^{i} \geq \widetilde{b}_{n g}^{i}, k, n \in H, i \in T  \tag{9}\\
-\frac{1}{\theta} \sqrt{d\left(\widetilde{b}_{k g}^{i}, \widetilde{b}_{n g}^{i}\right)}, \quad \widetilde{b}_{k g}^{i}<\widetilde{b}_{n g}^{i}, k, n \in H, i \in T
\end{array}\right.
$$

Let $\delta_{k n}^{i}$ be the overall attribute dominance of subject $\ell_{i}$ with respect to subject $\partial_{k}$ to all other subjects of side $\partial$, then $\delta_{k n}^{i}$ is calculated as follows:

$$
\begin{equation*}
\delta_{k n}^{i}=\sum_{n=1, k \neq n}^{h} \varphi_{k n}^{i}\left(\widetilde{b}_{k g}^{i}, \widetilde{b}_{n g}^{i}\right), k, n \in H, i \in T \tag{10}
\end{equation*}
$$

By Eqs. (9) and (10), the overall attribute dominance matrix $\boldsymbol{Z}^{\left(i_{i}\right)}=\left[\delta_{k n}^{i}\right]_{h \times q}$ of subject $\ell_{i}$ to subject $\partial_{k}$ under the attribute $d_{g}$ is constructed.

### 4.2. Calculation of attribute weights

To improve the reliability of multi-attribute group opinion aggregation results, some scholars use similarity measures to reflect the overall consistency of individual evaluation and the consistency of each decision scheme under the decision attributes [33]. Therefore, the following method is used to calculate the attribute weights.

According to the linguistic intuitionistic fuzzy matrix $\widetilde{\boldsymbol{A}}^{\left(\partial_{k}\right)}=\left[\tilde{a}_{i j}^{k}\right]_{t \times p}$, let $p_{i j}^{(k n)}$ be the similarity between $\tilde{a}_{i j}^{k}=\left(\mu_{\tilde{a}_{i j}^{k}}, v_{\hat{a}_{i j}^{k}}\right)$ and $\tilde{a}_{i j}^{n}=$ $\left(\mu_{\hat{a}_{i j}^{n}}, v_{\tilde{a}_{i j}^{n}}\right)$, then, $p_{i j}^{(k n)}$ is calculated as follows:

In Eq. (11), the calculation for similarity is extended by Eq. (2).
Let $p_{i j}^{(k)}$ be the mean similarity between subject $\partial_{k}$ and other subjects of side $\partial$ under the attribute $c_{j}$, then $p_{i j}^{(k)}$ is calculated as follows:

$$
\begin{equation*}
p_{i j}^{(k)}=\frac{1}{h-1} \sum_{n=1, k \neq n}^{h} p_{i j}^{(k n)} . \tag{12}
\end{equation*}
$$

Then, the mean value of similarity $p_{i j}^{(k)}$ is calculated by Eqs. (11) and (12), and let it be the induced value of LIFIOWA operator; let $\omega_{k}$ be the attribute weight of $\tilde{a}_{i j}^{k}$, where $\omega_{k}$ can be calculated according to the method proposed in Ref. [2]. The group opinion evaluation value $\widetilde{a}_{i j}^{\partial}$ can be calculated as follow:

In Eq. (13), the calculation for $\tilde{a}_{i j}^{\partial}$ is extended by Eqs. (5) and (6). By Eq. (13), $\widetilde{a}_{i j}^{\partial}$ is obtained by aggregating the evaluation value $\tilde{a}_{i j}^{k}(k=1, \ldots, h)$, and thus a group opinion matrix $\widetilde{\boldsymbol{A}}=\left[\tilde{a}_{i j}^{\partial}\right]_{t \times p}$ of side $\partial$ to $\ell_{i}$ under attribute $c_{j}$ is established.

Furthermore, the group opinion value $\widetilde{a}_{i j}^{\partial}$ is converted into the score value $r_{\tilde{a}_{i j}}$, and thus the group score matrix $\boldsymbol{R}^{(\partial)}=\left[r_{\tilde{a}_{i j}^{\partial}}\right]_{t \times p}$ of side $\partial$ to $\ell_{i}$ is established, where $r_{\tilde{a}_{i j}}$ is calculated as follows:

$$
r_{\tilde{a}_{i j}}=R\left(\tilde{a}_{i j}^{\partial}\right)=f\left(s_{\mu_{\frac{\partial}{\partial}}}^{\tilde{a}_{\tilde{a}_{j}}}\right)-f\left(\begin{array}{c}
s_{v_{\partial}^{\partial}}^{\tilde{a}_{i j}} \tag{14}
\end{array}\right) .
$$

Finally, the score value $r_{\tilde{a}_{i j}}$ is normalized to obtain the attribute weight vector $\omega^{c}=\left(\omega_{1}^{c}, \omega_{2}^{c}, \cdots, \omega_{p}^{c}\right)$, where $\omega_{j}^{c}$ is calculated as follows:

$$
\begin{equation*}
\omega_{j}^{c}=\frac{\sum_{i=1}^{t} r_{\tilde{a}_{i j}}}{\sum_{e=1}^{p} \sum_{i=1}^{t} r_{\partial}} . \tag{15}
\end{equation*}
$$

Analogously, according to the linguistic intuitionistic fuzzy matrix $\widetilde{\boldsymbol{B}}^{\left(\kappa_{i}\right)}=\left[\widetilde{b}_{k g}^{i}\right]_{h \times q}$, let $p_{k g}^{(i m)}$ be the similarity between $\widetilde{b}_{k g}^{i}=\left(\mu_{\tilde{b}_{k g}^{i}}, v_{\tilde{b}_{k g}^{i}}\right)$ and $\widetilde{b}_{k g}^{m}=\left(\mu_{\tilde{b}_{k g}}, v_{\tilde{b}_{k g}^{m}}^{m}\right)$, then $p_{k g}^{(i m)}$ is calculated as follows:

$$
\begin{equation*}
p_{k g}^{(i m)}=P\left(\widetilde{b}_{k g}^{i}, \widetilde{b}_{k g}^{m}\right)=1-\frac{1}{2}\left(\left|s_{\mu_{i_{i}}}-s_{\mu_{k_{k g} m}}\right|+\left|s_{v_{v_{k g}}}-s_{v_{v_{m g} m}}\right|+\left|s_{b_{k_{i g}}}-s_{b_{b_{k g} m}}\right|\right) . \tag{16}
\end{equation*}
$$

Let $p_{k g}^{(i)}$ be the mean similarity between subject $\ell_{g}$ and the other subjects of side $\ell$, then $p_{k g}^{(i)}$ is calculated as follows:

$$
\begin{equation*}
p_{k g}^{(i)}=\frac{1}{t-1} \sum_{m=1, i \neq m}^{t} p_{k g}^{(i m)} . \tag{17}
\end{equation*}
$$

Then, the mean value of similarity $p_{k g}^{(i)}$ is calculated by Eqs. (16) and (17), and let it be the induced value of LIFIOWA operator, and $\omega_{i}$ be the corresponding attribute weight of $\tilde{b}_{k g}^{i}$. The group opinion evaluation value $\tilde{b}_{k g}^{\prime}$ can be calculated as follow:

$$
\begin{equation*}
\widetilde{b}_{k g}^{\prime}=\operatorname{LIFIOWA}\left(\left\langle u_{1}, \widetilde{b}_{k g}^{1}\right\rangle,\left\langle u_{2}, \widetilde{b}_{k g}^{2}\right\rangle, \ldots,\left\langle u_{t}, \widetilde{b}_{k g}^{t}\right\rangle\right)=\sum_{i=1}^{t} \omega_{i} \widetilde{b}_{k_{g}}^{i}=\binom{s}{1-\prod_{i=1}^{t}\left(1-f\left(\mu_{\hat{b}_{k g}}\right)\right)^{\omega_{i}} \prod_{i=1}^{s} \prod_{i}^{t} f\left(v_{b_{k g} i}\right)^{\omega_{i}}} . \tag{18}
\end{equation*}
$$

By Eq. (18), the group opinion evaluation value $\widetilde{b}_{k g}^{\prime}$ is obtained by aggregating the evaluation value $\widetilde{b}_{k g}^{i}(i=1, \ldots, t)$, and thus a group opinion matrix $\widetilde{\boldsymbol{B}}=\left[\widetilde{b}_{k g}^{\prime}\right]_{h \times q}$ of side $\ell$ to $\partial_{k}$ under attribute $d_{g}$ is established.

Furthermore, the group opinion value $\widetilde{b}_{k g}^{\prime}$ is converted into the score value $r_{\tilde{b}_{k g}^{\prime}}$, and thus the group score matrix $\boldsymbol{R}^{(\nearrow)}=\left[r_{\tilde{b}_{k g}^{\prime}}\right]_{h \times q}$ of the side $\ell$ to $\partial_{i}$ is established, where $r_{\tilde{b}_{k g}^{\prime}}$ is calculated as follows:

$$
\begin{equation*}
r_{\tilde{b}_{k g}^{\prime}}=R\left(\widetilde{b}_{k g}^{\prime}\right)=f\left(s_{\mu_{b_{k_{k g}^{\prime}}}}\right)-f\left(s_{v_{b_{k g}}}\right) \tag{19}
\end{equation*}
$$

Finally, the score value $r_{\tilde{b}_{k g}^{\prime}}$ is normalized to obtain the attribute weight vector $\omega^{d}=\left(\omega_{1}^{d}, \omega_{2}^{d}, \ldots, \omega_{q}^{d}\right)$, where $\omega_{g}^{d}$ can be calculated as follows:

$$
\begin{equation*}
\omega_{g}^{d}=\frac{\sum_{k=1}^{t} r_{\tilde{b}_{k g}^{\prime}}}{\sum_{f=1}^{q} \sum_{k=1}^{t} r_{\tilde{b}_{k g}^{\prime}}} \tag{20}
\end{equation*}
$$

### 4.3. Calculation of overall dominances and satisfaction degrees

First, the overall attribute dominance $\delta_{i j}^{k}(k=1, \ldots, h)$ is aggregated to obtain the overall dominance $\delta_{k i}^{\partial}$, and thus the overall dominance matrix $Z^{(\partial)}=\left[\delta_{k i}^{\partial}\right]_{h \times t}$ of side $\partial$ to side $\ell$ is established, where $\delta_{k i}^{\partial}$ is calculated as follows:

$$
\begin{equation*}
\delta_{k i}^{d}=\sum_{j=1}^{p} \omega_{j}^{c} \delta_{i j}^{k} \tag{21}
\end{equation*}
$$

Then, the overall dominance $\delta_{k i}^{\partial}$ is normalized to obtain the satisfaction degree $\alpha_{k i}$ of $\partial_{k}$ to $\ell_{i}$, where $\alpha_{k i}$ is calculated as follows:

$$
\begin{equation*}
\alpha_{k i}=\frac{\delta_{k i}^{\partial}-\frac{h+1}{h} \min _{k \in H, i \in T}\left\{\delta_{k i}^{\partial}\right\}}{\max _{k \in H, i \in T}\left\{\delta_{k i}^{d}\right\}-\frac{h+1}{h} \min _{k \in H, i \in T}\left\{\delta_{k i}^{d}\right\}}, k \in H, i \in T \tag{22}
\end{equation*}
$$

By Eq. (22), the satisfaction degree matrix $\widetilde{\boldsymbol{Z}}^{(\partial)}=\left[\alpha_{i j}\right]_{h \times t}$ of side $\partial$ is constructed.
Analogously, the overall attribute dominance $\delta_{k g}^{i}(i=1, \ldots, t)$ is aggregated to obtain the overall dominance $\delta_{k i}^{\prime}$, and thus the overall dominance matrix $\boldsymbol{Z}^{(\digamma)}=\left[\delta_{k i}^{\ell}\right]_{h \times t}$ of side $\ell$ to side $\partial$ is established, where $\delta_{k i}^{\ell}$ is calculated as follows:

$$
\begin{equation*}
\delta_{k i}^{\prime}=\sum_{g=1}^{q} \omega_{g}^{d} \delta_{k g}^{i} \tag{23}
\end{equation*}
$$

Furthermore, the overall dominance $\delta_{k g}^{\prime}$ is normalized to obtain the satisfaction degree $\beta_{k i}$ of $\ell_{i}$ to $\partial_{k}$, where $\beta_{k i}$ is calculated as follows:

$$
\begin{equation*}
\beta_{k i}=\frac{\delta_{k i}^{\prime}-\frac{t+1}{t} \min _{k \in H, i \in T}\left\{\delta_{k i}^{\prime}\right\}}{\max _{k \in H, i \in T}\left\{\delta_{k i}^{\prime}\right\}-\frac{t+1}{t} \min _{k \in H, i \in T}\left\{\delta_{k i}^{\prime}\right\}}, k \in H, i \in T \tag{24}
\end{equation*}
$$

By Eq. (24), the satisfaction degree matrix $\widetilde{\boldsymbol{Z}}^{(ノ)}=\left[\beta_{k i}\right]_{h \times t}$ of side $\ell$ is constructed.

### 4.4. Calculation of fairness degrees

To get the best matching scheme, on the one hand, it is necessary to maximize the satisfaction degree of bilateral subjects, on the other hand, it is also necessary to consider the fairness degree of bilateral subjects; the greater the satisfaction degree of bilateral subjects is, the greater the success rate of matching is, and the ratio of satisfaction degree determines the degree of the fairness degree. When the satisfaction degree ratio of bilateral subjects is closer to 1 , the greater the matching fairness degree, the greater the probability of matching success.

Let $\wp_{k i}^{d}$ be the relative fairness degree of $\partial_{k}$ to $\ell_{i}, \wp_{k i}^{\prime}$ be the relative fairness degree of $\ell_{i}$ to $\partial_{k}$, and $\tilde{\wp}_{k i}$ be the relative fairness degree between $\partial_{k}$ and $\ell_{i}$. Then, $\varnothing_{k i}^{\partial}, \wp_{k i}^{\prime}$ and $\widetilde{\wp}_{k i}$ are calculated according to the TODIM idea as follows:

$$
\begin{align*}
& \wp_{k i}^{\partial}=\left\{\begin{array}{l}
\sqrt{\frac{\alpha_{k i}}{\beta_{k i}}}, \alpha_{k i}>\beta_{k i}, \\
1, \alpha_{k i}=\beta_{k i}, \\
\frac{1}{\rho} \sqrt{\frac{\alpha_{k i}}{\beta_{k i}}}, \alpha_{k i}<\beta_{k i} ;
\end{array}\right.  \tag{25}\\
& \wp_{k i}^{\prime}=\left\{\begin{array}{l}
\sqrt{\frac{\beta_{k i}}{\alpha_{k i}}}, \beta_{k i}>\alpha_{k i}, \\
1, \beta_{k i}=\alpha_{k i}, \\
\frac{1}{\rho} \sqrt{\frac{\beta_{k i}}{\alpha_{k i}}, \beta_{k i}}<\alpha_{k i} ;
\end{array}\right.  \tag{26}\\
& \tilde{\wp}_{k i}=\left\{\begin{array}{l}
\frac{\wp_{k i}^{d}+\wp_{k i}^{\prime}}{2}, \alpha_{k i} \neq \beta_{k i}, \\
1, \alpha_{k i}=\beta_{k i},
\end{array}\right. \tag{27}
\end{align*}
$$

In Eqs. (25) and (26), $\rho$ is the fair attenuation coefficient, which indicates the degree of fairness loss aversion. The smaller $\rho$ is, the greater the degree of loss aversion is. Then, the relative fairness degree $\widetilde{\wp}_{k i}$ is normalized to obtain the fairness degree $\hbar_{k i}$ of $\partial_{k}$ and $\ell_{i}$, and $\hbar_{k i}$ can be calculated as follows:

$$
\hbar_{k i}=\left\{\begin{array}{l}
\widetilde{\mathscr{~}}_{k i}, \widetilde{\varnothing}_{k i} \leq 1 ;  \tag{28}\\
\frac{1}{\widetilde{\mathscr{\wp}}_{k i}}, \widetilde{\varnothing}_{k i}>1
\end{array}\right.
$$

By Eq. (28), the fairness degree matrix $\overline{\boldsymbol{Z}}=\left[\hbar_{k i}\right]_{h \times t}$ of bilateral subjects is constructed.

### 4.5. Bilateral matching models based on satisfaction degree

First, the matching matrix $\boldsymbol{X}=\left[x_{k i}\right]_{h \times t}$ is introduced, where $x_{k i}=\left\{\begin{array}{l}1, \gamma\left(\partial_{k}\right)=\ell_{i}, \\ 0, \gamma\left(\partial_{k}\right) \neq \ell_{i} \text {. }\end{array}\right.$ Based on the satisfaction degree matrices $\widetilde{\mathbf{Z}}^{(\partial)}=$ $\left[\alpha_{k i}\right]_{h \times t}$ and $\widetilde{\mathbf{Z}}^{(\digamma)}=\left[\beta_{k i}\right]_{h \times t}$, the model of bilateral matching considering satisfaction degree under the one-to-one matching constraint is established as follows:

$$
(\mathrm{M}-1)\left\{\begin{array}{l}
\operatorname{Max} D_{1}=\sum_{k=1}^{h} \sum_{i=1}^{t} \alpha_{k i} x_{k i}, \\
\operatorname{Max} D_{2}=\sum_{k=1}^{h} \sum_{i=1}^{t} \beta_{k i} x_{k i} \\
\text { s.t. } \sum_{i=1}^{t} x_{k i}=1, k \in H \\
\sum_{k=1}^{h} x_{k i} \leq 1, i \in T \\
x_{k i} \in\{0,1\}, k \in H, i \in T
\end{array}\right.
$$

where $\operatorname{Max} D_{1}=\sum_{k=1}^{h} \sum_{i=1}^{t} \alpha_{k i} x_{k i}$ represents maximizing the satisfaction degree of side $\partial$, and $\operatorname{Max} D_{2}=\sum_{k=1}^{h} \sum_{i=1}^{t} \beta_{k i} x_{k i}$ represents maximizing the satisfaction degree of side $\ell$.

For objective functions $D_{1}$ and $D_{2}$, considering that $\alpha_{k i}$ and $\beta_{k i}$ are of the same dimension, the model (M-1) can be transformed into a single objective model (M-2) by the linear weighted method as follows:

$$
(\mathrm{M}-2)\left\{\begin{array}{l}
\operatorname{Max} D=\sum_{k=1}^{h} \sum_{i=1}^{t}\left[\omega_{1} \alpha_{k i}+\omega_{2} \beta_{k i}\right] x_{k i}, \\
\text { s.t. } \sum_{i=1}^{t} x_{k i}=1, k \in H \\
\sum_{k=1}^{h} x_{k i} \leq 1, i \in T \\
x_{k i} \in\{0,1\}, k \in H, i \in T
\end{array}\right.
$$

where $\omega_{1}$ and $\omega_{2}$ represent the weights of the objective functions $D_{1}$ and $D_{2}$ respectively. By using mathematical software such as Lingo to solve the model (M-2), the optimal matching scheme considering satisfaction degrees can be obtained.

Similarly, the model (M-1) can be transformed into a single objective model (M-3) by the multiplicative weighted method as follows:

$$
(\mathrm{M}-3)\left\{\begin{array}{l}
\operatorname{Max} D=\sum_{k=1}^{h} \sum_{i=1}^{t}\left[\alpha_{k i}{ }^{\omega_{3}} \times \beta_{k i}{ }^{\omega_{4}}\right] x_{k i} \\
\text { s.t. } \sum_{i=1}^{t} x_{k i}=1, k \in H \\
\sum_{k=1}^{h} x_{k i} \leq 1, i \in T \\
x_{k i} \in\{0,1\}, k \in H, i \in T
\end{array}\right.
$$

where $\omega_{3}$ and $\omega_{4}\left(0 \leq \omega_{3}, \omega_{4} \leq 1, \omega_{3}+\omega_{4}=1\right)$ represent the weights of objective function $D_{1}$ and $D_{2}$ respectively. By solving the model (M-3), the optimal matching scheme considering satisfaction degree can be obtained.
4.6. Bilateral matching models based on satisfaction and fairness degrees

Based on the matching matrix $\boldsymbol{X}=\left[x_{k i}\right]_{h \times t}$ and the fairness degree matrix $\breve{\boldsymbol{Z}}=\left[\hbar_{k i}\right]_{h \times t}$, the model of bilateral matching considering fairness degrees under the one-to-one matching constraint is established as follows:

$$
(\mathrm{M}-4)\left\{\begin{array}{l}
\operatorname{Max} \quad D_{3}=\sum_{k=1}^{h} \sum_{i=1}^{t} \hbar_{k i} x_{k i}, \\
\text { s.t. } \sum_{i=1}^{t} x_{k i}=1, k \in H \\
\sum_{k=1}^{h} x_{k i} \leq 1, i \in T \\
x_{k i} \in\{0,1\}, k \in H, i \in T
\end{array}\right.
$$

By using mathematical software such as Lingo to solve the model (M-4), the optimal matching scheme considering fairness degree can be obtained.

Considering the satisfaction and fairness degrees of bilateral matching, a multi-objective optimization model of bilateral matching is established as follows:

$$
(\operatorname{M}-5)\left\{\begin{array}{l}
\operatorname{Max} D_{1}=\sum_{k=1}^{h} \sum_{i=1}^{t} \alpha_{k i} x_{k i}, \\
\operatorname{Max} D_{2}=\sum_{k=1}^{h} \sum_{i=1}^{t} \beta_{k i} x_{k i} \\
\operatorname{Max} D_{3}=\sum_{k=1}^{h} \sum_{i=1}^{t} \hbar_{k i} x_{k i}, \\
\text { s.t. } \sum_{i=1}^{t} x_{k i}=1, k \in H \\
\sum_{k=1}^{h} x_{k i} \leq 1, i \in T \\
x_{k i} \in\{0,1\}, k \in H, i \in T
\end{array}\right.
$$

where $\operatorname{Max} D_{1}=\sum_{k=1}^{h} \sum_{i=1}^{t} \alpha_{k i} x_{k i}$ represents maximizing the satisfaction degree of side $\partial$, $\operatorname{Max} D_{2}=\sum_{k=1}^{h} \sum_{i=1}^{t} \beta_{k i} x_{k i}$ represents maximizing the satisfaction degree of side $\ell$, and $\operatorname{Max} D_{3}=\sum_{k=1}^{h} \sum_{i=1}^{t} \hbar_{k i} x_{k i}$ represents maximizing the fairness degree of bilateral
subjects.
For objective functions $D_{1}, D_{2}$ and $D_{3}$, considering that $\alpha_{k i}, \beta_{k i}$ and $\hbar_{k i}$ are of the same dimension, the model (M-5) can be transformed into a single objective model (M-6) by the linear weighted method as follows:

$$
(\mathrm{M}-6)\left\{\begin{array}{l}
\operatorname{Max} \quad D=\sum_{k=1}^{h} \sum_{i=1}^{t}\left(w_{1} \alpha_{k i}+w_{2} \beta_{k i}+w_{3} \hbar_{k i}\right), \\
\text { s.t. } \sum_{i=1}^{t} x_{k i}=1, k \in H, \\
\sum_{k=1}^{h} x_{k i} \leq 1, i \in T \\
x_{k i} \in\{0,1\}, k \in H, i \in T,
\end{array}\right.
$$

where $w_{1}, w_{2}$ and $w_{3}\left(0 \leq w_{1}, w_{2}, w_{3} \leq 1, w_{1}+w_{2}+w_{3}=1\right)$ represent the weights of objective function $D_{1}, D_{2}$ and $D_{3}$ respectively. By solving the model (M-6), the optimal matching scheme considering satisfaction and fairness degrees can be obtained.

Similarly, the model (M-6) can also be transformed into a single objective model (M-7) by using the multiplicative weighting method as follows:

$$
(\mathrm{M}-7)\left\{\begin{array}{l}
\operatorname{Max} \quad D=\sum_{k=1}^{h} \sum_{i=1}^{t}\left(\alpha_{k i}{ }^{\mathrm{v}_{1}}{\beta_{k i}}^{\mathrm{v}_{2}} \hbar_{k i}{ }^{\mathrm{v}_{3}}\right) x_{i j} \\
\text { s.t. } \sum_{i=1}^{t} x_{k i}=1, k \in H \\
\sum_{k=1}^{h} x_{k i} \leq 1, i \in T \\
x_{k i} \in\{0,1\}, k \in H, i \in T
\end{array}\right.
$$

where $v_{1}, v_{2}$ and $v_{3}\left(0 \leq v_{1}, v_{2}, v_{3} \leq 1, v_{1}+v_{2}+v_{3}=1\right)$ represent the weights of objective function $D_{1}, D_{2}$ and $D_{3}$ respectively. By solving the model (M-7), the optimal matching scheme considering the satisfaction and fairness degrees can be obtained.

## 5. Linguistic intuitionistic fuzzy bilateral matching decision steps

In summary, the steps to solve the multi-attribute bilateral matching decision problem based on linguistic intuitionistic fuzzy information are as follows.

Step 1. By Eqs. (7) and (8), the overall attribute dominance matrix $\boldsymbol{Z}^{\left(\partial_{k}\right)}=\left[\delta_{i j}^{k}\right]_{t \times p}$ of the subject $\partial_{k}$ to $\ell_{i}$ under the attribute $c_{j}$ is constructed. By Eqs. (9) and (10), the overall attribute dominance matrix $\mathbf{Z}^{\left(\ell_{i}\right)}=\left[\delta_{k g}^{i}\right]_{h \times q}$ of the subject $\ell_{i}$ to $\partial_{k}$ under the attribute $d_{g}$ is constructed.
Step 2. By Eqs. (11)-(13) and (16))-(18), group opinion matrices $\widetilde{\boldsymbol{A}}=\left[\tilde{a}_{i j}^{\partial}\right]_{t \times p}$ and $\widetilde{\boldsymbol{B}}=\left[\tilde{b}_{k g}^{\prime}\right]_{h \times q}$ are calculated; by Eqs. (14) and (19), group score matrices $\boldsymbol{R}^{(\partial)}=\left[r_{\tilde{a}_{i j}}\right]_{t \times p}$ and $\boldsymbol{R}^{(\nearrow)}=\left[r_{\tilde{b}_{k g}^{\prime}}\right]_{h \times q}$ are constructed; by Eqs. (15) and (20), attribute weight vectors $\omega^{c}=\left(\omega_{1}^{c}, \omega_{2}^{c}\right.$,. $\left.\ldots, \omega_{p}^{c}\right)$ and $\boldsymbol{\omega}^{d}=\left(\omega_{1}^{d}, \omega_{2}^{d}, \ldots, \omega_{q}^{d}\right)$ are obtained.
Step 3. By Eqs. (21) and (23), overall dominance matrices $\boldsymbol{Z}^{(\partial)}=\left[\delta_{k i}^{\partial}\right]_{h \times t}$ and $\boldsymbol{Z}^{(\nearrow)}=\left[\delta_{k i}^{\ell}\right]_{h \times t}$ are calculated. Then, by Eqs. (22) and (24), satisfaction degree matrices $\widetilde{\boldsymbol{Z}}^{(\partial)}=\left[\alpha_{k i}\right]_{h \times t}$ of side $\partial$ and $\widetilde{\mathbf{Z}}^{(\rho)}=\left[\beta_{k i}\right]_{h \times t}$ of side $\ell$ are constructed.
Step 4. By Eqs. (25) and (26), relative fairness degree matrices $\widehat{\mathbf{Z}}^{(\partial)}=\left[\widetilde{\wp}_{0 i}^{\partial}\right]_{h \times t}$ of side $\partial$ and $\widehat{\mathbf{Z}}^{(\curlywedge)}=\left[\widetilde{\wp}_{k i}^{\prime}\right]_{h \times t}$ of side $\ell$ are constructed.
By Eqs. (27) and (28), the bilateral relative fairness degree matrix $\widehat{\boldsymbol{Z}}=\left[\widetilde{\mathscr{O}}_{k i}\right]_{h \times t}$ and the fairness degree matrix $\bar{Z}=\left[\hbar_{k i}\right]_{h \times t}$ are constructed.

Step 5. A bilateral matching model (M-1) based on satisfaction degrees is constructed and transformed into the single-objective models (M-2) and (M-3); and the models (M-2) and (M-3) are solved to obtain the optimal matching scheme.

Step 6. A bilateral matching model (M-4) based on fairness degrees is constructed; a multi-objective model (M-5) considering satisfaction and fairness degrees is constructed and transformed into models (M-6) and (M-7); and the models (M-6) and (M-7) are solved to obtain the optimal matching scheme.

## 6. Example analysis

Consider the matching problem between enterprises and job seekers. There are four enterprises $\partial=\left\{\partial_{1}, \partial_{2}, \partial_{3}, \partial_{4}\right\}$ in a campus recruitment meeting that all need to recruit one employee for a certain position, and five undergraduates $\ell=\left\{\ell_{1}, \ell_{2}, \ell_{3}, \ell_{4}, \ell_{5}\right\}$ are candidates. The enterprises evaluating the undergraduates mainly considers the following four aspects $C=\left\{c_{1}, c_{2}, c_{3}, c_{4}\right\}$ : education, personal quality, professional knowledge and foreign linguistic level, The undergraduates evaluating the enterprises mainly considers
the following four aspects $D=\left\{d_{1}, d_{2}, d_{3}, d_{4}\right\}$ : salary status, company prospects, company address and promotion space. Let $\widetilde{\boldsymbol{A}}^{\left(\partial_{k}\right)}=$ $\left[\tilde{a}_{i j}^{k}\right]_{5 \times 4}$ be the linguistic intuitionistic fuzzy preference matrix of subject $\partial_{k}$ to subject $\ell_{i}$ under the attribute $c_{j}$; let $\widetilde{\boldsymbol{B}}^{\left(/_{i}\right)}=\left[\tilde{b}_{k g}^{i}\right]_{4 \times 4}$ be the linguistic intuitionistic fuzzy preference matrix of subject $\ell_{i}$ to subject $\partial_{k}$ under the attribute $d_{g}$. The considered linguistic assessment scale set is $S=\left\{s_{0}\right.$ : extremely poor; $s_{1}$ : very poor; $s_{2}$ : poor; $s_{3}$ : middle-lower; $s_{4}$ : middle; $s_{5}$ : middle-upper; $s_{6}$ : good; $s_{7}$ : very good; $s_{8}$ : extremely good\}. Linguistic intuitionistic fuzzy preference matrices $\widetilde{\boldsymbol{A}}^{\left(\partial_{k}\right)}=\left[\tilde{a}_{i j}^{k}\right]_{5 \times 4}$ and $\widetilde{\boldsymbol{B}}^{\left(\varepsilon_{g}\right)}=\left[\widetilde{b}_{i j}^{g}\right]_{4 \times 4}$ are shown in Tables 1-9.

### 6.1. Solution process

Step 1. By Eqs. (7) and (8), the overall attribute dominance matrix $\boldsymbol{Z}^{\left(\partial_{k}\right)}=\left[\delta_{i j}^{k}\right]_{5 \times 4}$ of the subject $\partial_{k}$ to $\ell_{i}$ under the attribute $c_{j}$ is constructed. By Eqs. (9) and (10), the overall attribute dominance matrix $\boldsymbol{Z}^{\left(/_{i}\right)}=\left[\delta_{k g}^{i}\right]_{4 \times 4}$ of the subject $\ell_{i}$ to $\partial_{k}$ under the attribute $d_{g}$ is constructed, as shown in Tables 10-18:
Step 2. By Eqs. (11)-(13) and (16))-(18), group opinion matrices $\widetilde{\boldsymbol{A}}=\left[\widetilde{a}_{i j}^{\partial}\right]_{5 \times 4}$ and $\widetilde{\boldsymbol{B}}=\left[\widetilde{b}_{k g}^{\prime}\right]_{4 \times 4}$ are calculated, as shown in Tables 19 and 20; by Eqs. (14) and (19), group score matrices $\boldsymbol{R}^{(\partial)}=\left[r_{\tilde{a}_{j i}}\right]_{5 \times 4}$ and $\boldsymbol{R}^{(/)}=\left[r_{\tilde{b}_{k g}}\right]_{4 \times 4}$ are constructed, as shown in Tables 21 and 22 .

By Eqs. (15) and (20), the attribute weights are calculated, i.e., $\omega^{C}=(0.29,0.22,0.25,0.24), \omega^{D}=(0.26,0.32,0.29,0.13)$.
Step 3. By Eqs. (21) and (23), overall dominance matrices $\boldsymbol{Z}^{(\partial)}=\left[\delta_{k i}^{\partial}\right]_{4 \times 5}$ and $\boldsymbol{Z}^{(\nearrow)}=\left[\delta_{k i}^{\ell}\right]_{4 \times 5}$ are calculated; by Eqs. (22) and (24), satisfaction degree matrices $\widetilde{\mathbf{Z}}^{(\partial)}=\left[\alpha_{k i}\right]_{4 \times 5}$ of side $\partial$ and $\widetilde{\mathbf{Z}}^{(\rho)}=\left[\beta_{k i}\right]_{4 \times 5}$ of side $\ell$ are constructed, as shown in Tables 23-26.
Step 4. By Eqs. (25) and (26), relative fairness degree matrices $\widehat{\mathbf{Z}}^{(\partial)}=\left[\widetilde{\wp}_{k i}^{\partial}\right]_{4 \times 5}$ of side $\partial$ and $\widehat{\boldsymbol{Z}}^{(\nearrow)}=\left[\widetilde{\wp}_{k i}^{\prime}\right]_{4 \times 5}$ of side $\ell$ are constructed. By Eqs. (27) and (28), the bilateral relative fairness degree matrix $\widehat{\boldsymbol{Z}}=\left[\widetilde{\mathscr{\delta}}_{k i}\right]_{4 \times 5}$ and the fairness degree matrix $\widehat{\boldsymbol{Z}}=\left[\hbar_{k i}\right]_{4 \times 5}$ are constructed, as shown in Tables 27-30:
Step 5. A bilateral matching model (M-1) based on satisfaction degrees is constructed, and it can be transformed into the singleobjective models (M-2) and (M-3) by the linear weighting method and the multiplicative weighting method respectively; let $\omega_{1}=$ $0.3, \omega_{2}=0.7, \omega_{3}=0.3, \omega_{4}=0.7$, then the optimal matching schemes are obtained by solving models (M-2) and (M-3), as shown in Tables 31 and 32 .

Therefore, the optimal matching scheme based on the model (M-2) is $\left\{\left(\partial_{1}, \ell_{5}\right),\left(\partial_{2}, \ell_{4}\right),\left(\partial_{3}, \ell_{2}\right),\left(\partial_{4}, \ell_{1}\right)\right\}$, which indicates that enterprise $\partial_{1}$ is matched with undergraduate $\ell_{5}$, enterprise $\partial_{2}$ is matched with undergraduate $\ell_{4}$, enterprise $\partial_{3}$ is matched with undergraduate $\ell_{2}$, enterprise $\partial_{4}$ is matched with undergraduate $\ell_{1}$, and undergraduate $\ell_{3}$ is unmatched; the optimal matching scheme based on the model (M-3) is $\left\{\left(\partial_{1}, \ell_{1}\right),\left(\partial_{2}, \ell_{4}\right),\left(\partial_{3}, \ell_{2}\right),\left(\partial_{4}, \ell_{5}\right)\right\}$, which indicates that enterprise $\partial_{1}$ is matched with undergraduate $\ell_{1}$, enterprise $\partial_{2}$ is matched with undergraduate $\ell_{4}$, enterprise $\partial_{3}$ is matched with undergraduate $\ell_{2}$, enterprise $\partial_{4}$ is matched with undergraduate $\ell_{5}$, and undergraduate $\ell_{3}$ is unmatched.

Step 6. : A bilateral matching model (M-4) based on fairness degrees is constructed; and a multi-objective model (M-5) considering satisfaction and fairness degrees is constructed; it can be transformed into models (M-6) and (M-7) by the linear weighted method and the multiplicative weighted method; let $w_{1}=w_{2}=w_{3}=\frac{1}{3}, \mathrm{v}_{1}=\mathrm{v}_{2}=\mathrm{v}_{3}=\frac{1}{3}$, then the optimal matching schemes are obtained by solving models (M-6) and (M-7), as shown in Tables 33-35.

Therefore, the optimal matching scheme based on model (M-4) is $\left\{\left(\partial_{1}, \ell_{4}\right),\left(\partial_{2}, \ell_{3}\right),\left(\partial_{3}, \ell_{1}\right),\left(\partial_{4}, \ell_{2}\right)\right\}$, which indicates that enterprise $\partial_{1}$ is matched with undergraduate $\ell_{4}$, enterprise $\partial_{2}$ is matched with undergraduate $\ell_{3}$, enterprise $\partial_{3}$ is matched with undergraduate $\ell_{1}$, enterprise $\partial_{4}$ is matched with undergraduate $\ell_{2}$, and undergraduate $\ell_{5}$ is unmatched; the optimal matching scheme based on models (M-6) and (M-7) both are $\left\{\left(\partial_{1}, \ell_{5}\right),\left(\partial_{2}, \ell_{4}\right),\left(\partial_{3}, \ell_{2}\right),\left(\partial_{4}, \ell_{1}\right)\right\}$, which indicates that enterprise $\partial_{1}$ is matched with undergraduate $\ell_{5}$, enterprise $\partial_{2}$ is matched with undergraduate $\ell_{4}$, enterprise $\partial_{3}$ is matched with undergraduate $\ell_{2}$, enterprise $\partial_{4}$ is matched with undergraduate $\ell_{1}$, and undergraduate $\ell_{3}$ is unmatched. At the end, the optimal matching scheme is selected as that considering satisfaction and fairness degrees, i.e., $\left\{\left(\partial_{1}, \ell_{5}\right),\left(\partial_{2}, \ell_{4}\right),\left(\partial_{3}, \ell_{2}\right),\left(\partial_{4}, \ell_{1}\right)\right\}$.

### 6.2. Comparative analysis

To verify the feasibility and effectiveness of the proposed decision method, this paper reconstructs and solves the models based on

Table 1
Linguistic intuitionistic fuzzy preference matrix $\widetilde{\boldsymbol{A}}^{\left(\partial_{1}\right)}=\left[\widetilde{a}_{i j}^{1}\right]_{5 \times 4}$ of subject $\partial_{1}$ to subject $\ell_{i}$ under attribute $c_{j}$.

|  | $c_{1}$ | $c_{2}$ | $c_{3}$ | $c_{4}$ |
| :--- | :--- | :--- | :--- | :--- |
| $\ell_{1}$ | $\left(S_{7}, S_{1}\right)$ | $\left(S_{6}, S_{2}\right)$ | $\left(S_{4}, S_{3}\right)$ | $\left(S_{7}, S_{1}\right)$ |
| $\ell_{2}$ | $\left(S_{5}, S_{2}\right)$ | $\left(S_{5}, S_{2}\right)$ | $\left(S_{6}, S_{1}\right)$ | $\left(S_{6}, S_{2}\right)$ |
| $\ell_{3}$ | $\left(S_{6}, S_{1}\right)$ | $\left(S_{5}, S_{3}\right)$ | $\left(S_{7}, S_{1}\right)$ | $\left(S_{5}, S_{2}\right)$ |
| $\ell_{4}$ | $\left(S_{6}, S_{1}\right)$ | $\left(S_{7}, S_{1}\right)$ | $\left(S_{6}, S_{2}\right)$ | $\left(S_{1}\right)$ |
| $\ell_{5}$ | $\left(S_{7}, S_{1}\right)$ | $\left(S_{6}, S_{2}\right)$ | $\left(S_{6}, S_{1}\right)$ |  |

Table 2
Linguistic intuitionistic fuzzy preference matrix $\widetilde{\boldsymbol{A}}^{\left(\partial_{2}\right)}=\left[\tilde{a}_{i j}^{2}\right]_{5 \times 4}$ of subject $\partial_{2}$ to subject $\ell_{i}$ under attribute $c_{j}$.

|  | $c_{1}$ | $c_{2}$ | $c_{3}$ |
| :--- | :--- | :--- | :--- |
| $\ell_{1}$ | $\left(S_{6}, S_{1}\right)$ | $\left(S_{4}, S_{4}\right)$ | $\left(S_{5}, S_{2}\right)$ |
| $\ell_{2}$ | $\left(S_{6}, S_{2}\right)$ | $\left(S_{5}, S_{1}\right)$ | $\left(S_{5}, S_{2}\right)$ |
| $\ell_{3}$ | $\left(S_{5}, S_{2}\right)$ | $\left(S_{6}, S_{1}\right)$ | $\left(S_{2}\right)$ |
| $\ell_{4}$ | $\left(S_{6}, S_{2}\right)$ | $\left(S_{6}, S_{1}\right)$ | $\left(S_{6}, S_{1}\right)$ |
| $\ell_{5}$ | $\left(S_{6}, S_{1}\right)$ | $\left(S_{5}, S_{3}\right)$ | $\left(S_{6}, S_{1}\right)$ |

Table 3
Linguistic intuitionistic fuzzy preference matrix $\widetilde{\boldsymbol{A}}^{\left(\partial_{3}\right)}=\left[\tilde{a}_{i j}^{3}\right]_{5 \times 4}$ of subject $\partial_{3}$ to subject $\ell_{i}$ under attribute $c_{j}$.

|  | $c_{1}$ | $c_{2}$ | $c_{3}$ |
| :--- | :--- | :--- | :--- |
| $\ell_{1}$ | $\left(S_{6}, S_{1}\right)$ | $\left(S_{5}, S_{2}\right)$ | $\left(S_{5}, S_{3}\right)$ |
| $\ell_{2}$ | $\left(S_{7}, S_{1}\right)$ | $\left(S_{6}, S_{2}\right)$ | $\left(S_{7}, S_{1}\right)$ |
| $\ell_{3}$ | $\left(S_{5}, S_{3}\right)$ | $\left(S_{5}, S_{2}\right)$ | $\left(S_{7}, S_{1}\right)$ |
| $\ell_{4}$ | $\left(S_{6}, S_{2}\right)$ | $\left(S_{6}, S_{2}\right)$ | $\left(S_{6}, S_{1}\right)$ |
| $\ell_{5}$ | $\left(S_{5}, S_{2}\right)$ | $\left(S_{5}, S_{1}\right)$ | $\left(S_{5}, S_{3}\right)$ |

Table 4
Linguistic intuitionistic fuzzy preference matrix $\widetilde{\boldsymbol{A}}^{\left(\partial_{4}\right)}=\left[\tilde{a}_{i j}^{4}\right]_{5 \times 4}$ of subject $\partial_{4}$ to subject $\ell_{i}$ under attribute $c_{j}$.

|  | $c_{1}$ | $c_{2}$ | $c_{3}$ | $c_{4}$ |
| :--- | :--- | :--- | :--- | :--- |
| $\ell_{1}$ | $\left(S_{5}, S_{3}\right)$ | $\left(S_{4}, S_{3}\right)$ | $\left(S_{6}, S_{1}\right)$ |  |
| $\ell_{2}$ | $\left(S_{6}, S_{1}\right)$ | $\left(S_{7}, S_{1}\right)$ | $\left(S_{1}\right)$ | $\left(S_{5}, S_{3}\right)$ |
| $\ell_{3}$ | $\left(S_{5}, S_{1}\right)$ | $\left(S_{4}, S_{3}\right)$ | $\left(S_{6}, S_{2}\right)$ | $\left(S_{4}, S_{3}\right)$ |
| $\ell_{4}$ | $\left(S_{4}, S_{3}\right)$ | $\left(S_{5}, S_{1}\right)$ | $\left(S_{6}, S_{2}\right)$ |  |
| $\ell_{5}$ | $\left(S_{6}, S_{2}\right)$ | $\left(S_{5}, S_{2}\right)$ | $\left(S_{5}, S_{3}\right)$ |  |

## Table 5

Linguistic intuitionistic fuzzy preference matrix $\widetilde{\boldsymbol{B}}^{\left(\ell_{1}\right)}=\left[\widetilde{b}_{k g}^{1}\right]_{4 \times 4}$ of subject $\ell_{1}$ to subject $\partial_{k}$ under attribute $d_{g}$.

|  | $d_{1}$ | $d_{2}$ | $d_{3}$ | $d_{4}$ |
| :--- | :--- | :--- | :--- | :--- |
| $\partial_{1}$ | $\left(S_{6}, S_{2}\right)$ | $\left(S_{4}, S_{3}\right)$ | $\left(S_{7}, S_{1}\right)$ | $\left(S_{5}, S_{2}\right)$ |
| $\partial_{2}$ | $\left(S_{5}, S_{2}\right)$ | $\left(S_{6}, S_{1}\right)$ | $\left(S_{6}, S_{2}\right)$ | $\left(S_{7}, S_{1}\right)$ |
| $\partial_{3}$ | $\left(S_{5}, S_{3}\right)$ | $\left(S_{7}, S_{1}\right)$ | $\left(S_{5}, S_{1}\right)$ | $\left(S_{4}, S_{3}\right)$ |
| $\partial_{4}$ | $\left(S_{7}, S_{1}\right)$ | $\left(S_{4}, S_{4}\right)$ | $\left(S_{6}, S_{1}\right)$ | $\left(S_{4}, S_{2}\right)$ |

## Table 6

Linguistic intuitionistic fuzzy preference matrix $\widetilde{\boldsymbol{B}}^{\left(/_{2}\right)}=\left[\widetilde{b}_{i j}^{2}\right]_{4 \times 4}$ of subject $\ell_{2}$ to subject $\partial_{k}$ under attribute $d_{g}$.

|  | $d_{1}$ | $d_{2}$ | $d_{3}$ | $d_{4}$ |
| :--- | :--- | :--- | :--- | :--- |
| $\partial_{1}$ | $\left(S_{5}, S_{3}\right)$ | $\left(S_{6}, S_{2}\right)$ | $\left(S_{6}, S_{2}\right)$ | $\left(S_{5}, S_{3}\right)$ |
| $\partial_{2}$ | $\left(S_{6}, S_{1}\right)$ | $\left(S_{6}, S_{1}\right)$ | $\left(S_{5}, S_{2}\right)$ | $\left(S_{5}, S_{3}\right)$ |
| $\partial_{3}$ | $\left(S_{6}, S_{1}\right)$ | $\left(S_{7}, S_{1}\right)$ | $\left(S_{5}, S_{3}\right)$ | $\left(S_{4}, S_{4}\right)$ |
| $\partial_{4}$ | $\left(S_{5}, S_{3}\right)$ | $\left(S_{5}, S_{2}\right)$ | $\left(S_{5}, S_{1}\right)$ | $\left.S_{3}\right)$ |

## Table 7

Linguistic intuitionistic fuzzy preference matrix $\widetilde{\boldsymbol{B}}^{\left.(/)_{3}\right)}=\left[\widetilde{b}_{i j}^{3}\right]_{4 \times 4}$ of subject $\ell_{3}$ to subject $\partial_{k}$ under attribute $d_{g}$.

|  | $d_{1}$ | $d_{2}$ | $d_{3}$ | $d_{4}$ |
| :--- | :--- | :--- | :--- | :--- |
| $\partial_{1}$ | $\left(S_{5}, S_{2}\right)$ | $\left(S_{5}, S_{2}\right)$ | $\left(S_{6}, S_{2}\right)$ |  |
| $\partial_{2}$ | $\left(S_{6}, S_{2}\right)$ | $\left(S_{7}, S_{1}\right)$ | $\left(S_{1}\right)$ | $\left(S_{3}, S_{4}\right)$ |
| $\partial_{3}$ | $\left(S_{5}, S_{2}\right)$ | $\left(S_{7}, S_{1}\right)$ | $\left(S_{2}\right)$ | $\left(S_{4}, S_{3}\right)$ |
| $\partial_{4}$ | $\left(S_{6}, S_{1}\right)$ | $\left(S_{4}, S_{3}\right)$ | $\left(S_{6}, S_{1}\right)$ |  |

Table 8
Linguistic intuitionistic fuzzy preference matrix $\widetilde{\boldsymbol{B}}^{\left(/_{4}\right)}=\left[\widetilde{b}_{i j}^{4}\right]_{4 \times 4}$ of subject $\ell_{4}$ to subject $\partial_{k}$ under attribute $d_{g}$.

|  | $d_{1}$ | $d_{2}$ | $d_{3}$ | $d_{4}$ |
| :--- | :--- | :--- | :--- | :--- |
| $\partial_{1}$ | $\left(S_{4}, S_{4}\right)$ | $\left(S_{7}, S_{1}\right)$ | $\left(S_{2}, S_{4}\right)$ |  |
| $\partial_{2}$ | $\left(S_{7}, S_{1}\right)$ | $\left(S_{6}, S_{1}\right)$ | $\left(S_{1}\right)$ | $\left(S_{5}, S_{2}\right)$ |
| $\partial_{3}$ | $\left(S_{4}, S_{3}\right)$ | $\left(S_{6}, S_{2}\right)$ | $\left(S_{1}\right)$ | $\left(S_{2}, S_{5}\right)$ |
| $\partial_{4}$ | $\left(S_{5}, S_{1}\right)$ | $\left(S_{4}, S_{2}\right)$ | $\left(S_{6}, S_{2}\right)$ | $\left(S_{4}, S_{3}\right)$ |

## Table 9

Linguistic intuitionistic fuzzy preference matrix $\widetilde{\boldsymbol{B}}^{(/ 5)}=\left[\widetilde{b}_{i j}^{5}\right]_{4 \times 4}$ of subject $\ell_{5}$ to subject $\partial_{k}$ under attribute $d_{g}$.

|  | $d_{1}$ | $d_{2}$ | $d_{3}$ | $d_{4}$ |
| :--- | :--- | :--- | :--- | :--- |
| $\partial_{1}$ | $\left(S_{5}, S_{3}\right)$ | $\left(S_{6}, S_{1}\right)$ | $\left(S_{5}, S_{2}\right)$ |  |
| $\partial_{2}$ | $\left(S_{6}, S_{1}\right)$ | $\left(S_{6}, S_{2}\right)$ | $\left(S_{3}\right)$ | $\left(S_{5}, S_{2}\right)$ |
| $\partial_{3}$ | $\left(S_{6}, S_{2}\right)$ | $\left(S_{6}, S_{1}\right)$ | $\left(S_{4}, S_{3}\right)$ | $\left(S_{3}, S_{3}\right)$ |
| $\partial_{4}$ | $\left(S_{4}, S_{3}\right)$ | $\left(S_{5}, S_{1}\right)$ | $\left(S_{6}, S_{2}\right)$ | $\left(S_{5}, S_{1}\right)$ |

Table 10
Overall attribute dominance matrix $\boldsymbol{Z}^{\left(\partial_{1}\right)}=\left[\delta_{i j}^{1}\right]_{5 \times 4}$ of subject $\partial_{1}$ to $\ell_{i}$ under attribute $c_{j}$.

|  | $c_{1}$ | $c_{2}$ | $c_{3}$ | $c_{4}$ |
| :--- | :--- | :--- | :--- | :--- |
| $\ell_{1}$ | 1.2071 | 0.5500 | -0.6515 | 1.5607 |
| $\ell_{2}$ | -0.7587 | -0.3401 | -0.1179 |  |
| $\ell_{3}$ | 0.0393 | -0.7436 | 2.1907 | -0.6936 |
| $\ell_{4}$ | 0.0393 | 2.2565 | 0.2127 | 0.5500 |
| $\ell_{5}$ | 1.2071 | 1.3405 | -0.6515 | 0.5500 |

Table 11
Overall attribute dominance matrix $\boldsymbol{Z}^{\left(\partial_{2}\right)}=\left[\delta_{i j}^{2}\right]_{5 \times 4}$ of subject $\partial_{2}$ to $\ell_{i}$ under attribute $c_{j}$.

|  | $c_{1}$ | $c_{2}$ | $c_{3}$ | $c_{4}$ |
| :--- | :--- | :--- | :--- | :--- |
| $\ell_{1}$ | -0.2480 | -0.9736 | -0.6285 |  |
| $\ell_{2}$ | 0.6964 | 1.0052 | 0.0393 | 1.2071 |
| $\ell_{3}$ | -0.6285 | 1.4659 | 1.0607 | 0.4849 |
| $\ell_{4}$ | 0.6964 | 1.4659 | -0.1829 |  |
| $\ell_{5}$ | 1.4142 | -0.4052 | -0.7436 |  |

Table 12
Overall attribute dominance matrix $\boldsymbol{Z}^{\left(\partial_{3}\right)}=\left[\delta_{i j}^{3}\right]_{5 \times 4}$ of subject $\partial_{3}$ to $\ell_{i}$ under attribute $c_{j}$.

|  | $c_{1}$ | $c_{2}$ | $c_{3}$ | $c_{4}$ |
| :--- | :--- | :--- | :--- | :--- |
| $\ell_{1}$ | 1.0500 | -0.4714 | -0.6016 | 1.7071 |
| $\ell_{2}$ | 1.7071 | 1.4977 | 1.3536 | -0.6016 |
| $\ell_{3}$ | -0.7587 | -0.5627 | 0.3928 | -0.6016 |
| $\ell_{4}$ | -0.1179 | 1.7031 | -0.6016 |  |
| $\ell_{5}$ | -0.1829 | 0.0044 | 0.3928 |  |

Table 13
Overall attribute dominance matrix $\boldsymbol{Z}^{\left(\partial_{4}\right)}=\left[\delta_{i j}^{4}\right]_{5 \times 4}$ of subject $\partial_{4}$ to $\ell_{i}$ under attribute $c_{j}$.

|  | $c_{1}$ | $c_{2}$ | $c_{3}$ | $c_{4}$ |
| :--- | :--- | :--- | :--- | :--- |
| $\ell_{1}$ | -0.2480 | -0.6515 | 1.8195 | 1.8536 |
| $\ell_{2}$ | 1.7071 | 2.5153 | -0.2480 | -0.0258 |
| $\ell_{3}$ | 0.6206 | -0.6218 | -0.7587 |  |
| $\ell_{4}$ | -0.8238 | 1.4179 | -0.8737 | 1.0500 |
| $\ell_{5}$ | 0.4742 | 0.0415 | 1.1964 |  |

Table 14
Overall attribute dominance matrix $\boldsymbol{Z}^{\left(\ell_{1}\right)}=\left[\delta_{k g}^{1}\right]_{4 \times 4}$ of subject $\ell_{1}$ to $\partial_{k}$ under attribute $d_{g}$.

|  | $d_{1}$ | $d_{2}$ | $d_{3}$ | $d_{4}$ |
| :--- | :--- | :--- | :--- | :--- |
| $\partial_{1}$ | 0.5500 | -0.1408 | 1.2071 | 0.4849 |
| $\partial_{2}$ | -0.0258 | 0.9552 | 0.1857 |  |
| $\partial_{3}$ | -0.5365 | 1.5783 | -0.6016 | -0.7247 |
| $\partial_{4}$ | 1.3536 | -0.7015 | 0.5500 | -0.0757 |

Table 15
Overall attribute dominance matrix $\boldsymbol{Z}^{\left(\ell_{2}\right)}=\left[\delta_{k g}^{2}\right]_{4 \times 4}$ of subject $\ell_{2}$ to $\partial_{k}$ under attribute $d_{g}$.

|  | $d_{1}$ | $d_{2}$ | $d_{3}$ | $d_{4}$ |
| :--- | :--- | :--- | :--- | :--- |
| $\partial_{1}$ | -0.4444 | 0.0393 | 0.5500 | 0.3536 |
| $\partial_{2}$ | 0.8429 | 0.5500 | -0.0258 |  |
| $\partial_{3}$ | 1.3536 | 1.2071 | -0.5365 | 0.3536 |
| $\partial_{4}$ | -0.4444 | -0.5365 | -0.4714 |  |

Table 16
Overall attribute dominance matrix $\boldsymbol{Z}^{\left(\ell_{3}\right)}=\left[\delta_{k g}^{3}\right]_{4 \times 4}$ of subject $\ell_{3}$ to $\partial_{k}$ under attribute $d_{g}$.

|  | $d_{1}$ | $d_{2}$ | $d_{3}$ | $d_{4}$ |
| :--- | :--- | :--- | :--- | :--- |
| $\partial_{1}$ | -0.3143 | -0.0909 | 1.0607 | 1.6124 |
| $\partial_{2}$ | 0.5500 | 0.2278 | -0.4714 | -0.5864 |
| $\partial_{3}$ | -0.3143 | 1.1124 | -0.0258 |  |
| $\partial_{4}$ | 1.0607 | -0.7015 | -0.0258 |  |

Table 17
Overall attribute dominance matrix $\boldsymbol{Z}^{(/ 4)}=\left[\delta_{k g}^{4}\right]_{4 \times 4}$ of subject $\ell_{4}$ to $\partial_{k}$ under attribute $d_{g}$.

|  | $d_{1}$ | $d_{2}$ | $d_{3}$ | $d_{4}$ |
| :--- | :--- | :--- | :--- | :--- |
| $\partial_{1}$ | -0.7015 | 1.3195 | 0.2778 | -0.1408 |
| $\partial_{2}$ | 1.7247 | 0.6964 | 0.2778 | 1.5783 |
| $\partial_{3}$ | -0.1408 | 0.1857 | -0.7166 | -0.6515 |
| $\partial_{4}$ | 0.8902 | -0.7166 | 1.6124 |  |

Table 18
Overall attribute dominance matrix $\boldsymbol{Z}^{(/ 5)}=\left[\delta_{k g}^{5}\right]_{4 \times 4}$ of subject $\ell_{5}$ to $\partial_{k}$ under attribute $d_{g}$.

|  | $d_{1}$ | $d_{2}$ | $d_{3}$ | $d_{4}$ |
| :--- | :--- | :--- | :--- | :--- |
| $\partial_{1}$ | -0.0258 | 0.7071 | 0.1964 | 0.0393 |
| $\partial_{2}$ | 1.3536 | 0.1857 | 0.1964 | 0.6964 |
| $\partial_{3}$ | 0.6964 | 0.7071 | -0.5365 | -0.6016 |
| $\partial_{4}$ | -0.6016 | -0.5365 | 1.2071 | 1.2071 |

Table 19
Group opinion matrix $\widetilde{\boldsymbol{A}}=\left[\tilde{a}_{i j}^{\partial}\right]_{5 \times 4}$ of side $\partial$ to $\ell_{i}$ under attribute $c_{j}$.

|  | $c_{1}$ | $c_{2}$ | $c_{3}$ | $c_{4}$ |
| :--- | :--- | :--- | :--- | :--- |
| $\ell_{1}$ | $\left(S_{6.29}, S_{1.18}\right)$ | $\left(S_{5.16}, S_{2.32}\right)$ | $\left(S_{6.34}, S_{1.30}\right)$ |  |
| $\ell_{2}$ | $\left(S_{6.11}, S_{1.52}\right)$ | $\left(S_{5.71}, S_{1.62}\right)$ | $\left(S_{5.15}, S_{2.25}\right)$ | $\left(S_{5.65}, S_{1.64}\right)$ |
| $\ell_{3}$ | $\left(S_{5.45}, S_{1.53}\right)$ | $\left(S_{4.92}, S_{2.16}\right)$ | $\left(S_{6.24}, S_{1.64}\right)$ | $\left(S_{5.91}, S_{2.77}\right)$ |
| $\ell_{4}$ | $\left(S_{5.86}, S_{1.58}\right)$ | $\left(S_{5.98}, S_{1.23}\right)$ | $\left(S_{5.54}, S_{1.57}\right)$ | $\left(S_{5.63}, S_{1.75}\right)$ |
| $\ell_{5}$ | $\left(S_{6.30}, S_{1.23}\right)$ | $\left(S_{5.34}, S_{2.19}\right)$ | $\left(S_{6.20}, S_{1.56}\right)$ | $\left(S_{5.93}, S_{1.57}\right)$ |

different fair attenuation coefficients and different weights of bilateral subjects. The results are shown in Tables 36 and 37. The extended method based on Lin et al. [34] and Liu and Wang [35] are compared with the decision method proposed in this paper. The results are shown in Table 38.

It can be seen from Tables 36 and 37 that the optimal matching scheme considering only fairness degree and that considering

Table 20
Group opinion matrix $\widetilde{\boldsymbol{B}}=\left[\widetilde{b}_{k g}^{\prime}\right]_{4 \times 4}$ of side $\ell$ to $\partial_{k}$ under attribute $d_{g}$.

|  | $d_{1}$ | $d_{2}$ | $d_{3}$ | $d_{4}$ |
| :--- | :--- | :--- | :--- | :--- |
| $\partial_{1}$ | $\left(S_{5.21}, S_{2.47}\right)$ | $\left(S_{5.96}, S_{1.50}\right)$ | $\left(S_{4.61}, S_{2.51}\right)$ |  |
| $\partial_{2}$ | $\left(S_{5.78}, S_{1.46}\right)$ | $\left(S_{6.20}, S_{1.02}\right)$ | $\left(S_{6.14}, S_{1.63}\right)$ | $\left(S_{5.45}, S_{2.04}\right)$ |
| $\partial_{3}$ | $\left(S_{5.44}, S_{2.06}\right)$ | $\left(S_{6.56}, S_{1.17}\right)$ | $\left(S_{5.02}, S_{1.83}\right)$ | $\left(S_{3.67}, S_{3.44}\right)$ |
| $\partial_{4}$ | $\left(S_{5.60}, S_{1.64}\right)$ | $\left(S_{4.59}, S_{1.95}\right)$ | $\left(S_{6.20}, S_{1.23}\right)$ |  |

Table 21
Group score matrix $\boldsymbol{R}^{(\partial)}=\left[r_{\tilde{a}_{i j}}\right]_{5 \times 4}$ of side $\partial$ to $\ell_{i}$ under attribute $c_{j}$.

|  | $c_{1}$ | $c_{2}$ | $c_{3}$ | $c_{4}$ |
| :--- | :--- | :--- | :--- | :--- |
| $\ell_{1}$ | 0.6386 | 0.3547 | 0.3624 | 0.6294 |
| $\ell_{2}$ | 0.5745 | 0.5113 | 0.5743 | 0.5462 |
| $\ell_{3}$ | 0.4894 | 0.3449 | 0.4949 | 0.2683 |
| $\ell_{4}$ | 0.5348 | 0.5931 | 0.4851 |  |
| $\ell_{5}$ | 0.6334 | 0.3936 | 0.5462 |  |

Table 22
Group score matrix $\boldsymbol{R}^{(\nearrow)}=\left[r_{\tilde{b}_{k g}^{\prime}}\right]_{4 \times 4}$ of side $\ell$ to $\partial_{k}$ under attribute $d_{g}$.

|  | $d_{1}$ | $d_{2}$ | $d_{3}$ | $d_{4}$ |
| :--- | :--- | :--- | :--- | :--- |
| $\partial_{1}$ | 0.3425 | 0.5579 | 0.5638 | 0.2635 |
| $\partial_{2}$ | 0.5399 | 0.6475 | 0.4267 | 0.3253 |
| $\partial_{3}$ | 0.4227 | 0.6740 | 0.3984 | 0.0283 |
| $\partial_{4}$ | 0.4946 | 0.3295 | 0.6208 | 0.2731 |

Table 23
Overall dominance matrix $\boldsymbol{Z}^{(\partial)}=\left[\delta_{k i}^{\partial}\right]_{4 \times 5}$ of side $\partial$.

|  | $\ell_{1}$ | $\ell_{2}$ | $\ell_{3}$ | $\ell_{4}$ |
| :--- | :--- | :--- | :--- | :--- | :--- |
| $\partial_{1}$ | 0.6827 | 0.0126 | 0.2290 | 0.6930 |
| $\partial_{2}$ | -0.1536 | 0.5493 | 0.3615 | 0.6112 |
| $\partial_{3}$ | 0.4601 | 1.4501 | -0.6386 | 0.2943 |
| $\partial_{4}$ | 0.6845 | 0.9802 | -0.0041 | 0.1066 |

Table 24
Overall dominance matrix $\boldsymbol{Z}^{(\ell)}=\left[\delta_{k i}^{\ell}\right]_{4 \times 5}$ of side $\ell$.

|  | $\ell_{1}$ | $\ell_{2}$ | $\ell_{3}$ | $\ell_{4}$ |
| :--- | :--- | :--- | :--- | :--- | :--- |
| $\partial_{1}$ | 0.5110 | 0.1025 | 0.4064 | 0.3021 |
| $\partial_{2}$ | 0.5770 | 0.4336 | 0.0030 | 0.9570 |
| $\partial_{3}$ | 0.1149 | 0.5213 | 0.3279 | -0.2697 |
| $\partial_{4}$ | 0.2771 | 0.1513 | 0.1049 | 0.5793 |

Table 25
Satisfaction degree matrix $\widetilde{\mathbf{Z}}^{(\partial)}=\left[\alpha_{k i}\right]_{4 \times 5}$ of side $\partial$.

|  | $\ell_{1}$ | $\ell_{2}$ | $\ell_{3}$ | $\ell_{4}$ |
| :--- | :--- | :--- | :--- | :--- | :--- |
| $\partial_{1}$ | 0.6587 | 0.3606 | 0.4569 | 0.6633 |
| $\partial_{2}$ | 0.2867 | 0.5994 | 0.5158 | 0.6269 |
| $\partial_{3}$ | 0.5597 | 1.0000 | 0.0710 | 0.4860 |
| $\partial_{4}$ | 0.6595 | 0.7910 | 0.3532 | 0.4025 |

satisfaction and fairness degrees are different with the variation of fairness attenuation coefficient $\rho$ and weights of objective functions. It shows the necessity of fairness degree constraints in the process of bilateral matching.

It can be seen from Table 38 that the optimal bilateral matching schemes are slightly different due to different forms of preference information, weight assignment, and model construction. The differences are as follows: (1) The linguistic intuitionistic fuzzy numbers

Table 26
Satisfaction degree matrix $\widetilde{\boldsymbol{Z}}^{(\ell)}=\left[\beta_{k i}\right]_{4 \times 5}$ of side $\ell$.

|  | $\ell_{1}$ | $\ell_{2}$ | $\ell_{3}$ | $\ell_{4}$ |
| :--- | :--- | :--- | :--- | :--- | :--- |
| $\partial_{1}$ | 0.6517 | 0.3327 | 0.5701 | 0.4886 |
| $\partial_{2}$ | 0.7033 | 0.5913 | 0.2550 | 1.0000 |
| $\partial_{3}$ | 0.3424 | 0.6598 | 0.5087 | 0.0421 |
| $\partial_{4}$ | 0.4691 | 0.3708 | 0.3346 | 0.7050 |

Table 27
$\underline{\text { Relative fairness degree matrix } \widehat{\boldsymbol{Z}}^{(\partial)}=\left[\widetilde{\mathscr{~}}_{k i}^{\partial}\right]_{4 \times 5} \text { of side } \partial .}$

|  | $\ell_{1}$ | $\ell_{2}$ | $\ell_{3}$ | $\ell_{4}$ |
| :--- | :--- | :--- | :--- | :--- | :--- |
| $\partial_{1}$ | 1.0053 | 1.0411 | 0.3979 | 1.1651 |
| $\partial_{2}$ | 0.2838 | 1.0068 | 1.4222 | 0.3519 |
| $\partial_{3}$ | 1.2785 | 1.2311 | 0.1660 | 3.3967 |
| $\partial_{4}$ | 1.1857 | 1.4605 | 1.0274 | 0.3358 |

Table 28
Relative fairness degree matrix $\widehat{\boldsymbol{Z}}^{(\nearrow)}=\left[\widetilde{\varnothing}_{k i}^{\prime}\right]_{4 \times 5}$ of side $\ell$.

|  | $\ell_{1}$ | $\ell_{2}$ | $\ell_{3}$ | $\ell_{4}$ |
| :--- | :--- | :--- | :--- | :--- | :--- |
| $\partial_{1}$ | 0.4421 | 0.4269 | 1.1170 | 0.3815 |
| $\partial_{2}$ | 1.5661 | 0.4414 | 0.3125 | 1.2630 |
| $\partial_{3}$ | 0.3476 | 0.3610 | 2.6766 | 0.1308 |
| $\partial_{4}$ | 0.3748 | 0.3043 | 0.4326 | 1.3236 |

Table 29
Bilateral relative fairness degree matrix $\widehat{\boldsymbol{Z}}=\left[\widetilde{\mathscr{\delta}}_{k i}\right]_{4 \times 5}$.

|  | $\ell_{1}$ | $\ell_{2}$ | $\ell_{3}$ | $\ell_{4}$ |
| :--- | :--- | :--- | :--- | :--- | :--- |
| $\partial_{1}$ | 0.7237 | 0.7340 | 0.7574 | 0.7733 |
| $\partial_{2}$ | 0.9249 | 0.7241 | 0.8674 | 0.8075 |
| $\partial_{3}$ | 0.8131 | 0.7961 | 1.4213 | 1.7638 |
| $\partial_{4}$ | 0.7803 | 0.8824 | 0.7300 | 0.8297 |

Table 30
Fairness degree matrix $\boldsymbol{Z}=\left[\hbar_{k i}\right]_{4 \times 5}$.

|  | $\ell_{1}$ | $\ell_{2}$ | $\ell_{3}$ | $\ell_{4}$ |
| :--- | :--- | :--- | :--- | :--- | :--- |
| $\partial_{1}$ | 0.7237 | 0.7340 | 0.7574 | 0.7733 |
| $\partial_{2}$ | 0.9249 | 0.7241 | 0.8674 | 0.8075 |
| $\partial_{3}$ | 0.8131 | 0.7961 | 0.7036 | 0.5670 |
| $\partial_{4}$ | 0.7803 | 0.8824 | 0.7300 | 0.8297 |

Table 31
Optimal matching scheme based on model (M-2).

|  | $\ell_{1}$ | $\ell_{2}$ | $\ell_{3}$ | $\ell_{4}$ |  |
| :--- | :--- | :--- | :--- | :--- | :--- |
| $\partial_{1}$ | 0 | 0 | 0 | 0 | 1 |
| $\partial_{2}$ | 0 | 0 | 0 | 0 | 0 |
| $\partial_{3}$ | 0 | 1 | 0 | 0 | 0 |
| $\partial_{4}$ | 1 | 0 | 0 | 0 |  |

are used to express preferences of subjects in the proposed method; then unknown attribute weights are calculated by the group opinion matrices; furthermore, multiple bilateral matching models considering satisfaction degrees and fairness degrees are constructed and solved to obtain the optimal scheme. (2) The 2-Tuple linguistic term numbers are used by Lin et al. (2019); then the qualitative evaluations are aggregated by 2TWA to calculate the attribute weights; furthermore, a bi-objective optimization model is constructed and the feedback process is proposed with the expected matching ordinal EMO constraint to obtain the optimal scheme.

Table 32
Optimal matching scheme based on model (M-3).

|  | $\ell_{1}$ | $\ell_{2}$ | $\ell_{3}$ | $\ell_{4}$ |  |
| :--- | :--- | :--- | :--- | :--- | :--- |
| $\partial_{1}$ | 1 | 0 | 0 | 0 | 0 |
| $\partial_{2}$ | 0 | 0 | 0 | 1 |  |
| $\partial_{3}$ | 0 | 1 | 0 | 0 | 0 |
| $\partial_{4}$ | 0 | 0 | 0 | 0 |  |

Table 33
Optimal matching scheme based on model (M-4).

|  | $\ell_{1}$ | $\ell_{2}$ | $\ell_{3}$ | $\ell_{4}$ |
| :--- | :--- | :--- | :--- | :--- |
| $\partial_{1}$ | 0 | 0 | 0 | 1 |
| $\partial_{2}$ | 0 | 0 | 1 | 0 |
| $\partial_{3}$ | 1 | 0 | 0 | 0 |
| $\partial_{4}$ | 0 | 1 | 0 | 0 |

Table 34
Optimal matching scheme based on model (M-6).

|  | $\ell_{1}$ | $\ell_{2}$ | $\ell_{3}$ | $\ell_{4}$ |  |
| :--- | :--- | :--- | :--- | :--- | :--- |
| $\partial_{1}$ | 0 | 0 | 0 | 0 | 1 |
| $\partial_{2}$ | 0 | 0 | 0 | 0 | 0 |
| $\partial_{3}$ | 0 | 1 | 0 | 0 |  |
| $\partial_{4}$ | 1 | 0 | 0 | 0 |  |

Table 35
Optimal matching scheme based on model (M-7).

|  | $\ell_{1}$ | $\ell_{2}$ | $\ell_{3}$ | $\ell_{4}$ |  |
| :--- | :--- | :--- | :--- | :--- | :--- |
| $\partial_{1}$ | 0 | 0 | 0 | 0 | 1 |
| $\partial_{2}$ | 0 | 0 | 0 | 1 | 0 |
| $\partial_{3}$ | 0 | 1 | 0 | 0 |  |
| $\partial_{4}$ | 1 | 0 | 0 | 0 |  |

Table 36
Comparison of optimal matching schemes under different fair attenuation coefficients.

| Method | Optimal matching scheme |
| :--- | :--- |
| Method based on fairness degree model (M-4) $(\rho=1.5)$ | $\left\{\left(\partial_{1}, \ell_{4}\right),\left(\partial_{2}, \ell_{3}\right),\left(\partial_{3}, \ell_{1}\right),\left(\partial_{4}, \ell_{2}\right)\right\}$ |
| Method based on satisfaction and fairness degree model (M-6) $(\rho=1.5)$ | $\left\{\left(\partial_{1}, \ell_{5}\right),\left(\partial_{2}, \ell_{4}\right),\left(\partial_{3}, \ell_{2}\right),\left(\partial_{4}, \ell_{1}\right)\right\}$ |
| Method based on satisfaction and fairness degree model (M-7) $(\rho=1.5)$ | $\left\{\left(\partial_{1}, \ell_{1}\right),\left(\partial_{2}, \ell_{4}\right),\left(\partial_{3}, \ell_{2}\right),\left(\partial_{4}, \ell_{5}\right)\right\}$ |
| Method based on fairness degree model (M-4) $(\rho=2.25)$ | $\left\{\left(\partial_{1}, \ell_{4}\right),\left(\partial_{2}, \ell_{3}\right),\left(\partial_{3}, \ell_{1}\right),\left(\partial_{4}, \ell_{2}\right)\right\}$ |
| Method based on satisfaction and fairness degree model (M-6) $(\rho=2.25)$ | $\left\{\left(\partial_{1}, \ell_{5}\right),\left(\partial_{2}, \ell_{4}\right),\left(\partial_{3}, \ell_{2}\right),\left(\partial_{4}, \ell_{1}\right)\right\}$ |
| Method based on satisfaction and fairness degree model (M-7) $(\rho=2.25)$ | $\left\{\left(\partial_{1}, \ell_{5}\right),\left(\partial_{2}, \ell_{4}\right),\left(\partial_{3}, \ell_{2}\right),\left(\partial_{4}, \ell_{1}\right)\right\}$ |
| Method based on fairness degree model (M-4) $(\rho=5)$ | $\left\{\left(\partial_{1}, \ell_{4}\right),\left(\partial_{2}, \ell_{3}\right),\left(\partial_{3}, \ell_{1}\right),\left(\partial_{4}, \ell_{2}\right)\right\}$ |
| Method based on satisfaction and fairness degree model (M-6) $(\rho=5)$ | $\left\{\left(\partial_{1}, \ell_{5}\right),\left(\partial_{2}, \ell_{4}\right),\left(\partial_{3}, \ell_{2}\right),\left(\partial_{4}, \ell_{1}\right)\right\}$ |
| Method based on satisfaction and fairness degree model (M-7) $(\rho=5)$ | $\left\{\left(\partial_{1}, \ell_{5}\right),\left(\partial_{2}, \ell_{4}\right),\left(\partial_{3}, \ell_{2}\right),\left(\partial_{4}, \ell_{1}\right)\right\}$ |

(3) The intuitionistic linguistic numbers are used by Liu and Wang (2021); then the weights of attributes are given by bilateral subjects directly; furthermore, a dual-objective optimization model considering satisfaction degrees is constructed to obtain the optimal matching scheme.

In addition, the methods proposed by Lin et al. (2019) and Liu and Wang (2021) cannot be directly used to solve the problem in this paper, and fail to consider the satisfaction and fairness degrees to construct multiple bilateral matching models, which may lead to inaccurate decision results. Therefore, the optimal matching scheme under a linguistic intuitionistic fuzzy environment obtained in this paper are relatively more reference.

## 7. Conclusions

A new decision method is proposed for a multi-attribute bilateral matching problem under a linguistic intuitionistic fuzzy environment. In the method, a novel method is proposed to calculate the attribute weights by LIFIOWA operator. Then, the satisfaction

Table 37
Comparison of optimal matching schemes under different weights.

| Method | Optimal matching scheme |
| :--- | :--- |
| Method based on satisfaction degree model (M-2) $\left(\omega_{1}=0.2, \omega_{2}=0.8\right)$ | $\left\{\left(\partial_{1}, \ell_{1}\right),\left(\partial_{2}, \ell_{4}\right),\left(\partial_{3}, \ell_{2}\right),\left(\partial_{4}, \ell_{5}\right)\right\}$ |
| Method based on satisfaction degree model (M-3) $\left(\omega_{3}=0.2, \omega_{4}=0.8\right)$ | $\left\{\left(\partial_{1}, \ell_{1}\right),\left(\partial_{2}, \ell_{4}\right),\left(\partial_{3}, \ell_{2}\right),\left(\partial_{4}, \ell_{5}\right)\right\}$ |
| Method based on satisfaction and fairness degree model (M-6) $\left(w_{1}=0.2, w_{2}=0.3, w_{3}=0.5\right)$ | $\left\{\left(\partial_{1}, \ell_{5}\right),\left(\partial_{2}, \ell_{4}\right),\left(\partial_{3}, \ell_{2}\right),\left(\partial_{4}, \ell_{1}\right)\right\}$ |
| Method based on satisfaction and fairness degree model (M-7) $\left(\widetilde{\omega}_{1}=0.2, \widetilde{\omega}_{2}=0.3, \widetilde{\omega}_{3}=0.5\right)$ | $\left\{\left(\partial_{1}, \ell_{5}\right),\left(\partial_{2}, \ell_{4}\right),\left(\partial_{3}, \ell_{2}\right),\left(\partial_{4}, \ell_{1}\right)\right\}$ |
| Method based on satisfaction degree model (M-2) $\left(\omega_{1}=0.5, \omega_{2}=0.5\right)$ | $\left\{\left(\partial_{1}, \ell_{5}\right),\left(\partial_{2}, \ell_{4}\right),\left(\partial_{3}, \ell_{2}\right),\left(\partial_{4}, \ell_{1}\right)\right\}$ |
| Method based on satisfaction degree model (M-3) $\left(\omega_{3}=0.5, \omega_{4}=0.5\right)$ | $\left\{\left(\partial_{1}, \ell_{1}\right),\left(\partial_{2}, \ell_{4}\right),\left(\partial_{3}, \ell_{2}\right),\left(\partial_{4}, \ell_{5}\right)\right\}$ |
| Method based on satisfaction and fairness degree model (M-6) $\left(w_{1}=\frac{1}{3}, w_{2}=\frac{1}{3}, w_{3}=\frac{1}{3}\right)$ | $\left\{\left(\partial_{1}, \ell_{5}\right),\left(\partial_{2}, \ell_{4}\right),\left(\partial_{3}, \ell_{2}\right),\left(\partial_{4}, \ell_{1}\right)\right\}$ |
|  | $\left\{\left(\partial_{1}, \ell_{5}\right),\left(\partial_{2}, \ell_{4}\right),\left(\partial_{3}, \ell_{2}\right),\left(\partial_{4}, \ell_{1}\right)\right\}$ |
| Method based on satisfaction and fairness degree model (M-7) $\left(\widetilde{\omega}_{1}=\frac{1}{3}, \widetilde{\omega}_{2}=\frac{1}{3}, \widetilde{\omega}_{3}=\frac{1}{3}\right)$ | $\left\{\left(\partial_{1}, \ell_{4}\right),\left(\partial_{2}, \ell_{5}\right),\left(\partial_{3}, \ell_{2}\right),\left(\partial_{4}, \ell_{1}\right)\right\}$ |
| Method based on satisfaction degree model (M-2) $\left(\omega_{1}=0.8, \omega_{2}=0.2\right)$ | $\left\{\left(\partial_{1}, \ell_{4}\right),\left(\partial_{2}, \ell_{5}\right),\left(\partial_{3}, \ell_{2}\right),\left(\partial_{4}, \ell_{1}\right)\right\}$ |
| Method based on satisfaction degree model (M-3) $\left(\omega_{3}=0.8, \omega_{4}=0.2\right)$ | $\left\{\left(\partial_{1}, \ell_{5}\right),\left(\partial_{2}, \ell_{4}\right),\left(\partial_{3}, \ell_{2}\right),\left(\partial_{4}, \ell_{1}\right)\right\}$ |
| Method based on satisfaction and fairness degree model (M-6) $\left(w_{1}=0.5, w_{2}=0.3, w_{3}=0.2\right)$ | $\left\{\left(\partial_{1}, \ell_{5}\right),\left(\partial_{2}, \ell_{4}\right),\left(\partial_{3}, \ell_{2}\right),\left(\partial_{4}, \ell_{1}\right)\right\}$ |
| Method based on satisfaction and fairness degree model (M-7) $\left(\widetilde{\omega}_{1}=0.5, \widetilde{\omega}_{2}=0.3, \widetilde{\omega}_{3}=0.2\right)$ |  |

Table 38
Comparison of optimal matching schemes for different methods.

| Method | Optimal matching scheme |
| :--- | :--- |
| Method based on satisfaction degree model (M-2) (Method 1) | $\wp_{1}=\left\{\left(\partial_{1}, \ell_{5}\right),\left(\partial_{2}, \ell_{4}\right),\left(\partial_{3}, \ell_{2}\right),\left(\partial_{4}, \ell_{1}\right)\right\}$ |
| Method based on satisfaction degree model (M-3) (Method 2) | $\wp_{2}=\left\{\left(\partial_{1}, \ell_{1}\right),\left(\partial_{2}, \ell_{4}\right),\left(\partial_{3}, \ell_{2}\right),\left(\partial_{4}, \ell_{5}\right)\right\}$ |
| Method based on fairness degree model (M-4) (Method 3) | $\wp_{3}=\left\{\left(\partial_{1}, \ell_{4}\right),\left(\partial_{2}, \ell_{3}\right),\left(\partial_{3}, \ell_{1}\right),\left(\partial_{4}, \ell_{2}\right)\right\}$ |
| Method based on satisfaction and fairness degree model (M-6) (Method 4) | $\wp_{4}=\left\{\left(\partial_{1}, \ell_{5}\right),\left(\partial_{2}, \ell_{4}\right),\left(\partial_{3}, \ell_{2}\right),\left(\partial_{4}, \ell_{1}\right)\right\}$ |
| Method based on satisfaction and fairness degree model (M-7) (Method 5) | $\wp_{5}=\left\{\left(\partial_{1}, \ell_{5}\right),\left(\partial_{2}, \ell_{4}\right),\left(\partial_{3}, \ell_{2}\right),\left(\partial_{4}, \ell_{1}\right)\right\}$ |
| Extended method based on the idea of Lin et al. (2019) (Method 6) | $\wp_{6}=\left\{\left(\partial_{1}, \ell_{4}\right),\left(\partial_{2}, \ell_{5}\right),\left(\partial_{3}, \ell_{2}\right),\left(\partial_{4}, \ell_{1}\right)\right\}$ |
| Extension method based on the idea of Liu and Wang (2021) (Method 7) | $\wp_{7}=\left\{\left(\partial_{1}, \ell_{1}\right),\left(\partial_{2}, \ell_{4}\right),\left(\partial_{3}, \ell_{2}\right),\left(\partial_{4}, \ell_{5}\right)\right\}$ |

degrees and fairness degrees are calculated using the TODIM idea and the fair attenuation coefficients to construct multiple bilateral matching models. These models can be solved to obtain the optimal bilateral matching scheme.

Compared with the existing methods, the main innovations of this paper are as follows: (1) The proposed method enrich the application of linguistic intuitionistic fuzzy sets in the field of bilateral matching decision, and can provide theoretical references for solving linguistic intuitionistic fuzzy bilateral matching problems. (2) An unknown attribute weight calculation method considering the consistency of group opinions is proposed based on LIFIOWA operator. (3) A fair degree calculation method considering the fair attenuation coefficient is proposed. (4) Multiple bilateral matching models considering satisfaction and fairness degrees under a linguistic intuitionistic fuzzy environment are established.

Limitations of this paper are as follows: (1) The bilateral matching decision problem under a linguistic intuitionistic fuzzy environment is preliminary discussed. The theories of complex types of linguistic preference information needs to be further studied. (2) It is difficult to solve the more complex bilateral matching problem, such as the multi-attribute group decision, multi-attribute multilateral matching and multi-attribute stable matching. (3) A more precise calculation method for fairness degrees considering the fair attenuation coefficient has not been designed.

Future research will mainly focus on the following areas: (1) The multi-attribute bilateral matching problem under a more complex linguistic fuzzy environment needs further study, where the evaluation information of bilateral subjects may be different types of linguistic fuzzy sets. (2) The determination method for attribute weights under other types of linguistic fuzzy environment needs to be discussed. (3) Considering that an unstable bilateral matching scheme may reduce satisfaction degrees of the bilateral subjects, the relevant theories and methods for stable matching under linguistic intuitionistic fuzzy environment will be studied in future. (4) The method for determining the fair attenuation coefficient needs to be explored to calculate fairness degrees of bilateral subjects.

## Data availability

No data was used for the research described in this article.

## CRediT authorship contribution statement

Shijie Huang: Writing - review \& editing, Writing - original draft, Software, Methodology, Conceptualization. Qi Yue: Writing review \& editing, Writing - original draft, Supervision, Software, Methodology, Funding acquisition, Conceptualization. Yuan Tao: Writing - review \& editing, Writing - original draft, Supervision, Software.

## Declaration of competing interest

The authors declare the following financial interests/personal relationships which may be considered as potential competing
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