

Interfacial Tension of the Lipid Membrane Formed from Phosphatidylcholine–Decanoic Acid and Phosphatidylcholine–Decylamine Systems

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Abstract Interfacial tension has been determined for phosphatidylcholine (PC)–decanoic acid (DA) and PC–decylamine (DE) membranes. PC (lecithin), DA and DE were used in the experiments; the interfacial tension values of the pure components are 1.62×10^{-3} , -2.38×10^{-2} and -3.88×10^{-2} N/m (hypothetical values for DA and DE), respectively. The 1:1 complexes were formed during formation of PC–DA and PC–DE membranes. The following parameters describing the complexes were determined: the surface concentrations of the lipid membranes formed from these complexes, A_3^{-1} ; the interfacial tensions of such membranes, γ_3 ; and the stability constants of these complexes, K .

Keywords Interfacial tension · Phosphatidylcholine · Decanoic acid · Decylamine · Complex 1:1

Introduction

Biological membranes generally contain a mixture of various types of amphiphilic molecules, such as phospholipids, glycolipids, fatty acids, glycerides and amines. These components vary in chain length, saturation and type of chain linkage. Although present at levels of only a few percent, fatty acids and amines are important constituents

of biomembranes (Kumar et al. 2005). They can affect any physiological function, such as enzyme activity (Gennis 2010), particularly the activation of lipid-metabolizing enzymes, and calcium transport (Felix 2006).

Since fatty acids belong to the lipids that form biological membranes and at the same time also possess a quite simple structure, they are frequently used by researchers for modeling. It is clear that there is a certain equilibrium between the lipid-forming bilayer and lipid molecules and substances present in electrolyte solution. The interactions between membrane lipids are studied by several techniques; however, quantitative descriptions of the systems are lacking. Formation of artificial membranes with built-in study components allows us to research in simpler systems than complicated biological membranes.

Many investigations have been reported on the effect of fatty acids on physical and chemical properties of model membranes, particularly on the phase behavior of hydrated phospholipid bilayers, using various techniques, such as differential thermal analysis (Ulkowski et al. 2005), differential scanning calorimetry (Ohta and Hatta 2002; Matricarde Falleiro et al. 2010; Inoue et al. 2001), fluorescence spectroscopy (Borst et al. 2000), X-ray diffraction (Kumar et al. 2005), magnetic resonance (Heimburg et al. 1990; Rama Krishna and Marsh 1990) and Fourier transform infrared spectroscopy (Inoue et al. 2001).

In this work, the interfacial tension of phosphatidylcholine (PC)–decanoic acid (DA) and PC–decylamine (DE) membranes was determined within the entire composition range where bilayer formation was possible.

The aim of these investigations was to study the mixed PC–DA and PC–DE bilayer, characterize the molecular interaction between phospholipids and fatty acids and between phospholipids and amine and compare the properties of these systems: stability constants of the formed

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complexes and surface areas occupied by pure membrane components.

Theory

In cases where the membrane components do not form chemical compounds, their interaction can be described by the following set of equations (Petelska and Figaszewski 1998; Petelska et al. 2006a):

$$\begin{aligned} \gamma_1 m_1 A_1 + \gamma_2 m_2 A_2 &= \gamma \\ \frac{m_1}{m_1 + m_2} &= x_1 \\ x_1 + x_2 &= 1 \end{aligned} \quad (1)$$

where A_1^{-1} , A_2^{-1} (mol m^{-2}) are the surface concentrations of components 1 and 2; m_1 , m_2 (mol m^{-2}) are the quantities of components 1 and 2 per unit area of the membrane; γ_1 , γ_2 (N m^{-1}) are the interfacial tensions of membranes assembled from pure components 1 and 2; γ (N m^{-1}) is the measured interfacial tension of the membrane; and x_1 , x_2 are the solution mole fractions of components 1 and 2.

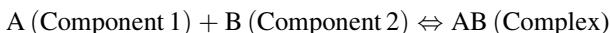
Elimination of m_1 and m_2 yields the following linear equation:

$$(\gamma - \gamma_1)x_1 = \frac{A_2}{A_1}(\gamma_2 - \gamma)x_2 \quad (2)$$

Membranes may also be assembled from two components capable of forming a complex. The stoichiometry of the complex may vary, but because the first stability constant in these complexes is usually the largest (Inczedy 1976; Beck and Nagypal 1990), we assumed that the complexes are primarily of 1:1 stoichiometry.

In cases where the membrane components form a 1:1 complex, interactions in the membrane may be described by a previously published set of equations (Petelska et al. 2006a, b).

The equilibrium between the individual components and the complex is represented by



and the basic equation describing the interaction between components 1 and 2 can be written as follows (Petelska et al. 2006a, b):

$$\begin{aligned} &[(\gamma - \gamma_1)B_2 x_1 + (\gamma - \gamma_2)B_1 x_2][(\gamma_3 - \gamma_1)B_2 x_1 \\ &+ (\gamma_3 - \gamma_2)B_1 x_2 + (\gamma_1 - \gamma_2)(x_1 - x_2)] \\ &= KA_3^{-1}B_1 B_2[(\gamma - \gamma_1)(x_2 - x_1) + (\gamma_3 - \gamma)B_1 x_2] \\ &\times [(\gamma - \gamma_2)(x_1 - x_2) + (\gamma_3 - \gamma)B_2 x_1] \end{aligned} \quad (3)$$

where $B_1 = A_3/A_1$ and $B_2 = A_3/A_2$.

Equation 3 may be simplified by taking into account the high stability constant of the complex. Applying this simplification results in linear behavior for small ($x_2 < x_1$) and

large ($x_2 > x_1$) x_2 values. When calculating the stability constant for the complex, Eq. 3 can be simplified to $x_1 = x_2$ (Petelska et al. 2006a, b).

The parameters describing the complex may be used to calculate theoretical points using the equation presented below (agreement between the theoretical and experimental values implies that the system is well described by the above equations):

$$\begin{aligned} &KA_1^{-1}A_2^{-1}(a_1 + a_2)(a_3 - a_1)\gamma^2 \\ &+ [KA_1^{-1}A_2^{-1}(\gamma_1 a_1 - \gamma_3 a_3)(a_1 + a_2) \\ &- KA_1^{-1}A_2^{-1}(\gamma_2 a_1 + \gamma_3 a_2)(a_3 - a_1) \\ &+ a_4 A_3^{-1}(a_3 + a_2)]\gamma \\ &+ KA_1^{-1}A_2^{-1}a_3\gamma_3(\gamma_3 a_2 + \gamma_2 a_1) \\ &- KA_1^{-1}A_2^{-1}a_1\gamma_1(a_1\gamma_2 + a_2\gamma_3) \\ &- a_4 A_3^{-1}(\gamma_2 a_3 + \gamma_1 a_2) = 0 \\ a_1 &= A_3^{-1}(x_2 - x_1) \\ a_2 &= A_2^{-1}x_1 \\ a_3 &= A_1^{-1}x_2 \\ a_4 &= [A_3^{-1}(\gamma_1 - \gamma_2)(x_2 - x_1) \\ &+ (\gamma_1 - \gamma_3)x_1 A_2^{-1} + (\gamma_2 - \gamma_3)x_2 A_1^{-1}] \end{aligned} \quad (4)$$

For systems containing two lipid components, 1:1 complex formation was assumed to be the explanation for deviation from the additivity rule. Model curves were constructed using calculated parameters such as equilibrium constants, molecular areas of the complexes and the interfacial tension of molecules and complexes. The accuracy of the models was verified by comparison to experimental results.

Experimental Procedure

Measuring Apparatus and Measuring Procedures

The interfacial tension method is based on Young and Laplace's equation. The tension in a lipid bilayer sample is determined by measuring the radius of curvature of the convex surface formed when a pressure difference is applied across the bilayer (Adamson 1960).

The apparatus and measurement method were described previously (Petelska and Figaszewski 1998; Petelska et al. 2006a, b). The measurement system consists of two glass chambers separated by a mount holding a 1.5-mm-diameter circular Teflon element axially pierced by a small orifice.

Membranes were formed by the Mueller–Rudin method (Tien and Ottova-Leitmannova 2003) on the flat end of the Teflon element. Both chambers were filled with an electrolyte solution. The membrane-forming solution was

introduced to the flat wall of the Teflon element using a micropipette, and pressure was applied to the left chamber using a manometer.

The convexity of the lipid membrane cap was measured to 0.05 mm precision. The radius of curvature was determined using this value and the diameter of the Teflon element, corresponding to diameter of the lipid cap.

Reagents

The following reagents were used for preparation of the membrane-forming solution:

1. 3-sn-phosphatidylcholine (99%; Fluka, Buchs, Switzerland) isolated from hen egg yolk
2. Decanoic acid (98%, Fluka)
3. Decylamine (99.5%, Fluka)

The as-received PC and DA were purified by dissolving in chloroform and evaporating the solvent under argon. The stock membrane-forming solutions consisted of 20 mg cm⁻³ of the desired lipids (PC, DA or DE) in 20:1 n-decane:butanol. The solution containing the membrane components was not saturated and could therefore contain the components in any proportion. During membrane formation, the solvent was removed, leaving a membrane composed of lipids in the same ratio as the stock solution.

The electrolyte solution contained 0.1 M potassium chloride and was prepared using triple-distilled water and KCl, produced by POCh (Gliwice, Poland). The KCl was calcined to remove any organic impurities.

All solvents were chromatographic standard grade. The n-decane was purchased from Merck (Darmstadt, Germany), and the chloroform and butanol were obtained from Aldrich (Milwaukee, WI).

All experiments were carried out at 293 ± 2 K.

Results and Discussion

The effect of the presence of DA or DE on interfacial tension of the membranes formed from PC was studied. The dependence of interfacial tension on the lipid membrane as a function of composition was studied at room temperature (293 ± 2 K) in the entire feasible concentration range. The interfacial tension values reported here refer to the two sides of the bilayer membrane surface area unit.

Figure 1 contains a graph of $(\gamma - \gamma_1)x_1$ vs. $(\gamma_2 - \gamma)x_2$ for the four systems PC-DA (Fig. 1a) and PC-DE (Fig. 1b). According to Eq. 2, when the membrane components do not interact, these functions should yield straight lines. This is clearly not the case, which suggests that a complex or other structure exists in PC-DA and

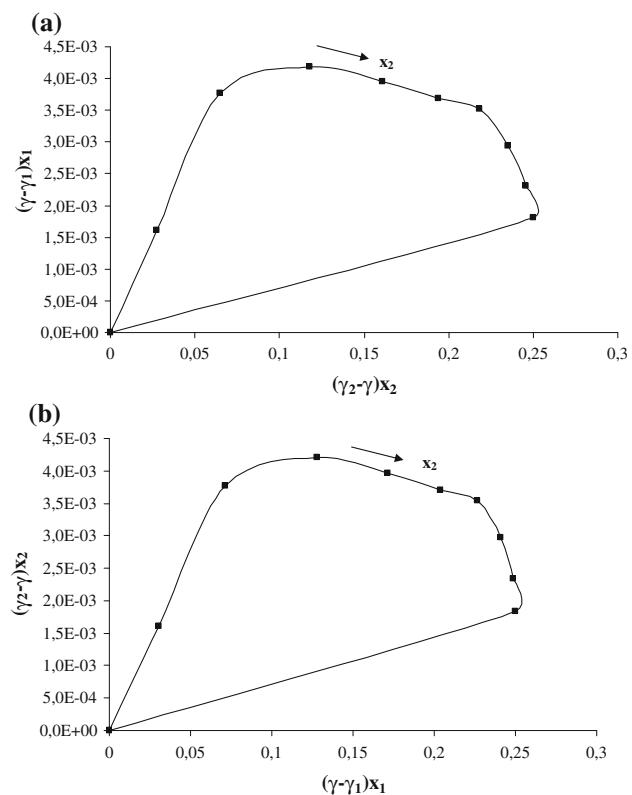


Fig. 1 Graph of Eq. 2 for PC-DA (a) and PC-DE (b), where x_2 is the mole fraction of component 2 (DA and DE, respectively)

PC-DE bilayers. Because the use of Eq. 3 presupposes the existence of 1:1 complexes, our initial assumption was that the complexes formed were 1:1. The interfacial tension of the lipid membrane was studied over a wide range of lipid compositions.

The dependence of interfacial tension of lipid membrane as a function of membrane composition for PC-DA and PC-DE systems was studied over a possible concentration range. The results are depicted in Fig. 2a, b. The dependence of interfacial tension on the lipid membranes formed from the PC-DA and PC-DE systems was executed in the function of the composition to 41% of the DA contents (to 40% of the DE) because only to such contents of component 2 (DA, DE) with lecithin was a bilayer membrane formed.

The interfacial tension value of pure lecithin membrane (component 1), γ_1 , was measured directly and presented earlier (Petelska and Figaszewski 1998), which is equal to 1.62×10^{-3} N m⁻¹. There are no accurate data on interfacial tension values for the pure component 2 (DA or DE) because these components do not create a bilayer membrane. However, in order to characterize the course of the experimental curves, the γ_2 value for the pure components is necessary, which will be used for calculation. In this case, the interfacial tension hypothetical values for membranes built from DA and DE were determined by adjusting the

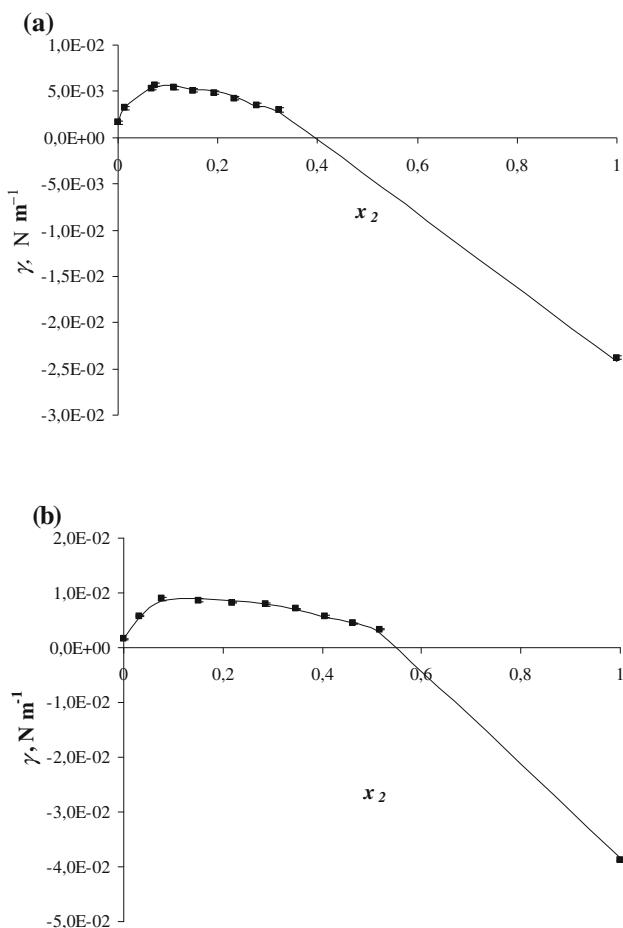


Fig. 2 The interfacial tension, γ , of the PC–DA (a) and PC–DE (b) membranes as a molar fraction of DA or DE, x_2 (experimental values are marked by *points* and theoretical ones by *curves*)

experimental curve with the polynomial of the other mark extrapolating the $x_2 = 1$ value, which is presented in Fig. 3. The interfacial tension values obtained in this way for pure DA and DE are equal to -2.38×10^{-2} and $-3.88 \times 10^{-2} \text{ N m}^{-1}$. Negative values of interfacial tension for membrane built from pure DA and DE point to the fact that it is not possible to create bilayer membranes from pure DA or DE. The thermodynamic potential for this bilayer would have a negative value; i.e., the bilayer is not forming.

The other constants— B_1 , B_2 , γ_3 —were determined by assuming that the values of the stability constant of the PC–DA and PC–DE complexes were sufficient to be simplified, i.e., Eq. 1 to Eqs. 2 and 3. Knowing the B_1 , B_2 constants, which were determined from Eqs. 2 and 3, it was possible to calculate the interfacial tension values of the PC–DA and PC–DE complexes, γ_3 . The mean values are equal to $7.25 \times 10^{-3} \text{ N m}^{-1}$ for PC–DA and $1.52 \times 10^{-2} \text{ N m}^{-1}$ for PC–DE.

Determining the interfacial tension value as a function of the composition made it possible to determine the surface concentrations of the membranes composed of pure

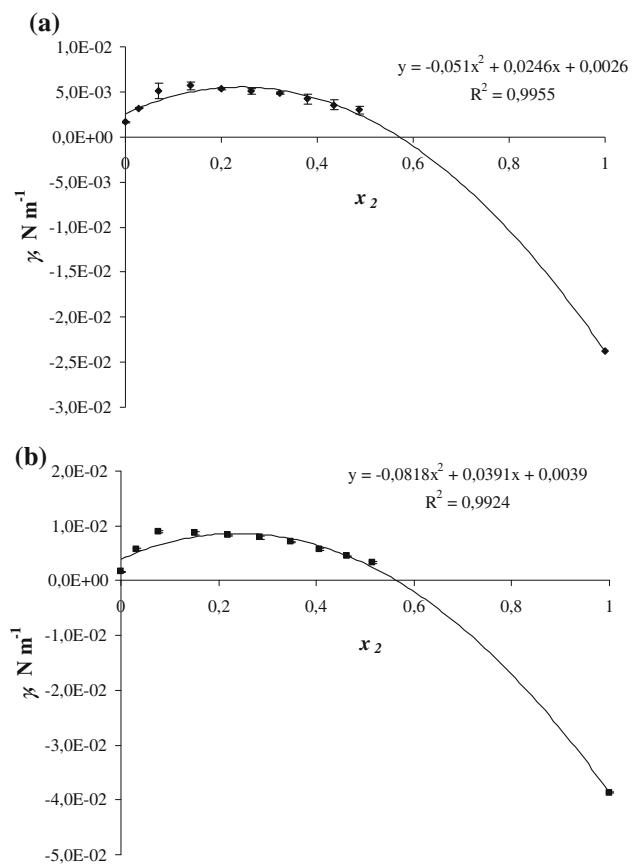


Fig. 3 Plot illustrating the hypothetical interfacial tension values for DA (a) and DE (b) membrane calculation

components. At least one of them is necessary for determination of the A_3^{-1} value. The surface area occupied by a lecithin molecule equal to 85 \AA^2 was determined in previous work (Petelska and Figaszewski 2000). The surface areas occupied by DA and DE are equal to 19 and 22 \AA^2 , respectively (Petelska and Figaszewski 2011). As mentioned earlier, the fatty acid forms a dimer (Brzozowska and Figaszewski 2003; Zhao and Olesik 2001); therefore, the surface area occupied by DA is equal to 38 \AA^2 .

Knowing the A_1^{-1} and A_2^{-1} as well as B_1 and B_2 values, the surface concentration of the membrane composed of the lecithin–DA and lecithin–DE complexes could be determined. The resulting surface concentration values, A_3^{-1} , for the PC–DA and PC–DE complexes were equal to 1.15×10^{-6} and $2.03 \times 10^{-6} \text{ mol m}^{-2}$, respectively. This made it possible to determine the area occupied by one lecithin–DA and one lecithin–DE complex, which were 144 and 82 \AA^2 , respectively. The value of area occupied by one lecithin–DA complex molecule is larger than the amount of the surface area occupied by each component of the complex. It is probably connected with the arrangement of lecithin molecules in such a complex and with the structural construction of such a complex. Previously

(Petelska and Figaszewski 2003), we suggested the arrangement of the lecithin molecules in a bilayer membrane at pH > 5. In these media, one particle from the lecithin molecule in the bilayer (orientated in this way) has two straightened chains; however, the next molecule of lecithin has one straightened and another chain fastened to the membrane surface. An association of ions occurs in such conditions with OH⁻ from the electrolyte solution. How these ions were characterized was previously reported (Petelska and Figaszewski 2003): These ions are strongly solvated, and they produce a separation of lecithin particles in the bilayer, which increases the surface occupied by the single molecule of lecithin.

The difference between surface area values occupied by one molecule of PC-DA and PC-DE complexes to appear from the fact than as the chain length increases, van der Waals interactions between the chain of the adjacent molecule increase, bringing these molecules closer to each other. When this happens, the carboxylic acid groups of the fatty acids are also packed closer, shielding the hydrogen atom between the two oxygen atoms (Kanicky et al. 2000; Kanicky and Shah 2002).

The only values to be determined were the stability constants of the PC-fatty acid and PC-amine complexes. It could be determined from Eq. 4 when $x_1 = x_2 = 0.5$; these parameters amount to 4.61×10^6 and $2.38 \times 10^5 \text{ m}^2 \text{ mol}^{-1}$, respectively. During the course of our investigations, we assumed the formation of PC-DE and PC-DE complexes. These complexes arise by producing a connection between the $-\text{N}(\text{CH}_3)_3^{(+)}$ group from the molecule of lecithin and $-\text{COO}^{(-)}$ groups from the dimer of DA, in the case of the complex PC-DA, and between the $-\text{PO}^{(-)}$ group from lecithin and the $-\text{NH}_3^{(+)}$ group from DE. The dissociation constants of the $-\text{N}(\text{CH}_3)_3^{(+)}$ group from PC and the $-\text{COO}^{(-)}$ groups from the dimer of DA are equal $10^{-5.7}$ (Petelska and Figaszewski 2000) and about 10^{-5} (Chemistry Tables 2004), respectively. It should be noted that the dissociation constants of the $-\text{PO}^{(-)}$ group from PC and the $-\text{NH}_3^{(+)}$ group from DE equal $10^{-2.6}$ (Petelska and Figaszewski 2000) and about 10^{-10} (Chemistry Tables 2004), respectively. Therefore, the connection between PC and DA will be stronger, and we can expect that the stability

constant of PC-DA will be higher than the stability constant of PC-DE.

The parameters describing these complexes determined from Eqs. 1 and 4 were in agreement with Eq. 1; i.e., data (solid lines) with the experimental data (points) in Fig. 1 using equation 5. As it is a square equation, this equation can yield two solutions. The values yielding a better agreement of the experimental points with equations describing complex formation between membrane lipid components were chosen.

The experimental values in Fig. 1 are marked by points and the theoretical ones obtained from equation 5, by lines. It can be seen from this figure that there is a good agreement between experimental and theoretical points, which verifies the assumption of formation of 1:1 PC-DA and PC-DE complexes in the lipid membrane. Good agreement of the experimental and theoretical points verifies the assumption of the correct choice of the γ_2 values for components of the membrane.

Table 1 lists several physicochemical parameters for membranes containing PC-DA and PC-DE complexes.

Conclusion

The following conclusions can be drawn from the parameters describing the complexes studied:

1. The stability constant of the PC-DA complex is $4.61 \times 10^6 \text{ m}^2 \text{ mol}^{-1}$, whereas the stability constant of the PC-DE complex is $2.38 \times 10^5 \text{ m}^2 \text{ mol}^{-1}$. High values confirm the legitimacy of simplifying Eq. 1. The values of the stability constants of the lipid-DA and lipid-DE complexes are reported for the first time. It can be observed that the stability constants of the fatty acid-containing complex are higher. Thus, the PC-DA complex is more stable than the PC-DE complex.
2. The experimental area occupied by one PC-DA complex is 144 \AA^2 , whereas the area occupied by the PC-DE complex is 82 \AA^2 .
3. Good agreement of the experimental and theoretical points verifies the assumption of formation of a 1:1 complex in the lipid membrane. A lack of variance between points indicates that complexes at different stoichiometries are not possible in the PC-DA or PC-DE membrane.

Table 1 Selected physicochemical parameters for two complexes: phosphatidylcholine-decanoic acid (PC-DA) and phosphatidylcholine-decylamine (PC-DE)

Examined system	Surface area occupied by one molecule of complex ($\text{\AA}^2 \text{ molecule}^{-1}$)	Stability constant of examined complex ($\text{m}^2 \text{ mol}^{-1}$)	Complex formation energy (Gibbs free energy) (kJ mol^{-1})
PC-DA	144 ± 1.44	4.61×10^6	-40.01 ± 1.20
PC-DE	82 ± 0.82	2.38×10^5	-32.45 ± 0.97

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