



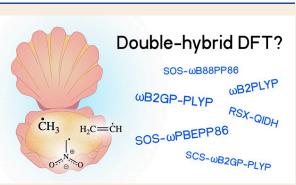
Article

# Assessing Recent Time-Dependent Double-Hybrid Density Functionals on Doublet–Doublet Excitations

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ABSTRACT: This work is the first thorough investigation of timedependent double-hybrid density functionals (DHDFs) for the calculation of doublet-doublet excitation energies. It sheds light on the current state-of-the-art techniques in the field and clarifies if there is still room for future improvements. Overall, 29 hybrid functionals and DHDFs are investigated. We separately analyze the individual impacts of the Tamm-Dancoff approximation (TDA), range separation, and spin-component/opposite scaling (SCS/SOS) on 45 doublet-doublet excitations in 23 radicals before concluding with an overarching analysis that includes and excludes challenging excitations with double-excitation or multireference character. Our results show again that so-called "nonempirical" DHDFs are outperformed by semiempirical ones. While the best assessed functionals are DHDFs,



some of the worst are also DHDFs and outperformed by all assessed hybrids. SCS/SOS is particularly beneficial for range-separated DHDFs. Spin-scaled, range-separated DHDFs paired with the TDA belong to the best tested methods here, and we particularly highlight SCS- $\omega$ B2GP-PLYP, SOS- $\omega$ B2GP-PLYP, SOS- $\omega$ B2GP-PLYP, SOS- $\omega$ B88PP86, SOS-RSX-QIDH, and SOS- $\omega$ PBEPP86. When comparing our functional rankings with previous studies on singlet–singlet and singlet–triplet excitations, we recommend TDA-SOS- $\omega$ B88PP86 and TDA-SOS- $\omega$ PBEPP86 as robust methods for excitation energies in general until further improvements have been achieved that surpass the chemical accuracy threshold for challenging open-shell excitations without increasing the computational effort.

**KEYWORDS:** time-dependent density functional theory, double hybrids, time-dependent double hybrids, excited states, radicals, open-shell excitations, benchmarking

# 1. INTRODUCTION

Density functional theory<sup>1,2</sup> (DFT) is the most popular methodology for computational chemistry calculations, in large part due to its efficiency compared to methods based entirely on wave function theory (WFT). Despite DFT being exact in principle, the functional that describes electron correlation and exchange is not known and must be approximated. The success of DFT is therefore highly dependent on the selection of the density functional approximation (DFA). The number of available DFAs continues to grow steadily, with each new DFA attempting to more accurately describe challenging quantummechanical effects without significantly increasing computational cost. Initial DFT methods, based on the Hohenberg-Kohn theorems<sup>1</sup> and the Kohn-Sham equations,<sup>2</sup> were only applicable to ground-state problems. In 1984, Runge and Gross developed equivalent theorems for excited-state calculations,<sup>3</sup> paving the way for time-dependent DFT (TD-DFT). As TD-DFT requires an initial ground-state DFT calculation as input, its success is also dependent on the underlying DFA. In TD-DFT calculations, matrices for both single-particle excitations and de-excitations are used. However, computational cost can

be decreased by using only the excitation matrix. This simplification is known as the Tamm–Dancoff approximation (TDA) leading to TDA-DFT applications.<sup>4</sup>

When considering DFT's metaphorical "Jacob's Ladder",<sup>5</sup> the description of electronic excitations with linear-response TD-DFT only becomes reasonable by using good representatives from at least the fourth rung of the ladder,<sup>6–8</sup> namely hybrid DFAs, which combine semilocal exchange and correlation from DFT with nonlocal Fock exchange originally derived for WFT. Even better results for excitation energies are obtained when going to the fifth rung, namely, double-hybrid density functionals (DHDFs)<sup>9,10</sup> which improve the description of electron correlation by adding information from unoccupied (virtual) molecular orbitals in the form of a

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In the past, several attempts have been made to improve upon the initial TD(A)-DHDFs. Most notably those were the introduction of spin-component and spin-opposite scaling<sup>22-25</sup> (SCS/SOS) to the perturbative part by Schwabe and Goerigk in 2017,<sup>17</sup> and the introduction of range separation<sup>26-29</sup> to non-SCS/SOS TD-(A)DHDFs by Casanova-Páez, Dardis, and Goerigk in 2019.<sup>18</sup> The latter improvement was an important step forward because prior to 2019 TD(A)-DHDFs following the Grimme-Neese idea had had the same incorrect decay of the exchange potential and electron density as other global DFAs.<sup>7,18,19,30-33</sup> This incorrect decay had caused global DHDFs to inadequately describe long-range transitions, in particular charge-transfer (CT) excitations. One popular attempt to combat this issue is range separation, also known as long-range correction,<sup>26–29</sup> which has been successfully applied to hybrid DFAs. The aforementioned work in 2019 followed the same spirit and introduced the first rangeseparated TD-DHDFs optimized for excitation energies called  $\omega$ B2PLYP and  $\omega$ B2GP-PLYP.<sup>18</sup> They seamlessly connect hybrid-DFT exchange in the short-range regime of the electron-electron distance with 100% Fock exchange in the long-range. Establishing 100% Fock exchange in the long-range has been the underlying principle in most range-separated DFAs in the past, with the CAM-B3LYP hybrid being a notable exception.<sup>28</sup> The strongly improved performance of  $\omega$ B2PLYP and  $\omega$ B2GP-PLYP has been demonstrated for singlet-singlet and singlet-triplet transitions, including for some infamously challenging local-valence, Rydberg, and CT excitations,<sup>18,19,30</sup> such as in polycyclic aromatic hydrocarbons.<sup>18</sup>

Further improvements of global and range-separated (in the exchange part) TD(A)-DHDFs have been achieved by our group in 2021 by revisiting the impact of SCS and SOS techniques.<sup>20</sup> In SCS/SOS, the perturbative component of the electron correlation energy is split into energies of electron pairs of same and opposite spin and those components are individually scaled. For instance, in the original SCS-MP2 from 2003 this prevented the overestimation of same-spin correlation.  $^{22}$  By ignoring the same-spin part, SOS-based methods can achieve an improved formal scaling behavior, which makes them particularly valuable for larger systems.<sup>2</sup> The superior performance of some of the 14 developed SCS/ SOS-based TD(A)-DHDFs has been demonstrated for singlet-singlet and singlet-triplet excitations with the best methods outperforming our original 2019 approaches, as well as some alternative DHDF definitions published in 2021,<sup>34,35</sup> which also employ range separation in the perturbative part.<sup>20</sup>

Nearly all benchmark studies exploring TD(A)-DHDFs dealt with closed-shell systems, and assessments of open-shell systems have been rare and very limited in scope. In 2007, Grimme and Neese assessed TDA-B2PLYP on 11 small radicals.<sup>11</sup> The only other two examples in the literature are the limited study of six open-shell atoms<sup>36</sup> and seven molecular open-shell systems<sup>37</sup> with four global DHDFs. To our knowledge, no systematic study of open-shell excitations has been conducted that also involves the latest developments in this area. Herein, we intend to close this knowledge gap. Our

study will be conducted on a set of 45 doublet–doublet excitations in 23 molecular radicals initially presented and analyzed with WFT methods by Loos, Jacquemin, and coworkers (Figure 1).<sup>38</sup> In particular, we will compare TD(A)-

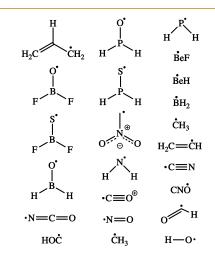


Figure 1. Set of 23 radicals published in ref 38.

DHDFs with hybrid functionals and separately address the impact of the TDA, range separation, and SCS/SOS on the excitation energies. Note that this radical set has later been included in the QUEST database,<sup>39</sup> which comprises 470 excitations distributed over five sets,<sup>38–42</sup> some of which have been previously used by our group to assess TD(A)-DHDFs.<sup>19,20</sup>

This is the most thorough study of DHDFs on open-shell systems, and it will provide insights on the current state-of-theart in the field of DHDFT for excitation energies, which will inform us of whether they perform as well as for closed-shell systems or whether there is the necessity for further developments.

#### 2. THEORETICAL BACKGROUND

According to Grimme, a DHDF consists of two components: a hybrid component and an additional second-order perturbative correlation term.<sup>9</sup> Herein, we only discuss DHDFs that include range separation solely in the exchange part, but range separation has also been suggested in the correlation portion.<sup>34,35</sup> Details on time-dependent DHDFs with and without SCS/SOS have been extensively provided in the literature,<sup>8,17,20</sup> here we only discuss the basics.

Vertical excitation energies for real orbitals are computed by solving the random-phase approximation (RPA) problem:<sup>43</sup>

$$\begin{pmatrix} \mathbf{A} & \mathbf{B} \\ \mathbf{B} & \mathbf{A} \end{pmatrix} \begin{pmatrix} \mathbf{X} \\ \mathbf{Y} \end{pmatrix} = \Delta E_{\text{TD-DFT}} \begin{pmatrix} 1 & 0 \\ 0 & -1 \end{pmatrix} \begin{pmatrix} \mathbf{X} \\ \mathbf{Y} \end{pmatrix}$$
(1)

where  $\Delta E_{\text{TD-DFT}}$  is the vertical excitation energy and X and Y are the eigenvectors for single-particle excitations and deexcitations, respectively. A and B are matrices containing information on these excitations and de-excitations. By removing the B matrix from eq 1, a simplified equation, the Tamm–Dancoff approximation,<sup>4</sup> is obtained:

$$\mathbf{A}\mathbf{X} = \Delta E_{\mathrm{TDA-DFT}}\mathbf{X} \tag{2}$$

According to Grimme and Neese, vertical excitation energies at the double-hybrid level are obtained by first solving the TD(A)-DFT eigenvalue problem with only the hybrid portion of the DHDF ( $\Delta E_{\text{TD}(A)-\text{hybrid}}$  in eq 3) and then adding Head-Gordon and co-workers' CIS(D) perturbative correction  $(\Delta_{\text{CIS}(D)})$ :<sup>44</sup>

$$\Delta E_{\rm TD(A)-DHDF} = \Delta E_{\rm TD(A)-hybrid} + a_{\rm C} \Delta_{\rm CIS(D)}$$
(3)

The parameter  $a_{\rm C}$  in eq 3 scales the CIS(D) contribution akin to ground-state DHDF calculations.<sup>11</sup>

According to Schwabe and Goerigk,<sup>17</sup> TD(A)-SCS/SOS-DHDF excitation energies are obtained by adding an SCS/ SOS-CIS(D)<sup>24</sup> correction ( $\Delta_{SCS/SOS-CIS(D)}$ ) to the TD(A)hybrid energy:

$$\Delta E_{\rm TD(A)-SCS/SOS-DHDF} = \Delta E_{\rm TD(A)-hybrid} + \Delta_{\rm SCS/SOS-CIS(D)}$$
(4)

 $\Delta E_{\rm TD(A)-hybrid}$  can be based on either a global or rangeseparated DHDF description.<sup>17,20</sup> An alternative SCS/SOS-DHDF definition in which the SCS/SOS-CIS(D) part is split into short- and long-range components has been recently suggested<sup>35</sup> but cannot be tested herein for technical reasons. Instead, we focus on TD(A)-DHDFs as defined above.

# 3. COMPUTATIONAL DETAILS

A local version of ORCA  $4.2.1^{45-47}$  was used to calculate the doublet-doublet excitation energies for the radical set. A total of 29 functionals were assessed, as listed in Table 1. All

#### Table 1. List of Assessed Functionals<sup>a</sup>

	global	range-separated
hybrid	B3LYP <sup>54,55</sup> BHLYP <sup>56</sup> PBE0 <sup>57,58</sup>	CAM-B3LYP <sup>28</sup>
double-hybrid	B2PLYP <sup>9</sup> SOS-B2PLYP <sup>20</sup> B2GP-PLYP <sup>60</sup> SCS-B2GP-PLYP <sup>20</sup> SOS-B2GP-PLYP <sup>20</sup> PBE0-DH <sup>61</sup> PBE-QIDH <sup>63</sup> SCS-PBE-QIDH <sup>20</sup> SOS-PBE-QIDH <sup>20</sup>	$\omega$ B97X <sup>59</sup> $\omega$ B2PLYP <sup>18</sup> SOS- $\omega$ B2PLYP <sup>20</sup> $\omega$ B2GP-PLYP <sup>18</sup> SCS- $\omega$ B2GP-PLYP <sup>20</sup> SOS- $\omega$ B2GP-PLYP <sup>20</sup> SOS- $\omega$ B2GP-PLYP <sup>20</sup> RSX-0DH <sup>62</sup> RSX-0DH <sup>62</sup> RSX-QIDH <sup>64</sup> SCS-RSX-QIDH <sup>20</sup> $\omega$ SOS-PBE-QIDH <sup>20</sup> $\omega$ B88PP86 <sup>20</sup> SCS- $\omega$ B88PP86 <sup>20</sup> SOS- $\omega$ B88PP86 <sup>20</sup> SOS- $\omega$ B88PP86 <sup>20</sup> SOS- $\omega$ PBEPP86 <sup>20</sup> SCS- $\omega$ PBEPP86 <sup>20</sup>

<sup>a</sup>Global and range-separated methods appearing in the same row are related.

functionals assessed herein are available in the newly released ORCA 5. As explained in ref 20, the SCS fit for B2PLYP and  $\omega$ B2PLYP led to the SOS variant. Herein, we use the shorthand notation "SOS-B2PLYP" and "SOS- $\omega$ B2PLYP" to refer to these two functionals, which are labeled SCS/SOS-B2PLYP21 and SCS/SOS- $\omega$ B2PLYP21, respectively, in ref 20. Note that we did not assess DFAs from rungs one to three of Jacob's Ladder as it is has been established that they are not suitable for the description of excitation energies due to large errors and the emergence of ghost states.<sup>6,8,14</sup> Instead, we focus on the assessment of new or popular DFAs from rungs four and five.

For all calculations, the SCF convergence criterion was set to  $10^{-8}E_{\rm h}$  and ORCA's numerical quadrature grid "5" and "finalgrid 6" were used. The resolution of the identity approximation was used with appropriate auxiliary basis sets for the perturbative parts of DHDFs.

Preoptimized  $UCCSD(T)^{48}/aug\text{-cc-pVTZ}^{49-51}$  groundstate geometries from ref 38 were used.  $UCC3^{52,53}/aug\text{-cc-}$ PVTZ excitation energies from ref 38 were used as reference energies in the statistical evaluation. The aug-cc-pVTZ basis set was used for all calculations presented herein to enable a direct comparison to the reference values. While a wave function method might have a slower basis set convergence than a DFT-based one, getting similar accuracy for the latter with the same basis set is a worthwhile achievement given the higher computational cost of wave function methods. Moreover, it has been established that TD-DHDFs are practically converged for excitation energies for large basis sets of triple- $\zeta$ quality.<sup>17</sup>

Two transitions listed in ref 38 were not analyzed in this paper due to some excited states being inexplicably missing when calculated with ORCA. These are the  ${}^{2}\Sigma^{+}$  transition of the CH radical and the second  ${}^{2}\Pi$  transition of the BeH radical. We would also like to point out that the tested systems are challenging and the automated assessment of all 29 functionals was not always straightforward, for instance due to swapping of states or the emergence of very close-lying states for some DFAs. In some instances, UCCSD energies from ref 38 had to be reproduced to obtain information about the correct orbital contributions. A very challenging excitation that showed multiple problems of this nature is the  ${}^{2}\Sigma^{+}$  transition in CO<sup>+</sup>. As we will discuss later, it also showed large doubleexcitation character and due to our observed problems we also excluded this state from our analysis. The complete set analyzed herein, thus, comprises 45 excitations.

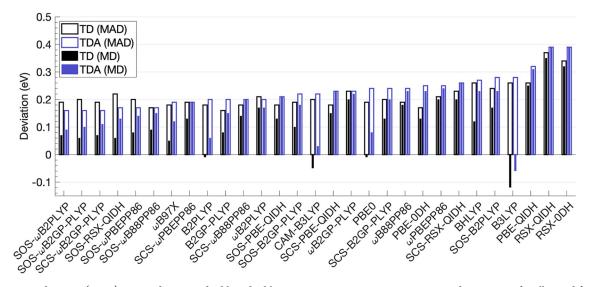
%T1 values were obtained with UCCSD calculations where necessary.

# 4. RESULTS AND DISCUSSION

We separate the discussion of our results into five brief sections. First, we analyze the differences between the use of TD- and TDA-DFT for the functionals tested. Then, we look at the effects of range separation and the impact of spincomponent/spin-opposite scaling on DHDFs. Following that, we compare DHDFs against conventional hybrids and comment on the robustness of particular functionals. Those first four sections comprise our results for all 45 excitations. The discussion then concludes with a second analysis that excludes four states due to high double excitation or multireference character. Throughout our discussion, a deviation is defined as the difference between the DFA and reference value, which means that negative deviations and mean deviations (MDs) stand for underestimated excitation energies. Individual excitations for each DFA as well as all statistical metrics, including root-mean-square deviations (RMSDs), minimum and maximum deviations, and deviation spans, are available in the Supporting Information (SI).

#### 4.1. On the Tamm–Dancoff approximation

The TDA is attractive to computational chemists due to its improved computational efficiency over TD-DFT. A second reason for preferring the TDA is that triplet instability issues lead to severely underestimated triplet excitations in TD-DFT.<sup>65–68</sup> While those instabilities are not solved by the TDA,



**Figure 2.** MDs and MADs (in eV) averaged over 45 doublet-doublet excitation energies using TD-DFT and TDA-DFT for all tested functionals, ranked by TDA MAD, followed by RMSDs and then absolute MDs in the case of identical MADs.

it induces a blue shift; as a result, TDA-DFT frequently produces more accurate singlet—triplet excitation energies than TD-DFT, which is also true for DHDFs.<sup>19,20</sup> Herein, we intend to determine whether this trend also applies to doublet—doublet excitations.

In Figure 2, we present the MDs and mean absolute deviations (MADs) of the 29 DFAs tested with TD- and TDA-DFT for the entire set of 45 excitations. Immediately notable is that doublet-doublet excitations are not subject to instability issues.  $\omega$ B2PLYP's MD is the only one not affected by the TDA. For all other functionals, there is an increase in MD from TD-DFT to TDA, ranging from 0.02 to 0.11 eV. The smallest MD increase is from TD-SOS-wB2PLYP to TDA-SOS- $\omega$ B2PLYP (from 0.07 to 0.09 eV) and from TD- $\omega$ B2GP-PLYP to TDA- $\omega$ B2GP-PLYP (from 0.20 to 0.22 eV). At the other end, the MD of BHLYP increases from 0.12 to 0.23 eV for the TDA. The increased MDs indicate that the TDA causes a systematic blueshift in excitation energies across the entire radical set, which is a known trend for other excitation types.<sup>19,30</sup> While this is unfavorable for most functionals, this blueshift improves some MDs; for instance, the blueshift results in an MD of -0.06 eV for TDA-B3LYP, which is more favorable than the -0.12 eV obtained with TD-B3LYP. Despite this, the MAD of TDA-B3LYP is 0.02 eV higher than TD-B3LYP. This indicates that the set contains examples of already blueshifted excitation energies at the TD-DFT level, whose deviations are exacerbated due to the additional blueshift from the TDA.

Interestingly, an increase in MD can still coincide with reduced deviation spans. For instance, despite an increase of 0.11 eV in the MD when going from TD- to TDA-BHLYP, we observe a decrease in the deviation span of 1.01 eV (see the SI). Other notable reductions in the deviation span of about 0.5 eV or more for the TDA are observed for B2PLYP, SOS-B2PLYP,  $\omega$ B2PLYP, and SOS- $\omega$ B2PLYP. While deviation spans are only marginally affected by the TDA for a large number of functionals, the largest increase of 0.16 eV is observed for B2GP-PLYP (see the SI).

In most cases, the systematic blueshift observed with a TDA approach also corresponds to an increase in MAD, however, with all increases being slightly under the chemical-accuracy threshold of 0.1 eV.<sup>6,69</sup> There are some notable exceptions: all variations of  $\omega$ B2PLYP have slightly lower MADs when using the TDA (decreases in MAD of 0.03 and 0.01 eV for SOS- $\omega$ B2PLYP and  $\omega$ B2PLYP, respectively). Employing the TDA also decreases MADs for SCS/SOS-wB2GP-PLYP, SOS-RSX-QIDH, and SOS-*w*PBEPP86. No MAD changes are observed for *w*B2GP-PLYP, SOS-*w*B88PP86, and SCS-*w*PBEPP86. Across the TDA results, the lowest MAD is 0.16 eV for SCS- and SOS-wB2GP-PLYP as well as SOS-wB2PLYP. This is also the lowest-found MAD value across the entire set of 45 excitations and all assessed functionals. SOS-RSX-QIDH, SOSwB88PP86, and SOS-wPBEPP86 perform similarly, with MADs of 0.17 eV. At 0.19 eV, SCS-@PBEPP86 is the only remaining TDA-DHDF with an MAD below 0.2 eV. Note that we adopted a 0.1 eV chemical-accuracy threshold to be commensurate with other TD-DHDF papers. We acknowledge that, in both ground and excited states, the idea of a chemical accuracy threshold is somewhat arbitrary. As this issue has already been discussed elsewhere and has no influence on our findings and functional rankings, we refer the reader to ref 19 for a discussion of the original literature around this topic.

Considering previous works that show that TD-DFT is unsuitable for singlet-triplet excitations,<sup>19,20,65,67,68,70</sup> the performance of these TDA-DHDFs makes them attractive for the calculation of doublet-doublet excitations. For the remainder of the analysis in this paper, we refer to only TDA excitation energies unless explicitly specified otherwise. The full set of TD- and TDA-DFT data is available in the SI.

# 4.2. Effects of Range Separation

The next aspect we investigate is range separation. The MDs and MADs of five global, unscaled DFAs and their rangeseparated counterparts are presented in Figure 3. In all of these cases, the range-separated functionals have more positive MDs than the global counterparts. Systematic blueshift from range separation is a known effect for DFAs, including DHDFs.<sup>8,18,19,30</sup>  $\omega$ B2GP-PLYP is the least blueshifted by range separation (an increase in MD of 0.07 eV from B2GP-PLYP to  $\omega$ B2GP-PLYP), and RSX-0DH shows the largest MD increase of 0.16 eV (from PBE0-DH to RSX-0DH).

For three of the four herein tested unscaled range-separated DHDFs ( $\omega$ B2GP-PLYP, RSX-0DH, and RSX-QIDH), the

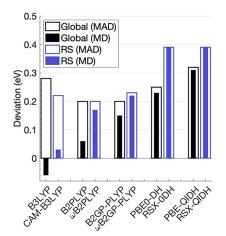


Figure 3. MDs and MADs (in eV) for global and range-separated (RS) functionals using TDA-DFT.

MADs are larger than those for their global counterparts. Of these, the smallest increase is 0.03 eV for  $\omega$ B2GP-PLYP and the largest increase, 0.14 eV, is again for RSX-0DH. B2PLYP and  $\omega$ B2PLYP share the same MAD. Interestingly, the range-separated hybrid CAM-B3LYP does not follow this trend. The MAD for CAM-B3LYP is 0.22 eV and therefore lower than the MAD of 0.28 eV for B3LYP. In this case, range separation improves the performance of the underlying functional, which may be due to the inclusion of 65% Fock exchange at long-range compared to 100% for the other range-separated functionals.

The trends observed for range separation become more complex when we introduce spin-component and spinopposite scaling, where we observe reductions of up to 0.14 eV in MD and 0.12 eV in MAD (from SOS-B2PLYP to SOS- $\omega$ B2PLYP) and the only marginal increase is seen when moving from SCS-PBE-QIDH to SCS-RSX-QIDH (0.03 eV both for MD and MAD) (see the SI). The impact of SCS and SOS is discussed in more detail in the following section.

#### 4.3. Impact of Spin-Component and Spin-Opposite Scaling

The effects of SCS and SOS on the MDs and MADs of eight unscaled parent DFAs are illustrated in Figure 4. For the vast majority of DFAs, SCS/SOS results in MDs and MADs closer to zero compared to the unscaled version of each functional, and these trends are nearly the same for both the TD-DFT (Figure 4, top) and TDA-DFT schemes (Figure 4, bottom). The global B2GP-PLYP and B2PLYP functionals are exceptions to this trend; these DFAs perform better when unscaled. This is especially notable for the latter functional: TDA-SOS-B2PLYP has a higher MD and MAD (increases of 0.17 and 0.08 eV, respectively) than those of unscaled TDA-B2PLYP.

Improvements in MADs from SCS compared to an unscaled DFA range from being marginal (0.01 eV for TD-SCS- $\omega$ B88PP86) to significant (0.14 eV for TD-SCS-RSX-QIDH). Improvements in the same range are also observed for most SOS methods albeit with a much larger maximum improvement (0.22 eV for TDA-SOS-RSX-QIDH). In the overwhelming number of cases, the SCS variant of a DFA results in higher MDs (and thus more blueshifted excitation energies) than the SOS version. Usually this also coincides with the SCS having slightly higher MADs than the SOS variants, with TDA- $\omega$ B2GP-PLYP being a notable exception due to having the same MADs. The observed trends are the same for full TD-

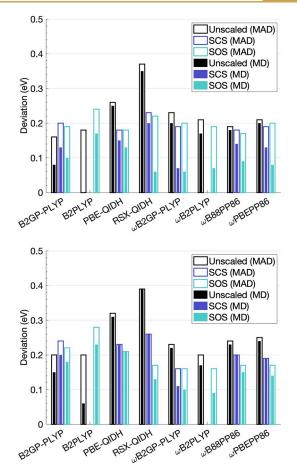


Figure 4. MDs and MADs (in eV) for scaled and unscaled functionals. Top: TD-DFT. Bottom: TDA-DFT.

DFT and TDA-DFT, with the full TD-DFT versions of SOS- $\omega$ PBEPP86 and SOS- $\omega$ B2GP-PLYP being exceptions because they have slightly higher MADs than their SCS counterparts, contrary to their TDA-DFT versions (Figure 4). The impact of SCS and SOS compared to the unscaled version is the highest for TD/TDA-RSX-QIDH. Also the difference between SCS and SOS is the highest for this functional compared to the other tested DFAs.

Returning to range separation we see that when SCS/SOS is introduced, some of the range-separated DFAs perform better than the global functionals on which they are based. While scaling yields worse results for B2(GP-)PLYP, the scaled variants of range-separated  $\omega$ B2GP-PLYP and  $\omega$ B2PLYP have lower MDs and MADs than the unscaled range-separated counterparts (Figure 4). This again indicates a beneficial interplay between SCS/SOS and range separation for some of the new TD(A)-DHDFs, as also reported for closed-shell systems in ref 20.

# 4.4. Comparison of All Functionals Tested for the Entire Set

We continue our discussion of the entire set of 45 excitations with a comprehensive comparison between all tested approaches, which combines the three different aspects that we have individually addressed in the preceding sections. All results are shown in Figure 2. When ranking the assessed DFAs, we consider the MADs first, followed by RMSDs and absolute MDs when necessary. It is known that DHDFs are the most accurate DFAs for ground-state calculations<sup>10,71-74</sup> as

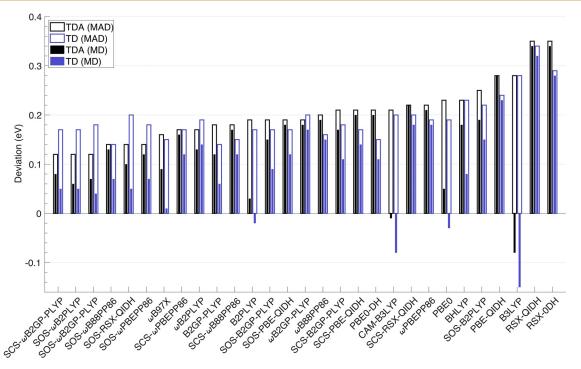


Figure 5. MDs and MADs (in eV) for the reduced set of 41 doublet-doublet excitation energies using TD-DFT and TDA-DFT for all tested functionals, ranked by TDA MAD, followed by RMSDs and then absolute MDs in the case of identical MADs.

well as singlet-singlet and singlet-triplet excitation energy calculations.  $^{6-8,10,12-15,17-20,30,34,35}$  Thus, it would be reasonable to expect that this would also be true for doublet-doublet excitations. While the best-performing DFAs for the radical test set are indeed DHDFs, as discussed below, the assessed hybrid functionals show comparable performance to some of the DHDFs tested. For instance, TD- $\omega$ B97X (MAD = 0.18 eV) is the 11th best of all tested approaches when TD- and TDA-DFT results are combined and ranked after the abovementioned criteria; it is the fourth-best among all full TD-DFT methods. Unexpectedly, the worst-performing functionals are also DHDFs, which highlights the challenging nature of doublet-doublet excitation energy calculations. A total of six DHDF-based approaches have the same or worse MAD than the worst hybrid approach TDA-B3LYP (MAD = 0.28 eV), namely, TDA-SOS-B2PLYP, TDA-PBE-QIDH, TD/TDA-RSX-0DH, and TD/TDA-RSX-QIDH.

For all assessed approaches, MADs range from 0.16 eV (TD-B2GP-PLYP, TDA-SOS- $\omega$ B2PLYP, and TDA-SCS/SOS- $\omega$ B2GP-PLYP) to 0.39 eV (TDA-RSX-QIDH and TDA-RSX-0DH), once again confirming that so-called "non-empirical" DHDFs are not automatically superior to semi-empirical ones; for other examples of this finding, see, e.g., refs 10, 19, 20, 75, and 76. With MADs of 0.17 or 0.18 eV, the following DHDFs are very close to the best DFAs: TD-PBE0-DH, TDA-SOS-RSX-QIDH, TDA-SOS- $\omega$ B88PP86, TD-B2PLYP, TD-SOS/SCS-PBE-QIDH, and TD-SCS- $\omega$ B88PP86.

When considering that TDA-DHDFs are more efficient for larger systems, we notice that TDA-DHDFs with SCS/SOS and range separation are among the best-performing methods, which parallels findings for various local and long-range singlet–singlet and singlet–triplet excitations.<sup>20</sup> That being said, we notice some discrepancies with our detailed recommendations from previous studies and also some unusually large blueshifts of 1 eV or more even for many of

the usually best-performing TD(A)-DHDFs. The potential reason for this will be discussed in the next section, which will provide an updated analysis.

# 4.5. Analysis after Excluding Double-Excitation States

One well-known flaw of TD(A)-DFT is its inability to describe transitions with high double-excitation character due to the adiabatic approximation.<sup>77,78</sup> TD(A)-DHDFs are no exception to this, and in fact their high amount of Fock exchange can further increase deviations.<sup>6,17,20</sup> Upon closer inspection of the WFT data in the original paper<sup>38</sup> that published the herein assessed radical set and after additionally conducted UCCSD calculations of systems with deviations of more than 0.5 eV for DHDFs that are known to usually perform well, we identified excitations with high double-excitation or multireference character. The relevant systems and states that caught our attention after such an analysis are CNO (state  ${}^{2}\Sigma^{+}$ ), CO<sup>+</sup> (state  ${}^{2}\Pi$ ), and NCO (states  ${}^{2}\Sigma^{+}$  and  ${}^{2}\Pi$ ).

Our reasoning for CNO and CO<sup>+</sup> is based on the %T1 diagnostic for UCCSD and large deviations of the latter from UCC3 numbers published in ref 38, which coincide also with large outliers for assessed TD(A)-DHDFs in this work. A %T1 diagnostic under 90 was used to identify problematic excitations. The reported  ${}^{2}\Sigma^{+}$  excitation energy for CNO at the UCCSD level is 2.24 eV (%T1 = 88.00), which represents a deviation of 0.49 eV compared to UCC3. Similarly, many (but not all) DHDFs have large deviations between 0.99 eV (TD-PBE-QIDH) and 1.35 eV (TDA-RSX-QIDH) The UCCSD excitation energy for the  ${}^{2}\Pi$  transition in CO<sup>+</sup> is 3.60 (%T1 = 87.79), which is why it was ruled out, too. Note that we had already discarded the  ${}^{2}\Sigma^{+}$  transition of the same molecule due to problems with this state. Its %T1 is 87.96 and its double excitation character might be a potential answer for the problems we alluded to in section 3.

In the case of NCO, we note that the  ${}^{2}\Sigma^{+}$  and  ${}^{2}\Pi$  transitions are mainly dominated by singly excited configurations (%T1 =

93.85 and %T1 = 90.96). Despite that, Loos et al. determined that EOM-CCSDTQ<sup>79</sup> calculations were mandatory to obtain reliable transitions, particularly for the <sup>2</sup> $\Pi$  state, and that they changed even more for MRCI+Q.<sup>38</sup> Because we cannot fully guarantee the accuracy of the reference or potential problems of the methods for such multireference cases, NCO was also regarded as a problematic case in this study.

Due to known inadequacies of TD(A)-DFT for closed-shell systems with similar difficulties (double-excitation or high multireference character), previous TD(A)-DHDF studies have presented two separate sets of statistics for the benchmark sets they were investigating, namely, with the challenging transitions included and excluded.<sup>20,80</sup> Here, we follow the same principle. While the previous section provided us with the statistics over 45 excitations of the entire set, this section presents a brief discussion of a reduced set with 41 excitations for 21 radicals. The statistical data for this slightly reduced set are provided in the SI and the relevant results are shown in Figure 5. While a recent double-hybrid approach based on the second-order algebraic-diagrammatic construction<sup>81</sup> [ADC(2)] looked promising for double excitations in closedshell systems,<sup>80</sup> that advantage is expected to also come at a higher computational cost, but could be pursued in a future study.

A direct comparison between Figure 5 and Figure 2 shows that there is a systematic improvement for the tested methods regardless of choosing the TD- or TDA-DFT scheme. The average MAD over all tested TD- and TDA-DFT approaches is 0.22 eV for the complete set and reduced to 0.20 eV after excluding the four difficult states. MADs now range from 0.12 to 0.35 eV (a 0.04 eV improvement at both ends of the spectrum). Most importantly, the best methods are now closer to the chemical accuracy threshold of 0.1 eV.

While there is overall little substantial change to the DFA ranking, we do notice a shift when comparing the best TDAwith the best TD-DFT methods. The six best approaches are now exclusively TDA-DHDFs with SCS/SOS and range separation, namely SCS- $\omega$ B2GP-PLYP, SOS- $\omega$ B2PLYP, and SOS- $\omega$ B2GP-PLYP with MADs of 0.12 eV, followed by SOS- $\omega$ B88PP86, SOS-RSX-QIDH, and SOS- $\omega$ PBEPP86 with MADs of 0.14 eV. The first full TD-DFT method in our ranking is TD-B2GP-PLYP with an MAD of 0.14 eV but a slightly higher RMSD than the preceding three TDA-DHDFs. B3LYP remains to be the worst hybrid functional and four DHDFs are still worse, namely the TD and TDA versions of RSX-0DH and RSX-QIDH.

During the review stage of our paper, one of the reviewers made us aware of a preprint that presented an analysis of more than 40 TDA-DFAs belonging to the first four rungs of Jacob's Ladder on a large part of the QUEST database, including parts of its radical test set, with the same basis set applied herein.<sup>82</sup> The reviewer asked us to compare their best-performing method with the herein assessed TD(A)-DHDFAs, but it turns out that a direct comparison with that data was difficult, as the preprint analyzed 42 doublet-doublet excitations without any information on exactly which excitations had been left out. Moreover, only the values for some selected RMSDs were given instead of all assessed methods and the values of other statistical data were not provided. Their RMSD of 0.313 eV for TDA-CAM-B3PLYP is slightly above ours (0.29 eV), but within reason we can still make a rough comparison between the preprint and our present study. The best RMSD that we could find for the radical set in the preprint is the rangeseparated hybrid  $\omega$ B97X-V,<sup>83</sup> which contains a reparametrized exchange-correlation expression of the herein assessed  $\omega$ B97X. That RMSD was reported as 0.275 eV, which is comparable to the herein obtained value of 0.27 eV for TDA-PBE0, a DFA whose RMSD was not presented in the preprint. We also note that our value for TDA- $\omega$ B97X has a lower RMSD of 0.21 eV. Most importantly, a total of 31 TD(A)-DHDFs have lower RMSDs than the best performing DFA from that study, which demonstrates again how double hybrids are superior to hybrids or other lower-rung functionals (see the SI for RMSD values).

UCCSD has an MAD of 0.12 eV based on the results taken from ref 38, which is the same as for the best three DFAs in our study; however, it seems to have a more systematic blueshift due to an MD with exactly the same value. The top three DFAs all have MDs closer to zero and therefore outperform CCSD on average. Therefore, we warn against using CCSD or approximate versions of it as a reference for benchmarking TD(A)-DHDFs.

Using the TDA and SOS can both provide computational advantages, which makes the top six DFAs in this study quite attractive for larger systems. Our findings for the best-performing methods mirror our previous benchmark studies on singlet—singlet and singlet—triplet excitations, with the difference being that SOS- $\omega$ B88PP86 and SOS- $\omega$ PBEPP86 performed better for those than the top-three functional in the present study. Given that their MADs for doublet—doublet excitations are only marginally larger than for the top three methods, we can recommend SOS- $\omega$ B88PP86 and SOS- $\omega$ PBEPP86 as more robust methods that work well for different types of excitations.

However, despite the success of DHDFs with range separation and SCS/SOS for doublet-doublet excitations, it is important to note that even the best functionals are still slightly above the chemical accuracy threshold and more development in this area might be warranted.

#### 5. SUMMARY AND CONCLUSIONS

In this work, we used a range of hybrid and double-hybrid (DHDF) density functionals to calculate doublet—doublet excitation energies in small radicals. The study of open-shell systems with time-dependent DHDFs was the first detailed of this kind, and our aim was to shed light on the current state-of-the-art techniques in the field and to clarify if there is still room for future improvements. The performance of 29 functionals was evaluated by comparing the calculated excitation energies against UCC3/aug-cc-PVTZ reference energies from ref 38.

First we investigated the Tamm–Dancoff approximation (TDA) and its effects on doublet–doublet transitions. Our findings indicate that doublet–doublet excitations are not subject to TD-DFT instability problems. The TDA was found to cause a systematic blueshift in excitation energies, and, unlike for triplet excitations, it slightly worsened the performance of most functionals except for the best-performing ones.

To investigate the effects of range separation, we compared range-separated functionals against global ones. Rangeseparated double hybrids resulted in larger mean absolute deviations (MADs) than their global counterparts unless spincomponent/spin-opposite scaling (SCS/SOS) was applied.

Introducing the effects of SCS/SOS revealed that many of the scaled DHDFs performed better with range separation. All range-separated DHDFs delivered lower MADs with SCS/ SOS; however, the results for the global B2(GP-)PLYP functionals were worsened with SCS/SOS. DHDFs did not

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categorically outperform hybrid functionals: while the bestperforming DFAs were indeed DHDFs, the worst-performing functionals also belonged to the fifth rung of Jacob's Ladder, more specifically to the class of so-called "nonempirical" DHDFs. Thus, once again, it has been demonstrated how those were outperformed by semiempirical DHDFs despite persistent claims of the opposite.

Further scrutiny revealed that four electronic states in the set are problematic due to pronounced double-excitation or multireference character; upon excluding those systems, we noticed improvements. The six best methods in our study had MADs of 0.12 and 0.14 eV, respectively, and they all have in common that they are spin-component or spin-opposite scaled double hybrids combined with range separation and applied within the TDA. More specifically, these methods are SCSωB2GP-PLYP, SOS-ωB2PLYP, SOS-ωB2GP-PLYP, SOSωB88PP86, SOS-RSX-QIDH, and SOS-ωPBEPP86. It is noteworthy that those methods worked without further optimization of their parameters, which had been determined on closed-shell systems. Given their better performance for singlet-singlet and singlet-triplet excitations, we recommend TDA-SOS-@B88PP86 and TDA-SOS-@PBEPP86 as robust methods for general excitation energies until further improvements have been achieved that surpass the chemical accuracy target, particularly for challenging systems, without increasing the computational effort.

# ASSOCIATED CONTENT

## **3** Supporting Information

The Supporting Information is available free of charge at https://pubs.acs.org/doi/10.1021/acsphyschemau.2c00014.

All excitation energies for all assessed functionals as well as their detailed statistics (XLSX)

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#### Notes

The authors declare no competing financial interest.

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